~~Atmospheric O~~Separating above canopy CO_2 and ~~CO~~O_2 measurements ~~at a single height provide weak constraint on surface carbon exchange~~into their atmospheric and biospheric signatures

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Abstract. ~~The ratios of atmospheric~~ Atmospheric tracers are often used to interpret the local CO_2 budget, where measurements at a single height are assumed to represent local flux signatures. Alternatively, these signatures can be derived from direct flux measurements or using fluxes derived from measurements at multiple heights. In this study, we contrast interpretation of surface CO_2 exchange from tracer ~~ratio~~ measurements at a single height versus measurements at multiple heights.

Specifically, we analyse the ratio between atmospheric O_2 and CO_2 (exchange ratio, ER) above a forest~~canopy~~. We consider two alternative approaches: the exchange ratio of the forest (ER_{forest}) obtained from the ratio of the surface fluxes of O_2 and CO_2, derived from ~~their vertical gradients measured~~ measurements at multiple heights, and the exchange ratio of the atmosphere (ER_{atmos}) obtained from changes in the O_2 and CO_2 mole fractions over time measured at a single ~~measurement~~ height. We investigate the diurnal cycle of both ER signals, ~~with the goal to relate the   signal to the   signal and to~~ to better understand the biophysical meaning of the ER_{atmos} signal. We have combined CO_2 and O_2 measurements from Hyytiälä, Finland during spring and summer of 2018 and 2019 with a conceptual land-atmosphere model ~~and a theoretical relationship between   and~~ to investigate the behavior of ER_{atmos} and ER_{forest}. We show that the CO_2 ~~during different environmental conditions. We~~and O_2 signals and their resulting ERs are influenced by climate conditions, such as variations in the soil moisture and temperature, for example during the 2018 heatwave. We furthermore show that the ER_{atmos} signal ~~rarely directly~~ obtained from single height measurements rarely represents the forest exchange directly, mainly because it is influenced by entrainment of air from the free troposphere into the atmospheric boundary layer. The influence of these larger scale ~~signals leads~~ processes can lead to very high ER_{atmos} values (even larger than 2), especially in the early morning~~transition~~. These high values do not directly represent carbon cycle processes, but are rather a mixture of different signals. ~~We show that the resulting   signal is not the average of the contributing processes, but rather an indication of the influence of large scale processes such as entrainment or advection. Our findings show that these processes are furthermore influenced by climate conditions, such as the 2018 heatwave, through their dependence on soil moisture and temperature.~~

We conclude that the ER_{atmos} signal ~~obtained from single height measurements rarely directly represents and therefore~~ only provides a weak constraint on local scale surface CO_2 exchange, ~~because large scale processes confound the signal~~and that ER_{forest} above the canopy should be used instead. Single height measurements ~~therefore~~ always require careful selection of the time of day and should be combined with atmospheric modelling to yield a meaningful representation of forest carbon exchange. More generally, we recommend ~~to always measure~~ always measuring at multiple heights when using multi-tracer measurements to study surface CO_2 exchange.

1 Introduction

Rising atmospheric carbon dioxide (CO_2) levels, resulting from fossil fuel combustion and land use change emissions~~and~~, moderated by ~~uptake by~~ the terrestrial biosphere and oceans, require a comprehensive assessment of the carbon exchange at local and global scales (Friedlingstein et al., 2022). Atmospheric oxygen (O_2) serves as a valuable tracer~~in~~, enhancing our understanding of carbon exchange ~~,~~ due to the close linkage between O_2 and carbon dioxide (CO_2) in carbon cycle processes such as fossil fuel combustion, photosynthesis and respiration (Manning and Keeling, 2006; Worrall et al., 2013; Keeling and Manning, 2014; Bloom, 2015; Hilman et al., 2022). The Exchange Ratio ($ER = -O_2/CO_2$), denoted as the number of moles of O_2 exchanged per mole of CO_2~~-~~, represents the specific link between O_2 and CO_2 for different processes (Keeling et al., 1998). Long-term O_2 and CO_2 measurements allow us to derive the global ocean carbon sink (Stephens et al., 1998; Rödenbeck et al., 2008; Tohjima et al., 2019) and to estimate changes in fossil fuel emissions (Pickers et al., 2022; Ishidoya et al., 2020; Rödenbeck et al., 2023).

For global applications, a constant ER of 1.1 [mol mol^{-1}] is assumed for the terrestrial biosphere (Severinghaus, 1995). However, the ER of terrestrial biosphere exchange is not uniform at smaller scales; it varies between ecosystems and over time (Angert et al., 2015; Bloom, 2015; Battle et al., 2019; Hilman et al., 2022). Measuring the ERs of ecosystems and the underlying gross processes facilitates the partitioning of Net Ecosystem Exchange (NEE) into Gross Primary Production (GPP) and Total Ecosystem Respiration (TER) (Ishidoya et al., 2015; Faassen et al., 2023) which is still challenging (Reichstein et al., 2005). The ER for net ecosystem exchange can be determined from the ratio of the net turbulent surface fluxes of O_2 and CO_2 above the canopy, referred to as ER_{forest} (see Figure 1). The O_2 surface fluxes can be inferred from the vertical gradient: the difference between O_2 mole fraction measurements at multiple heights, together with a turbulent exchange coefficient. Currently, available instruments ~~so far have not allowed~~ do not allow Eddy Covariance (EC) O_2 measurements. The ER_{forest} signal predominantly represents forest exchange occurring in and below the canopy (small scale processes), comprising the individual ERs of TER (ER_r) and GPP (ER_a) (Ishidoya et al., 2013, 2015; Faassen et al., 2023). Alternatively, net ecosystem ERs have been estimated based on measurements of O_2 and CO_2 mole fractions in the atmosphere at a single height above the canopy. This is referred to as ER_{atmos} (Figure 1) and is defined as the change in O_2 and CO_2 mole fractions over time (Seibt et al., 2004; Battle et al., 2019; Faassen et al., 2023).
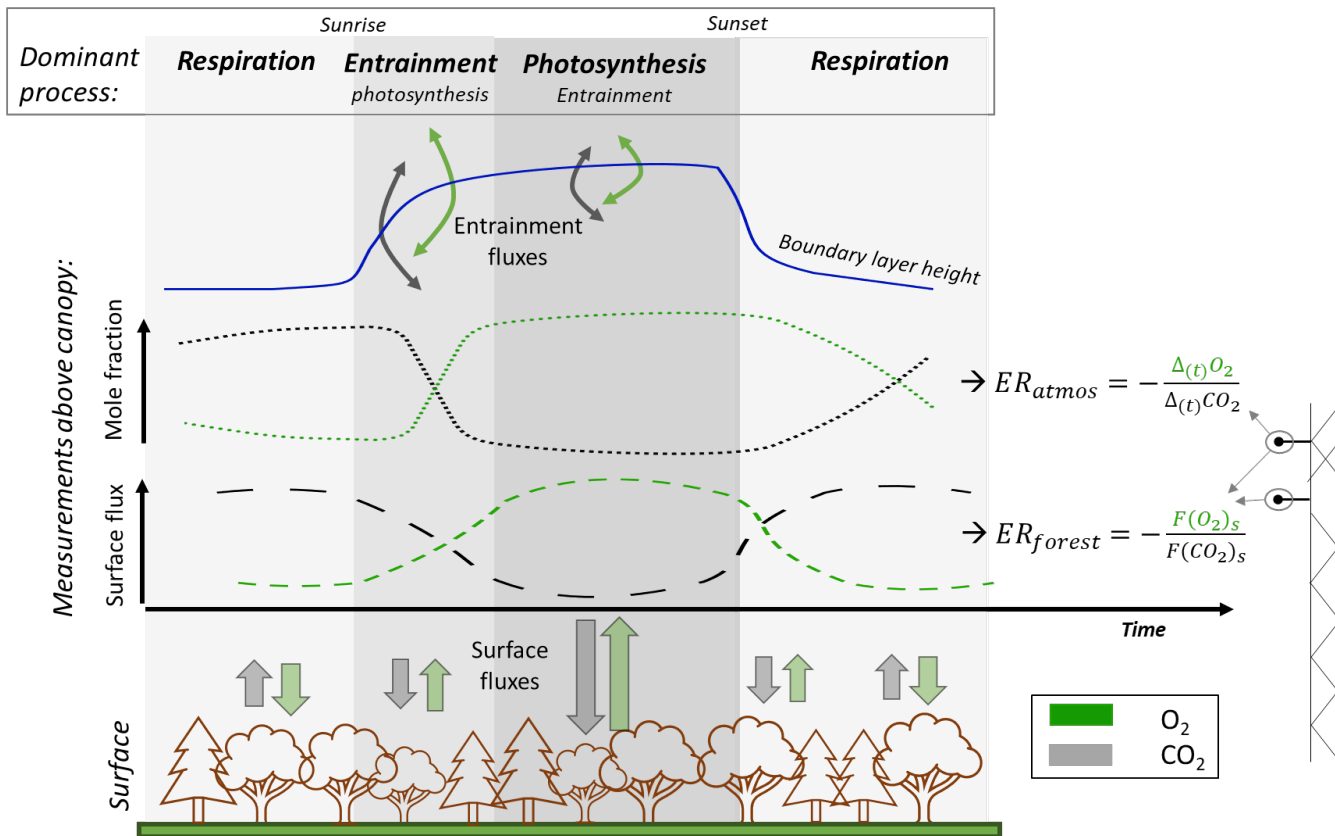
Figure 1. Schematic overview of the diurnal cycles of the surface fluxes and mole fractions of atmospheric O_2 and CO_2 above a forest canopy. The figure illustrates the dominant processes throughout the day, with forest exchange dominating the nocturnal and afternoon periods, while early morning signals are primarily influenced by entrainment of air from the residual layer or the free troposphere. The surface fluxes of O_2 and CO_2 result in the Exchange Ratio signal of the forest (ER_{forest}), while the changes in the mole fractions of O_2 and CO_2 over time can lead to variations of the Exchange Ratio signal of the atmosphere (ER_{atmos}). Note that the term "surface fluxes" refers to the fluxes from the surface layer, which includes the vegetation layer, including the top of the canopy. The surface layer is the lowest 10% of the boundary layer where the surface directly influences the atmospheric boundary layer.

In our recent study (Faassen et al., 2023), we showed a comprehensive comparison of the diurnal behaviour of ER_{forest} and ER_{atmos} using measurements collected above a boreal forest in Hyytiälä, Finland. Our analysis revealed that during the afternoon (the photosynthesis dominant period in Figure 1), the ER_{atmos} signal approaches the ER_{forest} value, although they did not converge completely. Furthermore, we showed that during the entrainment-dominant period (see Figure 1), the ER_{atmos} signal strongly exceeded the expected ER value for biosphere exchange, which is typically around 1.1 (Severinghaus, 1995), and even surpassed 2.0. Such high ER values (>2.0) cannot be attributed to a single process such as photosynthesis, respiration or fossil fuel combustion, as their ER values are below 2.0. We proposed that the high ER_{atmos} signal was likely influenced by large scale processes, specifically the entrainment of air from the free troposphere into the boundary layer (Faassen et al., 2023).

Also Seibt et al. (2004) and Yan et al. (2023) argue that ER_{atmos} cannot capture the ER signal of a forest. In contrast, in the studies by Ishidoya et al. (2013, 2015) ER_{forest} and ER_{atmos} do result in similar values when small scale processes dominate over large scale processes. In Faassen et al. (2023) we concluded that an atmospheric model was needed to interpret the observed diurnal signals of ER_{atmos} and ER_{forest}. The current study delivers this model-based analysis.

Until now atmospheric O_2 above forest canopies has primarily been modeled with relatively simple one-box models that use only the surface components, lacking implementation of boundary layer dynamics such as entrainment and boundary layer growth (Seibt et al., 2004; Ishidoya et al., 2013). Understanding how mole fractions, and consequently how ER_{atmos} evolves throughout the day requires accounting for these critical processes. Yan et al. (2023) recently modelled O_2 and CO_2 within and below a canopy using a multi-layer model and showed that ER_{atmos} and ER_{forest} have diurnal and annual patterns. However, ER_{atmos} was treated as a constant value above the canopy and boundary layer dynamics were not accounted for. To expand on the work by Yan et al. (2023) and gain further insight into the diurnal ER_{atmos} behaviour above a canopy, in this study we use the mixed layer model Chemistry Land-surface Atmosphere Soil Slab (CLASS) (Vilà-Guerau de Arellano et al., 2015). In short, the model is able to represent the thermodynamics and biophysical processes associated with the diurnal variation in the boundary layer and can provide insights into the processes contributing to ER_{atmos} formation. Additionally, the model facilitates the analysis of ER_{atmos} behavior under more extreme conditions ~~, that were not yet measured~~ such as droughts or heatwaves.

~~This study aims~~ In this study, we aim to enhance our understanding of single height O_2 and CO_2 measurements and the resulting ER_{atmos} signal, as observed above the canopy, and ~~proposes~~ we propose a new relationship between the ER_{atmos} and ER_{forest} signal. We seek to determine whether single height O_2 and CO_2 measurements ~~could potentially~~ can be employed to estimate the ecosystem's ER despite the ~~mentioned~~ aforementioned limitations. Additionally, we explore whether the ER_{atmos} signal ~~allows to constrain~~ constrains boundary layer dynamics ~~and~~, and we identify cases where large scale processes (e.g. entrainment of background air) influence the signal of small scale processes (e.g. NEE) by analyzing different diurnal regimes of ER_{forest} and ER_{atmos}. We combine measurements from campaigns in Hyytiälä, Finland during the spring/summer of 2018 and 2019 with an analysis of the mixed layer model CLASS. This combined approach allows us to address the following research questions: 1) When does ER_{atmos} represent local forest exchange processes, and become equal to ER_{forest}? and 2) What is the underlying physical explanation for the high ER_{atmos} values observed in the recent study by Faassen et al. (2023)?

In this paper we first derive a theoretical relationship between ER_{atmos} and ER_{forest} that can help us to understand which components influence the diurnal cycle of ER_{atmos} and when ER_{atmos} should indicate the same processes as ER_{forest} (Sect. 2). To evaluate the diurnal cycle of ER_{atmos} we combine observational data with the ~~model CLASS which are described in~~ CLASS model (Sect. 3. ~~We~~). We then show the model evaluation and the ER_{atmos} and ER_{forest} model results in Sect. ~~4, where~~ 4.2 and we analyse different cases to explain the diurnal behaviour of ER_{atmos} during distinct periods of the day and investigate when ER_{atmos} represents forest exchange ~~. In Sect. 5~~ (Sect. 4.3). Next, we place our results in perspective and show how ER_{atmos}

should (not) be used .(Sect. 5). Finally, we present our conclusions on the physical explanations for the differences between the diurnal behaviour of both ER_{atmos} and ER_{forest}.

2 Fundamental concepts

2.1 The mixed layer theory
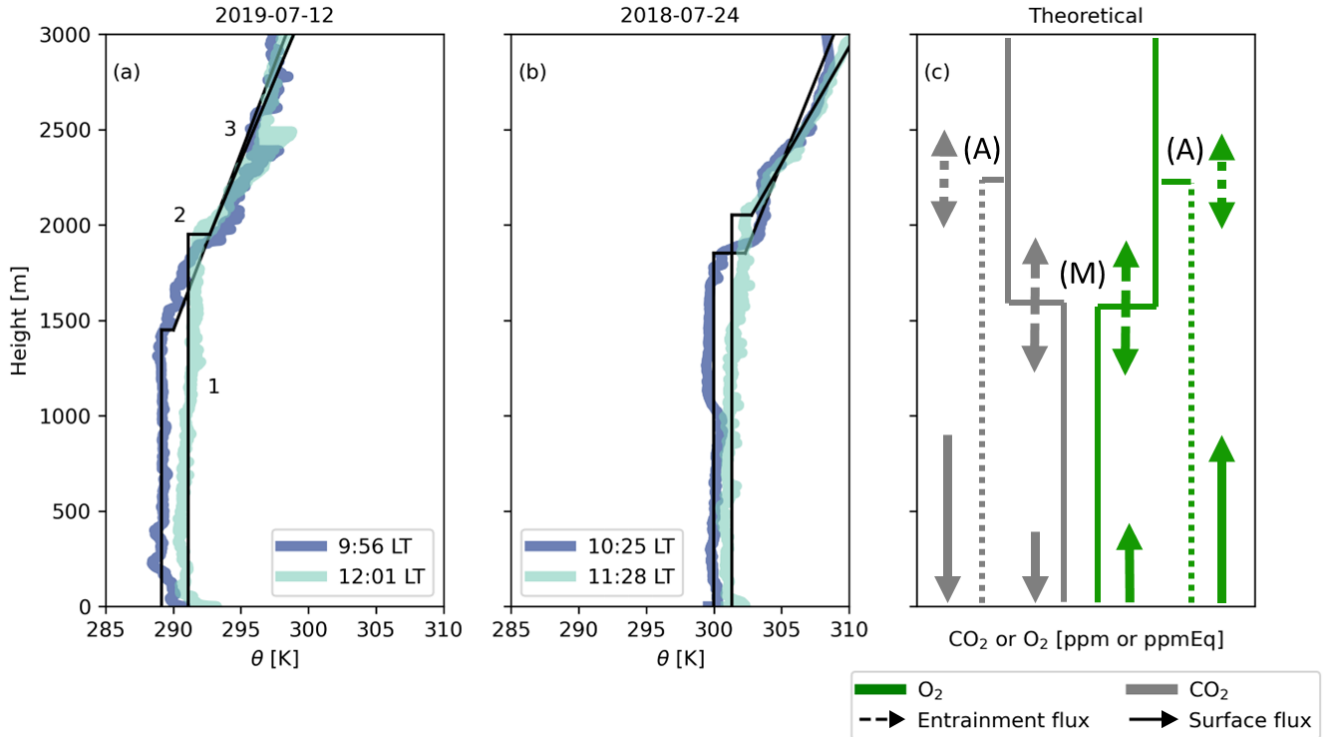
Figure 2. Vertical profiles of potential temperature (θ) measured by radiosondes at Hyytiälä on 12 July 2019 (a) and 24 July 2018 (b). The observations are conceptualized (black lines) to show: 1) the well-mixed profiles at different time steps, 2) the jump between the boundary layer and the free troposphere, and 3) the lapse rate in the free troposphere. 1, 2 and 3 are used to initialize the CLASS model. (c) gives the theoretical vertical profiles of O_2 and CO_2 for the early morning (M) and late afternoon (A). The sizes of the arrows indicate the effects of entrainment (dashed lines) and the surface fluxes (solid lines) on the vertical profiles.

The land-atmosphere model CLASS (Vilà-Guerau de Arellano et al., 2015) is based on the mixed-layer theory which assumes that scalars (such as O_2, CO_2, θ) are constant with height in the atmospheric boundary layer (Lilly, 1968; Tennekes, 1973). Figure 2 illustrates these assumptions for potential temperature (θ), O_2 and CO_2. Within the mixed layer theory, no distinct surface layer exists, and a capping inversion links the mixed layer value (the bulk constant value) with the lapse rate of the free troposphere. This inversion, termed the 'jump' ($\Delta_{(ft-bl)}$), represents the difference of a scalar (e.g. the CO_2 mole

fraction) between the atmospheric boundary layer and the free troposphere. The free troposphere is represented by a linear change of the scalar with height (the lapse rate).

CLASS describes the well-mixed layer with a scalar constant in height (Figure 2). This scalar (ϕ) can then be solved in the
110 mixed-layer with the following equations (Vilà-Guerau de Arellano et al., 2015):

$$\frac{\partial \phi}{\partial t} = \frac{(\overline{w'\phi'})_s - (\overline{w'\phi'})_e}{h} - adv(\phi) \tag{1}$$

where $\partial\phi/\partial t$ is the tendency (i.e. change over time) of a generic well-mixed scalar, _w′ are the deviations of the mean for w which is the vertical wind speed, and ϕ' are the deviations from the mean for a scalar ϕ._ The term $(\overline{w'\phi'})_s$ is the surface flux of ϕ and represents the small scale processes, $(\overline{w'\phi'})_e$ is the entrainment flux, h is the boundary layer height and $adv(\phi)$ is the
115 horizontal advection of scalar ϕ into the well-mixed layer. $(\overline{w'\phi'})_e$ and $adv(\phi)$ represent ~~the~~ large scale processes, in contrast to the local surface exchange $(\overline{w'\phi'})_s$.

The entrainment flux is dependent on the entrainment velocity and the jump:

$$(\overline{w'\phi'})_e = -w_e \cdot \Delta_{(ft-bl)}\phi = \left(\frac{\partial h}{\partial t} - w_{sub}\right) \cdot \Delta_{(ft-bl)}\phi \tag{2}$$

120 where w_e is the entrainment velocity, $\Delta_{(ft-bl)}\phi$ is the jump between the free troposphere and the atmospheric boundary layer, and w_{sub} is the mean vertical subsidence velocity associated normally ~~to~~ with high pressure systems~~, which we assume to be~~. We assume w_{sub} is negligible, because our focus does not lie on the influence of synoptic scale processes.

$\Delta_{(ft-bl)}\phi$ changes over time (see Figure 2) and depends on the surface fluxes and the air that is entrained from the free
125 troposphere (see Equation 1):

$$\frac{\partial \Delta_{(ft-bl)}\phi}{\partial t} = \gamma_\phi \cdot w_e - \frac{\partial \phi}{\partial t} \tag{3}$$

where γ_ϕ is the lapse rate of ϕ in the free troposphere~~.~~, and $\partial\phi/\partial t$ is the change over time of the well-mixed scalar ϕ (i.e. in the boundary layer).

130 Last, the growth of the boundary layer height (~~h) is of importance for~~ $\frac{\partial h}{\partial t}$) effectively determines the entrainment velocity and ~~as a result~~ therefore the entrainment flux of a certain scalar. The growth of the boundary layer is caused by the virtual potential temperature (θ_v), also called buoyancy:

$$\frac{\partial h}{\partial t} = -\frac{(\overline{w'\theta_v'})_e}{\Delta\theta_v}\frac{(\overline{w'\theta_v'})_e}{\Delta_{(ft-bl)}\theta_v} + w_{\underline{s}\,sub} \tag{4}$$

where θ_v is the virtual potential temperature (i.e. potential temperature of dry air) and ~~w_s~~ w_{sub} is the subsidence velocity. For
135 more details on these equations, see Vilà-Guerau de Arellano et al. (2015) and Sect. 3.2.2 and Sect. A2 for the application of O_2.

2.2 Theoretical relationship between ER$_{atmos}$ and ER$_{forest}$

The ER signal of the forest (ER$_{forest}$) is defined as (Faassen et al., 2023):

$$ER_{forest} = -\frac{(F_{O_2})_s}{(F_{CO_2})_s} \approx -\frac{-K_\phi \cdot \Delta_{(z)}O_2/\Delta z}{-K_\phi \cdot \Delta_{(z)}CO_2/\Delta z} \tag{5}$$

where $(F_{O_2})_s$ and $(F_{CO_2})_s$ are the mean net turbulent surface fluxes of O_2 and CO_2 respectively over a certain time period above the canopy, and can be derived from the vertical gradient of O_2 $(\Delta_{(z)}O_2)$ and CO_2 $(\Delta_{(z)}CO_2)$ measurements at two heights together with an exchange coefficient following the K-theory (K_ϕ) (Faassen et al., 2023). Note that ~~here~~ the K-theory does not apply when one of the measurement levels is inside the canopy. For readability, we write the surface fluxes for both O_2 and CO_2 as F_ϕ instead of ~~the general form~~ $\overline{(w'\phi')}_s$ that was used above for the general theory.

The ER signal of the atmosphere (ER$_{atmos}$) is defined as (Faassen et al., 2023):

$$ER_{atmos} = -\frac{\partial O_2/\partial t}{\partial CO_2/\partial t} \approx -\frac{\Delta_{(t)}O_2}{\Delta_{(t)}CO_2} \tag{6}$$

where $\Delta_{(t)}O_2$ and $\Delta_{(t)}CO_2$ are the changes of the O_2 and CO_2 mole fractions over time (tendencies) at a single height. Linear regression between O_2 and CO_2 can be applied and the slope gives the ER$_{atmos}$ value for a certain event or time period. For this study, a linear regression was applied for the three periods described in Section 4.2.1 for the observations (1 value per 30 minutes) and the CLASS model output (1 value per 10 seconds).

~~By assuming~~ According to the mixed-layer theory described above, the tendencies in equation 6 depend on the surface and entrainment fluxes, together with the boundary layer height (h) (see Equation 1). Equation 6 can be rewritten by implementing Equation 1:

$$ER_{atmos} = -\frac{((F_{O_2})_s - (F_{O_2})_e)/h}{((F_{CO_2})_s - (F_{CO_2})_e)/h} \tag{7}$$

where $(F_{O_2})_s$ and $(F_{CO_2})_s$ are the net surface fluxes of O_2 and CO_2, and $(F_{O_2})_e$ and $(F_{CO_2})_e$ are the entrainment fluxes of O_2 and CO_2 respectively. For simplicity we ignored the advection term in ~~Equation~~ Eq. 1 here, ~~and~~ but we will add it later (~~see Equation~~ Eq. 9). As shown in ~~Equation~~ Eq. 2, the entrainment flux depends on the entrainment velocity (w_e) and the jump between the free troposphere and the boundary layer ($\Delta_{(ft-bl)}\phi$). Combining the definition ~~for~~ of ER$_{forest}$ (~~Equation~~ Eq. 5) with ~~Equation~~ Eq. 2, allows ~~to rewrite Equation~~ us to rewrite Eq. 7 to:

$$ER_{atmos} = ER_{forest} \cdot \left(\frac{1 + \frac{w_e \cdot \Delta_{(ft-bl)}O_2}{(F_{O_2})_s}}{1 + \frac{w_e \cdot \Delta_{(ft-bl)}CO_2}{(F_{CO_2})_s}}\right) = ER_{forest} \cdot \left(\frac{1 + \beta_{O_2}}{1 + \beta_{CO_2}}\right) \tag{8}$$

where $\Delta_{(ft-bl)}O_2$ and $\Delta_{(ft-bl)}CO_2$ are the jumps of O_2 and CO_2 between the free troposphere and the boundary layer, and β_ϕ is the ratio between the entrainment flux and the surface flux (Vilà-Guerau de Arellano et al., 2004). Equation 8 shows a

165   clear relationship between ER_{atmos} and ER_{forest} ~~by assuming~~ following the mixed-layer theory.

     Using the definition of Equation 1, we can extend Equation 8 to include the effect of ~~the other relevant large scale process,~~ advection of O_2 (adv_{O_2}) and CO_2 (adv_{CO_2}), which is next to entrainment, the second important large scale process influencing the O_2 and CO_2 values:

$$170 \qquad ER_{atmos} = ER_{forest} \cdot \left(\frac{1 + \beta_{O_2} + \frac{h}{(F_{O_2})_s} \cdot adv_{O_2}}{1 + \beta_{CO_2} + \frac{h}{(F_{CO_2})_s} \cdot adv_{CO_2}} \right) \qquad\qquad (9)$$

Note that in this paper, we mostly focus on cases without advection. We do include it here for completeness and discuss the influence of advection in Section 5.2.

     In Appendix A1 we analyse Equation 8 by determining when ER_{atmos} would theoretically be close to ER_{forest} during the day. We show that the β values are ~~specifically of importance here. When~~ of particular importance here: when the β's of O_2

175   and CO_2 are equal or very small, ER_{atmos} gives the same signal as ER_{forest}. To fully unravel the diurnal variations of ER_{atmos} under realistic conditions and identify influencing factors, we need to analyse a real case. Therefore, we study two observed situations by means of the coupled land-atmosphere model, CLASS which we will describe ~~next.~~ in Sect. 3.2.

3   Methods

In this section we describe the measurements that were used in this study, together with the mixed-layer model used to evaluate

180   the ER_{atmos} and ER_{forest} signals.

3.1   Hyytiälä 2018 and 2019 measurement campaigns

The observational data were obtained from the SMEAR II Forestry Station of the University of Helsinki in Finland, located in Hyytiälä, Finland ($61°$ 51'N, $24°$ 17'E, +181 MSL) (Hari et al., 2013). The SMEAR II station serves as a measurement

185   site within a boreal forest equipped with a 128 m tower for continuous measurements of atmospheric variables, fluxes and greenhouse gas mole fractions. These data are accessible at https://smear.avaa.csc.fi/. The tower is situated in a homogeneous Scots pine forest, with an average canopy height of 18 m and a podzolic soil. The measurement site is predominantly influenced by the surrounding forest and has minimal impact from signals of fossil fuel combustion (Faassen et al., 2023). For a comprehensive description, see Hari et al. (2013).

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     During the spring/summer of 2018 (03-Jun until 02-Aug) and 2019 (10-Jun until 17-Jul), two measurement campaigns, referred to as OXHYYGEN (Oxygen in Hyytiälä), were conducted at Hyytiälä. Continuous measurements of both O_2 and CO_2 mole fractions were taken at two heights (125 m and 23 m). O_2 was measured using an Oxzilla II fuel cell analyser, and CO_2 was measured with a non-dispersive infrared (NDIR) photometer (URAS26). Further details about these measurements and

195   the measurement system are given in Faassen et al. (2023). The measurement precision for O_2 was 19 per meg and for CO_2, it

was 0.07 ppm. Although the precision for O_2 is relatively poor compared to previous studies, it is still adequate for studying the diurnal time scale, as shown in Faassen et al. (2023).

O_2 measurements are typically expressed as $\delta O_2/N_2$ ratios in 'per meg' units due to the high abundance of O_2 in the atmosphere (20.946%), classifying it as a non-trace gas. For direct comparison with CO_2 and implementation into our model, we convert per meg to ppm equivalents (ppmEq) by multiplying with the standard mole fraction of O_2 in air of 0.20946 (Keeling et al., 1998)since and change concurrently. We use conserved variables, by using mole fractions to indicate the abundance of and in the atmosphere, and therefore we can assume that the vertical profiles of and are well-mixed (Figure 2)..

During the OXHYYGEN campaigns, radiosondes were launched on multiple days several times per day to quantify the impact of boundary-layer dynamics on the O_2 and CO_2 diurnal cycles. The radiosondes (Windsond, model S1H3-R, Sweden) measured vertical profiles of air pressure, wind speed, wind direction, relative humidity and temperature, with flight heights reaching a maximum of 4500 m and rising rate of about 1.7 m s^{-1}. The measurements have an accuracy of 1.0 hPa for air pressure, 5% for wind speed, 0.2 C for temperature and 1.8% for the relative humidity. The temperature and humidity probe has a response time of 6 seconds, effectively averaging over about 10 m of altitude. For our analysis, we computed vertical profiles of potential temperature (θ) and specific humidity (q) based on pressure, temperature and relative humidity measurements. Based on the vertical profile of vertical temperature, we also determine the boundary layer height with the parcel method (Kaimal and Finnigan, 1994). Figure 2 shows examples of vertical profile measurements of θ for July 12, 2019, and July 24, 2018.

3.2 Modelling setup in CLASS

3.2.1 Implementation of CO_2 in CLASS

CLASS serves as a fundamental tool that enables further understanding of specific processes within the atmospheric boundary layer. Several studies have shown that CLASS is successful in reproducing observational data (Vilà-Guerau de Arellano et al., 2012, 2019; Schulte et al., 2021). The study of Ouwersloot et al. (2012) specifically showed that CLASS is able to reproduce the boundary dynamics at the Hyytiälä measurement site. Within CLASS, the vegetation is described using a big-leaf model. The surface stomatal conductance that is representative for the canopy is up-scaled from leaf stomatal conductance by integrating over the leaf area index and incorporating soil moisture. The leaf stomatal conductance is calculated with the A-gs model. The A-gs model relates leaf stomatal conductance (g_s) to the net leaf CO_2 assimilation (A) (Jacobs et al., 1996; Ronda et al., 2001). The model computes the dependece dependence of g_s and A with the internal CO_2 mole fraction, the amount of light, the atmospheric temperature, the vapor pressure deficit, and the soil water content at the root zone. Finally, the canopy net CO_2 assimilation is obtained with a function that is inspired by Fick's law of diffusion, that considers based on the difference of the atmospheric CO_2 and the internal CO_2 mole fractions, the aerodynamic resistance and the surface stomatal conductance.

The soil respiration is implemented as a function of soil temperature and soil moisture (Vilà-Guerau de Arellano et al., 2012). Combining the net assimilation (A_n) of the plants on canopy level and the soil respiration flux results in the net ecosystem exchange (NEE). This means that the model does not produces exactly the GPP and TER fluxes. ~~These~~ The differences between A_n and GPP, and soil respiration and TER are not directly relevant for our study and we therefore refer to GPP and TER in the following Sections, as these terms are more commonly used in the atmospheric CO_2 community. The water cycle is connected to the CO_2 cycle through the surface stomata and the soil moisture inhibition functions for assimilation and respiration.

3.2.2 Implementation of O_2 in CLASS

To model both ER_{forest} and ER_{atmos}, we incorporated the surface flux and the atmospheric mole fraction of O_2 into the CLASS model. We represent the surface flux of O_2 by multiplying the ER of assimilation (ER_a) and the ER of respiration (ER_r) with the CLASS-calculated CO_2 fluxes at the canopy scale. We used the observationally derived ER_a and ER_r values as previously determined in Faassen et al. (2023) for the same site, which were 0.96 and 1.03 respectively. The net surface flux of O_2 was then resolved with the following equation:

$$F(O_2)_s = F_{CO_2(a)} \cdot -ER_a + F_{CO_2(r)} \cdot -ER_r \tag{10}$$

where $F(O_2)_s$ is the net O_2 surface flux above the canopy, $F_{CO_2(a)}$ is the net assimilation flux and $F_{CO_2(r)}$ is the soil respiration flux. The change of atmospheric O_2 over time was resolved with Equation A1 (similar to Equation 1) and the entrainment flux is based on Equation A2 (see also Equation 2). Note that the ER_a from Faassen et al. (2023) was based on GPP fluxes and this ER_a is now linked to the net assimilation flux (GPP minus the photo and dark respiration) of the model (Jacobs et al., 1996; Ronda et al., 2001). Seibt et al. (2004) and Ishidoya et al. (2013) showed that ER_a values based on net assimilation have similar values compared to the 0.96 based on GPP. We therefore expect that this discrepancy will not influence our results.

It is important to note that the resulting ER_{forest} signal is not the (weighted) average between ER_a and ER_r, as was also shown by Faassen et al. (2023). The ER_{forest} signal results from the TER and GPP fluxes with different sizes and signs, ~~with each~~ each with their own ER signals (ER_r and ER_a respectively). Figure 3 shows that the resulting ER_{forest} signal does not necessarily fall inside the range of the ER_a and ER_r signals because the TER and GPP have opposite signs of the O_2 and CO_2 fluxes. This counter-intuitive situation can also occur for combining signals with different isotopic signatures (Miller and Tans, 2003).

3.2.3 Initial conditions

We determined initial and boundary conditions for two cases, to constrain the model to the observations. One case was based on the year 2019 (base case) and the other case was based on the year 2018 (characterized by a warm summer in Finland; Peters et al., 2020; Lindroth et al., 2020). Using the two years to initialize CLASS we were able to better constrain the vegetation's response in the CLASS model under extreme conditions. For each year, we selected one representative day for the initialization and validation of the CLASS model. We used 10-07-2019 for the base case and an aggregate between 28-08-2018 and
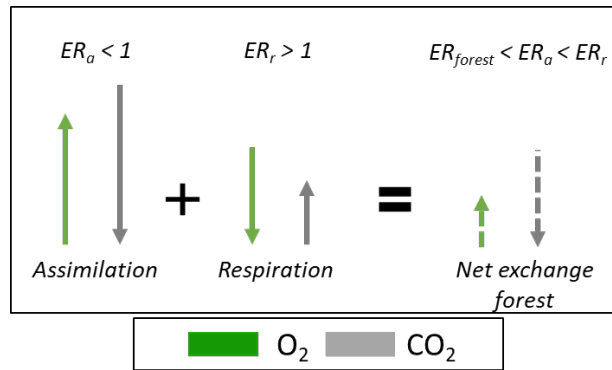
Figure 3. Schematic overview of how two processes with different ER signals produce a combined ER signal that is not necessarily the average of the two processes, nor necessarily falls inside the range of the two combined ER signals. This is due to the different signs for the O_2 and CO_2 fluxes. The example is given for combining the ER signal of Assimilation (ER_a) and Respiration (ER_r) into ER_{forest} and uses values from our study that are by coincidence larger and smaller than 1.

29-08-2018 for the warm case. The ~~final~~ initial and boundary conditions for the initialisation of the CLASS runs can be found in Tables C1 and C2 in the Appendix. Note that the initial jumps ($\Delta_{(ft-bl)}$) of O_2 and CO_2 are based on the best fit between the model and the observations during the day, as direct observations of the jumps were not available. A detailed discussion can be found in section 5.3.

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We deliberately made only minimal adjustments for the initialization of the 2018 case compared to the 2019 base case, to ensure consistency. We assumed that the initial relative humidity remained constant at 80%, regardless of temperature variations, similar to the studies of Vilà-Guerau de Arellano et al. (2012) and van Heerwaarden and Teuling (2014).

270   We adjusted several parameters of the A-g_s land surface scheme and the soil respiration to improve the agreement between the surface fluxes of the model and the observations in Hyytiälä for both the base case (2019) and the warmer case (2018) (Table C1). We decreased the mesophyll conductance (g_m: 2 mm s^{-1}) to better match pine forest conditions (Gibelin et al., 2008; ECMWF IV, 2014; Visser et al., 2021). Furthermore, the reference temperature of g_m ($T_{2(g_m)}$: 305 K) was increased to reduce afternoon plant stress and to make the CLASS run more comparable with the observations. Lastly, we adjusted the

275 curvature of the drought response curve (c_β) from zero to 15% (Combe et al., 2015), ~~considering~~ given that several studies demonstrate the pine forest in Hyytiälä to be relatively resilient to lower soil moisture values and thus needing a higher (c_β) value (Gao et al., 2017; Lindroth et al., 2020).

3.2.4 Sensitivity analyses

We conducted two sensitivity analyses to gain a deeper understanding of the ER_{atmos} behaviour under varying conditions and to identify factors that lead to a smaller difference between ER_{atmos} and ER_{forest}. ~~With these sensitivity analyses, the effect of Specifically, we looked at changes in~~ ER_{atmos} resulting from changing the different components of ~~Equation 8on is tested~~Eq. 8. The first sensitivity analysis uses the 2019 base case ~~, where we altered the initial jumps of and to and~~ investigate the effect of background air with a different composition by altering the initial jumps of O_2 and CO_2. By only changing the initial jump and keeping the rest of the 2019 case the same, we simulate situations in which the free troposphere mole fractions of O_2 and CO_2 have changed. In the second sensitivity analysis, we examined the impact of climate conditions by modifying the soil moisture and air temperature, mimicking the conditions observed during the 2018 heatwave. Table A1 presents the variables used for initializing four cases for these two sensitivity studies.

4 Results

In this results section, we first show our results for the validation of the CLASS model with observations (Section 4.1). Subsequently, we discuss the diurnal variability of both the ER_{forest} and ER_{atmos} signals (Section 4.2). We identify three distinct periods throughout the day in which ER_{atmos} shows large variability (Section 4.2.1). We address the large ER_{atmos} that we find in both the observations and the model results (Section 4.2.2). Finally, we perform sensitivity analyses to study the effects of changing large scale conditions, to show that our findings are not only valid for a single day (Section 4.3).

4.1 Validation of the O_2 and CO_2 model results

Overall, the modelled O_2 and CO_2 diurnal cycles match well with the observational data. Figures A3 and A2 in Appendix A4 show that CLASS accurately reproduces the diurnal cycles and captures the O_2 mole fraction changes on a daily time scale for both 2018 and 2019 (Figure A3b and A3c). The figure shows that the differences between the 2 years are relatively small and indicate that the boundary layer dynamics and the surface fluxes are well represented in CLASS. To accurately replicate the rapid decrease of CO_2 and the sharp increase of O_2 during the rapid growth of the atmospheric boundary layer (between 6:30 and 11:30), we adjusted the jump between the boundary layer and the free troposphere ($\Delta_{(ft-bl)}$) for both O_2 (30 ppmEq) and CO_2 (8 ppm), ensuring that the model aligned with the measurements. Based on values from previous studies, it is realistic for the CO_2 jump to range between 8 ppm and 40 ppm (Vilà-Guerau de Arellano et al., 2004; Casso-Torralba et al., 2008). ~~However,~~ While there is limited data available to validate the jump of O_2, based on preliminary results from a campaign in Loobos, the Netherlands, a jump of 30 ppmEq for O_2 seems reasonable. Our chosen combination of O_2 and CO_2 jumps remains an uncertain component in our analysis and will be further discussed in Section 5.3.

4.2 Diurnal variability of ER_{atmos} and ER_{forest} in 2018 and 2019

In this section, we discuss the diurnal variability of the ER_{atmos} ~~signals~~ signal for both the 2018 and 2019 cases~~and use Equation 8 to explain this diurnal variability~~. First, we focus on the budget components (GPP, TER and entrainment) that influence the ~~tendencies of~~ O_2 and CO_2 signals (Section 4.2.1). To complete the analysis, we support the numerical analysis with Equation 8 to gain a more comprehensive understanding of the underlying processes driving the ER_{atmos} signal for the 2019 case (Section 4.2.2).

4.2.1 The three distinct periods of the ER_{atmos} signal during daytime
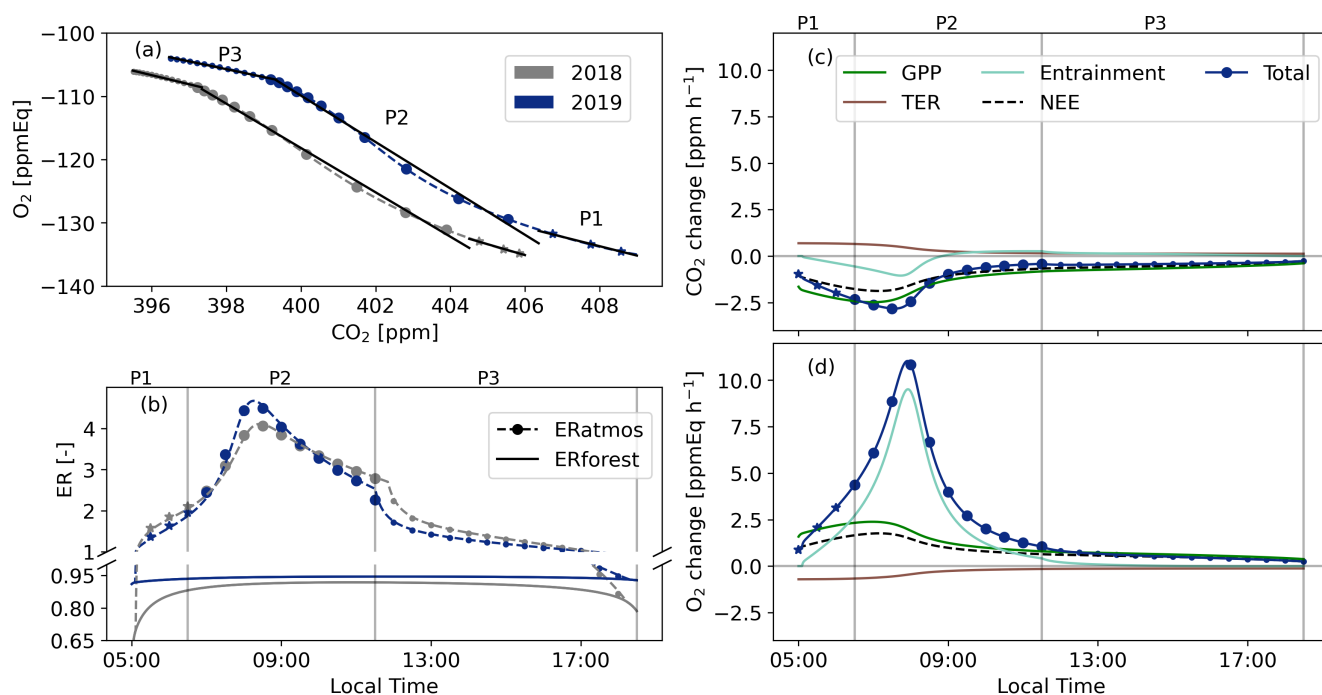
Figure 4. Diurnal cycles of O_2 and CO_2 mole fractions (a) and ER_{atmos} and ER_{forest} (b~~and e~~) as modelled with CLASS for the selected days in 2018 and 2019. We identify 3 distinct periods; P1 05:00-06:30 LT, P2 06:30-11:30 LT, and P3 11:30-18:30 LT, based on panels ~~d~~ c and ~~e~~d, which show the tendencies for the 2019 case (change over time) for CO_2 and O_2 for each process that influences their mole fractions (Equation 1). The symbols represent half hourly averaged values of the CLASS model output.

The ER_{atmos} signals obtained for the 2018 and 2019 experiments display large variability throughout the daytime (panels a and b in Figure 4). We identify three distinct periods during the day based on the processes shown in Figure 4~~d and 4e~~c and 4d: 1) the early morning regime (P1, 5:00-6:30 LT), characterised by an increasing net CO_2 flux ~~out~~ into of the forest but a non-growing boundary layer (Figure A3a), during which the ER_{atmos} signal during P1 is still relatively close to ER_{forest}; 2) the entrainment dominant period (P2, 6:30-11:30 LT), where air from a residual layer or air masses from the free troposphere are

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entrained into the boundary layer and significantly influence the signals, leading to large ER_{atmos} values, with an average greater than 3 and extreme values reaching close to 5; 3) the afternoon period (P3, 11:30-18:30 LT), where surface processes dominate the observed signals and ER_{atmos} moves slowly again towards ER_{forest} and become more consistent with values expected for surface processes. The ER_{atmos} values during the three identified periods show a good agreement between the observations and the model results (Table 1). This analysis confirms from a model perspective that values above 2 for ER_{atmos}, as we reported in Faassen et al. (2023), are indeed possible. Figures 4~~d and 4e~~ c and 4d give first indications on what could cause these high values for ER_{atmos}: high influence of entrainment and a different behaviour of the tendencies that influence O_2 compared to CO_2. In the next Section we discuss the diurnal behaviour of ER_{atmos} in more detail by using Equation 8.

We find that ER_{forest} is much less variable throughout the day than ER_{atmos} (Figure 4b~~and 4e~~). In the early morning and later afternoon the ER_{forest} value is lower than the mid-day period. This is caused by an almost equal TER flux (with a higher ER signal) to the GPP flux (with a lower ER signal) caused by low sun light (Figure 3). During mid-day the assimilation of CO_2 by the canopy, with a lower ER signal, becomes increasingly dominant causing the ER_{forest} signal to move closer to the ER_a value.

Table 1. ER_{atmos} values (calculated as the slope of the O_2 and CO_2 mole fractions) and ER_{forest} for the selected days in 2018 and 2019 for both observations (Obs) and the CLASS model for the three selected periods (P1: 5:00-06:30 LT, P2: 06:30-11:30 LT and P3: 11:30-19:30 LT). The uncertainties of the observed ER_{atmos} and ER_{forest} signals are determined following Faassen et al. (2023). Note that due to limited observational data we were unable to derive ER_{atmos} values for P1 and P2 in 2018 and for P1 in 2019.

| Year | ER_{atmos} (P1) | | ER_{atmos} (P2) | | ER_{atmos} (P3) | | ER_{forest} (P1-P3) | |
	Obs	Model	Obs	Model	Obs	Model	Obs	Model
2018	n.a.	1.72	n.a.	3.50	1.67 ± 0.51	1.43	0.87 ± 0.07	0.90
2019	n.a.	1.48	3.33 ± 0.31	3.66	1.23 ± 0.10	1.24	0.86 ± 0.06	0.94

4.2.2 Explanation of the large ER_{atmos} values

Analysing the diurnal cycle of the different components of Equation 8 for the 2019 case reveals that the peak value of ER_{atmos} during P2 is caused by the higher ~~values for β_{O_2} compared to β_{CO_2}~~ β values (the entrainment flux divided by the surface flux) for O_2 compared to CO_2 (Figure 5). The difference between β_{O_2} and β_{CO_2} is a result of a high $\Delta_{(ft-bl)}O_2/\Delta_{(ft-bl)}CO_2$ ratio (higher than 3). ~~These~~ The terms $\Delta_{(ft-bl)}O_2$ and $\Delta_{(ft-bl)}CO_2$ represent the jump across the boundary layer top, and each has a different diurnal cycle caused by a different surface flux (Figure 5c and 5g). ~~These~~ The different diurnal cycles for the jumps lead to an increase in the $\Delta_{(ft-bl)}O_2/\Delta_{(ft-bl)}CO_2$ ratio, consequently raising the ratio between the β values. This effect is further amplified by a higher surface flux of CO_2 compared to O_2, caused by an ER_{forest} value that is slightly lower than 1. The peak value of ER_{atmos} during P2 occurs when both w_e and the $\Delta_{(ft-bl)}O_2/\Delta_{(ft-bl)}CO_2$ ratio are high and the surface fluxes
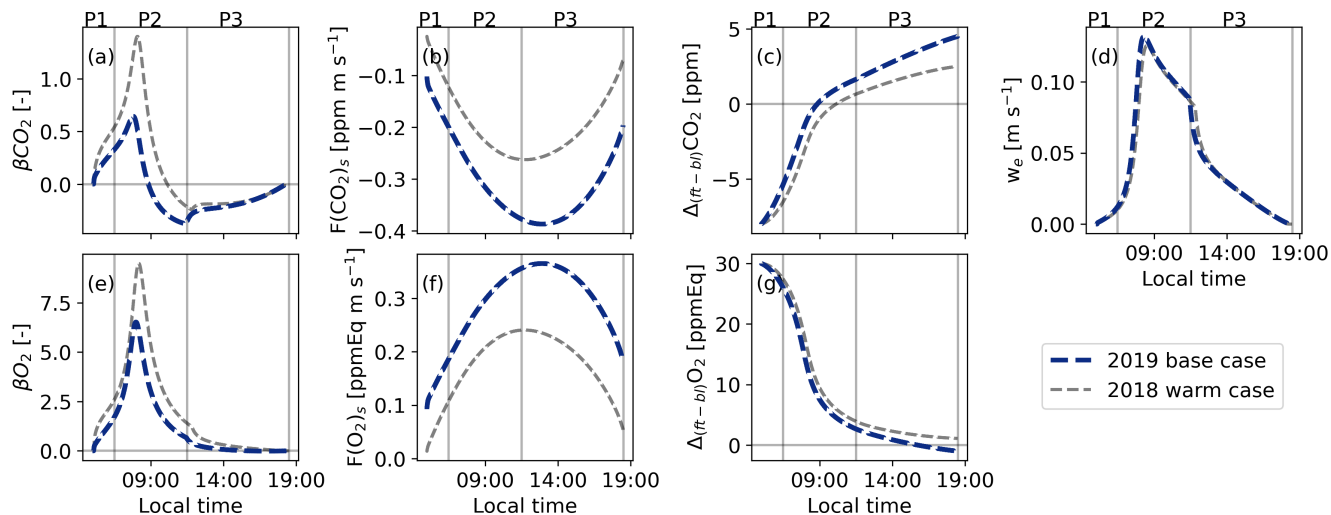
Figure 5. The diurnal variability of the different components of Equation 8 for the base case (2019) and the warm case (2018) derived with the CLASS model. (a) and (e) show the β values for CO_2 and O_2 where β is the entrainment flux divided by the surface flux (Equation 8), (b) and (f) show the net surface flux, (c) and (g) show the jumps between the free troposphere and the boundary layer ($\Delta_{(ft-bl)}$), (d) shows the entrainment velocity (w_e w_e)~~and (e) shows the resulting ratio between and during the day~~. The vertical lines represent three distinct periods: 05:00-06:30 LT (P1), 06:30-11:30 LT (P2), 11:30-18:30 LT (P3).

345   are still relatively low. This combination contributes to the distinctive peak in ER_{atmos} observed during P2.

      Later in the afternoon (P3), both β values gradually decrease and become similar, resulting in an ER_{atmos} signal that becomes closer to ER_{forest}. This indicates that ER_{atmos} becomes more representative for surface processes (see also Sect. A1). This decrease in P3 is primarily caused by a reduction in the entrainment velocity (w_e) (Figure 5d), indicating a slow growth of the

350   atmospheric boundary layer at end of the day (Figure A3). Additionally, the β values become more similar because $\Delta_{(ft-bl)}O_2$ moves closer to $\Delta_{(ft-bl)}CO_2$ during this period (Figure 5c and 5g), caused by the mixing of air with the surface.

      The ER_{atmos} signals exhibit higher values ~~compared to~~ than the theoretical analysis ~~in~~ of Sect. A1, because the diurnal cycles of the components of Equation 8 are taken into account (Figure A1 vs Figure 5). Each component of Equation 8 follows

355   its individual diurnal cycle, leading to higher ER_{atmos} values. Consequently, ER_{atmos} is integrating individual contributions of several processes, particularly during P2, since it is dominated by the influence of mixing with large scale processes. Careful consideration is needed when interpreting the ER_{atmos} signal during this period. During P3, the ER_{atmos} signal appears to align with ER_{forest} at the end of the day. However, in the 2019 case, this alignment was only observed for a very short period.

360 We find only small differences for the diurnal behaviour of the ER_{forest} and ER_{atmos} signal between the 2018 and 2019 case (Figure 4 and Figure 5). The ER_{forest} value is lower in 2018 compared to ~~2019.~~ 2019, specifically in the early morning and at the end of the day. This can be attributed to a higher respiration flux caused by the elevated air and soil temperatures during that day ~~which also results in an increase of the soil temperature~~ in 2018 (Figure A3e). A higher TER flux compared to the GPP flux will decrease the ER_{forest} value (Figure 3. While we do not have direct measurements of ER_r and ER_a for both 2018 and

365 2019, it is likely that the overall diurnal cycle pattern of ER_{forest} in Figure 4b (low ER_{forest} values in the morning and afternoon, higher ER_{forest} values during mid-day) for both years would have remained consistent. Previous studies suggest that ER_r is generally higher than ER_a, even under different atmospheric conditions (Angert et al., 2015; Fischer et al., 2015; Hilman et al., 2022). The effect of a warmer and dryer environment on the ER_{atmos} signal will be further quantified in Sect. 4.3.2 with a more extreme case.

370 ## 4.3 Sensitivity analyses: effects of changing large scale conditions

With the next two sensitivity analyses we evaluate whether our findings for the 2019 case ~~was an exception and if there are cases where the signal could become equal to when large scale conditions would change. We~~ are exceptional, or whether they can also occur under different (large scale) conditions. We therefore analyse days with different initial conditions compared to our 2019 and 2018 cases. We focus on the effect of changes in the background air (Sect. 4.3.1) and the effect of ~~climate~~

375 ~~(changes in~~ changes in the climate conditions (soil moisture and air temperature~~) (~~, Sect. 4.3.2). ~~Figure 6 shows~~ With these sensitivity analyses we show the complexity of the ER_{atmos} signal and all the processes that can influence it. Figure 6 is used to illustrate how ER_{atmos} is formed by the different components of ~~Equation 8, and how the variables changed in the sensitivity analyses impact these components and therefore~~ Eq. 8.

380 ## 4.3.1 Effects of changing background air on ER_{atmos}

Changing the background air in the free troposphere by decreasing the initial jump ratio or the jump sizes of O_2 and CO_2 compared to the 2019 case, moves the ER_{atmos} signal closer to ER_{forest} during P2 and P3 (Figure B1). A lower jump ratio than the 2019 case, but still relatively high jump values ($\Delta_{(ft-bl)}O_2$ = 30 ppmEq and $\Delta_{(ft-bl)}CO_2$ = -20 ppm) lead to a decrease in the peak of ER_{atmos} during P2 and bring ER_{atmos} closer to ER_{forest} during P3 (yellow line in Figure B1). As the jump ratio

385 decreases, the β_{O_2} becomes less dominant and ~~more identical~~ closer to β_{CO_2}. When the O_2 and CO_2 β values become closer, the ER_{atmos} value also moves closer to ER_{forest} (Figure 6). However, this does not necessarily mean that the surface has become more dominant since the $\Delta_{(ft-bl)}$ values are still relatively high.

Reducing the jump sizes of both O_2 and CO_2 ($\Delta_{(ft-bl)}O_2$ = 10 and $\Delta_{(ft-bl)}CO_2$ = -8) still results in a relatively high peak

390 for ER_{atmos} during P2 and bring ER_{atmos} closer to ER_{forest} during P3 (purple line in Figure B1). Including the diurnal cycle of the jumps accounts for the effect that the CO_2 jump changes from a negative to a positive value during the day. When the initial CO_2 jump is lower, the sign change occurs earlier in the day and leads to a more negative β_{CO_2} value. This leads to

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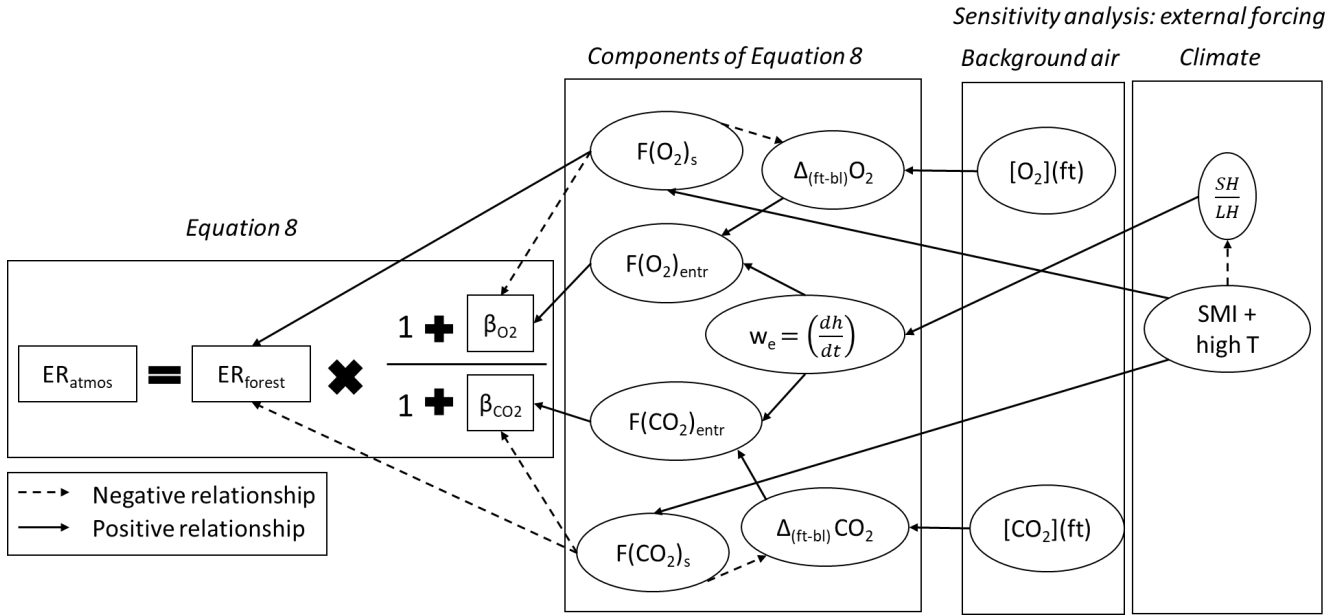
Figure 6. The components of Equation 8 and how these influence the ER_{atmos} signal, including: the exchange ratio of the forest (ER_{forest}), the ratio between the net surface flux (F_s) and the entrainment flux (F_{entr}) which result in the β, the jump between the free troposphere and the boundary layer ($\Delta_{(ft-bl)}$) and the entrainment velocity (w_e). The right part of the Figure shows the variables that are changed in the two sensitivity analyses: the background air in the free troposphere ($[O_2](ft)$ and $[CO_2](ft)$) and the initial Soil Moisture Index (SMI) in combination with a high initial potential temperature (θ_0) that will influence the ratio between the sensible heat flux (SH) and the latent heat flux (LH) at the surface. The dotted arrows indicate a negative influence and the solid arrows indicate a positive influence.

higher ER_{atmos} values during P2 (Figure 6). In contrast, a lower jump size would cause the ER_{atmos} signal to move more quickly towards ER_{forest} during P3 because the surface fluxes dominate over the lowered entrainment flux.

395

Guided by our theoretical and numerical results and constrained by observations, a high ER_{atmos} signal during the entrainment dominant period (P2) can therefore be a result of two cases:

1. The $\Delta_{(ft-bl)}O_2$ is substantially larger compared to $\Delta_{(ft-bl)}CO_2$ and therefore β_{O_2} dominates over β_{CO_2}.

2. $\Delta_{(ft-bl)}CO_2$ changes sign from negative to positive and as a result β_{CO_2} becomes negative resulting in a denominator
400   closer to zero.

Changes in the background air result in a distinct change in the diurnal pattern of ER_{atmos}. The difference between the ER_{atmos} and ER_{forest} signal could therefore provide extra information on the changes of large scale processes. This is further discussed in Sect. 5.2.

4.3.2 Effect of climate conditions on ER_{atmos} and ER_{forest}

By studying the influence of changes in air temperature and soil moisture index (SMI: [soil moisture - w_{wilt}]/[w_{fc} - w_{wilt}]) on the ER_{atmos} signal (see Figure 7), we gain insights into how climate conditions can effect ER_{atmos} compared to ER_{forest}. This allows us to study the effects of seasonality or future climate with dryer and warmer conditions. The 2018 case already showed how the ER_{atmos} signal could change with a decreasing SMI and increasing temperature compared to a more normal year in 2019 (Figure 4 and 5). As a next step, we evaluate the full range of how ER_{atmos} could change and how ER_{atmos} compares to ER_{forest}. Given the same net radiation, a higher SMI enhances soil respiration, photosynthesis and latent heat fluxes, and thus decreases the sensible heat flux because of the energy balance closure, this therefore leads to a smaller boundary layer growth and as a result, decrease the entrainment velocity (see Figure 6). In addition, higher air temperatures accelerate both the photosynthesis and the respiration, up to a threshold (Jacobs et al., 1996), resulting in increased GPP and TER fluxes. A lower SMI in combination with higher temperatures can stress plants, leading to decreased O_2 and CO_2 surface fluxes and an enhanced sensible heat flux. This will increase the boundary layer growth and the entrainment velocity (Equation 2 and 4). Note that there are also minor changes for ER_{forest} when the SMI and air temperature change as a result of GPP and TER changes.

Increasing or decreasing the SMI in combination with changes in air temperature makes the diurnal variability of ER_{atmos} more complex because all the components of Equation 8 are now affected (Figure 6 and Figure 7). We focus on two particular locations in the parameter space shown in Figure 7: a low soil moisture (red symbol) and a high soil moisture case (green symbol), both with higher temperatures compared to the 2019 case (Figure B2).

A lower soil moisture of 0.14 m^3 m^{-3} (SMI = 0.27) with an air temperature of 290 K decreases ER_{atmos} during P2 and increases ER_{atmos} during P3 compared to the 2019 base case (the red lines in Figure B2 and red symbol in Figure 7). The lower ER_{atmos} values during P2 are primarily a consequence of a more dominant entrainment flux. Due to a decrease in the O_2 and CO_2 surface fluxes because of stressed plants, both the $\Delta_{(ft-bl)}$ values for O_2 and CO_2 change more slowly and remain high. Higher $\Delta_{(ft-bl)}$ values, along with a higher entrainment velocity caused by a higher sensible heat flux, lead to elevated entrainment fluxes. By increasing both the O_2 and CO_2 entrainment fluxes and decreasing the O_2 and CO_2 net surface fluxes, the β values increase and the ratios of the β values move towards the $\Delta_{(ft-bl)}$ ratios. As a result, the ER_{atmos} also moves towards the $\Delta_{(ft-bl)}$ ratios multiplied with the ER_{forest} signal (Figure 6). This is similar to the effect observed when increasing both the initial jumps of O_2 and CO_2 (Sect. 4.3.1). The β values stay high during P3 because of the low net O_2 and CO_2 surface fluxes. Therefore, the ER_{atmos} signal also remains close to the ratio of the $\Delta_{(ft-bl)}$ values during P3 and the ER_{atmos} signal does not approach ER_{forest} (Figure 6).
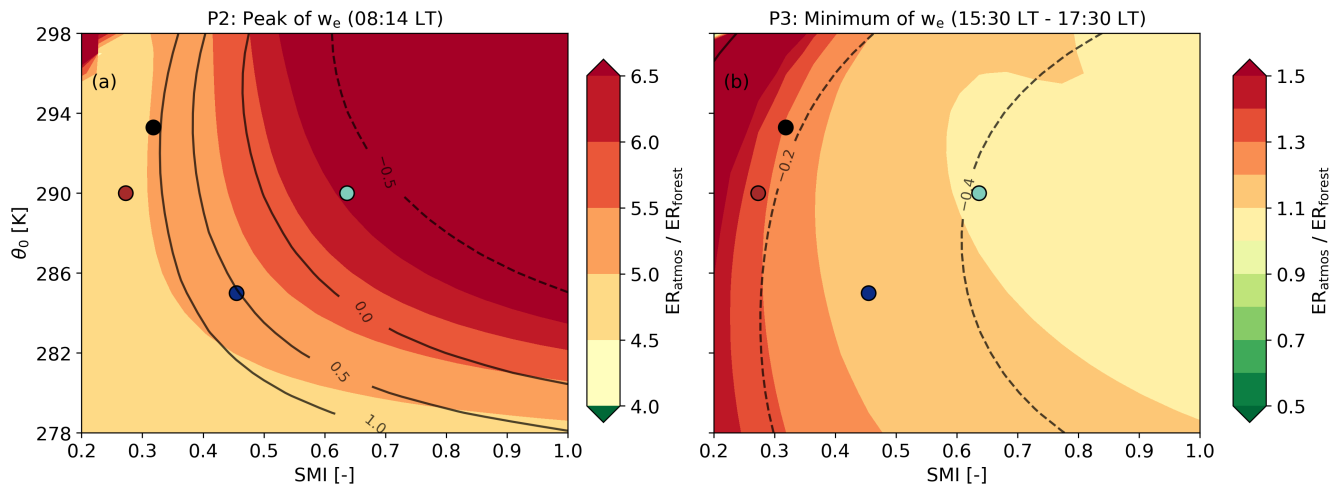
Figure 7. Evaluation of the ratio between ER_{atmos} and ER_{forest} as a function of two key variables that show the effect of a drier and warmer climate: the Soil Moisture Index (SMI) and the initial potential temperature (θ_0). Two moments in the day are analysed, (a) during the maximum value of w_e at 08:14 LT (P2) and (b) at the end of the day between 15:30 - 17:30 LT when the w_e is minimal (P3). The grey lines in (a) indicate β_{CO_2} values, which is the ratio between the entrainment and the surface flux. The grey lines in (b) indicate net CO_2 surface flux values in ppm m s^{-1}. The coloured symbol (brown and light blue) indicate the example cases that are also shown in Figure B2 and the black dot is the 2018 case and the dark blue dot the 2019 case.

In contrast, a higher soil moisture of 0.22 m^3 m^{-3} (SMI = 0.64) with an air temperature of 290 K increases the ER_{atmos}
440   signal during P2 and decreases the ER_{atmos} signal during P3 compared to the 2019 base case (the green lines in Figure B2 and green symbol in Figure 7). This is consistent with the effect observed when lowering the initial $\Delta_{(ft-bl)}$ value (Sect. 4.3.1).

In addition to the conclusions in Sect. 4.3.1 on the causes of the high ER_{atmos} signals during P2, the sensitivity analyses for changing climate conditions showed that the large differences between ER_{atmos} and ER_{forest} at the end of the day (P3) can be
445   caused by:

1. A substantially larger $\Delta_{(ft-bl)}O_2$ compared to $\Delta_{(ft-bl)}CO_2$ causing β_{O_2} to dominate over β_{CO_2}.

2. High β_{O_2} and β_{CO_2} values because of high O_2 and CO_2 entrainment fluxes and/or low net O_2 and CO_2 surface fluxes.

Our two sensitivity analyses show that several factors, including the entrainment velocity, the $\Delta_{(ft-bl)}$ values and their ratio and the net surface flux of CO_2 can significantly influence the diurnal behaviour of ER_{atmos}. When using ER_{atmos} as an
450   indication of ER_{forest}, these four factors should be carefully considered. This is crucial to correctly interpret ER_{atmos} values and to understand the underlying processes that influence the carbon exchange above a forest canopy.

5   Discussion

In this discussion section, we first address the evaluation of the CLASS model (Section 5.1). Secondly, we elaborate on the issues we found with ER_{atmos}, and how this value should (and should not) be used (Section 5.2). Thirdly, we discuss the importance of the differences between the free troposphere and boundary layer values for O_2 and CO_2 (Section 5.3). Finally, we put our work in perspective by comparing it to other studies using atmospheric O_2 (Section 5.4) and to studies on other carbon cycle tracers (Section 5.5).

5.1   Evaluation of the CLASS model

Our implementation of O_2 in the CLASS model could be improved in future studies. Similar to the approach used by Yan et al. (2023), both the ER_r and ER_a signals were kept constant and did not account for potential variations under different climate conditions. To advance our understanding of the ER signals over forest canopies, it is crucial to incorporate ER signals that can respond to varying soil and atmospheric conditions. For instance, the ER_r of the soil respiration depends on air temperature and soil moisture (Hilman et al., 2022; Angert et al., 2015), while the ER_a is primarily influenced by ~~nitrogen content and~~ light on leaf level, and nitrogen availability in the soil (Bloom, 2015; Fischer et al., 2015). Additionally, in our current implementation, we did not include the ER for stem respiration (ER_{stem}) (Hilman and Angert, 2016) due to the absence of stem respiration in the CLASS model.

While we utilized CLASS in this study as a proof of concept to demonstrate how ER_{atmos} ~~changes~~ can change during the day, employing a more elaborate model could allow for more detailed exploration of these ER_{atmos} dynamics and the contributions of various processes. Models with more vertical levels could simulate vertical gradients and analyze differences in the ER_{atmos} signal at various heights, similar to the approach in Yan et al. (2023). Implementing more vertical levels gives the opportunity to determine the dominance of large scale processes over small scale surface processes at different measurement heights. By incorporating a canopy into the model, the surface resistance could be accounted for, enhancing the accuracy of the modeled surface fluxes. Furthermore, exploring larger temporal and spatial scales could yield valuable insights in the variability of ER_{forest} over time and space, in contrast to our CLASS model that is only valid during the day when the SH flux is larger than zero. Increasing the temporal ~~scales~~ scale gives the opportunity to improve estimates of ~~the~~ ER_{forest} ~~values used as the globally used~~. This also has the potential to improve estimates of the global biospheric ER, currently taken to be 1.1 ~~biosphere ERsignal~~ (Severinghaus, 1995).

5.2   How ER_{atmos} should be used

Single height O_2 and CO_2 measurements and their ER_{atmos} signal should be analysed very carefully when using it as an indicator for surface exchange. During the complete diurnal cycle, ER_{forest} should be utilized as the primary indicator of the ER signals from the surface, while ER_{atmos} should not be used for this purpose. In situations where only one height measurement

is available, and therefore only ER_{atmos} can be obtained, a first estimate of ER_{forest} could be made using ER_{atmos}. The ER_{atmos} signal at the end of the day should then be used to avoid the large influence of entrainment earlier in the day. However, any analysis or discussion based on this estimation should include a comprehensive examination of how entrainment might have influenced the ER_{atmos} signal. This also applies for less representative or non-typical days where the mixed layer theory may be difficult to apply. An example of such case is given by Casso-Torralba et al. (2008), where it is shown that entrainment is still important on a non-typical day, when polluted air is influencing the diurnal CO_2 measurements.

Several studies have showed that ER_{atmos} can also serve as an indicator of potential advection from carbon source/sink regions (Ishidoya et al., 2020, 2022a). ~~Nevertheless~~However, caution should be exercised when directly inferring the specific source based solely on the ER_{atmos} value. Equation 9 shows that mixing advected air with the air above a forest will result in an ER_{atmos} signal that cannot be directly linked to the source of the advected air. ~~Next to the influence of the surface and entrainment, the signal also depends on the magnitude of the advected flux because of the effect that~~ This is because mixing two ER signals with opposite fluxes does not result in a weighted average (Figure 3). Advection of a source with the ~~same~~ a known ER signal but with different magnitudes can therefore give different ER_{atmos} ~~signals~~values. A solution could be to include other ~~pollutants~~ tracers in the analysis such as NO_x or CO (Liu et al., 2023a).

When two or more measurement heights of O_2 and CO_2 are available, and therefore ER_{forest} can be derived, ER_{atmos} of a single height could be used to provide extra information on large scale processes ~~,~~ by analysing the difference between ER_{atmos} and the ER_{forest} signal. ~~Throughout~~ During the day, ER_{atmos} provides insights into larger scale processes, while ER_{forest} reflects local or small-scale processes. Therefore, any discrepancy between ER_{atmos} and ER_{forest} indicates a significant influence of large scale processes. Nonetheless, the exact difference between ER_{atmos} from ER_{forest} should not be used as an indication of the strength of the influence of large processes. To get more detail on how the large scale processes change between days, the diurnal cycle of ER_{atmos} has to be compared during the entrainment dominant period (P2) and the surface dominant periods (P3). During P2, an increase in the difference between ER_{atmos} and ER_{forest} ~~can be attributed~~ may be due to either a low β_{CO_2} or a change in the jump ($\Delta_{(ft-bl)}$) ratio. ~~When a~~ If the cause is the former (low β_{CO_2} ~~causes the high values during P2~~), the ER_{atmos} signal during P3 should be closer to ER_{forest}~~, compared to the situation where~~. If the latter (a high jump ratio~~leads to elevated~~)~~,~~ ER_{atmos} ~~values~~should remain well above ER_{forest} in P3.

5.3 Different $\Delta_{(ft-bl)}$ ratios

Knowing the vertical profile of O_2 and CO_2 especially during sunrise is essential to gain a more comprehensive understanding of the formation of different jump ratios ($\Delta_{(ft-bl)}O_2$ / $\Delta_{(ft-bl)}CO_2$) and to better interpret the diurnal behavior of the ER_{atmos} signal. However, due to lack of observational data we cannot validate the vertical profile of O_2 and CO_2 and the jump ratios~~and we recommend for~~. We therefore strongly recommend that future measurement campaigns ~~to~~ include vertical measurements of both species~~, e. g.~~. This can for example be done by flask sampling from aircraft.~~ Although some studies have~~ , as we
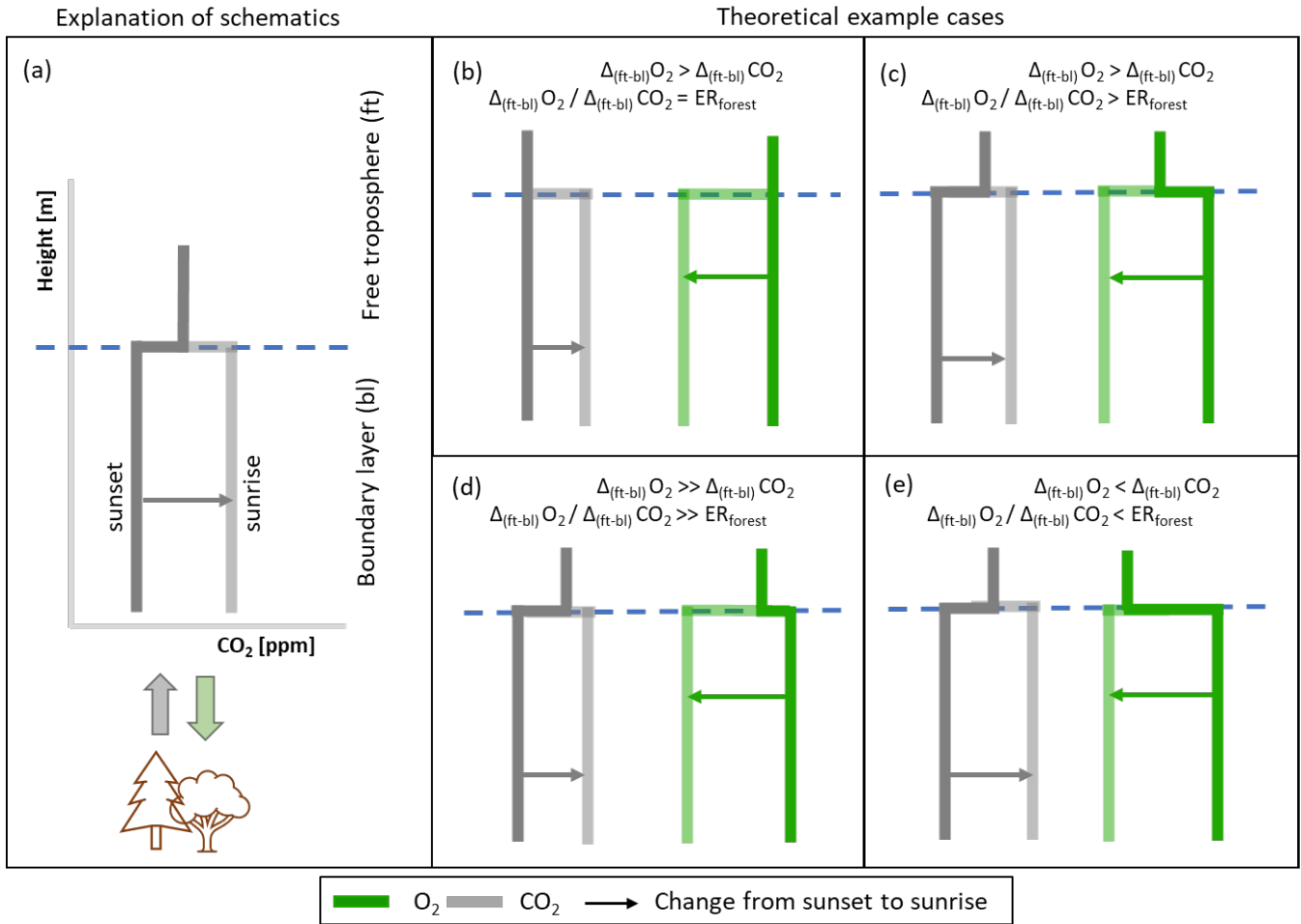
Figure 8. A schematic overview of how different ~~jump~~ ratios ~~are possible between~~ of the jumps of O_2 ($\Delta_{(ft-bl)}O_2$) and CO_2 ($\Delta_{(ft-bl)}CO_2$) are formed in the nighttime and how the ratio relates to the Exchange Ratio of the forest (ER_{forest}). Panel (a) ~~shows~~ gives an ~~overview explanation of~~ the schematics and the other panels show ~~different~~ four possibilities of different jump ratios ~~: (b)~~ $\Delta_{(ft-bl)}O_2/\Delta_{(ft-bl)}CO_2$): (b) the jump ratio is equal to ER_{forest}, (c) ~~$\Delta_{(ft-bl)}/\Delta_{(ft-bl)}$~~ the jump ratio is larger than ER_{forest}, (d) ~~$\Delta_{(ft-bl)}/\Delta_{(ft-bl)}$~~ the jump ratio is much larger than ER_{forest}, (e) ~~$\Delta_{(ft-bl)}$~~ the jump ratio is smaller than ~~$\Delta_{(ft-bl)}$~~ER_{forest}. The ~~numbers in (a) indicate: (1) Surface flux size during night, (2a) mixed layer mole fraction~~ bold lines represent the vertical profile just ~~before~~ after sunset ~~, (2b) mixed layer mole fraction just before sunrise~~ and ~~(3) mole fraction in~~ the ~~free troposphere with~~ shaded lines represent the ~~corresponding lapse rate, which for~~ ~~and the lapse rate is assumed to be 0 ppm m^{-1}~~ vertical profile just before sunrise.

have done in a recent campaign in the Netherlands, of which preliminary results confirm that the values we have used here are realistic. Previous studies have also measured vertical profiles of O_2 and CO_2, but they primarily focused on well-mixed profiles during daytime or profiles over the ocean (Morgan et al., 2019; Stephens et al., 2021; Ishidoya et al., 2022b). Hence, careful consideration of the timing and location of the vertical measurements is important to advance our knowledge of the

diurnal behaviour of ER_{atmos}.

525 ~~Due to lack~~ In the absence of observational data, we show with hypothetical situations that various jump ratios become possible (Figure 8). Both the O_2 and CO_2 jumps are formed as a result of three processes; the mixed-layer value before sunset (2a), the surface flux during the night (1) and the free troposphere value with the lapse rate (3) (we assume the lapse rate to be 0 mol m^{-1} for CO_2 and O_2). Most cases indicate that $\Delta_{(ft-bl)}O_2$ is larger than $\Delta_{(ft-bl)}CO_2$ above a forest, primarily because ER_{forest} is higher than 1.0 during the night ($ER_r > 1.0$) as was shown in previous studies (Ishidoya et al., 2013; Angert et al., 2015; Hilman et al., 202

530 . It is noteworthy that the movement of the mixed-layer values from (P2a) to (P2b) in Figure 8 differs from its depiction in Figure 2c, where the focus was primarily on the transition between sunrise and sunset. We ignore the effect of subsidence (caused by mesoscale or synoptic processes) on the jump evaluation in this analysis, ~~caused by mesoscale or synoptic processes,~~ because it is likely of less importance compared to the other three processes.

535 It is highly likely that the jump ratio between O_2 and CO_2 cannot be directly linked to a specific ER for a certain process because of the interplay between the three processes that form the O_2 and a CO_2 jump (Figure 8d). The likelihood of both $\Delta_{(ft-bl)}O_2$ and $\Delta_{(ft-bl)}CO_2$ being zero at the end of the day is low because the surface flux during the day would form a jump (Figure 8c). Additionally, it is possible that the $\Delta_{(ft-bl)}O_2$ is smaller than $\Delta_{(ft-bl)}CO_2$ at the end of the day (Figure 8d) due to the daytime ER_{forest} being smaller than 1.0~~(Figure 8d)~~. Consequently, O_2 will exhibit a faster movement across the zero

540 line, resulting in a significantly larger $\Delta_{(ft-bl)}O_2/\Delta_{(ft-bl)}CO_2$ ratio compared to ER_r.

Decoupling between the free troposphere and the boundary layer can lead to a scenario in which $\Delta_{(ft-bl)}CO_2$ becomes larger than $\Delta_{(ft-bl)}O_2$ (Figure 8e). This can ~~e.g. occur~~ occur for example, when the influence of fossil fuel sources causes a decrease in the O_2 mole fraction and an increase in the CO_2 mole fraction in the free troposphere, but large surface fluxes from

545 the forest prevent such changes from occurring in the boundary layer. The jump ratio in this case again cannot be attributed to a single process. Some studies have demonstrated that decoupling between the boundary layer and the free troposphere can occur, leading to different ER signals (Sturm et al., 2005; van der Laan et al., 2014).

5.4 Comparison with other studies

550 To the best of our knowledge, no previous studies have reported such high deviations of ER_{atmos} from ER_{forest}, or ER_{atmos} values higher than 2 for above forest canopy measurements as we found in Faassen et al. (2023). Only Liu et al. (2023b) found a ~~difficult to explain nonlinear~~ non-linear relationship between O_2 and other ~~pollutants~~tracers that was difficult to explain. While some differences between ER_{atmos} and ER_{forest} have been observed in previous studies, these differences typically fall within a range of 0.5 (Seibt et al., 2004; Ishidoya et al., 2015; Battle et al., 2019; Yan et al., 2023). A possible reason for

555 these smaller differences could be that most studies do not focus on such detailed diurnal analyses of ER_{atmos} for specific days but rather aggregate data from multiple days, which could mitigate the extreme effects of entrainment by combining

various jump possibilities. However, even in the study by Stephens et al. (2007), in which measurements at different heights are shown, no discernible difference in the ER_{atmos} signal for various diurnal cycles was observed, a finding that contrasts with our own analysis. The height at which measurements are made also influences the resulting ER_{atmos} signal. Closer to the canopy, the influence of entrainment is lower and ER_{atmos} is closer to ER_{forest} compared to measurements further away from the canopy (Faassen et al., 2023). However, we still found a high ER_{atmos} value of 2.28, even at a level just above the canopy (Faassen et al., 2023). Large values for ER_{atmos} have only been found at high latitude measurement stations (Sturm et al., 2005), due to the influence of the ocean.

There are several possibilities that could explain a constant ER_{atmos} signal during the day, which are not shown in our study. One possibility is that entrainment dominates throughout the day, caused by high jumps. If both the O_2 and CO_2 jumps are extremely high while the surface flux remains low, the ER_{atmos} value reflects the ratios between the jumps. In this scenario, ER_{atmos} cannot be used as an accurate indicator for the surface processes. Another explanation could be that the ER_{forest} signal is exactly 1.0 and entrainment is relatively low. When ER_{forest} equals 1.0, the diurnal cycle of the jumps would respond similarly. Together with a low entrainment flux (resulting from low jumps), it could lead to a constant ER_{atmos} ~~signal~~value. Additionally, when the peak of ER_{atmos} occurs rapidly, there is a possibility that a low measurement precision would miss the extreme changes of ER_{atmos}. However, even in such cases, ER_{atmos} would still be influenced by entrainment, although its impact may be less discernible. It is crucial to note that ~~,~~ in all these cases, ER_{atmos} remains influenced by entrainment to varying degrees.

Our study provides evidence that ER_{atmos} is almost always influenced by large scale processes and their diurnal variability, specifically entrainment, making it important to exercise caution when using it as an indicator for the surface ER processes. Instances where ER_{atmos} remains constant throughout daytime and serves as a reliable indication for ER_{forest} are likely rare. In comparison to previous studies (Seibt et al., 2004; Stephens et al., 2007; Ishidoya et al., 2013; Battle et al., 2019), it is unclear why Faassen et al. (2023) yields such extreme values for ER_{atmos} while the other studies do not show this, even though our modelling study here confirms the extreme ER_{atmos} values. Therefore, we recommend conducting more studies or performing detailed analyses of existing O_2 and CO_2 data sets to gain a better understanding of how changes in ER_{atmos} vary with time and space.

5.5 Comparison with other multi-tracer analyses

The impact of changes in large scale conditions such as entrainment on multi-tracer analyses above forest canopies extends beyond atmospheric O_2, encompassing other carbon cycle tracers such as carbon and oxygen isotopes ($\delta^{13}C$ and $\delta^{18}O$) (Wehr et al., 2016), and carbonyl sulfide (COS) (Whelan et al., 2018). Caution is required when employing methods of determining ratios between two species (eg. leaf relative uptake for COS and the ratios between different isotopes) that rely solely on single-height measurements. However, the influence of entrainment on these ratios would be less extreme compared to the ER_{atmos} signal because both COS and isotopes move in the same direction as CO_2 itself. This is different compared to O_2, which always

moves in the opposite direction compared to CO_2. When both species that form the ratio move in the same direction, ratios of different processes could be averaged and a one height measurement is more readily interpretable. Nevertheless, entrainment would still cause the two compounds that form the ratio to behave differently. We therefore emphasize the need to separately analyze the composition of the signal for each compound when ratios are analyzed.

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Furthermore, we demonstrate in this study the potential of using ER_{atmos} as an indicator of the extent of large scale processes. Additional tracers can ~~contribute to this question~~strengthen this approach. $\delta^{13}C$, $\delta^{18}O$ and COS signals exhibit differences between the surface and the free troposphere. Similar to O_2, the onset of entrainment causes these signals to mix, yielding insights into how large scale processes influence the carbon cycle above a canopy (Berkelhammer et al., 2014; Vilà-Guerau de Arellano et al., 2019). By combining various tracers for CO_2, we can create a comprehensive picture of the effects of small scale and large scale processes that influence carbon exchange.

6   Conclusions

We used a mixed-layer model to analyze the diurnal behavior of two Exchange Ratio (ER = O_2/CO_2) signals above a forest canopy: the ER of the atmosphere (ER_{atmos} determined from the change over time of O_2 and CO_2 mole fraction measurements at a single height above the canopy) and the ER of the forest (ER_{forest} determined from O_2 and CO_2 fluxes derived from the vertical gradient observations at two levels). We disentangled the biophysical processes influencing ER_{atmos} to interpret single height O_2 and CO_2 measurements and to evaluate how both ER_{atmos} and ER_{forest} can be used to constrain carbon exchange above the canopy. The analysis is supported by the derivation of a new theoretical relationship that connects ER_{atmos} and ER_{forest} and by the use of a mixed-layer model that reproduces the O_2 and CO_2 diurnal cycles coupled to the dynamics of the atmospheric boundary layer. By combining the model with observations in a boreal forest during two contrasting summers of 2018 and 2019, we found three regimes during the day for ER_{atmos}.

We find that the entrainment of air from the free troposphere leads to a diurnal cycle in ER_{atmos}, resulting in three distinctive regimes: P1 at the start of the day, when the boundary layer has not yet started to grow, P2 when entrainment of air from the free troposphere into the boundary layer is dominant, and P3 at the end of the afternoon when entrainment becomes negligible. ER_{atmos} can exhibit high values during P2 that cannot be attributed to an ER signal from a single process. During P3, ER_{atmos} becomes closer to ER_{forest}, and is therefore more representative for the forest exchange.

The large diurnal variability in ER_{atmos} shows that single height O_2 and CO_2 measurements are insufficient to be used as an indication for the O_2/CO_2 ratios of forest exchange. Our theoretical relationship between ER_{atmos} and ER_{forest} and model results show that the large diurnal variability is a result of the different behaviour of the O_2 and CO_2 diurnal cycle, which results in ER_{atmos} values that cannot be attributed to a single process. To estimate the ER signal of the surface fluxes from above canopy

measurements, ER_{forest} should be used and therefore O_2 and CO_2 signals need to be measured at at least two heights, to allow fluxes to be calculated from the vertical gradient. A single measurement height of O_2 and CO_2 could still be used to indicate the presence of advection of other carbon sources. However, the resulting ER_{atmos} signal should be analysed with care, by taking into account the diurnal variability and the fact that the resulting ER is not necessarily the average of the individually ER signals of the contributing processes.

When O_2 and CO_2 measurements are available from 2 heights, the relationship between ER_{atmos} and ER_{forest} during P2 and P3 could provide valuable information about the changes in large-scale carbon processes (e.g. entrainment) and their influence on the smaller scale processes of the surface. A discrepancy between ER_{atmos} and ER_{forest} shows that large scale processes occur together with small scale processes at the surface. The difference between ER_{atmos} and ER_{forest} should be analysed with care as the size of the difference is not a direct indication of the size of the influence of the large scale processes. Differences between ER_{forest} and ER_{atmos} could be caused by several factors: changes in the size of the entrainment flux, the net surface flux or the difference between the free troposphere and the boundary layer (the 'jump') for O_2 and/or CO_2, or changes in the jump ratio between O_2 and CO_2.

In conclusion, single height O_2 and CO_2 measurements need to be analyzed with care, accounting for their dependence on canopy processes (represented by ER_{forest}), but also for their capacity to integrate large scale processes resulting in values that cannot be attributed to a single process. To represent the forest exchange, the ER_{forest} signal based on measurements at at least two heights should be used instead.

Appendix A: Appendix

A1 Evaluation of the theoretical relationship between ER_{atmos} and ER_{forest}

In this Section, we analyze Equation 8 to explore the response of ER_{atmos} to changes in the variables in this equation and to investigate when ER_{atmos} aligns with ER_{forest} and thereby accurately reflects local processes. Based on Equation 8, the ER_{atmos} signal equals ER_{forest} when the β values of O_2 and CO_2 are equal. We can define four different regimes where the β values change significantly. As depicted in Figure 1 we can define two regimes based on the entrainment velocity: an entrainment driven (left panels in Figure A1) and a photosynthesis driven regime right panels in Figure A1). To complete the analysis we considered two distinct cases for the jump of O_2 (top versus bottom panels).

Based on Equation 8 we systematically varied $\Delta_{(ft-bl)}CO_2$ and $(F_{CO_2})_s$ over plausible ranges and kept the other variables constant. As a result we derived ER_{forest}:ER_{atmos} ratios for these four regimes, where a value of 1.0 now indicates that ER_{atmos} is equal to ER_{forest}. The selected values and ranges for the four different cases were informed by initial conditions from the Hyytiälä case, studied in Faassen et al. (2023) and the corresponding model simulations presented in Section 3.2.4.
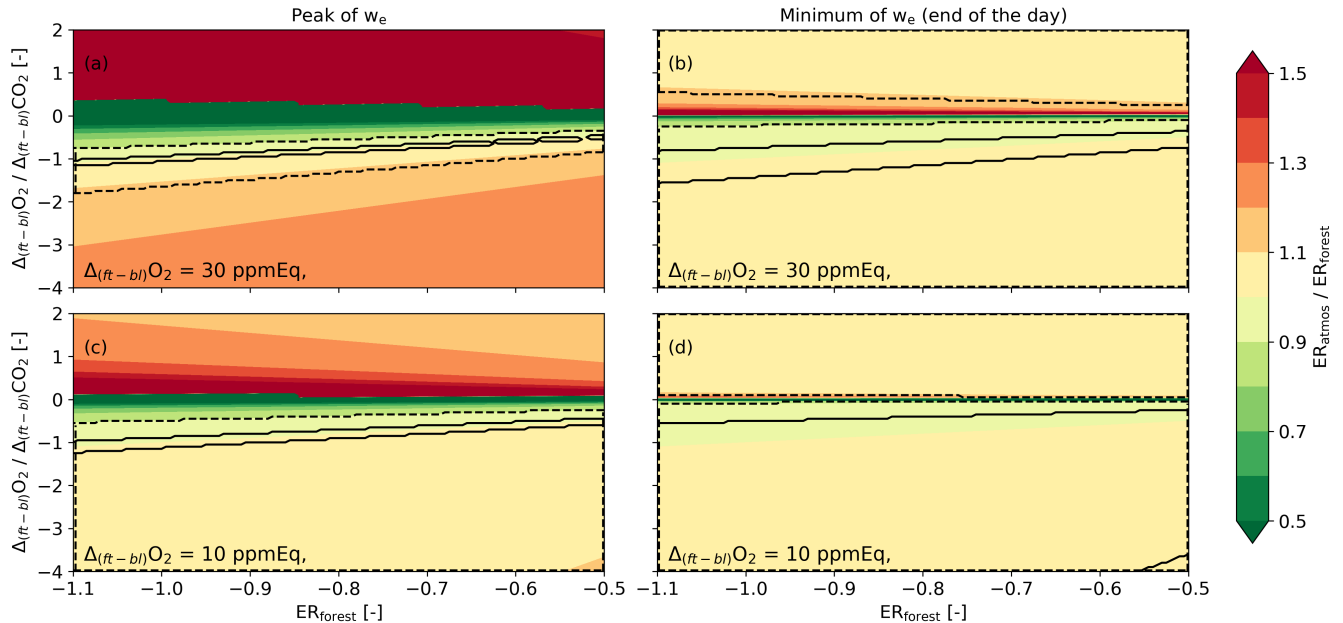
Figure A1. Analysis of Equation 8 for the entrainment- and photosynthesis-driven regimes. The ratio between ER_{forest} and ER_{atmos} is evaluated based on changes in ER_{forest} and the ratio of the jumps of O_2 and CO_2 between the free troposphere and the boundary layer ($\Delta_{(ft-bl)}$) for 4 cases: with a high entrainment velocity ($w_e = 0.10$ m s^{-1}) (left panels) and a low entrainment velocity (($w_e = 0.01$ m s^{-1}) (right panels) and for situations with a high O_2 jump ($\Delta_{(ft-bl)}O_2 = 0.30$ ppmEq) (top panels) and a low O_2 jump ($\Delta_{(ft-bl)}O_2 = 0.10$ ppmEq) (bottom panels). The O_2 surface flux $F(O_2)_s$ is kept constant for all the panels, at 8.5 μmol m s^{-1}.

There are a few situations where the β values of O_2 and CO_2 are equal and these are indicated in Figure A1 as the area between the black solid lines (ER_{atmos} deviates <1% from ER_{forest}) and dashed lines (ER_{atmos} deviates <10% from ER_{forest}):

1. During the photosynthesis dominant regime. When the entrainment velocity (w_e) is close to zero, both β values become zero. This is likely at the end of the day (right panels in Figure 1).

2. When the β values for O_2 and CO_2 become equal which happens when $\Delta_{(ft-bl)}O_2/\Delta_{(ft-bl)}CO_2 = ER_{forest}$. A specific case is when the $\Delta_{(ft-bl)}O_2 = \Delta_{(ft-bl)}CO_2$. In that case, the ER_{forest} has to be 1.0 for the β values of O_2 and CO_2 to become equal. The β values of O_2 and CO_2 are become closer during the lower O_2 jump case (lower panels in Figure 1).

The last situation only occurs under very specific conditions when the ratio of the O_2 and CO_2 entrainment and surface fluxes are the same. This is visible in the left panels of Figure A1, where only a small part of the graph shows values of ER_{atmos} close to ER_{forest} (indicated by the area between solid lines). In contrast, during low entrainment velocities at the end of the afternoon, it is more likely that the ER_{atmos} values become close to ER_{forest}, and this is shown by the larger area in the right panels of Figure A1. Low entrainment velocities could also occur when the growth of the boundary layer is reduces due to subsidence. During this study we will not focus on this specific case.

There are also differences between ER_{atmos} and ER_{forest} that arise from variations in the β values. Figure A1 demonstrates that substantial differences between ER_{atmos} and ER_{forest} originate due to differences in the entrainment fluxes for both species. When $\Delta_{(ft-bl)}O_2$ exceeds $\Delta_{(ft-bl)}CO_2$, this implies a dominant entrainment flux of O_2 over CO_2 and β_{O_2} deviates further from β_{CO_2} (Equation 8). This effect is almost absent when the jumps themselves are lower, because the ER_{atmos} / ER_{forest} ratio stays around 1 (Figure A1c). Moreover, when $\Delta_{(ft-bl)}CO_2$ transitions from negative to positive, the sign of β_{CO_2} also changes, subsequently elevating the ER_{atmos} values (Equation 8).

ER_{atmos} can also become smaller than ER_{forest} when $\Delta_{(ft-bl)}CO_2$ is larger than $\Delta_{(ft-bl)}O_2$ (Figure A1). This difference results in a large value for β_{CO_2} compared to β_{O_2}, causing the ER_{forest} value to be multiplied by a factor less than 1 and leading to a lower ER_{atmos} value than ER_{forest} (equation 8). By assessing ER_{atmos} and ER_{forest} values, we can see whether $\Delta_{(ft-bl)}O_2$ exceeds $\Delta_{(ft-bl)}CO_2$ ($ER_{atmos} > ER_{forest}$) or vice versa ($ER_{atmos} < ER_{forest}$).

This illustrative analysis, based on prescribed values in Equation 8 and Figure A1, provides an initial estimate of the variability in ER_{atmos}. However, it lacks insights into the diurnal behavior of the individual components of equation 8 and their potential combinations.

A2 Implementation of O_2 in CLASS

The following equation shows the implementation of the tendency (change over time) of O_2 into CLASS:

$$\frac{dO_2}{dt} = \frac{F_{O_2(s)} - F_{O_2(e)}}{h} + adv_{O_2} \tag{A1}$$

where $F_{O_2(s)}$ is the net surface O_2 flux at the canopy, $F_{O_2(e)}$ is the O_2 entrainment flux, h is the boundary layer height and adv_{O_2} is the advection term. The surface flux is calculated with equation 10 and the entrainment flux is based on the following equation (see also equation 2):

$$F_{O_2(e)} = -w_e \cdot \Delta_{(ft-bl)}O_2 \tag{A2}$$

where w_e is the entrainment velocity and $\Delta_{(ft-bl)}O_2$ is the jump of O_2. The jump of O_2 was determined the same way as for CO_2, by tuning the jump until the decrease/increase in CO_2/O_2 matched during the entrainment dominant period.

A3 Sensitivity analyses

A3.1 Table with initialisation for the first two sensitivity analyses

Table A1. The initial conditions used for the three sensitivity analyses, compared to the initial conditions for the 2019 base case. The subscript (0) indicates the first time step.

Variable	2019 base	background air		climate	
		lower $\Delta_{(ft-bl)}$ ratio	lower intial $\Delta_{(ft-bl)}$	high SMI	low SMI
$\Delta_{(ft-bl)}O_{2(0)}$ [ppmEq]	30	30	10	2019 case	2019 case
$\Delta_{(ft-bl)}CO_{2(0)}$ [ppm]	-8	-20	-5	2019 case	2019 case
θ_0 [K]	285.2	2019 case	2019 case	290	290
Soil moisture [m^3 m^{-3}]	0.18	2019 case	2019 case	0.22	0.14

A4 Validation of CLASS

Figures A3 and A2 present a comparison between the model output of CLASS and the corresponding measurements for the representative days of 2018 and 2019, assessing various parameters. Both figures demonstrate that the model compares well to the observed data. CLASS accurately follows the observed temperature increase (Figure A2a). A constant difference of approximately 8K between 2018 and 2019 is seen for both model and observations. This persistent difference is attributed to a heat wave rather than a drought in Hyytiälä, as a drought would have intensified the divergence between the 2018 and 2019 simulations throughout the day. Moreover, CLASS adequately models specific humidity for both years, assuming an initial relative humidity of 80% for 2018 (Figure A2b). The sensible heat flux (Figure A2c) and latent heat (Figure A2d) exhibit minimal differences between the 2018 and 2019 simulations. The accurate representation of atmospheric properties in CLASS consequently results in a satisfactory comparison of the boundary layer height development for both years in comparison to the observed data from radiosondes (Figure A3a)

The various CO_2 fluxes simulated by CLASS exhibit a high level of agreement with the observational data for both 2018 and 2019 (Figure A3d and A3e). While there are subtle differences evident between the observations for the two years, CLASS adeptly captures these nuances. Consequently, the model provides an accurate representation of plant behavior under both normal and warmer conditions. The elevated temperatures (+8K) and slightly reduced soil moisture (-0.03 m^3 m^{-3}) contribute to a slightly higher GPP and TER flux. Our study reaffirms that the vegetation in Hyytiälä did not undergo any stress during the 2018 European drought, which would have resulted in a lower GPP and lower latent heat flux (Lindroth et al., 2020).

For the 2018 case, we only altered a few initial conditions (see Table C2). However, both the decrease in CO_2 and the increase in O_2 during the day exhibit close similarity between the model and the observations. This outcome underscores that
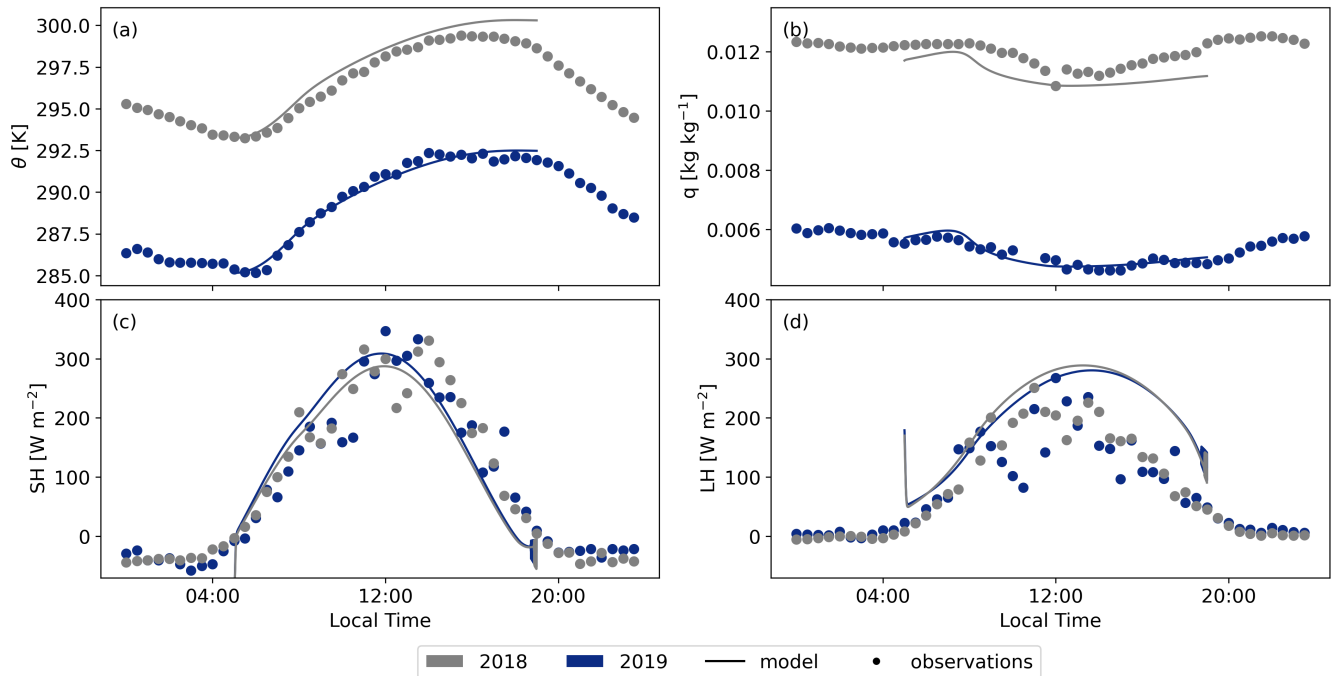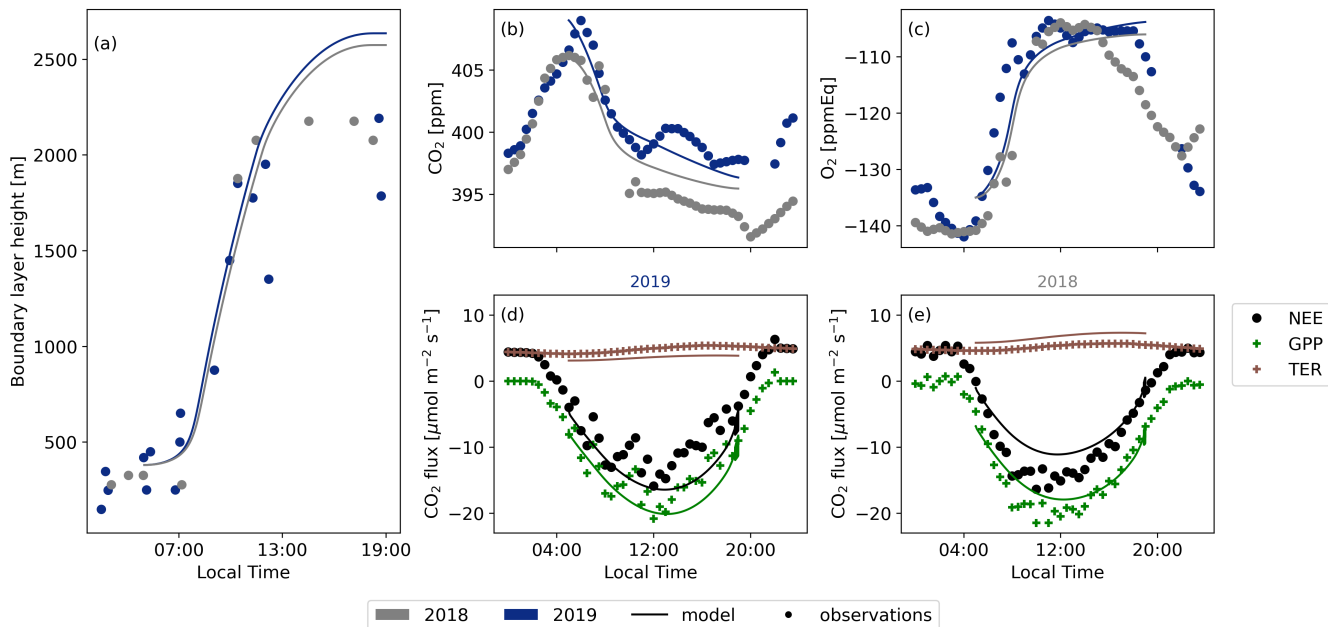
Figure A2. Comparison between the 2019 and 2018 case modelled with CLASS with the observational data for the potential temperature (θ) (a), specific humidity (q) (b), Sensible heat flux (SH) (c), Latent heat flux (LH) (d).

even with minimal changes in the initial conditions for the 2018 case and keeping the other variables constant (e.g., the jumps), we can successfully replicate a realistic new day based on the base case.

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It is important to note that only the Net Ecosystem Exchange (NEE) data are obtained directly from Eddy Covariance measurements. The Gross Primary Production (GPP) is inferred from a light and temperature based function and the total ecosystem respiration is calculated as the residual between NEE and GPP (Kulmala et al., 2019; Kohonen et al., 2022). This distinction may explain the challenge in aligning the TER flux of the observations with the model, as the model exhibits notable

730 discrepancies from the observations for both the 2018 and 2019 cases. The model's simulated respiration increase based on temperature appears more extreme compared to the observations. However, several studies (Lindroth et al., 2008; Gao et al., 2017; Heiskanen et al., 2023) indicate that the model's increase in TER between 2018 and 2019 is slightly too high, while the change based on observations is too low. As a result, it is plausible that the true respiration flux lies somewhere between the model output and the observational data.

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Figure A3. Comparison between the 2019 and 2018 case modelled with CLASS with the observational data for the boundary layer height (a), CO_2 (b), O_2 (c), the 2019 CO_2 surface fluxes (d) and the 2018 CO_2 surface fluxes (e).

Appendix B: Figures

Appendix C: Tables

Table C1: Initialisation of the CLASS model for the base case of 2019, based on 10-07-2019. The initialisation is based on the SMEAR II data (Hari et al., 2013), our OXHYYGEN campaign data (radiosondes or O_2 and CO_2 measurements) (Faassen et al., 2023) and studies that show ranges for parameters for the plants and soil (Lindroth et al., 2008; ECMWF IV, 2014; Vilà-Guerau de Arellano et al., 2015) .

Parameter [Source]	Description	Initial value
Lat	Latitude [deg]	61.51
Lon	Longitude [deg]	24.17
DOY	Day of year [-]	191
t_0	Starting time [UTC]	3
h_1	Initial boundary layer height [m]	380
h_2	Height of the residual layer [m]	2016

Continues next page

P	Surface pressure [hPa]	988.72

Temperature:

θ_0	Initial potential temperature [K]	285.15
$\Delta\theta_0$	Initial potential temperature jump [K]	2.4
$\lambda\theta_1$	Potential temperature lapse rate of residual layer [K m^{-1}]	0.0023
$\lambda\theta_2$	Potential temperature lapse rate of free troposphere [K m^{-1}]	0.0057

Specific humidity:

q_0	Initial specific humidity [kg kg^{-1}]	5.7 x 10^{-3}
Δq_0	Initial specific humidity jump [kg kg^{-1}]	-1.2 x 10^{-3}
λq_1	Specific humidity lapse rate of residual layer [kg kg^{-1} m^{-1}]	-8.3 x 10^{-7}
λq_2	Specific humidity lapse rate of free troposphere [kg kg^{-1} m^{-1}]	-2.3 x 10^{-6}

Carbon:

$CO_{2,0}$	Initial CO_2 mole fraction [ppm]	409
$\Delta CO_{2,0}$	Initial CO_2 jump [ppm]	-8
λCO_2	CO_2 lapse rate of free troposphere [ppm m^{-1}]	0

Oxygen:

$O_{2,0}$	Initial O_2 [ppm]	-135
$\Delta O_{2,0}$	Initial O_2 jump [ppm]	30
λO_2	O_2 lapse rate of free troposphere [ppm m^{-1}]	0

Vegetation:

LAI	Leaf Area Index [-]	3.3
C_{veg}	Vegetation cover [-]	0.9
$r_{c,min}$	Minimum resistance transpiration [s m^{-1}]	500
$r_{s,soil,min}$	Minimum resistance soil evaporation [s m^{-1}]	250
g_D	VPD correction factor for surface resistance [-]	0.03
$z_{0,m}$	Roughness length for momentum [m]	2.0
$z_{0,h}$	Roughness length for heat and moisture [m]	2.0
α	albedo [-]	0.10
R_{10}	Respiration at 10 degrees [mg CO_2 m^{-2} s^{-1}]	0.148
g_m	Mesophyl conducatance [mm s^{-1}]	2
T_{2gm}	reference temperature to calculate gm [K]	305
C_β	Curvature of response curve to drought [-]	0.15

Soil:

T_s	Initial surface temperature [K]	287.7
$T_{soil,1}$	Initial top soil temperature [K]	284.2
$T_{soil,2}$	Initial deeper soil temperature [K]	282.0
w_{sat}	Saturated volumetric water content [$m^3\ m^{-3}$]	0.5
w_{fc}	Volumetric water content field capacity [$m^3\ m^{-3}$]	0.30
w_{wilt}	Volumetric water content wilting point [$m^3\ m^{-3}$]	0.08
w_g	Volumetric water content of top soil layer [$m^3\ m^{-3}$]	0.18
w_2	Volumetric water content of deeper soil layer [$m^3\ m^{-3}$]	0.12
a	Clapp and Hornberger retention curve parameter [-]	0.387
b	Clapp and Hornberger retention curve parameter [-]	4.05
p	Clapp and Hornberger retention curve parameter [-]	4
CG_{sat}	Saturated soil conductivity for heat [$K\ m^{-2}\ J^{-1}$]	3.22 x 10^{-6}
$C1_{sat}$	Coefficient force term moisture [-]	0.082
$C2_{ref}$	Coefficient restore term moisture [-]	3.9
Λ	Thermal diffusivity skin layer [-]	5

Table C2. Adjustments for the 2018 case (warm case) compared to the 2019 values shown in in table C1. Only the initial potential temperature (θ_0), initial soil moisture (w_g) and CO_2 mole fraction ($CO_{2,0}$) are adjusted based on the aggregate of 28-07-2018 and 29-07-2018. It was assumed that the initial relative humidity stayed constant at 80% with increasing temperatures, therefore the initial specific humidity was also adjusted.

Parameter	Description	Initial value
θ_0	Initial potential temperature [K]	293.3
$T_{soil,1}$	Initial top soil temperature [K]	θ_0 - 2
$T_{soil,2}$	Initial deeper soil temperature [K]	θ_0 - 3
q_0	Initial specific humidity [$kg\ kg^{-1}$]	$f(\theta_0)$
w_g	Volumetric water content of top soil layer [$m^3\ m^{-3}$]	w_2 - 0.04
w_2	Volumetric water content of deeper soil layer [$m^3\ m^{-3}$]	0.15
$CO_{2,0}$	Initial CO_2 mole fraction [ppm]	406
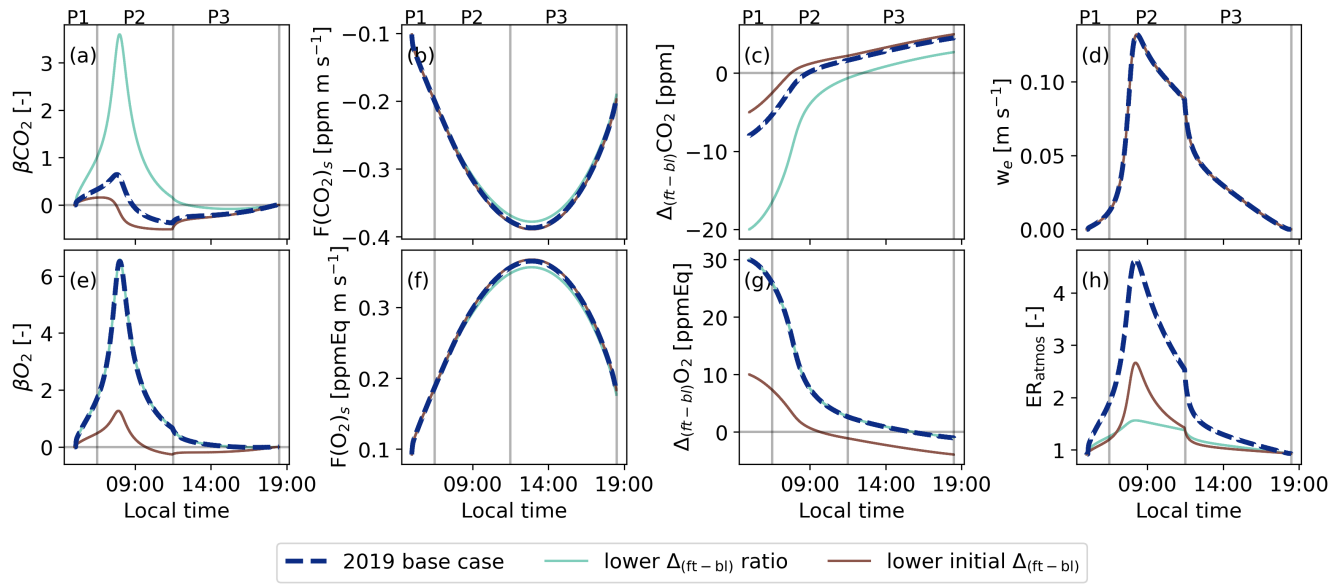
Figure B1. Similar to Figure 5 but now for the base case (2019) and the background sensitivity studies with a lower jump ratio between O_2 and CO_2 (lower $\Delta_{(ft-bl)}$) and with a lower initial jump for CO_2 (lower initial $\Delta_{(ft-bl)}$). The diurnal variability of the exchange ratio of the atmosphere is now added (ER_{atmos}: (h))
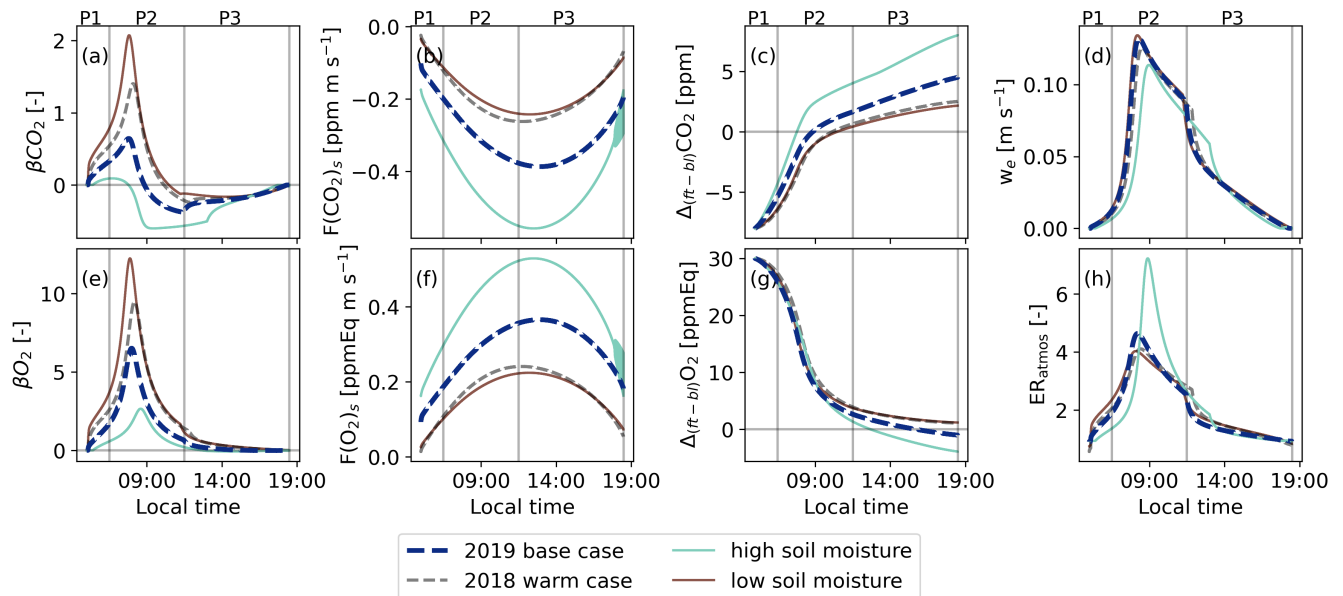
Figure B2. Similar to Figure 5 but now for the base case (2019) and the dry and warm sensitivity studies with a high soil moisture and a low soil moisture, both with higher air temperatures compared to the 2019 base case. The diurnal variability of the exchange ratio of the atmosphere is now added (ER_{atmos}: (h))

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