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1 2	Particle size distributions in Earth Sciences: a review of techniques and	
3	a new procedure to match 2D and 3D analyses	
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10	ABSTRACT	
11	Particle size is an essential tool in many research areas including Earth Sciences, Engineering,	Deleted: spanning from
12	Material Sciences, Soil Sciences and Pharmacology, among others. Over the last decades,	
13	several techniques and methodologies have been developed to calculate particle size	
14	distributions on different sample types (i.e., cohesive versus loose), from volumetric (3D) to	Deleted: spanning
15	image-aided (2D) analyses. Here, we (1) present a critical review of most commonly used	
16	techniques to calculate particle size distributions from cohesive and loose samples, and (2) we	
17	illustrate a new calculation formula to extract reliable 3D grain size distributions from 2D	
18	datasets. We propose the use of the "corrected volume-weighted mean diameter" $(D_{w}),$ as a	
19	new particle size descriptor, which results from the summation of products between equivalent	
20	particle diameter and particle volume, divided by the total volume of analyzed particles. In this	
21	calculation, particles were approximated to perfect circles-spheres, but a shape correction	
22	factor was applied to consider deviations from the perfect spherical shape. We tested the	
23	accuracy of D_{w} calculation formula by analyzing 2D datasets acquired from thin sections of 5	
24	selected granular sand samples having different mean grain diameters and grain size	



- 27 distributions (i.e., different sorting degree, grain size distribution width and skewness). Grains
- 28 were manually digitized, and per each thin section more than 5,000 particles were acquired.
- 29 Two-dimensional grain size distributions were cross-checked with the results provided via laser
- 30 diffraction granulometry on the same samples and were compared with previously published
- 31 and widely used calculation methods. Our promising results encourage the usage of D_w
- 32 formula as it provides best matching results with 3D laser granulometry and needs basic input
- 33 parameters that can be easily extracted from any image analysis software.
- 34

35 Keywords

- 36 Particle size distribution; equivalent diameter; volume-weighted mean diameter; granular
- 37 materials; image analysis technique; laser diffraction granulometry.
- 38
- 39 1. Introduction

40 1.1 Particle size analysis in Earth Sciences and beyond

- 41 The quantification of particle size distribution is a fundamental parameter to be determined in
- 42 different scientific disciplines including Earth and Planetary Sciences, Engineering, Life
- Sciences, Material Sciences, Soil Sciences, and Pharmacology. Particle size is defined as a
 scalar property of granular media and is typically calculated as the nominal diameter of
 particles (Udden, 1914; Wentworth, 1922; Krumbein and Pettijohn, 1938; Krumbein and Sloss,
 1963; Pettijohn et al., 1972). Particle size is a fundamental component of the texture of granular
- 47 materials (sediments, rocks, and aggregates) together with particle shape (Wadell, 1935;
- 48 Krumbein, 1941a; Moss, 1962; Krumbein and Sloss, 1963; Barrett, 1980;

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- 50 Mora and Kwan, 2000), rounding degree (Wadell, 1933; Powers, 1953; Taylor, 2002), surface
- 51 morphological features (Wentworth, 1919; Bowman et al., 2001; Russ, 1990), overall fabric
- 52 (particle preferred orientation) (Griffiths, 1961), and mineralogical composition
- 53 (Krumbein and Sloss, 1963; Folk, 1974; Boggs, 2009). In particular, in the field of Earth 54 Sciences, particle size determination plays a major role in stratigraphic and sedimentological studies where it provides fundamental information related to the physical and dynamic 55 transport processes (Krumbein, 1941b; Spencer, 1952; Folk and Ward, 1957; Bull, 1962; Sahu, 56 57 1964; Middleton, 1976; Goldbery and Richardson, 1989; Kranck, 1984; Pickering and Hiscott, 58 2015), provenance and maturity of clastic sediments and rocks (Dapples et al., 1953; Cadigan, 1961; Folk, 1974; Boggs, 2009; Garzanti, 2019), fluid storage potential of sedimentary 59 sequences (Fraser, 1935; Griffiths, 1952) and recognition of sedimentary environments (Keller, 60 1945; Buller and McManus, 1973; Mutti, 1992; Selley, 2001; Nichols, 2009). Particle size 61 quantification is also fundamental in structural geology studies, where the correct definition of 62 63 clast-grain size provides important information to constrain brittle deformation mechanisms 64 from fault rock analysis (Blenkinsop, 1991; Storti et al., 2003; Billi,
- 2005; Heilbronner and Keulen, 2006; Keulen et al., 2007; Luther et al., 2013; Montheil et al.,
- 66 2020), to understand the overall faulting processes (Engelder, 1974; Sibson, 1977; Marone
- and Scholz, 1989; Doan and Gary, 2009; Sammis and Ben-Zion, 2008; Balsamo and Storti,
- 68 2011), and to define plastic deformation styles (Ranalli, 1984; Freeman and Ferguson, 1986;
- 69 Stipp and Tullis, 2003; Passchier and Trouw, 2005; Hirsch, 2008; Lopez-Sanchez and Llana-
- 70 Fúnez, 2016). Planetary geology employs the analysis of particle size to unravel sedimentary
- 71 and surficial transport processes on terrestrial planets of the Solar System (De Pater and
- 12 Lissauer, 2001; Faure and Mensing, 2007; Bridges and Muhs, 2012; Grotzinger and Milliken,
- 2012), and to study meteoritic bodies (Dodd, 1976; Hughes, 1978a; Martin and Mills, 1978;
- 74 Eisenhour, 1996). Petrophysics takes into account the evaluation of particle size to understand
- 75 the primary and secondary porosity and overall fluid flow patterns and magnitude through



76 porous media (Tiab and Donaldson, 2004; Torabi and Fossen, 2009; Balsamo et al., 2010). 77 Hydrogeology studies deal with the quantification of grain size to document fluid pathways in deformed and undeformed rocks and soils (Davis and DeWiest, 1966; Fetter, 1994; Bense et 78 79 al., 2013). Particle size determination is also important in the field of diagenesis, as in the case 80 of ore-mineral deposits in conjunction with studies regarding structural geology (Jébrak, 1997) or selective cementation of sedimentary sequences (McBride et al., 1995; Mozley and Davis, 81 1996; Morad et al., 2000; Dutton et al., 2002; Cavazza et al., 2009; Van Den Bril and Swennen, 82 83 2009; Balsamo et al., 2012; Pizzati et al., 2018; Dimmen et al., 2020). Geomorphology employs 84 particle size analysis to identify the products of various geomorphic agents in different environments (marine, fluvial and continental) (Easterbrook, 1969). Glaciology extensively 85 86 implements particle size determination to quantitatively describe the past and present glacial-87 related deposits (different types of moraines, tills, and cryo-clastic materials) and to define glacier evolution over time (Washburn, 1979; Molnia, 1983; Eicken, 1993; Menzies, 2000). 88 89 Particle-crystal size is adopted also in petrology of both intrusive and effusive igneous rocks, 90 where it can provide constraints regarding crystal growth processes occurring inside magma 91 chambers

92 (Higgins, 1994; Means and Park, 1994; Bryon et al., 1995; Higgins, 2000; Zieg and Marsh,

2002; Mock and Jerram, 2005; Gualda, 2006; Morgan and Jerram, 2006; Jerram and Higgins,

- 2007; Jerram et al., 2009). Volcanology is particularly interested in particle size analysis to
 define the magnitude of past eruptions (Kaminski and Jaupart, 1998), to infer the explosivity
- 96 index (Giachetti et al., 2021) and to characterize the texture and sedimentary transport
- 97 mechanisms of volcaniclastic deposits (McPhie et al., 1993; Eychenne and Engwell, 2022).

The broad list of fields of application reported above helps to understand the critical importance of particle size determination as an effective tool to constrain a wide variety of physical processes. The techniques employed to calculate particle size distribution span from threedimensional volumetric analysis performed on bulk materials (e.g., classical sieve analysis 4



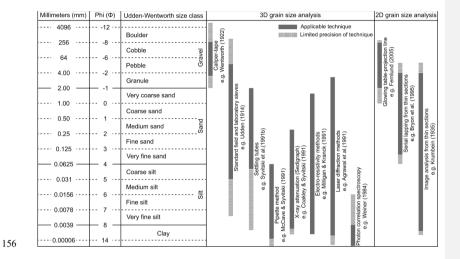
102	applied to loose samples) (Udden, 1914) up to two-dimensional automated-manual image	Deleted: bi
103	analysis (e.g., using thin section images of cohesive samples) (Heilbronner and Barrett, 2014).	
104	Nowadays, laser diffraction-based techniques provide accurate, precise, and relatively fast 3D	
105	particle size determination and are particularly effective in the case of loose powder samples	Deleted: is
106	(Agrawal et al., 1991). In the field of Earth Sciences, rock samples may show different degrees	
107	of cohesion, thus implying the use of different techniques in defining grain size distributions.	
108	Unfortunately, the direct comparison among results from different analytical procedures is not	
109	straightforward, thus limiting the ability of researchers to compare data obtained in different	
110	times and from different case studies. This limitation is even more important when results from	
111	3D and 2D analyses need to be compared. The reasons for such discrepancy between 3D and	
112	2D analyses lie, in the type of samples (Cortinovis et al., 2019), number of analyzed particles	Deleted: s
113	(Lopez-Sanchez, 2020), particle shape and density (Matthews, 1991a), and instrumental	
114	limitations associated with the resolution in the upper and lower grain size ranges (Syvitski et	
115	al., 1991a).	
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133	provided results matching well with optical granulometry data and proved to be a reliable and	(Deleted: well	matching
134	an easy-to-use tool to analyze samples with different particle size distributions, textures,			
135	sorting degrees, and mineralogical compositions.			
136				
137	1.2 Particle size distribution analysis techniques: a review			
138	Since the beginning of the last century, particle size was measured adopting the metric			
139	dimensional scale (Wentworth, 1922), which then became the standard sedimentological scale			
140	and it is still widely adopted nowadays (Fig. 1). However, in the following years, a base-2			
141	logarithm scale, also known as the phi-scale (Φ), was proposed (Krumbein, 1938; Krumbein			
142	and Sloss, 1963). Due to the diversity of objects to be characterized, particle size has			

- 143 historically been achieved through the adoption of several methods. The first and simplest
- 144 employed technique was the direct analysis of particles in the field by caliper or tape
- 145 measurements (Wentworth, 1922). This methodology was mainly used in the case of coarse-
- 146 $\,$ grained materials (coarse gravels, pebbles, cobbles, and boulders), for which size
- 147 determination was easier, but could not be applied with the same precision to fine-grained
- 148 media. Sieve analysis has been, and it still is, largely adopted to quickly define the particle size
- 149 $\,$ of loose granular media and works well in the case of coarse to medium-grained samples
- 150 (Udden, 1914; Rosenfeld et al., 1953; Friedman, 1962a; Van Der Plas, 1962; Krumbein and
- 151 Sloss, 1963; Folk, 1966). However, this method struggles in properly characterizing the size of
- 152 fine-grained fractions (< 31-62.5 µm), which must be analyzed with other, specifically designed,
- 153 techniques (Krumbein, 1932; Singer et al., 1988; Bianchi et al.,
- 154 1999) (Fig. 1).





157 Figure 1. Most common techniques applied in grain size analysis with analytical upper and lower size 158 boundaries. For a comprehensive literature background of the reported methodologies the reader is referred to 159 the introduction section 1.2.

160 The adoption of electro-formed sieves may extend the granulometric range down to the fine 161 silt size (> 5 µm), however this procedure is impractical and requires specifically designed sieves. Sieving allows the definition of the intermediate axis of particles, considering particles 162 163 as anisotropic ellipses, defined by a major (a), intermediate (b) and a minor (c) axis, and can be used to build mass or volume distribution curves (Bush, 1951; Adams, 1977). Sieving is 164 165 typically coupled with sedimentation and pipette analysis to cover the finest (clay and silt-size particles) fractions of granular samples (Syvitski et al., 1991a; Krumbein and Pettijohn, 1938; 166 167 McCave and Syvitski, 1991). However, these techniques may show pitfalls in matching sieving 168 and sedimentation-pipette results in one single granulometric curve and are also time-169 consuming and not suitable to analyze large sample amounts (Syvitski et al., 1991b; 170 Beuselinck et al., 1998; Bittelli et al., 2019) (Fig. 1). For coarse-grained granular samples (sizes 171 > 2 mm), image analysis applied to particles or grains manually dispersed on a glowing table 172 was adopted and the projection of the particle boundaries was used to reconstruct their volume 7

Deleted: technique



174 and size (Fernlund, 2005). Such a technique proved to be useful in the case of relatively coarse 175 and well disaggregated samples, while it showed limitations dealing with fine-grained or 176 aggregate particles (Fig. 1). The detailed analysis of particle images was implemented also in 177 digital sieving software, coupled with statistical programs (Matlab®), particularly useful to 178 determine the size of loose medium to coarsegrained materials (Kwan et al., 1999; Tafesse et al., 2012). Again, the limitations of this methodology reside in the scarcely representative 179 180 number of analyzed particles and in the relatively tiny grain size span that can be considered 181 (Fig. 1). In the last decades, the introduction of light diffraction instruments allowed to 182 automatically analyze samples with wide grain size ranges (from clay to gravel) in a single analytical process (de Boer et al., 1987; Agrawal et al., 1991; Blott et al., 2004; Sperazza et 183 184 al., 2004; Bah et al., 2009). Optical granulometry provides reliable and relatively quick analyses, resulting particularly indicated in the case of numerous samples (Kimura et al., 2018; 185 Brooks et al., 2022). However, reliability of results may depend upon the chosen instrumental 186 187 parameters, which should be carefully tested to minimize sample alteration (Matthews, 1991; 188 Konert and Vandenberghe, 1997; Blott and Pye, 2006; Storti and Balsamo, 2010; Schulte et 189 al., 2016; Celia Magno et al., 2018; Cortinovis et al., 2019). Moreover, sample treatment, either chemical or mechanical, before the analysis must be conducted carefully to avoid incorrect or 190 191 biased results (Folk, 1974; McCave et al., 1986; Matthews, 1991; Maithel et al., 2019). 192 Laserdiffraction-based instruments tend to underestimate the clay fraction especially in the 193 case of particles with equivalent diameter finer than 0.1 µm (Sperazza et al., 2004; Brooks et 194 al., 2022). This issue is mainly related to the dispersion medium, and techniques adopted by 195 most of the available equipment, that are not designed to efficiently disaggregate 196 claydominated samples into their constitutive elementary particles (Fig. 1). Techniques relying on electro-resistivity methods, such as the widely used Coulter Counter, measure particle 197 volume based on variations of electrical field induced by grains of different size dispersed in 198 199 an electrolyte dispersant, which are recorded as electrical pulses with different intensities



200 (Milligan and Kranck, 1991; Beuselinck et al., 1998; Roberson and Weltje, 2014). In a similar 201 way to laser granulometers, electro-resistivity-based instruments have wide applicability in 202 term of particle size but struggle in the clay range (< 2 µm) (Fig. 1). X-ray particle attenuation 203 technique (Sedigraph) uses the attenuation of incident radiation caused by sample suspended 204 in a dispersion medium to calculate the concentration of particles settling from suspension (Coakley and Syvitski, 1991; Bianchi et al., 1999; Celia Magno et al., 2018). This method is 205 206 accurate in analyzing particles with equivalent diameter from 1 to ~300 µm, while it provides 207 less reliable results outside this grain size interval (McCave and Syvitski, 1991; Cheetham et 208 al., 2008) (Fig. 1). Photon correlation spectroscopy uses the fluctuations of light diffraction generated by Brownian motion of particles suspended in liquid media (Weiner, 1984). This 209 210 technique is capable of efficiently define the size of particles with equivalent diameter down to 211 1 nm, thus including colloids and is particularly reliable in the clay size range (Fig. 1).

The techniques described above are particularly indicated for loose or weakly cemented granular samples that can be easily disaggregated into the elementary constitutive particles. Among the methods involved in particle size analysis in the case of indurated or tightly cemented samples that cannot be easily disaggregated, thin sectioning coupled with petrographic analysis has been the most widely used for decades (Krumbein, 1935; Greenman, 1951; Packham, 1955; Friedman, 1958; Basumallick, 1964; Smith, 1966;

Kellerhals et al., 1975; Schäfer and Teyssen, 1987; Kennedy and Mazzullo, 1991; Francus,
1999; van den Berg et al., 2003) (Fig. 1). Within the thin section area particles accounted for
the analysis may be chosen through the grid point count technique (Chayes, 1949;

Friedman, 1965; Folk, 1966), the intersection line (Van Der Plas, 1962; Stauffer, 1966) or via manual-automatic identification (Grassy, 1943; Mazzullo and Kennedy, 1985; Kennedy and Mazzullo, 1991; Heilbronner, 2000; Ketcham, 2005; Heilbronner and Barrett, 2014). This latter procedure may be aided by image analysis software (Seelos and Sirocko, 2005; Schneider et al., 2012; Heilbronner and Barrett, 2014; Liu et al., 2021; Théodon et al., 2023). Image analysis



226 techniques can give good results in a wide span of particle sizes, from few mm down to the 227 clay fraction (~1 µm), provided that images allow a precise discrimination of fine particles. To 228 this end, image analysis can be performed at several scales of observation spanning from 229 optical microscopy, scanning electron microscopy (SEM) or with transmission electron 230 microscopy (TEM) according to the size of the object to be characterized (Fig. 1). Following thin section cutting, the grain size is determined as the apparent diameter of randomly 231 232 sectioned particles, which is generally lower than the real or maximum equivalent diameter, a 233 phenomenon known as the corpuscle effect (Wicksell, 234 1925; Rosenfeld et al., 1953; Burger and Skala, 1976; Boggs, 2009; Lopez-Sanchez and 235 Llana-Fúnez, 2016). In order to gain the real and maximum diameter, particles need to be cut 236 along the equatorial diameter, a peculiar configuration that is rather uncommon in sectioned 237 materials (Krumbein and Sloss, 1963). To avoid discrepancy between granulometric data gained from thin section analysis and other methodologies, several correction factors and 238 239 equations have been developed. Some of them rely on statistical (Chayes, 1950; Burger and 240 Skala, 1976; Kong et al., 2005), stereological (Elias, 1967; Russ, 1986; Sahagian and 241 Proussevitch, 1998; Gallagher et al., 2023), or theoretical-mathematical treatise (Krumbein, 1935; Sahu, 1966; Cruz-Orive, 1983), considering particles as perfect spheres randomly cut 242 243 along the thin section plane. Other correction methodologies apply statistical autocorrelation 244 functions (Panozzo Heilbronner, 1992), software-aided projections of digitized particle outlines 245 (Panozzo Heilbronner, 1983) or empirical correction equations (Harrell and Eriksson, 1979) to 246 compare results from image analysis with data acquired by sieving. Some authors attempted 247 to determine the real grain size distributions by sample serial sectioning to reconstruct the 3D 248 shapes of particles (Bryon et al., 1995; Cooper and Hunter, 1995). Nowadays, there is no univocal Uniquivocal? correlation function linking particle size data from 2D image analysis to 249 the corresponding 3D grain size distributions acquired either by sieving or light diffraction 250 251 techniques, because all available conversion tools are sample or method sensitive. This

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Commented [TB1]: Also known as the tomato salad problem or the cut effect.





253	problem prevents a direct comparison between grain size data gained by different analytical	Deleted: does not allow
254	techniques.	
255		
256	1.3 A new parameter to match 2D and 3D particle size analyses: volume-weighted	
257	mean diameter (D _w)	
258	The employed volume-weighted mean diameter (D_{w}) includes both the equivalent diameter	
259	and the shape of analyzed grains. We performed the calculation of volume-weighted mean	
260	diameter based on the entire grain size datasets that were extracted from each thin section.	
261	The adopted formula operates a weighting of particle diameters according to the volume of the	
262	equivalent spheres. Following this, a fine-grained particle influences the final average diameter	
263	less than a coarse-grained one. The formula employed for the calculations is:	
264	$\sum_{i=o}^{i=n} d^{i*} V^i$	
265	$D_w = (v_i) \tag{1}$	
266	$\sum_{i=0}^{i=n}$	
267	where d_i is the equivalent diameter of the circle having the same area of the traced grains, V_i	
268	is the converted spherical volume of grains and <i>i</i> is the number of grains used in the calculation.	
269	By developing the formula of spherical volume, equation 1 can be simplified as follows:	

270	$\sum_{i=0}^{l=n} \frac{\pi}{6} *_{di4}$	
271	$D_w = (_{i=n\pi di3})$	

 $\Sigma_{i=0} = \frac{1}{6}^*$ 272

(2)



- 262 Grain shape was also implemented in the final calculation of the proposed weighted mean
- 263 diameter. In particular, we considered the deviation of grains from the perfect two-
- 264 dimensional circular shape. To this aim, we adopted the λ shape correction factor (surface 265 area correction), which can be calculated from the raw grain size datasets extracted via 266 image analysis as follows (Johnson et al., 2021):

267
$$\lambda = K * (p^{grain})$$
(3)

- 268 where p_{grain} is the outer perimeter of the manually traced grain boundary and p_{circle} is the
- 269 circumference of the equivalent circle having the same area of the grain. K is a constant
- 270 value multiplying the perimeter ratio and can be simplified to 1 in the case of grains with 271 aspect ratio (elongation of particles) comprised between 1 and 10 (Davies et al., 2019; Song
- et al., 2020). In calculation of λ shape correction factor we used the average values of grain
- 273 perimeter and equivalent circle circumference to be inserted in equation 3, considering the
- 274 entire grain size dataset for each thin section. Following this, we implemented the average 275 λ correction factor in equation 2 to develop the corrected volume-weighted mean diameter 276 formula as indicated below:

277
$$D_{w} = \lambda * \left(\frac{\sum_{i=0}^{i=n} \frac{\pi}{a_{i}}}{\sum_{i=0}^{i=n} \frac{\pi}{a_{i}} d_{i}^{3}} \right)$$
(4)

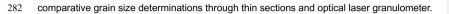
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279 4. Analytical methods

280 4.1 Sampled test sandy sediments

281 We collected 5 different granular sand samples that were used as benchmarks for



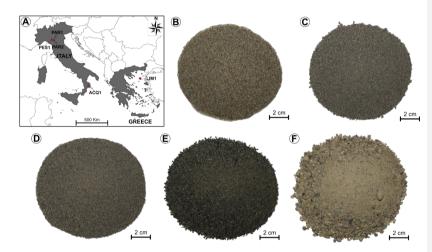


283 All samples were characterized by low to no cohesion and were easily collected by hand or

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- 283 with sampling tools. About 500 g of sandy materials were collected. Sand specimens belonged
- 284 to different sedimentological environments spanning from continental-fluvial (braided stream
- rivers) to shallow marine (beach and deltaic settings) (Fig. 2a).



286

- Figure 2. Geographical position and pictures of collected sand samples. (a) Central and Eastern Mediterranean Sea area showing the position of collected samples. (b) Sample amount LIM1 beach sand from Lemnos Island, NE Greece. (c) Sample amount PAR1 from the bottom of a fluvial sand bar collected in the Parma Creek, Northern Apennines. (d) Sample amount PAR2 from the top of a fluvial sand bar collected in the Parma Creek, Northern Apennines. (e) Sample amount PES1 fluvial sand from the Pessola Creek, Northern Apennines. (f) Sample amount ACQ1 deltaic sand from fossil fluviatile-shallow marine setting from Crotone Basin, Southern Apennines.
- Sampling strategy was aimed to collect sands with different modal compositions, average grain sizes and grain size distributions (different sorting degree, modal peak, curve shape and asymmetry). In particular, sample LIM1 was collected in a recent foreshore swashing zone along the eastern coast of Lemnos Island in the North Aegean Sea, Greece. The beach sand is medium-grained, well sorted, and displays high-textural maturity with rounded to subrounded grains mainly composed of quartz and lithic fragments (Fig. 2b). Three sand specimens were sampled from different braided stream type, creeks, of Northern Apennines in North Italy, with



301 samples PAR1 and PAR2 representing the bottom and the top of a recent fluvial sand bar along 302 the Parma Creek, respectively. The sand bar is interfingered with coarse gravel and boulder-303 cobble bodies. The sand samples are fine to medium-grained, with moderate sorting degree, 304 fair textural maturity with subrounded grains composed of quartz, feldspar, and silt-clay 305 aggregates (Fig. 2c and d). Conversely, PES1 sample was collected at the base of a recent slope debris talus slightly reworked by stream current along the Pessola Creek in the Northern 306 Apennines. The sand exhibits medium to coarse grain size, moderate to poor sorting, and low 307 308 textural maturity indicated by subrounded to subangular grains mainly composed of lithics and 309 subsidiary quartz and feldspar (Fig. 2e). Finally, ACQ1 sand sample was collected from a 310 Lower Pliocene age deltaic sandstone bar from the Crotone Basin in South Italy. Although this 311 sample belongs to a fossil siliciclastic deposit, the sandstone is almost devoid of any diagenetic 312 cements, thus allowing an easy sampling. This fluvial-deltaic sandstone is coarse-grained, poorly sorted and displays low textural maturity, with subangular feldspar grains dominating 313 with respect to rock fragments and quartz (Fig. 2f). 314

315

316 4.2 X-ray diffraction mineralogical analysis

The detailed analysis of the mineralogical composition of sampled sands was achieved through 317 318 X-Ray Powder Diffraction (XRPD) technique. Before the analyses, all samples were dried at 319 the controlled temperature of 35 °C for 48 hours and representative sand amounts (~2 g) were 320 manually milled in a jade mortar to attain an average grain size < 63 µm. A Bruker D2 Phaser 321 powder diffractometer with θ-θ focalizing geometry was used, operating at 30 kV and 10 mA 322 with Cu-Ka (λ = 1.54178 Å) radiation. Data were collected in the 5-60° 20 angular range, with 0.02° step size and 1 s/step counting time. Each sample was spun at 30 rpm. To identify the 323 324 crystalline phases EVA software (Bruker EVA, 2018) and the Crystallography Open Database (COD) were used. Semi-quantitative analysis of the detected mineralogical phases was 325 15

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327	conducted using the RIR method, adding a 10 wt% high purity Si standard in each sample.	
328	Through the adoption of semi-quantitative technique, the identification of clay minerals through	
329	emission peak position cannot be considered exhaustive. Further investigation and analysis of	
330	samples under different conditions (dry, heated, and swollen) would be required for a precise	
331	clay mineral identification but such in_depth analysis falls beyond the scope of the present	
332	study.	
333		
334	4.3 Laser-diffraction grain size analysis	
335	All granular samples were dried in an oven at the controlled temperature of 40 $^\circ C$ for two days	Deleted: to
336	to remove most of the water content. After sample drying, the total amount (~500 g) was sieved	
337	with a 2,000 μm mesh to remove grains with equivalent diameter coarser than 3,500 $\mu m,$ which	
338	represents the upper instrumental limit of the laser granulometer. By doing this, we slightly	
339	restricted the original grain size distribution of all samples, removing fine gravel sized grains.	
340	The alteration by sieving of original grain size distribution was the same for all samples. The	
341	original sample amounts were split in aliquots using Quantachrome Instruments macro and	
342	micro rifflers to achieve the sample mass required for grain size analysis (0.8-1.3 g) (Fig. 3a).	
343	This process also allowed creation of sub-samples still preserving the original grain size	Deleted: als
344	distribution of the total starting sample amount. Grain size analyses were performed with a	
345	Malvern Panalytical Mastersizer 3000 optical granulometer, with operating size range spanning	
346	from 10 nm to 3,500 μm (Fig. 3b). The instrument was equipped with an Aero S air-dispersed	
347	analysis unit, using pressurized air as particle dispersant medium (Fig. 3b). The adoption of air	
348	as dispersant allowed to analyze samples minimizing the alteration and mechanical	
349	disaggregation operated by commonly used liquid dispersant media (distilled water or alcohol).	
350	For all five analyzed samples, a specific standard operating procedure was set to give the most	Deleted: gra
351	reliable and reproducible analysis.	

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Figure 3. Instrumental apparatus and sample preparation used to perform laser diffraction analysis. (a) Macro and micro rifflers necessary to split the initial sample amount in sub-samples suitable to be inserted in the laser granulometer and to be dedicated to thin sectioning. (b) Mastersizer 3000 laser granulometer optical unit, equipped with an Aero S air-dispersion modulus with the dedicated analysis cell designed to work on incohesive granular media.

361 The operating procedures included several analytical-instrumental parameters to be set prior 362 to the definitive analysis. In our analyses, the granular sample quantity, laser power 363 obscuration, negative air pressure and feed rate were carefully tested (details are provided in Supplementary material 1). The granulometer has two different light sources producing two 364 laser beams with red (632.8 nm) and blue (470 nm) wavelength, respectively (Fig. 3b). 365 366 Calculation of the equivalent grain diameter was made via a light diffraction law, employing the Mie light scattering theory, which requires the refractive and adsorption indexes of particles. 367 368 Our granular materials are multi-dispersed (particles with different size and shape) mixtures of 369 several mineralogical phases including quartz, K-feldspar, plagioclase, mica, and rock 370 fragments in different proportions. Nevertheless, we adopted the optical parameters of 371 crystalline quartz, which is the most abundant mineral phase, with diffraction index of 1.54 and adsorption index of 0.1. This simplification was needed because the granulometer is not 372 designed to work on complex polymineralic assemblages. Particle volume was back-calculated 373

374 from light diffraction scattering distribution and, under the



- 373 assumption of perfect spherical objects, the equivalent diameter was calculated. Optical
- 374 diffraction is operated differently according to grain size, with fine particles producing wide
- 375 light scattering angles, while coarse grains induce low angles (Brooks et al., 2022). The
- 376 laser granulometer performs the calculation of equivalent grain diameter adopting the 377 method of moments as indicated in the generic formula below:

378
$$D[m, n] = (\sum_{u===nonVi*dinn--33})_{m-n}$$

(5)
 $\sum_{i=0}Vi*di$

1

- 379 in which V_i stands for particle volumetric density in size class d_i (median value of grain size
- 380 class), while *m* and *n* are the exponents to be substituted with different indexes according
- 381 to the adopted method of moments. In our case, the granulometer calculates the volume382 weighted mean diameter (De Broucker mean diameter or D[4:3]), adopting as indexes m
- and *n* in equation 5, 4 and 3, respectively. The granulometer also provides the span, or the
- width of the grain size distribution curves calculated at half height of modal peak, accordingto the formula:

386
$$Span = d_{(x,0.9)-d(x,0.1)}$$

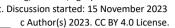
(6)
 $d(x,0.5)$

where, *d* is the equivalent particle diameter value at 0.1, 0.5 and 0.9 thresholds of the grain
size distribution, and *x* can be substituted according to the distribution type adopted during
the analysis (number or volume of particles). Optical granulometric analyses were replicated
on 5 aliquots of each sample. Grain size distribution curves were averaged to obtain mean
grain diameters and related parameters with associated standard deviations.

392

https://doi.org/10.5194/egusphere-2023-2636 Preprint. Discussion started: 15 November 2023



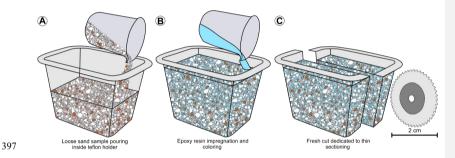


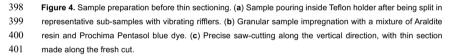


393 4.4 Thin sectioning technique of loose sand samples



- 393 Petrographic thin sections having thickness of 30 µm were made from granular sand samples.
- 394 To prevent any preferential grain orientation and to preserve the original grain size distribution,
- 395 all samples were split with macro and micro rifflers, and several aliquots were added into Teflon
- 396 containers (Fig. 4a).





402 Typically, 20-28 g of loose sand were used to fill 4 × 3 × 2.5 cm Teflon sample holders, with mass variations due to different sample density and grain size. Loose sand samples were 403 404 impregnated with a mixture of Araldite BY156 epoxy resin and Aradur 21 resin hardener (resinhardener mass proportion of 100:28), which was diluted to 10% of total volume with ethyl 405 406 acetate to grant lower viscosity. The mix was colored by adding a Prochima Pentasol (UN) blue 407 dye with a mass equal to 6% of the Araldite resin (Fig. 4b). The coloring provided a uniform 408 light blue background which helped in identifying grains and tracing grain boundaries. 409 Indurated samples were cut vertically, and the fresh cut was used to create petrographic thin sections (Fig. 4c). Thin rock slices were glued onto transparent glass using an Epoteck 301 410 411 epoxy resin mixed with Aradur 21 hardener (resin-hardener mass proportion of 20:5). Finally, 412 thin sections were manually polished with polycrystalline synthetic diamond powder, having a

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- 415 grain size of 1 µm, above a Tanganyika soft wooden surface. The polishing procedure was
- 416 needed to precisely identify grain mineralogy, to detect grain outer boundaries and to increase
- 417 the overall thin section transparency and quality.
- 418

419 4.5 Sand sample modal composition

The definition of the modal composition of sand samples was obtained by means of 420 421 petrographic analysis, with recognition of the principal mineralogical phases (quartz, feldspar, 422 and lithic fragments) in thin section. Quantification of areal percentage of minerals was done 423 on high resolution photomicrographs acquired with a Zeiss Axioplan 2 petrographic 424 microscope, equipped with a Leica MC 170 HD high sensitivity camera. Photomicrographs 425 were acquired at 12.5× magnifications (picture area of 4,747 × 3,560 µm) both under plane 426 and cross polarized light, to ease mineral identification. A total of 5 dedicated photomicrographs 427 were taken and analyzed for each sample. Sand samples were classified adopting the standard Q-F-L ternary classification diagram used for sandstones (Folk, 1974). 428

429

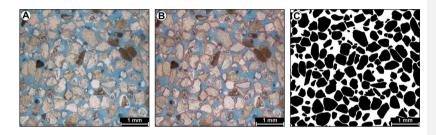
430 4.6 Particle size analysis through 2D image analysis

The analysis of grain size via image analysis on thin section was performed on petrographic photomicrographs acquired with the standard microscope setting described above. For each thin section, 48 to 64 photomicrographs were taken at 12.5× magnifications (picture area of 4,747 × 3,560 µm) under plane polarized light to cover the entire thin section area and were stitched together to form photomosaics. Photomosaics were imported and calibrated in ImageJ image analysis, open-source software (Schneider et al., 2012). Little processing was required



437 to enhance image quality mainly through brightness-contrast adjustments and noise-outlier

438 pixel removal (Fig. 5a).



439

Figure 5. Image analysis technique adopted to obtain 2D particle size distribution from the selected samples.
 (a) Original photomicrograph acquired at 12.5× magnification, composing the analyzed photo-mosaics. (b)
 Results of manually traced particle outer boundaries. (c) Transformed binary (black and white) photomicrograph
 used to extract particle equivalent diameter.

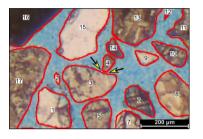
- 444 Grains were traced on modified photomosaics with ImageJ manual tracing tool, taking care to
- 445 keep a constant 2-pixel width of the traced boundaries (Fig. 5b). After digitization, grains were
- 446 identified by the software with color thresholding technique applied to red grain boundaries and
- 447 photomosaics were converted to binary images (black grains on white background) (Fig. 5c).
- 448 Special attention was paid to, drawing grain boundaries, to avoid grains in contact with each
- 449 other. In the case of touching grains, instead of operating image segmentation, we preferred
- 450 double-checking the results to find errors and mistakes during tracing, that were corrected by
- 451 manual separation of grains adding different color pixels (Fig.
- 452 6).

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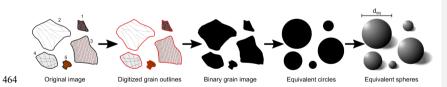
455

Figure 6. Double-checking of grains in contact with each other. Final digitized photo-mosaics quality check to 456 identify tangent grains which were manually segmented by adding pixels with different color from the red 457 particle outline (yellow arrows).

- 458 After image correction, grain size-shape data were extracted. For grain size, we extracted
- 459 the area fraction in μm² of grains which were approximated to perfect circles, and the 460 equivalent diameters were calculated from the inverse formula of the circle's area (Fig. 7):

$$461 \qquad d_{eq} = 2 * \sqrt{\frac{A}{\pi}}$$
(7)

462 where d_{eq} is the equivalent diameter of the circle having the same area of the particle and *A* 463 is the real area of the particle measured with image analysis.



- Figure 7. Sequence of progressive steps to perform manual image analysis and to extract particle equivalent
 circles and spheres. d_{eq}, equivalent particle diameter.
- 467 Values extracted from this formula composed the basis of the proposed volume-weighted
- 468 mean diameter. A total of 133,372 grains were considered and typically more than 5,000



- 469 grains were used in each thin section. Large datasets allowed to tune the volume-weighted
- 470 calculation formula and to minimize the effect of random grain sectioning (Krumbein, 1935;
 471 Friedman, 1958; Kellerhals et al., 1975; Kong et al., 2005). Grain size distributions were
- 472 created from the conversion of particle number into volume density percentage associated
- 473 with each grain size bin. Conversion was made considering the total volume of spherical474 shape grains divided according to the instrumental grain size classes adopted by the laser 475 granulometer. By doing this, we kept the same boundary and instrumental conditions for 476 both grain size data acquired through laser granulometry and image analysis, facilitating the 477 comparison.

478 Regarding grain shape, aspect ratio (AR) was calculated and used to describe the deviation 479 of grains with respect to the perfect circle. Aspect ratio was obtained by the formula:

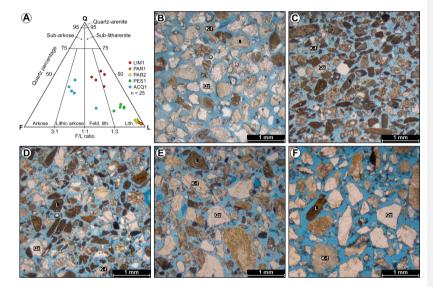
- 480 AR = Major____axis
 (8)
 Minor axis
- 481 where Major axis indicates the longest axis of the particle best fit ellipse (segment
- 482 connecting the two farthest points along the grain perimeter) and *Minor axis* stands for the
- 483 shortest axis of the best fit ellipse (segment having as tips the two closest points along the 484 grain perimeter).
- 485
- 486 5. Main results
- 487 5.1 Petrographic-mineralogical sample description
- 488 Micro-textural and modal analyses performed on the foreshore beach sand sample (LIM1),
- 489 point out a mineralogical composition made of almost equal proportions of quartz (38.8149053.32%) and lithic fragments (32.05-46.8%), while feldspar and plagioclase are subordinate



- 491 (8.37-20.17%) (Fig. 8a and b). Lithic fragments are mainly composed of calcite-aragonite
- 492 bioclasts, peloids, and to a lesser extent of metamorphic and igneous rock fragments. This
- 493 sample plots between the feldspathic litharenite and litharenite compositional fields in the



- 493 Q-F-L classification diagram (Fig. 8a). Grains are rounded to subrounded, with quartz being
- 494 more equant than feldspar and lithics which appear more elongate. Sorting degree is high with
- 495 grains of different mineral composition showing similar overall size.



496

497 Figure 8. Micro-textural characteristics and mineralogical composition of the collected sand samples. (a) 498 Ternary Quartz-Feldspar-Lithics modal classification diagram reporting the composition of studied sands (Folk, 499 1974). Sand composition was calculated from 5 photomicrographs per each sample. (b) Rounded to 500 subrounded siliciclastic and biogenic particles composing LIM1 beach sand sample. (c) Subrounded and 501 elongate lithic-dominated grains of PAR1 fluvial sample. (d) Subrounded lithic-dominated particles with lesser 502 extents of quartz and feldspar composing PAR2 fluvial sample. (e) Subangular and poorly sorted fluvial sand of 503 PES1 sample. (f) Angular to subangular, poorly sorted fluvial-deltaic sand composing ACQ1 sample. Q, quartz; 504 K-f, feldspar; L, lithic fragment; n, number of used photomicrographs.

505	The sand sample collected along the base of a fluvial bar (PAR1), displays a completely
506	different mineral assemblage compared to the beach sand. In particular, the modal analysis
507	returns a high lithic percentage (92.75-95.74%), while quartz (3-4.51%) and feldspar
508	(1.252.86%) compose the remaining areal amounts of the sample (Fig. 8a, c). Lithics have a

509 sedimentary origin with silt-clay aggregates incorporating fine-grained quartz and feldspar 26

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512 particles to produce coarse-grained aggregates. The fine-grained matrix of aggregates is 513 dominantly composed of muscovite and chlorite-group minerals, as confirmed by XRD 514 analysis. Metamorphic and igneous fragments are present as subordinate mineral 515 components. Due to the high lithic content, PAR1 sample can be inserted in the litharenite field 516 in the Q-F-L ternary diagram, close to the 100% lithic endmember (Fig. 8a). Grains are generally subrounded, with lithics exhibiting more anisotropic shapes with smooth outer 517 boundaries, while quartz grains are subangular with rougher boundaries. The sorting degree 518 519 is average with grains covering different grain size classes.

The sample from the top of the fluvial bar (PAR2), shows a mineral composition close to the 520 521 underlying PAR1 previously described, with lithics dominating with respect to quartz and 522 feldspar. Lithic fragments compose most of the areal percentage of the sample (88.6591.36%), 523 while quartz (4.01-6.72%) and feldspar-plagioclase (3.22-4.84%) are subordinate (Fig. 8a, d). 524 Lithics are mainly made of sedimentary aggregates of silt and clay-sized particles (muscovite 525 and chlorite), but a lesser content of metamorphic rock fragments occurs (polycrystalline quartz 526 grains). This sample can be inserted in the litharenite, lithicdominated field in the Q-F-L ternary 527 diagram, next to PAR1 sample (Fig. 8a). Lithic fragments are subrounded with highly elongate 528 shapes and smooth boundaries. Conversely, quartz grains are subangular to angular with 529 marked asperities and edges along the outer boundaries. Feldspar and plagioclase are 530 subrounded and grains display smooth perimeters. The sorting of the sample is average with 531 a considerable span through grain size classes.

The fluvial-reworked talus debris sample (PES1) is characterized by a mineral composition shifted towards lithics, with considerable amounts of quartz and feldspar. Again, lithic fragments constitute more than half of the sample (66.44-73.57%), followed by quartz (15.5-

535 21.62%) and feldspar-plagioclase (7.96-18.05%) (Fig. 8a, e). Most of lithics are composed of 536 ultramafic rock fragments (basalts, peridotites and gabbros), with lesser contribution from



537 metamorphic, hydrothermally altered rocks (serpentinites). Sedimentary lithic aggregates of 538 silt and clay, encasing siliciclastic particles, occur. The fine-grained matrix forming aggregates is composed of clay minerals as documented by XRD analysis (Supplementary material 2). 539 540 According to the Q-F-L ternary diagram, PES1 sample can be ascribed to the litharenite field, 541 although slightly enriched in quartz and feldspar with respect to PAR1 and PAR2 (Fig. 8a). Lithic fragment shape varies from subrounded to angular, with very rough outer boundaries. 542 Feldspar grains show subrounded and isotropic crystal form, while quartz has subangular to 543 544 angular shape. The sorting degree is poor, with particles displaying a wide grain size span.

- Finally, the sand sample collected from the deltaic sandstone bar (ACQ1) displays a mineral 545 546 composition with similar percentage of feldspar, quartz and lithics. In this sample, feldspar and 547 plagioclase compose most of the sample (31.58-43.81%), followed by quartz (18-44.83%) and 548 lithic fragments (17.9-50.41%) (Fig. 8a, f). Lithics have different composition, with igneous-549 intrusive terms (granites) dominating with respect to metamorphic (schists-gneisses) and 550 sedimentary ones (sandstones). Feldspar and plagioclase crystals are severely affected by 551 alteration to sericite minerals (muscovite and paragonite). ACQ1 sample can be inserted in the 552 lithic arkose field of the Q-F-L classification diagram (Fig. 8a), although one of the used 553 photomicrographs falls in the feldspathic litharenite field due to the heterogeneous distribution 554 of several coarse feldspar grains. Feldspar grains have subrounded shapes, while quartz is 555 subangular to angular. Lithic fragments of igneous origin have subangular shapes with rough outer boundaries, while sedimentary lithics are subrounded and more elongate, with smooth 556 557 boundaries. The sorting degree is low, with a wide span of grain size classes.
- 558

559 5.2 Laser-diffraction grain size analysis

560 Optical granulometry grain size analyses on loose samples were replicated with 5 aliquots of

561 equal mass, and the grain size distribution curves were averaged to obtain a mean grain 28

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diameter value and related parameters. The following results are presented considering thecalculated average grain size distribution curve for each sample.

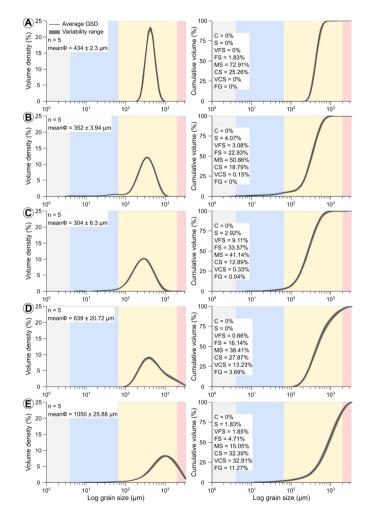
565 5.2.1 Beach sand sample (LIM1)

566 LIM1 sample displays a narrow grain size distribution curve, with subtle positive asymmetry. 567 The grain size distribution has intercepts with the X axis at 174 and 1,041 µm, respectively. 568 The calculated average grain diameter is $434 \pm 2.3 \ \mu$ m, with a modal value of $419 \pm 1.9 \ \mu$ m 569 and a median of 420 ± 1.9 µm (Fig. 9a). The span of grain size distribution is low (good sorting degree) with an average value of 0.665 \pm 0.01. All grains fall in the sand grain size interval with 570 571 the most recurrent size class being the medium-grained sand with 72.91% of particle volume 572 density. Coarse-grained particles compose 25.26% of the total sample volume, while the remaining 1.83% is due to the fine-grained sand fraction (Fig. 9a). 573

574 5.2.2 Basal fluvial sand bar sample (PAR1)

The sand sample collected along the basal surface of a fluvial sand bar along the 575 576 braidedstream Parma Creek (PAR1), is characterized by an average grain size distribution curve with medium width showing positive asymmetry. The left (finer) tail of the distribution 577 578 curve is more pronounced than the right (coarse) one with particles being detected at 2.9 µm 579 on the fine-ward side. Conversely, the right tail of the grain size curve intercepts the X axis at 580 1,182 μ m. The average particle diameter is 352 ± 3.9 μ m, with a modal value of 350 ± 1.9 μ m and a median of 328 ± 2.6 µm (Fig. 9b). Grain size distribution span is higher than the one 581 582 shown by the previous sample and the calculation returns a mean value of 1.343 ± 0.02. The 583 most recurrent grain size class is the medium-grained sand with 50.89% of particle volume 584 density. Fine-grained and coarse-grained classes compose 22.93% and 18.79% of the total 585 sample volume, respectively. Minor amounts of volumetric densities are measured in the silt 586 size (4.07%), very fine-grained sand size (3.08%), and in very coarse-grained sand size 587 (0.15%) (Fig. 9b).





588

Figure 9. Grain size distribution curve obtained through laser granulometer analysis. (a) Volume density and
 cumulative distribution for LIM1 sample. (b) Volume density and cumulative distribution for PAR1 sample. (c)
 Volume density and cumulative distribution for PAR2 sample. (d) Volume density and cumulative distribution for
 PES1 sample. (e) Volume density and cumulative distribution for ACQ1 sample. GSD, grain size distribution; Φ
 particle diameter; n, number of analyses; C, clay; S, silt; VFS, very fine-grained sand; FS, finegrained sand; MS,
 medium-grained sand; CS, coarse-grained sand; VCS, very coarse-grained sand; FG, fine gravel.



595 5.2.3 Upper fluvial sand bar sample (PAR2)

596 The medium-grained sand collected on the top surface of a sandy bar along the Parma Creek 597 (PAR2), displays an average grain size distribution curve with medium width and slight positive skewness. On the left tail, finest particles are recorded at 4.9 µm, while on the right tail coarsest 598 599 grains are detected at 1,343 μ m. The calculated average grain diameter is 304 ± 6.3 μ m, with 600 a mode at 286 \pm 3.3 µm (Fig. 9c). The span of the average grain size curve is higher than 601 previous samples, with a mean value of 1.608 \pm 0.03 and a median of 267 \pm 2.7 μ m. Higher span is recorded also by the particle volume distribution, with 41.14% of grains falling in the 602 medium-grained sand class and 33.57% of grains composing the finegrained sand size. A 603 604 considerable volume of particles falls in the coarse-grained sand size (12.89%), while only a small fraction is recorded in the very coarse-grained sand (0.33%) and fine gravel grain size 605 606 classes (0.04%). On the fine-ward side, no clay-sized particles are recorded, while silt-size and 607 very fine-grained sand classes compose 2.92% and 9.11% of the total sample volume, 608 respectively (Fig. 9c).

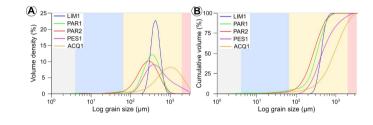
609 5.2.4 Fluvially-reworked debris talus sand sample (PES1)

The medium to coarse-grained sand sample collected from a debris talus reworked by river 610 611 stream (PES1) is characterized by an average grain size distribution curve with high width and 612 strong positive asymmetry. Grain size distribution tails are not symmetric, with the left one 613 being steeper than the right tail. On the left tail, finest grains are recorded at 81 µm, while on 614 the right tail coarsest particles reach 3,300 µm of equivalent diameter. The average grain diameter gained from the mean curve is $639 \pm 20.72 \ \mu$ m, with a modal value of $386 \pm 2.41 \ \mu$ m 615 and a median of 455 ± 8.6 µm (Fig. 9d). The span of average grain size curve is higher than 616 617 the samples described before, with a mean value of 2.495 ± 0.11 µm. Higher span can be 618 traced also in the volumetric particle distribution among grain size classes. In particular, the dominant grain size class is the medium-grained sand size with 38.41% of volume density. 619



- 620 Relatively high particle volumes are recorded also in the coarse-grained sand (27.87%), fine-
- 621 grained sand (16.14%) and in the very coarse-grained sand classes (13.23%). Minor amounts
- 622 of grains can be detected in the fine gravel class (3.69%) and in the very fine-grained sand
- 623 range (0.66%) (Fig. 9d).
- 624 5.2.5 Deltaic sand sample (ACQ1)
- 625 The coarse-grained sandstone collected along an exposed fossil deltaic bar (ACQ1) displays
- 626 a wide grain size distribution curve with a weak positive asymmetry. The average curve shows
- 627 asymmetric tails, with a steep right tail (coarse) and a gentle left tail (fine).
- 628 Finest particles are recorded at 8.1 μm, while coarse ones have equivalent diameters of
- $3,300 \ \mu\text{m}$. The average equivalent grain diameter is $1,050 \pm 25.88 \ \mu\text{m}$, with a mode of $1,020 \pm 25.88 \ \mu\text{m}$, where $1,020 \pm 25.88 \ \mu\text{m}$, whe
- $_{630}$ $57.92\,\mu\text{m}$ and a median of 897 \pm 27.1 μm (Fig. 9e). The span shown by the mean granulometric
- $_{631}$ curve is equal to 1.993 \pm 0.02 $\mu\text{m},$ slightly lower than PES1 sample. Data regarding single
- 632 grain size classes point out the high curve width. In this sample is difficult to identify a single
- dominant grain size class, since coarse and very coarse-grained classes compose 32.39%
- and 32.91% of total volumetric particle density, respectively. Considerable particle amounts are
- also displayed by medium-grained sand (15.05%) and fine gravel size classes (11.27%). Minor
- volumetric densities are recorded in fine-grained sand range (4.71%), very fine-grained sand
- class (1.85%) and in the silt grain size interval (1.83%). No grains have been measured in the
 clay-sized fraction (Fig. 9e).
- To summarize, from sample LIM1 to ACQ1 we record a coarsening of average grain diameter, a general broadening of grain size distribution curves (decrease of sorting degree), and a more marked asymmetry between left and right tails of the curves (Fig. 10a and table 1). The same observations can be made checking the cumulative grain size distributions, which show a progressive decrease of slope following an increase of grain size (Fig. 10b and table 1).





644

Figure 10. Comparison of grain size distribution obtained with air-dispersed laser granulometer. (a) Volume
 density grain size distributions. (b) Cumulative volume percentage grain size distributions.

647

648

Sample	Sample type	Age	D _m (µm)	D _{x10}	D _{x50} (µm)	D _{x90} (µm)	Mode	Span
name				(µm)			(µm)	
LIM1	Foreshore beach sand	Recent	434 ± 2.3	303 ± 1.87	420 ± 1.92	582 ± 4.15	419 ± 1.94	0.665 : 0.01
PAR1	Base of fluvial sand bar	Recent	352 ± 3.94	152 ± 1.48	328 ± 2.61	593 ± 9.76	350 ± 1.92	1.343 0.02
PAR2	Top of fluvial sand bar	Recent	304 ± 6.3	115 ± 1.34	267 ± 2.68	545 ± 12.18	286 ± 3.29	1.608 0.03
PES1	Talus debris reworked along river	Recent	639 ± 20.72	211 ± 1.92	455 ± 8.62	1350 ± 71.55	386 ± 2.41	2.495 0.11
ACQ1	Deltaic sandstone bar	Lower-Middle Pliocene	1050 ± 25.83	283 ± 8.02	897 ± 27.14	2070 ± 40.86	1020 ± 57.92	1.993

649

650 Table 1. Summary of grain size analysis via laser granulometry. D_m, average particle diameter; D_{x10}, D_{x50}, D_{x90},

grain size thresholds (percentiles) at 10, 50 and 90% of particle volume distribution.

652

653 5.3 Thin section-image analysis grain size distributions

654 Two-dimensional grain size analysis was based on data gained from petrographic thin sections

analyzed through image analysis technique. All grains composing the thin sections were

656 digitized to provide robust datasets which served to set the 3D volume-weighted mean

- diameter conversion formula (Fig. 11). 5.3.1 Beach sand sample (LIM1)
- 658 For the foreshore-beach sand sample LIM1, a total of 5,419 grains were acquired (Fig. 11a).
- 659 The resulting particle number grain size distribution curve has intercepts with the X axis at 40
- 660 and 756 µm and a mode of 352 µm. The volume density converted distribution shows a roughly



- 661 symmetric bell shape with a weak skew towards finer particles and a modal value of 390 μm
- 662 (Fig. 12a). The sorting degree is high as testified by most of the grains falling in the medium-
- 663 grained sand size class (87.54%), while lesser particle amounts are recorded in the fine-
- grained sand (6.89%) and in the coarse-grained sand intervals (5.29%). Only small fractions
- of silt-sized and very fine-grained sand material were detected, with percentage of 0.01% and
- 666 0.26%, respectively (Fig. 12a).



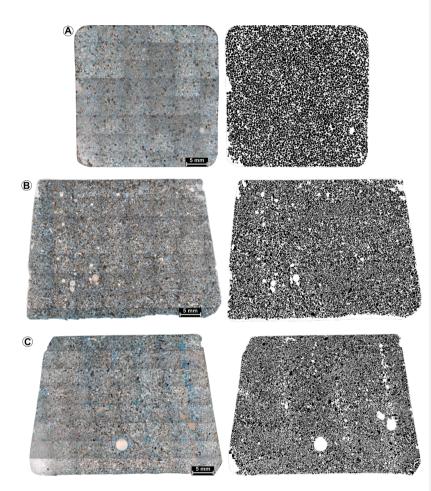




Figure 11. Original and binary photo-mosaics of the analyzed thin sections composed of tens of
 photomicrographs stitched together. (a) LIM1 beach sample. (b) PAR1 fluvial sample. (c) PAR2 fluvial sample.
 (d) PES1 fluvial sample. (e) ACQ1 fluvial-deltaic sample.

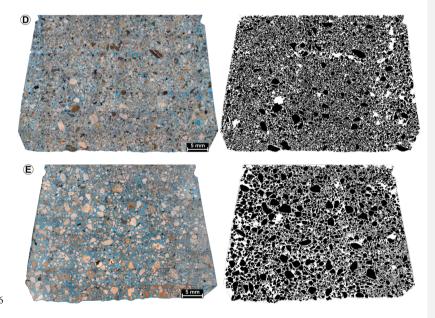
671

672 5.3.2 Basal fluvial sand bar sample (PAR1)





- 676 The fluvial sand bar sample PAR1 was analyzed by acquisition of 20,105 grains (Fig. 11b).
- 677 The particle number distribution describes a "bell-shape" curve, with the finest grains
- 678 recorded at 16.4 µm, coarsest ones at 859 µm and a mode of 186 µm. The density 679 volumetric distribution is described by a slight left asymmetry with a modal peak at 310 µm 680 (Fig. 12b). Sorting is lower compared to LIM1 sample, with a broader grain size distribution 681 as can be observed by particle volume density distribution through standard grain size 682 classes. The dominant size class is the medium-grained sand composing 59.04% of the 683 sample volume, followed by the fine-grained sand constituting 32.81% of volume density. 684 Lesser amounts of very fine-grained sand (3.32%) and coarse-grained sand (4.49%) have
- been detected. Silt-sized material composes only 0.33% of the analyzed sample (Fig. 12b).



686

687 Figure 11 continued.



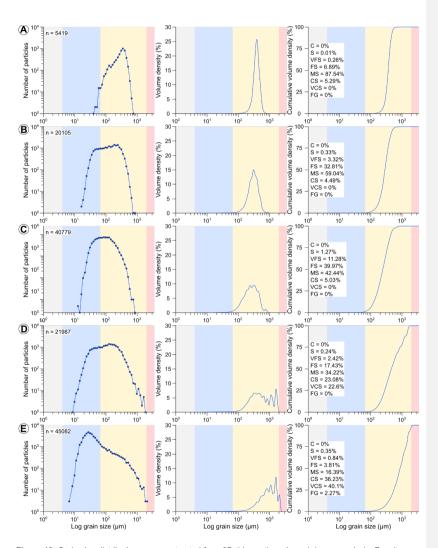
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Figure 12. Grain size distribution curves extracted from 2D thin sections through image analysis. Results are presented as number of particles, volume density and cumulative volume percentage distributions. (a) LIM1 beach sample. (b) PAR1 fluvial sample. (c) PAR2 fluvial sample. (d) PES1 fluvial sample. (e) ACQ1 fluvialdeltaic sample. n, number of particles. C, clay; S, silt; VFS, very fine-grained sand; FS, fine-grained sand; MS, medium-grained sand; CS, coarse-grained sand; VCS, very coarse-grained sand; FG, fine gravel.



694

695 5.3.3 Upper fluvial sand bar sample (PAR2)

40,779 grains were obtained from the second fluvial sand bar sample PAR2 (Fig. 11c). The 696 697 distribution of particle number is characterized by a symmetrical bell-shaped curve with finest recorded particles at 12.7 µm, equivalent diameter of coarsest grains up to 859 µm and a 698 699 modal value of 86.4 µm. Although we defined one single modal value, the modal peak 700 described is wide and most of the grains have equivalent diameter falling between 58.9 and 127 µm. Data converted in particle volume density show a left asymmetry of the distribution 701 702 curve and a modal peak at 310 µm (Fig. 12c). The width of the curve (i.e., sorting degree) is higher than the previous samples. Grains are almost equally distributed between the medium 703 and fine-grained sand size classes, with volume densities of 42.44% and 39.97%, respectively. 704 705 Significant particle volume is recorded in the very fine-grained sand size class (11.28%), while 706 only 5.03% of particles fall in the coarse-grained sand interval. Silt-sized material composes 1.27% of the total sample volume (Fig. 12c). 707

708 5.3.4 Fluvially-reworked debris talus sand sample (PES1)

709 PES1 sample, the reworked debris talus along the river stream, was analyzed by considering a total of 21,987 grains (Fig. 11d). The distribution by number of particles describes a wide, 710 711 almost symmetrical bell-shape, having as lower and higher intercepts with X axis at 8.68 and 712 1,850 µm, respectively. The modal peak is broad, with most recurrent data in between 111 and 240 µm size interval and a modal value of 127 µm. The volume density corrected curve 713 714 displays a left asymmetry with a modal peak of 352 µm and a right curve tail with oscillating volume density associated with coarser particles (Fig. 12d). The sorting degree is low as 715 716 indicated by the width of the modal peak. The volume density curve has a high width, testified by the significant spread of particles in different grain size classes. In particular, the most 717 718 recurrent size class is the medium-grained sand interval with 34.22% of total grains, followed 39

 \odot \odot



by the coarse-grained sand class composing 23.08% of the sample. Significant volume
densities of very coarse-grained and fine-grained sand are documented, with percentages of
22.6% and 17.43%, respectively. Small volume of very fine-grained sand material is recorded
(2.42%), together with silt-sized particles (0.24%) (Fig. 12d).

723 5.3.5 Deltaic sand sample (ACQ1)

724 Two-dimensional grain size of ACQ1 sample, collected along a fossil deltaic bar, was 725 investigated with a total amount of 45,082 grains (Fig. 11e). The number of grain distribution highlights an asymmetric shape with right skew, and finest particles recorded at 6.72 µm and 726 727 coarsest ones at 2,100 µm. The modal value of the distribution lies in the fine-grained interval at 27.4 µm. The volume density distribution curve displays a left asymmetry, with a gentle left 728 729 tail and a steep right tail showing marked data oscillations. The modal peak is located at 1,630 730 µm in the coarser end of the distribution curve and the sorting degree is low (Fig. 12e). In this 731 sample the dominant grain size fraction is the very coarse-grained sand with 40.1% of total 732 sample volume. Coarse and medium-grained sand classes compose 36.23% and 16.39% of total sample volume, respectively. Minor amounts of fine-grained sand (3.81%) and fine gravel 733 734 (2.27%) are also documented. Finally, tiny fractions of very fine-grained sand and silt-size 735 material compose the fine tail of the curve with 0.84% and 0.35% of volume density, respectively (Fig. 12e). 736

Summarizing the main results obtained from thin section analysis, we observe a progressive
broadening and coarsening of granulometric curves with different distribution of particles from
LIM1 to ACQ1 samples (Fig. 13a). In coarse-grained samples (PES1 and ACQ1) the coarse,
right tail of the distribution curves shows oscillating volume density values due to the presence
of a few tens of grains providing higher data scattering. The comparison of cumulative
frequency distribution confirms the diminishing of the slope due to lowering sorting degree (Fig.
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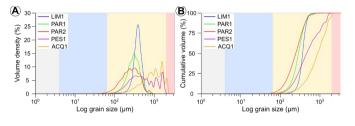






Figure 13. Comparison of grain size distributions obtained from image analysis technique applied to thin sections. (a) Volume density grain size distributions. (b) Cumulative volume percentage grain size distributions.

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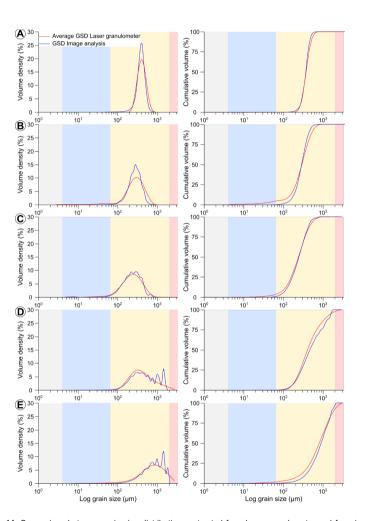
749 5.4 Laser granulometry vs. thin section grain size distributions

750 The comparison between volume density distribution curves acquired via optical granulometry 751 and thin section analysis, shows striking similarities (Fig. 14). For all the 5 considered samples both methods provide similar overall shape of grain size distributions with almost overlapping 752 753 modal peak values. Slight differences in modal peak height can be documented especially for 754 highly to moderately sorted samples (LIM1 and PAR1), in which the grain size distribution 755 curve obtained through image analysis has higher modal values compared to the laser granulometer data (Fig. 14a and b). On the same samples, the laser granulometer technique 756 757 recorded higher particle volumes in the right (coarse) tail of granulometric curve with respect 758 to image analysis data. Tiny differences can be seen in the left (fine) tail of curves, with LIM1 759 displaying smaller particle volume recorded by laser granulometry with respect to thin sections, 760 while the opposite occurs for PAR1 sample. For the other 3 coarser and less sorted samples (PAR2, PES1 and ACQ1) the match between the granulometric curves gained with different 761 methods is good and the intercepts with X axis are almost coincident (Fig. 14c-e). 762

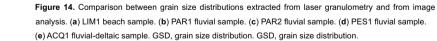
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769	The main differences are related to the right (coarse) tail of the curves, especially for PES1
770	and ACQ1 samples, where the thin section distribution curve displays volume density
771	variability in the coarser grain size range. This data variability is induced by few very coarse
772	(1-2 mm size) particles, which influence the final volume density distribution (Fig. 14d and e).
773	
774	5.5 Volume-weighted mean diameter calculation
775	Calculations of volume-weighted mean diameter were performed with the formula reported in
776	equation 2. The entire grain size datasets associated with thin sections of granular samples
777	were considered. The foreshore beach sand sample LIM1, returns a value of volume-weighted
778	mean diameter equal to 364.16 $\mu\text{m},$ while for the fluvial sand bar samples
779	(PAR1 and PAR2) mean values of 296.54 μm and 256.08 μm are obtained, respectively. PES1
780	fluvial coarse sand shows a volume-weighted mean diameter of 625.83 µm, and the fossil
781	deltaic sand ACQ1 sample provides a value of 955.79 $\mu\text{m}.$ All the obtained mean diameter
782	values are lower than the equivalent obtained through optical laser granulometry.
783	We then applied a surface area correction factor (λ), as indicated in equation 3, to consider the
784	deviations of grain shape from spherical particles (Fig. 15) (Davies et al., 2019; Johnson et al.,
785	2021). λ factor was calculated for every sample and implemented in equation 2 as indicated in
786	the modified volume-weighted mean diameter formula reported in equation 4. For LIM1
787	sample, the aspect ratio of grains spans from 1.01 to 7.01, with a mean value of
788	1.65 \pm 0.49, thus equation 3 can be simplified and returns an average λ value of 1.17 \pm 0.08
789	(Fig. 15a). By multiplying the volume-weighted mean diameter by λ factor, we obtain a
790	corrected grain diameter of 425.35 μm . PAR1 has grain aspect ratio falling between 1.01 and
791	12.84, with a mean value of 1.89 \pm 0.72, thus providing a mean λ correction factor of 1.19 \pm
792	0.11 (Fig. 15b).



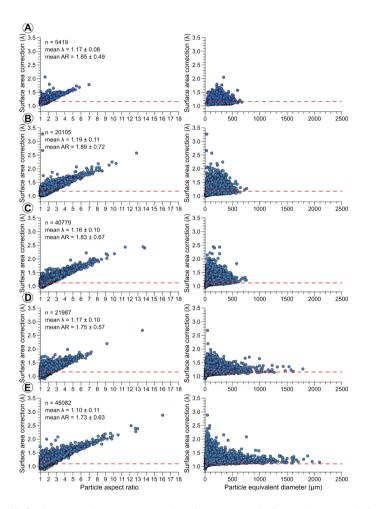




Figure 15. Graphs reporting the particle aspect ratio-surface area correction factor and particle equivalent
 diameter-surface area correction factor relationships for the analyzed sand samples. (a) LIM1 beach sample.
 (b) PAR1 fluvial sample. (c) PAR2 fluvial sample. (d) PES1 fluvial sample. (e) ACQ1 fluvial-deltaic sample.

The horizontal dashed red line indicates the average surface area correction factor. n, number of particles; λ,
 surface area correction factor; AR, particle aspect ratio.



800	The resulting corrected volume-weighted mean diameter is equal to 351.78 $\mu\text{m}.$ For PAR2	
801	sample, grains have aspect ratios from 1.0 to 13.88 with an average value of 1.83	Deleted: comprised
802	\pm 0.67, giving a mean λ value of 1.16 \pm 0.1 (Fig. 15c). The volume-weighted mean diameter	
803	corrected according to particle shape results 307.39 $\mu\text{m}.$ PES1 is composed of grains with	
804	aspect ratios spanning from 1.0 to 13.55, with an average value of 1.75 \pm 0.57, returning a	
805	mean λ correction factor of 1.17 \pm 0.1 (Fig. 15d). Applying the correction to equation 4, the final	
806	volume-weighted mean diameter is equal to 731.08 µm. Finally, ACQ1 sample is characterized	Deleted: Eventually
807	by grains with aspect ratios between 1.0 and 16.06 with an average value of	
808	$1.73\pm0.63,$ giving back a λ mean surface area correction factor of 1.10 ± 0.11 (Fig. 15e). The	
809	obtained corrected equivalent diameter for this sample is 1,055.64 $\mu\text{m}.$ Volumeweighted mean	
810	diameter displays values close to the ones obtained through optical granulometry. The only	
811	exception is PES1 sample, which has an average grain size measured with laser granulometry	
812	90-100 μm finer than the values calculated via image analysis on thin section.	
813		
814	6. Discussion	
815	6.1 Comparison between 2D (image analysis) and 3D (laser granulometry) grain size	
816	analyses	
817	Grain size distribution curves of analyzed samples obtained from 2D (image analysis) and	
818	3D (laser granulometry) methods show striking similarities. The overall shape, skew	
819	(asymmetry) and modal peak position is equal in both the adopted methodologies (Fig. 14).	
820	Slight differences can be traced in modal peak height, with data obtained through laser	
821	granulometry displaying typically lower modal height with respect to grain size distributions	
822	provided by image analysis from thin sections. Moreover, grain size distributions gained with	
823	the optical granulometer appear to be smoother especially on the coarser tail compared to	
824	image analysis data (Fig. 14). This can be explained by the usage of the 100 instrumental $$45\!$	

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827 grain size classes adopted by the laser granulometer, which were extended also to image 828 analysis grain size distributions. Such detailed subdivision of the 10 nm to 3,500 µm size 829 interval in tiny frequency bins, caused variations in the coarser end of grain size distributions 830 gained from image analysis. These variations are mainly related to the presence of a few tens 831 of grains in coarser grain size classes inducing volume frequency oscillations. We employed the very same grain size classes for both analytical methods to allow precise comparison of 832 data distribution, without the bias induced by different bin sizes. It is likely that the adoption of 833 834 the standard sedimentological grain size classes (Udden-Wentworth scale) (Udden, 1914; 835 Wentworth, 1922) could have provided more stable volume frequency results at the cost of less detail between different classes. Still, we preferred to prioritize and put emphasis on 836 837 evidencing small differences between grain size classes rather than achieving volume frequency stability across the whole grain size distributions. 838

839 The comparison of volume-weighted mean diameters extracted from granulometry data, and 840 the corrected volume-weighted mean diameters from image analysis technique provided 841 matching results for 4 out of 5 total sand samples. In particular, for LIM1 sample, laser 842 granulometry returned a mean equivalent diameter of 434 µm, while image analysis technique 843 gave 425.3 µm. Fluvial sand PAR1 showed an equivalent diameter from laser granulometry of 352 µm, with related volume-weighted mean diameter of 351.8 µm, while for PAR2 returned 844 845 diameter values of 304 and 307.4 µm, respectively. In the case of PES1, the laser granulometer measured a mean particle diameter of 639 µm, while data acquired with image 846 847 analysis provided a mean value of 731.1 µm. Finally, for the ACQ1 deltaic sand sample, 848 laboratory grain size analysis gave a mean diameter of 1,050 µm, while image analysis technique provided a value of 1,055.6 µm. The only deviation from matching results was 849 related to PES1 sample, which showed image analysis derived data 90-100 µm coarser than 850 851 the equivalent diameter measured via laser granulometry. We explain this difference 852 considering the mineralogical composition of the sample and the limits imposed by the involved 46

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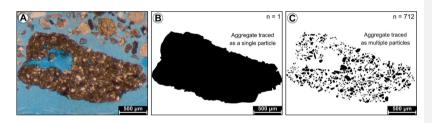
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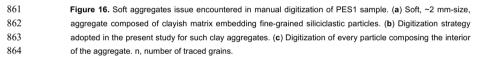




860

855	analytical techniques. Apart from quartz, feldspar, and plagioclase, PES1 sample is composed
856	of coarse aggregates of silt-clay matrix binding fine-grained siliciclastic grains (Fig. 16a).
857	During manual tracing of particle outer boundaries, we treated these aggregates as single
858	particles, without distinguishing the fine-grained particles interspersed within the matrix (Fig.
859	16b and c).





865	Thin sectioning of loose granular media, proved to be a conservative method in preserving the
866	original size and shape of weak sand framework components, minimizing the overall sample
867	alteration. Conversely, laser granulometry operated via pressured air dispersion may cause
868	alteration of original grain size in sensitive and mechanically weak samples (Storti and
869	Balsamo, 2010; Cortinovis et al., 2019). Before the analyses we performed tests to set the
870	instrumental parameters to be used giving the least sample alteration (Supplementary material
871	1). In the case of PES1, which is the weakest sample, even the adoption of the most
872	conservative analytical parameters was not enough to completely avoid sample damage, This
873	sample is the only one displaying aggregates whose matrix is made of clay minerals, which
874	could have been damaged during laser granulometry analysis. In PES1 some alteration,
875	related to splitting and partial disaggregation of soft silt-clay aggregates caused the fine-ward
876	shift of the average particle diameter. In such weak sample types, we considered data derived

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879	from image analysis technique to be more reliable and representative of the real grain size
880	distribution than laser granulometry analysis. The same alteration was not documented in the
881	other 4 samples likely due to their different mineral composition and higher relative particle
882	resistance, preventing any significant mechanical alteration of the original grain size during the
883	analysis.
884	
885	6.2 Volume-weighted mean diameter (D_w) vs. literature calculation methods
886	Mean particle diameter values based on optical granulometry and image analysis (corrected
887	volume-weighted mean diameter) methods were compared with previously published and
888	widely used calculation equations reported in the Appendix 1 (tables 2 and 3). In particular, we
889	focused on the comparison with the method of moments (both arithmetic and geometric
890	equation) (Krumbein and Pettijohn, 1938), the graphical method (geometric mean) (Folk and
891	Ward, 1957), median, mode, arithmetic mean and area-weighted mean diameter. In comparing
892	different equations, we assumed the mean diameter values extracted from the laser
893	granulometer as reference, with relative differences between calculation formulas expressed
894	as percentages (positive values represent grain diameter underestimation, while negative
895	ones indicate overestimation with respect to the reference) (tables 2 and 3). Considering laser
896	granulometry reference data, the arithmetic mean calculated with the method of moments,
897	provides close results with the ones gained with the mean diameter formula employed by the
898	optical granulometer (equation 5) (maximum difference in the average grain diameter of 0.36%
899	from the reference value). Conversely, the geometrical mean of method of moments returns
900	small percentage errors for well sorted samples (3.1% difference for LIM1 sample) with a
901	progressively increasing error following sorting diminishing (from 16.4 to 24.4% error in PAR1,
902	PAR2, PES1 and ACQ1 samples) (table 2).

903

Table 2: Comparison of results from different calculation equations applied to laser granulometry analyses



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	Method of moments		Graphical method	GSD laser granulometry					
Sample name	Arithmetic (µm)	Geometric (µm)	Geometric (µm)	Sorting	D _m (µm)	Median (µm)	Mode (µm)		
LIM1	434.7	420.5	420.6	0.37	434	420	419		
PAR1	352.9	294.3	319.8	0.845	352	328	350		
PAR2	305.1	252.7	261.1	0.877	304	267	286		
PES1	640.3	492.6	487.5	1.029	639	455	386		
ACQ1	1053.6 794.1		850.7	1.137	1050	897	1020		
Sample name	Complementary	percentage ratio wit	h respect to volume-v (%)	veighted n	nean diame	eter from laser g	granulometry		
LIM1	-0.16	3.11	3.09	-	0	3.22	3.45		
PAR1	-0.25	16.39	9.15	-	0	6.82	0.57		
PAR2	-0.36	16.87	14.11		0	12.17	5.92		
PES1	-0.20	22.91	23.71		0	28.79	39.59		
ACQ1	-0.34	24.37	18.98		0	14.57	2.86		

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2).

 Table 2. Comparison of results given by different calculation formulas for grain size distribution acquired through laser granulometry. Calculation equations are reported in the Appendix 1. GSD, grain size distribution; D_m, average grain diameter (laser granulometer).

908 The same increasing error trend can be seen for the geometric mean of graphical method, with 909 a maximum deviation of 23.7% calculated for PES1 sample. Finally, the median of distribution 910 curves is close to the mean diameter gained from laser granulometry only in the case of well 911 sorted samples (deviation of 3.2 and 6.8% in LIM1 and PAR1, respectively), while it deviates 912 far from it in more poorly sorted ones (PAR2, PES1 and ACQ1, with errors up to 28.8%). The 913 mode can approximate the average diameter only in the case of weakly skewed grain size 914 distributions (errors comprised from 0.5 to 5.9% in LIM1, PAR1, PAR2 and ACQ1), but it fails 915 in the case of strongly skewed ones (39.6% deviation in PES1) (table

Utilizing grain size distribution datasets extracted via image analysis (the corrected volume-

weighted mean diameter is used as reference) the best results are provided by applying the

arithmetic method of moments, with standard errors from 1.7 to 3.9% in all samples. As already

observed for laser granulometer size distributions, geometrical mean calculated with the

method of moments returns good results only for well sorted samples, and tends to

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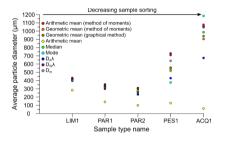
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926 underestimate the mean diameter up to 25.3% of reference value in poorly sorted sands (Fig.

927

17 and table 3).



928

929	Figure 17. Comparison of average particle diameter values calculated with literature equations and the proposed
930	volume-weighted mean diameter formula for the 5 samples. Used datasets are derived from thin sections
931	analyzed with image analysis. $D_A\lambda$, area-weighted mean diameter (shape corrected); $D_w\lambda$, volume-weighted
932	mean diameter (shape corrected). $D_{m_{r}}$ laser granulometer mean diameter. Similar results are extracted
933	from the geometric mean diameter formula of the graphical method, with the best result
934	achieved for LIM1 sample (4.2% mean diameter underestimation) and worst attained for PES1
935	sand sample (23.7% diameter underestimation). Adoption of the median value gives good
936	results for properly sorted samples (-0.4 to 7.7% in LIM1 and PAR1), while deviations become
937	bigger in poorly sorted ones (10.9 and 28.9% in PAR2 and PES1, respectively) (Fig. 17). The
938	mode follows similar trends and fails in describing weakly to poorly sorted granular media
939	(errors from -12.2 to
940	48.6% in PAR2, PES1 and ACQ1). Severe mean diameter underestimation is documented 932
941	in the case of simple arithmetic mean diameter and area-weighted mean diameter with 933

942 943

 Table 3: Comparison of results from different calculation equations applied to image analysis grain size data

 Method of moments
 Graphical method
 GSD Image analysis

standard errors reaching 94.1 and 41.3%, respectively (Fig. 17 and table 3).

									_
Sample name	Arithmetic (µm)	Geometric (µm)	Geometric (µm	n) Sorting	Arithmetic (µm)	Median (µm)	Mode (µm)	D _A λ (μm)	D _w λ (μm)
LIM1	415.4	403.2	407.5	0.329	283.8	427	411.2	401.4	425.3
PAR1	337.8	313.5	317.7	0.544	141.4	324.5	331	300	351.8
PAR2	302	264.6	267.2	0.757	98.63	273.9	256	232.7	307.4

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PES1	709.6	546.3	557.4	1.097	127.8	519.6	376	428.9	731.1
ACQ1	1079.1	906.5	940.5	0.901	62.4	989.1	1185	674.6	1055.6
Sample name	Com	plementary percen	tage ratio with r	espect to volu	ume-weighted r	mean diameter	from image a	analysis (%)	
LIM1	2.33	5.19	4.18	-	33.27	-0.4	3.31	5.62	0
PAR1	3.98	10.88	9.69	-	59.81	7.76	5.91	14.72	0
PAR2	1.75	13.92	13.08	-	67.91	10.89	16.72	24.30	0
PES1	2.94	25.27	23.76	-	82.52	28.93	48.57	41.33	0
ACQ1	-2.22	14.12	10.90		94.09	6.29	-12.26	36.09	0

946

947 Table 3. Comparison of results provided by different calculation formulas for grain size distributions gained with 948 image analysis. Calculation equations are reported in the Appendix 1. GSD, grain size distribution; $D_A \lambda$, area-949 weighted mean diameter (shape corrected); D_wλ, volume-weighted mean diameter (shape corrected). Summarizing the comparative results, the proposed corrected volume-weighted mean 950 951 diameter equation proves to be a reliable calculation formula and provides matching results 952 with the arithmetic method of moments, as well as with data gained from laser granulometry 953 technique. Conversely, the geometrical mean diameter of both method of moments and 954 graphical method can describe only well to moderately sorted samples, while it struggles in poorly sorted ones. The same deviations, with even bigger magnitudes, can be highlighted by 955 956 the adoption of the median and modal value as parameters describing grain size distributions. Similarly, the simple arithmetic mean, and area-weighted mean diameter are not reliable 957 calculation equations, and their usage should be avoided as they show the highest difference 958 959 from the reference (tables 2 and 3).

960

961

6.3 Shape correction factor (λ) vs. literature empirical correction parameters

962	In the past years, <u>many</u> efforts were made to achieve robust conversion factors that could <u>give</u>						
963	reliable 3D average particle diameter starting from 2D equivalent diameter distributions						
964	obtained with different analytical methods. Correction equations have been developed in						
965	different research areas of Earth Sciences from sedimentology, planetary geology, to structural						
966	geology. Correction coefficients are based on geometrical considerations						

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970 (Roethlisberger, 1955; Hughes, 1978b), statistical-mathematical relationships (Krumbein, 971 1935; Chayes, 1950; Greenman, 1951; Sahu, 1966; Rose, 1968; Johnson, 1994; Kong et al., 972 2005), empirical rules (Friedman, 1962a) or software aided simulations (Panozzo Heilbronner, 973 1992; Heilbronner and Bruhn, 1998). All these methods bring different correction coefficients 974 to account for mean diameter underestimation related to random particle sectioning. Correction values are between 1.0 and 1.5 and must by multiplied by the average grain 975 diameter obtained from image analysis performed on rock thin sections (table 4). We tested 976 977 the precision of equations proposed in literature by applying the correction coefficient to the volume-weighted mean diameter values obtained from the 5 studied sand samples. In this 978 979 process, we did not multiply the mean diameter by the λ shape correction factor, thus using only the raw, uncorrected volume-weighted mean diameter values (table 4). Such a procedure 980 981 allowed a direct comparison of λ shape correction factor with other correction parameters. By 982 using our grain size datasets, closest results compared to the ones obtained with equation 4, are gained employing the correction factors proposed by Friedman (1958, 1962b), Sahu 983 (1966), and Johnson (1994). Other correction methods (Krumbein, 1935; Chayes, 1950; 984 Greenman, 1951; Hughes, 1978b; Panozzo, 1982; Panozzo Heilbronner, 1992; Kong et al., 985 986 2005) typically tend to overestimate the average grain diameter by a significant margin (table 987 4). This is especially true in the case of poorly sorted, coarse-grained samples (PES1 and 988 ACQ1), while differences are less pronounced in well to moderately sorted and medium-989 grained ones (LIM1 and PAR1) (table 990 4). Although some of the correction methods discussed above provide close results with the shape corrected volume-weighted mean diameter values, we prefer to apply different λ 991 992 correction factors to different samples. This sample specific procedure should give more 993 reliable results, due to shape correction bound to the grain size distribution and particle form

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of each sample.

Table 4: Comparison of correction parameters with the presented original data





	Mear	n diamet	er of ana (µm)	alyzed s	amples	
Literature correction method	LIM1	PAR1	PAR2	PES1	ACQ1	Correction factor
Krumbein (1935), Chayes (1950), Kong et al. (2005)	463.65	447.88	337.5	796.81	1216.91	1.2732
Krumbein (1935)	477.27	388.64	335.62	820.21	1252.65	1.3106
Greenman (1951)	494.86	402.39	348.03	851.04	1299.63	1.3589
Friedman (1958), (1962)	430.18	350.30	363.12	739.29	1129.07	1.1813
Sahu (1966)	412.15	335.62	289.83	708.31	1081.76	1.1318
Hughes (1978)	445.98	363.17	313.62	766.45	1170.55	1.2247
Panozzo (1982)	466.12	379.57	327.78	801.06	1223.41	1.28
Heilbronner (1992)	546.24	444.81	384.12	938.74	1433.68	1.5
Johnson (1994)	418.79	340.56	294.53	720.26	1099.92	1.15
$D_w \lambda$ image analysis	425.35	351.78	307.39	731.08	1055.64	1.10-1.19
D _w uncorrected image analysis	364.16	296.54	256.08	625.83	955.79	
D _m laser granulometry	434	352	304	639	1050	

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Table 4. Comparison of different published correction factors to be applied in switching from 2D to 3D grain size distributions. D_m, mean grain diameter (laser granulometer); D_w, volume-weighted mean diameter; λ, shape correction factor.

1002

1003 6.4 Representative number of particles-sorting relationship

1004	In all the analyzed samples, we acquired large particle size datasets (> 5,000 particles), as we
1005	were interested in testing the reliability and reproducibility of mean diameter calculated with
1006	the proposed volume-weighted mean diameter formula. The number of digitized particles was
1007	higher in samples characterized by low sorting degree, and this was required to extract stable
1008	mean diameter values. At the same time, the adoption of large datasets allowed to check the
1009	critical number of particles required to achieve a certain standard error



992 associated with the mean diameter, using as reference the volume-weighted mean diameter 993

calculated with all available particles.

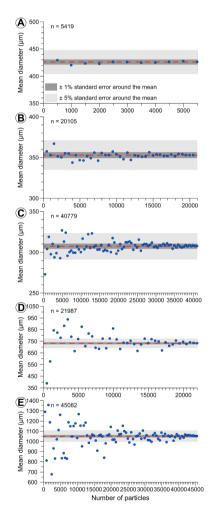






Figure 18. Volume-weighted mean diameter vs number of particles relationship calculated for 500 grains 996 incremental bins. Standard error (±1 and 5%) intervals are calculated with respect to the average diameter



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obtained from the entire grain size datasets (red dashed line). (a) LIM1 beach sample. (b) PAR1 fluvial sample.
(c) PAR2 fluvial sample. (d) PES1 fluvial sample. (e) ACQ1 fluvial-deltaic sample. n, number of particles.

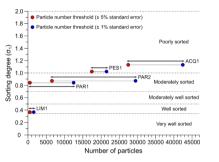
999 To do so, we calculated the volume-weighted mean diameter at incremental steps of 500 1000 particles and we checked the deviation with respect to the reference value. At every calculation 1001 step, particles were randomized using a modified shuffle Matlab[®] algorithm to avoid any bias 1002 in particle extraction. We assumed two different confidence levels compiled at ± 1% and ± 5% standard error of the average diameter obtained with all available particles (Fig. 18). For LIM1 1003 1004 beach sand sample, volume-weighted mean diameter lays just outside the ± 1% standard 1005 error interval, using only 500-1,000 particles, while it becomes more stable and between ± 1% 1006 standard error for datasets > 1,500 grains (Fig. 18a). For this sample the minimum particle number is low due to the good sorting degree. PAR1 fluvial sand sample displays average 1007 1008 diameter values always between the ± 5% error interval (already for 500 grains), but only using 1009 12,500 particles or more, the calculated values fall in the ± 1% standard error (Fig. 18b). PAR2 1010 sample shows a more marked scattering of data for limited particle number (< 5,000 grains), 1011 while the critical ± 5% error threshold is attained at 6,500 grains and the more restrictive ± 1% 1012 standard error is achieved for 29,500 particles (Fig. 18c). Mean diameter values for PES1 1013 sample are characterized by strong variations up to 5,000-7,000 used grains, while they become more stable above 10,000 particles, reaching the ± 5% standard error threshold at 1014 17,500 particle and the ± 1% error at 21,500 grains, respectively (Fig. 18d). Eventually, the 1015 1016 poorly sorted ACQ1 sample displays volumeweighted mean diameter values outside the \pm 5% 1017 error interval up to 10,000-15,000 grains. At least 27,500 particles are needed to calculate 1018 average diameter values in the ± 5% standard error interval and 42,500 grains must be used 1019 to achieve the ± 1% threshold (Fig. 18e). A decrease of sorting degree (widening of 1020 granulometric curves) from 0.37 to 1.137 causes an increase in the minimum number of 1021 particles to be used in average diameter calculation from 500 to 27,500 to reach the ± 5% 1022 standard error threshold (Fig. 19). To attain the ± 1% error interval on the same samples, 1,500



1023 to 42,500 particles are required (Fig. 19). We tested the importance of the number of particles

1024 used in sample with relatively simple size distribution curves (single mode and gentle curve

1025 asymmetry).



1026

1027 **Figure 19.** Critical particle number vs sorting degree relationship calculated for the 5 analyzed samples based 1028 on volume-weighted mean diameter calculations.

1029 It is likely that samples with poorer sorting, multi-mode distributions and stronger asymmetry

1030 could require even larger particle amounts (Friedman, 1962a; Heilbronner and Barrett, 2014;

1031 Lopez-Sanchez, 2020). This aspect should be carefully considered when extracting average

1032 particle diameter from small datasets and results should be treated cautiously, being aware of

1033 the low reliability induced by limited data.

1034

1035 **6.5** Fields of application and usefulness of the proposed method

Volume-weighted mean diameter proved to be a reliable parameter to describe 3D grain size distribution from 2D grain size datasets acquired through image analysis applied on thin sections. The addition of sample-specific λ shape correction factors facilitates the conversion from 2D to 3D grain size distributions. Moreover, the calculation formula is straightforward and can be easily used, without requiring specific stereologicalmathematical knowledge (Elias, 1967; Underwood, 1970; Russ, 1986; Gallagher et al., 2023). Our tests have been performed



1042 on loose sand samples, but the volume-weighted mean diameter could be particularly useful in the case of cohesive and hardened granular media not suitable to be analyzed through 1043 1044 other laboratory techniques (optical granulometry, electro-resistivity methods, pipette, or 1045 sedimentation). Grain size analysis on such sample types must be conducted by means of 1046 microscopy characterization in conjunction with image analysis (Krumbein, 1935). Basic 1047 image analysis software, such as ImageJ, provides every required factor to be inserted in the 1048 calculation equation (Schneider et al., 2012). We preferred to manually digitize all the 2D grain 1049 size datasets employed to set the mean diameter formula, to achieve the maximum precision 1050 in defining particle shape and outer boundaries. However, as this procedure is extremely time 1051 consuming (7-10 days of work for each thin section image), it may be seen as poorly viable 1052 and suitable in the case numerous samples to be analyzed (Heilbronner and Barrett, 2014). 1053 In the past years, many efforts have been made to process large number of images both with 1054 semi-automatic and automatic methods (Mazzullo and Kennedy, 1985; Eicken, 1993; 1055 Heilbronner and Bruhn, 1998; Ketcham, 2005; Mock and Jerram, 2005; Gualda, 2006; Berger 1056 et al., 2011; LopezSanchez and Llana-Fúnez, 2016). Image segmentation has become a more reliable, efficient and easy procedure, leading to the acquisition of thousands of grain size data 1057 1058 in few hours of processing with acceptable errors (Heilbronner and Barrett, 2014). In recent years, some authors developed image segmentation algorithms which employ computer 1059 1060 artificial intelligence and machine learning processes in particle segmentation, further reducing data acquisition time (Saxena et al., 2021). By taking advantage of these recent 1061 1062 techniques, users should not be concerned about the minimum number of representative 1063 particles to be used in calculating volume-weighted mean diameter, even at the highest 1064 desired precision intervals. Following this, we encourage scientists of different research areas, 1065 to experiment and test the usefulness of the proposed corrected volume-weighted mean 1066 diameter as it provided precise and reliable results in samples with different textural 1067 characteristics, grain size distributions and mineral compositions.

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1069		
1070	7. Concluding remarks	
1071	The correct measuring of particle size distributions and particle-grain mean diameters is	
1072	fundamental in the study and characterization of both natural and artificial granular media.	
1073	Several analytical procedures and calculation equations have been set up in the last decades.	
1074	However, the comparison between 2D and 3D datasets acquired with different techniques is	
1075	not straightforward. To address, this issue, we proposed the use of volume-weighted mean	Deleted: help
1076	diameter, an easy-to-use equation designed to define 3D equivalent particle diameter from 2D	Deleted: ing
1077	datasets gained through image analysis technique. The corrected volume-weighted mean	
1078	diameter equation that has been set is capable of accurately describing grain size distribution	
1079	on different sample types. Apart for the volume-weighing, the equation takes also into account	
1080	particle shapes and is suitable for granular samples with different textural characteristics and	
1081	mineral compositions. The following conclusive points can be drawn from our study:	
1082	1- Volume-weighted mean diameter provides matching results with particle size data	
1083	gained through optical granulometry technique, and combined with thin sectioning, can	
1084	be useful in the case of weak or sensitive samples that can be partially compromised	
1085	by laser diffraction or other analytical methodologies. In such sample types, 2D image	
1086	analysis gives much more conservative and representative results than laser	Deleted: grants
1087	granulometry.	
1088	2- Employing both laser granulometry and image analysis datasets, volume-weighted	
1089	mean diameter returns close results compared to the methods of moments (arithmetic	
1090	mean) equation. Conversely, other calculation formulas (geometric mean of method of	
1091	moments, geometric mean of graphical method, median, and mode) proved to be less	
1092	reliable and more sample sensitive (goodness of results may vary according to sample	
1093	sorting and skewness).	



1097	3- The calculation of accurate and precise average diameter values requires an		
1098	increasing particle number following the diminishing of sorting degree (widening of		
1099	grain size distribution). However, automatic to semi-automatic particle identification and		
1100	image analysis processing could help in reducing the time required for the acquisition		
1101	of such large particle datasets.		
1102	4- The adoption of volume-weighted mean diameter provides reliable data and allows the		
1103	estimation of 3D average diameter from 2D particle datasets. This process is based on		
1104	a relatively simple equation, employing basic input parameters, without recurring to		
1105	advanced stereology concepts or difficult mathematical equations.		
1106	Given the summary points described above, we suggest researchers working on different		
1107	disciplines dealing with particle size determination to test the volume-weighted mean diameter		
1108	equation and check whether it could be a viable solution for straightforward mean diameter		
1109	calculation from 2D data distributions.		
1110			
1110			
1111	Declaration of competing interests		
1112	The authors declare that they have no known competing financial interests or personal		
1113	relationships that could have appeared to influence the work reported in this paper.		
1114			
1115	Author contributions		
1116	Mattia Pizzati: Conceptualization, Supervision, Data curation, Formal analysis, Methodology,		

- 1117 Writing original draft, Writing review & editing, Validation.
- 1118 Luciana Mantovani: Conceptualization, Data curation, Formal analysis, Methodology, Writing
- 1119 review & editing.



- 1120 Antonio Lisotti: Conceptualization, Data curation, Methodology.
- 1121 Fabrizio Storti: Conceptualization, Supervision, Writing review & editing.
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- 1133

1134 Supplementary material

- 1135 Details regarding the standard operating procedures adopted in optical granulometry
- analyses, XRD patterns, and high-resolution thin section photomosaics shown in Fig. 11 are
- 1137 reported in the online Supplementary material.
- 1138

1139 Appendix 1

- 1140 Hereafter are listed and explained the equations of the calculation formulas used in comparing
- 1141 particle diameter values in tables 2 and 3. We adopted the equations implemented in



GRADISTAT, grain size statistical analysis software (Blott and Pye, 2001). Arithmetic and 1142 1143 geometric means from the method of moments have been used (Krumbein and Pettijohn, 1938), and the first one is defined as: 1144 $\bar{x}_a = \frac{\sum_{i=0}^{i=n} fm_m}{100}$ 1145 (A1) where, \overline{x} a is the arithmetic mean, fm_m stands for the frequency percentage of particles at the 1146 1147 midpoint (m) of each size class (i). Conversely, the geometric mean of the method of moments is given by the equation: 1148 $x_g^- = \frac{\sum_{i=0}^{i=n} f \ln m_m}{100}$ 1149 (A2) where, \overline{x}_g is the geometric mean, fln m_m is the logarithmic frequency of particles at the midpoint 1150 1151 (m) of each size class (i). 1152 The graphical method has been employed as well, with the geometrical mean and sorting 1153 degree (Folk and Ward, 1957; Folk, 1974). The geometrical mean diameter is described by 1154 the equation: 1155 ln P¹⁶+ln P⁵⁰+ln P⁸⁴ 1156 $M_G = \exp -$ 1157 (A3) where, M_G is the geometrical mean and P_{16} , P_{50} and P_{84} are the particle diameter values in 1158 1159 metric units at the 16, 50 and 84% cumulative percentile of the particle size distribution curve, 1160 respectively. Sorting degree (σ_1) is provided by the standard deviation associated with the logarithmic mean 1161

1162 (Folk, 1974) and is given by the equation:

1163
$$\sigma_1 = \frac{\Phi_{84} - \Phi_{16}}{4} + \frac{\Phi_{95} - \Phi_5}{6.6}$$
(A4)



- 1164 in which, ϕ is the grain diameter in phi units, at 5, 16, 84 and 95% cumulative percentile values
- 1165 of the particle size distribution curve, respectively.
- 1166
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