

On the relationship between $\delta\text{O}_2/\text{N}_2$ variability and ice sheet surface conditions in Antarctica

Romilly Harris Stuart¹, Amaëlle Landais¹, Laurent Arnaud², Christo Buizert³, Emilie Capron², Marie Dumont⁴, Quentin Libois⁵, Robert Mulvaney⁶, Anaïs Orsi^{1,7}, Ghislain Picard², Frédéric Prié¹, Jeffrey Severinghaus⁸, Barbara Stenni⁹, and Patricia Martinerie²

¹Laboratoire des Sciences du Climat et de l'Environnement, LSCE-IPSL, CEA-CNRS-UVSQ, Univ. Paris-Saclay, 91190 Gif-sur-Yvette, France

²Université Grenoble Alpes, CNRS, INRAE, IRD, Grenoble INP, IGE, 38000 Grenoble, France

³College of Earth, Ocean, and Atmospheric Sciences, Oregon State University, Corvallis, OR 97331, USA

⁴Univ. Grenoble Alpes, Université de Toulouse, Météo-France, CNRS, CNRM, Centre d'Etudes de la Neige, 38000 Grenoble, France

⁵CNRM, Université de Toulouse, Météo-France, CNRS, Toulouse, France

⁶British Antarctic Survey, Natural Environment Research Council, Madingley Road, Cambridge CB3 0ET, UK

⁷The University of British Columbia, Department of Earth, Ocean and Atmospheric Sciences, Vancouver, Canada

⁸Scripps Institution of Oceanography, University of California, San Diego, La Jolla, CA 92093, USA

⁹Ca' Foscari University of Venice, Department of Environmental Sciences, Informatics and Statistics, Venezia, 30172, Italy

Correspondence: Romilly Harris Stuart (romilly.harris-stuart@lsce.ipsl.fr)

Abstract. Processes controlling pore closure are broadly understood yet defining the physical mechanisms controlling associated elemental fractionation remains ambiguous. Previous studies have shown that the pore closure process leads to a decrease in concentration of small-size molecules (e.g., H_2 , O_2 , Ar, Ne, He) in the bubbles. Ice core $\delta(\text{O}_2/\text{N}_2)$ records – the ratio of O_2 to N_2 molecules in bubbles within the ice relative to the modern atmosphere – are therefore depleted owing to this O_2 loss and show a clear link with local summer solstice insolation making it a useful dating tool. In this study, we compile $\delta(\text{O}_2/\text{N}_2)$ records from 14 polar ice cores and show a new additional link between $\delta(\text{O}_2/\text{N}_2)$ and local surface temperature and/or accumulation rate. Using the Crocus snowpack model, we perform sensitivity tests to identify the response of near-surface snow properties to changes in insolation, accumulation rate, and air temperature. These tests support a mechanism linked to snow grain size, such that the larger the grain size for a given density, the stronger the pore closure fractionation, and hence, lower $\delta(\text{O}_2/\text{N}_2)$ values. Based on both snowpack model outputs and data compilation, our findings suggest that local accumulation rate and temperature should be considered when interpreting $\delta(\text{O}_2/\text{N}_2)$ as an insolation proxy.

1 Introduction

Ice cores store crucial information for our understanding of past climate variability and atmospheric composition. Interpreting ice core gas records first requires an understanding of the evolution of snow into ice via the firnification processes. Firn is the name given to the layer of consolidated snow which makes up the top 50-120 m of ice sheets. Atmospheric air moves through porous networks within the firn until a critical depth (known as the lock-in depth) where vertical diffusion effectively stops,

and pores gradually become sealed off from the atmosphere. The lock-in depth and the depth at which all pores are closed (close-off depth) are largely determined by local accumulation rate, temperature, and possibly the degree of density layering (Schwander et al., 1997; Martinerie et al., 1994; Mitchell et al., 2015). The region between the lock-in depth and close-off depth is known as the lock-in zone (LIZ).

Gas records from ice cores provide a vital dating tool, especially at low accumulation sites where other methods are unsuitable. One such tool is orbital dating, which enables certain gas records to be tuned to insolation curves directly calculated from astronomical variables (Laskar et al., 2004). Ice core $\delta^{18}\text{O}_{\text{atm}}$ records ($\delta^{18}\text{O}$ of atmospheric O_2) are strongly correlated with precession (mid-June 65°N insolation) (Bender et al., 1994). $\delta^{18}\text{O}_{\text{atm}}$ provides a direct atmospheric signal which may ultimately be used to align different ice core records (Extier et al., 2018). The two alternative proxies for orbital dating are 1) total air content, which is anti-correlated with integrated summer insolation, i.e., the annual sum of daily insolation above a certain threshold (Raynaud et al., 2007), and 2) $\delta(\text{O}_2/\text{N}_2)$, which is anti-correlated with summer solstice insolation intensity (e.g., Kawamura et al., 2007; Bouchet et al., 2023). Unlike $\delta^{18}\text{O}_{\text{atm}}$, TAC and $\delta(\text{O}_2/\text{N}_2)$ reflect processes within the firn column making the records site specific. The term $\delta(\text{O}_2/\text{N}_2)$ – hereafter, simply $\delta\text{O}_2/\text{N}_2$ – describes the relative difference between the ratio of O_2 to N_2 molecules trapped within the ice and that of the standard atmosphere and is expressed in the delta notation commonly used for stable isotope ratios.

The use of $\delta\text{O}_2/\text{N}_2$ for dating was first proposed by Bender (2002) after observations of an anti-correlation with local summer solstice insolation (hereafter SSI). Data from the Vostok ice core showed that high SSI corresponds to low $\delta\text{O}_2/\text{N}_2$ values (Bender, 2002). A similar relationship was then observed at other sites such as Dome Fuji (Kawamura et al., 2007) and EPICA Dome C (Landais et al., 2012) in Antarctica, and GISP2 (Suwa and Bender, 2008b) in Greenland. Over orbital timescales, $\delta\text{O}_2/\text{N}_2$ is in anti-phase with local SSI when drawn on the ice-age chronology, indicating that the firn properties controlling the $\delta\text{O}_2/\text{N}_2$ fractionation are set near the surface. It is understood that temperature gradients are increased with high summer insolation leading to enhanced near surface snow metamorphism, thus increasing near-surface grain size which persists throughout the firnification process down to the close-off depth (Bender, 2002; Severinghaus and Battle, 2006; Suwa and Bender, 2008a; Fujita et al., 2009).

Parallel firn air studies of the open porosity revealed an enrichment in O_2 and other small molecules, such as Ar, Ne and He, compared to air within the closed porosity at the close-off depth, providing further evidence of size-dependent fractionation during pore-closure (Battle et al., 1996; Huber et al., 2006; Severinghaus and Battle, 2006). While the physical mechanisms controlling the amount of fractionation are not fully understood, it is believed that smaller molecules ($<3.6\text{ \AA}$ diameter) escape during pore closure via molecular diffusion through the ice lattice (or permeation) driven by pressure gradients between recently closed pores and neighbouring open pores (Ikeda-Fukazawa et al., 2004; Huber et al., 2006; Severinghaus and Battle, 2006). This process is facilitated by the pore network's capacity to export the fugitive gases back to the atmosphere, which is required for the observed depletion in O_2 in bubbles (Fujita et al., 2009).

In addition, Fujita et al. (2009) proposed that $\delta\text{O}_2/\text{N}_2$ would be low under high SSI conditions due to enhanced density stratification in the deep firn. They argue that layers characterised by large grains and relatively low density in the deep firn ('summer' layers) close-off deeper and take longer to do so than neighbouring layers, which are denser and have smaller grains

(‘winter’ layers). ‘Summer’ layers therefore remain permeable for longer, allowing the O₂ enriched air in open porosity to be exported to the atmosphere, and hence, reducing bulk ice $\delta\text{O}_2/\text{N}_2$ under high SSI conditions (Fujita et al., 2009). While the proposed mechanisms are posited to explain the SSI imprint on $\delta\text{O}_2/\text{N}_2$, they are also influenced by local climate conditions such as temperature and accumulation rate. Indeed, there is a substantial amount of evidence linking local climate conditions with both firm physical properties (Casado et al., 2021; Inoue et al., 2023) and deep firm layering (Hörhold et al., 2011).

There is a growing body of evidence for a local climatic imprint on ice core $\delta\text{O}_2/\text{N}_2$ records. Firstly, spectral analysis has revealed climate related 100-ka cyclicity at EPICA Dome C (Bazin et al., 2016). However, this 100 ka-cyclicity is not apparent in the Dome Fuji $\delta\text{O}_2/\text{N}_2$ record, which Kawamura et al. (2007) attribute to the idea that temperature and accumulation effects cancel each other out. Secondly, millennial scale variability in $\delta\text{O}_2/\text{N}_2$ records from GISP2 appeared in-phase with local temperature fluctuations driven by Dansgaard-Oeschger events (Suwa and Bender, 2008b). In contrast, Kobashi et al. (2015) evidenced an anti-phase effect of accumulation rate on $\delta\text{Ar}/\text{N}_2$ records at GISP2 over the last 6000 years. Like O₂, Ar is a smaller molecule than N₂ such that the same driving mechanisms are invoked for the $\delta\text{Ar}/\text{N}_2$ and $\delta\text{O}_2/\text{N}_2$ variations, but the $\delta\text{Ar}/\text{N}_2$ anomaly tends to be half as large as the $\delta\text{O}_2/\text{N}_2$ anomaly (Bender et al., 1995; Buizert et al., 2023). Kobashi et al. (2015) proposed a direct effect of accumulation rate or temperature on the $\delta\text{Ar}/\text{N}_2$ ($\delta\text{O}_2/\text{N}_2$) variations through the firm depth. The higher the accumulation rate or the lower the temperature, the higher the firm weight and hence the overloading pressures in microbubbles preferentially expelling Ar (O₂) in the LIZ. Alternatively, Severinghaus and Battle (2006) proposed that the higher the accumulation rate, the more rapid the burial of bubbles, allowing less time for gases to escape during pore closure.

Using a combination of data compilation and snowpack modelling, we aim to develop our understanding of the formation of the $\delta\text{O}_2/\text{N}_2$ records by first determining the role of local climate parameters, accumulation rate and temperature, on $\delta\text{O}_2/\text{N}_2$ variability, and subsequently identifying potential mechanisms related to snow physical properties using snowpack sensitivity tests. We use a compilation of datasets from 14 ice cores from both Antarctica and Greenland to identify spatial and temporal patterns in $\delta\text{O}_2/\text{N}_2$ depending on local surface conditions. The impacts of SSI and local climate on snow properties are then assessed using the SURFEX-ISBA-Crocus detailed snowpack model (Vionnet et al., 2012). We aim to constrain the influence of near-surface snow properties on $\delta\text{O}_2/\text{N}_2$ variability, potentially contributing to a mechanistic explanation for elemental fractionation during pore closure.

2 Methods

2.1 Ice core sites

We compiled $\delta\text{O}_2/\text{N}_2$ records from 18 ice cores from Antarctica and Greenland but use data from 14 of those sites for reasons explained in Section 2.2.3. Previously published data were measured on ice cores from: Dome Fuji (DF), EPICA Dome C (EDC), Greenland Ice Core Project 2 (GISP2), Law Dome DE08 and DSSW20k, North Greenland Ice core Project (NGRIP), Roosevelt Island Climate Evolution (RICE), Siple Dome (SD), South Pole (SP), Talos Dome (TALDICE), Vostok (VK), and the West Antarctic Ice Sheet Divide (WAIS) ice cores (references for all datasets are presented in Table S2). We also present unpublished data from Berkner Island (BI), EPICA Dronning Maud Land (EDML), Fletcher Promontory (FP), GISP2, James

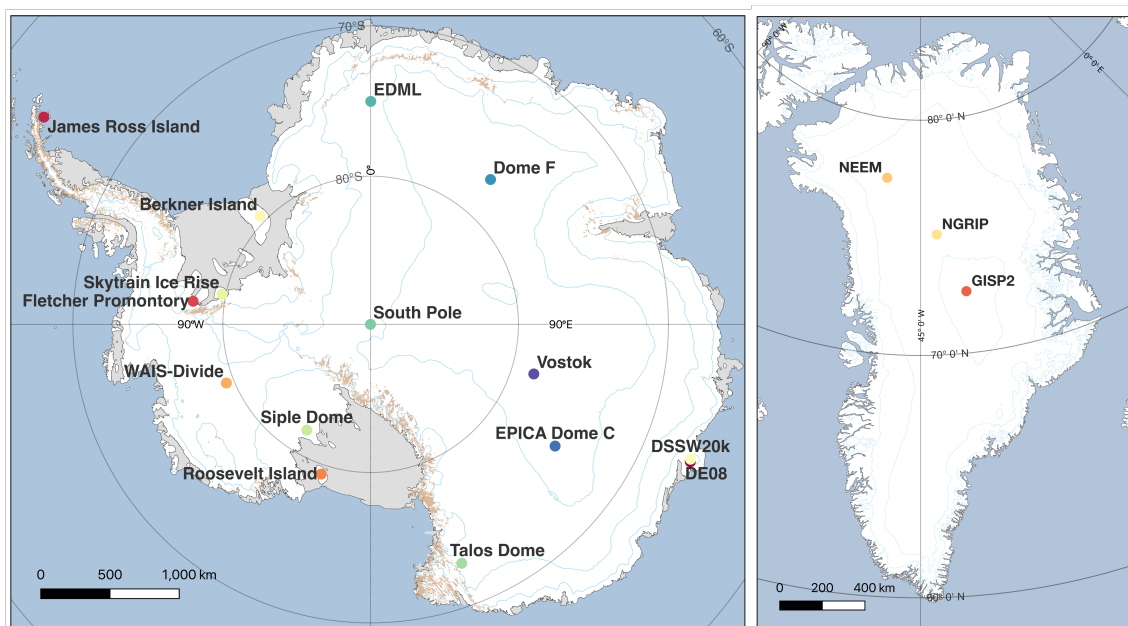


Figure 1. Locations of each ice core site initially included in our study (Matsuoka et al., 2018; Moon et al., 2023).

85 Ross Island (JRI), North Greenland Eemian Ice Drilling (NEEM), Skytrain Ice Rise (SIR) and Talos Dome (TALDICE) ice samples (overview of unpublished datasets in Table S1). Table 1 provides an overview of the site characteristics.

2.2 Analytical techniques for previously unpublished data

The previously unpublished $\delta\text{O}_2/\text{N}_2$ datasets were measured at the Laboratoire des Sciences du Climat et de l'Environnement (LSCE), with the addition of some GISP2 data measured at Scripps Institution of Oceanography (Scripps). At both LSCE and
 90 Scripps, gases are extracted from the ice using a melt-refreeze technique based on the method described by Sowers et al. (1989) with modifications to the LSCE method as described by Landais et al. (2003), and to the Scripps method as outlined in Petrenko et al. (2006). In short, ice samples are placed into glass flasks at -20°C while the atmospheric air is evacuated. Samples are then left to slowly melt to release the trapped gases, before being refrozen. The extracted air samples are then passed through a CO_2 and water vapour trap, before being trapped in the stainless-steel dip-tube submerged in liquid helium. An alternative semi-
 95 automated extraction technique is now more commonly used at LSCE which removes the need for refreezing of the samples (Bazin et al., 2016; Bouchet et al., 2023).

2.2.1 New $\delta\text{O}_2/\text{N}_2$ measurements

Samples from the following sites were measured at LSCE, France on a 10-collector Thermo Delta V Plus, unless otherwise stated. In all cases, the values used in this study are the average of at least two replicate measurements and have an average
 100 analytical uncertainty of 0.5% for $\delta\text{O}_2/\text{N}_2$.

Table 1. Overview of ice core site characteristics. The acronym BCTZ stands for brittle-clathrate transition zone, and COD stands for close-off depth.

Site	Latitude (°S)	Longitude (°E)	Elevation (m)	BCTZ ^a (m)	Accumulation rate ^b (cm w.eq a ⁻¹)	Temperature ^c (°C)	COD ^d (m)
Berkner Island ¹	79.55	-45.68	890		16.2	-26	63
Dome Fuji ²	77.32	39.7	3810	450–1200	2.6	-58	104
EPICA Dome C ³	75.1	123.35	3233	600–1200	2.8	-55	100
EPICA Dronning Maud Land ⁴	75	0.04	2892	800–1200	6.4	-45	83
Fletecher Promontory ⁵	77.9	-82.61	873		38	-27	79
GISP2 ⁶	-72.6	-38.5	3200	650–1400	24	-31.4	75
James Ross Island ⁷	64.2	-57.69	1542		58	-14	67
DE08 ⁸	66.72	113.2	1250		110	-19	88.5
DSSW20k ⁹	66.77	112.81	1370		15	-20.7	53
NEEM ¹⁰	-77.45	-51.6	2450	600–1200	20	-28.9	78.8
NGRIP ¹¹	-75.1	-42.32	3090	790–1200	17.5	-31.5	78
Roosevelt Island ¹²	79.36	-161.71	550		21	-23.5	52
Siple Dome ¹³	81.65	-148.81	621		12.4	-25.4	57.5
Skytrain Ice Rise ¹⁴	79.74	-78.55	784		13.5	-26	58
South Pole ¹⁵	89.99	-98.16	2835	619–1078	8	-49	125
Talos Dome ¹⁶	72.82	159.07	2315	667–1002	8	-41	72
Vostok ¹⁷	78.47	106.87	3488	500–1250	2.2	-57	99.2
WAIS-Divide ¹⁸	79.47	-112.09	1766	1100–1200	20.2	-31.1	76.5

¹Mulvaney et al., 2007^{a,b,c,d}; ²Oyabu et al., 2021^a, Fujita et al., 1998^{b,c}; Watanabe et al., 1997^d; ³Parrenin et al., 2012^a EPICA community members, 2004^{b,c}; Landais et al., 2006^d; ⁴Neff, 2014^a, Oerter et al., 2000^{b,d}, EPICA community members, 2006^c; ⁵Mulvaney et al., 2014^{a,b,c,d}; ⁶Gow et al., 1997^a, Alley et al., 1993^b, Alley and Koci, 1988^c, Cuffey and Paterson, 2010^d; ⁷Mulvaney et al., 2014^{a,d}, Capron et al., 2013^{b,c}; ⁸Rubino et al., 2019^a, Etheridge and Wookey, 1988^{b,c}, Etheridge et al., 1996^d; ⁹Rubino et al., 2019^a, Morgan et al., 1997^{b,c}, Buizert and Severinghaus, 2016^d; ¹⁰Warming et al., 2013^a, Buizert et al., 2012^{b,c,d}; ¹¹NGRIP project members, 2004^{a,b,c}, Martinerie et al., 2009^d; ¹²Neff, 2014^a, Winstrup et al., 2019^b, Bertler et al., 2017^{c,d}; ¹³Hamilton, 2002^a, Severinghaus et al., 2001^{b,c,d}; ¹⁴Mulvaney et al., 2021^{a,b,c}, Hoffmann et al., 2022^d; ¹⁵Lazzara et al., 2012^a, Mosley-Thompson et al., 1999^{b,c}, Severinghaus et al., 2001^d; ¹⁶Neff, 2014^a, Stenni et al., 2002^{b,c}; ¹⁷Uchida et al., 1994^a, Petit et al., 1999^{b,c}, Cuffey and Paterson, 2010^d; ¹⁸Fegyveresi et al., 2011^{b,c}, Battle et al., 2011^d.

Berkner Island

Measurements were performed on bubbly ice from the BI ice core every 55 cm (every bag) between 631 m and 680 m, corresponding to 10,269–21,350 aBP (Capron et al., 2013). Replicate samples were prepared at LSCE using the melt-refreeze method between March 2010 and March 2011.

105 *EDML*

Nine samples were measured on bubbly ice from the EDML ice core over five depth levels between 328–473 m (327.8 m (4.51 ka BP), 354.2 m (4.95 ka BP), 381 m (5.43 ka BP), 467 m (7.04 ka BP), and 473 m (7.16 ka BP)) (Bazin et al., 2013). The samples were prepared using the melt-refreeze method at LSCE.

Fletcher Promontory

110 In January 2015, 39 depth levels were measured from the FP ice core, retrieved in 2012. Measurements were performed approximately every 3 m starting at 289 m down to 388 m. There is currently no published age-scale for the FP ice core. All samples were prepared using the melt extraction method.

James Ross Island

115 Between February and March 2011, measurements were performed at 16 depth levels on the JRI ice core. The depth resolution varied between 2–50 m starting at 52 m until 363 m corresponding to 0.03–14.3 ka BP (Mulvaney et al., 2012). Samples were prepared using the melt extraction method.

NEEM

120 Clathrate ice from the NEEM ice core was measured between February and April 2011, a year after the core was retrieved. A total of 119 depth levels were sampled were measured at varying resolutions over the following intervals: 55 cm intervals (every bag) between 1757–1773 m (38.127–39.735 ka B2k), 5.5 m intervals (every 10 bags) between 2205 and 2370 m (108.56–120.237 ka B2k), every 2 bags from 2375–2434 m (no published age-scale available below these depths), and 5.5 m intervals (every 10 bags) between 2436 and 2519 m (Gkinis et al., 2021; Rasmussen et al., 2013). In total, samples from 119 depth levels were prepared using the melt-refreeze method.

Skytrain Ice Rise

125 Measurements were performed on bubbly ice from the SIR ice core between March and April 2021. Samples were taken sporadically (1–15 m intervals) at 16 depth levels between 307 and 436 m depth (4.707–11.696 ka BP) (Mulvaney et al., 2023). Each sample was prepared at LSCE using the melt extraction method.

TALDICE

130 Numerous measurements have been performed on bubbly and clathrate ice from TALDICE between 2008 and 2022 at LSCE. A total of 308 depth levels were measured at varying intervals starting at 155 m down to 1617 m. Published age-scales reach 1548 m, giving an age range of 1.55–343 ka for TALDICE samples (Buiron et al., 2011; Crotti et al., 2021). All samples were prepared using the melt extraction technique. Some measurements between 1356–1620 m depth have been published previously and are available in Crotti et al. (2021).

135 Samples from GISP2 were measured at Scripps Institution of Oceanography on a 3 kV Thermo Finnigan Delta V plus 217 dual inlet IRMS (isotope ratio mass spectrometer).

GISP2

140 Measurements were performed on samples from 643 depths between 1740 and 2400m (13–50 ka BP) over several measurement campaigns between 2017–2020 and referenced to La Jolla pier air. The melt-refreeze technique was used for gas extraction, and the $\delta^{15}\text{N}$ of N_2 data from these samples were previously reported (Martin et al., 2023). Again, the majority of the samples were analysed in replicate.

2.2.2 Corrections

Chemical slope and pressure imbalance corrections are applied to the measurements during data processing (Landais et al., 2003). In addition, all data are corrected for gravitational fractionation in the firm using $\delta^{15}\text{N}$ of N_2 from the same samples.

$$\delta\text{O}_2/\text{N}_2\text{grav.corr.} = \delta\text{O}_2/\text{N}_2 - 4 \cdot \delta^{15}\text{N} \quad (1)$$

145 Gas loss effects during ice core storage are well documented to modify $\delta\text{O}_2/\text{N}_2$, causing significant depletion in O_2 in clathrate ice stored above -50°C (Ikeda-Fukazawa et al., 2005; Kawamura et al., 2007; Landais et al., 2012). Ikeda-Fukazawa et al. (2005) proposed a correction for storage gas loss effects as a function of temperature and time. However, given the incomplete storage history for all ice cores we do not attempt to correct for storage gas loss, but rather define rejection criteria outlined in Section 2.2.3.

150 2.2.3 Data rejection criteria

Ice core storage histories need to be considered before interpreting the data to account for post-coring gas loss effects which disturb the signal (Section 2.2.2). Successive $\delta\text{O}_2/\text{N}_2$ measurements from TALDICE and GISP2 clathrate ice samples show strong depletion of O_2 through time (Supplement S1), which is consistent with observations from EDC (Bouchet et al., 2023). We systematically reject measurements from clathrate ice stored at -20°C for over 3 years, or at -36°C for more than 4 years. 155 Bubbly ice stored at these same temperatures appear to be mostly unaffected by gas loss (Supplement S1), with the exception of Vostok (Bender, 2002).

Several measurements were performed on ice within the bubble-clathrate transition zone (BCTZ: where the high hydrostatic pressure in the bubbles cause entrapped gases to form clathrate hydrates (Schaefer et al., 2011)). At these depths, elemental fractionation occurs due to some gas species being preferentially incorporated into the clathrate structures (Ikeda-Fukazawa 160 et al., 2001), thus making the interpretation of gas measurements unreliable (Bender, 2002). While brittle ice is reported at intermediate depth sites, such as BI, JRI, DE08, DSSW20k, RICE, and SD, we do not consider these BCTZs due to the absence of clathrate hydrates (Neff, 2014; Rubino et al., 2019). Measurements from the BCTZ may either have increased mean $\delta\text{O}_2/\text{N}_2$ (usually in excess of 0‰) or strong data scattering, expressed as a high standard deviation (Oyabu et al., 2021). To avoid adding biases to our analysis, measurements from BCTZ are removed. Additional scattering in elemental ratios, characterised 165 by a standard deviation of 6.2‰ compared to 1.8‰ in pure bubble and clathrate ice, is observed below the BCTZ in the WAIS record between 1300–1500m (Shackleton, 2019). Similar effects have been documented in the EDC and TALDICE ice cores

(Lüthi et al., 2010), and the Dome Fuji ice core (Oyabu et al., 2021). Data influenced by this scattering effect were also removed from our analysis, followed by the removal of outliers from the cleaned datasets.

We note that these criteria result in the removal of all data from NGRIP and Vostok, as well as sections of data from other sites (see Supplement S1 for overview). The remaining 14 datasets are presented in Table 3 and were used to analyse the drivers of $\delta\text{O}_2/\text{N}_2$ variability. We also exclude FP and SIR due to limited availability of accumulation rate and temperature records.

2.3 Modelling near-surface snow properties

The second component of our study addresses the modelled response of snow physical properties to perturbations in SSI, accumulation rate, and temperature with the aim of identifying which properties may be influencing elemental fractionation during pore closure. We use the SURFEX-ISBA-Crocus detailed snowpack model (Crocus hereafter) to simulate snowpack evolution (Vionnet et al., 2012). Crocus simulates changes in snow physical properties induced by surface metamorphism and the evolution of these properties with depth. The model is forced by ERA5 reanalysis data (Hersbach et al., 2020), and the snowpack is initialised with measurements of snow density, effective optical radius of snow grains and snow temperature. Optical radius is defined as the radius which snow grains would have for their surface area-to-volume ratio if they were spherical (Domine et al., 2006). Optical radius is thus directly linked to specific surface area (SSA), defined as the surface area of snow at the ice-air interface per unit mass (units m^2kg^{-1}) (Legagneux et al., 2002), via the following equation:

$$\text{SSA} = \frac{3}{r_{\text{opt}} \cdot \rho_{\text{ice}}} \quad (2)$$

Where r_{opt} is the optical radius and ρ_{ice} is the density of ice (Gallet et al., 2014). We use this model to assess changes in snow physical properties near the surface which are invoked to explain $\delta\text{O}_2/\text{N}_2$ variability. Dome C is used as the test site given the abundance of snowpack observations as well as high resolution $\delta\text{O}_2/\text{N}_2$ data.

2.3.1 Crocus model description

Crocus is a 1-dimensional model which simulates the evolution of snow properties with time and depth on a layer-by-layer basis, i.e., in a Lagrangian framework (Vionnet et al., 2012). A detailed description of the model can be found in Vionnet et al. (2012). Briefly, the initial number of layers is defined by the user, with the thickness of each layer allowed to change along the simulation (layer thickness ranging from 2 mm at the surface to metres thick). The maximum number of layers available in the model was increased from 50 (Libois et al., 2014) to 80 (this study) to maximise the resolution with depth owing to the higher number of thin layers forming at Dome C than at Alpine sites. Once the simulated snowpack consists of 80 layers, the aggregation scheme merges internal neighbouring layers with similar properties allowing a new surface layer to form. The key physical processes incorporated into Crocus for dry snow conditions are accumulation of snowfall, snow metamorphism, compaction of snow by the wind, compaction due to the weight of the overlaying layers, absorption of solar radiation, heat diffusion, and surface energy budget.

For our study, two fundamental user-defined model components are the snow metamorphism and radiative transfer schemes. We use the semi-empirical model from Flanner and Zender (2006) (F06) for the metamorphism scheme which describes

the evolution of optical radius with time. F06 was found to be the most appropriate formulation for Dome C conditions
200 (Carmagnola et al., 2014; Libois et al., 2014). To successfully reproduce the snow temperature profile – vital for realistically
simulating snow metamorphism – the Two-streAm Radiative TransfEr in Snow model (TARTES) is used to account for vertical
distribution of absorbed solar radiation in the snowpack (Libois et al., 2013). TARTES also considers the effect of impurities
on snow temperature via albedo. For Dome C, we include black carbon content which is set to 3 ng g^{-1} (Warren et al., 2006;
Libois et al., 2015). Here we assess the simulated snow density, snow temperature, and snow SSA from Crocus model outputs.

205 **2.3.2 Dome C specific Crocus configuration**

Crocus was initially developed for alpine or sub-polar regions with seasonal snowpacks. Libois et al. (2014) modified multiple
components of the Crocus model to improve its suitability to high latitude sites with low accumulation rates - specifically for
Dome C. The modifications are extensively described in Libois et al. (2014) and were implemented into the current version of
Crocus for this study. The changes are as follows:

- 210 1. *Fresh snow properties*: The parameterisation of fresh snow density is based on temperature and wind-speed which results
in an unrealistically low density for Dome C (50 kg m^{-3}). Fresh snow density is fixed to a minimum of 170 kg m^{-3} , the
lowest fifth percentile from Dome C observations (Libois et al., 2014). Similarly, fresh snow SSA is set to $100 \text{ m}^2 \text{ kg}^{-1}$
instead of $65 \text{ m}^2 \text{ kg}^{-1}$ used in the standard version of the model (Grenfell et al., 1994; Libois et al., 2014).
- 215 2. *Wind-induced compaction*: At low-accumulation sites, snow remains at the surface for prolonged periods of time. The
long exposure time to surface winds facilitates compaction, and hence, increases density. The maximum surface snow
density is increased from 350 kg m^{-3} to 450 kg m^{-3} to account for this effect (Albert et al., 2004; Libois et al., 2014).
- 220 3. *Aggregation scheme*: The formation of a new snow layer requires a minimum amount of snowfall. Due to the low
accumulation rate at Dome C, the amount of snowfall needed to form a new layer was decreased from 0.03 mm h^{-1} to
 0.003 mm h^{-1} . In the instance when the snowpack has the maximum number of layers (80) at the time a new snow layer
is formed, layers with similar properties will be aggregated, resulting in a smoothed signal. The aggregation scheme
was disabled for the top 6 layers to resolve realistic near-surface snow temperature profiles and gradients, required to
accurately simulate snow metamorphism.

2.3.3 Model initialisation

The snowpack was initialised with density and optical radius profiles measured in January 2010 at Dome C down to 20m
225 (Champollion et al., 2019), and snow temperature data from a probe installed at Dome C in 2012 with 5 cm resolution near
the surface, coarsening with depth down to 12m. ERA5 reanalysis data from Dome C was used to force the model at 3-
hourly resolution over the period between 1 January 2000 and 1 December 2020 (Hersbach et al., 2020). The model requires
atmospheric forcings for air temperature, accumulation rate, wind speed and direction, incoming shortwave and longwave
radiation, and specific humidity. ERA5 gives a mean annual snowfall rate between 2000 and 2020 of $2.3 \text{ cm w.eq. a}^{-1}$, and as

230 such, the snowfall rate was multiplied by 1.2 to match the observed mean annual accumulation rate of around 2.8 cm w.eq. a⁻¹ (Frezzotti et al., 2004; Libois et al., 2014). To ensure that at least the top 1 m consists of accumulated snow, a 100-year spin up was used by running the forcing file ten times between 2000 and 2010, followed by the period from 2000 to 2020. The outputs from 2010 to 2020 were then used for analysis.

2.3.4 Sensitivity tests

235 The sensitivity of snowpack properties to perturbations in surface forcings are tested by modifying one of three forcing parameters: incoming shortwave radiation, accumulation rate, or 2 m air temperature. The magnitude of the perturbation to each parameter correspond to minimum and maximum values reconstructed over the last 800 ka. We use shortwave radiation as a proxy of insolation and scale the values in proportion to the SSI values. A total of seven simulations are used to perform sensitivity analysis and are outlined in Table 2. The model configuration and initial snow profile were kept constant for each
240 simulation; only the tested parameter in the atmospheric forcing file was modified as follows:

Summer solstice insolation (SSI): Over the last 1000 years, the average SSI at 75.1°S was 544 W m⁻² (Laskar et al., 2004), compared to 462 W m⁻² and 601 W m⁻², corresponding to minimum and maximum SSI over the past 800 ka. To translate to forcing perturbations, the incoming shortwave radiation (SWR) is scaled by 85% and 111%, respectively to reach the target values (462 W m⁻² and 601 W m⁻²). No additional modifications are applied to annual distribution of SWR.

245 *Annual mean accumulation rate (A)*: Present-day accumulation rate at Dome C is set to 2.8 cm w.eq. a⁻¹ following Libois et al. (2014). Hereafter, accumulation rate is expressed as ice equivalent centimetres per year. ERA5 snowfall was scaled by 36% to reach the target accumulation rate of 1.0 cm w.eq. a⁻¹, representing the 800 ka minimum, and 146% to produce an accumulation rate of 4.1 cm w.eq. a⁻¹ which corresponds to the 800 ka maximum (Bazin et al., 2013).

Annual mean air temperature (T): Snowpack sensitivity to air temperature is tested by decreasing the 2 m air temperature by
250 10°C for glacial conditions (Jouzel et al., 2007), and applying a 4°C, increase to represent 800 ka maximum temperatures. We note, however, that borehole temperature measurements and delta-age are more consistent with a 5°C cooling (Buizert et al., 2021). Furthermore, these temperature modifications do not include changes in seasonal temperature variability but suffices for the purpose of identifying bulk changes in the snow properties. The average seasonal cycle is kept constant with an average amplitude of 35°C.

Table 2. Overview of modifications made to forcing test parameter in Crocus snowpack sensitivity test scenarios.

Simulation	Reference	SSI min	SSI max	A min	A max	T min	T max
Incoming SWR (Scaled)	100%	85%	111%	100%	100%	100%	100%
Accumulation rate (cm w.eq. a ⁻¹)	2.8	2.8	2.8	1.0	4.1	2.8	2.8
Air temperature (°C)	-55	-55	-55	-55	-55	-65	-51

255 It is important to highlight that, at polar sites, accumulation rate is dependent on temperature, and temperature is influenced by insolation, such that these parameters are not independent. However, we use the model to constrain the influences of each forcing parameter in an independent manner to understand the mechanisms, even if, in reality, these parameters are inter-dependent.

3 Results

260 3.1 Influence of SSI and local climate on $\delta\text{O}_2/\text{N}_2$ variability in ice cores

Figure 2 shows $\delta\text{O}_2/\text{N}_2$ versus SSI for EDC, Dome F and South Pole. These three sites are used owing to their long temporal range and high-resolution $\delta\text{O}_2/\text{N}_2$ measurements, but with negligible gas loss. The regression slopes vary between $-0.09 \pm 0.006\text{‰ W}^{-1}\text{m}^2$ for South Pole to $-0.06 \pm 0.005\text{‰ W}^{-1}\text{m}^2$ for EDC. The regression for Dome F falls within 2 standard deviations (2σ) of the regression for EDC, but the regression for South Pole falls outside the 2σ uncertainty. $\delta\text{O}_2/\text{N}_2$ values from South Pole are higher than for EDC and Dome F for the same SSI, suggesting additional factors are influencing the records, such as accumulation rate, which at South Pole is around three times that of both EDC and Dome F. In the following sections, we provide evidence for the influences of accumulation rate and air temperature on $\delta\text{O}_2/\text{N}_2$, in addition to SSI, using both spatial (inter-site) and temporal (EDC ice core) variability of $\delta\text{O}_2/\text{N}_2$.

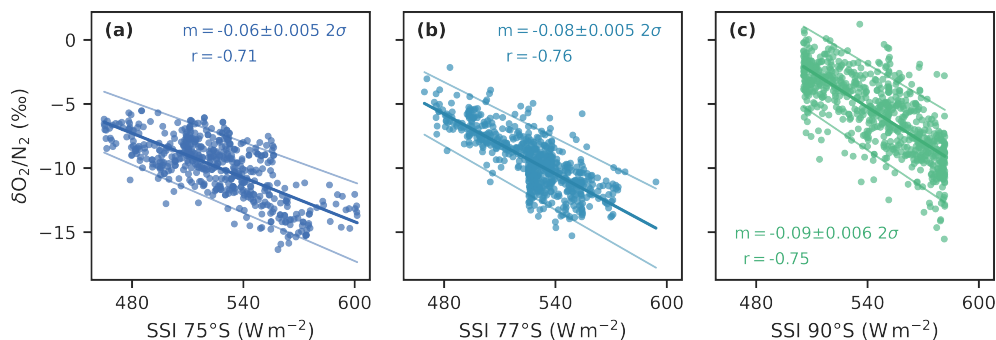


Figure 2. Scatter plots showing the negative correlation between SSI and $\delta\text{O}_2/\text{N}_2$. Significant negative correlations (over 99% confidence) are observed using relatively high resolution data from (a) EDC (Bouchet et al., 2023), (b) Dome F (Kawamura et al., 2007; Oyabu et al., 2021), and (c) South Pole (Severinghaus, 2019). The slope (m , units $\text{‰ W}^{-1}\text{m}^2$) and r values are presented for each site.

3.1.1 Inter-site comparison of mean $\delta\text{O}_2/\text{N}_2$

270 In addition to the $\delta\text{O}_2/\text{N}_2$ datasets, we compile SSI, accumulation rate, and temperature reconstructions from each site and take the mean values over the time periods which overlap in all records (Table 3). Drivers of mean $\delta\text{O}_2/\text{N}_2$ are then explored using regression analysis as presented in Fig. 3. The range of accumulation rates and temperatures over the given time period are included as error bars in Fig. 3b and 3c to indicate the climate histories for each site. SSI ranges for each site are excluded given

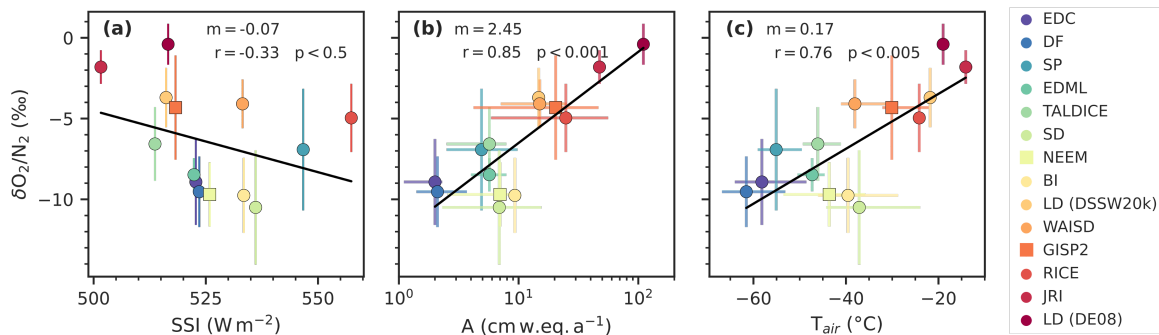


Figure 3. Scatterplots showing the dependence of $\delta\text{O}_2/\text{N}_2$ on a) SSI, b) accumulation rate (A), and c) air temperature (T_{air}). Each point represents the mean values of each site over the depth interval in Table 3. Error bars on y-axis show the standard deviation of $\delta\text{O}_2/\text{N}_2$, while x-axis error bars in (b) and (c) show the range of values over the depth interval. Linear regressions are shown in black, along with the associated slope (m), correlation coefficient (r), and p-value.

that they are substantially larger than the range in mean SSI between sites. Due to limited data availability from the Berkner
 275 Island ice core we take the average temperature and accumulation rate using present day values and last glacial maximum
 values (Capron et al., 2013). This is justified given that the data spans approximately the last glacial maximum to the start
 of the Holocene (Massam, 2018). Finally, present-day values are used for accumulation rate and temperature at DE08 and
 DSSW20k due to the relatively young ages corresponding to the $\delta\text{O}_2/\text{N}_2$ data (~ 90 a BP).

No significant correlation is observed between mean $\delta\text{O}_2/\text{N}_2$ and SSI in Fig. 3a ($r = -0.33$, $p < 0.5$), but the slope of -
 280 $0.07\text{‰ W}^{-1}\text{m}^2$ is the same as observed in Fig. 2. In contrast, Fig. 3b and 3c show a strong, significant correlation between
 mean $\delta\text{O}_2/\text{N}_2$ and both the natural log of accumulation rate ($r = 0.85$, $p < 0.001$) and temperature ($r = 0.76$, $p < 0.005$).
 The linear model in Fig. 3b indicates that a doubling of accumulation rate would result in a 1.3‰ increase in $\delta\text{O}_2/\text{N}_2$
 ($\delta\text{O}_2/\text{N}_2 = 2.5 \cdot \log(A) - 12$). However, it is important to note that temperature and the logarithm of accumulation rate
 are strongly correlated in Antarctica, such that the correlations seen in panels (b) and (c) of Fig. 3 are dependent on one another.

285 Deviations from the regression lines in Fig. 3b and 3c may be linked to discrepancies in site latitude resulting from the ice
 flow speed at different sites. Indeed, data from NEEM were measured on ice between 1757 and 2525 m depth (approximately
 38–130 ka BP), when the site would have been upstream of the current site at a lower latitude (Rasmussen et al., 2013;
 Members, 2013). In the case of Berkner Island and Siple Dome, we suggest that relatively low $\delta\text{O}_2/\text{N}_2$ values are the result of
 storage gas loss effects (Section 2.2.3) given that the measurements were carried out ~ 7 and ~ 8 years after coring for Berkner
 290 Island and Siple Dome, respectively. While clathrates are reportedly absent from both sites (Mulvaney et al., 2007; Neff, 2014),
 the low values may link to gas loss during storage within increasingly brittle ice at depth in the core.

3.1.2 Temporal variability of $\delta\text{O}_2/\text{N}_2$ at Dome C

High resolution data is required to investigate the temporal variability in $\delta\text{O}_2/\text{N}_2$ as a function of accumulation rate and
 temperature. The δ -deuterium (δD) record from water isotope measurements is used as a qualitative proxy for accumulation

Table 3. An overview of data used in Fig. 3. The depth range of data included may differ from the entire available $\delta\text{O}_2/\text{N}_2$ records given that we aim to compare the same intervals between each parameter. Mean values are presented for $\delta\text{O}_2/\text{N}_2$, annual accumulation rate, annual mean temperature, and SSI at the current site latitude. Where age scales are available, the SSI represents the mean values at the present day site latitude. For sites without age scales, the average SSI over last 1000 years is used.

Site	Depth range (m)	Age range (kaBP)	$\delta\text{O}_2/\text{N}_2^a$ (‰)	Accu. rate ^b (cm w.eq a ⁻¹)	Temp. ^c (°C)	SSI (W m ⁻²)
BI ¹	609–694		-9.8 ± 2.3	9.3	-39.6	533
DF ²	113–794, 1456–2149	2.9–38.1, 10.0–207.8	-9.5 ± 2.2	2.1	-61.5	524
EDC ³	1421–3189	105.9–805.1	-8.9 ± 2.8	2.0	-58.2	523
EDML ⁴	595–860	9.3–16.4	-8.5 ± 1.0	5.7	-47.3	522
GISP2 ⁵	73–2395	0.2–50	-4.3 ± 3.2	20.4	-30.1	518
JRI ⁶	76–359	0.03 - 14.3	-1.8 ± 1.0	47.4	-14.1	502
LD (DE08) ⁷	175–218	0.008–0.011	-0.4 ± 1.3	110.3	-19.0	517
LD (DSSW20k) ⁸	61–63		-3.7 ± 1.8	14.7	-21.8	516
NEEM ⁹	1757–2396	38.1–121.4	-9.7 ± 2.0	7.0	-43.6	526
RICE ¹⁰	60–344	0.1–2.6	-5.0 ± 2.1	24.8	-24.2	557
SD ¹¹	500–969	7.6–95.0	-10.5 ± 3.5	6.9	-37.1	536
SP ¹²	125–1749	1.1–54.2	-6.9 ± 3.8	4.9	-55.1	547
TALDICE ¹³	155–1072	1.5–40.0	-6.6 ± 2.3	5.7	-46.1	514
WAIS ¹⁴	80–962, 1700–3397	0.2–4.1, 9.0–66.2	-4.1 ± 1.5	15.0	-38.1	533

¹This study^a, Capron et al., 2013^{b,c};

²Kawamura et al., 2007^a, Oyabu et al., 2021^a, Kawamura et al., 2017^b, Uemura et al., 2018^c;

³Bouchet et al., 2023^a, Bazin et al., 2013^b, Jouzel et al., 2007^c;

⁴This study^a, Bazin et al., 2013^b, Stenni et al., 2010^c;

⁵This study^a, Suwa and Bender, 2008b^a, Cuffey and Clow, 1999^b, Clow, 1999^c;

⁶This study^a, Mulvaney et al., 2012^{b,c};

⁷Buizert et al., 2020^a; Rubino et al., 2013^b, Etheridge and Wookey, 1988^c;

⁸Buizert et al., 2020^a, Rubino et al., 2013^b, Morgan et al., 1997^c;

⁹This study^a, Rasmussen et al., 2013^{b,c};

¹⁰Lee et al., 2020^a, Winstrup et al., 2019^b, Bertler et al., 2017^c;

¹¹Severinghaus, 2009^a, Buizert, 2021^{b,c};

¹²Severinghaus, 2019^a, Kahle et al., 2020^{b,c};

¹³This study^a, Bazin et al., 2013^{b,c};

¹⁴Severinghaus, 2015^a, Fudge et al., 2017^b, White et al., 2019^c.

295 rate and temperature, whereby higher δD values are generally associated with increased accumulation rate and temperature in ice cores from the East Antarctic plateau (Jouzel et al., 2007; Parrenin et al., 2007). The following analysis uses the longest period of relatively high-resolution $\delta O_2/N_2$ measurements from the EDC ice core between 190–259 ka BP (1980–2350 m) on the AICC2023 ice-age chronology (Bouchet et al., 2023).

Two approaches are used to extract the non-SSI signals in the $\delta O_2/N_2$ records. First, we interpolate SSI onto the $\delta O_2/N_2$ ages and take the deviations from the $\delta O_2/N_2$ -SSI linear regression to isolate the $\delta O_2/N_2$ variability not explained by SSI (hereafter, $\delta O_2/N_2$ -SSI residual). The second approach directly investigates the millennial-scale variability by applying a low pass filter to the $\delta O_2/N_2$ and δD records (interpolated onto a 100-year time step), using a 10-kyr cut-off to isolate the low-frequency signals associated with SSI. The filtered curves are then subtracted from the original curves to remove the orbital (SSI) signal, and a 5-point moving average is applied to the residuals to reduce noise but retain millennial-scale variability in the records.

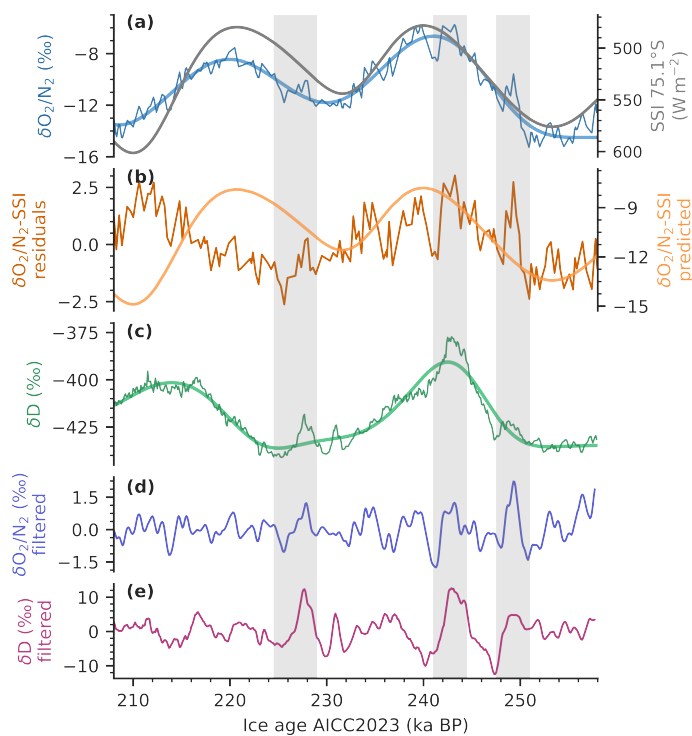


Figure 4. Evolution of $\delta O_2/N_2$, SSI and δD on the AICC2023 ice age timescale from EDC (Bouchet et al., 2023). Panel (a) presents the 100-year interpolated $\delta O_2/N_2$ overlain with the low pass filtered curve (blue). The right y-axis in panel (a) shown SSI at $75.1^\circ S$ (grey). The predicted $\delta O_2/N_2$ as a function of SSI ($\delta O_2/N_2$ -SSI predicted) is shown on the right axis of panel (b), and the residuals of the observed $\delta O_2/N_2$ and predicted are on the left axis. Panel (c) shows the 100-year interpolated δD overlain with the low pass filtered curve (green). The bottom two panels present the residuals of the low pass filtered curves for $\delta O_2/N_2$ (d) and δD (e). Grey bars highlight the pronounced millennial-scale variability.

305 Figure 4 primarily shows the dominant SSI cyclicity in the $\delta\text{O}_2/\text{N}_2$ record, as has been documented previously (e.g., Landais
et al., 2012). Superimposed onto this signal are millennial-scale peaks in $\delta\text{O}_2/\text{N}_2$ which appear to coincide with peaks in δD ,
highlighted by grey bars. This high frequency variability is more clearly identified from the filtered curves in Fig. 4d and
4e. The coherence between millennial-scale peaks in $\delta\text{O}_2/\text{N}_2$ and δD suggests a positive correlation with accumulation rate
and temperature, which shares analogy with the spatial positive correlation between $\delta\text{O}_2/\text{N}_2$ and both accumulation rate and
310 temperature (Fig. 3). We note a remnant 20-kyr variability in the $\delta\text{O}_2/\text{N}_2$ -SSI residual which is in phase with δD . This orbital-
scale signal is present when using either the AICC2012 chronology or the AICC2023 chronology (Bazin et al., 2013; Bouchet
et al., 2023). Given that the new AICC2023 age scale (used here) has been orbitally tuned using this data (Bouchet et al., 2023),
this signal is not expected to be the result of phase difference between the EDC chronology and SSI.

3.2 Crocus model results

315 3.2.1 Crocus model evaluation for Dome C

The Crocus model outputs are first evaluated by comparing the reference simulation (Ref in Table 2) to observational data
from Dome C. Simulated density and SSA profiles are compared to data from Libois et al. (2014), measured daily between 23
November 2012 and 16 January 2013 at two sites within 600m of Concordia station, Dome C. Density was measured at 2.5 cm
resolution down to 25 cm, while SSA was measured at 1 cm depth intervals down to 50 cm. Snow temperature at Dome C has
320 been continuously measured since 2012 at 30-minute intervals. Simulated snow density and SSA were interpolated to a fixed
grid of 1 cm depth resolution and a 24-hour timestep between 1 January 2010 and 1 December 2020, while snow temperature
was interpolated onto a 1 mm by 6-hourly grid over the same time period.

Density and SSA outputs presented in Fig. 5a and 5b are averaged values over the measurement period. For the most part,
the observations fall within the range of the simulations. Density is well-simulated throughout the top 25 cm. The simulated
325 SSA profile is consistently within one standard deviation of the measurements below 10 cm, above this depth, simulated SSA
is overestimated by up to $10\text{ m}^2\text{ kg}^{-1}$. Small standard deviations associated with simulated density and SSA, suggests that
variability is not well reproduced. As discussed in Libois et al. (2014), the standard version of Crocus is unable to reproduce
density and SSA variability with depth due to its one-dimensional nature. For the purpose of our study, we consider the standard
version sufficient to assess the overall sensitivity of snowpack properties to perturbations in forcings.

330 Snow temperature in Fig. 5c covers the period between 23 November 2019 and 16 January 2020. A 3°C cold bias is apparent,
but the mean falls within 1σ of the observations. Figure 5d presents distributions of the stacked January snow temperatures
between 2016 and 2020, further showing this 3°C cold bias during summer ($-37.1 \pm 3.6^\circ\text{C}$ and $-34.4 \pm 4.1^\circ\text{C}$ for Crocus outputs
and observations, respectively). However, winter snow temperatures are well simulated with a 1 m mean of $-64.7 \pm 4.5^\circ\text{C}$ and
 $-63.9 \pm 5^\circ\text{C}$ from Crocus outputs and observations, respectively. The overestimation of simulated SSA in the top 10 cm may
335 be linked to the cold bias in modelled snow temperature during summer via the reduced rate of snow metamorphism in near-
surface snow. Alternatively, high SSA may be the result of a recent precipitation event. During large precipitation events the
fresh snow will be buried rapidly and undergo less metamorphism than the topmost snow given that most metamorphism occurs

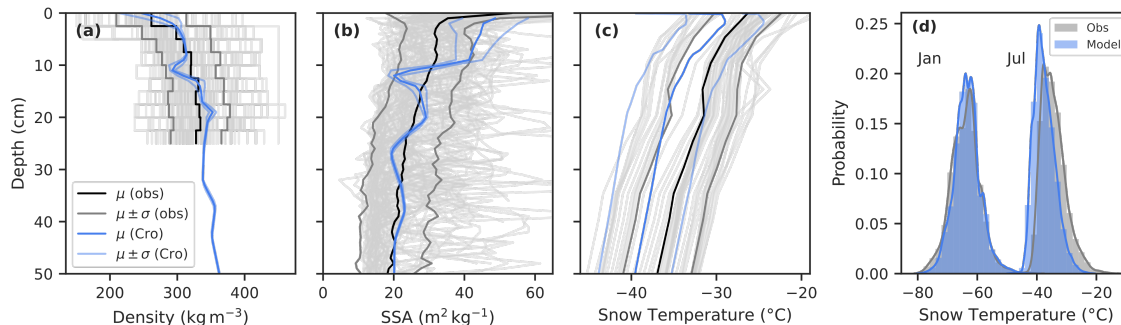


Figure 5. Comparison of observations and Crocus simulated snowpack profiles. Density (a) and SSA (b) profiles represent the average from 23 November 2012 and 16 January 2013, to cover the measurement period (Libois et al., 2014). The snow temperature (c) profiles both from Crocus and the observations are the average from 23 November 2019 and 16 January 2020. Faded grey lines represent individual profiles from observations, and the shaded bands show the standard deviations. Snow temperature distributions (d) from January and July between 2016 and 2020.

in the top 5 cm where solar radiation drives strong temperature gradients (Picard et al., 2012). This could result in sustained high SSA in the top 10 cm.

340 3.2.2 Simulated response of snowpack properties to surface perturbations

Sensitivity tests were run using the Crocus model to assess the response of near-surface snowpack properties to perturbations in local surface forcings. The following analysis uses optical radius as a measure of grain size – which is directly linked to SSA and the density of ice (Section 2.3.1) – and focuses on the response of near-surface snow density and grain size to the six scenarios outlined in Table 2. We firstly assess the bulk changes in physical properties before looking at the variability with
 345 depth.

3.2.3 Bulk snowpack sensitivity

Numerous studies have suggested that modifications in near-surface density and grain size are key parameters influencing elemental fractionation during pore closure (e.g., Bender, 2002; Fujita et al., 2009). Figure 6c shows the mean difference in density and grain size from the Dome C reference simulation and each of the test scenarios (outlined in Table 2). Overall, grain
 350 size is more sensitive to changes in surface forcing than density in the upper 20 cm. The sensitivity tests reveal that a 15% decrease in SSI (SSI min) decreases grain size by 8% and an 11% increase in SSI (SSI max) causes a 12% increase in grain size. Both directions of perturbation result in <1% change in density. The magnitudes of change in both density and grain size are much larger under accumulation rate and temperature perturbations than under SSI perturbations.

Accumulation rate and temperature have the opposite effect on density and grain size. A 4°C increase in temperature (T
 355 max) increases density and grain size by 8% and 29%, respectively, while increasing the accumulation rate to 4.1 cm w.eq. a⁻¹ (A max) results in a 7% decrease in density and a 10% decrease in grain size. The opposing influence of accumulation rate

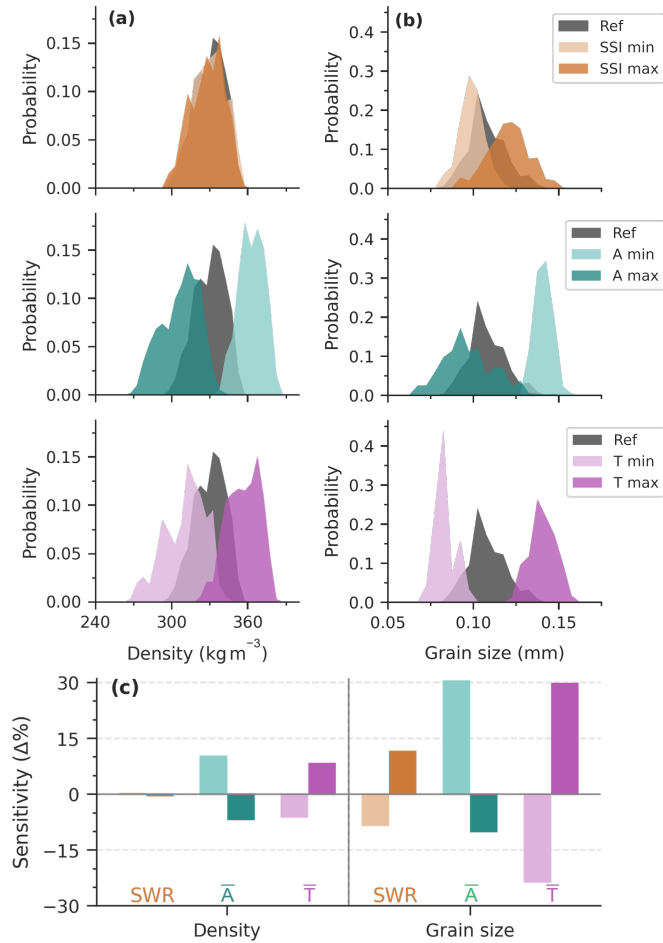


Figure 6. Comparison of density and grain size (r_{opt}) over the top 20cm from Crocus sensitivity simulations. Distributions of a) density and b) grain size outputs from each test simulation are compared to the reference simulation (bin size is 5 kg m^{-3} , and 0.005 mm). In panel c) bars represent the percentage change in mean density and mean grain size for perturbations in SSI (orange), accumulation rate (green), and temperature (purple); with the decreased scenarios represented by the faded colour, and the increased by the bold colour.

and temperature at first appears to contradict the observations in Fig. 3, where $\delta\text{O}_2/\text{N}_2$ increases with both variables. Mean density and grain size respond non-linearly to perturbations in all forcing parameters, as is shown by the magnitude of increase in grain size from decreased accumulation rate being three times greater than the magnitude of decrease induced by an increase in accumulation rate (right panel of Fig. 6c, green bars). This is in line with the dependence of $\delta\text{O}_2/\text{N}_2$ to the logarithm of accumulation rate documented in Fig. 3.

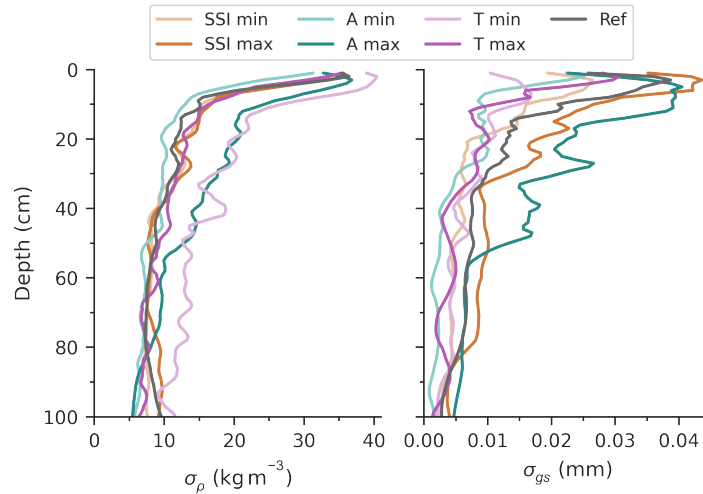


Figure 7. Variability in density and grain size with depth over the top 1 m. Each pair of simulations is represented by a colour, SSI in orange, accumulation rate in green, and temperature in purple. The faded line of each pair represents the 800-ka minimum simulation, and the bold line represents the 800-ka maximum simulation.

3.2.4 Depth variability sensitivity

An alternative (although possibly complementary) explanation for the mechanistic control of snow properties on elemental fractionation links to stratigraphic layering due to seasonality (Fujita et al., 2009). Here we explore the influence of layering
 365 by looking at the depth variability in density and grain size as a qualitative measure of stratification (Hörhold et al., 2011), assuming that higher variability indicates stronger layering. Variability is defined as the standard deviation of each depth interval (denoted σ) over the period between January 1st 2010 and December 1st 2020.

The σ values for each simulation are presented in Fig. 7 for the top 1 m of snowpack. In all runs, σ peaks near the surface and decreases with depth for both density and grain size (σ_ρ and σ_{gs}). Density variability for four out of the six test simulations
 370 is largely similar to the reference. High-accumulation rate (A max) and low-temperature (T min) are the exception, with an increase in σ_ρ of up to 5 kg m^{-3} compared to all other runs. Increased σ_ρ values correspond to a decrease in mean density in the A max and T min simulations (Fig. 6). The spread in σ_{gs} between simulations is broader than for σ_ρ over the top 50 cm, with T min, SSI min, A min, and T max all resulting in reduced variability compared to the reference run. σ_{gs} appears to increase with an increase in SSI and accumulation rate throughout the top metre.

375 To summarise, outputs from the Crocus model indicate that insolation modifies mean grain size but has negligible effect on mean density in the top 20 cm. On the other hand, higher air temperature and lower accumulation rate result in increases in both mean density and mean grain size, although this change is not necessarily proportional. The depth variability of the two snowpack parameters is strongly influenced by increased accumulation rate, with decreased temperature also having a large

effect on density variability, and increased SSI causing an increase in grain size variability. At 100 cm, there is no significant
 380 difference in the σ_ρ and σ_{gs} for the different forcing scenarios, which is discussed in Section 4.4.

4 Discussion

4.1 Evidence for non-SSI dependence of $\delta O_2/N_2$

The compilation of deep ice core $\delta O_2/N_2$ records in Fig. 2 reinforces the widely documented anti-correlation between SSI and $\delta O_2/N_2$ (e.g. Oyabu et al., 2022; Bouchet et al., 2023). However, a comparison of EDC, Dome F, and South Pole (Fig. 2)
 385 reveals an additional influence of site conditions which cannot be explained by SSI. Indeed, our compilation of records from 14 sites shows that mean $\delta O_2/N_2$ is strongly correlated with accumulation rate and temperature (Fig. 3). Interestingly, SSI does not significantly influence site mean $\delta O_2/N_2$ but the spatial slope ($0.07\text{‰}W^{-1}m^2$; Fig. 3) is the same as the temporal slope ($0.07\text{‰}W^{-1}m^2$; Fig. 2). A key difference between the temporal and spatial variations in $\delta O_2/N_2$ may link to the range
 390 of variations in the three forcing parameters. For example, the spatial variations in accumulation rate are much larger than the variations at a single site through time. Conversely, the spatial range of SSI values is between $500\text{--}560Wm^{-2}$, whereas the range at EDC, for example, is between $470\text{--}600Wm^{-2}$.

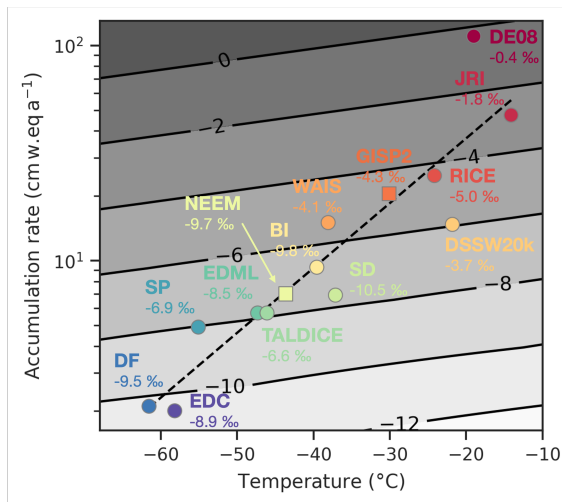


Figure 8. $\delta O_2/N_2$ as a function of accumulation rate and temperature ($Avg. \delta O_2/N_2 = 0.03 \cdot T + 2.8 \cdot \log(A) - 14.3$). Measured mean $\delta O_2/N_2$ values are noted alongside each site. The accumulation rate-temperature regression (dashed, black line) is defined using a regression on temperature and accumulation rate for all sites in the data compilation.

To further constrain the drivers of $\delta O_2/N_2$ variability, we construct a multiple regression to parameterize mean $\delta O_2/N_2$ as a function of accumulation rate and temperature (Fig. 8). Combined, accumulation rate and temperature can explain up to 70% of the total variance in mean $\delta O_2/N_2$. Adding SSI does not improve the adjusted r^2 of the multiple regression. Results
 395 are summarised in Fig. 8 and reiterate that $\delta O_2/N_2$ is highly sensitive to accumulation rate, especially at low accumulation

sites. The site dependence of $\delta\text{O}_2/\text{N}_2$ we observe has been noted in previous studies. Indeed, Bazin et al. (2016) identified an offset in absolute $\delta\text{O}_2/\text{N}_2$ values in the Vostok core compared to Dome F and EDC, similar to our observation in Fig. 2. By including records from numerous ice cores we are able to definitively show that absolute values are systematically linked to site accumulation rate and temperature.

400 4.2 Millennial scale variability in $\delta\text{O}_2/\text{N}_2$ records

Further investigation into drivers of $\delta\text{O}_2/\text{N}_2$ variability in the EDC core reveals a millennial-scale climate signal in the $\delta\text{O}_2/\text{N}_2$ records. The timing of these anomalies in $\delta\text{O}_2/\text{N}_2$ correspond to those in the δD record from EDC between 200–260 ka BP (Fig. 4). This suggests that millennial-scale variations can arise from changes in accumulation rate and/or temperature. The anomalies observed in the EDC $\delta\text{O}_2/\text{N}_2$ record are not unique to this period but vary between time periods and sites
405 (Supplement S2). Indeed, a similar effect was previously observed in the GISP2 core, where $\delta\text{O}_2/\text{N}_2$ was found to be positively correlated with local temperature over millennial timescales (Dansgaard-Oeschger events) (Suwa and Bender, 2008b).

Previous studies suggest an overlap between the drivers of $\delta\text{O}_2/\text{N}_2$ variability and those of total air content (TAC) variability (Fujita et al., 2009; Lipenkov et al., 2011). Ice core $\delta\text{O}_2/\text{N}_2$ and TAC records exhibit slight differences in their spectral signals, whereby $\delta\text{O}_2/\text{N}_2$ is dominated by precession (hence SSI pacing), whereas TAC is dominated by obliquity (hence the integrated
410 summer insolation pacing). However, variability in both records is linked to local insolation via the modulation of near-surface snow properties, which ultimately influence pore closure processes (Lipenkov et al., 2011). Fujita et al. (2009) hypothesised that the permeation mechanism, driving fractionation of $\delta\text{O}_2/\text{N}_2$, can explain half the variation in TAC, with the rest being driven by effusion. Therefore, we draw on TAC studies to help interpret millennial-scale variability in $\delta\text{O}_2/\text{N}_2$. Recent observations found a hemispheric contradiction in the millennial-scale drivers of TAC variability. TAC is anti-correlated with accumulation
415 rate in the NGRIP core (Eicher et al., 2016) but positively correlated in the South Pole ice core (Epifanio et al., 2023).

Several mechanisms have been proposed to explain millennial-scale variability in TAC and $\delta\text{O}_2/\text{N}_2$. Eicher et al. (2016) attributed the anti-correlation between TAC and accumulation rate during Dansgaard-Oeschger (D-O) events at NGRIP to transient effects in the firn column. During the initial stage of the D-O event, rapid increases in accumulation rate increase overburden pressure, reducing the pore volume at close off, and hence, TAC (Eicher et al., 2016). Changes in overburden
420 pressure were also proposed to explain an anti-correlation between $\delta\text{Ar}/\text{N}_2$ (and thus, $\delta\text{O}_2/\text{N}_2$), and accumulation rate over multi-decadal timescales at GISP2 (Kobashi et al., 2015). In contrast, the positive correlation between TAC and accumulation rate at South Pole is attributed to increased snow burial rates, leading to smaller grains and thus, increased pore volume at close-off (Epifanio et al., 2023). Such a grain size mechanism is understood to drive the integrated summer insolation signal in TAC records (Raynaud et al., 2007), and also the SSI signal in $\delta\text{O}_2/\text{N}_2$ records (e.g. Bender, 2002).

425 Transient effects in the firn column in response to rapid climatic changes (linked to overburden pressure) are expected to be largely absent from Antarctic sites due to reduced magnitude in climate variability compared to Greenland. However, an accumulation-dependent grain size mechanism may explain the positive correlation between δD and $\delta\text{O}_2/\text{N}_2$ at EDC. Epifanio et al. (2023) proposed that the contradictory behaviour of TAC between NGRIP and South Pole may be explained by varying responses of the firn to changes in accumulation rate depending site surface climate conditions. They suggest that a grain

430 size mechanism dominates TAC modulation at low accumulation sites while transient effects from rapid climatic changes
 are more important at warm, high accumulation sites. We expect that the mechanisms driving $\delta O_2/N_2$ are also modulated
 by accumulation rate. Indeed, observations of $\delta O_2/N_2$ records from South Pole appear to support the in-phase coherence
 between $\delta O_2/N_2$ and δD in the EDC core, but only when δD is sufficiently low (Fig. S5 in Supplement). A shifted, anti-
 435 accumulation conditions. phase relationship is apparent when δD is higher, which suggests that different mechanisms may be dominant under high

4.3 Towards a mechanistic understanding of $\delta O_2/N_2$ variability at low-accumulation sites

While a link between climate and snow metamorphism has been evidenced in previous studies - whereby snow metamorphism
 is enhanced during summers with very low accumulation rates (Picard et al., 2012; Casado et al., 2021) – the link to pore
 closure processes has received less attention. A possible reason for this is the added complexity which would be required to
 440 implement surface snow metamorphism into firn models, accompanied with the need for prior information such as surface
 grain size. The following sections propose some ideas to bridge this gap by focusing on both local climate parameters and SSI,
 their influence on near-surface snow metamorphism, and how this might modulate elemental fractionation during pore closure.

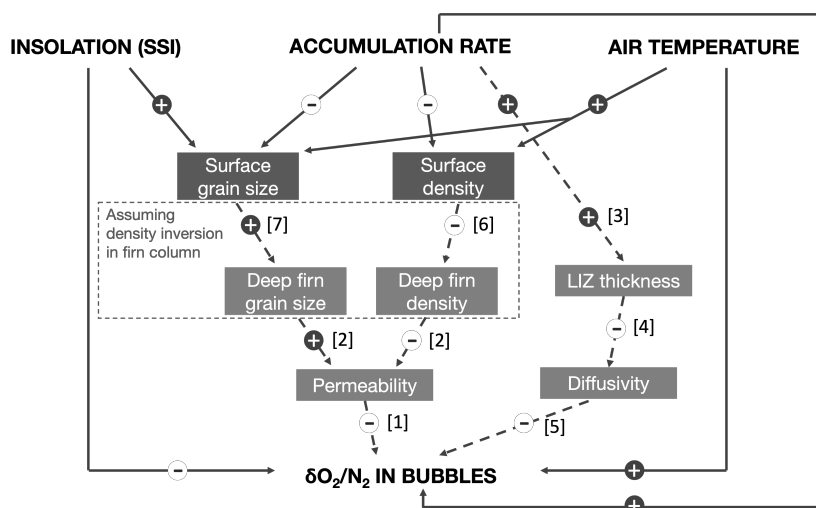


Figure 9. Schematic to show interactions between surface forcings, physical properties, and close-off fractionation. Plus signs show a direct relationship (i.e., increase in SSI corresponds to increase in grain size), and minus signs indicate an inverse relationship. We use full lines to show results from our study, and dashed lines to show links based on previous studies, the numbers for which can be found in the text with associated references.

4.3.1 Surface snow properties

Variations in grain properties are thought to drive the SSI signal in $\delta\text{O}_2/\text{N}_2$ records (Raynaud et al., 2007). Indeed, results
445 from sensitivity tests in Fig. 6 show an increase in grain size under increased SSI, which is attributed to both stronger near-
surface temperature gradients (Appendix B in Vionnet et al., 2012) and higher snow temperatures during summer (Fig. S4 in
Supplement). Negligible change in simulated density under perturbations in SSI appears to support the hypothesis of a near-
surface grain size mechanism (e.g., Bender, 2002), although this may be due to the absence of vapour transport in the Crocus
model. Increased snow metamorphism rate can also explain the increased grain size with increased temperature (Legagneux
450 et al., 2003), while an increase in density results from increased compaction rates (Vionnet et al., 2012). The decrease in grain
size with increased accumulation rate is the result of longer residence time of a snow layer in the upper centimetres to metres
of the snowpack, where temperature gradients are strongest (Picard et al., 2012).

It is widely accepted that permeation is the process by which small molecules escape during pore closure (Fig. 9 [1]; e.g.,
Ikeda-Fukazawa et al., 2004; Huber et al., 2006; Severinghaus and Battle, 2006). Gregory et al. (2014) found that permeability
455 is increased in high-density, large-grained firn due to a less complex pore structure. Indeed, Calonne et al. (2022) showed that
grain size has a strong influence on permeability, such that for a given density, permeability is increased with grain size (Fig.
9 [2]). Our results show that high SSI and low accumulation rate are associated with larger grain size and lower $\delta\text{O}_2/\text{N}_2$. This
observation supports the hypothesis that increased SSI (decreased accumulation rate) ultimately leads to lower $\delta\text{O}_2/\text{N}_2$ due to
the increased permeability associated with increased grain size (e.g., Severinghaus and Battle, 2006; Fujita et al., 2009), and
460 suggests a similar mechanism can explain the accumulation rate dependence.

Identifying the mechanisms driving the accumulation rate dependence of $\delta\text{O}_2/\text{N}_2$ is complicated by the fact that, at polar
sites, accumulation rate tends to covary with temperature (Fig. 8). Thus, an increase in grain size with increased near-surface
residence time (decreased accumulation rate) will be countered by reduced snow metamorphism rates with a decrease in
temperature (Fig. 6). These counteracting effects were invoked by Kawamura et al. (2007) to explain the absence of a 100-ka
465 periodicity in $\delta\text{O}_2/\text{N}_2$ records at Dome Fuji. However, the stronger correlation between $\delta\text{O}_2/\text{N}_2$ and accumulation rate than
temperature in Fig. 3 suggests a dominant role of accumulation. Therefore, we propose that a grain size mechanism – like that
of SSI – may explain the positive correlation between accumulation rate and $\delta\text{O}_2/\text{N}_2$ in the EDC core (Fig. 3b).

Previous studies propose that firn column characteristics, such as delta-age, will also modulate $\delta\text{O}_2/\text{N}_2$ via changes in
accumulation rate and temperature (Severinghaus and Battle, 2006; Bazin et al., 2016). One mechanism links to the time
470 for pores to close off. At low accumulation sites, pores will take longer to fully close, and thus, experience more elemental
fractionation (Severinghaus and Battle, 2006). Additional hypotheses point to LIZ thickness and pore space geometry (or
tortuosity) (e.g., Fujita et al., 2009). Low accumulation sites tend to have thinner LIZs (Fig. 9 [3]; e.g., Landais et al., 2006;
Witrant et al., 2012) and less tortuous pore structure in deep firn associated with large, rounded grains (Gregory et al., 2014).
Such characteristics are associated with increased gas diffusivity that would facilitate the removal of O_2 -enriched gas back to
475 the atmosphere (Fig. 9 [4]). In contrast, at high accumulation sites, the associated decrease in gas diffusivity in the LIZ would
lead to a build up of a stagnant air enriched in O_2 resulting in the trapping of gas with relatively high $\delta\text{O}_2/\text{N}_2$ (Fig. 9 [5]).

Alternatively, Hutterli et al. (2009) proposed that varying near-surface temperature gradients under different SSI intensities modulate anisotropy of the snow, as was confirmed by Leinss et al. (2020), leading to vertically elongated pores under high SSI (low accumulation) conditions. They argue that elongated pores facilitate vertical diffusivity in the LIZ, leading to greater
480 fractionation of $\delta\text{O}_2/\text{N}_2$ (Hutterli et al., 2009), an alternative but complimentary mechanism to LIZ thickness.

The aforementioned mechanisms relating to firn column characteristics indicate a positive correlation between $\delta\text{O}_2/\text{N}_2$ and accumulation rate. This is consistent with Fig. 3b but cannot be directly supported by our sensitivity results. Based on the sensitivity tests in Fig. 6, a link to surface density is not clear. We expect that the role of density in modulating $\delta\text{O}_2/\text{N}_2$ derives from the grain size dependence of densification rates invoked by Freitag et al. (2004), providing an additional link between
485 near-surface grain size and $\delta\text{O}_2/\text{N}_2$, as is outlined in the following section.

4.3.2 Depth-dependent variability as a proxy for layering

Density stratification in deep firn has also been invoked to modulate $\delta\text{O}_2/\text{N}_2$ (Fujita et al., 2009). Results from the Crocus model are used to infer the sensitivity of near-surface density and grain size variability to perturbations in input forcing parameters. Figure 7 shows that grain size variability is increased with an increase in both SSI and accumulation rate. For SSI, this is
490 expected given enhanced snow metamorphism during summer due to higher snow temperatures (Fig. S4 in Supplement), while winter conditions are largely unchanged. Decreased grain size variability in both the increased and decreased temperature simulations is likely linked to the way in which temperature forcing is perturbed. By applying a constant increase in air temperature, the strength of metamorphism is increased during winter due to higher temperatures (Legagneux et al., 2003; Flanner and Zender, 2006), but largely unchanged during summer due to the dominant influence of insolation on summer snow
495 temperature (Fig. S4), resulting in homogeneity within the snowpack.

Linking variability near the surface with variability in deep firn is not trivial. Indeed, a study by Hörhold et al. (2011) used a compilation of firn cores from numerous polar sites to show that density variability in deep firn is positively correlated with local accumulation rate and temperature, but anti-correlated with near-surface density variability. However, this anti-correlation was not observed by Inoue et al. (2023) when comparing firn cores in the Dome Fuji area. Additional consideration both from
500 data and modelling approaches is required for density inversions in the firn column – whereby relatively low-density layers located in the upper part of the firn become relatively high-density layers below the density inversion depth, due to preferential deformation in the upper firn (Fig. 9 [6]; Freitag et al., 2004; Fujita et al., 2009). Freitag et al. (2004) proposed that the inversion is largely driven by grain size, such that initially low-density layers associated with large grain size become relatively high-density layers with large grain size below the density inversion (Fig. 9 [7]). This has since been supported by Gregory et al.
505 (2014) who further show that near surface grain size determines the density at which pores close-off. They show that large-grained, high-density layers are more permeable and hence, close off deeper than fine-grained, low-density layers. In addition, Hörhold et al. (2012) suggested that stratification at depth is influenced by impurity content, with impurity-rich layers being more susceptible to densification. Given the array of factors proposed to influence deep firn density variability, we focus on the role of grain size variability.

510 No inversion is observed for grain size variability. Deep firn layers retain evidence of near-surface grain size, which is determined by snow metamorphism and accumulation rate, as mentioned previously (Gregory et al., 2014). While our sensitivity tests are constrained to the near surface, we draw on previous studies to suggest potential implications for deep firn properties and $\delta\text{O}_2/\text{N}_2$. Given the presence of a density inversion at Dome C (Hörhold et al., 2011), we may expect that relatively increased variability in near-surface grain size from our sensitivity tests would translate to increased grain size and density
515 variability in the deep firn. As such, increased grain size variability in our SSI max simulation (Fig. 7) supports the conclusions of Fujita et al. (2009), that elemental fractionation is enhanced under high SSI conditions due partially to layering.

The link to accumulation rate is less clear. As for SSI, we observe an increase in grain size variability with increased accumulation rate. However, according to the layering hypothesis, this should result in more $\delta\text{O}_2/\text{N}_2$ fractionation at close off, which contradicts our observations of a positive correlation between $\delta\text{O}_2/\text{N}_2$ and accumulation rate (Fig. 3b). Instead, we
520 suggest that a decrease in mean grain size with increased accumulation rate is dominant over the layering effect. Future work would benefit from an inter site comparison of deep firn properties alongside gas measurements in order to disentangle these effects.

Extracting concrete conclusions from our variability analysis and extrapolating these into the deep firn is inhibited by both the ascribed forcing perturbations and the aggregation scheme of the model, which is particularly sensitive to changes in
525 accumulation rate. We thus conclude that the simulations performed with the Crocus model can support a mechanism linked to average grain size on $\delta\text{O}_2/\text{N}_2$ but not a mechanism implying density or grain size variability. However, our conclusion does not rule out the effect of layering or grain size variability on $\delta\text{O}_2/\text{N}_2$ variability but highlights a limitation in our study, as explained in the next section.

4.4 Limitations and perspectives

530 A number of limitations have been mentioned throughout our study and warrant some further discussion. As mentioned in Section 4.3.2, our study is unable to fully consider the sensitivity of layering to perturbations in forcing parameters. Firstly, near-surface density and grain size variability are not fully captured by the model which can be partially attributed to the absence of snow transport by the wind in the standard version of Crocus (Libois et al., 2014). While wind is known to strongly influence snow properties (e.g. Inoue et al., 2023), we are limited in our understanding of winds throughout the past 800 ka
535 and therefore wind effects are not considered in our study. Secondly, the aggregation of layers with depth in Crocus make it difficult to focus on both the fine-layered near-surface snow, and the propagation of stratified layers into the deep firn. Accurate assessment of the layering effect would require a new dedicated snow model preserving individual snow layers and properties over a large depth range, from the surface to LIZ, and at high resolution.

While the single-parameter sensitivity tests presented here provide useful insights for understanding physical mechanisms,
540 they do not account for complex compound effects associated with the covariance of accumulation rate and temperature at polar sites. Additional tests perturbing both accumulation rate and temperature simultaneously indicate that snowpack properties are very sensitive to the ascribed accumulation rate and temperature values i.e., for glacial temperature reconstructions which are debated to have been overestimated by up to 5°C (Buizert et al., 2021). Moreover, the additive effects from the single-parameter

sensitivity tests (accumulation rate and temperature) do not equal the effects of the multi-parameter sensitivity simulations (i.e.,
545 perturbing both accumulation rate and temperature), highlighting the complex influence of quasi-covarying accumulation rate
and temperature on snow properties. Given the uncertainties in climatic reconstructions and the limitations mentioned above,
we did not attempt to use the model for glacial-interglacial simulations to avoid misinterpreting the results.

Finally, the limited availability and temporal range of $\delta\text{O}_2/\text{N}_2$ records from Greenland cores meant that our study is slightly
biased towards Antarctic sites, which tend to be characterised by low accumulation rates. Although peaks in $\delta\text{O}_2/\text{N}_2$ corre-
550 sponding to Dansgaard-Oeschger events are apparent in data from GISP2, previously observed by Suwa and Bender (2008b),
much of the data was either of too low resolution or influenced by storage gas-loss to perform additional analysis. Given
this bias, we were unable to explore the opposing millennial-scale behaviour observed at low and high accumulation sites for
both $\delta\text{O}_2/\text{N}_2$ and TAC (Kobashi et al., 2015; Eicher et al., 2016). Future studies would therefore benefit from obtaining high
resolution measurements from sites with different characteristics.

555 **5 Conclusions**

We present a compilation of $\delta\text{O}_2/\text{N}_2$ records measured on multiple ice cores from Greenland and Antarctica, to improve the
mechanistic explanation for $\delta\text{O}_2/\text{N}_2$ variability. Analysis of both temporal (single-site) and spatial (multi-site) variability in
 $\delta\text{O}_2/\text{N}_2$ presents new evidence of a dependence on local climate (accumulation rate and temperature), in addition to the well-
documented SSI dependence. High resolution measurements from the EDC ice core reveals millennial-scale variability in
560 $\delta\text{O}_2/\text{N}_2$ in-phase with δD records when both parameters are plotted on the AICC2023 ice-age scale. The inter-site analysis
showed an increase in mean $\delta\text{O}_2/\text{N}_2$ for sites with higher accumulation rate and temperature, which is analogous with the
temporal analysis from EDC showing $\delta\text{O}_2/\text{N}_2$ to increase together with δD .

We suggest that a mechanism relating to firn physical properties can partially explain both the influence of SSI and local
climate on $\delta\text{O}_2/\text{N}_2$ variability. Sensitivity tests using the Crocus model show that grain size is very responsive to perturbations
565 in SSI, accumulation rate and air temperature, while density responds to all but SSI perturbations. Our findings support the
hypothesis that a grain size mechanism is the dominant driver of elemental fractionation at low accumulation sites, such that
increased grain size for a given density facilitates O_2 expulsion via enhanced permeability. Furthermore, our results support
the hypothesis that the presence, or lack thereof, of a local climatic signal in $\delta\text{O}_2/\text{N}_2$ variability is due to the delicate balance
between the counter-effects of accumulation rate and temperature on grain properties. However, the inter-site results suggest
570 that low accumulation, low temperature sites experience stronger elemental fractionation, having a comparable effect to high
insolation.

While our findings from the $\delta\text{O}_2/\text{N}_2$ data compilation can be supported by the Crocus sensitivity tests, we acknowledge that
additional mechanisms are at play. In particular, the influence of deep firn layering – itself linked to surface snow metamorphism
– could not be tested fully in this study but is believed to play a major role in modulating $\delta\text{O}_2/\text{N}_2$. Determining the relative
575 influence of stratification, firn physical properties, and residence time in the lock-in zone, using a combination of firn models
and observations would be useful for future studies.

Code availability. The Crocus model is open-source, and the code is available at https://opensource.umr-cnrm.fr/projects/snowtools_git/wiki/Procedure_for_new_users. The version used is labeled as Surfex V8_1.

580 *Data availability.* All unpublished $\delta\text{O}_2/\text{N}_2$ data measured at LSCE will be made available online. Published datasets are available online at the references in Table S2 in the supplement.

Author contributions. AL, EC and FP performed measurements/produced the unpublished datasets measured at LSCE - on ice provided by RM and BS - and CB and JS provided unpublished datasets measured at Scripps. Snow temperature data from Dome C was acquired and shared by LA and GP. RHS ran the Crocus simulations, with the support of MD and QL. RHS and AL prepared the manuscript with contributions from all co-authors.

585 *Competing interests.* At least one of the authors is a member of the editorial board of The Cryosphere.

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