



1 **Particle size distributions in Earth Sciences: a review of techniques and**
2 **a new procedure to match 2D and 3D analyses**

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9 **ABSTRACT**

10 Particle size is an essential tool in many research areas spanning from Earth Sciences,
11 Engineering, Material Sciences, Soil Sciences and Pharmacology, among others. Over the
12 last decades, several techniques and methodologies have been developed to calculate
13 particle size distributions on different sample types (i.e., cohesive versus loose), spanning
14 from volumetric (3D) to image-aided (2D) analyses. Here, we (1) present a critical review of
15 most commonly used techniques to calculate particle size distributions from cohesive and
16 loose samples, and (2) we illustrate a new calculation formula to extract reliable 3D grain
17 size distributions from 2D datasets. We propose the use of the “corrected volume-weighted
18 mean diameter” (D_w), as a new particle size descriptor, which results from the summation of
19 products between equivalent particle diameter and particle volume, divided by the total
20 volume of analyzed particles. In this calculation, particles were approximated to perfect
21 circles-spheres, but a shape correction factor was applied to consider deviations from the
22 perfect spherical shape. We tested the accuracy of D_w calculation formula by analyzing 2D
23 datasets acquired from thin sections of 5 selected granular sand samples having different
24 mean grain diameters and grain size distributions (i.e., different sorting degree, grain size



25 distribution width and skewness). Grains were manually digitized, and per each thin section
26 more than 5,000 particles were acquired. Two-dimensional grain size distributions were
27 cross-checked with the results provided via laser diffraction granulometry on the same
28 samples and were compared with previously published and widely used calculation
29 methods. Our promising results encourage the usage of D_w formula as it provides best
30 matching results with 3D laser granulometry and needs basic input parameters that can be
31 easily extracted from any image analysis software.

32

33 **Keywords**

34 Particle size distribution; equivalent diameter; volume-weighted mean diameter; granular
35 materials; image analysis technique; laser diffraction granulometry.

36

37 **1. Introduction**

38 **1.1 Particle size analysis in Earth Sciences and beyond**

39 The quantification of particle size distribution is a fundamental parameter to be determined
40 in different scientific disciplines spanning from Earth and Planetary Sciences, Engineering,
41 Life Sciences, Material Sciences, Soil Sciences, and Pharmacology. Particle size is defined
42 as a scalar property of granular media and is typically calculated as the nominal diameter of
43 particles (Udden, 1914; Wentworth, 1922; Krumbein and Pettijohn, 1938; Krumbein and
44 Sloss, 1963; Pettijohn et al., 1972). Particle size is a fundamental component of the texture
45 of granular materials (sediments, rocks, and aggregates) together with particle shape
46 (Wadell, 1935; Krumbein, 1941a; Moss, 1962; Krumbein and Sloss, 1963; Barrett, 1980;
47 Mora and Kwan, 2000), rounding degree (Wadell, 1933; Powers, 1953; Taylor, 2002),



48 surface morphological features (Wentworth, 1919; Bowman et al., 2001; Russ, 1990),
49 overall fabric (particle preferred orientation) (Griffiths, 1961), and mineralogical composition
50 (Krumbein and Sloss, 1963; Folk, 1974; Boggs, 2009). In particular, in the field of Earth
51 Sciences, particle size determination plays a major role in stratigraphic and sedimentological
52 studies where it provides fundamental information related to the physical and dynamic
53 transport processes (Krumbein, 1941b; Spencer, 1952; Folk and Ward, 1957; Bull, 1962;
54 Sahu, 1964; Middleton, 1976; Goldbery and Richardson, 1989; Kranck, 1984; Pickering and
55 Hiscott, 2015), provenance and maturity of clastic sediments and rocks (Dapples et al.,
56 1953; Cadigan, 1961; Folk, 1974; Boggs, 2009; Garzanti, 2019), fluid storage potential of
57 sedimentary sequences (Fraser, 1935; Griffiths, 1952) and recognition of sedimentary
58 environments (Keller, 1945; Buller and McManus, 1973; Mutti, 1992; Selley, 2001; Nichols,
59 2009). Particle size quantification is also fundamental in structural geology studies, where
60 the correct definition of clast-grain size provides important information to constrain brittle
61 deformation mechanisms from fault rock analysis (Blenkinsop, 1991; Storti et al., 2003; Billi,
62 2005; Heilbronner and Keulen, 2006; Keulen et al., 2007; Luther et al., 2013; Montheil et al.,
63 2020), to understand the overall faulting processes (Engelder, 1974; Sibson, 1977; Marone
64 and Scholz, 1989; Doan and Gary, 2009; Sammis and Ben-Zion, 2008; Balsamo and Storti,
65 2011), and to define plastic deformation styles (Ranalli, 1984; Freeman and Ferguson, 1986;
66 Stipp and Tullis, 2003; Passchier and Trouw, 2005; Hirsch, 2008; Lopez-Sanchez and
67 Llana-Fúnez, 2016). Planetary geology employs the analysis of particle size to unravel
68 sedimentary and surficial transport processes on terrestrial planets of the Solar System (De
69 Pater and Lissauer, 2001; Faure and Mensing, 2007; Bridges and Muhs, 2012; Grotzinger
70 and Milliken, 2012), and to study meteoritic bodies (Dodd, 1976; Hughes, 1978a; Martin and
71 Mills, 1978; Eisenhour, 1996). Petrophysics takes into account the evaluation of particle size
72 to understand the primary and secondary porosity and overall fluid flow patterns and
73 magnitude through porous media (Tiab and Donaldson, 2004; Torabi and Fossen, 2009;



74 Balsamo et al., 2010). Hydrogeology studies deal with the quantification of grain size to
75 document fluid pathways in deformed and undeformed rocks and soils (Davis and DeWiest,
76 1966; Fetter, 1994; Bense et al., 2013). Particle size determination is also important in the
77 field of diagenesis, as in the case of ore-mineral deposits in conjunction with studies
78 regarding structural geology (Jébrak, 1997) or selective cementation of sedimentary
79 sequences (McBride et al., 1995; Mozley and Davis, 1996; Morad et al., 2000; Dutton et al.,
80 2002; Cavazza et al., 2009; Van Den Bril and Swennen, 2009; Balsamo et al., 2012; Pizzati
81 et al., 2018; Dimmen et al., 2020). Geomorphology employs particle size analysis to identify
82 the products of various geomorphic agents in different environments (marine, fluvial and
83 continental) (Easterbrook, 1969). Glaciology extensively implements particle size
84 determination to quantitatively describe the past and present glacial-related deposits
85 (different types of moraines, tills, and cryo-clastic materials) and to define glacier evolution
86 over time (Washburn, 1979; Molnia, 1983; Eicken, 1993; Menzies, 2000). Particle-crystal
87 size is adopted also in petrology of both intrusive and effusive igneous rocks, where it can
88 provide constraints regarding crystal growth processes occurring inside magma chambers
89 (Higgins, 1994; Means and Park, 1994; Bryon et al., 1995; Higgins, 2000; Zieg and Marsh,
90 2002; Mock and Jerram, 2005; Gualda, 2006; Morgan and Jerram, 2006; Jerram and
91 Higgins, 2007; Jerram et al., 2009). Volcanology is particularly interested in particle size
92 analysis to define the magnitude of past eruptions (Kaminski and Jaupart, 1998), to infer the
93 explosivity index (Giachetti et al., 2021) and to characterize the texture and sedimentary
94 transport mechanisms of volcanoclastic deposits (McPhie et al., 1993; Eychenne and
95 Engwell, 2022).

96 The broad list of fields of application reported above helps to understand the critical
97 importance of particle size determination as an effective tool to constrain a wide variety of
98 physical processes. The techniques employed to calculate particle size distribution span



99 from three-dimensional volumetric analysis performed on bulk materials (e.g., classical sieve
100 analysis applied to loose samples) (Udden, 1914) up to bi-dimensional automated-manual
101 image analysis (e.g., using thin section images of cohesive samples) (Heilbronner and
102 Barrett, 2014). Nowadays, laser diffraction-based techniques provide accurate, precise, and
103 relatively fast 3D particle size determination and is particularly effective in the case of loose
104 powder samples (Agrawal et al., 1991). In the field of Earth Sciences, rock samples may
105 show different degrees of cohesion, thus implying the use of different techniques in defining
106 grain size distributions. Unfortunately, the direct comparison among results from different
107 analytical procedures is not straightforward, thus limiting the ability of researchers to
108 compare data obtained in different times and from different case studies. This limitation is
109 even more important when results from 3D and 2D analyses need to be compared. The
110 reason for such discrepancy between 3D and 2D analyses lies in the type of samples
111 (Cortinovis et al., 2019), number of analyzed particles (Lopez-Sanchez, 2020), particle
112 shape and density (Matthews, 1991a), and instrumental limitations associated with the
113 resolution in the upper and lower grain size ranges (Syvitski et al., 1991a).

114 In the present contribution, we first provide a critical review of available 3D and 2D analytical
115 techniques employed for grain size calculation and related correction methods. Techniques
116 are critically revised highlighting pros, cons, weaknesses, strengths, and applicability on
117 different sample types. Then we focus on defining and testing a new conversion equation to
118 extract 3D average grain diameters from 2D granulometric distributions. To this end, we
119 calculated 2D grain size distributions of 5 selected sand samples through image analysis
120 technique from petrographic thin sections. The obtained results were corrected with
121 literature methods and with our new equation and were compared with data gained by 3D
122 laser diffraction granulometry technique, which served as reference benchmark. A shape
123 correction factor was applied to the calculated mean diameter to consider particle deviations

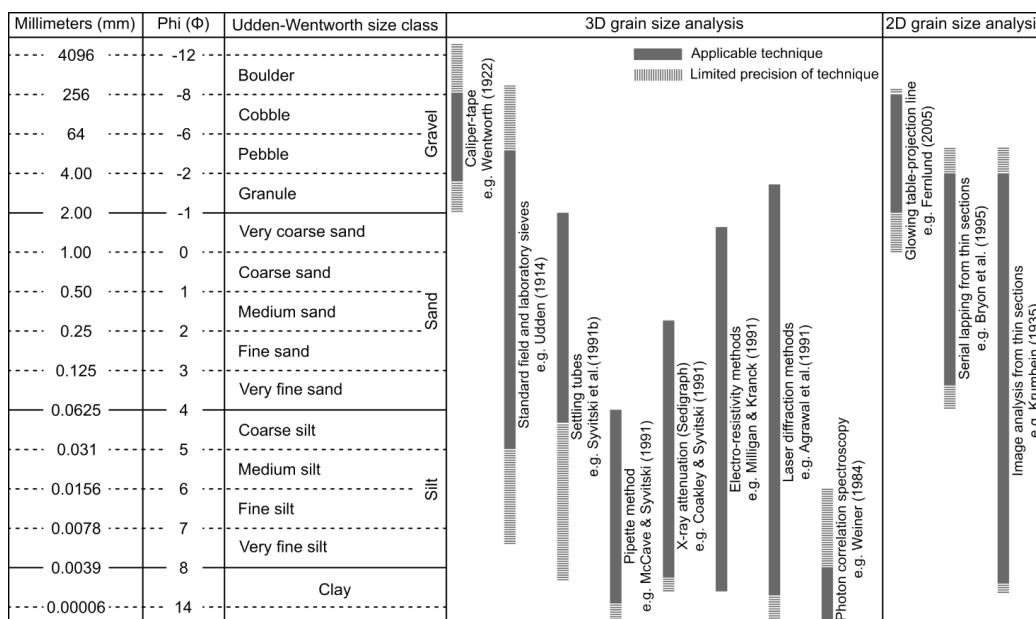


124 from the perfect circular shape. In our case, the correction factor was grounded to particle
125 shape, and it slightly varied according to the sample to be analyzed. The volume-weighted
126 mean diameter (D_w) equation provided well matching results with optical granulometry data
127 and proved to be a reliable and an easy-to-use tool to analyze samples with different particle
128 size distributions, textures, sorting degrees, and mineralogical compositions.

129

130 **1.2 Particle size distribution analysis techniques: a review**

131 Since the beginning of the last century, particle size was measured adopting the metric
132 dimensional scale (Wentworth, 1922), which then became the standard sedimentological
133 scale and it is still widely adopted nowadays (Fig. 1). However, in the following years, a
134 base-2 logarithm scale, also known as the phi-scale (Φ), was proposed (Krumbein, 1938;
135 Krumbein and Sloss, 1963). Due to the diversity of objects to be characterized, particle size
136 has historically been achieved through the adoption of several methods. The first and
137 simplest employed technique was the direct analysis of particles in the field by caliper or
138 tape measurements (Wentworth, 1922). This methodology was mainly used in the case of
139 coarse-grained materials (coarse gravels, pebbles, cobbles, and boulders), for which size
140 determination was easier, but could not be applied with the same precision to fine-grained
141 media. Sieve analysis has been, and it still is, largely adopted to quickly define the particle
142 size of loose granular media and works well in the case of coarse to medium-grained
143 samples (Udden, 1914; Rosenfeld et al., 1953; Friedman, 1962a; Van Der Plas, 1962;
144 Krumbein and Sloss, 1963; Folk, 1966). However, this method struggles in properly
145 characterizing the size of fine-grained fractions ($< 31\text{-}62.5\ \mu\text{m}$), which must be analyzed with
146 other, specifically designed, techniques (Krumbein, 1932; Singer et al., 1988; Bianchi et al.,
147 1999) (Fig. 1).



148

149 **Figure 1.** Most common techniques applied in grain size analysis with analytical upper and lower size
 150 boundaries. For a comprehensive literature background of the reported methodologies the reader is referred
 151 to the introduction section 1.2.

152 The adoption of electro-formed sieves may extend the granulometric range down to the fine
 153 silt size ($> 5 \mu\text{m}$), however this procedure is impractical and requires specifically designed
 154 sieves. Sieving allows the definition of the intermediate axis of particles, considering
 155 particles as anisotropic ellipses, defined by a major (a), intermediate (b) and a minor (c) axis,
 156 and can be used to build mass or volume distribution curves (Bush, 1951; Adams, 1977).
 157 Sieving is typically coupled with sedimentation and pipette analysis to cover the finest (clay
 158 and silt-size particles) fractions of granular samples (Syvitski et al., 1991a; Krumbein and
 159 Pettijohn, 1938; McCave and Syvitski, 1991). However, these techniques may show pitfalls
 160 in matching sieving and sedimentation-pipette results in one single granulometric curve and
 161 are also time-consuming and not suitable to analyze large sample amounts (Syvitski et al.,
 162 1991b; Beuselinck et al., 1998; Bittelli et al., 2019) (Fig. 1). For coarse-grained granular
 163 samples (sizes $> 2 \text{ mm}$), image analysis technique applied to particles or grains manually



164 dispersed on a glowing table was adopted and the projection of the particle boundaries was
165 used to reconstruct their volume and size (Fernlund, 2005). Such a technique proved to be
166 useful in the case of relatively coarse and well disaggregated samples, while it showed
167 limitations dealing with fine-grained or aggregate particles (Fig. 1). The detailed analysis of
168 particle images was implemented also in digital sieving software, coupled with statistical
169 programs (Matlab®), particularly useful to determine the size of loose medium to coarse-
170 grained materials (Kwan et al., 1999; Tafesse et al., 2012). Again, the limitations of this
171 methodology reside in the scarcely representative number of analyzed particles and in the
172 relatively tiny grain size span that can be considered (Fig. 1). In the last decades, the
173 introduction of light diffraction instruments allowed to automatically analyze samples with
174 wide grain size ranges (from clay to gravel) in a single analytical process (de Boer et al.,
175 1987; Agrawal et al., 1991; Blott et al., 2004; Sperazza et al., 2004; Bah et al., 2009). Optical
176 granulometry provides reliable and relatively quick analyses, resulting particularly indicated
177 in the case of numerous samples (Kimura et al., 2018; Brooks et al., 2022). However,
178 reliability of results may depend upon the chosen instrumental parameters, which should be
179 carefully tested to minimize sample alteration (Matthews, 1991; Konert and Vandenberghe,
180 1997; Blott and Pye, 2006; Storti and Balsamo, 2010; Schulte et al., 2016; Celia Magno et
181 al., 2018; Cortinovis et al., 2019). Moreover, sample treatment, either chemical or
182 mechanical, before the analysis must be conducted carefully to avoid incorrect or biased
183 results (Folk, 1974; McCave et al., 1986; Matthews, 1991; Maithel et al., 2019). Laser-
184 diffraction-based instruments tend to underestimate the clay fraction especially in the case
185 of particles with equivalent diameter finer than 0.1 μm (Sperazza et al., 2004; Brooks et al.,
186 2022). This issue is mainly related to the dispersion medium, and techniques adopted by
187 most of the available equipment, that are not designed to efficiently disaggregate clay-
188 dominated samples in their constitutive elementary particles (Fig. 1). Techniques relying on
189 electro-resistivity methods, such as the widely used Coulter Counter, measure particle



190 volume based on variations of electrical field induced by grains of different size dispersed in
191 an electrolyte dispersant, which are recorded as electrical pulses with different intensities
192 (Milligan and Kranck, 1991; Beuselinck et al., 1998; Roberson and Weltje, 2014). In a similar
193 way to laser granulometers, electro-resistivity-based instruments have wide applicability in
194 term of particle size but struggle in the clay range ($< 2 \mu\text{m}$) (Fig. 1). X-ray particle attenuation
195 technique (Sedigraph) uses the attenuation of incident radiation caused by sample
196 suspended in a dispersion medium to calculate the concentration of particles settling from
197 suspension (Coakley and Syvitski, 1991; Bianchi et al., 1999; Celia Magno et al., 2018). This
198 method is accurate in analyzing particles with equivalent diameter from 1 to $\sim 300 \mu\text{m}$, while
199 it provides less reliable results outside this grain size interval (McCave and Syvitski, 1991;
200 Cheetham et al., 2008) (Fig. 1). Photon correlation spectroscopy uses the fluctuations of
201 light diffraction generated by Brownian motion of particles suspended in liquid media
202 (Weiner, 1984). This technique is capable of efficiently define the size of particles with
203 equivalent diameter down to 1 nm, thus including colloids and is particularly reliable in the
204 clay size range (Fig. 1).

205 The techniques described above are particularly indicated for loose or weakly cemented
206 granular samples that can be easily disaggregated in the elementary constitutive particles.
207 Among the methods involved in particle size analysis in the case of indurated or tightly
208 cemented samples that cannot be easily disaggregated, thin sectioning coupled with
209 petrographic analysis has been the most widely used for decades (Krumbein, 1935;
210 Greenman, 1951; Packham, 1955; Friedman, 1958; Basumallick, 1964; Smith, 1966;
211 Kellerhals et al., 1975; Schäfer and Teyssen, 1987; Kennedy and Mazzullo, 1991; Francus,
212 1999; van den Berg et al., 2003) (Fig. 1). Within the thin section area particles accounted
213 for the analysis may be chosen through the grid point count technique (Chayes, 1949;
214 Friedman, 1965; Folk, 1966), the intersection line (Van Der Plas, 1962; Stauffer, 1966) or



215 via manual-automatic identification (Grassy, 1943; Mazzullo and Kennedy, 1985; Kennedy
216 and Mazzullo, 1991; Heilbronner, 2000; Ketcham, 2005; Heilbronner and Barrett, 2014).
217 This latter procedure may be aided by image analysis software (Seelos and Sirocko, 2005;
218 Schneider et al., 2012; Heilbronner and Barrett, 2014; Liu et al., 2021; Théodon et al., 2023).
219 Image analysis techniques can grant good results in a wide span of particle sizes, from few
220 mm down to the clay fraction ($\sim 1 \mu\text{m}$), provided that images allow a precise discrimination
221 of fine particles. To this end, image analysis can be performed at several scales of
222 observation spanning from optical microscopy, scanning electron microscopy (SEM) or with
223 transmission electron microscopy (TEM) according to the size of the object to be
224 characterized (Fig. 1). Following thin section cutting, the grain size is determined as the
225 apparent diameter of randomly sectioned particles, which is generally lower than the real or
226 maximum equivalent diameter, a phenomenon known as the corpuscle effect (Wicksell,
227 1925; Rosenfeld et al., 1953; Burger and Skala, 1976; Boggs, 2009; Lopez-Sanchez and
228 Llana-Fúnez, 2016). In order to gain the real and maximum diameter, particles need to be
229 cut along the equatorial diameter, a peculiar configuration that is rather uncommon in
230 sectioned materials (Krumbein and Sloss, 1963). To avoid discrepancy between
231 granulometric data gained from thin section analysis and other methodologies, several
232 correction factors and equations have been developed. Some of them rely on statistical
233 (Chayes, 1950; Burger and Skala, 1976; Kong et al., 2005), stereological (Elias, 1967; Russ,
234 1986; Sahagian and Proussevitch, 1998; Gallagher et al., 2023), or theoretical-mathematical
235 treatise (Krumbein, 1935; Sahu, 1966; Cruz-Orive, 1983), considering particles as perfect
236 spheres randomly cut along the thin section plane. Other correction methodologies apply
237 statistical autocorrelation functions (Panozzo Heilbronner, 1992), software-aided projections
238 of digitized particle outlines (Panozzo Heilbronner, 1983) or empirical correction equations
239 (Harrell and Eriksson, 1979) to compare results from image analysis with data acquired by
240 sieving. Some authors attempted to determine the real grain size distributions by sample



241 serial sectioning to reconstruct the 3D shapes of particles (Bryon et al., 1995; Cooper and
242 Hunter, 1995). Nowadays, there is no univocal correlation function linking particle size data
243 from 2D image analysis to the corresponding 3D grain size distributions acquired either by
244 sieving or light diffraction techniques, because all available conversion tools are sample or
245 method sensitive. This does not allow a direct comparison between grain size data gained
246 by different analytical techniques.

247

248 **1.3 A new parameter to match 2D and 3D particle size analyses: volume-weighted** 249 **mean diameter (D_w)**

250 The employed volume-weighted mean diameter (D_w) includes both the equivalent diameter
251 and the shape of analyzed grains. We performed the calculation of volume-weighted mean
252 diameter based on the entire grain size datasets that were extracted from each thin section.
253 The adopted formula operates a weighing of particle diameters according to the volume of
254 the equivalent spheres. Following this, a fine-grained particle influences the final average
255 diameter less than a coarse-grained one. The formula employed for the calculations is:

$$256 \quad D_w = \left(\frac{\sum_{i=0}^{i=n} d_i \cdot V_i}{\sum_{i=0}^{i=n} V_i} \right) \quad (1)$$

257 where d_i is the equivalent diameter of the circle having the same area of the traced grains,
258 V_i is the converted spherical volume of grains and i is the number of grains used in the
259 calculation. By developing the formula of spherical volume, equation 1 can be simplified as
260 follows:

$$261 \quad D_w = \left(\frac{\sum_{i=0}^{i=n} \frac{\pi}{6} d_i^4}{\sum_{i=0}^{i=n} \frac{\pi}{6} d_i^3} \right) \quad (2)$$



262 Grain shape was also implemented in the final calculation of the proposed weighted mean
263 diameter. In particular, we considered the deviation of grains from the perfect two-
264 dimensional circular shape. To this aim, we adopted the λ shape correction factor (surface
265 area correction), which can be calculated from the raw grain size datasets extracted via
266 image analysis as follows (Johnson et al., 2021):

$$267 \quad \lambda = K * \left(\frac{p_{grain}}{p_{circle}} \right) \quad (3)$$

268 where p_{grain} is the outer perimeter of the manually traced grain boundary and p_{circle} is the
269 circumference of the equivalent circle having the same area of the grain. K is a constant
270 value multiplying the perimeter ratio and can be simplified to 1 in the case of grains with
271 aspect ratio (elongation of particles) comprised between 1 and 10 (Davies et al., 2019; Song
272 et al., 2020). In calculation of λ shape correction factor we used the average values of grain
273 perimeter and equivalent circle circumference to be inserted in equation 3, considering the
274 entire grain size dataset for each thin section. Following this, we implemented the average
275 λ correction factor in equation 2 to develop the corrected volume-weighted mean diameter
276 formula as indicated below:

$$277 \quad D_w = \lambda * \left(\frac{\sum_{i=0}^{i=n} \frac{\pi}{6} * d_i^4}{\sum_{i=0}^{i=n} \frac{\pi}{6} * d_i^3} \right) \quad (4)$$

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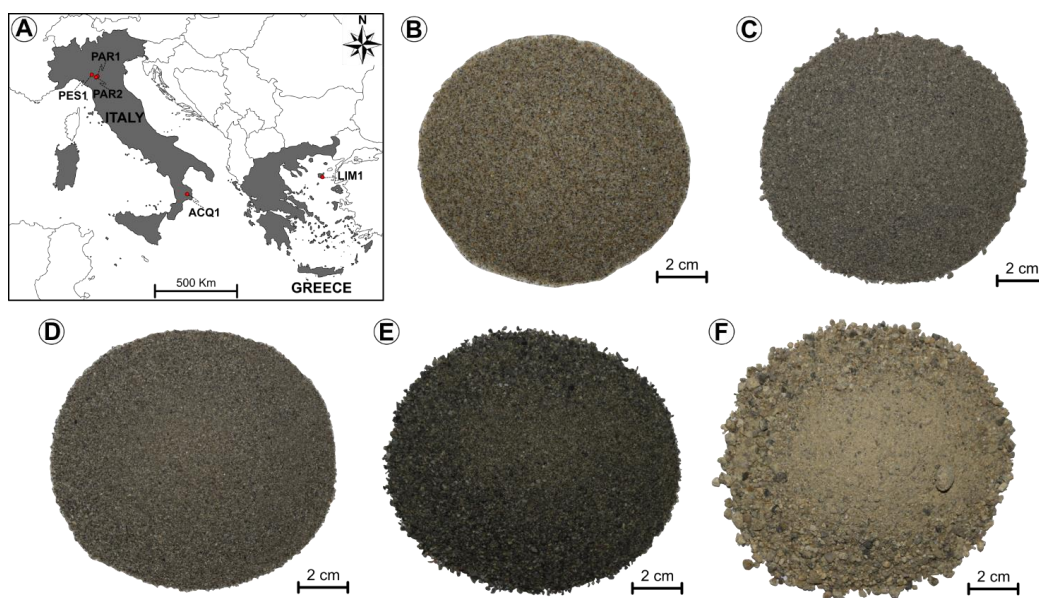
279 **4. Analytical methods**

280 **4.1 Sampled test sandy sediments**

281 We collected 5 different granular sand samples that were used as benchmarks for
282 comparative grain size determinations through thin sections and optical laser granulometer.
283 All samples were characterized by low to no cohesion and were easily collected by hand or



284 with sampling tools. About 500 g of sandy materials were collected. Sand specimens
285 belonged to different sedimentological environments spanning from continental-fluvial
286 (braided stream rivers) to shallow marine (beach and deltaic settings) (Fig. 2a).



287

288 **Figure 2.** Geographical position and pictures of collected sand samples. (a) Central and Eastern
289 Mediterranean Sea area showing the position of collected samples. (b) Sample amount LIM1 beach sand from
290 Lemnos Island, NE Greece. (c) Sample amount PAR1 from the bottom of a fluvial sand bar collected in the
291 Parma Creek, Northern Apennines. (d) Sample amount PAR2 from the top of a fluvial sand bar collected in
292 the Parma Creek, Northern Apennines. (e) Sample amount PES1 fluvial sand from the Pessola Creek,
293 Northern Apennines. (f) Sample amount ACQ1 deltaic sand from fossil fluvial-shallow marine setting from
294 Crotone Basin, Southern Apennines.

295 Sampling strategy was aimed to collect sands with different modal compositions, average
296 grain sizes and grain size distributions (different sorting degree, modal peak, curve shape
297 and asymmetry). In particular, sample LIM1 was collected in a recent foreshore swashing
298 zone along the eastern coast of Lemnos Island in the North Aegean Sea, Greece. The beach
299 sand is medium-grained, well sorted, and displays high-textural maturity with rounded to
300 subrounded grains mainly composed of quartz and lithic fragments (Fig. 2b). Three sand
301 specimens were sampled from different braided stream type, creeks, of Northern Apennines



302 in North Italy, with samples PAR1 and PAR2 representing the bottom and the top of a recent
303 fluvial sand bar along the Parma Creek, respectively. The sand bar is interfingered with
304 coarse gravel and boulder-cobble bodies. The sand samples are fine to medium-grained,
305 with moderate sorting degree, fair textural maturity with subrounded grains composed of
306 quartz, feldspar, and silt-clay aggregates (Fig. 2c and d). Conversely, PES1 sample was
307 collected at the base of a recent slope debris talus slightly reworked by stream current along
308 the Pessola Creek in the Northern Apennines. The sand exhibits medium to coarse grain
309 size, moderate to poor sorting, and low textural maturity indicated by subrounded to
310 subangular grains mainly composed of lithics and subsidiary quartz and feldspar (Fig. 2e).
311 Eventually, ACQ1 sand sample was collected from a Lower Pliocene age deltaic sandstone
312 bar from the Crotone Basin in South Italy. Although this sample belongs to a fossil siliciclastic
313 deposit, the sandstone is almost devoid of any diagenetic cements, thus allowing an easy
314 sampling. This fluvial-deltaic sandstone is coarse-grained, poorly sorted and displays low
315 textural maturity, with subangular feldspar grains dominating with respect to rock fragments
316 and quartz (Fig. 2f).

317

318 **4.2 X-ray diffraction mineralogical analysis**

319 The detailed analysis of the mineralogical composition of sampled sands was achieved
320 through X-Ray Powder Diffraction (XRPD) technique. Before the analyses, all samples were
321 dried at the controlled temperature of 35 °C for 48 hours and representative sand amounts
322 (~2 g) were manually milled in a jade mortar to attain an average grain size < 63 µm. A
323 Bruker D2 Phaser powder diffractometer with θ - θ focalizing geometry was used, operating
324 at 30 kV and 10 mA with Cu-K α ($\lambda = 1.54178 \text{ \AA}$) radiation. Data were collected in the 5-60°
325 2 θ angular range, with 0.02° step size and 1 s/step counting time. Each sample was spun
326 at 30 rpm. To identify the crystalline phases EVA software (Bruker EVA, 2018) and the



327 Crystallography Open Database (COD) were used. Semi-quantitative analysis of the
328 detected mineralogical phases was conducted using the RIR method, adding a 10 wt% high
329 purity Si standard in each sample. Through the adoption of semi-quantitative technique, the
330 identification of clay minerals through emission peak position cannot be considered
331 exhaustive. Further investigation and analysis of samples under different conditions (dry,
332 heated, and swollen) would be required for a precise clay mineral identification but such in-
333 depth analysis falls beyond the scope of the present study.

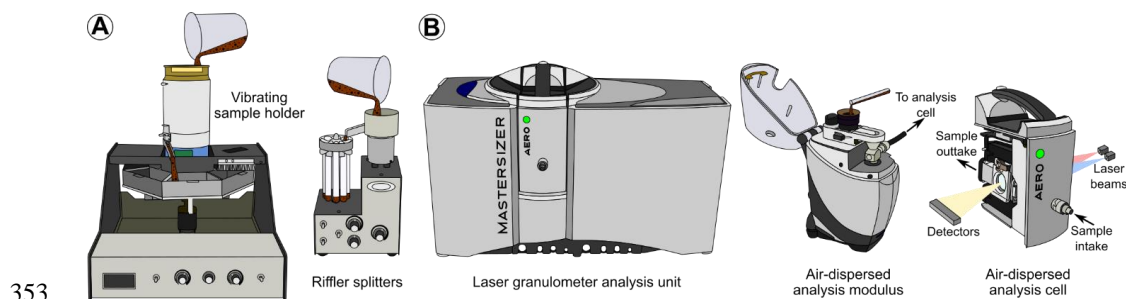
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335 **4.3 Laser-diffraction grain size analysis**

336 All granular samples were dried into an oven at the controlled temperature of 40 °C for two
337 days to remove most of the water content. After sample drying, the total amount (~500 g)
338 was sieved with a 2,000 µm mesh to remove grains with equivalent diameter coarser than
339 3,500 µm, which represents the upper instrumental limit of the laser granulometer. By doing
340 this, we slightly restricted the original grain size distribution of all samples, removing fine
341 gravel sized grains. The alteration by sieving of original grain size distribution was the same
342 for all samples. The original sample amounts were split in aliquots using Quantachrome
343 Instruments macro and micro riffers to achieve the sample mass required for grain size
344 analysis (0.8-1.3 g) (Fig. 3a). This process allowed also to create sub-samples still
345 preserving the original grain size distribution of the total starting sample amount. Grain size
346 analyses were performed with a Malvern Panalytical Mastersizer 3000 optical granulometer,
347 with operating size range spanning from 10 nm to 3,500 µm (Fig. 3b). The instrument was
348 equipped with an Aero S air-dispersed analysis unit, using pressurized air as particle
349 dispersant medium (Fig. 3b). The adoption of air as dispersant allowed to analyze samples
350 minimizing the alteration and mechanical disaggregation operated by commonly used liquid



351 dispersant media (distilled water or alcohol). For all five analyzed samples, a specific
352 standard operating procedure was set to grant the most reliable and reproducible analysis.



354 **Figure 3.** Instrumental apparatus and sample preparation used to perform laser diffraction analysis. (a) Macro
355 and micro rifflers necessary to split the initial sample amount in sub-samples suitable to be inserted in the laser
356 granulometer and to be dedicated to thin sectioning. (b) Mastersizer 3000 laser granulometer optical unit,
357 equipped with an Aero S air-dispersion modulus with the dedicated analysis cell designed to work on
358 incohesive granular media.

359 The operating procedures included several analytical-instrumental parameters to be set
360 prior to the definitive analysis. In our analyses, the granular sample quantity, laser power
361 obscuration, negative air pressure and feed rate were carefully tested (details are provided
362 in Supplementary material 1). The granulometer has two different light sources producing
363 two laser beams with red (632.8 nm) and blue (470 nm) wavelength, respectively (Fig. 3b).
364 Calculation of the equivalent grain diameter was made via a light diffraction law, employing
365 the Mie light scattering theory, which requires the refractive and adsorption indexes of
366 particles. Our granular materials are multi-dispersed (particles with different size and shape)
367 mixtures of several mineralogical phases including quartz, K-feldspar, plagioclase, mica,
368 and rock fragments in different proportions. Nevertheless, we adopted the optical
369 parameters of crystalline quartz, which is the most abundant mineral phase, with diffraction
370 index of 1.54 and adsorption index of 0.1. This simplification was needed because the
371 granulometer is not designed to work on complex polymineralic assemblages. Particle
372 volume was back-calculated from light diffraction scattering distribution and, under the



373 assumption of perfect spherical objects, the equivalent diameter was calculated. Optical
374 diffraction is operated differently according to grain size, with fine particles producing wide
375 light scattering angles, while coarse grains induce low angles (Brooks et al., 2022). The
376 laser granulometer performs the calculation of equivalent grain diameter adopting the
377 method of moments as indicated in the generic formula below:

$$378 \quad D[m, n] = \left(\frac{\sum_{i=0}^{i=n} V_i * d_i^{m-3}}{\sum_{i=0}^{i=n} V_i * d_i^{n-3}} \right)^{\frac{1}{m-n}} \quad (5)$$

379 in which V_i stands for particle volumetric density in size class d_i (median value of grain size
380 class), while m and n are the exponents to be substituted with different indexes according
381 to the adopted method of moments. In our case, the granulometer calculates the volume-
382 weighted mean diameter (De Broucker mean diameter or D[4:3]), adopting as indexes m
383 and n in equation 5, 4 and 3, respectively. The granulometer also provides the span, or the
384 width of the grain size distribution curves calculated at half height of modal peak, according
385 to the formula:

$$386 \quad Span = \frac{d(x,0.9) - d(x,0.1)}{d(x,0.5)} \quad (6)$$

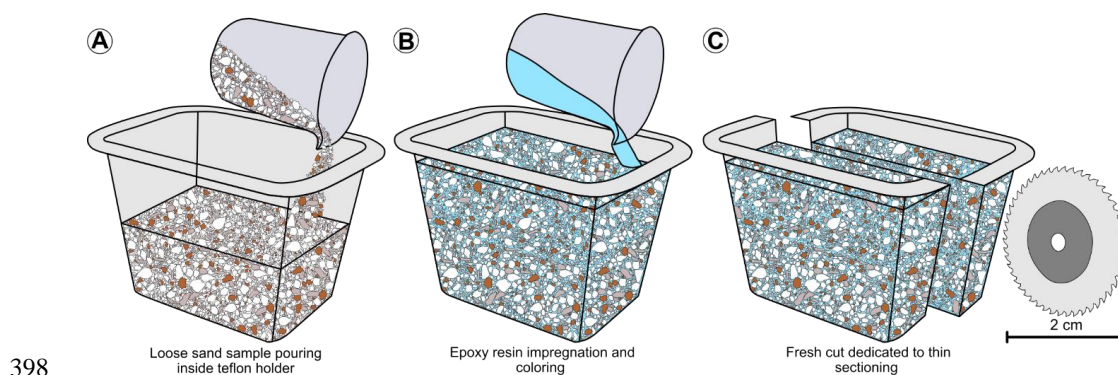
387 where, d is the equivalent particle diameter value at 0.1, 0.5 and 0.9 thresholds of the grain
388 size distribution, and x can be substituted according to the distribution type adopted during
389 the analysis (number or volume of particles). Optical granulometric analyses were replicated
390 on 5 aliquots of each sample. Grain size distribution curves were averaged to obtain mean
391 grain diameters and related parameters with associated standard deviations.

392

393 4.4 Thin sectioning technique of loose sand samples



394 Petrographic thin sections having thickness of 30 μm were made from granular sand
395 samples. To prevent any preferential grain orientation and to preserve the original grain size
396 distribution, all samples were split with macro and micro riffers, and several aliquots were
397 added into Teflon containers (Fig. 4a).



399 **Figure 4.** Sample preparation before thin sectioning. (a) Sample pouring inside Teflon holder after being split
400 in representative sub-samples with vibrating riffers. (b) Granular sample impregnation with a mixture of
401 Araldite resin and Prochima Pentasol blue dye. (c) Precise saw-cutting along the vertical direction, with thin
402 section made along the fresh cut.

403 Typically, 20-28 g of loose sand were used to fill 4 × 3 × 2.5 cm Teflon sample holders, with
404 mass variations due to different sample density and grain size. Loose sand samples were
405 impregnated with a mixture of Araldite BY156 epoxy resin and Aradur 21 resin hardener
406 (resin-hardener mass proportion of 100:28), which was diluted to 10% of total volume with
407 ethyl acetate to grant lower viscosity. The mix was colored by adding a Prochima Pentasol
408 (UN) blue dye with a mass equal to 6% of the Araldite resin (Fig. 4b). The coloring provided
409 a uniform light blue background which helped in identifying grains and tracing grain
410 boundaries. Indurated samples were cut vertically, and the fresh cut was used to create
411 petrographic thin sections (Fig. 4c). Thin rock slices were glued onto transparent glass
412 adopting an Epoteck 301 epoxy resin mixed with Aradur 21 hardener (resin-hardener mass
413 proportion of 20:5). Eventually, thin sections were manually polished with polycrystalline



414 synthetic diamond powder, having a grain size of 1 μm , above a Tanganyika soft wooden
415 surface. The polishing procedure was needed to precisely identify grain mineralogy, to
416 detect grain outer boundaries and to increase the overall thin section transparency and
417 quality.

418

419 **4.5 Sand sample modal composition**

420 The definition of the modal composition of sand samples was obtained by means of
421 petrographic analysis, with recognition of the principal mineralogical phases (quartz,
422 feldspar, and lithic fragments) in thin section. Quantification of areal percentage of minerals
423 was done on high resolution photomicrographs acquired with a Zeiss Axioplan 2
424 petrographic microscope, equipped with a Leica MC 170 HD high sensitivity camera.
425 Photomicrographs were acquired at 12.5 \times magnifications (picture area of 4,747 \times 3,560 μm)
426 both under plane and cross polarized light, to ease mineral identification. A total of 5
427 dedicated photomicrographs were taken and analyzed for each sample. Sand samples were
428 classified adopting the standard Q-F-L ternary classification diagram used for sandstones
429 (Folk, 1974).

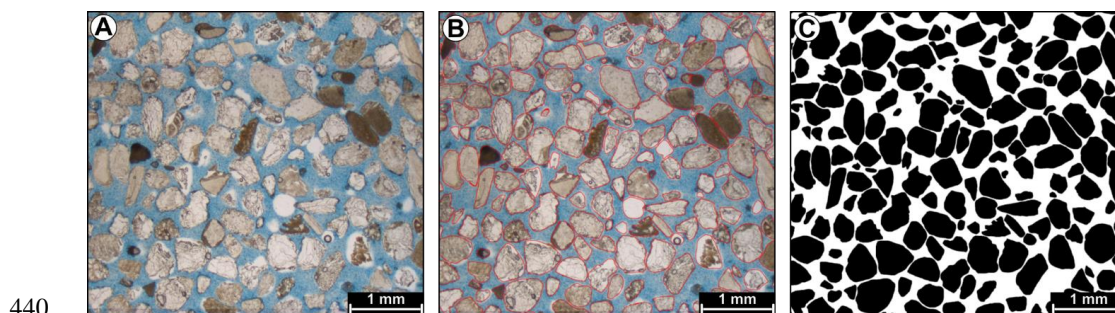
430

431 **4.6 Particle size analysis through 2D image analysis**

432 The analysis of grain size via image analysis on thin section was performed on petrographic
433 photomicrographs acquired with the standard microscope setting described above. For each
434 thin section, 48 to 64 photomicrographs were taken at 12.5 \times magnifications (picture area of
435 4,747 \times 3,560 μm) under plane polarized light to cover the entire thin section area and were
436 stitched together to form photomosaics. Photomosaics were imported and calibrated in

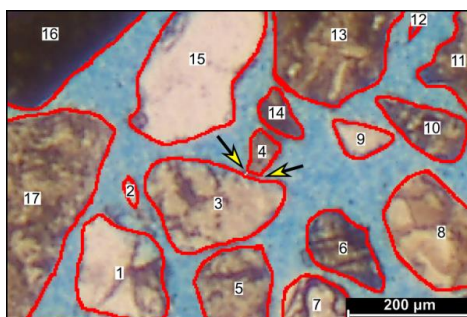


437 ImageJ image analysis, open-source software (Schneider et al., 2012). Little processing was
438 required to enhance image quality mainly through brightness-contrast adjustments and
439 noise-outlier pixel removal (Fig. 5a).



441 **Figure 5.** Image analysis technique adopted to obtain 2D particle size distribution from the selected samples.
442 (a) Original photomicrograph acquired at 12.5x magnification, composing the analyzed photo-mosaics. (b)
443 Results of manually traced particle outer boundaries. (c) Transformed binary (black and white)
444 photomicrograph used to extract particle equivalent diameter.

445 Grains were traced on modified photomosaics with ImageJ manual tracing tool, having care
446 to keep a constant 2-pixel width of the traced boundaries (Fig. 5b). After digitization, grains
447 were identified by the software with color thresholding technique applied to red grain
448 boundaries and photomosaics were converted to binary images (black grains on white
449 background) (Fig. 5c). Special attention was paid in drawing grain boundaries, to avoid
450 grains in contact with each other. In the case of touching grains, instead of operating image
451 segmentation, we preferred double-checking the results to find errors and mistakes during
452 tracing, that were corrected by manual separation of grains adding different color pixels (Fig.
453 6).



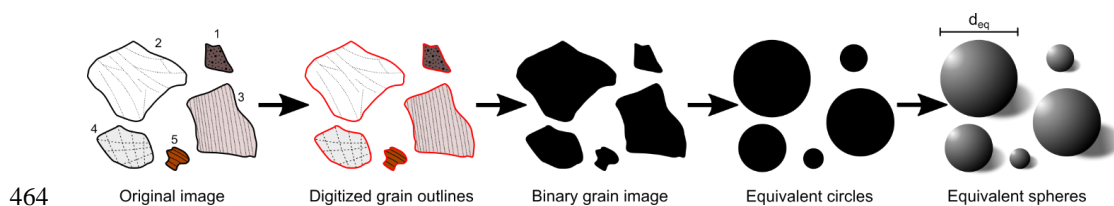
454

455 **Figure 6.** Double-checking of grains in contact with each other. Final digitized photo-mosaics quality check to
 456 identify tangent grains which were manually segmented by adding pixels with different color from the red
 457 particle outline (yellow arrows).

458 After image correction, grain size-shape data were extracted. For grain size, we extracted
 459 the area fraction in μm^2 of grains which were approximated to perfect circles, and the
 460 equivalent diameters were calculated from the inverse formula of the circle's area (Fig. 7):

461
$$d_{eq} = 2 * \sqrt{\frac{A}{\pi}}$$
 (7)

462 where d_{eq} is the equivalent diameter of the circle having the same area of the particle and A
 463 is the real area of the particle measured with image analysis.



465 **Figure 7.** Sequence of progressive steps to perform manual image analysis and to extract particle equivalent
 466 circles and spheres. d_{eq} , equivalent particle diameter.

467 Values extracted from this formula composed the basis of the proposed volume-weighted
 468 mean diameter. A total of 133,372 grains were considered and typically more than 5,000
 469 grains were used in each thin section. Large datasets allowed to tune the volume-weighted
 470 calculation formula and to minimize the effect of random grain sectioning (Krumbein, 1935;



471 Friedman, 1958; Kellerhals et al., 1975; Kong et al., 2005). Grain size distributions were
472 created from the conversion of particle number into volume density percentage associated
473 with each grain size bin. Conversion was made considering the total volume of spherical-
474 shape grains divided according to the instrumental grain size classes adopted by the laser
475 granulometer. By doing this, we kept the same boundary and instrumental conditions for
476 both grain size data acquired through laser granulometry and image analysis, facilitating the
477 comparison.

478 Regarding grain shape, aspect ratio (AR) was calculated and used to describe the deviation
479 of grains with respect to the perfect circle. Aspect ratio was obtained by the formula:

$$480 \quad AR = \frac{Major \ axis}{Minor \ axis} \quad (8)$$

481 where *Major axis* indicates the longest axis of the particle best fit ellipse (segment
482 connecting the two farthest points along the grain perimeter) and *Minor axis* stands for the
483 shortest axis of the best fit ellipse (segment having as tips the two closest points along the
484 grain perimeter).

485

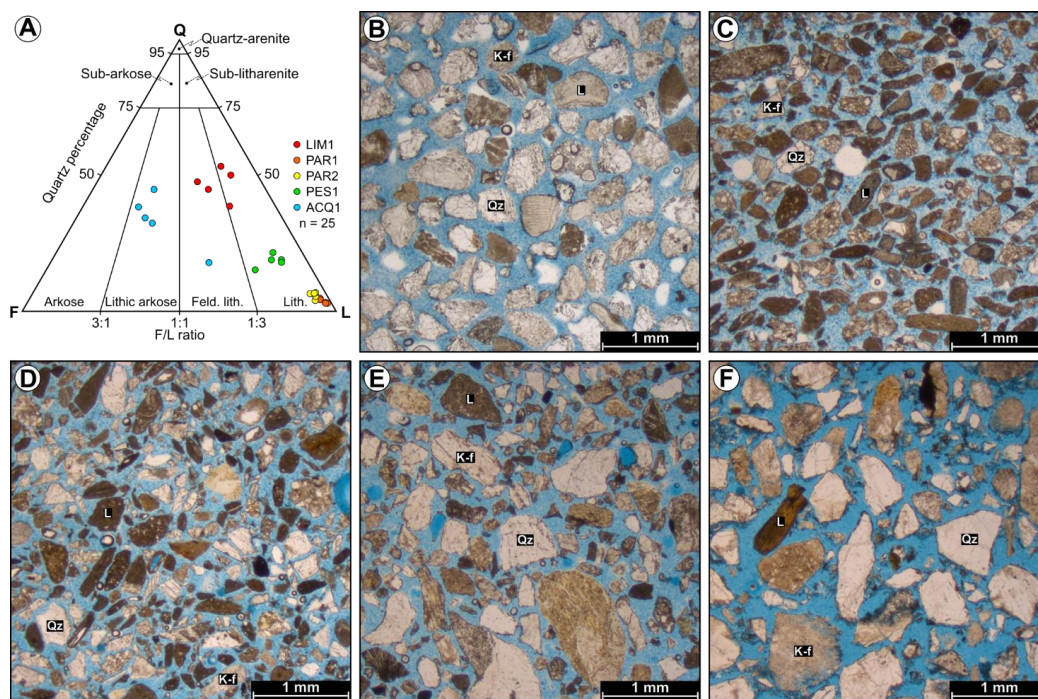
486 **5. Main results**

487 **5.1 Petrographic-mineralogical sample description**

488 Micro-textural and modal analyses performed on the foreshore beach sand sample (LIM1),
489 point out a mineralogical composition made of almost equal proportions of quartz (38.81-
490 53.32%) and lithic fragments (32.05-46.8%), while feldspar and plagioclase are subordinate
491 (8.37-20.17%) (Fig. 8a and b). Lithic fragments are mainly composed of calcite-aragonite
492 bioclasts, peloids, and to a lesser extent of metamorphic and igneous rock fragments. This
493 sample plots between the feldspathic litharenite and litharenite compositional fields in the



494 Q-F-L classification diagram (Fig. 8a). Grains are rounded to subrounded, with quartz being
495 more equant than feldspar and lithics which appear more elongate. Sorting degree is high
496 with grains of different mineral composition showing similar overall size.



497

498 **Figure 8.** Micro-textural characteristics and mineralogical composition of the collected sand samples. (a)
499 Ternary Quartz-Feldspar-Lithics modal classification diagram reporting the composition of studied sands (Folk,
500 1974). Sand composition was calculated from 5 photomicrographs per each sample. (b) Rounded to
501 subrounded siliciclastic and biogenic particles composing LIM1 beach sand sample. (c) Subrounded and
502 elongate lithic-dominated grains of PAR1 fluvial sample. (d) Subrounded lithic-dominated particles with lesser
503 extents of quartz and feldspar composing PAR2 fluvial sample. (e) Subangular and poorly sorted fluvial sand
504 of PES1 sample. (f) Angular to subangular, poorly sorted fluvial-deltaic sand composing ACQ1 sample. Q,
505 quartz; K-f, feldspar; L, lithic fragment; n, number of used photomicrographs.

506 Sand sample collected along the base of a fluvial bar (PAR1), displays a completely different
507 mineral assemblage compared to the latter beach sand. In particular, the modal analysis
508 returns a high lithic percentage (92.75-95.74%), while quartz (3-4.51%) and feldspar (1.25-
509 2.86%) compose the remaining areal amounts of the sample (Fig. 8a, c). Lithics have a



510 sedimentary origin with silt-clay aggregates incorporating fine-grained quartz and feldspar
511 particles to produce coarse-grained aggregates. The fine-grained matrix of aggregates is
512 dominantly composed of muscovite and chlorite-group minerals, as confirmed by XRD
513 analysis. Metamorphic and igneous fragments are present as subordinate mineral
514 components. Due to the high lithic content, PAR1 sample can be inserted in the litharenite
515 field in the Q-F-L ternary diagram, close to the 100% lithic endmember (Fig. 8a). Grains are
516 generally subrounded, with lithics exhibiting more anisotropic shapes with smooth outer
517 boundaries, while quartz grains are subangular with rougher boundaries. The sorting degree
518 is average with grains covering different grain size classes.

519 The sample from the top of the fluvial bar (PAR2), shows a mineral composition close to the
520 underlying PAR1 previously described, with lithics dominating with respect to quartz and
521 feldspar. Lithic fragments compose most of the areal percentage of the sample (88.65-
522 91.36%), while quartz (4.01-6.72%) and feldspar-plagioclase (3.22-4.84%) are subordinate
523 (Fig. 8a, d). Lithics are mainly made of sedimentary aggregates of silt and clay-sized
524 particles (muscovite and chlorite), but a lesser content of metamorphic rock fragments
525 occurs (polycrystalline quartz grains). This sample can be inserted in the litharenite, lithic-
526 dominated field in the Q-F-L ternary diagram, next to PAR1 sample (Fig. 8a). Lithic
527 fragments are subrounded with highly elongate shapes and smooth boundaries.
528 Conversely, quartz grains are subangular to angular with marked asperities and edges along
529 the outer boundaries. Feldspar and plagioclase are subrounded and grains display smooth
530 perimeters. The sorting of the sample is average with a considerable span through grain
531 size classes.

532 The fluvial-reworked talus debris sample (PES1) is characterized by a mineral composition
533 shifted towards lithics, with considerable amounts of quartz and feldspar. Again, lithic
534 fragments constitute more than half of the sample (66.44-73.57%), followed by quartz (15.5-



535 21.62%) and feldspar-plagioclase (7.96-18.05%) (Fig. 8a, e). Most of lithics are composed
536 of ultramafic rock fragments (basalts, peridotites and gabbros), with lesser contribution from
537 metamorphic, hydrothermally altered rocks (serpentinites). Sedimentary lithic aggregates of
538 silt and clay, encasing siliciclastic particles, occur. The fine-grained matrix forming
539 aggregates is composed of clay minerals as documented by XRD analysis (Supplementary
540 material 2). According to the Q-F-L ternary diagram, PES1 sample can be ascribed to the
541 litharenite field, although slightly enriched in quartz and feldspar with respect to PAR1 and
542 PAR2 (Fig. 8a). Lithic fragment shape varies from subrounded to angular, with very rough
543 outer boundaries. Feldspar grains show subrounded and isotropic crystal form, while quartz
544 has subangular to angular shape. The sorting degree is poor, with particles displaying a
545 wide grain size span.

546 Eventually, the sand sample collected from the deltaic sandstone bar (ACQ1) displays a
547 mineral composition with similar percentage of feldspar, quartz and lithics. In this sample,
548 feldspar and plagioclase compose most of the sample (31.58-43.81%), followed by quartz
549 (18-44.83%) and lithic fragments (17.9-50.41%) (Fig. 8a, f). Lithics have different
550 composition, with igneous-intrusive terms (granites) dominating with respect to metamorphic
551 (schists-gneisses) and sedimentary ones (sandstones). Feldspar and plagioclase crystals
552 are severely affected by alteration to sericite minerals (muscovite and paragonite). ACQ1
553 sample can be inserted in the lithic arkose field of the Q-F-L classification diagram (Fig. 8a),
554 although one of the used photomicrographs falls in the feldspathic litharenite field due to the
555 heterogeneous distribution of several coarse feldspar grains. Feldspar grains have
556 subrounded shape, while quartz is subangular to angular. Lithic fragments of igneous origin
557 have subangular shape with rough outer boundaries, while sedimentary lithics are
558 subrounded and more elongate, with smooth boundaries. The sorting degree is low, with a
559 wide span of grain size classes.



560

561 **5.2 Laser-diffraction grain size analysis**

562 Optical granulometry grain size analyses on loose samples were replicated with 5 aliquots
563 of equal mass, and the grain size distribution curves were averaged to obtain a mean grain
564 diameter value and related parameters. The following results are presented considering the
565 calculated average grain size distribution curve for each sample.

566 *5.2.1 Beach sand sample (LIM1)*

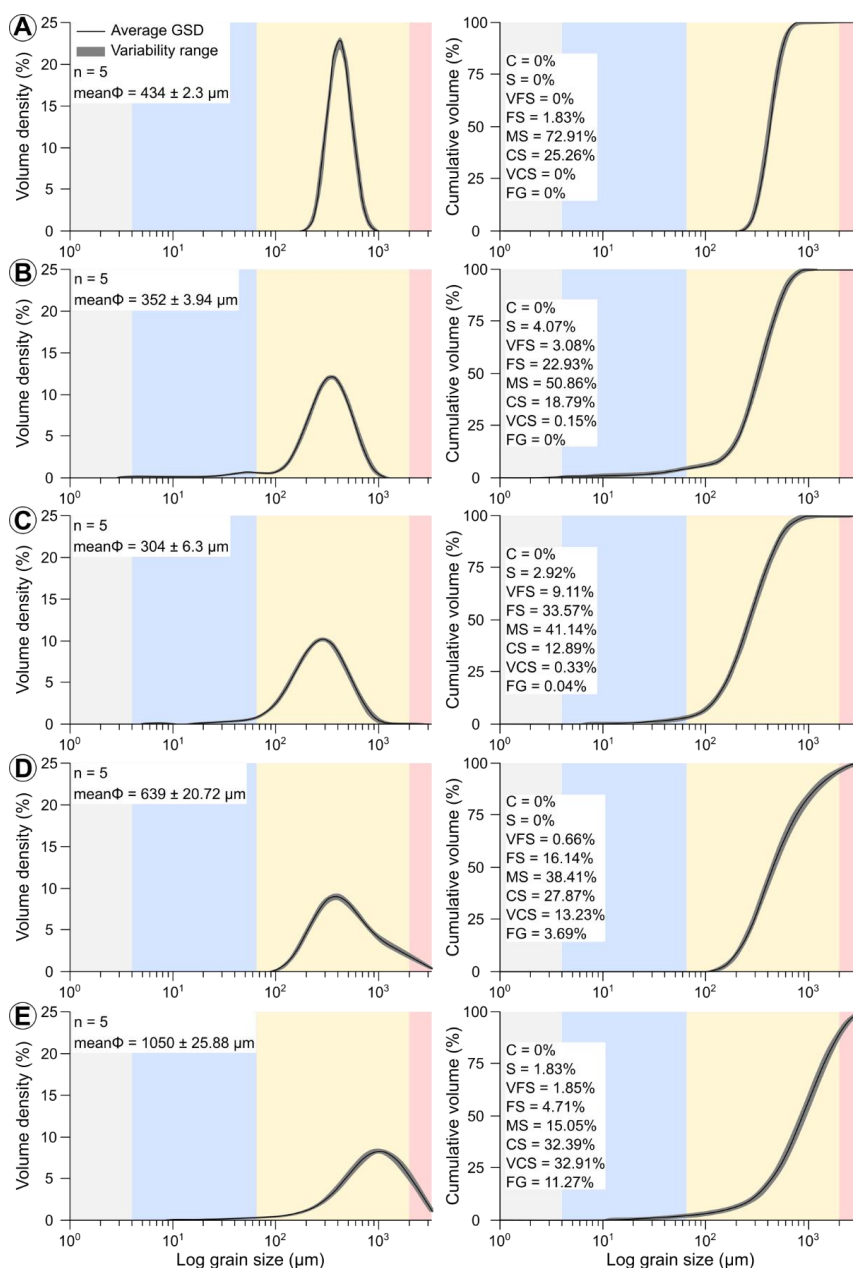
567 LIM1 sample displays a narrow grain size distribution curve, with subtle positive asymmetry.
568 The grain size distribution has intercepts with X axis at 174 and 1,041 μm , respectively. The
569 calculated average grain diameter is $434 \pm 2.3 \mu\text{m}$, with a modal value of $419 \pm 1.9 \mu\text{m}$ and
570 a median of $420 \pm 1.9 \mu\text{m}$ (Fig. 9a). The span of grain size distribution is low (good sorting
571 degree) with an average value of 0.665 ± 0.01 . All grains fall in the sand grain size interval
572 with the most recurrent size class being the medium-grained sand with 72.91% of particle
573 volume density. Coarse-grained particles compose 25.26% of the total sample volume, while
574 the remaining 1.83% is due to the fine-grained sand fraction (Fig. 9a).

575 *5.2.2 Basal fluvial sand bar sample (PAR1)*

576 The sand sample collected along the basal surface of a fluvial sand bar along the braided-
577 stream Parma Creek (PAR1), is characterized by an average grain size distribution curve
578 with medium width showing positive asymmetry. The left (finer) tail of the distribution curve
579 is more pronounced than the right (coarse) one with particles being detected at 2.9 μm on
580 the fine-ward side. Conversely, the right tail of the grain size curve intercepts the X axis at
581 1,182 μm . The average particle diameter is $352 \pm 3.9 \mu\text{m}$, with a modal value of 350 ± 1.9
582 μm and a median of $328 \pm 2.6 \mu\text{m}$ (Fig. 9b). Grain size distribution span is higher than the



583 one shown by the previous sample and the calculation returns a mean value of 1.343 ± 0.02 .
584 The most recurrent grain size class is the medium-grained sand with 50.89% of particle
585 volume density. Fine-grained and coarse-grained classes compose 22.93% and 18.79% of
586 the total sample volume, respectively. Minor amounts of volumetric densities are measured
587 in the silt size (4.07%), very fine-grained sand size (3.08%), and in very coarse-grained sand
588 size (0.15%) (Fig. 9b).



589

590 **Figure 9.** Grain size distribution curve obtained through laser granulometer analysis. (a) Volume density and
 591 cumulative distribution for LIM1 sample. (b) Volume density and cumulative distribution for PAR1 sample. (c)
 592 Volume density and cumulative distribution for PAR2 sample. (d) Volume density and cumulative distribution
 593 for PES1 sample. (e) Volume density and cumulative distribution for ACQ1 sample. GSD, grain size
 594 distribution; Φ particle diameter; n, number of analyses; C, clay; S, silt; VFS, very fine-grained sand; FS, fine-
 595 grained sand; MS, medium-grained sand; CS, coarse-grained sand; VCS, very coarse-grained sand; FG, fine



596 gravel.

597 *5.2.3 Upper fluvial sand bar sample (PAR2)*

598 The medium-grained sand collected on the top surface of a sandy bar along the Parma
599 Creek (PAR2), displays an average grain size distribution curve with medium width and
600 slight positive skewness. On the left tail, finest particles are recorded at 4.9 μm , while on the
601 right tail coarsest grains are detected at 1,343 μm . The calculated average grain diameter
602 is $304 \pm 6.3 \mu\text{m}$, with a mode at $286 \pm 3.3 \mu\text{m}$ (Fig. 9c). The span of the average grain size
603 curve is higher than previous samples, with a mean value of 1.608 ± 0.03 and a median of
604 $267 \pm 2.7 \mu\text{m}$. Higher span is recorded also by the particle volume distribution, with 41.14%
605 of grains falling in the medium-grained sand class and 33.57% of grains composing the fine-
606 grained sand size. A considerable volume of particles falls in the coarse-grained sand size
607 (12.89%), while only a small fraction is recorded in the very coarse-grained sand (0.33%)
608 and fine gravel grain size classes (0.04%). On the fine-ward side, no clay-sized particles are
609 recorded, while silt-size and very fine-grained sand classes compose 2.92% and 9.11% of
610 the total sample volume, respectively (Fig. 9c).

611 *5.2.4 Fluvially-reworked debris talus sand sample (PES1)*

612 The medium to coarse-grained sand sample collected from a debris talus reworked by river
613 stream (PES1) is characterized by an average grain size distribution curve with high width
614 and strong positive asymmetry. Grain size distribution tails are not symmetric, with the left
615 one being steeper than the right tail. On the left tail, finest grains are recorded at 81 μm ,
616 while on the right tail coarsest particles reach 3,300 μm of equivalent diameter. The average
617 grain diameter gained from the mean curve is $639 \pm 20.72 \mu\text{m}$, with a modal value of $386 \pm$
618 $2.41 \mu\text{m}$ and a median of $455 \pm 8.6 \mu\text{m}$ (Fig. 9d). The span of average grain size curve is
619 higher than the samples described before, with a mean value of $2.495 \pm 0.11 \mu\text{m}$. Higher
620 span can be traced also in the volumetric particle distribution among grain size classes. In



621 particular, the dominant grain size class is the medium-grained sand size with 38.41% of
622 volume density. Relatively high particle volumes are recorded also in the coarse-grained
623 sand (27.87%), fine-grained sand (16.14%) and in the very coarse-grained sand classes
624 (13.23%). Minor amounts of grains can be detected in the fine gravel class (3.69%) and in
625 the very fine-grained sand range (0.66%) (Fig. 9d).

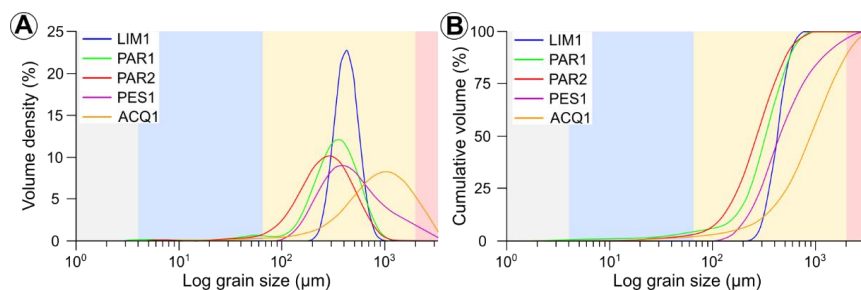
626 *5.2.5 Deltaic sand sample (ACQ1)*

627 The coarse-grained sandstone collected along an exposed fossil deltaic bar (ACQ1)
628 displays a wide grain size distribution curve with a weak positive asymmetry. The average
629 curve shows asymmetric tails, with a steep right tail (coarse) and a gentle left tail (fine).
630 Finest particles are recorded at 8.1 μm , while coarse ones have equivalent diameters of
631 3,300 μm . The average equivalent grain diameter is $1,050 \pm 25.88 \mu\text{m}$, with a mode of $1,020$
632 $\pm 57.92 \mu\text{m}$ and a median of $897 \pm 27.1 \mu\text{m}$ (Fig. 9e). The span shown by the mean
633 granulometric curve is equal to $1.993 \pm 0.02 \mu\text{m}$, slightly lower than PES1 sample. Data
634 regarding single grain size classes point out the high curve width. In this sample is difficult
635 to identify a single dominant grain size class, since coarse and very coarse-grained classes
636 compose 32.39% and 32.91% of total volumetric particle density, respectively. Considerable
637 particle amounts are also displayed by medium-grained sand (15.05%) and fine gravel size
638 classes (11.27%). Minor volumetric densities are recorded in fine-grained sand range
639 (4.71%), very fine-grained sand class (1.85%) and in the silt grain size interval (1.83%). No
640 grains have been measured in the clay-sized fraction (Fig. 9e).

641 To summarize, from sample LIM1 to ACQ1 we record a coarsening of average grain
642 diameter, a general broadening of grain size distribution curves (decrease of sorting
643 degree), and a more marked asymmetry between left and right tails of the curves (Fig. 10a
644 and table 1). The same observations can be made checking the cumulative grain size



645 distributions, which show a progressive decrease of slope following an increase of grain size
 646 (Fig. 10b and table 1).



647

648 **Figure 10.** Comparison of grain size distribution obtained with air-dispersed laser granulometer. (a) Volume
 649 density grain size distributions. (b) Cumulative volume percentage grain size distributions.

650

Table 1: Summary of analytical parameters extracted from laser granulometry analyses

Sample name	Sample type	Age	D_m (µm)	D_{x10} (µm)	D_{x50} (µm)	D_{x90} (µm)	Mode (µm)	Span
LIM1	Foreshore beach sand	Recent	434 ± 2.3	303 ± 1.87	420 ± 1.92	582 ± 4.15	419 ± 1.94	0.665 ± 0.01
PAR1	Base of fluvial sand bar	Recent	352 ± 3.94	152 ± 1.48	328 ± 2.61	593 ± 9.76	350 ± 1.92	1.343 ± 0.02
PAR2	Top of fluvial sand bar	Recent	304 ± 6.3	115 ± 1.34	267 ± 2.68	545 ± 12.18	286 ± 3.29	1.608 ± 0.03
PES1	Talus debris reworked along river	Recent	639 ± 20.72	211 ± 1.92	455 ± 8.62	1350 ± 71.55	386 ± 2.41	2.495 ± 0.11
ACQ1	Deltaic sandstone bar	Lower-Middle Pliocene	1050 ± 25.83	283 ± 8.02	897 ± 27.14	2070 ± 40.86	1020 ± 57.92	1.993 ± 0.02

651

652 **Table 1.** Summary of grain size analysis via laser granulometry. D_m , average particle diameter; D_{x10} , D_{x50} , D_{x90} ,
 653 grain size thresholds (percentiles) at 10, 50 and 90% of particle volume distribution.

654

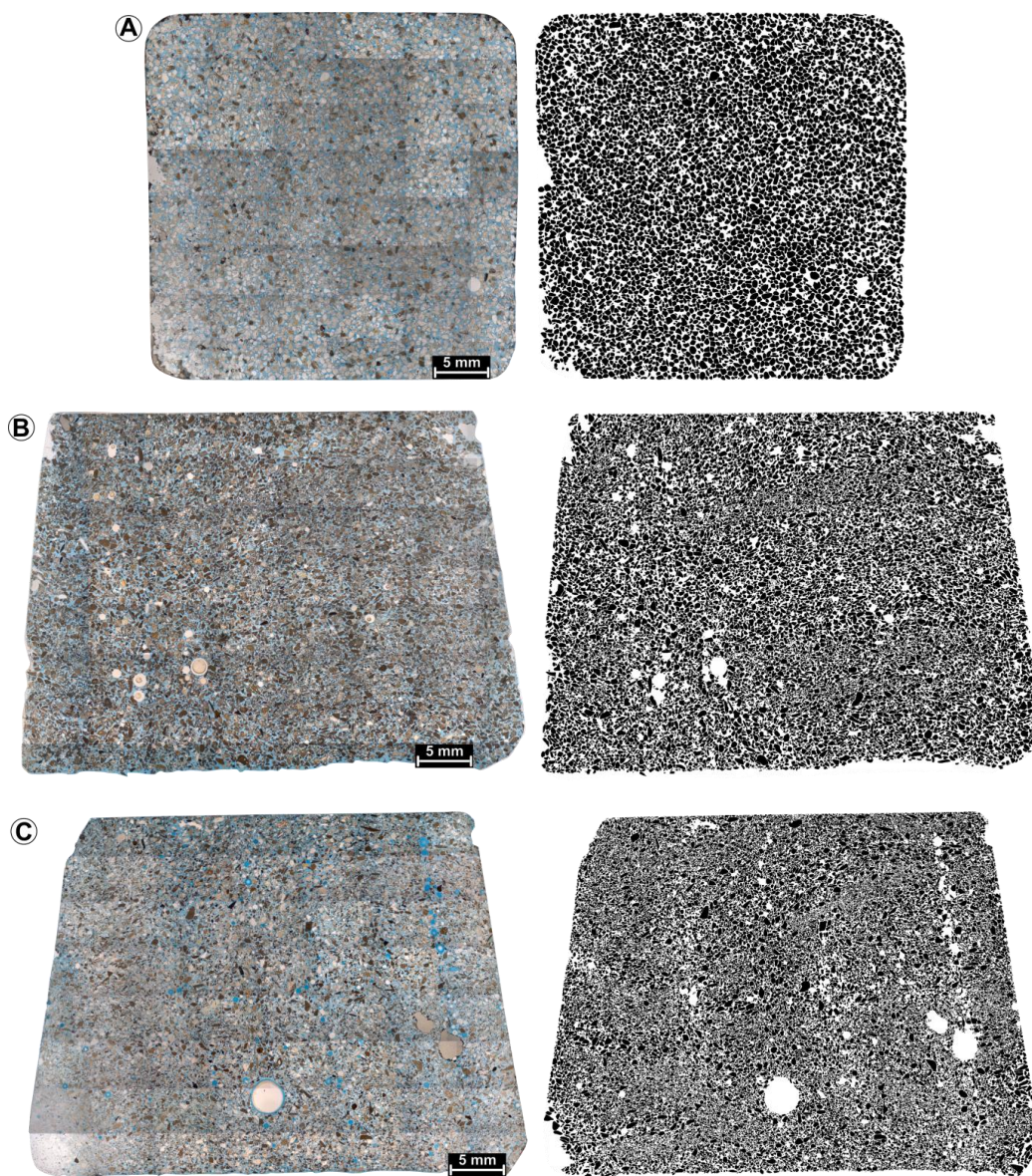
655 5.3 Thin section-image analysis grain size distributions

656 Two-dimensional grain size analysis was based on data gained from petrographic thin
 657 sections analyzed through image analysis technique. All grains composing the thin sections
 658 were digitized to provide robust datasets which served to set the 3D volume-weighted mean
 659 diameter conversion formula (Fig. 11).

660 5.3.1 Beach sand sample (LIM1)



661 For the foreshore-beach sand sample LIM1, a total of 5,419 grains were acquired (Fig. 11a).
662 The resulting particle number grain size distribution curve has intercepts with the X axis at
663 40 and 756 μm and a mode of 352 μm . The volume density converted distribution shows a
664 roughly symmetric bell shape with a weak skew towards finer particles and a modal value
665 of 390 μm (Fig. 12a). The sorting degree is high as testified by most of the grains falling in
666 the medium-grained sand size class (87.54%), while lesser particle amounts are recorded
667 in the fine-grained sand (6.89%) and in the coarse-grained sand intervals (5.29%). Only
668 small fractions of silt-sized and very fine-grained sand material were detected, with
669 percentage of 0.01% and 0.26%, respectively (Fig. 12a).



670

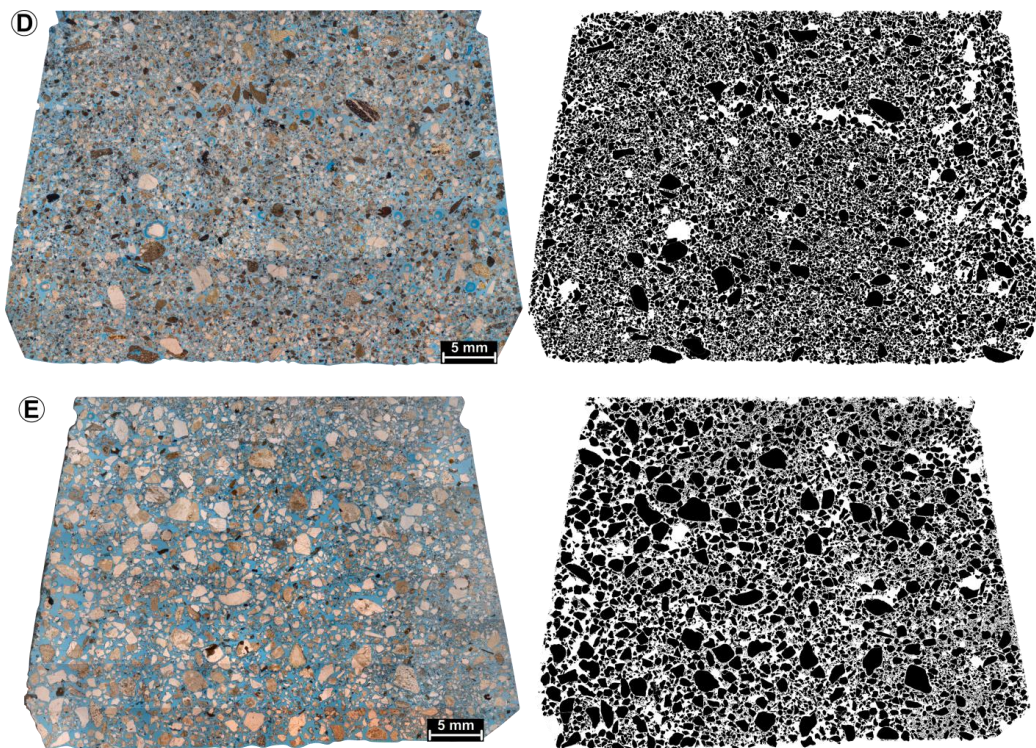
671 **Figure 11.** Original and binary photo-mosaics of the analyzed thin sections composed of tens of
672 photomicrographs stitched together. (a) LIM1 beach sample. (b) PAR1 fluvial sample. (c) PAR2 fluvial sample.
673 (d) PES1 fluvial sample. (e) ACQ1 fluvial-deltaic sample.

674

675 5.3.2 Basal fluvial sand bar sample (PAR1)



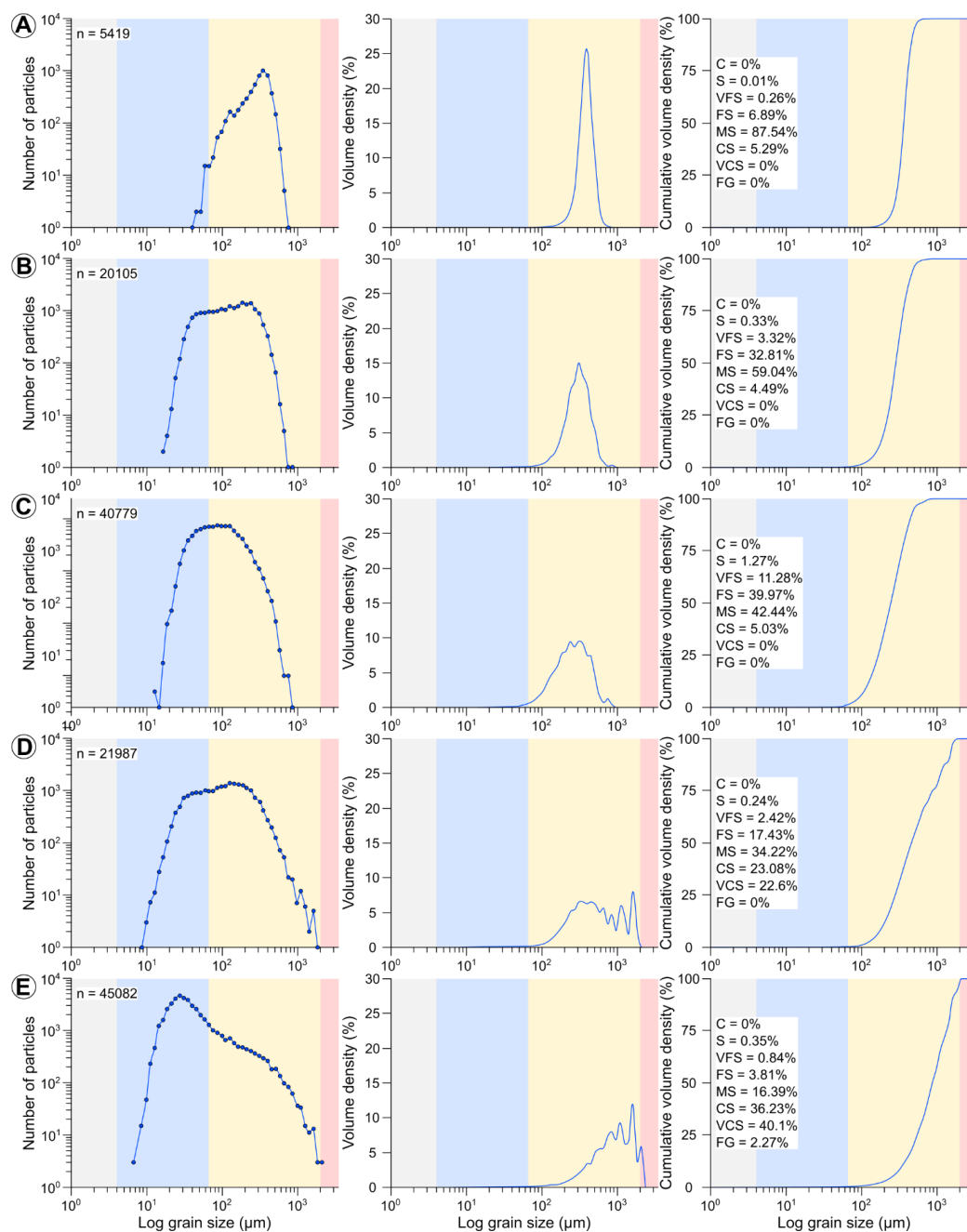
676 The fluvial sand bar sample PAR1 was analyzed by acquisition of 20,105 grains (Fig. 11b).
677 The particle number distribution describes a “bell-shape” curve, with the finest grains
678 recorded at 16.4 μm , coarsest ones at 859 μm and a mode of 186 μm . The density
679 volumetric distribution is described by a slight left asymmetry with a modal peak at 310 μm
680 (Fig. 12b). Sorting is lower compared to LIM1 sample, with a broader grain size distribution
681 as can be observed by particle volume density distribution through standard grain size
682 classes. The dominant size class is the medium-grained sand composing 59.04% of the
683 sample volume, followed by the fine-grained sand constituting 32.81% of volume density.
684 Lesser amounts of very fine-grained sand (3.32%) and coarse-grained sand (4.49%) have
685 been detected. Silt-sized material composes only 0.33% of the analyzed sample (Fig. 12b).



686

687 **Figure 11 continued.**

688



689

690 **Figure 12.** Grain size distribution curves extracted from 2D thin sections through image analysis. Results are
 691 presented as number of particles, volume density and cumulative volume percentage distributions. (a) LIM1
 692 beach sample. (b) PAR1 fluvial sample. (c) PAR2 fluvial sample. (d) PES1 fluvial sample. (e) ACQ1 fluvial-
 693 deltaic sample. n, number of particles. C, clay; S, silt; VFS, very fine-grained sand; FS, fine-grained sand; MS,



694 medium-grained sand; CS, coarse-grained sand; VCS, very coarse-grained sand; FG, fine gravel.

695

696 *5.3.3 Upper fluvial sand bar sample (PAR2)*

697 40,779 grains were obtained from the second fluvial sand bar sample PAR2 (Fig. 11c). The
698 distribution of particle number is characterized by a symmetrical bell-shaped curve with
699 finest recorded particles at 12.7 μm , equivalent diameter of coarsest grains up to 859 μm
700 and a modal value of 86.4 μm . Although we defined one single modal value, the modal peak
701 described is wide and most of the grains have equivalent diameter falling between 58.9 and
702 127 μm . Data converted in particle volume density show a left asymmetry of the distribution
703 curve and a modal peak at 310 μm (Fig. 12c). The width of the curve (i.e., sorting degree)
704 is higher than the previous samples. Grains are almost equally distributed between the
705 medium and fine-grained sand size classes, with volume densities of 42.44% and 39.97%,
706 respectively. Significant particle volume is recorded in the very fine-grained sand size class
707 (11.28%), while only 5.03% of particles fall in the coarse-grained sand interval. Silt-sized
708 material composes 1.27% of the total sample volume (Fig. 12c).

709 *5.3.4 Fluvially-reworked debris talus sand sample (PES1)*

710 PES1 sample, the reworked debris talus along the river stream, was analyzed by
711 considering a total of 21,987 grains (Fig. 11d). The distribution by number of particles
712 describes a wide, almost symmetrical bell-shape, having as lower and higher intercepts with
713 X axis at 8.68 and 1,850 μm , respectively. The modal peak is broad, with most recurrent
714 data in between 111 and 240 μm size interval and a modal value of 127 μm . The volume
715 density corrected curve displays a left asymmetry with a modal peak of 352 μm and a right
716 curve tail with oscillating volume density associated with coarser particles (Fig. 12d). The
717 sorting degree is low as indicated by the width of the modal peak. The volume density curve



718 has a high width, testified by the significant spread of particles in different grain size classes.
719 In particular, the most recurrent size class is the medium-grained sand interval with 34.22%
720 of total grains, followed by the coarse-grained sand class composing 23.08% of the sample.
721 Significant volume densities of very coarse-grained and fine-grained sand are documented,
722 with percentages of 22.6% and 17.43%, respectively. Small volume of very fine-grained
723 sand material is recorded (2.42%), together with silt-sized particles (0.24%) (Fig. 12d).

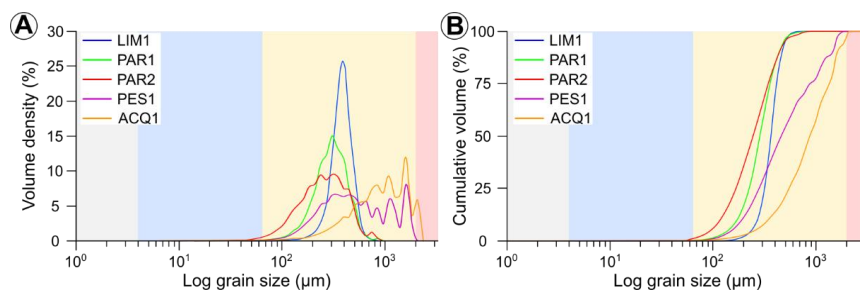
724 *5.3.5 Deltaic sand sample (ACQ1)*

725 Two-dimensional grain size of ACQ1 sample, collected along a fossil deltaic bar, was
726 investigated with a total amount of 45,082 grains (Fig. 11e). The number of grain distribution
727 highlights an asymmetric shape with right skew, and finest particles recorded at 6.72 μm
728 and coarsest ones at 2,100 μm . The modal value of the distribution lies in the fine-grained
729 interval at 27.4 μm . The volume density distribution curve displays a left asymmetry, with a
730 gentle left tail and a steep right tail showing marked data oscillations. The modal peak is
731 located at 1,630 μm in the coarser end of the distribution curve and the sorting degree is low
732 (Fig. 12e). In this sample the dominant grain size fraction is the very coarse-grained sand
733 with 40.1% of total sample volume. Coarse and medium-grained sand classes compose
734 36.23% and 16.39% of total sample volume, respectively. Minor amounts of fine-grained
735 sand (3.81%) and fine gravel (2.27%) are also documented. Eventually, tiny fractions of very
736 fine-grained sand and silt-size material compose the fine tail of the curve with 0.84% and
737 0.35% of volume density, respectively (Fig. 12e).

738 Summarizing the main results obtained from thin section analysis, we observe a progressive
739 broadening and coarsening of granulometric curves with different distribution of particles
740 from LIM1 to ACQ1 samples (Fig. 13a). In coarse-grained samples (PES1 and ACQ1) the
741 coarse, right tail of the distribution curves shows oscillating volume density values due to
742 the presence of a few tens of grains providing higher data scattering. The comparison of



743 cumulative frequency distribution confirms the diminishing of the slope due to lowering
744 sorting degree (Fig. 13b).



745

746 **Figure 13.** Comparison of grain size distributions obtained from image analysis technique applied to thin
747 sections. (a) Volume density grain size distributions. (b) Cumulative volume percentage grain size distributions.

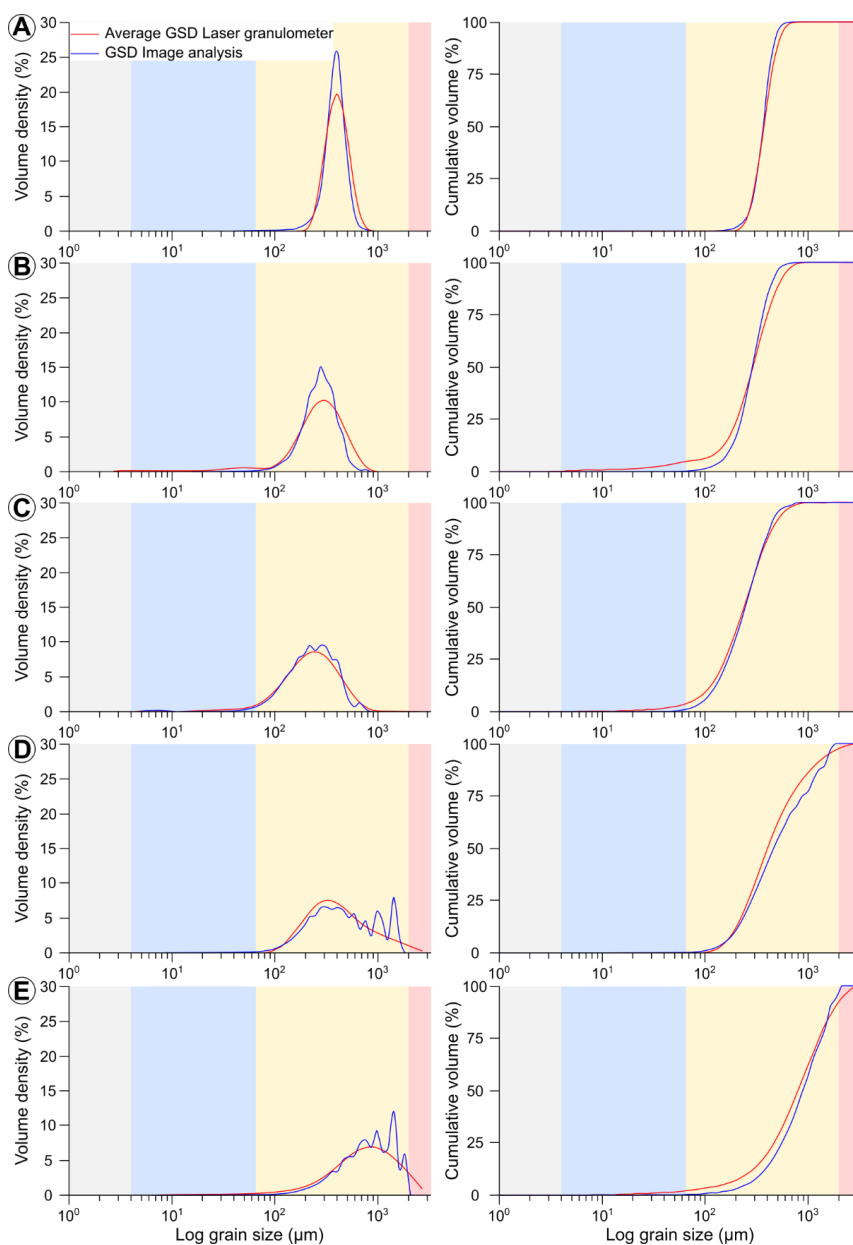
748

749 **5.4 Laser granulometry vs. thin section grain size distributions**

750 The comparison between volume density distribution curves acquired via optical
751 granulometry and thin section analysis, shows striking similarities (Fig. 14). For all the 5
752 considered samples both methods provide similar overall shape of grain size distributions
753 with almost overlapping modal peak values. Slight differences in modal peak height can be
754 documented especially for highly to moderately sorted samples (LIM1 and PAR1), in which
755 the grain size distribution curve obtained through image analysis has higher modal values
756 compared to the laser granulometer data (Fig. 14a and b). On the same samples, laser
757 granulometer technique recorded higher particle volumes in the right (coarse) tail of
758 granulometric curve with respect to image analysis data. Tiny differences can be seen in the
759 left (fine) tail of curves, with LIM1 displaying minor particle volume recorded by laser
760 granulometry with respect to thin sections, while the opposite occurs for PAR1 sample. For
761 the other 3 coarser and less sorted samples (PAR2, PES1 and ACQ1) the match between



762 the granulometric curves gained with different methods is good and the intercepts with X
763 axis are almost coincident (Fig. 14c-e).



764

765 **Figure 14.** Comparison between grain size distributions extracted from laser granulometry and from image
766 analysis. (a) LIM1 beach sample. (b) PAR1 fluvial sample. (c) PAR2 fluvial sample. (d) PES1 fluvial sample.
767 (e) ACQ1 fluvial-deltaic sample. GSD, grain size distribution.



768

769 The main differences are related to the right (coarse) tail of the curves, especially for PES1
770 and ACQ1 samples, where the thin section distribution curve displays volume density
771 variability in the coarser grain size range. This data variability is induced by few very coarse
772 (1-2 mm size) particles, which influence the final volume density distribution (Fig. 14d and
773 e).

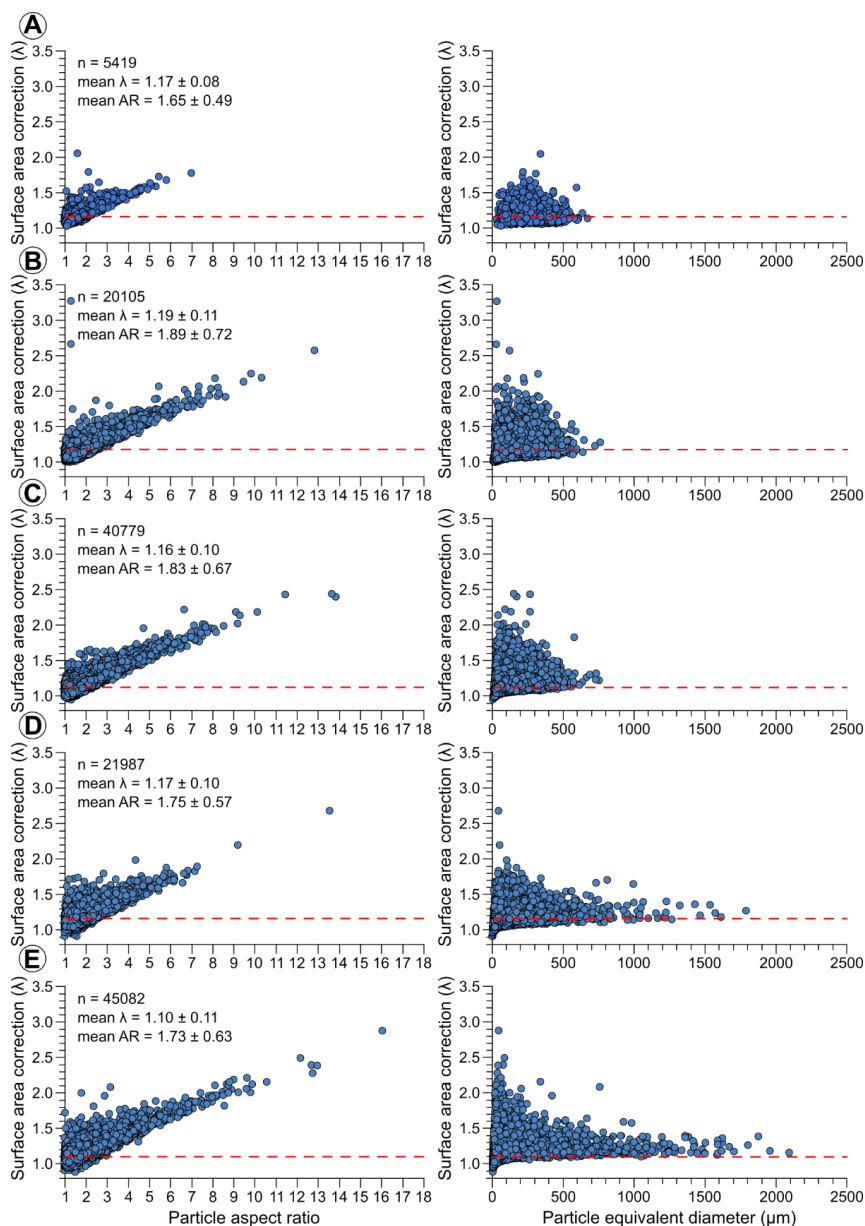
774

775 **5.5 Volume-weighted mean diameter calculation**

776 Calculations of volume-weighted mean diameter were performed with the formula reported
777 in equation 2. The entire grain size datasets associated with thin sections of granular
778 samples were considered. The foreshore beach sand sample LIM1, returns a value of
779 volume-weighted mean diameter equal to 364.16 μm , while for the fluvial sand bar samples
780 (PAR1 and PAR2) mean values of 296.54 μm and 256.08 μm are obtained, respectively.
781 PES1 fluvial coarse sand shows a volume-weighted mean diameter of 625.83 μm , and the
782 fossil deltaic sand ACQ1 sample provides a value of 955.79 μm . All the obtained mean
783 diameter values are lower than the equivalent obtained through optical laser granulometry.
784 We then applied a surface area correction factor (λ), as indicated in equation 3, to consider
785 the deviations of grain shape from spherical particles (Fig. 15) (Davies et al., 2019; Johnson
786 et al., 2021). λ factor was calculated for every sample and implemented in equation 2 as
787 indicated in the modified volume-weighted mean diameter formula reported in equation 4.
788 For LIM1 sample, the aspect ratio of grains spans from 1.01 to 7.01, with a mean value of
789 1.65 ± 0.49 , thus equation 3 can be simplified and returns an average λ value of 1.17 ± 0.08
790 (Fig. 15a). By multiplying the volume-weighted mean diameter by λ factor, we obtain a
791 corrected grain diameter of 425.35 μm . PAR1 has grain aspect ratio falling between 1.01



792 and 12.84, with a mean value of 1.89 ± 0.72 , thus providing a mean λ correction factor of
793 1.19 ± 0.11 (Fig. 15b).



794

795 **Figure 15.** Graphs reporting the particle aspect ratio-surface area correction factor and particle equivalent
796 diameter-surface area correction factor relationships for the analyzed sand samples. (a) LIM1 beach sample.
797 (b) PAR1 fluvial sample. (c) PAR2 fluvial sample. (d) PES1 fluvial sample. (e) ACQ1 fluvial-deltaic sample.



798 The horizontal dashed red line indicates the average surface area correction factor. n , number of particles; λ ,
799 surface area correction factor; AR, particle aspect ratio.

800

801 The resulting corrected volume-weighted mean diameter is equal to 351.78 μm . For PAR2
802 sample, grains have aspect ratio comprised from 1.0 to 13.88 with an average value of 1.83
803 ± 0.67 , giving a mean λ value of 1.16 ± 0.1 (Fig. 15c). The volume-weighted mean diameter
804 corrected according to particle shape results 307.39 μm . PES1 is composed of grains with
805 aspect ratio spanning from 1.0 to 13.55, with an average value of 1.75 ± 0.57 , returning a
806 mean λ correction factor of 1.17 ± 0.1 (Fig. 15d). Applying the correction to equation 4, the
807 final volume-weighted mean diameter is equal to 731.08 μm . Eventually, ACQ1 sample is
808 characterized by grains with aspect ratio between 1.0 and 16.06 with an average value of
809 1.73 ± 0.63 , giving back a λ mean surface area correction factor of 1.10 ± 0.11 (Fig. 15e).
810 The obtained corrected equivalent diameter for this sample is 1,055.64 μm . Volume-
811 weighted mean diameter displays values close to the ones obtained through optical
812 granulometry. The only exception is PES1 sample, which has an average grain size
813 measured with laser granulometry 90-100 μm finer than the values calculated via image
814 analysis on thin section.

815

816 **6. Discussion**

817 **6.1 Comparison between 2D (image analysis) and 3D (laser granulometry) grain size** 818 **analyses**

819 Grain size distribution curves of analyzed samples obtained from 2D (image analysis) and
820 3D (laser granulometry) methods show striking similarities. The overall shape, skew
821 (asymmetry) and modal peak position is equal in both the adopted methodologies (Fig. 14).

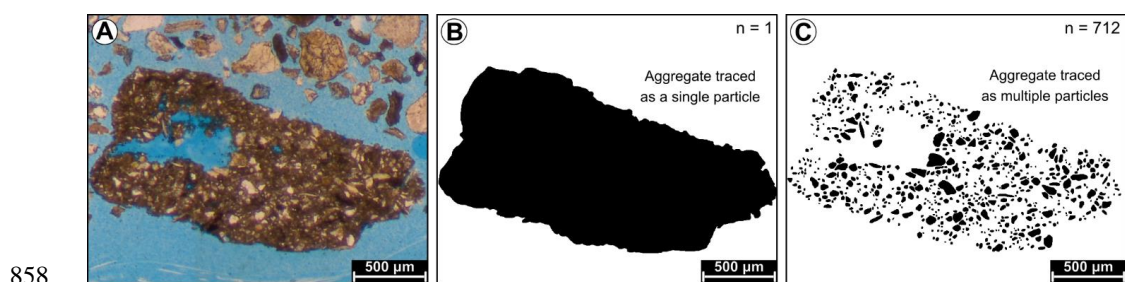


822 Slight differences can be traced in modal peak height, with data obtained through laser
823 granulometry displaying typically lower modal height with respect to grain size distributions
824 provided by image analysis from thin sections. Moreover, grain size distributions gained with
825 the optical granulometer appear to be smoother especially on the coarser tail compared to
826 image analysis data (Fig. 14). This can be explained by the usage of the 100 instrumental
827 grain size classes adopted by the laser granulometer, which were extended also to image
828 analysis grain size distributions. Such detailed subdivision of the 10 nm to 3,500 μm size
829 interval in tiny frequency bins, caused variations in the coarser end of grain size distributions
830 gained from image analysis. These variations are mainly related to the presence of a few
831 tens of grains in coarser grain size classes inducing volume frequency oscillations. We
832 employed the very same grain size classes for both analytical methods to allow precise
833 comparison of data distribution, without the bias induced by different bin sizes. It is likely
834 that the adoption of the standard sedimentological grain size classes (Udden-Wentworth
835 scale) (Udden, 1914; Wentworth, 1922) could have provided more stable volume frequency
836 results at the cost of less detail between different classes. Still, we preferred to prioritize and
837 put emphasis on evidencing small differences between grain size classes rather than
838 achieving volume frequency stability across the whole grain size distributions.

839 The comparison of volume-weighted mean diameters extracted from granulometry data, and
840 the corrected volume-weighted mean diameters from image analysis technique provided
841 matching results for 4 out of 5 total sand samples. In particular, for LIM1 sample, laser
842 granulometry returned a mean equivalent diameter of 434 μm , while image analysis
843 technique gave 425.3 μm . Fluvial sand PAR1 showed an equivalent diameter from laser
844 granulometry of 352 μm , with related volume-weighted mean diameter of 351.8 μm , while
845 for PAR2 returned diameter values of 304 and 307.4 μm , respectively. In the case of PES1,
846 the laser granulometer measured a mean particle diameter of 639 μm , while data acquired



847 with image analysis provided a mean value of 731.1 μm . Eventually, for ACQ1 deltaic sand
848 sample, laboratory grain size analysis gave a mean diameter of 1,050 μm , while image
849 analysis technique provided a value of 1,055.6 μm . The only deviation from good and
850 matching results was related to PES1 sample, which showed image analysis derived data
851 90-100 μm coarser than the equivalent diameter measured via laser granulometry. We
852 explain this difference considering the mineralogical composition of the sample and the limits
853 imposed by the involved analytical techniques. Apart from quartz, feldspar, and plagioclase,
854 PES1 sample is composed of coarse aggregates of silt-clay matrix binding fine-grained
855 siliciclastic grains (Fig. 16a). During manual tracing of particle outer boundaries, we treated
856 these aggregates as single particles, without distinguishing the fine-grained particles
857 interspersed within the matrix (Fig. 16b and c).



859 **Figure 16.** Soft aggregates issue encountered in manual digitization of PES1 sample. (a) Soft, ~2 mm-size,
860 aggregate composed of clayish matrix embedding fine-grained siliciclastic particles. (b) Digitization strategy
861 adopted in the present study for such clay aggregates. (c) Digitization of every particle composing the interior
862 of the aggregate. n, number of traced grains.

863 Thin sectioning of loose granular media, proved to be a conservative method in preserving
864 the original size and shape of weak sand framework components, minimizing the overall
865 sample alteration. Conversely, laser granulometry operated via pressured air dispersion
866 may cause alteration of original grain size in sensitive and mechanically weak samples
867 (Storti and Balsamo, 2010; Cortinovis et al., 2019). Before the analyses we performed tests
868 to set the instrumental parameters to be used granting the least sample alteration



869 (Supplementary material 1). In the case of PES1, which is the weakest sample, even the
870 adoption of the most conservative analytical parameters was not enough to completely avoid
871 sample damaging. This sample is the only one displaying aggregates whose matrix is made
872 of clay minerals, which could have been damaged during laser granulometry analysis. In
873 PES1 some alteration, related to splitting and partial disaggregation of soft silt-clay
874 aggregates caused the fine-ward shift of the average particle diameter. In such weak sample
875 types, we considered data derived from image analysis technique to be more reliable and
876 representative of the real grain size distribution than laser granulometry analysis. The same
877 alteration was not documented in the other 4 samples likely due to their different mineral
878 composition and higher relative particle resistance, preventing any significant mechanical
879 alteration of the original grain size during the analysis.

880

881 **6.2 Volume-weighted mean diameter (D_w) vs. literature calculation methods**

882 Mean particle diameter values based on optical granulometry and image analysis (corrected
883 volume-weighted mean diameter) methods were compared with previously published and
884 widely used calculation equations reported in the Appendix 1 (tables 2 and 3). In particular,
885 we focused on the comparison with the method of moments (both arithmetic and geometric
886 equation) (Krumbein and Pettijohn, 1938), the graphical method (geometric mean) (Folk and
887 Ward, 1957), median, mode, arithmetic mean and area-weighted mean diameter. In
888 comparing different equations, we assumed the mean diameter values extracted from the
889 laser granulometer as reference, with relative differences between calculation formulas
890 expressed as percentages (positive values represent grain diameter underestimation, while
891 negative ones indicate overestimation with respect to the reference) (tables 2 and 3).
892 Considering laser granulometry reference data, the arithmetic mean calculated with the
893 method of moments, provides close results with the ones gained with the mean diameter



894 formula employed by the optical granulometer (equation 5) (maximum difference in the
 895 average grain diameter of 0.36% from the reference value). Conversely, the geometrical
 896 mean of method of moments returns small percentage errors for well sorted samples (3.1%
 897 difference for LIM1 sample) with a progressively increasing error following sorting
 898 diminishing (from 16.4 to 24.4% error in PAR1, PAR2, PES1 and ACQ1 samples) (table 2).

Table 2: Comparison of results from different calculation equations applied to laser granulometry analyses

Sample name	Method of moments		Graphical method	GSD laser granulometry			
	Arithmetic (μm)	Geometric (μm)	Geometric (μm)	Sorting	D_m (μm)	Median (μm)	Mode (μm)
LIM1	434.7	420.5	420.6	0.37	434	420	419
PAR1	352.9	294.3	319.8	0.845	352	328	350
PAR2	305.1	252.7	261.1	0.877	304	267	286
PES1	640.3	492.6	487.5	1.029	639	455	386
ACQ1	1053.6	794.1	850.7	1.137	1050	897	1020
Sample name	Complementary percentage ratio with respect to volume-weighted mean diameter from laser granulometry (%)						
LIM1	-0.16	3.11	3.09	-	0	3.22	3.45
PAR1	-0.25	16.39	9.15	-	0	6.82	0.57
PAR2	-0.36	16.87	14.11	-	0	12.17	5.92
PES1	-0.20	22.91	23.71	-	0	28.79	39.59
ACQ1	-0.34	24.37	18.98	-	0	14.57	2.86

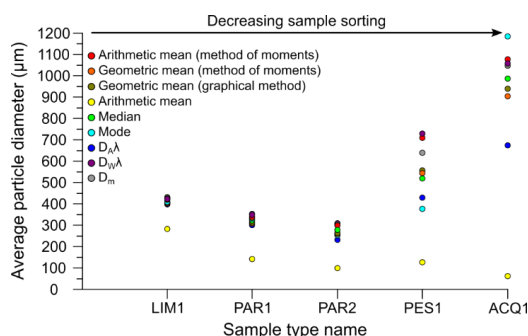
899

900 **Table 2.** Comparison of results given by different calculation formulas for grain size distribution acquired
 901 through laser granulometry. Calculation equations are reported in the Appendix 1. GSD, grain size distribution;
 902 D_m , average grain diameter (laser granulometer).

903 The same increasing error trend can be seen for the geometric mean of graphical method,
 904 with a maximum deviation of 23.7% calculated for PES1 sample. Eventually, the median of
 905 distribution curves is close to the mean diameter gained from laser granulometry only in the
 906 case of well sorted samples (deviation of 3.2 and 6.8% in LIM1 and PAR1, respectively),
 907 while it deviates far from it in more poorly sorted ones (PAR2, PES1 and ACQ1, with errors
 908 up to 28.8%). The mode can approximate the average diameter only in the case of weakly
 909 skewed grain size distributions (errors comprised from 0.5 to 5.9% in LIM1, PAR1, PAR2
 910 and ACQ1), but it fails in the case of strongly skewed ones (39.6% deviation in PES1) (table
 911 2).



912 Utilizing grain size distribution datasets extracted via image analysis technique (the
 913 corrected volume-weighted mean diameter is used as reference) the best results are
 914 provided by applying the arithmetic method of moments, with standard errors spanning from
 915 1.7 to 3.9% in all samples. As already observed for laser granulometer size distributions,
 916 geometrical mean calculated with the method of moments returns good results only for well
 917 sorted samples, while tends to underestimate the mean diameter up to 25.3% of reference
 918 value in poorly sorted sands (Fig. 17 and table 3).



919

920 **Figure 17.** Comparison of average particle diameter values calculated with literature equations and the
 921 proposed volume-weighted mean diameter formula for the 5 considered sand samples. Used datasets are
 922 derived from thin sections analyzed with image analysis. $D_{v\lambda}$, area-weighted mean diameter (shape corrected);
 923 $D_{w\lambda}$, volume-weighted mean diameter (shape corrected). D_m , laser granulometer mean diameter.

924 Similar results are extracted from the geometric mean diameter formula of the graphical
 925 method, with the best result achieved for LIM1 sample (4.2% mean diameter
 926 underestimation) and worst attained for PES1 sand sample (23.7% diameter
 927 underestimation). Adoption of the median value grants good results for properly sorted
 928 samples (-0.4 to 7.7% in LIM1 and PAR1), while deviations become bigger in poorly sorted
 929 ones (10.9 and 28.9% in PAR2 and PES1, respectively) (Fig. 17). The mode follows similar
 930 trends and fails in describing weakly to poorly sorted granular media (errors from -12.2 to
 931 48.6% in PAR2, PES1 and ACQ1). Severe mean diameter underestimation is documented



932 in the case of simple arithmetic mean diameter and area-weighted mean diameter with
 933 standard errors reaching 94.1 and 41.3%, respectively (Fig. 17 and table 3).

Table 3: Comparison of results from different calculation equations applied to image analysis grain size data

Sample name	Method of moments		Graphical method		GSD Image analysis				
	Arithmetic (μm)	Geometric (μm)	Geometric (μm)	Sorting	Arithmetic (μm)	Median (μm)	Mode (μm)	$D_A \lambda$ (μm)	$D_w \lambda$ (μm)
LIM1	415.4	403.2	407.5	0.329	283.8	427	411.2	401.4	425.3
PAR1	337.8	313.5	317.7	0.544	141.4	324.5	331	300	351.8
PAR2	302	264.6	267.2	0.757	98.63	273.9	256	232.7	307.4
PES1	709.6	546.3	557.4	1.097	127.8	519.6	376	428.9	731.1
ACQ1	1079.1	906.5	940.5	0.901	62.4	989.1	1185	674.6	1055.6

Sample name	Complementary percentage ratio with respect to volume-weighted mean diameter from image analysis (%)								
LIM1	2.33	5.19	4.18	-	33.27	-0.4	3.31	5.62	0
PAR1	3.98	10.88	9.69	-	59.81	7.76	5.91	14.72	0
PAR2	1.75	13.92	13.08	-	67.91	10.89	16.72	24.30	0
PES1	2.94	25.27	23.76	-	82.52	28.93	48.57	41.33	0
ACQ1	-2.22	14.12	10.90	-	94.09	6.29	-12.26	36.09	0

934

935 **Table 3.** Comparison of results provided by different calculation formulas for grain size distributions gained
 936 with image analysis. Calculation equations are reported in the Appendix 1. GSD, grain size distribution; $D_A \lambda$,
 937 area-weighted mean diameter (shape corrected); $D_w \lambda$, volume-weighted mean diameter (shape corrected).

938 Summarizing the comparative results, the proposed corrected volume-weighted mean
 939 diameter equation proves to be a reliable calculation formula and provides matching results
 940 with the arithmetic method of moments, as well as with data gained from laser granulometry
 941 technique. Conversely, the geometrical mean diameter of both method of moments and
 942 graphical method can describe only well to moderately sorted samples, while it struggles in
 943 poorly sorted ones. The same deviations, with even bigger magnitudes, can be highlighted
 944 by the adoption of the median and modal value as parameters describing grain size
 945 distributions. Similarly, the simple arithmetic mean, and area-weighted mean diameter are
 946 not reliable calculation equations, and their usage should be avoided as they show the
 947 highest difference from the reference (tables 2 and 3).

948

949 **6.3 Shape correction factor (λ) vs. literature empirical correction parameters**



950 In the past years, a lot of efforts were made to achieve robust conversion factors that could
951 grant reliable 3D average particle diameter starting from 2D equivalent diameter distributions
952 obtained with different analytical methods. Correction equations have been developed in
953 different research areas of Earth Sciences spanning from sedimentology, planetary geology,
954 to structural geology. Correction coefficients are based on geometrical considerations
955 (Roethlisberger, 1955; Hughes, 1978b), statistical-mathematical relationships (Krumbein,
956 1935; Chayes, 1950; Greenman, 1951; Sahu, 1966; Rose, 1968; Johnson, 1994; Kong et
957 al., 2005), empirical rules (Friedman, 1962a) or software aided simulations (Panozzo
958 Heilbronner, 1992; Heilbronner and Bruhn, 1998). All these methods bring different
959 correction coefficients to account for mean diameter underestimation related to random
960 particle sectioning. Correction values are comprised between 1.0 and 1.5 and must by
961 multiplied by the average grain diameter obtained from image analysis performed on rock
962 thin sections (table 4). We tested the precision of equations proposed in literature by
963 applying the correction coefficient to the volume-weighted mean diameter values obtained
964 from the 5 studied sand samples. In this process, we did not multiply the mean diameter by
965 the λ shape correction factor, thus using only the raw, uncorrected volume-weighted mean
966 diameter values (table 4). Such a procedure allowed a direct comparison of λ shape
967 correction factor with other correction parameters. By using our grain size datasets, closest
968 results compared to the ones obtained with equation 4, are gained employing the correction
969 factors proposed by Friedman (1958, 1962b), Sahu (1966), and Johnson (1994). Other
970 correction methods (Krumbein, 1935; Chayes, 1950; Greenman, 1951; Hughes, 1978b;
971 Panozzo, 1982; Panozzo Heilbronner, 1992; Kong et al., 2005) typically tend to overestimate
972 the average grain diameter by a significant margin (table 4). This is especially true in the
973 case of poorly sorted, coarse-grained samples (PES1 and ACQ1), while differences are less
974 pronounced in well to moderately sorted and medium-grained ones (LIM1 and PAR1) (table
975 4). Although some of the correction methods discussed above provide close results with the



976 shape corrected volume-weighted mean diameter values, we prefer to apply different λ
 977 correction factors to different samples. This sample specific procedure should grant more
 978 reliable results, due to shape correction bound to the grain size distribution and particle form
 979 of each sample.

Table 4: Comparison of correction parameters with the presented original data

Literature correction method	Mean diameter of analyzed samples (μm)					Correction factor
	LIM1	PAR1	PAR2	PES1	ACQ1	
Krumbein (1935), Chayes (1950), Kong et al. (2005)	463.65	447.88	337.5	796.81	1216.91	1.2732
Krumbein (1935)	477.27	388.64	335.62	820.21	1252.65	1.3106
Greenman (1951)	494.86	402.39	348.03	851.04	1299.63	1.3589
Friedman (1958), (1962)	430.18	350.30	363.12	739.29	1129.07	1.1813
Sahu (1966)	412.15	335.62	289.83	708.31	1081.76	1.1318
Hughes (1978)	445.98	363.17	313.62	766.45	1170.55	1.2247
Panozzo (1982)	466.12	379.57	327.78	801.06	1223.41	1.28
Heilbronner (1992)	546.24	444.81	384.12	938.74	1433.68	1.5
Johnson (1994)	418.79	340.56	294.53	720.26	1099.92	1.15
D_w λ image analysis	425.35	351.78	307.39	731.08	1055.64	1.10-1.19
D_w uncorrected image analysis	364.16	296.54	256.08	625.83	955.79	
D_m laser granulometry	434	352	304	639	1050	

980

981 **Table 4.** Comparison of different published correction factors to be applied in switching from 2D to 3D grain
 982 size distributions. D_m , mean grain diameter (laser granulometer); D_w , volume-weighted mean diameter; λ ,
 983 shape correction factor.

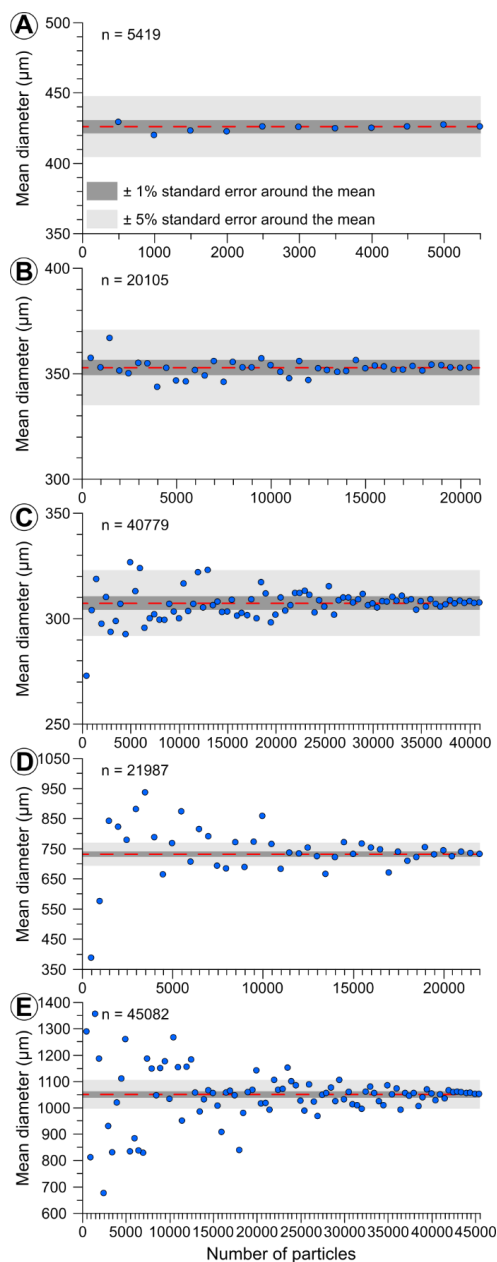
984

985 **6.4 Representative number of particles-sorting relationship**

986 In all the analyzed samples, we acquired large particle size datasets (> 5,000 particles), as
 987 we were interested in testing the reliability and reproducibility of mean diameter calculated
 988 with the proposed volume-weighted mean diameter formula. The number of digitized
 989 particles was higher in samples characterized by low sorting degree, and this was required
 990 to extract stable mean diameter values. At the same time, the adoption of large datasets
 991 allowed to check the critical number of particles required to achieve a certain standard error



992 associated with the mean diameter, using as reference the volume-weighted mean diameter
993 calculated with all available particles.



994

995 **Figure 18.** Volume-weighted mean diameter vs number of particles relationship calculated for 500 grains
996 incremental bins. Standard error (± 1 and 5%) intervals are calculated with respect to the average diameter

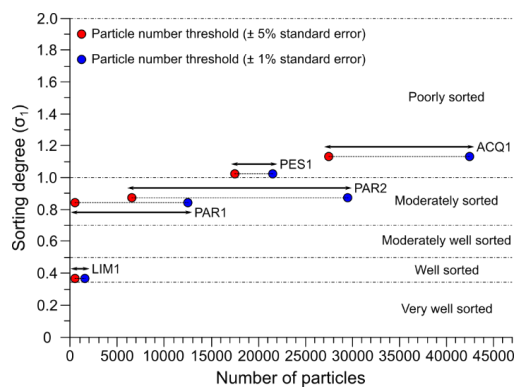


997 obtained from the entire grain size datasets (red dashed line). (a) LIM1 beach sample. (b) PAR1 fluvial sample.
998 (c) PAR2 fluvial sample. (d) PES1 fluvial sample. (e) ACQ1 fluvial-deltaic sample. n, number of particles.

999 To do so, we calculated the volume-weighted mean diameter at incremental steps of 500
1000 particles and we checked the deviation with respect to the reference value. At every
1001 calculation step, particles were randomized using a modified shuffle Matlab® algorithm to
1002 avoid any bias in particle extraction. We assumed two different confidence levels compiled
1003 at $\pm 1\%$ and $\pm 5\%$ standard error of the average diameter obtained with all available particles
1004 (Fig. 18). For LIM1 beach sand sample, volume-weighted mean diameter lays just outside
1005 the $\pm 1\%$ standard error interval, using only 500-1,000 particles, while it becomes more
1006 stable and between $\pm 1\%$ standard error for datasets $> 1,500$ grains (Fig. 18a). For this
1007 sample the minimum particle number is low due to the good sorting degree. PAR1 fluvial
1008 sand sample displays average diameter values always between the $\pm 5\%$ error interval
1009 (already for 500 grains), but only using 12,500 particles or more, the calculated values fall
1010 in the $\pm 1\%$ standard error (Fig. 18b). PAR2 sample shows a more marked scattering of data
1011 for limited particle number ($< 5,000$ grains), while the critical $\pm 5\%$ error threshold is attained
1012 at 6,500 grains and the more restrictive $\pm 1\%$ standard error is achieved for 29,500 particles
1013 (Fig. 18c). Mean diameter values for PES1 sample are characterized by strong variations
1014 up to 5,000-7,000 used grains, while they become more stable above 10,000 particles,
1015 reaching the $\pm 5\%$ standard error threshold at 17,500 particle and the $\pm 1\%$ error at 21,500
1016 grains, respectively (Fig. 18d). Eventually, the poorly sorted ACQ1 sample displays volume-
1017 weighted mean diameter values outside the $\pm 5\%$ error interval up to 10,000-15,000 grains.
1018 At least 27,500 particles are needed to calculate average diameter values in the $\pm 5\%$
1019 standard error interval and 42,500 grains must be used to achieve the $\pm 1\%$ threshold (Fig.
1020 18e). A decrease of sorting degree (widening of granulometric curves) from 0.37 to 1.137
1021 causes an increase in the minimum number of particles to be used in average diameter
1022 calculation from 500 to 27,500 to reach the $\pm 5\%$ standard error threshold (Fig. 19). To attain



1023 the $\pm 1\%$ error interval on the same samples, 1,500 to 42,500 particles are required (Fig.
1024 19). We tested the importance of the number of particles used in sample with relatively
1025 simple size distribution curves (single mode and gentle curve asymmetry).



1026

1027 **Figure 19.** Critical particle number vs sorting degree relationship calculated for the 5 analyzed samples based
1028 on volume-weighted mean diameter calculations.

1029 It is likely that samples with poorer sorting, multi-mode distributions and stronger asymmetry
1030 could require even larger particle amounts (Friedman, 1962a; Heilbronner and Barrett, 2014;
1031 Lopez-Sanchez, 2020). This aspect should be carefully considered when extracting average
1032 particle diameter from small datasets and results should be treated cautiously, being aware
1033 of the low reliability induced by limited data.

1034

1035 **6.5 Fields of application and usefulness of the proposed method**

1036 Volume-weighted mean diameter proved to be a reliable parameter to describe 3D grain
1037 size distribution from 2D grain size datasets acquired through image analysis applied on thin
1038 sections. The addition of sample-specific λ shape correction factors facilitates the
1039 conversion from 2D to 3D grain size distributions. Moreover, the calculation formula is
1040 straightforward and can be easily used, without requiring specific stereological-



1041 mathematical knowledge (Elias, 1967; Underwood, 1970; Russ, 1986; Gallagher et al.,
1042 2023). Our tests have been performed on loose sand samples, but the volume-weighted
1043 mean diameter could be particularly useful in the case of cohesive and hardened granular
1044 media not suitable to be analyzed through other laboratory techniques (optical granulometry,
1045 electro-resistivity methods, pipette, or sedimentation). Grain size analysis on such sample
1046 types must be conducted by means of microscopy characterization in conjunction with image
1047 analysis technique (Krumbein, 1935). Basic image analysis software, such as ImageJ,
1048 provides every required factor to be inserted in the calculation equation (Schneider et al.,
1049 2012). We preferred to manually digitize all the 2D grain size datasets employed to set the
1050 mean diameter formula, to achieve the maximum precision in defining particle shape and
1051 outer boundaries. However, as this procedure is extremely time consuming (7-10 days of
1052 work for each thin section image), it may be seen as poorly viable and suitable in the case
1053 numerous samples to be analyzed (Heilbronner and Barrett, 2014). In the past years, many
1054 efforts have been made to process large number of images both with semi-automatic and
1055 automatic methods (Mazzullo and Kennedy, 1985; Eicken, 1993; Heilbronner and Bruhn,
1056 1998; Ketcham, 2005; Mock and Jerram, 2005; Gualda, 2006; Berger et al., 2011; Lopez-
1057 Sanchez and Llana-Fúnez, 2016). Image segmentation has become a more reliable,
1058 efficient and easy procedure, leading to the acquisition of thousands of grain size data in
1059 few hours of processing with acceptable errors (Heilbronner and Barrett, 2014). In recent
1060 years, some authors developed image segmentation algorithms which employ computer
1061 artificial intelligence and machine learning processes in particle segmentation, further
1062 reducing data acquisition time (Saxena et al., 2021). By taking advantage of these recent
1063 techniques, users should not be concerned about the minimum number of representative
1064 particles to be used in calculating volume-weighted mean diameter, even at the highest
1065 desired precision intervals. Following this, we encourage scientists of different research
1066 areas, to experiment and test the usefulness of the proposed corrected volume-weighted



1067 mean diameter as it provided precise and reliable results in samples with different textural
1068 characteristics, grain size distributions and mineral compositions.

1069

1070 **7. Concluding remarks**

1071 The correct measuring of particle size distributions and particle-grain mean diameters is
1072 fundamental in the study and characterization of both natural and artificial granular media.
1073 Several analytical procedures and calculation equations have been set up in the last
1074 decades. However, the comparison between 2D and 3D datasets acquired with different
1075 techniques is not straightforward. To help addressing this issue, we proposed the use of
1076 volume-weighted mean diameter, an easy-to-use equation designed to define 3D equivalent
1077 particle diameter from 2D datasets gained through image analysis technique. The corrected
1078 volume-weighted mean diameter equation that has been set is capable of accurately
1079 describing grain size distribution on different sample types. Apart for the volume-weighting,
1080 the equation takes also into account particle shapes and is suitable for granular samples
1081 with different textural characteristics and mineral compositions. The following conclusive
1082 points can be drawn from our study:

1083 1- Volume-weighted mean diameter provides matching results with particle size data
1084 gained through optical granulometry technique, and combined with thin sectioning,
1085 can be useful in the case of weak or sensitive samples that can be partially
1086 compromised by laser diffraction or other analytical methodologies. In such sample
1087 types, 2D image analysis grants much more conservative and representative results
1088 than laser granulometry.

1089 2- Employing both laser granulometry and image analysis datasets, volume-weighted
1090 mean diameter returns close results compared to the methods of moments



1091 (arithmetic mean) equation. Conversely, other calculation formulas (geometric mean
1092 of method of moments, geometric mean of graphical method, median, and mode)
1093 proved to be less reliable and more sample sensitive (goodness of results may vary
1094 according to sample sorting and skewness).

1095 3- The calculation of accurate and precise average diameter values requires an
1096 increasing particle number following the diminishing of sorting degree (widening of
1097 grain size distribution). However, automatic to semi-automatic particle identification
1098 and image analysis processing could help in reducing the time required for the
1099 acquisition of such large particle datasets.

1100 4- The adoption of volume-weighted mean diameter provides reliable data and allows
1101 the estimation of 3D average diameter from 2D particle datasets. This process is
1102 based on a relatively simple equation, employing basic input parameters, without
1103 recurring to advanced stereology concepts or difficult mathematical equations.

1104 Given the summary points described above, we suggest researchers working on different
1105 disciplines dealing with particle size determination to test the volume-weighted mean
1106 diameter equation and check whether it could be a viable solution for straightforward mean
1107 diameter calculation from 2D data distributions.

1108

1109 **Declaration of competing interests**

1110 The authors declare that they have no known competing financial interests or personal
1111 relationships that could have appeared to influence the work reported in this paper.

1112

1113 **Author contributions**



1114 Mattia Pizzati: Conceptualization, Supervision, Data curation, Formal analysis,
1115 Methodology, Writing original draft, Writing - review & editing, Validation.

1116 Luciana Mantovani: Conceptualization, Data curation, Formal analysis, Methodology,
1117 Writing - review & editing.

1118 Antonio Lisotti: Conceptualization, Data curation, Methodology.

1119 Fabrizio Storti: Conceptualization, Supervision, Writing - review & editing.

1120 Fabrizio Balsamo: Conceptualization, Supervision, Writing - review & editing, Validation,
1121 Funding acquisition.

1122

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1131

1132 **Supplementary material**

1133 Details regarding the standard operating procedures adopted in optical granulometry
1134 analyses, XRD patterns, and high-resolution thin section photomosaics shown in Fig. 11 are
1135 reported in the online Supplementary material.



1136

1137 **Appendix 1**

1138 Hereafter are listed and explained the equations of the calculation formulas used in
1139 comparing particle diameter values in tables 2 and 3. We adopted the equations
1140 implemented in GRADISTAT, grain size statistical analysis software (Blott and Pye, 2001).
1141 Arithmetic and geometric means from the method of moments have been used (Krumbein
1142 and Pettijohn, 1938), and the first one is defined as:

1143
$$\bar{x}_a = \frac{\sum_{i=0}^{i=n} f m_m}{100} \quad (A1)$$

1144 where, \bar{x}_a is the arithmetic mean, $f m_m$ stands for the frequency percentage of particles at the
1145 midpoint (m) of each size class (i).

1146 Conversely, the geometric mean of the method of moments is given by the equation:

1147
$$\bar{x}_g = \frac{\sum_{i=0}^{i=n} f \ln m_m}{100} \quad (A2)$$

1148 where, \bar{x}_g is the geometric mean, $f \ln m_m$ is the logarithmic frequency of particles at the
1149 midpoint (m) of each size class (i).

1150 The graphical method has been employed as well, with the geometrical mean and sorting
1151 degree (Folk and Ward, 1957; Folk, 1974). The geometrical mean diameter is described by
1152 the equation:

1153
$$M_G = \exp \frac{\ln P_{16} + \ln P_{50} + \ln P_{84}}{3} \quad (A3)$$

1154 where, M_G is the geometrical mean and P_{16} , P_{50} and P_{84} are the particle diameter values in
1155 metric units at the 16, 50 and 84% cumulative percentile of the particle size distribution
1156 curve, respectively.



1157 Sorting degree (σ_1) is provided by the standard deviation associated with the logarithmic
1158 mean (Folk, 1974) and is given by the equation:

$$1159 \sigma_1 = \frac{\Phi_{84} - \Phi_{16}}{4} + \frac{\Phi_{95} - \Phi_5}{6.6} \quad (A4)$$

1160 in which, Φ is the grain diameter in phi units, at 5, 16, 84 and 95% cumulative percentile
1161 values of the particle size distribution curve, respectively.

1162

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