

1 Identification of ice-over-water multilayer clouds using multispectral 2 satellite data in an artificial neural network

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7 **Abstract.** An artificial neural network (ANN) algorithm, employing several Aqua MODerate-resolution Imaging
8 Spectroradiometer (MODIS) channels, the retrieved cloud phase and total cloud visible optical depth, and temperature and
9 humidity vertical profiles is trained to detect multilayer (ML) ice-over-water cloud systems identified by matched 2008
10 CloudSat and CALIPSO (CC) data. The trained MLANN was applied to 2009 MODIS data resulting in combined ML and
11 single layer detection accuracies of 87% (89%) and 86% (89%) for snow-free (snow-covered) regions during the day and
12 night, respectively. Overall, it detects 55% and ~30% of the CC ML clouds over snow-free and snow-covered surfaces,
13 respectively, and has a relatively low false alarm rate. The net gain in accuracy, which is the difference between the true and
14 false ML fractions, is 7.5% and ~2.0% over snow-free and snow/ice-covered surfaces. Overall, the MLANN is more accurate
15 than most currently available methods. When corrected for the viewing-zenith-angle dependence of each parameter, the ML
16 fraction detected is relatively invariant across the swath. Compared to the CC ML variability, the MLANN is robust seasonally
17 and interannually, and produces similar distribution patterns over the globe, except in the polar regions. Additional research is
18 needed to conclusively evaluate the VZA dependence and further improve the MLANN accuracy. This approach should
19 greatly improve the monitoring of cloud vertical structure using operational passive sensors.

20 1 Introduction

21 Passive remote sensing with polar-orbiting and geostationary passive imagers is currently the only approach suitable for nearly
22 continuous monitoring of clouds day and night around the globe. While cloud remote sensing is well established and the
23 methodologies are abundant (e.g., Stubenrauch et al., 2013), detecting and characterizing multilayered clouds remains a
24 continuing challenge. Typically, algorithms employed to retrieve properties, such as cloud optical depth or phase, treat the
25 radiances for a given cloudy imager pixel as emanating from a single plane-parallel cloud sheet. Rarely, if ever, will an actual
26 cloud entirely satisfy the plane-parallel assumptions. Instead, the sizes and densities of the hydrometeors vary vertically and
27 horizontally within the atmospheric column corresponding to a cloudy imager pixel. The top and side surfaces of clouds, even
28 stratus, typically have bumps and troughs that deviate to various degrees from the uniformity implicit in the plane-parallel

29 model (e.g., Loeb and Coakley, 1998). Simply having vertical extent can cancel the plane-parallel assumption when viewing
30 parts of a cloud side (e.g., Liou and Ou, 1979). Multilayered clouds also violate the model.

31 Accounting for variations in single-layer-cloud morphology with a non-plane-parallel type of model is too complex for
32 use in operational retrieval algorithms and likely requires information that is currently unavailable in most imager radiance
33 datasets. Moreover, radiative transfer calculations used in weather and climate models are based on the same plane-parallel
34 premise, although methods are being developed to account for some 3D structure (e.g., Schäfer et al., 2016). For single-layer
35 (SL) clouds, the nonuniform geometry is the predominant deviation from the plane-parallel ideal. It mostly affects retrievals
36 of cloud optical depth (COD) and particle effective radius (CER), but, less so, cloud-top phase and height (CTH). The presence
37 of two water phases and separation of the upper and lower layers in ice-over-water multilayer (ML) systems can also produce
38 large errors in COD and CER, and significantly diminish the accuracies of thermodynamic phase and cloud-top height (CTH)
39 retrievals (e.g., Minnis et al., 2007; Yost et al., 2023). Reducing uncertainties in the retrievals due to nonconformance with the
40 SL plane-parallel ideal, particularly for ML clouds, is critical to increasing the value of imager cloud retrievals for a variety of
41 applications.

42 Reliable determination of cloud characteristics is critical to the Clouds and the Earth's Radiant Energy System (CERES,
43 Loeb et al., 2016) for converting broadband radiance measurements to reliable shortwave and longwave fluxes at the top of
44 the atmosphere, within the atmosphere, and at the surface. Cloud properties extracted from satellite imagery are also exploited
45 in a wide variety of applications. These include, among others, verifying climate model cloud parameters (e.g., Zhang et al.,
46 2010; Stanfield et al., 2014), enhancing aviation safety (Mecikalski et al., 2007; Smith et al., 2012), improving short-term
47 weather forecasts (e.g., Kurzock et al., 2019; Benjamin et al., 2021), and estimating surface radiative fluxes (e.g., Rutan et al.,
48 2015; Ryu et al., 2018). All of these applications and others (e.g., Chen and Zhang, 2000; Morcrette and Christian, 2000) will
49 benefit from more accurate cloud properties, especially for ML systems.

50 Active instruments such as the Cloud-Aerosol Lidar with Orthogonal Polarization (CALIOP) lidar on the Cloud-Aerosol
51 Lidar and Infrared Pathfinder Satellite Observations (CALIPSO) satellite (Winker et al., 2009) and the Cloud Penetrating
52 Radar (CPR) on CloudSat (Stephens et al., 2008) together have produced the most detailed depictions of cloud vertical structure
53 on a global scale. These satellites are part of the A-Train, the Afternoon Constellation of sun-synchronous orbiters that, for
54 years, flew nearly the same tracks (13:30 Equatorial crossing time) separated by only a few minutes. Other satellites with
55 imagers, particularly Aqua with the MODerate-resolution Imaging Spectroradiometer (MODIS), are also members of the A-
56 Train. The CALIOP and the CPR are both near-nadir viewing instruments that generate profiles of atmospheric particles only
57 in a narrow curtain along the satellite track. Those profiles, which often include overlapping clouds, are valuable for many
58 uses, especially when combined with other instruments on the A-Train. Because they sample only a tiny fraction of the globe
59 at two local times each day, the current active instruments have limited utility for many of the applications served by
60 operational satellite imager products.

61 Efforts to accurately identify and unscramble ML clouds from passive imagery have yielded a variety of methods that
62 have either been demonstrated as efficacious or are being applied routinely. They are based on interpreting radiances from
63 either multiple instruments or from a single instrument with multiple channels. To identify ML clouds, Lin et al. (1998)
64 matched microwave radiometer (MWR) retrievals of cloud liquid water path (LWP) from polar-orbiting satellites with
65 retrievals of COD from geostationary satellites. Minnis et al. (2007) used MWR retrievals of LWP matched with imager
66 retrievals of COD and CER to detect and retrieve ML cloud properties over water surfaces. By combining Aqua MODIS CTP
67 and COD with the optical centroid cloud pressure retrieved from the Ozone Monitoring Instrument on the Aura satellite, *Joiner*
68 *et al.* [2010] discriminated between vertically extended and ML clouds.

69 The single-instrument approach, which is more viable for monitoring ML clouds from a greater number of satellites, often
70 relies on discrepancies between the visible (VIS, $\sim 0.65 \mu\text{m}$) channel COD and that determined from other channels. For
71 example, COD derived from infrared radiances is limited to values of less than ~ 5 because the usable signal diminishes for
72 thicker clouds. Thus, the two COD retrievals can be used to detect thin cirrus over a thicker lower cloud. Pavolonis and
73 Heidinger (2004) identified ML clouds by comparing the COD retrieved from the brightness temperature differences from the
74 11 and 12- μm channels, BTD₁₁₁₂, with the VIS COD. They suggested that the MODIS 1.38- μm and 1.63- μm reflectances
75 could be combined with BTD₁₁₁₂ to retrieve the cirrus optical depths for comparison with the VIS COD. The MODIS CO₂
76 channels were used by *Chang and Li* [2005] to retrieve IR COD for ML cloud detection. Their method was simplified by
77 *Chang et al.* [2010] to employ brightness temperatures from CO₂ and 11- μm channels to identify high clouds and ultimately
78 to detect ML clouds in the CERES MODIS Edition 4 products (CM4; Minnis et al., 2021). Similarly, *Wind et al.* [2010]
79 contrasted the cloud top pressure (CTP) derived with a CO₂ method to that based on absorption in the MODIS 0.94- μm channel
80 along with other tests to identify ML clouds in MODIS pixels. To further improve ML detection, this technique was enhanced
81 with additional tests, including the Pavolonis and Heidinger (2002) method (Platnick et al., 2017; Marchant et al., 2020).

82 Desmons et al. (2017) exploited multi-angle polarized spectral reflectances and two different retrievals of CTP from the
83 Polarization and Directionality of the Earth's Reflectance (POLDER) instrument on another A-Train satellite. Instead of using
84 COD retrievals, Wang et al. (2019) utilized a series of tests applied to three spectral reflectances and two infrared brightness
85 temperatures measured by the Visible Infrared Imaging Radiometer Suite (VIIRS) to classify clouds as single-layer ice or
86 water, multilayer, probable multilayer, or uncertain phase and layering. Their technique yielded results similar to those from
87 Platnick et al. (2017). For detecting ML clouds in VIIRS data, CERES replaced the CO₂ channel with the 12- μm channel in
88 the Chang et al. (2010) approach. It found fewer ML clouds than the method using the CO₂ channel (Minnis et al. 2023).

89 These physically based approaches to ML detection are limited in many respects by a priori knowledge and ambiguous
90 spectral signals in the imager radiance complement, problems that affect many cloud remote sensing approaches. To minimize
91 these limitations, artificial neural networks (ANNs) are increasingly employed to characterize clouds from passive imager
92 data. By training with a select set of relevant input parameters and a known output value, the ANN has the potential to better
93 interpret several subtle, but often ambiguous radiative signals that are difficult to reconcile in physically based retrievals. Kox

94 et al. (2014) and Strandgren et al. (2017) employed an ANN to determine cirrus COD and CTH, while Cerdena et al. (2007)
95 used it to estimate liquid water cloud COD and CER and Taravat et al. (2015) detected the presence of clouds with it. Using
96 an ANN, Minnis et al. (2016) retrieved thick ice cloud COD at night and Håkansson et al. (2018) more accurately determined
97 CTP and CTH than available physical methods. Stengel et al. (2020), Wang et al. (2020), and White et al. (2021) use ANNs
98 for cloud detection and phase discrimination. Machine learning techniques were employed by Haynes et al. (2022) to detect
99 low clouds in both single- and multilayered conditions for geostationary satellites. Tan et al. (2022) found that a random-forest
100 technique was highly accurate in detecting multilayered clouds from geostationary satellite imager data. These and other
101 examples have clearly demonstrated that ANNs have significant potential for advancing the characterization of global
102 cloudiness from passive imager radiances.

103 To improve the CERES ML detection, Sun-Mack et al. (2017) began developing a multi-layer cloud detection ANN
104 (MLANN) to distinguish between SL and ML clouds using MODIS radiance data matched to CALIPSO and CloudSat vertical
105 profiles of clouds. Minnis et al. (2019) further enhanced the MLANN by including more input parameters and additional
106 output variables such as upper layer CTH, COD, and cloud-base height (CBH). They also used only high-confidence CloudSat
107 and CALIPSO data for training. They found that, for nonpolar clouds, the MLANN correctly identified ML and SL clouds
108 together 80.4% and 77.1% of the time during day and night, respectively, using CALIPSO data averaged over an 80-km
109 distance. While those results are quite encouraging, the approach needs further refinement and complete seasonal and global
110 coverage.

111 This paper reports on continued development of the MLANN to detect ML clouds. Revisions to the previous training are
112 made using newer versions of CALIPSO and CloudSat products with constrained horizontal resolution. In addition to the
113 separate day/night training used in previous versions, the MLANN herein is trained separately for CERES ice and water cloud
114 pixels separately for snow-free and snow/ice-covered surfaces using an entire year of data. Input to the MLANN is also
115 enhanced with some new variables. Finally, because the MLANN is trained with near-nadir data, its utility for full swath
116 MODIS data is examined.

118 2 Data

119 The MLANN is trained with input taken from Aqua MODIS imager data and cloud products, and numerical weather model
120 reanalyses. Different datasets are used for daytime and nighttime. Daytime corresponds to all measurements taken when the
121 solar zenith angle, $SZA < 82^\circ$. Active sensor data serve as the output.

123 2.1 C3M and MODIS

124 MODIS on Aqua, the CALIOP, and the CPR, took measurements continuously within ± 3 min of each other over a given
125 location until 2011, when CloudSat suffered battery problems and thereafter only collected data during the day. CloudSat
126 exited the A-Train during February 2018. The CALIOP and the CPR were aligned to view nearly the same area along their
127
128

129 respective orbits. Because their flight tracks are typically close to the Aqua nadir path, MODIS scans the same scene at viewing
130 zenith angles, $VZA < 18^\circ$. Vertical profiles of clouds from the CALIPSO Version 4 (Vaughan et al., 2016) and the CloudSat
131 2B-CLDCLASS_R05 (Sassen and Wang, 2008), 2B-CWC-RO (Austin et al. 2009), and 2C-ICE (Deng et al., 2015) datasets
132 were collocated with 1-km Aqua MODIS Collection 6.1 radiances and CERES-retrieved cloud properties to produce an
133 updated version of the CloudSat, CALIPSO, CERES, and MODIS (C3M) product (Kato et al., 2010). The C3M also includes
134 CERES MODIS cloud properties, such as cloud-top phase, cloud particle effective radius (R_{CM}), and COD (τ_{CM}), which were
135 retrieved from the MODIS radiances using an interim CERES Edition 5 algorithm, CM4+. Those retrievals assumed that all
136 of the clouds were single-layered.

137 The CM4+ methodology is the same as the that of the CM4 algorithms except for two changes. In CM4+, τ_{CM} is retrieved
138 over snow and ice surfaces using a combination of 1.61- μm and 1.24- μm reflectances, as suggested by Minnis et al. (2021).
139 The former channel is used for thinner clouds ($COD < 8$ for ice clouds, $COD < 32$ for water clouds) and the latter for thicker
140 clouds. The Aqua MODIS 1.6- μm channel consists of 10 sensors. Of those ten, only six operate properly. To obtain full 1.6-
141 μm imagery, the 1.6- μm reflectance for each bad pixel was replaced with that from the nearest good detector. That method
142 was applied to the 101-pixel-wide MODIS swath of the C3M. The other change for CM4+ is the use of the two-habit ice
143 crystal model of Loeb et al. (2018) for retrieving ice cloud properties.

144 A separate dataset is the full-swath Aqua CM4+ cloud product and the Aqua MODIS Collection 6.1 radiances, which are
145 sampled every other scan line and every fourth pixel. Note that the 1.6- μm channel is only available from 3 of the five sensors
146 on the CERES sampled Aqua MODIS Collection 6.1 data. The corrections applied to faulty 1.6- μm sensors for C3M have not
147 yet been implemented for CERES Aqua MODIS data prior to 2019. Therefore, the sampling is reduced and all data from the
148 faulty sensors are excluded in the full-swath 2009 and 2013 data.

149 To produce a complete vertical profile of cloud-filled layers in a given pixel, the C3M converts the CloudSat CLDCLASS
150 high-confidence cloud profiles from 240-m to 60-m vertical resolution, then merges them with the CALIPSO cloud profile
151 and vertical feature mask. The nominal horizontal footprint of a CALIOP shot at the Earth's surface is 330 m in diameter. To
152 detect fainter clouds, the CALIPSO processing system computes horizontal averages (HA) of the lidar signals from multiple
153 shots corresponding to increasing distances along the track: 1, 5, 20, and 80 km. The last three HA values are for altitudes
154 above 8 km. This analysis uses only those clouds detected at $HA \leq 5$ km to define the cloud profiles, because nearly all of the
155 clouds identified solely at lower resolutions had $COD < 0.1$. Since the CM4 detection rate drops significantly for those
156 extremely small optical depths (Trepte et al., 2019), few of those cirrus clouds are discernible and are less likely to be identified
157 in ML conditions. Additionally, in the previous formulation (Minnis et al., 2019), all three CALIPSO 0.33-km pixels matched
158 to a given MODIS pixel were required to be cloudy after the horizontal averaging was performed. Here, only two out of three
159 0.33-km pixels are required to be cloudy and any cloud having $\tau_{CM} < 0.5$ is assumed to be single-layered. The latter constraint
160 assumes that the ML signal from such optically thin clouds is negligible, and any retrieval attempt will yield upper and lower
161 cloud-layer properties that are, at most, highly uncertain. To perform additional analyses, the CC COD (τ_{CC}) was computed

162 for each ice-layer pixel identified as ML in the CALIPSO-CloudSat profiles. The value of τ_{CC} is equal to the CALIPSO ice
163 COD, when the CALIOP signal shows a return from the lower layer cloud, otherwise it is equal to the combined CALIPSO-
164 CloudSat COD. To cover all seasons for snow-free surfaces and facilitate computer processing for training, the C3M data were
165 sampled every fourth pixel of 2008 for snow/ice-free (SF) areas, while all pixels were used for the snow/ice-covered (SC)
166 scenes. This full-year training set is more comprehensive than the 1-month dataset of Minnis et al. (2019). The complete,
167 upsampled 2009 C3M data were employed as an independent dataset for validating the MLANN.

168 The C3M data were merged with the relevant surface skin temperature and vertical profiles of relative humidity taken
169 from the CERES Meteorology, Ozone, and Aerosol (MOA) product (Gupta et al., 1997). The latest MOA product is the result
170 of regridding and interpolating spatially and temporally the version 5.4 reanalysis produced by the Global Modeling
171 Assimilation Office Global Earth Observing System (GEOS-5.4), an update of the versions described by Rienecker et al.
172 (2008). These are the same data employed in the CM4+ retrievals.

173

174 2.2 Input variables

175 The MODIS input variables are listed in Table 1. Both daytime and nighttime MLANN input include latitude, longitude,
176 surface type (land or water), surface elevation, brightness temperatures T_λ and brightness temperature differences, $BTD_{\lambda_1\lambda_2} =$
177 $T_{\lambda_1} - T_{\lambda_2}$, where λ is the wavelength in μm abbreviated to the first two digits. Here, brightness temperatures at 3.7, 6.7, 8.5,
178 11, 12, and 13.3 μm are used together with BTD_{3711} , BTD_{6711} , BTD_{8511} , BTD_{1112} , and BTD_{1113} . The parameters involving the
179 13.3- μm channel were not used over snow-covered surfaces because of striping in the 13.3- μm images over Greenland and
180 Antarctica. Also included are τ_{CM} and the GEOS-5.4 input data. During the day, τ_{CM} is retrieved using solar reflectances and
181 corresponds to the total cloud optical depth. At night, it is estimated from three infrared channels and typically represents the
182 uppermost cloud COD (e.g., Minnis et al., 2021). Nocturnal values exceeding ~ 5 are often not very accurate, but serve to
183 indicate that the cloud is not optically thin. The GEOS input data comprise the surface skin temperature and the relative
184 humidities at the surface and at 850, 700, 500, 400, 300, 200, and 100 hPa. Relative humidity can indicate the presence of a
185 cloud at a given altitude depending on the quality of the source (e.g., Minnis et al., 2005).

186 During the day, the additional input data consist of the SZA, the 1.38- μm reflectance ($\rho_{1.38}$), the reflectance difference
187 between 1.6 and 2.1 μm , $\rho_{1.38} - \rho_{1.38}$. CM4+ retrievals of R_{CM} are also employed for the MLANN formulation. The reflectances
188 and R_{CM} were not used by Minnis et al. (2019).

189

190 2.3 Output: Single or multilayered

191 According to Kato et al. (2010), approximately 51% of cloud systems identified by the CPR and CALIOP consist of two or
192 more layers separated by at least 200 m. Of that 51%, atmospheric columns having 2, 3, 4, 5, and 6+ layers account for 57, 28,

193 10, 4, and 1% of the pixels, respectively. Those statistics include liquid-over-liquid, ice-over-ice, water-over-ice as well as ice-
194 over-water cloud overlap. Unscrambling this variety of layering is a daunting task.

195 To simplify ML detection and later retrievals, only those clouds having the greatest differences in properties are assumed
196 to be multilayered. Thus, only systems having ice-over-liquid clouds are considered because they differ in phase, scattering
197 properties, and altitude, and are more common than liquid-over-ice clouds. Thus, multilayered clouds are defined here as any
198 combination of ice-cloud layers above one or more water cloud layers with the constraint that the top of the uppermost water
199 layer must be at least 1 km below the bottom of the lowest ice cloud layer. All ice cloud layers together are considered to
200 constitute a single cloud layer. Similarly, all liquid layers are considered together as a single layer.

201 Selection of 1 km as the minimum separation distance is based on the need to ensure complete separation between the ice
202 and water layers and to maximize the number of detected ML clouds. Using a smaller separation would likely diminish
203 detection accuracy significantly, as demonstrated by Tan et al. (2022). Sun-Mack et al. (2017) and Minnis et al. (2019) found
204 that a larger separation distance can result in greater accuracy but at the expense of missing a significant number of actual ML
205 clouds.

206 An ice-cloud layer is assumed to be present in the profile, if

207 (1) the CALIPSO VFM cloud phase is either ice clouds or mixed phase clouds, or

208 (2) at least, one layer with extinction occurs at a height above the altitude corresponding to 253 K and no temperature
209 inversion exists in the atmospheric layer between the altitudes corresponding to 273 K and 253 K. This constraint is used
210 to eliminate the possibility of warm clouds occurring above the assumed ice threshold of 253 K.
211

212 For training, all C3M pixels having an ice-cloud layer over a water cloud layer are assigned an output value of 1, while all
213 other cloudy pixels are assumed to be single-layered and are assigned a value of zero.

214 215 3.0 Methodology

216 The MLANN is trained using the MathWorks Patternnet software ([https://www.mathworks.com/help/deeplearning/gs/pattern-
217 recognition-with-a-shallow-neural-network.html](https://www.mathworks.com/help/deeplearning/gs/pattern-recognition-with-a-shallow-neural-network.html)). The scaled conjugate gradient training function was employed here because
218 it seemed best suited to handling very large training datasets with many iterations. This is a switch from the Levenberg-
219 Marquardt method used in the previous version of MLANN. Only one hidden layer is used for this shallow neural network. It
220 was found that a second layer yielded no significant increase in accuracy, but greatly increased training time. Each layer
221 employed the logarithmic sigmoid and hyperbolic tangent sigmoid functions [logsig, transig] as the activation type. In the
222 hidden layer, the number of neurons varies from 50 to 70 depending on the data category (e.g., snow-free daytime ice clouds).
223 The exact number was determined by adding neurons until gains in accuracy ended. An epoch of 2000 was used for ending
224 the fitting but it was not always reached. Mean squared error was used to measure performance. For final training, the sampled

225 2008 data for each category were divided into 60%, 20%, and 20% each for training, testing, and validation, respectively. All
226 other training parameters are determined by the Patternnet program.

227 To avoid local minima in the neural network, the training runs were repeated many times using different samplings of the
228 dataset (e.g., every 3rd pixel or every 5th pixel); different random initial weights; and various percentages for training, testing,
229 and validation. Local minima were identified when the training convergence time was abnormally short or long. Overfitting
230 was avoided by using a very large dataset (typically more than a million datapoints), which forces the net to generalize. It was
231 also avoided by using a minimal number of neurons. Additionally, unreasonable data, such as fill values, were filtered out to
232 minimize the noise. A set of range limits was used to eliminate any obviously errant data. Leaving such data in the input set
233 prevents the training from generalizing. Unnecessary input parameters were also removed by trial and error to streamline the
234 training. Finally, similar performances of the MLANN with the 2008 training and 2009 independent validation datasets ensured
235 that the trained network was producing global minima without overfitting.

236 The input variables in Table 1 were selected by adding in parameters suspected of enhancing ML detectability and
237 computing the accuracy for each addition. If no gain in accuracy occurred, the parameter was not used. Each predictive
238 parameter's influence on the final MLANN formulation was assessed by computing the relative decrease in recall (defined in
239 section 4.1) when a given parameter was removed from the training. The decrease for each parameter was divided by the sum
240 of all of the values to produce a relative ranking of importance. The ranks ranged from 0.038 for BT₁₁ to 0.082 for the relative
241 humidity profiles, which were treated as a single input for these purposes. The second highest ranked parameter is latitude,
242 followed in the daytime by SZA and $\rho_{1.38}$. In general, the brightness temperatures were ranked lower than the BTDs, similar
243 to the rankings reported by Tan et al. (2023) for their random forest method.

244 Output from the trained MLANN is a probability between 0 and 1 for each pixel. The latter value denotes certainty that
245 the pixel includes ML clouds as defined here. For practical purposes it is necessary to select a threshold probability above
246 which a pixel is designated as multilayered. A threshold value of 0.5 was chosen based on analysis of the accuracy of the
247 results for probabilities between 0.3 and 0.60. The accuracies (risks) were found to be greatest (least) for thresholds between
248 0.50 and 0.55.

249 **4 Results**

250 The results presented here consist of comparisons of the MLANN and corresponding CC parameters for the 2008 training
251 dataset along with data from 2009 to ensure robustness of the estimates. Weights and constants were determined by training
252 for each category and parameter and then applied to the independent datasets. The MLANN was trained using the C3M data
253 for the four categories in Fig. 1 to obtain four sets of weights and constants for each surface type.

254 4.1 Multi-layer cloud detection

255 Figure 2 plots the CC cloud profiles retrieved over six areas during 25 December, 2009. The CC layering classification uses
256 gray for SL and blue for ML. In addition to the cloud profiles, the MLANN selection of SL (gray) and ML (blue) is indicated
257 by the lines of dots across the top section of each panel. The surface elevation is denoted by the black dashed line in each
258 panel. On the left are daytime observations over the tropical Atlantic (Fig. 2a), eastern Europe (Fig. 2b), and eastern Antarctica
259 (Fig. 2c). Nocturnal profiles are given on the right for passes over the tropical Indian Ocean (Fig. 2d), the south Pacific (Fig.
260 2e), and northern Russia (Fig. 2f). In the tropical overpasses, the MLANN detects a large fraction of the ML clouds, but also
261 misses a noticeable number of ML pixels. For example, only a few of the intermittent ML clouds between 2.5°N and 6.1°N
262 are identified by the MLANN in Fig. 2a and a segment of continuous ML clouds near 12°S in Fig. 2d is missed by the MLANN.
263 Similar results are seen for the mid-latitude SF areas, where a few ML clouds are missed around 59°N in Fig. 2b and near 35°S
264 in Fig. 2e.

265 Some false ML clouds are also found in these panels. In Fig. 2b, for example, false ML clouds are evident at 51°N and
266 also in two areas between 56 and 58°N. In the latter case, there are ML clouds in the profile but they were not classified as
267 such by the CC constraints, possibly due to the 253 K liquid cloud temperature threshold. Thus, some of the false ML may
268 actually be ML clouds. The detection rates for the two SC profiles are much reduced. During the daytime case (Fig. 2c), only
269 one stretch of ML clouds is detected, while even fewer ML clouds are detected at night around 76°N (Fig. 2f). The unidentified
270 ML clouds are more common in both cases.

271 To summarize the results for all of the data, a confusion matrix was constructed for each category. Referring to Table 2,
272 agreements between the MLANN and CC SL and ML classifications are denoted as SS and true negative (SM), respectively,
273 while false SL and ML pixels are given by SM and MS, respectively. Each classification is defined as the number of pixels
274 satisfying the agreement condition divided by the total number of pixels. Those percentages are used to define the following
275 metrics.

276

$$277 \text{ Accuracy: } ACC = SS + MM. \quad (1)$$

$$278 \text{ Real Risk: } RR = MS + SM = 1 - ACC. \quad (2)$$

$$279 \text{ False ML rate: } FM = MS / (MS + MM). \quad (3)$$

$$280 \text{ Precision: } PR = MM / (MS + MM) \quad (4)$$

$$281 \text{ Recall: } RC = MM / (SM + MM). \quad (5)$$

$$282 \text{ Single-layer Confidence: } CoS = SS / (SS + SM). \quad (6)$$

$$283 \text{ F1 Score: } F1 = 2 * PR * RC / (PR + RC) \quad (7)$$

$$284 \text{ Net Gain of Accuracy: } NGA = MM - MS. \quad (8)$$

285

286 These parameters facilitate the reporting and discussion of the results and the comparisons with other algorithms.

287 The training results in Table 3 include the confusion matrices for all eight categories with ACC in bold along with the
288 number of CC SL and ML pixels and their sum. During the day, ACC is 84.1% for CM4 ice clouds over SF areas, with the
289 fraction of ML correctly identified, i.e., RC = 49%. The classification during the day is a bit better for CM4 liquid clouds:
290 ACC = 88.7% and RC = 63%. The real risk for ice clouds is 15.9% compared to 11.3% for the liquid clouds. At night the
291 results are similar, although a little worse for ice clouds, with ACC = 81.3%. However, the ice clouds yield a larger fraction,
292 RC = 55%, of true ML pixels than during the day. Fewer ML clouds are found for liquid clouds at night. More of the ML
293 clouds are classified as ice because the nocturnal cloud temperature retrieval is based strictly on infrared radiances (Yost et al.
294 2021, 2023). Nevertheless, ACC is the same for both times of day for liquid phase clouds. At night, RR for ice clouds increases
295 to 18.7% and drops slightly for water clouds. A total of ~12 million pixels was used in the SF training.

296 As suggested by Fig. 2, the efficacies of the MLANN for detecting ML clouds over snow-covered areas are considerably
297 reduced relative to their snow-free counterparts. While the ACC values are actually greater than those during the day (Table
298 3), recall drops to 35% and 45% for ice and liquid clouds, respectively, during the day. The fraction detected, RC~ 22%, is
299 even lower at night. Nevertheless, because fewer pixels qualify as ML clouds over SC surfaces, according to the definition
300 used here, the MLANN RR values are smaller than those over SF surfaces. It is notable that, for both SF and SC surfaces, the
301 ML false alarm rate is less than 55%.

302 4.2 Independent evaluation

303 The results from the training are encouraging, but they are not based on an independent dataset. To evaluate the robustness of
304 the MLANN, all 2009 Aqua MODIS data were processed with the trained algorithm. In general, the statistics for the eight
305 categories are all very similar to those in Table 3. To summarize the effectiveness of the MLANN, the 2009 ice and liquid ML
306 results for the SF/SC and day/night categories are combined in Table 4. Over SF surfaces, ACC is 87.0% and 85.6% for day
307 and night, respectively, while the corresponding values over SC surfaces are 89.3% and 88.7%. Despite the large ACC values,
308 the MLANN underestimates the ML fraction over SF surfaces by 5.8% and 4.8% during night and day, respectively, for the
309 matched CC and MODIS cloudy pixels. A total of 80 million SF pixels were processed, compared to 26 million for SC surfaces.
310 Over SF areas, RR is 13% for day and 15% at night. Real risks drop to 11% for SC regions. It should be noted that the ML
311 fractions reported here are for the number of multi-layer MODIS pixels divided by the total number of cloudy matched CC
312 and MODIS pixels. Since the CERES MODIS mean cloud fraction is ~0.66, the actual fraction of MODIS pixels that are
313 classified as ML would need be multiplied by 0.66.

314 The net gain of accuracy relative to the SL assumption is an important parameter to consider in any ML detection scheme.
315 Using the SL assumption in cloud retrievals, the accuracy would be equal to the sum of SS and MS. Introducing a multilayer
316 detection method yields both false and true ML pixels. Thus, a new source of error comes with the additional information. The
317 net gain of accuracy is not simply equal to ACC - SS; it must account for the newly introduced error, represented in MS. The
318 falsely detected ML clouds are a potentially worse source of error than the SL assumption for ML clouds. Multi-layered cloud
319 property retrievals for a false ML pixel require the creation of a second cloud layer and inference of its properties, whereas a

320 single-layered retrieval for a true ML pixel results in a cloud with properties somewhere between the upper and lower layer.
321 Thus, including a ML detection algorithm in a retrieval may not be reasonable if FM is too large. Based on Table 3, the
322 MLANN NGA = 7.6% and 7.3% during day and night, respectively, over SF surfaces. The corresponding values over snow-
323 covered surfaces are 3.4% and 1.0%. While the MLANN provides a nearly negligible amount of information over SC areas at
324 night, elsewhere it clearly represents an improvement over simply assuming that all clouds are single-layered.

325 Global distributions of the mean 2009 ML cloud fraction from the validation results are plotted in Fig. 3. While the
326 daytime MLANN means (Fig. 3b) are noticeably smaller than the average CC ML fractions (Fig. 3a), the two datasets have
327 similar distributions. At night (bottom), the patterns are much like those during the daytime, except in the polar regions. More
328 CC pixels (Fig. 3c) are classified as ML in the tropics than during the daytime. A comparable increase occurs in the MLANN
329 nocturnal results (Fig. 3d), which have ML fractions over much of the Amazon Basin and central Africa that are comparable
330 to their CC counterparts, although they are smaller elsewhere. As expected from Table 4, the MLANN ML fractions in the
331 polar regions are relatively small during the day and negligible at night.

332 The latitudinal variations of the mean ML fractions are plotted in Fig. 4. As expected from Fig. 3, the zonal patterns
333 are much the same with the MLANN values (triangles) being consistently less than their CC counterparts (circles). In the
334 tropics, the daytime differences generally fall between -0.06 to -0.04 and drop to as low as -0.08 in the polar regions. During
335 the night, the minimum of -0.10 is found over the polar regions, but the differences are comparable to the daytime values
336 between 45°S and 45°N. The MLANN is clearly less effective during the night over snow and ice-covered areas, especially at
337 night. Overall, the MLANN underestimates the 2009 ML cloud amount by 0.05 and 0.06 relative to the CC ML cloud fraction
338 during day and night, respectively. The non polar MLANN zonal night-day ML mean fractional differences from Fig. 4 are
339 plotted against their CC counterparts in Fig. 5 to determine how well the MLANN captures the changes in ML fractions from
340 day to night. The MLANN and CC differences are well correlated as indicated by the squared correlation coefficient, $R^2 =$
341 0.88. While the absolute differences are quite comparable when small, the absolute night-day differences from MLANN tend
342 to be greater than their CC counterparts at the extremes. The greatest MLANN night-day differences are found in the deep
343 tropics and north of 45°N.

344 5 Discussion

345 These results represent a significant improvement over the previous MLANN formulation (Minnis et al. 2019), which only
346 attained accuracies of 80.4% and 77.1% during the day and night, respectively over SF surfaces. Much of the increased
347 accuracy is due to use of shorter CALIPSO horizontal averaging distances here. By employing CALIPSO averages over
348 distances up to 80 km, Minnis et al. (2019) attempted to detect ML cloud systems that included many cirrus clouds having
349 optical depths smaller than 0.2. Such clouds are difficult to detect with passive remote sensing even when they are single-
350 layered. According to Yost et al. (2021), systems having $\tau_{cc} < 0.2$ account for ~42% of all ML clouds for CALIPSO data using
351 $HA \leq 80$ km compared to only 18% for $HA \leq 5$ km. A majority of those low-optical-depth ML clouds were not detected in

352 Minnis et al. (2019), resulting in lower accuracies. Typically, cloud identification or multilayered cloud detection methods that
353 use CALIPSO for validation or training employ data with $HA \leq 1$ or ≤ 5 km (e.g., Desmons et al., 2017; Marchant et al., 2020;
354 Tan et al., 2022; White et al., 2021). By using that smaller averaging distance in this study, the fraction of CC ML clouds is
355 $\sim 25\%$ less than that used by Minnis et al. (2019), but a larger portion of them is detected. Other sources for the improvement
356 arise from utilizing additional input parameters, including those based on the $13.3\text{-}\mu\text{m}$ channel and $\rho_{1.38}$, and $\rho_{1.61} - \rho_{2.13}$.
357 Additionally, the assumption that all pixels having $\tau_{CM} < 0.5$ are automatically SL, regardless of the CALIPSO classification,
358 probably removed some difficult but less important cases.

359 **5.1. Dependence on cloud properties**

360 Much like other retrievals, the MLANN is sensitive to various cloud conditions, such as the altitudes of the two layers and
361 their respective optical depths. Because the MLANN uses a minimum separation distance of 1 km between the ice and liquid
362 cloud layers, the dependence on separation distance is not explicitly considered here. Its impact on MLANN, examined by
363 Sun-Mack et al. (2017) and Minnis et al. (2019), is similar to that from other studies. Tan et al. (2022), for example, found that
364 the probability of ML detection using a random forest method was greatest for separation differences of 3 km or more and that
365 it dropped from values exceeding 0.8 to less than 0.5 for cloud gaps smaller than 1 km. Greater discrepancies in altitude
366 between the upper and lower clouds increase the differences in the layer temperatures yielding stronger signals in the thermal
367 channels. It is assumed that this type of dependency, found in the aforementioned MLANN studies, is operative for this version
368 of the MLANN. Despite the apparent increase in accuracy using wider separation in the training, Minnis et al. (2019) found
369 that NGA was 60% greater for 1-km separation compared to the 3-km separation dataset. Moreover, the smaller separation
370 yielded nearly 50% more actual ML clouds than the greater separation. The increase in apparent accuracy in the dataset using
371 a minimum 3-km gap relative to its 1-km counterpart is primarily due to assuming that a significant fraction of the ice-over-
372 water systems is single-layered, even though there is separation and two different phases in the column.

373 As formulated here, the MLANN assumes that all clouds with $\tau_{CM} < 0.5$ are SL. To examine this assumption, the MLANN
374 was also trained without any minimum COD limit. On average, ACC dropped by 1.2% and the total fraction of ML clouds
375 from CC increased by 1.8%. Despite the drop in ACC, NGA rose by 0.1%. Thus, the net impact is small and the downstream
376 task of unscrambling the upper and lower cloud properties from a cloud system with such a small COD will be eased somewhat.

377 For the radiation budget, some of the most important factors are the CODs associated with the detected and missed ML
378 systems. To determine the efficacy of the MLANN as a function of COD, the MLANN recall is plotted in Fig. 6 for each (τ_{CC} ,
379 τ_{CM}) bin for 2009. In the plots, τ_{CC} is the ice COD for ML clouds, i.e., the upper layer COD. Irregular scales are used for the
380 axes to provide more detail for the lower COD values. Because of large uncertainties and reduced sampling, bins having τ_{CC}
381 > 20 are not reliable. During the day, RC is greatest ($\sim 90\%$) for the bins having $\tau_{CC} \sim 1.7$ and $\tau_{CM} \sim 11$ for both ice (Fig. 6a) and
382 water clouds (Fig. 6b). Recall exceeds 0.5 for ice clouds having $\tau_{CM} > 3$ and $0.3 < \tau_{CC} < 5$. When $1.5 < \tau_{CM} < 3$ and $0.3 < \tau_{CC}$

383 < 1.3, RC remains above the halfway mark. The shape of the 50th percentile envelope for the water clouds differs from the ice
384 clouds as a result of more upper-cloud CODs being smaller than for ML clouds identified as ice (Yost et al. 2021). Thus, the
385 training for liquid clouds produces better ML detection when the ice clouds have small CODs.

386 At night, τ_{CM} is based only on thermal channels and, therefore, is mostly constrained to values of 8 or less. Default values
387 of 8, 16, and 32 are employed whenever the cloud is assumed to be optically thick. The particular default value depends on
388 the circumstances (Minnis et al., 2021). Sometimes, the CM4 and CM4+ analytical COD retrievals produce a value exceeding
389 8. Typically, τ_{CM} is closer to the upper-cloud COD at night, being influenced little by the lower cloud when the separation
390 distance is large. Ignoring the high τ_{CC} bins, the nocturnal RC maxima are found around bins (1.1, 2.0) and (1.3, 4.5) for ice
391 (Fig. 6c) and water clouds (Fig. 6d), respectively. True ML clouds are found more often than false SL clouds for $1 < \tau_{CM} < 5$,
392 when the phase is ice and $0.1 < \tau_{CC} < 3$. The halfway COD bounds narrow to $0.2 < \tau_{CC} < 0.4$ for greater values of τ_{CM} . For
393 water-phase clouds, $RC > 50\%$ occurs mostly for $1.5 < \tau_{CM} < 8$ and $1.5 < \tau_{CC} < 4$. It is clear that the thermal channel method
394 is sensitive to thinner upper clouds compared to the daytime methods when the solar channel signal is overwhelmed by the
395 lower cloud reflectances. Conversely, the daytime method detects more ML clouds when $\tau_{CC} > 3$ or so.

396 This is more evident in Fig. 7, which shows histograms of the matrix parameters as a function of upper-layer τ_{CC} for MM
397 and SM and τ_{CM} for SS and MS over SF surfaces. For water phase clouds (Fig. 7a) the relative frequency of true ML pixels
398 (TN), shown as solid lines, is greater at night than during the day when $\tau_{CC} < 0.5$, but the occurrence of daytime MM pixels
399 exceeds their nighttime counterparts when $\tau_{CC} > 0.9$. Similar behavior is seen for the ice phase pixels (Fig. 7b), but the
400 thresholds shift from 0.5 to 1.4 and from 0.9 to 1.9. The false SL or missed ML clouds (MM), shown as dashed lines, vary
401 differently. For the ice phase pixels (Fig. 7b), the MM pixel frequency rises with increasing τ_{CC} up to $\sim 8\%$ at $\tau_{CC} = 3.5$ before
402 decreasing to 5-7%, then dropping toward zero at $\tau_{CC} = 25$. This peak for the thick ice clouds reflects the difficulty of inferring
403 a lower layer under a nearly opaque cloud. For water-phase clouds (Fig. 7a), MM is most common for $\tau_{CC} < 0.3$ and diminishes
404 steadily to near zero around $\tau_{CC} = 30$. As τ_{CC} increases, the ML system is more likely to be identified as ice phase, so fewer
405 cases of ML systems having large upper-layer COD will be included in this population. In both cases, the night and day MM
406 frequencies track each other relatively closely with τ_{CC} . Similar variations are found over the SC surfaces (not shown).
407 Cumulative probability distribution functions based on the SF and SC results, presented in Fig. S1, show that 50% of the
408 missed ML clouds have $\tau_{CC} < 0.25$ for SF water clouds and < 0.5 for SC water clouds.

409 Figures 7c and 7d show the frequency histograms of SS and MS for CC SL liquid and ice clouds, respectively, as a
410 function of τ_{CM} . As expected, the peak SS (true SL) frequency occurs for $\tau_{CM} < 0.5$ for both phases, day and night. During the
411 day, a secondary true SL maximum is found around $\tau_{CM} \approx 25$ for ice and water clouds. At night, that secondary peak is around
412 $\tau_{CM} \approx 14$ for ice pixels and near $\tau_{CM} \approx 9$ for liquid clouds. Nocturnal false ML clouds (MS) are found mostly between CODs
413 of 1 and 5 at night for ice pixels and between 2 and 6 for water clouds. During the day, MS occurs most often for $\tau_{CM} \approx 14$ for

414 water clouds. In fact, the MS frequency seems to follow the SS values, except for $\tau_{CM} < 0.5$. The daytime MS occurrence is
415 relatively flat for ice clouds with $\tau_{CM} > 1.0$.

416 Another factor that can influence ML detection is the assumption that the lower cloud layer is composed of liquid water
417 whenever the cloud temperature is less than 253 K. While that is true for most clouds, a small fraction of ice clouds have top
418 temperatures above 253 K (e.g., Hu et al., 2010). In those instances, the ML signal would likely be reduced because of
419 similarities in the optical properties of the two layers. Mixed-phase clouds, which often occur in the supercooled temperature
420 range, would have a similar effect, but to a smaller degree depending on the amount of ice in the cloud. On the other hand,
421 supercooled clouds globally account for about half of the clouds having an infrared CTT between 243 K and 253 K. If only
422 snow and ice surfaces are considered, the range is 239 K to 242 K (see Fig. 6 of Hu et al., 2010). Thus, some systems with
423 cold (CTT < 233 K) ice clouds over supercooled liquid clouds with CTT < 253 K could be identified as SL ice by the definition
424 used here. These complementary effects due to supercooled clouds could produce some confusion in the training of the
425 MLANN, particularly in polar regions.

426 The CODs used in the training would not be the same as those determined using the standard CM4 algorithms employed
427 for the 2009 retrievals because the CM4+ algorithms used a different ice crystal model and a new method for retrieving COD
428 over snow. This change in COD retrieval apparently had minimal impact on the detection as the 2008 training and 2009
429 validation results are nearly identical.

430 **5.2 Comparisons with other results**

431 As noted earlier, multilayered cloud detection has been the subject of many different algorithmic studies, so it is important to
432 better understand how the current approach compares to those other algorithms. Direct comparisons are not straightforward
433 because each algorithm was developed with its own specific constraints and ML definitions. The CERES Ed4 ML algorithm
434 (Chang et al., 2010a, Minnis et al., 2021) was applied only when a cloud with pressure below 500 hPa was detected using a
435 CO₂-absorption method (Chang et al., 2010b). The MODIS science team algorithm (Wind et al. 2010) was applied to a 5-km
436 cloud product and was only used when the MODIS optical depth exceeded 4. The latest version, MYD06 C6.1 (Platnick et al.,
437 2017), adds the BTD₁₁₁₂ technique developed by Pavolonis and Heidinger (2004). Desmons et al. (2017) used data from the
438 Polarization and Directionality of the Earth's Reflectance (POLDER) to detect ML clouds of all types, but only for $\tau > 5$. Ice-
439 over-water multilayered clouds were detected by Wang et al. (2019) during daytime using Suomi-NPP (SNPP) Visible Infrared
440 Imager Radiometer Suite (VIIRS) data in a thresholding method. Tan et al. (2022) placed no restrictions on either τ or the
441 number of layers, but they applied their random forest algorithm and other machine learning techniques only to geostationary
442 Himawari-8 data. Because of its orbit, the Himawari-8 observations are taken over a full range of VZA when matched with
443 the CC profiles, but the VZA is constant for a given location. Other published methods have either not produced extended
444 datasets or performed only case-study evaluations with objective data. Despite the sampling disparities, it is informative to

445 compare some of the statistics to provide some context to the performance of the MLANN. These comparisons are summarized
446 in Table 5.

447 Comparing with CC data, Desmons et al. (2017) found that for overcast clouds with $\tau > 5$, ACC = 70% and CoS = 74%.
448 For the same conditions, they determined that MYD06 C6.1 yields ACC = 67% and CoS = 73%. Additional parameters
449 computed from their Table 4 are listed in Table 5. Precision and recall from MYD06 are 54% and 47%, respectively, while
450 they are 58% and 47% from POLDER. These can be compared to the MLANN daytime validation results (Table 5), which
451 combine the SC and SF daytime data in Table 4 weighted by 0.13 and 0.87, fractions that roughly correspond to the areal
452 coverage of the respective surface types (e.g., Yost et al., 2023). All of the MLANN parameter values exceed their restricted
453 MYD06 and POLDER counterparts. Wang et al. (2019) only reported validation results in terms of percent of CALIOP ML
454 and SL. Thus, only RC and CoS could be determined from their results. For $\tau > 1$, the recall is about the same as the daytime
455 MLANN value, if the ML and probably ML categories from their algorithm are combined. Similarly, their CoS is ~10%
456 smaller than the MLANN value. If clouds with $\tau < 1$ are included, both CoS and RC drop substantially. Note that Wang et al.
457 (2019) did not include CloudSat retrievals in their evaluation, so ML clouds with an optically thick upper cloud are not included
458 in the statistics.

459 Although no value for ACC was given, the values of certain parameters can be estimated for all clouds with an unrestricted
460 optical depth from the figures in Desmons et al. (2017). From their Fig. 8, RR \approx 38%, so ACC = 62%. The value of CoS is the
461 same for restricted and all clouds. The MODIS parameters change only negligibly for all clouds compared to the restricted
462 case because the MYD06 algorithm only uses clouds with $\tau > 4$. Marchant et al. (2020) also compared the MYD06 to the 2B-
463 CLDCLASS-lidar products and found that for clouds with $\tau > 4$, ACC = 63% with the Pavolonis and Heidinger (2004)
464 algorithm and 65% without it. If it assumed that all clouds with $\tau < 4$ are SL, then ACC jumps to 80% and 81% for the two
465 algorithm options. But that assumption excludes 45% of the ML clouds as defined by Marchant et al. (2020).

466 Except for the definition of what constitutes a ML cloud (ice over water, water over water, etc.), NGA is the one parameter
467 that is not too dependent on cloud optical depth assumptions. From Desmons et al. (2017), the daytime POLDER and MYD06
468 C6.1 cases yield NGA = 4.4% and 2.2%, respectively. Presumably, some of the POLDER results include water-over-water
469 clouds. Nevertheless, the POLDER algorithm yields a net gain in information. The results of the Marchant et al. (2020) analysis
470 yield slightly lower numbers for the MODIS C6.1 NGA, 0.2% and 1.4%, with and without the Pavolonis and Heidinger (2004)
471 method. In either case, the MLANN daytime NGA exceeds those of the MYD06 and POLDER techniques. Moreover, it greatly
472 exceeds the CERES Ed4 ML results (not shown). The F1 scores track the relative NGA rankings with the Himawari training
473 values at the top followed by the MLANN, POLDER, and MODIS C6.1 in diminishing order.

474 The random forest results from Tan et al. (2022), confined to 60°S - 60°N and 80°E and 160°W, were trained with 1-km
475 matched 2B-CLDCLASS-LiDAR profiles using the product's layer flag to determine if a given pixel is SL or has more than
476 one layer, regardless of layer phase. That training dataset produced ACC = 85% and 79%, respectively, for the daytime and

477 all-hours algorithms. The latter method included no reflectance input from solar channels so it can be used for both day and
478 night conditions. It is included in the bottom section of Table 5 for comparison to the MLANN night version. For this technique,
479 PR = 81% and 73% for day and all-hours, respectively, with corresponding RC values of 72% and 64%. While ACC is less
480 than that found with the MLANN for both day and night, the random forest PR and RC results are greater than their MLANN
481 counterparts. At night, the MLANN PR is nearly equal to the Himawari-All value. The Himawari CoS and NGA daytime
482 values were deduced from the values in their Table V and their equations (1) - (3). The MLANN CoS values exceed their
483 Himawari counterparts, but the MLANN global NGAs are less than half of those from the random forest training results. Those
484 larger values arise, in part, from including many more types of ML clouds in the random forest training than used for the
485 MLANN.

486 A fairer comparison would use independent validation sets from both algorithms. While a complete summary of the
487 validation comparisons was not provided in Tan et al. (2022), several parameters can be determined from their Fig. 5, which
488 utilized a dataset independent of the training data. The resulting values of PR are 70% and 64% for day and all-hours,
489 respectively, while CoS = 89% and 85%. The MLANN SL confidences are slightly greater at 90% and 88% and its PR values
490 exceed the Himawari validation results, especially for night/all-hours. Without further information it is not possible to
491 determine the values of ACC and RC for the geostationary validation dataset. However, because CoS is the same or larger for
492 the validation dataset and PR dropped by 11 points from the training results, it can be inferred that the fraction of false ML
493 clouds increased considerably. This would reduce ACC and substantially diminish NGA.

494 Interestingly, the best results from the Tan et al. (2022) validation analysis are for ice-over-liquid and ice-over-mixed
495 clouds. The former corresponds to conditions that the MLANN was developed to detect, while at least some of the latter were
496 included in the MLANN analysis. Approximately 30% of the actual ML clouds detected in the Tan et al. (2022) validation
497 analysis are for single phase or upper-layer mixed phase ML clouds that MLANN was not designed to identify. Assuming that
498 the portion of the ice-over-water/mixed is the same for the training dataset, the correctly detected ice-over-water cloud amount
499 is 0.10. Adding the ice-over-mixed would yield 0.17. Reducing that by the ratio of PRs from the validation and training sets
500 would drop the range to 0.09 - 0.15, which bounds the correct ML fraction from the SF cases in Table 4.

501 **5.3 Full-swath detection**

502 The MLANN training is based on near-nadir measurements from both the CC and MODIS instruments. Increasing optical path
503 lengths due to increasing VZA modify the radiances emanating from a given location through absorption and scattering. This
504 is particularly true for radiances at solar wavelengths. Thus, the near-nadir-based MLANN coefficients are not necessarily
505 valid for observations taken at other VZAs. For operational use with Aqua MODIS data, the MLANN must be reliable across
506 all viewing angles.

507 5.3.1 Angular dependence

508 The VZA dependency is examined by first computing the mean radiances for each viewing angle across the full scan for data
509 taken during JAJO 2019. It was found that the radiance VZA dependence is sensitive to the forward or backward portion of
510 the scan cycle. The former view is toward the sun, while the latter is directed away from the sun. Figure 8 plots the reflectance
511 averages for each VZA bin in the forward (positive) and backward (negative) directions. From near-nadir to 65° , the $1.60\text{-}\mu\text{m}$
512 reflectance (solid lines) for water cloud pixels increases by 11% and 25% in forward and back directions, respectively. For ice
513 clouds, the corresponding increases are 22% and 37%. Similar changes are seen for the $2.13\text{ }\mu\text{m}$ reflectances (dashed lines).
514 The $1.38\text{-}\mu\text{m}$ reflectance for ice behaves in much the same manner (Fig. S2), but is nearly constant with VZA for water clouds.
515 The daytime $3.75\text{-}\mu\text{m}$ radiances (Fig. S3) are relatively flat in the back direction, but increase with VZA for liquid clouds. At
516 night, the radiances show the classic limb-darkening behavior of thermal radiation. This can be seen in Fig. 9. During the day
517 (solid lines), the water-cloud $10.8\text{-}\mu\text{m}$ radiances are relatively flat in the forward direction and drop a little at the higher VZAs
518 in the back direction. Ice cloud radiances decrease in both directions, but more so in the forward view where the $10.8\text{-}\mu\text{m}$
519 radiances are lower than their back-direction counterparts. The forward scan views more shadowed areas that could affect the
520 thin cloud and partly cloudy scenes over land (Minnis et al., 2004). At night (dashed lines), the limb-darkening is more
521 apparent. No back and forward differences are considered at night. Similar variations in radiance are seen at $8.55\text{-}\mu\text{m}$ (Fig. S5)
522 and $11.90\text{-}\mu\text{m}$ (Fig. S6). There are only minor radiance differences between the forward and back directions during the day
523 for the $6.70\text{-}\mu\text{m}$ channel (Fig. S4), presumably because it is mostly unaffected by the layers below the cloud. Additional plots
524 of radiances as a function of VZA (Figs. S6 -S14) are provided in the Supplemental Material.

525 To adjust the MODIS radiances, ice and water correction factors were determined for each waveband, day and night,
526 separately over SF and SC surfaces. For daytime, the correction factors were computed for both forward and back scans. These
527 factors were developed for both the channel radiances and reflectances and each of the BTM parameters. The correction factor
528 is simply the ratio of the mean radiance for VZA between -3° and -18° divided by the mean radiance at a given VZA. Thus,
529 the observed radiance is adjusted to the near-nadir view of MODIS by simply multiplying it by the correction factor.

530 To test the impact of these factors on the retrievals, the MLANN was applied to the uncorrected and corrected full-swath
531 MODIS data for April 2009. Figure 10 shows the variation of mean ML fraction as a function of VZA for SF ice and water
532 clouds, day and night. During the day (Fig. 10a), the uncorrected and corrected ML fractions are nearly identical suggesting
533 that the correction factors for water phase clouds have minimal effect on the radiances. This is not surprising, given the
534 relatively flat daytime curves in Fig. 9 and for other thermal channels. In contrast to the daytime results, the nocturnal ML
535 fractions have a nonmonotonic variation with VZA for the uncorrected radiances and a significant steady decrease to a value
536 near zero for the corrected case. The uncorrected radiances for daytime ice clouds (Fig. 10b) yield a rise in ML detection in
537 the forward direction with a much smaller rise in the back direction. At night, the ice cloud ML amounts drop for $|VZA| >$
538 40° . When the correction factors are applied to the radiances, the ML amounts are relatively constant with VZA for both time

539 periods. To obtain the most consistent product across the swath, the adjustments are applied to all of the radiances, except for
540 water cloud pixels observed during the night.

541 5.3.2 Example images

542 Figure 11 shows the results of applying the MLANN with VZA correction to an Aqua MODIS image taken over the Southern
543 Ocean centered near 57°S, 165°E at ~3:50 UTC, 16 April 2019. The pseudo color RGB image (Fig. 11b) shows an extensive
544 area of stratocumulus on the left side that is apparently overlaid with thin cirrus that blurs the view of the underlying clouds.
545 A second extensive liquid cloud deck appears near the top center that might overlay some StCu clouds, but is itself covered
546 by thicker ice clouds. The CM4 cloud phase results (Fig. 11a) highlight those contiguous dense ice clouds, which likely obscure
547 lower clouds. Thin cirrus also appear to overlies parts of the second liquid deck. The MLANN (Fig. 11c) determines that a large
548 portion of the image consists of ice-over-water clouds. In general, the outline of the cloud effective heights (CEH) above 1 km
549 correspond to the ML pixels (Fig. 11d) except where the ice cloud is very thick, or perhaps, the ice cloud is in close proximity
550 to or contiguous with the lower deck, as over parts of the white clouds in top center part of the image. Other higher, SL liquid
551 clouds are seen near the top left corner and bottom right of center. Cloud phase is very mixed over the thin cirrus areas, yet
552 the MLANN determines most of the pixels as ML.

553 Multilayered clouds detected with the nighttime MLANN are shown in Fig. 12 for a MODIS image taken around 4:45
554 UTC the same day over the North Atlantic. The scene (Fig. 12b) contains extensive but variable cirrus coverage (white) and
555 broken stratus clouds typically between 1 and 3 km (Fig. 12d). Thicker cirrus clouds are identified as ice (Fig. 12a) while many
556 of faintest ones, primarily those over the low clouds, are classified as liquid. Denser ice clouds and those over open water
557 appear to be at altitudes between 9 and 14 km, while the thin Ci over St range from 3 to 7 km, which is expected, given the SL
558 cirrus altitudes. The MLANN appears to identify many of those ML clouds (Fig. 12c), but tends to miss those with overlying
559 thick cirrus. There may be some false ML clouds in the upper right, but it is difficult to tell because the thinnest Ci is not
560 always discernible in the RGB image.

561 The final example shown here (Fig. 13) is taken the same day around 01:50 UTC over the polar ice cap centered near
562 80°N, 155°E. Snow and ice cover provide the scarlet background (Fig. 13b), which is overlaid with low clouds in various
563 shades of white to gray and a slightly higher deck in the center with thin Ci covering much of the top half of the image. That
564 cirrus appears as blurry pinkish gray and identified as ice or liquid depending on the thickness (Fig. 13a), while most of the
565 cirrus over the deck in the middle is designated as liquid. Those clouds are identified as ML by the MLANN along with the
566 small area at the bottom and in the upper left (Fig. 13c). Only a few parts of the cloud left of center are classified as ML, while
567 it appears more ML clouds should have been detected. Most of the SL ice cloud CEHs are only between 3 and 6 km (Fig.
568 13d), while those over the middle deck are less than 3 km. The low CEH values are likely due to overestimation of the COD
569 by the CM4 retrieval for SL clouds and to the presence of the thick lower cloud for the ML retrievals. Detection of the ML

570 clouds will allow reclassification of the cloud tops as ice and recalculation of the cloud properties, when the components of a
571 two-layer retrieval system are in place.

572 These three examples and the two additional cases shown in Figs. S15 and S16 demonstrate that MLANN performs
573 reasonably well across the full swath. No wild false ML clouds are evident although some recognizable misses are seen, as
574 expected from the analyses above. Quantifying the accuracy of the correction-factor approach to full swath application of the
575 MLANN would ultimately require using the method on similar data taken by a different satellite, such as SNPP VIIRS, that
576 overlapped with the CC data at various VZAs. Using VIIRS data, Wang et al. (2019) found that the ML clouds they detected
577 showed minimal changes with VZA. That result is similar to the daytime curves in Fig. 10b. Developing and analyzing a
578 comparable VIIRS-CC dataset is beyond the scope of this paper, but is planned for future research.

579 **5.3.3 Assessment of full swath results**

580 In the interim, more indirect approaches are available. For example, the off-nadir and near-nadir results should be spatially
581 consistent if the swath approach is working properly. To examine this aspect, Figure 14 shows the distributions of ML cloud
582 fractions averaged over the months of January, April, July, and October (JAJO) 2009 from three different data sources. These
583 include daytime retrievals from all CC data (Fig. 14a), MLANN applied to Aqua MODIS radiances observed at the reference
584 near-nadir ($-3^\circ < \text{VZA} < 18^\circ$) angles (Fig. 14b), and to Aqua MODIS data taken at all VZAs (Fig. 14c). The corresponding
585 nocturnal results are plotted in Figs. 14d-f. These results are noisier than those in Fig. 3 because they are based on only 4
586 months of data and they include all observations, not just those having good CC and C3M cloudy pixel matches. The MODIS
587 results include both false and partially cloudy pixels.

588 As in Fig. 3, the CC and near-nadir patterns are comparable although the MLANN means are often smaller than their CC
589 counterparts. The areas with minimal ML amount in the near-nadir results (Fig. 14b) are in the same locations as those from
590 the CC retrievals, but are more pronounced. Some CC maxima are reproduced by the MLANN, but the MLANN fractions
591 near the maxima drop off more precipitously than their CC counterparts. For example, the maximum off the southern Chilean
592 coast in Fig. 14b is nearly identical that in Fig. 14a, but the MLANN fractions in the surrounding areas are generally smaller
593 than the CC values. While much smoother, the non-polar patterns in both all-VZA cases (Fig. 14c) are similar to those from
594 the near-nadir results, but the Chilean maximum is diminished somewhat. Linear regression between the daytime CC and the
595 MLANN regional means yields R^2 values of 0.80 and 0.66 for the near-nadir and full-swath results, respectively. The smaller
596 value for the full-swath data is not surprising given its greater sampling. For the matched near-nadir and full-swath means, R^2
597 = 0.81.

598 Distributions of ML fractions from the same datasets appear to be more consistent at night. The maxima over northern
599 South America, central Africa, and Indonesia are well defined in all three maps. Like the daytime results, the non-polar minima
600 are much better delineated in Figs. 14e and 14f than in the CC data (Fig. 14d). The correlation coefficients are 0.71 and 0.64
601 for the nocturnal CC regional means matched with their respective MLANN near-nadir and full-swath counterparts, while R^2

602 is 0.89 for the matched near-nadir and full-swath averages. Overall, the distributions in Fig. 14 demonstrate that the full-swath
603 MLANN does not yield spurious ML clouds in areas where they are not expected to occur and generally produce results similar
604 to the near-nadir values.

605 Another measure of robustness of the algorithm is its ability to reproduce the seasonal cycle. This is examined by
606 computing the monthly mean ML anomaly, which is defined as the monthly mean minus the annual average divided by the
607 annual average. It is clear that the SC results over snow miss many ML clouds, especially at night. Thus, to minimize the
608 influence of SC regions on the seasonal cycle, only nonpolar (60°S - 60°N) data are considered. Figure 15 plots the ML fraction
609 anomaly for each month of 2009 from CC and the MLANN applied to full-swath Aqua MODIS data. The MLANN day and
610 night anomalies track their CC counterparts remarkably well, within a few percent in most cases. The values of R^2 between
611 the CC and MLANN monthly means are 0.92 and 0.90 for day and night, respectively.

612 To further examine the reliability of the MLANN on longer time scales, it was applied to January, April, July, and October
613 (JAJO) 2013 Aqua MODIS full swath data. The global distributions of the 2009 and 2013 results (Fig. S16) are similar, but
614 reveal shifts in the locations of the maxima. Table 6 presents the global mean JAJO 2009 and 2013 ML fractions along with
615 the land-ocean ratio, L/O, which is the global average ML fraction over land divided by that over water surfaces. Overall, ML
616 fractions for all CC data are 3 - 5% greater than their MODIS-matched counterparts, a result comparable to the differences in
617 Fig. 4. The 2009 MLANN near-nadir values are 0.01 smaller than those for all VZAs. ML fractions in Table 6 are all less than
618 their counterparts in Fig. 4. This is due to the fact that the CC data in Table 6 include all cloudy pixels that the CERES cloud
619 mask classified as clear and the MLANN results include many partly cloudy pixels that are not likely to be ML. The clouds
620 detected by CALIPSO, but missed by CERES are mostly SL thin cirrus and SL low clouds (Yost et al. 2021, 2023), which
621 would dilute the ML fraction determined using all of the CC data. The differences between the CC and near-nadir MLANN
622 are reduced by ~2% compared to those using only the matched data. During daytime, the MLANN mean ML fractions from
623 2013 are 0.5% greater than those in 2009, while at night the 2013 averages exceed their 2009 counterparts by 0.2% near nadir
624 and 0.6% across the full swath. For both years, the nocturnal near-nadir values are ~1% less than for data taken at all VZAs.

625 The CC land-ocean ratios, L/O, in Table 6 reveal that fewer ML clouds occur over land than over water surfaces. For CC,
626 L/O is between 0.77 and 0.84, while it varies from 0.64 to 0.77 for the MLANN results, indicating that the MLANN is less
627 efficient at detecting ML clouds over land than over water bodies. Together with the similarity of the CC and ML seasonal
628 cycles, the consistency of the near-nadir and full-swath L/O values and small differences in ML amounts during both years
629 are quite encouraging for using the MLANN on an operational basis.

630 **5.3.4 Operational considerations**

631 CERES is a long-term project that utilizes many different satellites and imagers to characterize cloud properties. The MODIS
632 on Aqua and Terra and the VIIRS on SNPP and NOAA-20 are coincident with the CERES broadband radiometers and observe
633 non-polar regions at fixed times each day. Any system designed to detect ML clouds should be applicable to both the VIIRS

634 and MODIS imagers and, ideally, to the geostationary imagers that are used to help assess the radiation budget at other times
635 of day. Because the latter have had widely varying spectral channel complements since 2000, use of MLANN with them is
636 beyond the scope of this discussion. The VIIRS lacks certain channels used here (13.3 μm and 6.7 μm) and the channels
637 common to MODIS and VIIRS differ in spectral coverage and filtering. Additionally, the VIIRS is a higher resolution
638 instrument. Thus, it may be necessary to train VIIRS with CC data to obtain a consistent ML result. Another approach would
639 require careful inter calibration of the VIIRS and MODIS channels using spectral corrections (e.g., Scarino et al., 2016) and
640 the addition of radiances from the missing channels determined from a process that fuses data from VIIRS and the Crosstrack
641 Infrared Sounder (e.g., Weisz et al., 2017). If those are not available, then the MLANN would need to be retrained with fewer
642 input radiances, likely at the expense of accuracy. To that end, initial training tests indicate that without those channels, ACC
643 decreases from 87.0% to 86.4% during the day and from 85.6% to 84.3% during the night over SF surfaces.. During the day,
644 NGA drops from 7.6 to 7.1%, while at night NGA goes from 7.3 % to 6.2%. NGA is relatively unaffected by the loss of the
645 13.3- μm channel; almost all of the diminished accuracy is due to the absence of the 6.7- μm channel, particularly at night. Even
646 with the loss of those channels, the resulting detection capability would still represent a significant advancement over previous
647 efforts.

648 As in all retrievals, reliable and consistent calibration across platforms is essential to providing an accurate ML product.
649 It may be even more important for the MLANN because the neural network relies on subtle radiance differences that may be
650 lost in the noise of a physical retrieval. Thus, any small trend in the calibration of one channel may introduce a growing bias
651 in the ML fraction. Similarly, inter platform calibration differences could cause a similar effect. Updated retrieval algorithms
652 and input data are introduced into the CERES data processing whenever major improvements are developed and errors
653 diminished. Since the MLANN relies on a few retrieval inputs such as COD and cloud phase, it would need to be retrained
654 whenever a new CERES cloud algorithm edition is introduced.

655 Further improvement of the MLANN itself, particularly over snow-covered areas, might be gained by using additional
656 parameters or spatial context. For example, Tan et al. (2022) found that radiances from the 7.3- μm channel comprise a highly
657 ranked predictor of ML clouds in their random forest approach. The MODIS equivalent channel was not considered here, but
658 would have to be created for VIIRS using the fusion process noted above. Information about the pixels surrounding the pixel
659 of interest increased the accuracy of ice water path retrieved from a Meteosat imager with a convolutional neural network
660 (Amell et al., 2022). Including selected radiances or BTDs from surrounding pixels might also enhance the MLANN.
661 Additional partitioning of the training categories might also raise ML detectability as it did when the original MLANN (Sun-
662 Mack et al, 2017) was divided into ice and water phase categories (Minnis et al. 2019). These and other approaches could lead
663 to greater accuracies than found here.

664 6. Summary and Conclusions

665 An artificial neural network method has been enhanced to more accurately identify ice-over-water ML cloud systems from
666 multispectral MODIS observations. The algorithm requires as input a variety of radiances, brightness temperature differences,
667 atmospheric profiles of temperature and humidity, and the CERES Edition 4 cloud phase and optical depths. Based on the
668 definitions of single and multilayer clouds used here for CALIPSO-CloudSat profiles, the MLANN correctly identifies SL and
669 ML clouds together 87.0% and 85.6% of the time over surfaces free of ice and snow during day and night, respectively. Over
670 ice or snow-covered areas, the corresponding correct identifications are 89.3% and 88.7%. Despite the good overall agreement,
671 the MLANN only detects 55% of the CC ML clouds over SF regions and only 40% and 20% over SC areas during day and
672 night, respectively. The majority of the missed SF ML clouds are those having an upper-cloud COD < 0.3 (water) or COD \geq
673 3 (ice), although $\sim 35\%$ and 20% of the water and ice-phase detected ML clouds meet those conditions. Over SC surfaces, the
674 undetected ML pixels mainly have an upper-cloud COD < 0.5 or COD > 2 .

675 Despite its shortcomings, the MLANN, unlike many other techniques, yields a significant net gain in layering
676 identification accuracy because the number of false ML pixels is substantially less than that for true ML pixels. Overall, the
677 daytime MLANN evaluation metrics are more favorable than those based on physical retrievals or decision tree algorithms,
678 even with the differences in sampling, ML cloud definitions, and optical depth constraints. Few methods have been developed
679 for nocturnal application. Comparisons with results from a machine learning algorithm applied to geostationary satellite data
680 have yielded a more ambiguous assessment. The accuracy and SL confidence from MLANN are greater than those from the
681 Tan et al. (2022) random forest training results for day and night. Yet, the MLANN precision, recall, and NGA values are
682 smaller. If the validation results from Tan et al. (2022) are considered, the MLANN precision values are greater. It is not
683 known how much the MLANN recall and NGA would fare relative to the random forest validation results. Even if it were
684 known, the relative merits of the two methods would be difficult to quantify without accounting for the discrepancies in ML
685 definition and sampling areas and time periods. However, it can be concluded from the comparisons that the MLANN is among
686 the most capable of current ML detection methods.

687 Operationally, the MLANN, trained with near-nadir MODIS views, must be applicable to all the MODIS viewing angles.
688 To account for the variation of radiances with viewing zenith angle, the MODIS-based input parameters are normalized to the
689 nadir view using empirical correction factors. The adjustments yield ML cloud amounts that are mostly invariant with VZA
690 and produce visually reasonable ML detection across the MODIS swath. Spatial distributions of ML cloud fractions from full-
691 swath results are consistent with the near-nadir results and manifest similar detection efficiencies over land and water surfaces
692 that are the same as their near-nadir counterparts. Temporally, the MLANN produces the same seasonal cycle in ML clouds
693 as the active sensor data, albeit with the noted bias. Moreover, the results are similar in magnitude and distribution for different
694 years with shifts in maxima. While more detailed pixel-to-pixel comparisons should be performed using CC data matched to
695 imagery taken at off-nadir VZAs, the analyses performed here indicate that the MLANN should be as successful off of nadir
696 as it is in the near-nadir mode.

697 Applying the MLANN to other imagers should be performed with caution as sensors on other satellites can differ
698 spectrally and spatially (e.g., VIIRS) or may observe at other times of day (e.g., Terra MODIS). Platforms that are not in Sun-
699 Synchronous orbits, for example geostationary satellites, will observe a given scene at times of day and at viewing and
700 illumination angles that are not seen by Aqua MODIS and hence not in the training complement. Adapting the MLANN to
701 different types of orbits or times of day presents a challenge as there are few options for global training and validation. Current
702 and future cloud radar and lidar combinations are confined to afternoon Sun-synchronous satellites (e.g., Heliere et al. 2017).
703 Lidars that can be used for cloud detection have flown on the International Space Station (e.g., Pauly et al., 2019) in a
704 precessing orbit and on Aeolus in a sunrise/sunset Sun-synchronous orbit (Straume et al., 2020). CALIPSO has been slowly
705 moving away from its 1330 LT orbit covering several more hours of the day since 2018. Without the cloud radar, any and all
706 of those lidars could be used to define ML clouds to some extent, depending on their penetration depths, and may be of value
707 for training and validating ML clouds for geostationary imager data. Regardless of the particular satellite, the MLANN would
708 need to be retrained or the spectral channels normalized to MODIS.

709 With layer detection accuracies below 90%, there is clearly room for future improvement, especially over polar regions
710 covered with snow and ice. Use of additional channels or subsets of the current training categories may add a few more points
711 to the overall accuracy. Combining physical retrievals with the neural network may also be the means for detecting more ML
712 pixels. The definition of ML clouds used here is rather restrictive in that it is nominally confined to ice over liquid water
713 clouds. It is also somewhat ambiguous because 253 K serves as the threshold between ice and water clouds for the underlying
714 cloud deck. In lieu of any better information to define the lower cloud phase, the threshold should be altered to account for
715 variability of the 50th percentile ice phase in the supercooled temperature range. Other cloud combinations such as liquid over
716 liquid could be included in the MLANN but they might reduce the accuracy and would probably be more resolvable if treated
717 separately from the ice over water clouds.

718 Detecting multilayer clouds is a first step toward improving the characterizations of global vertical cloud structure using
719 passive sensors. Once identified, the upper and lower layer cloud properties need to be estimated. A number of approaches
720 have been suggested for estimating the top heights of the upper and lower clouds. These include physical retrievals (e.g., Chang
721 et al. 2010) and machine learning (e.g., Minnis et al. 2019). Similarly cloud optical depth and particle effective size could be
722 derived with a physical retrieval (e.g., Chang et al. 2010), a neural network (e.g., Cerdeña et al. 2007), or an optimal estimation
723 method that requires the cloud heights (e.g., Sourdeval et al., 2016). Having a reliable detection method, like the MLANN,
724 should serve as motivation for formulating a robust technique for unscrambling the upper and lower cloud layer properties in
725 future research.

726

727 *Data availability.*

728 The MLANN training data used in here can be obtained from CERES Ordering Tool: <https://ceres.larc.nasa.gov/data/>.

729 Selecting the CCCM-Level 2 product will provide the C3M data, which also include the MOA data.

730

731 *Author contributions.* S. Sun-Mack, P. Minnis, and G. Hong developed the detection method. S. Sun-Mack implemented the

732 technique. Y. Chen, S. Sun-Mack, and P. Minnis performed the data analyses. The paper was first drafted by P. Minnis and

733 revised by S. Sun-Mack and W. Smith, Jr. The project was supervised by P. Minnis and W. Smith, Jr.

734

735 *Competing interests.* The authors declare no competing interests.

736

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921 **Tables**
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924 **Table 1.** Input parameters for MLANN.

Regional Parameters	GEOS-5.4	MODIS Thermal Data (K)	MODIS Solar Data [†]
Latitude (°), Longitude (°)	Surface skin temp (K)	T ₃₇ , T ₆₇ , T ₈₅ , T ₁₁ , T ₁₂ , T ₁₃ [@]	R _{CM} , τ _{CM}
Surface type, elevation	Relative humidity (%) at 8 levels*	BTD ₃₇₁₁ , BTD ₆₇₁₁ , BTD ₈₅₁₁ , BTD ₁₁₁₂ , BTD ₁₁₁₃ [@]	ρ _{1.38}
Solar zenith angle (°) [†]		τ _{CM}	ρ _{1.61} - ρ _{2.13}

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* levels: surface, 850, 700, 500, 400, 300, 200, 100 hPa

† day only

@ snow/ice free only

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Table 2. Confusion matrix definition.

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	CC Single	CC Multi	Total
MLANN Single	SS	SM	SS+SM
MLANN Multi	MS	MM	MS+MM
Total	SS+MS	MM + SM	SS+MM

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Table 3. Confusion matrices (each bounded by dashed lines) for MLANN applied to Aqua MODIS relative to layer identification from CloudSat-CALIPSO, 2008, from the training set. The bold numbers indicate the percent correct for each matrix.

<u>CloudSat and CALIPSO</u>												
	<u>Snow-free, Day</u>			<u>Snow-free, Night</u>			<u>Snow-cover, Day *</u>			<u>Snow-cover, Night*</u>		
<u>MLANN</u>	<u>SL</u>	<u>ML</u>	<u>Total</u>	<u>SL</u>	<u>ML</u>	<u>Total</u>	<u>SL</u>	<u>ML</u>	<u>Total</u>	<u>SL</u>	<u>ML</u>	<u>Total</u>
Ice SL,%	73.2	11.3	84.5	65.9	12.7	78.6	86.6	7.8	94.4	86.4	9.4	95.8
Ice ML,%	4.6	10.9	15.5	6.0	15.4	21.4	1.8	3.9	5.7	1.5	2.7	4.2
Total, %	77.8	22.2	84.1	71.9	28.1	81.3	88.4	11.7	90.4	87.9	12.1	89.1
# pixels x 10 ³	3,748	1,070	4,818	4,097	1,599	5,696	2,549	390	2,884	1,141	1,500	1,291
Liquid SL, %	76.3	7.4	83.7	79.5	7.9	87.4	82.7	8.2	90.9	87.3	9.0	96.3
Liquid ML, %	3.9	12.4	16.3	3.3	9.3	12.6	2.5	6.6	9.1	1.3	2.4	3.7
Total, %	80.2	19.8	88.7	82.8	17.2	88.8	85.2	14.8	89.3	88.6	11.4	89.7
# pixels x 10 ³	4,502	1,112	5,614	5,297	1,100	6,397	5,647	996	6,643	844	319	3,941

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Table 4. Same as Table 3, but for combined liquid and ice results from applying MLANN to the 2009 validation dataset.

<u>CloudSat and CALIPSO</u>												
	<u>Snow-free, Day</u>			<u>Snow-free, Night</u>			<u>Snow-cover, Day</u>			<u>Snow-cover, Night</u>		
<u>MLANN</u>	<u>SL</u>	<u>ML</u>	<u>Total</u>	<u>SL</u>	<u>ML</u>	<u>Total</u>	<u>SL</u>	<u>ML</u>	<u>Total</u>	<u>SL</u>	<u>ML</u>	<u>Total</u>
SL,%	75.3	8.9	84.2	74.0	10.1	84.1	83.6	8.4	92.0	86.2	9.8	96.0
ML,%	4.1	11.7	15.8	4.3	11.6	15.9	2.3	5.7	8.0	1.5	2.5	4.0
Total, %	79.4	20.6	87.0	77.3	21.7	85.6	85.9	14.1	89.3	87.7	12.3	88.7
# pixels x 10 ³	28,883	7,493	36,376	33,739	9,908	43,647	8,235	1,352	9,587	14,277	2,002	16,279

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Algorithm	ACC	PR	RC	CoS	F1	NGA
MYD06 C6.1, $\tau > 5$	67	54	46	73	0.50	2.2
POLDER 95, $\tau > 5$	70	58	47	74	0.52	4.4
VIIRS, $\tau > 1$ ($\tau < 1$)	-	65 (53)	65 (53)	79 (64)		-
Himawari Training Day	85	81	72	87	0.76	18.3
Himawari Validation Day	-	70	-	89		-
MLANN day	87	74	55	90	0.63	7.6
Himawari Training All	79	73	64	82	0.68	14.3
Himawari Validation All	-	64	-	85		-
MLANN Night	86	72	52	88	0.60	6.5

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952 **Table 5.** Confusion matrix metrics in % for various multilayer algorithms. MYD06 and POLDER 95 are based on Table 4 of
953 Desmons et al. (2017). VIIRS results are from Wang et al. (2019). Himawari results are based on Tan et al. (2022) random
954 forest results. MLANN results based on the 2009 validation parameters in Table 4. Dotted line separates results for day (top)
955 and night (bottom).

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Table 6. Average ML fractions from CC and Aqua MODIS MLANN for JAJO.

Time	CC 2009	MLANN near-nadir, 2009	MLANN all VZA, 2009	MLANN near-nadir, 2013	MLANN all VZA, 2013
Day, ML (%)	15.4	12.1	11.8	12.6	12.3
Night, ML (%)	17.7	12.6	13.5	12.8	14.1
Day, L/O	0.77	0.64	0.65	0.63	0.64
Night, L/O	0.84	0.74	0.75	0.76	0.77

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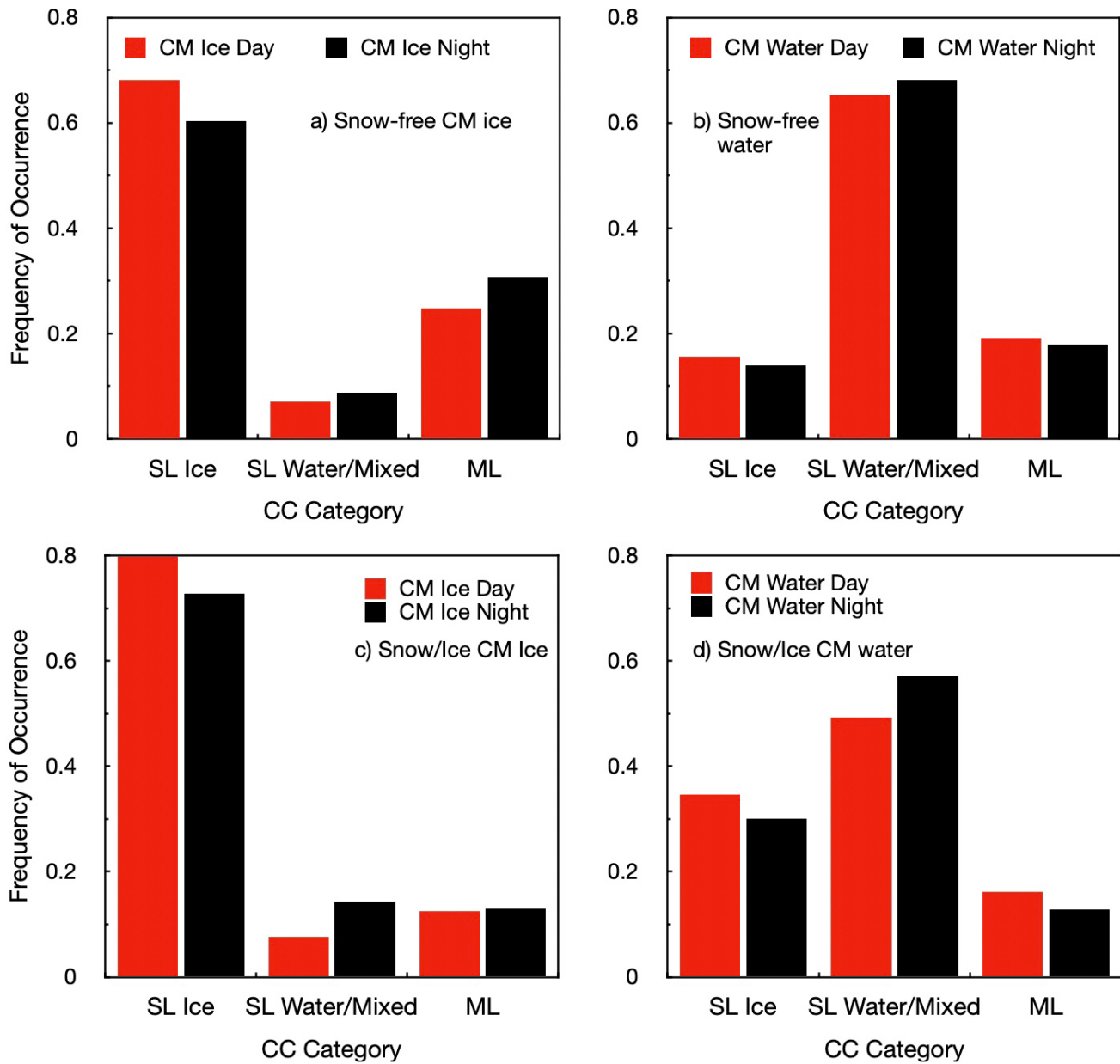
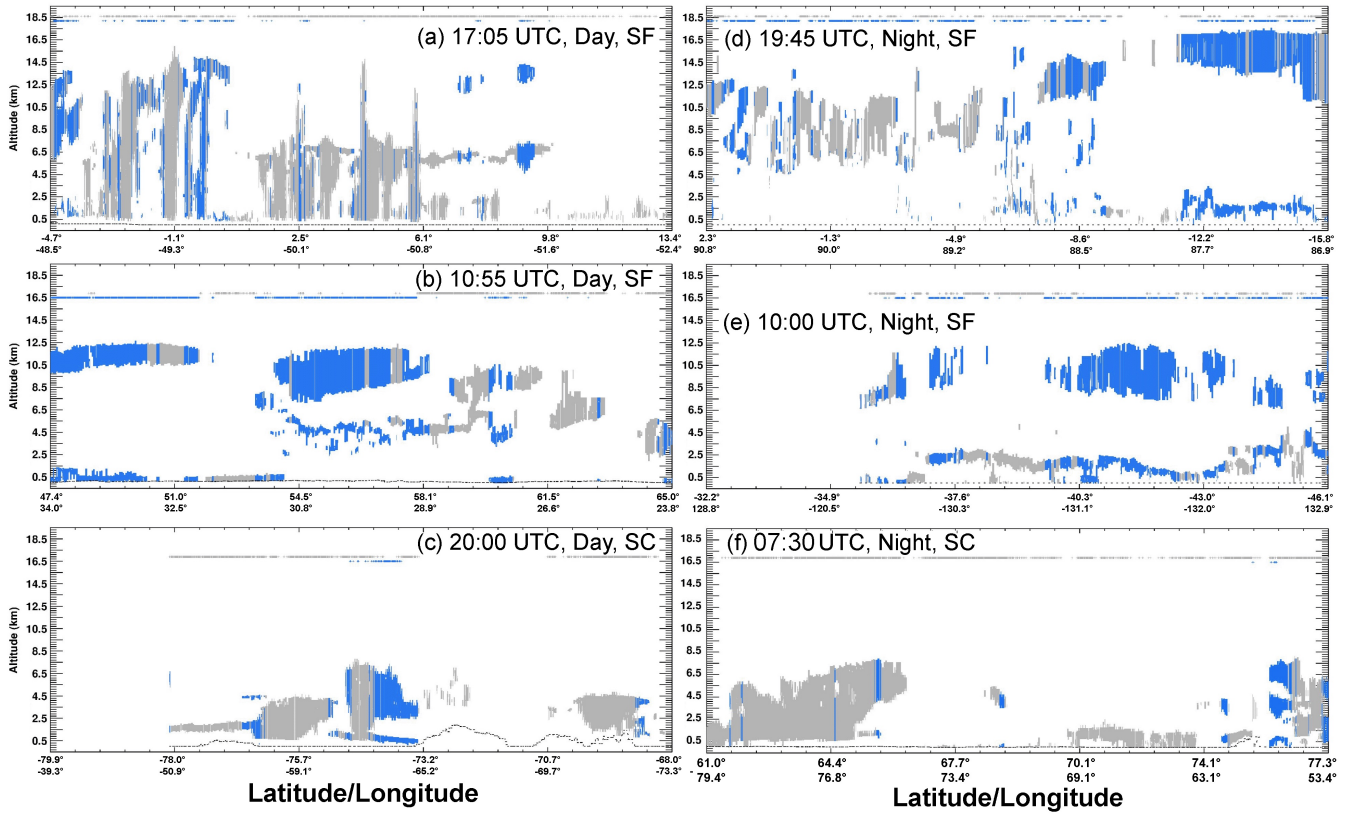


Figure 1. CALIPSO-CloudSat classification frequency of occurrence for matched 2008 CERES-MODIS cloud phase selection, ice (left) and liquid (right) for snow-free surfaces (top) and snow/ice-covered surfaces (bottom).



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Figure 2. CALIPSO-CloudSat cloud profiles from C3M for 25 December 2009 with CC ML clouds indicated in blue and CC SL denoted in gray. The MLANN ML identification for each profile is indicated as a blue dot at the top of each figure. MLANN SL clouds are indicated with a gray dot. Surface elevation is given as the dotted line at the bottom of each panel. Tropical, midlatitude, and polar cloud profiles are given in the top, middle, and bottom profiles, respectively. SF and SC indicate snow-free and snow/ice-covered surfaces, respectively.

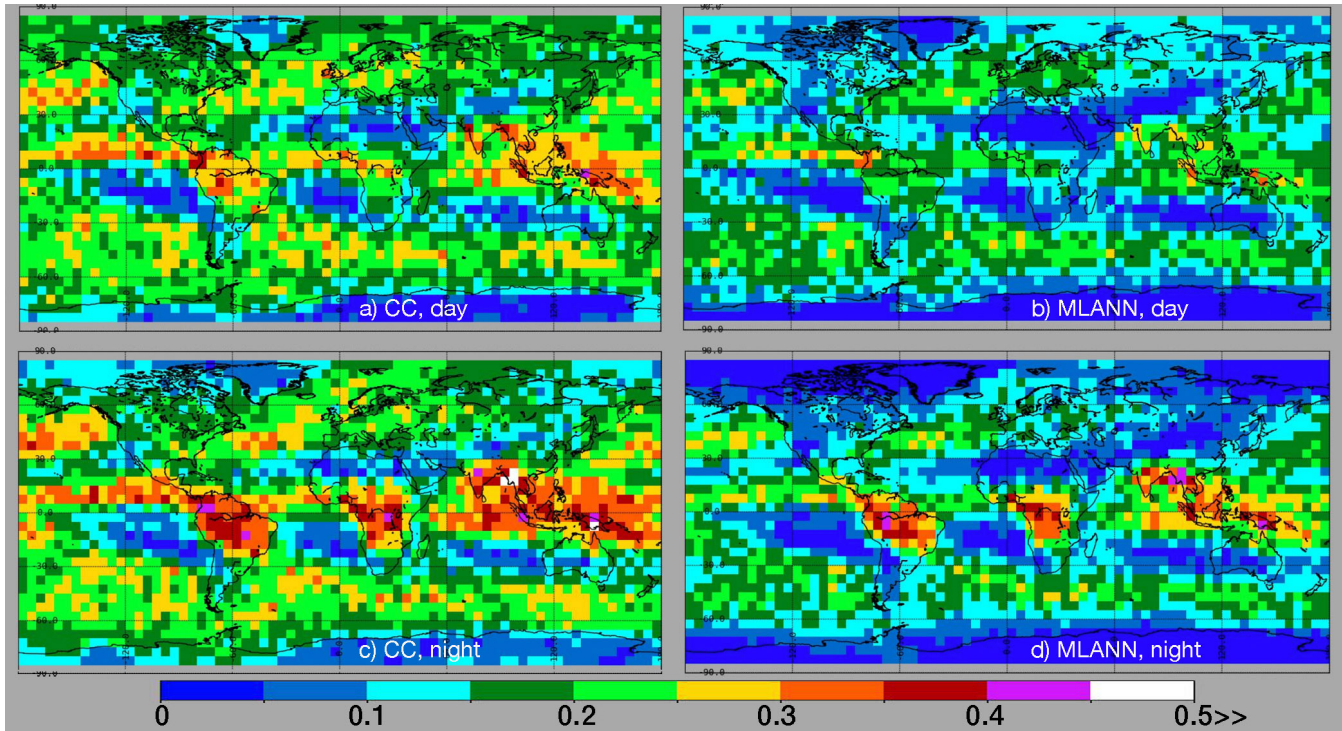
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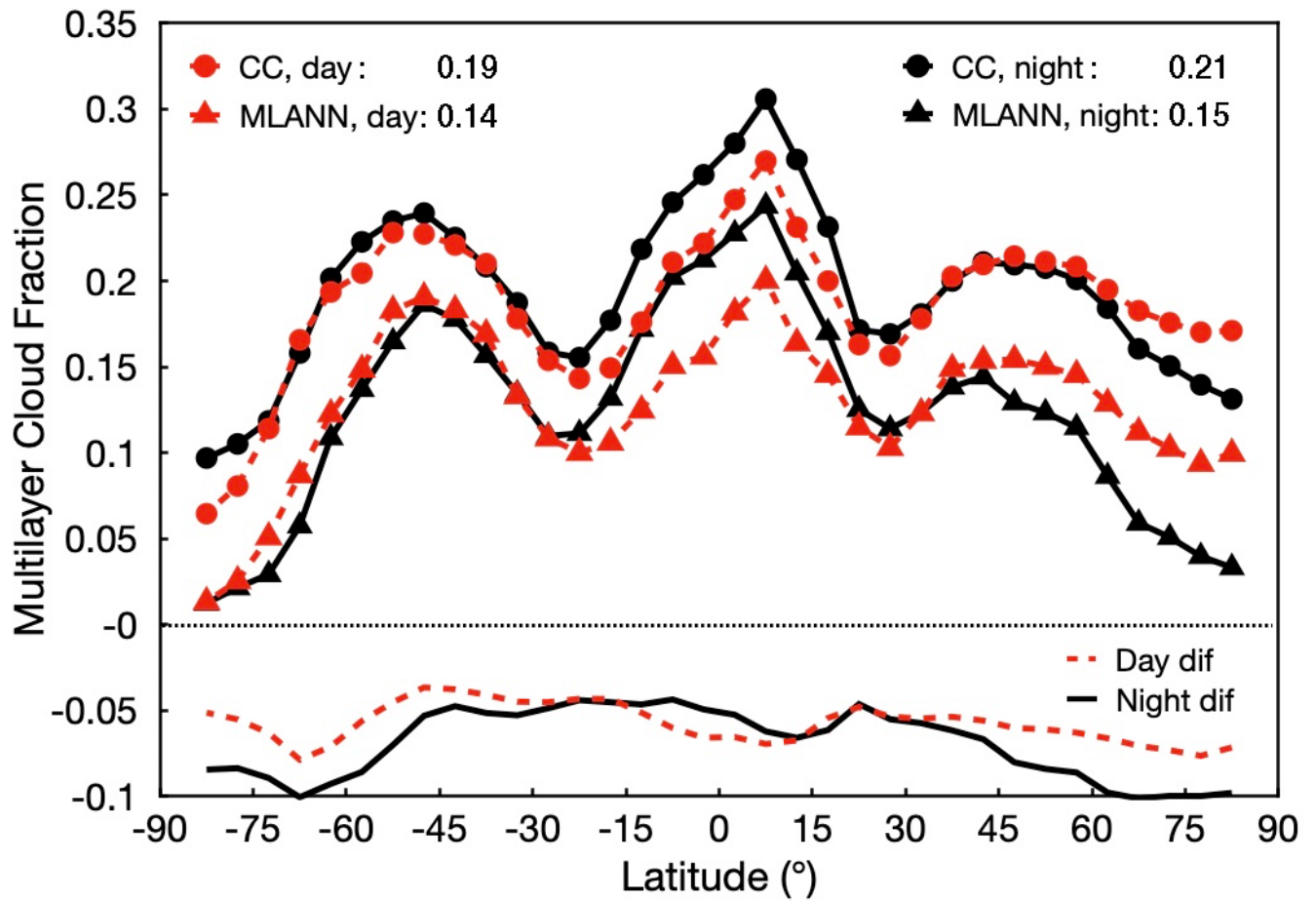
987 **Figure 3.** Fraction of matched 2009 CC and Aqua MODIS pixels classified as multilayer clouds. CALIPSO-CloudSat and Aqua
988 MODIS ML classifications on left and right, respectively. Day and night pixels on top and bottom, respectively.

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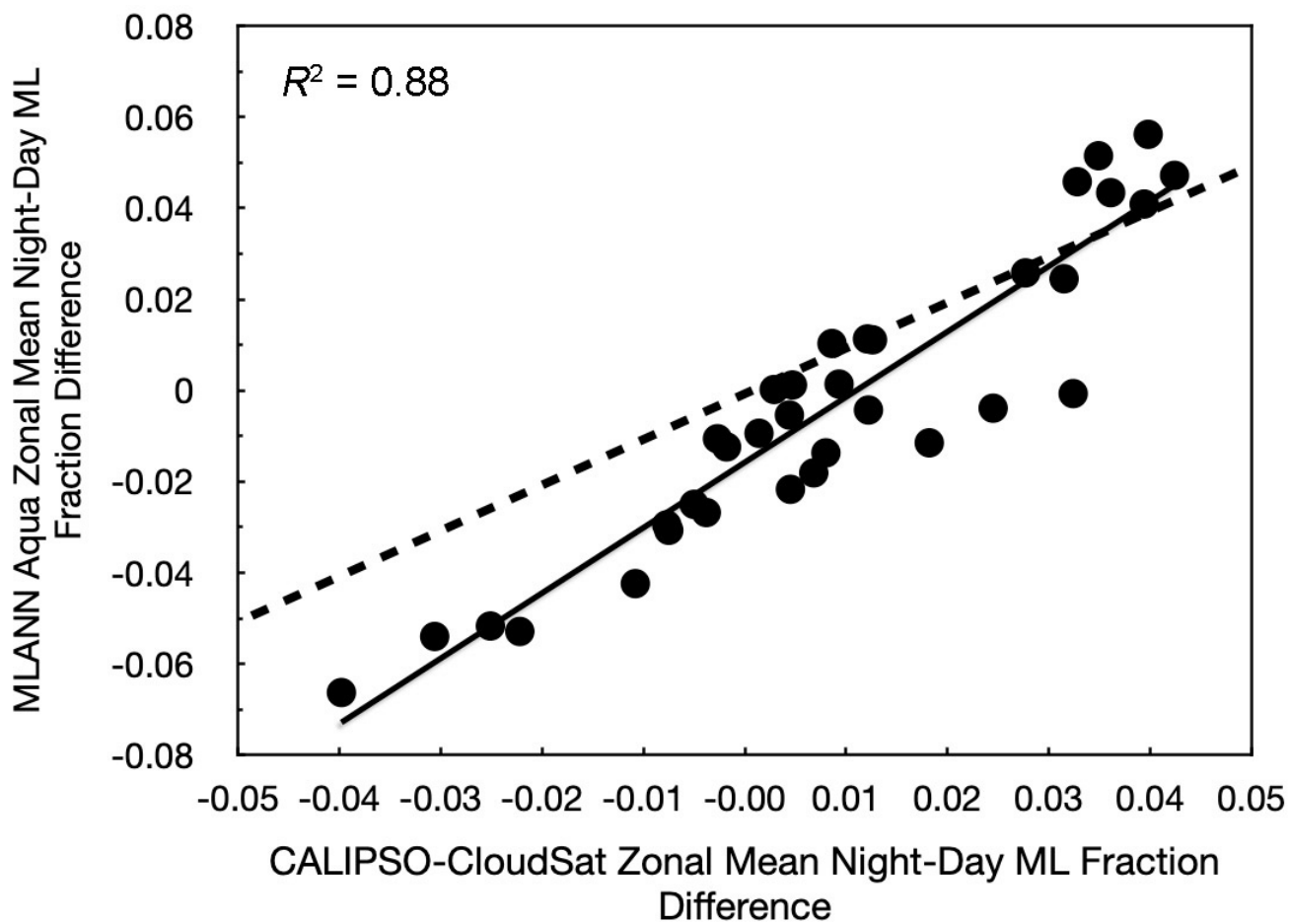
996 **Figure 4.** Zonal mean 2009 ML cloud fraction from matched CALIPSO-CloudSat and Aqua MODIS as in Fig. 4. Zonal differences,
 997 MLANN - CC, are also plotted. Global averages are indicated in the legend.

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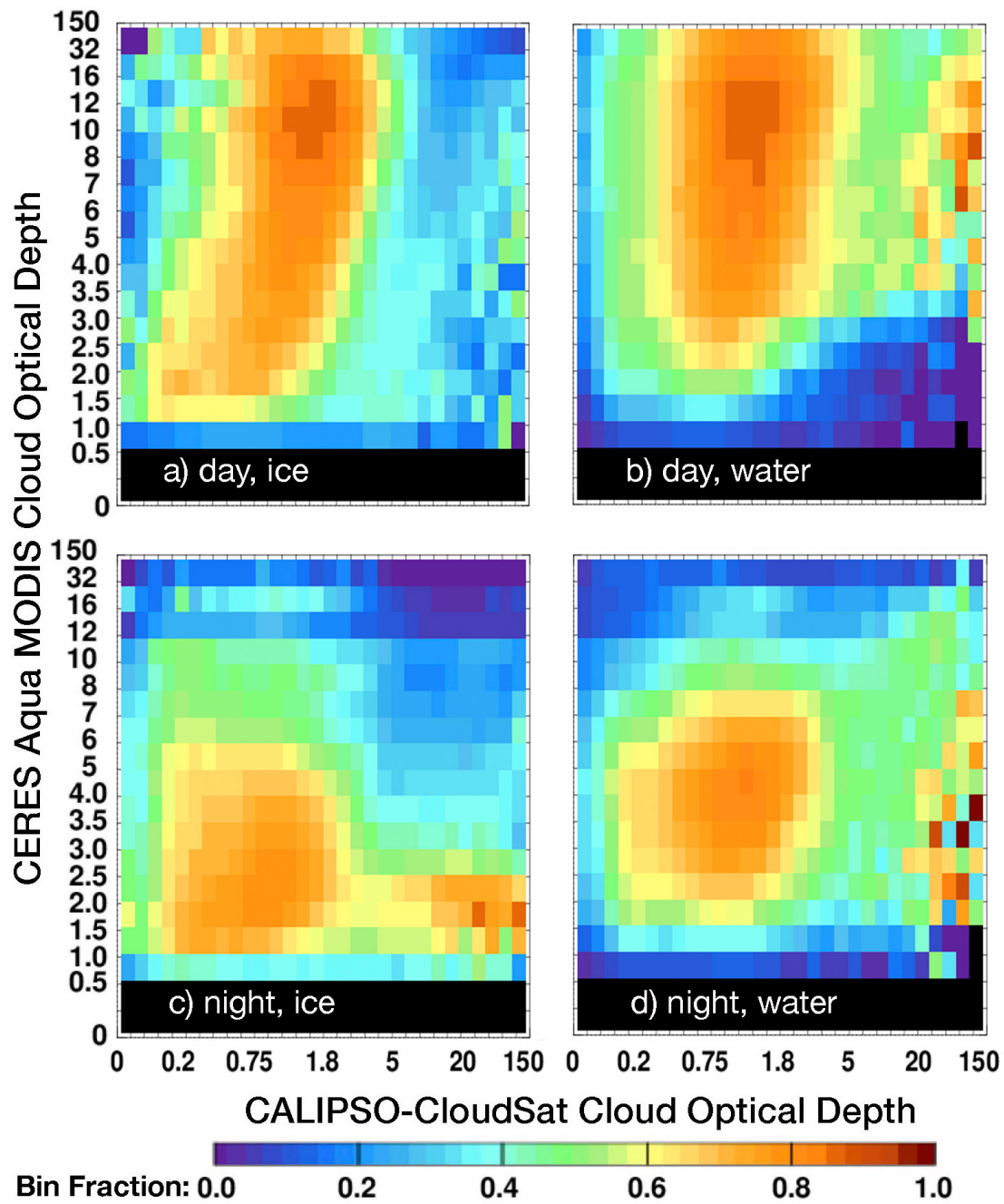
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1005 **Figure 5.** Scatterplot and correlation of MLANN and CC night-day differences in non polar zonal mean ML cloud fractions in Fig. 4.

1006 Dashed line indicates 1:1 correspondence. Solid line is linear regression fit.

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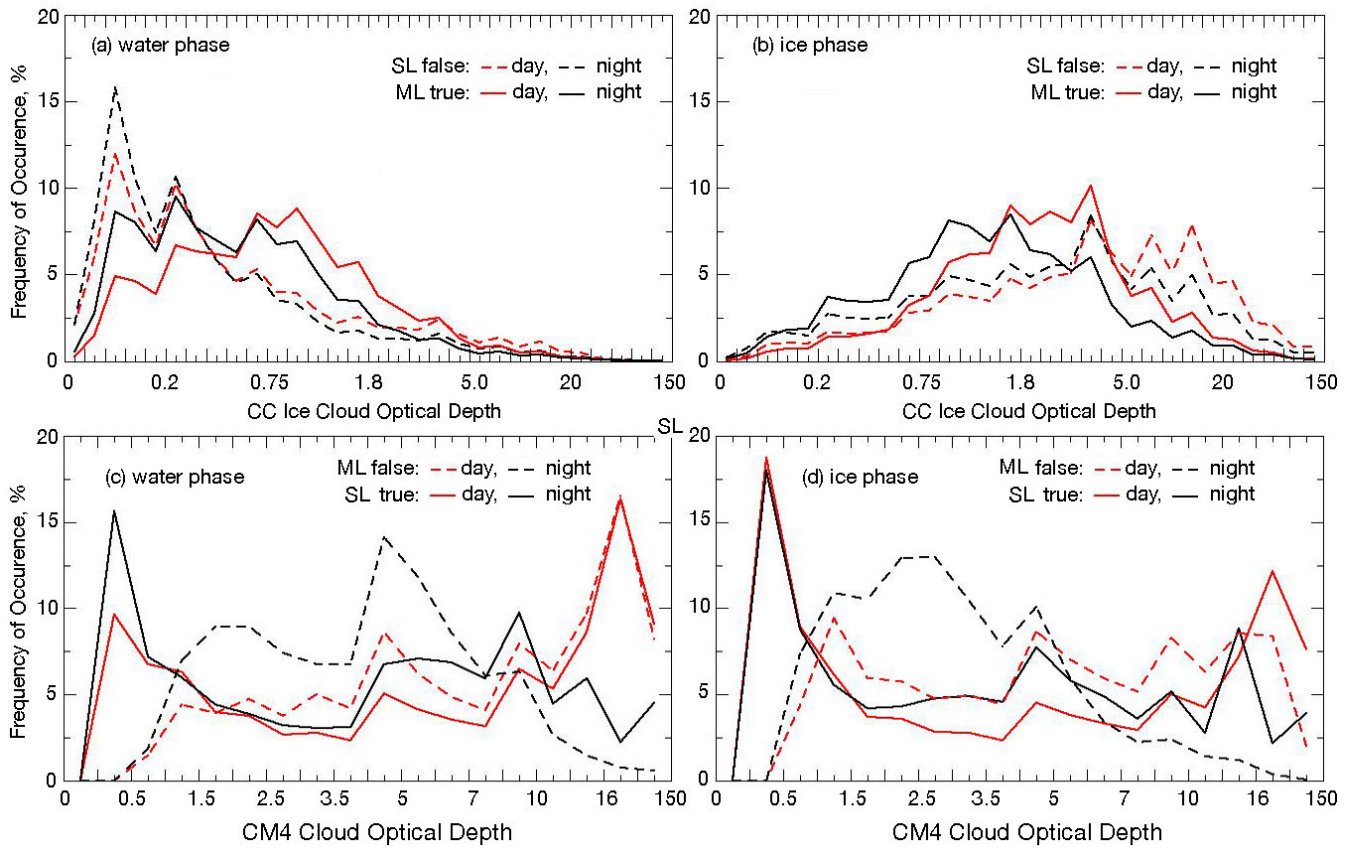


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1010 **Figure 6.** Recall or fraction of ML clouds detected within a given CC and CM cloud optical depth bin, 2009. Note, the irregular axis
1011 scales. The tick marks for the x-axis are 0, 0.0025, 0.05, 0.1, 0.15, 0.2, 0.3, 0.4, 0.5, 0.6, 0.75, 0.9, 1.1, 1.3, 1.5, 1.8, 2.1, 2.5, 3, 4,
1012 5, 6, 8, 10, 15, 20, 30, 40, 60, 80, and 150.

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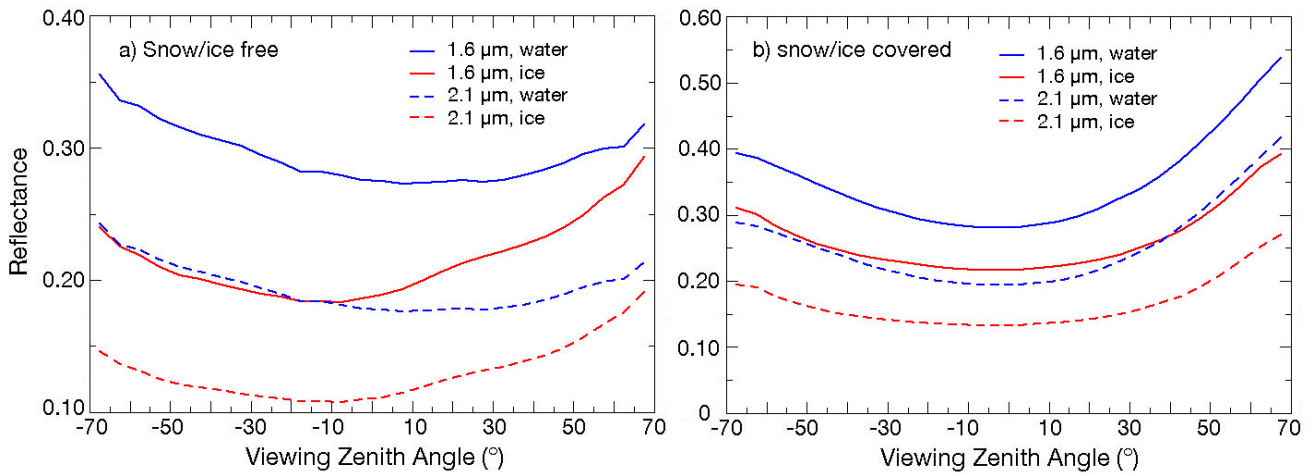
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Figure 7. Probability distributions of 2009 false SL and true ML clouds from MLANN as functions of upper-layer cloud optical depth over SF surfaces for MODIS (a) water phase and (b) ice phase. Probability distributions of 2009 false ML and true SL clouds from MLANN as functions of total column cloud optical depth over SF surfaces for MODIS (c) water phase and (d) ice phase. The major tick marks for the x-axes on the top panels are 0, 0.0025, 0.05, 0.1, 0.15, 0.2, 0.3, 0.4, 0.5, 0.6, 0.75, 0.9, 1.1, 1.3, 1.5, 1.8, 2.1, 2.5, 3, 4, 5, 6, 8, 10, 15, 20, 30, 40, 60, 80, and 150. The major tick marks for the x-axes on the bottom panels are 0, 0.025, 0.5, 1.0, 1.5, 2.0, 2.5, 3.0, 3.5, 4, 5, 6, 7, 8, 10, 12, 16, 32, and 150.

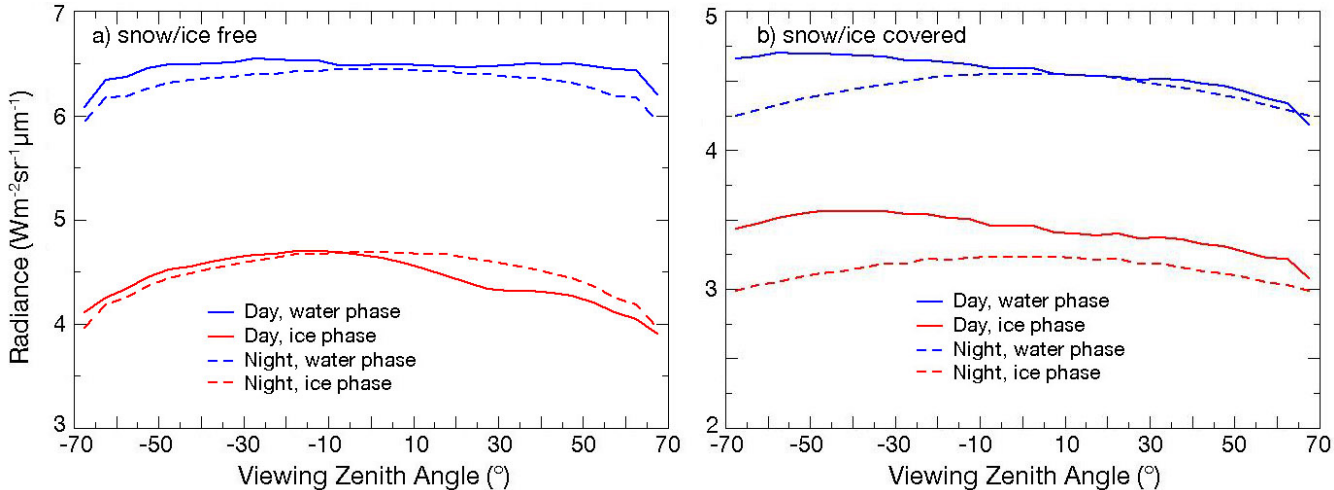
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Figure 8. Mean reflectance from Aqua MODIS as a function of VZA for CERES water and ice-phase clouds, JAJO 2019.

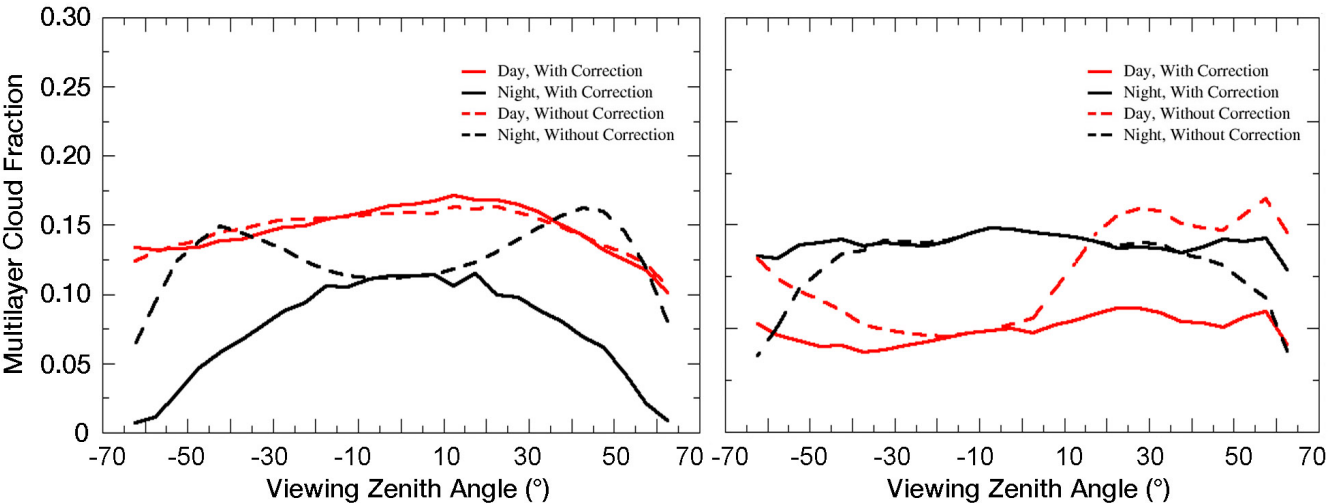
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Figure 9. Mean 10.8-μm radiance from Aqua MODIS as a function of VZA for CERES water and ice-phase clouds, JAJO 2019.

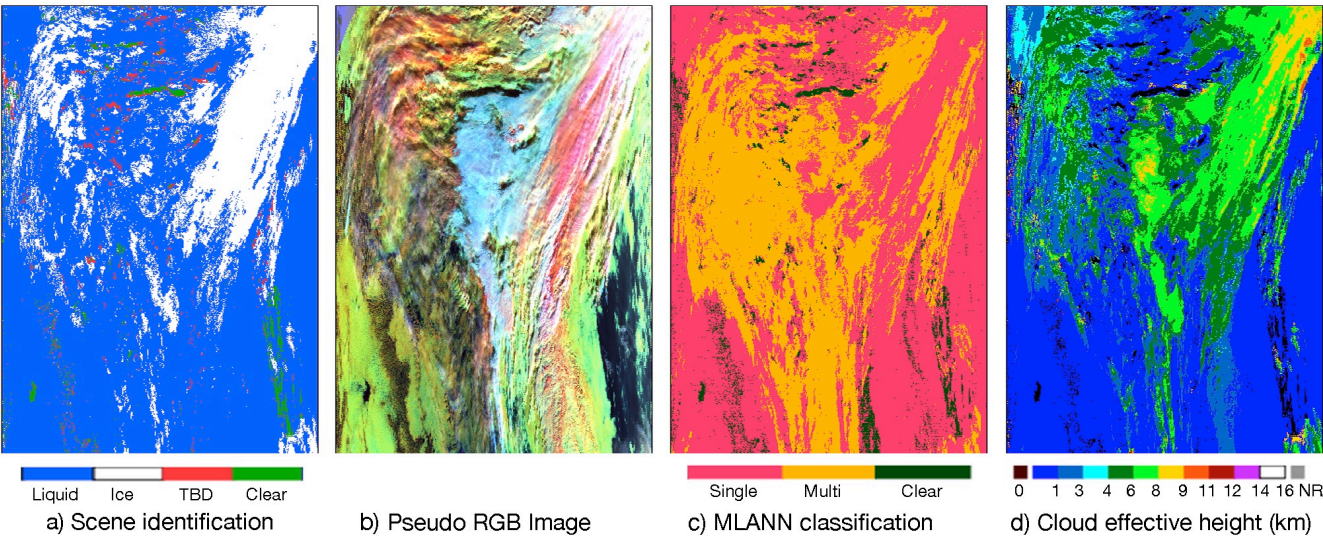
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Figure 10. Mean MLANN multilayer cloud fraction from Aqua MODIS as a function viewing zenith angle, April 2009. MLANN was run with the MODIS data as observed (without correction) and after applying a VZA correction (with correction).

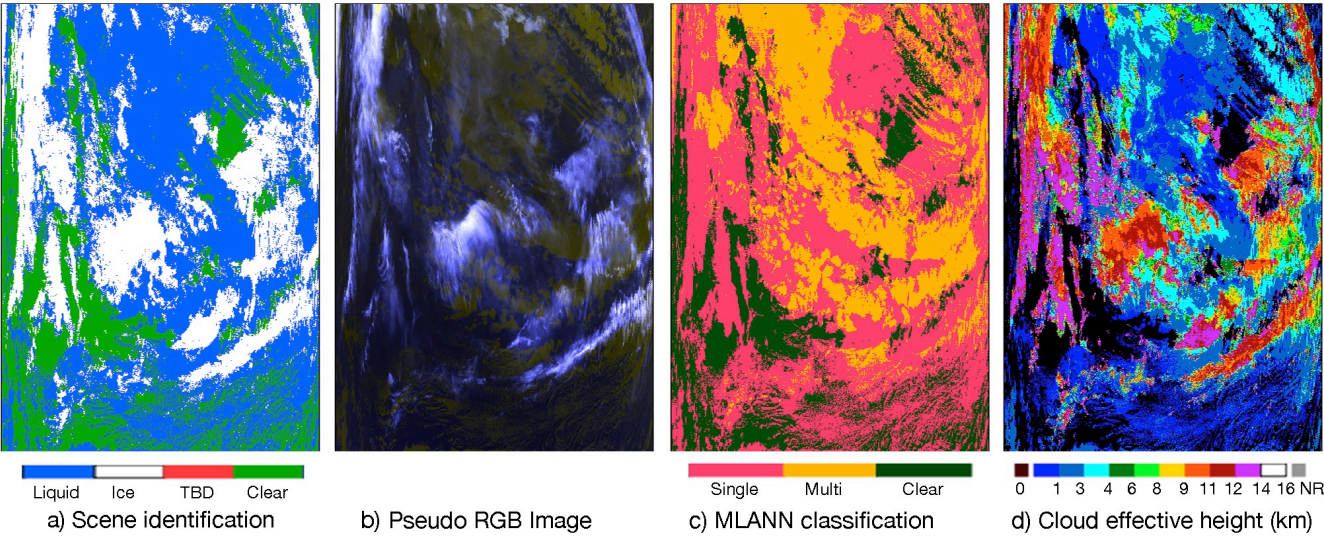
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Figure 11. Cloud parameters derived from Aqua MODIS data between 62°S (top) and 52°S (bottom) around 165°E, at ~3:50 UTC, 16 April 2019. (a) CM4 pixel scene classification, (b) Pseudocolor RGB image, red: 0.64 μm reflectance, green: BT₃₇, green; blue: reverse BT₁₁. (c) MLANN classification, and (d) CM4 cloud effective height.

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Figure 12. Cloud parameters derived from Aqua MODIS data between 42°N (top) and 24°N (bottom) around 50°W, at ~4:45 UTC, 16 April 2019. (a) CM4 pixel scene classification, (b) Pseudocolor RGB image, red: reverse BT₁₁, green: reverse BT₁₂, green; blue: BT_{D3711}. (c) MLANN classification, and (d) CM4 cloud effective height.

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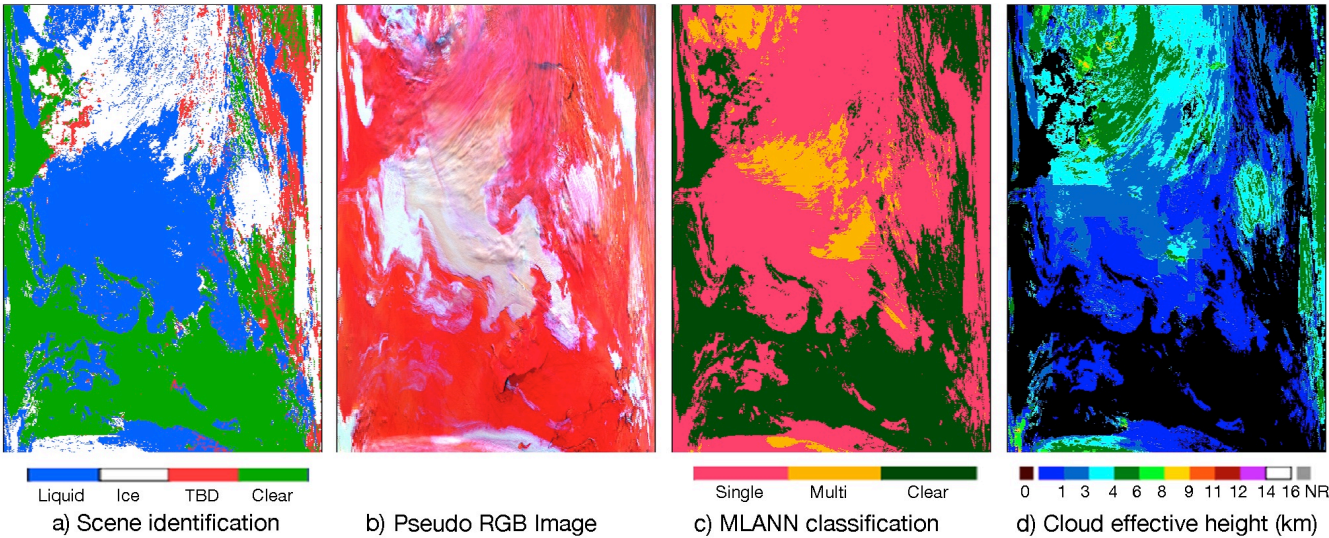
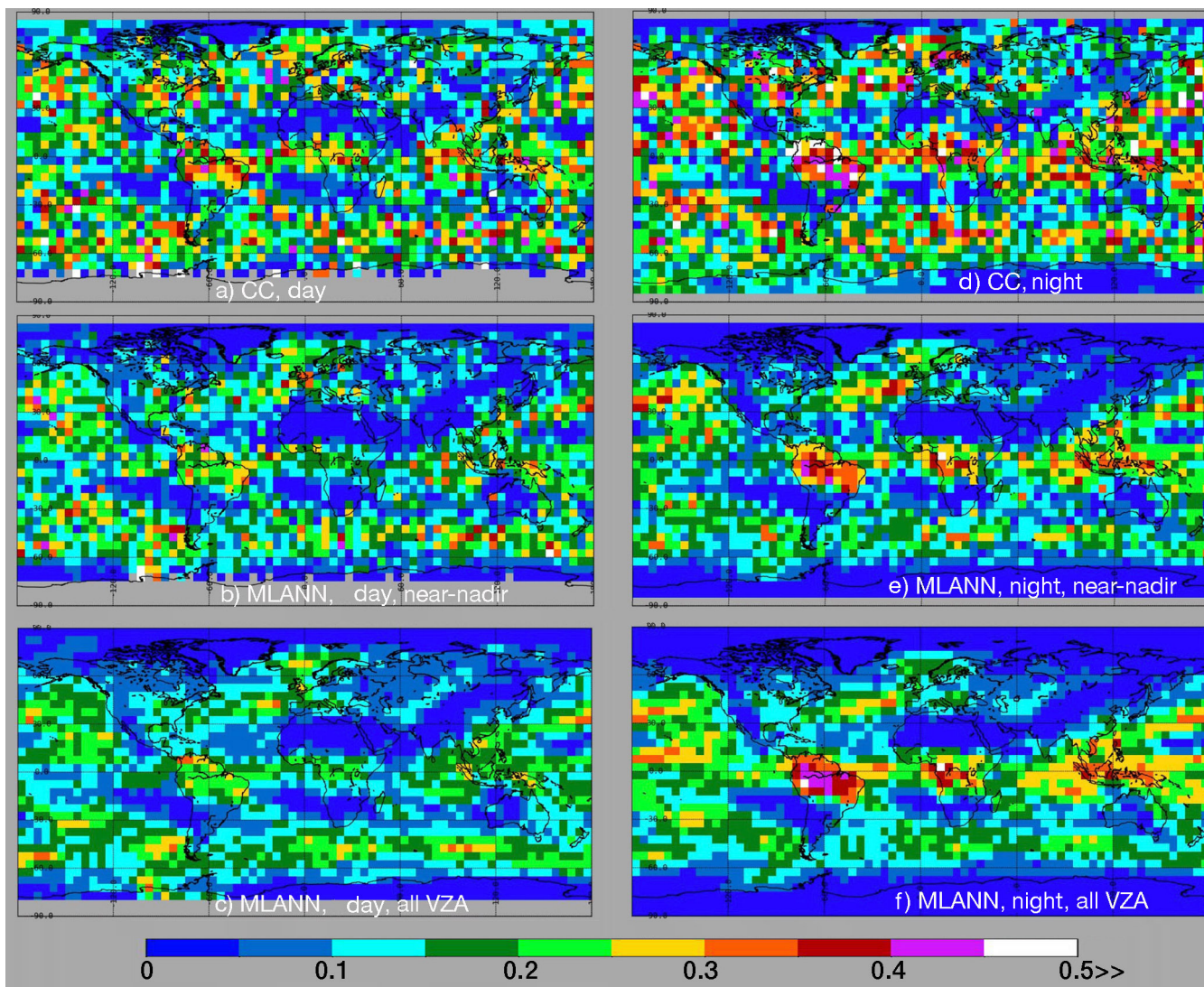


Figure 13. Cloud parameters derived from Aqua MODIS data between 77°N (top) and 83°N (bottom) around 155°E, at ~1:50 UTC, 16 April 2019. (a) CM4 pixel scene classification, (b) Pseudocolor RGB image, red: 0.64 μm reflectance, green: BT₃₇, green; blue: reverse BT₁₁. (c) MLANN classification, and (d) CM4 cloud effective height.

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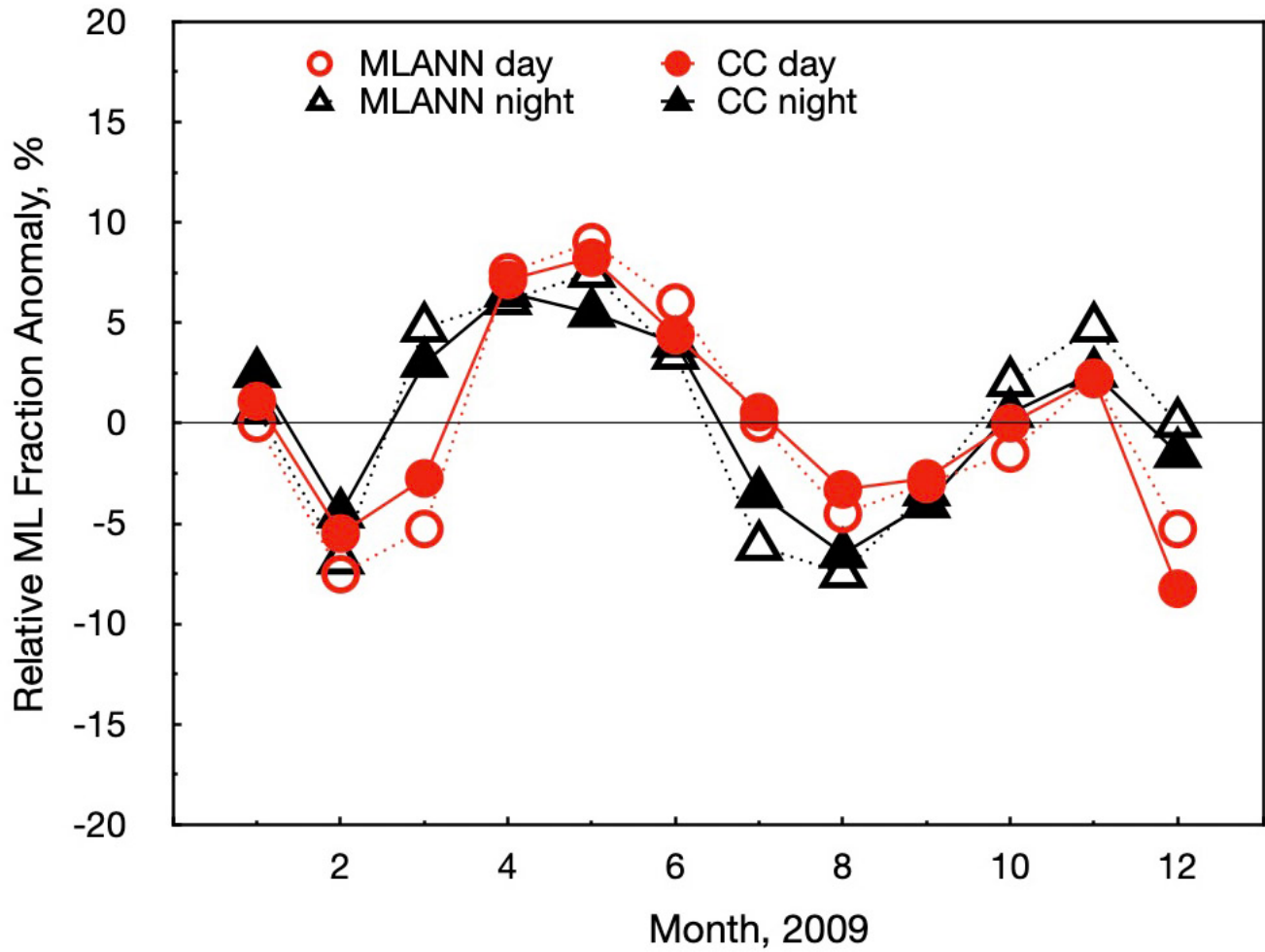
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Figure 14. Multilayer fraction of total cloud cover for JAJO 2009 using all CC data from 2009 (top), and using Aqua MODIS MLANN retrievals (middle) at near-nadir ($-18^\circ < \text{VZA} < 3^\circ$), and (bottom) for all VZAs. Daytime on left, nighttime on right.

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1081 **Figure 15.** Monthly mean anomaly of multilayer fraction relative to total cloud cover for 2009 using all CC data and full-swath
1082 MODIS data.