

1 Referee #1

2 Overall comments:

3

4 The paper is packed with useful information, and it seems the authors have invested tremendous effort.  
5 While some details are missing, making certain parts challenging to follow, the prior simulation itself  
6 is commendable. I believe this paper is suitable for publication in EGU sphere once the authors address  
7 the comments.

8

9 I would like to suggest that the authors dedicate some time to refining the sentence structures for a  
10 smoother reading experience. Additionally, as mentioned below, I recommend relocating certain  
11 paragraphs from the Results section to the Methodology section or the supplementary materials, as the  
12 two sections appear to be mixed.

13

14 Furthermore, I have a specific request regarding Figure S5: It would be beneficial to include a scatter  
15 plot comparison that depicts “local” enhancements by subtracting the background. I am curious about  
16 how the background estimation was carried out and affects the scatter plot comparison. Additionally,  
17 I am curious to know whether the inversion was performed after the background subtraction.

18

19 I hope that the authors will thoroughly address the detailed comments below.

20 We thank you for your careful reading of our paper and for providing your valuable comments. We  
21 have refined the sentence structures, clarified the treatment of background, and revised our manuscript  
22 according to your comments. Please see our specific responses below.

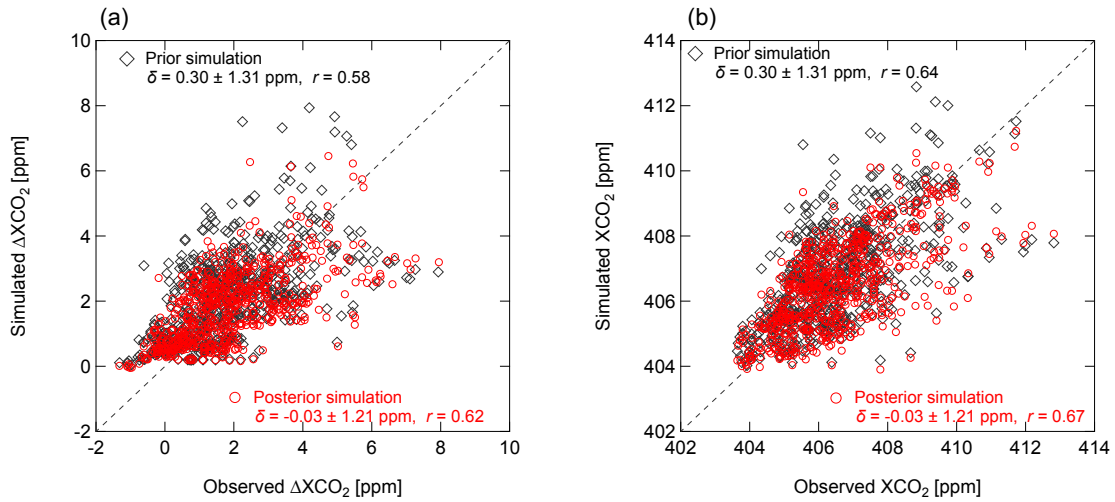
23

24 Regarding Figure S5 (Figure 9 in the revised manuscript), a scatter plot between the simulated XCO<sub>2</sub>  
25 enhancements ( $\Delta$ XCO<sub>2</sub>) and the observed  $\Delta$ XCO<sub>2</sub> after subtracting the background is shown in Figure  
26 R1a, together with a scatter plot for XCO<sub>2</sub> (Figure R1b, same as Figure 9 in the main text). The  
27 background is defined as the Tsukuba TCCON XCO<sub>2</sub> data minus the simulated Tsukuba XCO<sub>2</sub>  
28 enhancements.

29 In the initial manuscript, the differences in XCO<sub>2</sub> measurements between the urban and Tsukuba sites  
30 were considered observational data and the corresponding XCO<sub>2</sub> differences were simulated (as  
31 represented by Equation (7) in the initial manuscript). However, in Figures 8 and 9 (in the initial  
32 manuscript), the observed and simulated “XCO<sub>2</sub>” were shown by transforming the equation. This may  
33 have caused some confusion. In the revised manuscript, the XCO<sub>2</sub> measurements at the urban sites  
34 have been considered observational data (as represented by Equation (2) in the revised manuscript) to  
35 be consistent with what those figures show. We note that this change is mathematically identical in the  
36 inverse analysis (just movement of a few terms in the equation) and does not affect the inversion

37 results at all.

38



39

40 Figure R1. (a) Scatter plot between the  $XCO_2$  enhancements ( $\Delta XCO_2$ ) simulated from the prior (black)  
41 and posterior (red) emission fluxes and the observed  $\Delta XCO_2$ . (b) Scatter plot between the simulated  
42 and observed  $XCO_2$  values. The mean difference between the simulations and observations  
43 (simulation minus observation) with the standard deviation ( $\pm 1\sigma$ ) is denoted as  $\bar{\delta}$ , and  $r$  is the  
44 correlation coefficient.

45

46 Detailed comments:

47

48 L28-29: The following statement is subjective because it depends on the a priori assumption. For  
49 example, if the prior is assigned with large uncertainty, the percentage of uncertainty reduction in the  
50 posterior will be larger, e.g., even larger than a factor of 3. So, the author needs to clarify this sentence:  
51 “In addition, the inverse analysis reduced the uncertainty in total  $CO_2$  emissions in the TMA by a  
52 factor of  $\sim 2$ .”

53

54 We have revised the last two sentences of the abstract as follows: “The prior and posterior total  $CO_2$   
55 emissions in the TMA are  $1.026 \pm 0.116$  and  $1.037 \pm 0.054$   $Mt-CO_2 d^{-1}$  at the 95% confidence level,  
56 respectively. The posterior total  $CO_2$  emissions agreed with emission inventories within the posterior  
57 uncertainty, demonstrating that the EM27/SUN spectrometer data can constrain urban-scale monthly  
58  $CO_2$  emissions.”

58

59 L30 – 31: Instead of the current conclusion, I recommend the authors use a statement, e.g., the posterior  
60 emissions are  $X \pm Y$  times the prior emissions (at the 95% CI). This way, the readers get more  
61 information, e.g., how tightly the measurements constrain the emissions.

62 We have revised the sentence as mentioned above.

63

64 L76 – 78: I strongly recommend that the authors add a couple of sentences describing this work's  
65 unique contribution in addition to the previous work for the TMA.

66 We have added the following sentences: “We constructed CO<sub>2</sub> emission inventories with more accurate  
67 information on both the locations and emissions of large point sources. Anthropogenic CO<sub>2</sub> emissions  
68 from area sources and large point sources were estimated separately using this inventory as the prior.  
69 In addition, the area source emission estimates with higher spatial resolution allow verification of the  
70 emissions reported by each administrative division.”

71

72 L90: I would recommend that the authors add a map of Japan as an inset to show the relative location  
73 of the study area. The elevation map is good, but it is hard for those unfamiliar with the area to make  
74 sense of the study area relative to the entire country.

75 We have added a map of Japan to Figure 1. In addition, we have added the following sentence to the  
76 caption of Figure 1: “The upper right figure shows the location of the study area relative to Japan as a  
77 whole.”

78

79 L142: Was the footprint normalized? The unit for footprint should be “ppm/flux” or, specifically, “ppm  
80 /(umol/m<sup>2</sup>/s)?” It seems that clarification is needed.

81 We have corrected the unit for the footprint to “ppm/(μmol/m<sup>2</sup>/s)”.

82

83 L258: Are the authors referring to the GVF data from VIIRS? It would be useful to add the exact  
84 VIIRS product name.

85 We have revised the sentence as follows: “we spatially downscaled the hourly VISITc NEE data using  
86 GVF data from the Visible Infrared Imaging Radiometer Suite (VIIRS) sensor onboard the Suomi  
87 National Polar-orbiting Partnership satellite (VIIRS Global Green Vegetation Fraction). The GVF data  
88 are produced with an approximately 4-km spatial resolution on a daily basis from the past 7 days of  
89 VIIRS observations (Ding and Zhu, 2018).”

90

91 L263: As written, it is not clear. Was the ratio of the interpolated GVF versus the original GVF applied  
92 to the NEE data at 1 km? Or something else?

93 We have revised the sentence as follows: “The ratio of the original GVF to the interpolated GVF was  
94 multiplied by the interpolated NEE data to produce the downscaled NEE data (Fig. 4c).”

95

96 Section 3.3: Overall, I think the authors did a good job of making the prior fluxes more accurate!

97 Thank you for your positive feedback.

98

99 L264 – 265: Suggestion for rewriting to improve clarity: “The downscaling process was conducted in  
100 a manner that ensured all original sums of the NEE data from the TMA were preserved following the  
101 downscaling.”

102 **We have made this revision.**

103

104 L268: “forward” seems wrong. First, WRF-STILT is not a physical “forward” model in this setting,  
105 although it can be used for forward simulation. Second, this is a linear or nonlinear model, statistically  
106 speaking.

107 **As you pointed out, the WRF-STILT simulations were performed in “backward” mode to trace back  
108 the origin of the observed airmasses. However, in the present study, the terms “forward simulation”  
109 and “forward model” mean the process for calculating XCO<sub>2</sub> values from surface fluxes via  
110 atmospheric transport as opposed to an “inverse analysis” or “inverse model” that infers surface fluxes  
111 from XCO<sub>2</sub> values. In the revised manuscript, we have explicitly written the forward model (Equations  
112 (2) to (4)). In addition, we note that the term “forward simulation” is also used in other similar studies  
113 on top-down emission estimates (e.g., Cusworth et al., 2020; Huang et al., 2019; Maksyutov et al.,  
114 2021; Pisso et al., 2019).**

115

116 **Cusworth, D. H. et al.: Synthesis of methane observations across scales: Strategies for deploying a  
117 multitiered observing network, Geophys. Res. Lett., 47, e2020GL087869,  
118 <https://doi.org/10.1029/2020GL087869>, 2020.**

119 **Maksyutov, S. et al.: Technical note: A high-resolution inverse modelling technique for estimating  
120 surface CO<sub>2</sub> fluxes based on the NIES-TM-FLEXPART coupled transport model and its adjoint,  
121 Atmos. Chem. Phys., 21, 1245–1266, <https://doi.org/10.5194/acp-21-1245-2021>, 2021.**

122 **Huang, Y. et al.: Seasonally resolved excess urban methane emissions from the Baltimore/Washington,  
123 DC Metropolitan region, Environ. Sci. Technol., 53, 11285–11293,  
124 <https://doi.org/10.1021/acs.est.9b02782>, 2019.**

125 **Pisso, I. et al.: Assessing Lagrangian inverse modelling of urban anthropogenic CO<sub>2</sub> fluxes using in  
126 situ aircraft and ground-based measurements in the Tokyo area, Carbon Balance Manage., 14, 6,  
127 <https://doi.org/10.1186/s13021-019-0118-8>, 2019.**

128

129 L269: I suggest that the authors present  $H(x, b)$  more explicitly, e.g., by writing out the Jacobian matrix  
130 and  $x$  together. That way, the reader can understand the nonpoint and point source inversion more  
131 easily. This is related to Eq. (3), where “K” is introduced. Showing how “K” is associated with “b”  
132 should be useful (unless it is presented in the supplemental; I don’t see it).

133 **We have added the following sentences: “The forward model simulates XCO<sub>2</sub> values at the urban sites  
134 (Saitama or Sodegaura) as follows:**

135  $H(\mathbf{x}, \mathbf{b}) = \Delta XCO_2^{\text{urban}}_{\text{STILT}}(\mathbf{x}, \mathbf{b}) + XCO_2^{\text{BG}}(\mathbf{x}, \mathbf{b}),$  (2)

136 where  $\Delta XCO_2^{\text{urban}}_{\text{STILT}}$  is the  $XCO_2$  enhancement at the urban sites simulated by the pressure-weighted  
 137 footprint and the surface fluxes, and  $XCO_2^{\text{BG}}$  is the background value. We calculated the  $\Delta XCO_2$   
 138 values as follows:

139  $\Delta XCO_2^{\text{urban}}_{\text{STILT}}(\mathbf{x}, \mathbf{b}) = F_{\text{aggr}}^{\text{urban}} \mathbf{x}_{\text{area}} + F_{\text{fine}}^{\text{urban}} \mathbf{b}_{\text{point}} x_{\text{point}} + F_{\text{fine}}^{\text{urban}} \mathbf{b}_{\text{bio}},$  (3)

140 where  $F_{\text{fine}}$  and  $F_{\text{aggr}}$  are the original and the spatially aggregated footprints, respectively.  $\mathbf{x}_{\text{area}}$   
 141 and  $x_{\text{point}}$  are the emission flux vector for area sources and the (scalar) scaling factor for large point  
 142 sources, respectively.  $\mathbf{b}_{\text{point}}$  and  $\mathbf{b}_{\text{bio}}$  are the emission flux vectors for large point sources and  
 143 biogenic sources, respectively.”

144 “We therefore obtained the background  $XCO_2$  values by subtracting the simulated  $\Delta XCO_2$  values at  
 145 the Tsukuba site ( $\Delta XCO_2^{\text{Tsukuba}}_{\text{STILT}}$ ) from the Tsukuba TCCON  $XCO_2$  values ( $XCO_2^{\text{Tsukuba}}_{\text{TCCON}}$ ):

146  $XCO_2^{\text{BG}}(\mathbf{x}, \mathbf{b}) = XCO_2^{\text{Tsukuba}}_{\text{TCCON}} - \Delta XCO_2^{\text{Tsukuba}}_{\text{STILT}}(\mathbf{x}, \mathbf{b})$   
 147  $= XCO_2^{\text{Tsukuba}}_{\text{TCCON}} - (F_{\text{aggr}}^{\text{Tsukuba}} \mathbf{x}_{\text{area}} + F_{\text{fine}}^{\text{Tsukuba}} \mathbf{b}_{\text{point}} x_{\text{point}} + F_{\text{fine}}^{\text{Tsukuba}} \mathbf{b}_{\text{bio}}),$  (4)”

148

149 Also, it is not clear at which temporal resolution the authors solve for “x.” Are you solving for sub-  
 150 daily emissions for each pixel? Yes, is it also solved for each pixel as well? If so, how the “b” matrix  
 151 is constructed? I am asking this question because the authors use hourly emissions, at least for NEE  
 152 and anthropogenic. Then the “b” matrix should be extensive. As it is written, many things are not clear.  
 153 The state vector  $\mathbf{x}$  was optimized as a single average during the entire campaign period. The temporal  
 154 variation of anthropogenic emissions (weekly and diurnal correction factors from the TIMES model)  
 155 was taken into account in summing the hourly footprints over the STILT run time. On the other hand,  
 156  $\mathbf{x}$  consists of only “average” area source emission fluxes from ODIAC for each pixel, and such a single  
 157 set of fluxes were optimized. The hourly biogenic fluxes are all included in  $\mathbf{b}$ .

158 We have revised the two descriptions on the application of the TIMES model as follows:

159 (1) “The hourly footprints calculated over the STILT run time (24 h) at a given time were weighted by  
 160 temporal correction factors of  $CO_2$  emissions (described in Sect. 3.3) and aggregated in each grid cell.”  
 161 (Section 3.1)

162 (2) “Because we applied weekly and diurnal correction factors from the TIMES model to the hourly  
 163 footprints in summing them over the STILT run time, we optimized one static emission distribution  
 164 during the campaign period, assuming that the temporal variation of the emissions followed the  
 165 TIMES model.” (Section 3.5)

166 In addition, we have added the following sentence in Section 3.5: “Similarly, a single average scaling  
 167 factor for the large point sources was optimized from the data over the entire campaign period.”

168

169 L270: I would not recommend using “state” in the fixed quantity as in the sentence “b is the fixed state  
 170 vector”; “State” is typically suitable for parameters (please change accordingly if “state” was used for

171 “b.” in other places)

172 We have revised the sentence as follows: “***b*** is the vector consisting of fixed physical quantities.”

173

174 L272-273: Based on “the state vector  $x$  includes spatially resolved nonpoint source emissions and a  
175 scaling factor of the large point source emissions,” the reader may be confused about how the inversion  
176 was done. Are you solving for the “flux” directly for the nonpoint source but the “scaling factor” for  
177 the point source? If it is the case, it is ok. But it needs clarification. Maybe, the authors did this way,  
178 but it is not clear from the writing.

179 We did it the way you suggest. To clarify, we have revised the sentence as follows: “the state vector  $x$   
180 includes spatially resolved fluxes for the area source emissions and a scaling factor for the large point  
181 source emissions.”

182

183 L288: How is “the Levenberg–Marquart parameter” estimated? Or prescribed?

184 We have revised the sentence as follows: “ $\gamma$  is the Levenberg–Marquart parameter fixed at 10 (Chen  
185 et al., 2022).”

186

187 Chen, Z., Jacob, D. J., Nesser, H., Sulprizio, M. P., Lorente, A., Varon, D. J., Lu, X., Shen, L., Qu, Z.,  
188 Penn, E., and Yu, X.: Methane emissions from China: a high-resolution inversion of TROPOMI  
189 satellite observations, *Atmos. Chem. Phys.*, 22, 10809–10826, [https://doi.org/10.5194/acp-22-10809-](https://doi.org/10.5194/acp-22-10809-2022)  
190 [2022](https://doi.org/10.5194/acp-22-10809-2022), 2022.

191

192 L314-315: I am curious how the authors matched the vertical profiles between CarbonTracker (CT)  
193 and EM27 to get the background for EM27. A weighting scheme was used? Ideally, the particle  
194 trajectory for each receptor (at different locations and vertical levels) of EM27 should be computed  
195 and then averaged using a kernel (or a set of weights, likely based on pressure distributions) compatible  
196 with EM27. To sample values from CT (using particle trajectories), the same method should be used  
197 to match the vertical profile between the two. I wonder if the authors did that or something else.

198 We did not use the CO<sub>2</sub> profile product of CarbonTracker, but rather the XCO<sub>2</sub> product  
199 (CT2019B.xCO<sub>2</sub>), so we did not perform any weighing by the column averaging kernel. We have  
200 added the product name (CT2019B.xCO<sub>2</sub>), and these sentences have been moved to Section 3.4.

201

202 L310: By “XCO<sub>2</sub> differences”, do the authors mean “enhancement” above the background? The  
203 phrase “XCO<sub>2</sub> differences (XCO<sub>2</sub>Diff) from daily background values” needs to be revised for  
204 clarification.

205 We have revised the sentence as follows: “To characterize the diurnal variation in XCO<sub>2</sub> at each  
206 observation site, we examined the diurnal variation in XCO<sub>2</sub> enhancements (XCO<sub>2</sub><sup>Enh</sup>) above the daily

207 XCO<sub>2</sub> baseline.” We note that the “5 percentile value of the Tsukuba TCCON measurements” has been  
208 referred to as the “baseline” in the revised manuscript, not to be confused with the “background”  
209 defined and used in the simulations and inverse analyses.

210

211 L313: How did the author account for the background uncertainty based on this “5 percentile”  
212 assumption?

213 We have added the following sentences: “When the 2 (10) percentile values of the Tsukuba TCCON  
214 measurements were used as the daily XCO<sub>2</sub> baseline, the maximum XCO<sub>2</sub><sup>Enh</sup> values were 9.6 (9.4)  
215 ppm at Saitama and 9.5 (8.9) ppm at Sodegaura. These changes had little effect on the standard  
216 deviations of the mean XCO<sub>2</sub><sup>Enh</sup> values and the pattern of the diurnal variation.”

217

218 L318: Please add “diurnal” so that it reads “The average diurnal XCO<sub>2</sub>Diff.” By the way, I think  
219 “ΔXCO<sub>2</sub>” is more informative to represent the local signal (I find both are used). Some people use  
220 “XCO<sub>2</sub>” to describe the local mixing ratio (after subtracting background). I suggest the authors review  
221 the notation a bit more to avoid confusion. In fact, what is the difference between “XCO<sub>2</sub>Diff” and  
222 “ΔXCO<sub>2</sub>” in Line 277? I may have misunderstood, but further clarification would help. Thank you.

223 We have revised the sentence as follows: “The average diurnal XCO<sub>2</sub><sup>Enh</sup> value per 15-min bin was  
224 calculated for each site using the entire field campaign dataset (Fig. 6).”

225 “ΔXCO<sub>2</sub>” is used only to represent the simulated local enhancements. “XCO<sub>2</sub><sup>Enh</sup> (XCO<sub>2</sub><sup>diff</sup> in the initial  
226 manuscript)” represents the observed XCO<sub>2</sub> enhancements above the daily 5-percentile value of the  
227 Tsukuba TCCON measurement. We have added the following sentence: “We note that the XCO<sub>2</sub><sup>Enh</sup>  
228 values were calculated using only the observed XCO<sub>2</sub> values, whereas the ΔXCO<sub>2</sub> values represent  
229 the simulations of local XCO<sub>2</sub> enhancement.”

230

231 L321: I am a bit confused to see that there is a moderate-level effect of biogenic fluxes while the  
232 authors said, “the biogenic flux was allocated to the state vector *b*” in Line 276; it was assumed  
233 negligible there. Any clarification?

234 The biogenic effect due to photosynthesis is not so large and the value is expected to be (relatively)  
235 similar at the different sites. This is seen both for the observations (Figure 6) and simulations (Figure  
236 S5). However, the biogenic fluxes are not small enough to be negligible, so they are included in the  
237 forward calculation of ΔXCO<sub>2</sub> (as the vector *b*). We have revised the sentences in Line 276 as follows:  
238 “the biogenic flux was allocated to the fixed vector *b*. Note that the contribution of biogenic flux to  
239 the simulated ΔXCO<sub>2</sub> was small compared to that of anthropogenic flux and the differences among  
240 ΔXCO<sub>2</sub> calculated from four different biogenic flux products are also small (Sect. 4.2).”

241

242 L323: It is unclear what the authors mean by “the high early morning values at Saitama may reflect

243 an airmass-dependent bias.”

244 We have added the following sentences: “The airmass-dependent variation in XCO<sub>2</sub> is caused by the  
245 effects of inaccurate spectroscopic parameters on the retrievals, which vary with the depth of the  
246 absorption lines (i.e., airmass) (Wunch et al., 2015). Although this effect is corrected in the GGG2014  
247 software, the error may remain for a large airmass.”

248

249 L330-334: The sentence sound awkward. Please revise.

250 We have revised the sentences as follows: “the XCO<sub>2</sub> enhancement ( $\Delta$ XCO<sub>2</sub>) was calculated from the  
251 column-averaged footprint and the surface fluxes from area sources, large point sources, and biological  
252 activity. The  $\Delta$ XCO<sub>2</sub> values resulting from the large point source emissions and biogenic fluxes were  
253 calculated from the original footprints with a spatial resolution of approximately 1 km × 1 km (0.0083°  
254 × 0.0083°). For area source emissions, however, we re-gridded the original footprints to a spatial  
255 resolution of 0.025° × 0.025° to degrade the spatial resolution for the inverse analysis. First, the area  
256 source emissions were summed for each 0.025° × 0.025° grid cell. Then, individual footprints for the  
257 0.025° × 0.025° grid were derived by dividing the sum of the nine XCO<sub>2</sub> contributions for the 0.0083°  
258 × 0.0083° grid by the emissions for the 0.025° × 0.025° grid.”

259

260 L330-345: I would recommend that the authors move this particular paragraph to the Methodology  
261 section or possibly to the supplementary materials. As it stands, the Results section seems a bit  
262 extensive, and this adjustment could help with maintaining focus and flow.

263 We have moved L331-342 to the Methodology section.

264

265 L350-355: Here, the authors describe the background again, which I thought was done in Section 4.1.  
266 Given that both mention “Tsukuba,” I understood that site measurements were used as the background  
267 common to the other sites. What’s surprising to me is that the authors subtract the simulations at  
268 “Tsukuba” from the “Tsukuba” measurements to remove the local enhancements for the background  
269 site. It is possible, but it adds more uncertainty to the background because the simulated quantity itself  
270 is uncertain. Typically, using the particle trajectories from the STILT model, we would sample 4-D  
271 background data (over the ocean) simulated from a global model. The method used here is somewhat  
272 convenient but adds uncertainty.

273 We believe that a method that takes the background from measurements away from the emissions is  
274 as typical as the method that combines the trajectory with the global model. In the present study, the  
275 Tsukuba measurements were considered background due to their distance from the main emission  
276 sources. However, as demonstrated by Babenhauserheide et al. (2020), the Tsukuba measurements can  
277 sometimes be impacted by emissions in the central area of the TMA. Therefore, the simulated  
278 enhancements (from anthropogenic and biogenic emissions) at Tsukuba were subtracted from the



279 Tsukuba measurements. As you pointed out, the simulated enhancements at Tsukuba added uncertainty  
280 to the background. However, optimizing the anthropogenic emission fluxes in the inversion analyses  
281 would reduce the uncertainties.

282

283 Also, I suggest this paragraph be merged with the relevant paragraph in Section 4.1. Otherwise, the  
284 manuscript gets longer, and the reader is distracted/confused.

285 We have refined the structure; this paragraph and the first paragraph of Section 4.3 have been  
286 combined and moved to Section 3.4.

287

288 L358-359: I suggest the authors add a scatter plot for predicted versus measured, corresponding to  
289 Figure 8, only for the 15-min average. I think the figures are already many, but Figure 2 and Figure 4  
290 (maybe more) can be moved to the supplemental.

291 Such a scatter plot was shown as Figure S5 in the supplemental material. In the revised manuscript,  
292 we have moved Figure S5 to the main text (Figure 8). In addition, Figures 2 and 4 in the initial  
293 manuscript have been moved to the supplemental section.

294

295 L360: By “the sum of the WRF–STILT  $\Delta XCO_2$  value every 15 min at each site and the background  
296  $XCO_2$  value”, I assume “ $\Delta XCO_2$ ” is the local enhancement. It needs to clarify between “ $\Delta XCO_2$ ”  
297 and “ $XCO_2^{diff}$ .”

298 “ $\Delta XCO_2$ ” is used only to represent the simulated local enhancements. “ $XCO_2^{Enh}$  ( $XCO_2^{diff}$  in the initial  
299 manuscript)” represents the observed  $XCO_2$  enhancements above the daily 5-percentile value of the  
300 Tsukuba TCCON site. In the revised manuscript, these have been clarified. We note, however, that this  
301 sentence itself has been removed in the refinement of the sentence structure.

302

303 L361: “forward”? STILT back trajectories were used.

304 Although the STILT model was used in “backward” mode to calculate footprints, “forward” simulation  
305 means the process to calculate  $XCO_2$  values from the footprints and the surface  $CO_2$  fluxes.

306 We have added a description of forward simulation in Section 4.2: “We compared the  $XCO_2$  data for  
307 the forward simulations, which correspond to the  $XCO_2$  simulations from the footprints and the surface  
308  $CO_2$  fluxes based on Eqs. (2) to (4), with the EM27/SUN observations at Saitama and Sodegaura (Figs.  
309 7 and 8).”

310

311 L363: What kind of point source? Is it identifiable, e.g., a power plant?

312 As shown in Figure 3 in the revised manuscript, there are several point sources near the Sodegaura  
313 site, including steel plants as well as power plants, so it would not be possible to identify the source.

314 We have revised the sentence as follows: “which were likely caused by the plume from large point

315 sources such as the power plants and steel plants located near the Sodegaura site.”

316

317 L369: I don't necessarily agree with the statement: “Therefore, we attribute this large model–  
318 observation discrepancy to errors in the WRF-STILT model rather than to the emission data.” First, I  
319 don't expect ERA5 to perform better than WRF because it is a much coarse resolution model product  
320 (I also see that in this work's Figure S3). From my experience, it can be much worse than WRF,  
321 depending on the region. I would say that the authors only considered a limited set of meteorology,  
322 not exploring a broader set of meteorological data. So, it is possible that the limited meteorology didn't  
323 capture the temporal variation. However, as the author said, it is still possible that the short-term local  
324 source not included in the prior fluxes is associated with this discrepancy between measurements and  
325 predictions. To summarize, although it is likely that the transport source is the primary source of the  
326 discrepancy, I don't see evidence for the strong statement above.

327 Since the simulations using the prior emission fluxes were able to reproduce the diurnal variation well,  
328 except for 3 March 2016, we thought that the modeling error on specific meteorological conditions  
329 might be the dominant cause of the discrepancy on that day. However, as you pointed out, a short-term  
330 local source not included in the prior fluxes could be the cause of the mismatch between the prior  
331 simulations and the observations on 3 March 2016.

332 We have revised the sentences as follows: “However, we cannot rule out the possibility that short-term  
333 local sources not included in the prior fluxes may cause the discrepancy between the prior simulations  
334 and the observations. Therefore, we attribute this large model–observation discrepancy to errors in the  
335 WRF-STILT model, or to the short-term local sources not included in the prior fluxes, or both.”

336

337 L380: Equation 7 is confusing. What is the purpose of this equation? If this should be included, it  
338 should be presented in the section (e.g., 4.1) where the background is described. Based on the earlier  
339 description, wasn't “*XCOBG* “ derived from *XCOTsukuba\_TCCON*? As pointed out, this whole  
340 paragraph should be in the Method section, not the Result section.

341 In the revised manuscript, Equation (7) has been removed, and new equations that provide a detailed  
342 description of the forward model (Equations (2) to (4)) have been added. These equations make it clear  
343 that background is defined as the difference between the Tsukuba TCCON measurements and the  
344 Tsukuba STILT simulations (i.e., Tsukuba TCCON minus Tsukuba STILT). In addition, this paragraph  
345 has been moved to Section 3.4.

346

347 L387-445: This should be included in the Method section for the abovementioned reason. There is no  
348 meaningful result described or discussed. They would agree with me if the authors read similar inverse  
349 modeling papers.

350 We have moved the description on the construction of the prior error covariance matrix and

351 measurement error covariance matrix to the Methodology section (i.e., L387-412 in the initial  
352 manuscript). Because the remaining part (L413-446 in the initial manuscript) discusses the  
353 uncertainties in our model–observation system based on the simulation results, it has been moved to  
354 Section 4.2.

355

356 L417-418: This work differs from the system in Turner et al., where they have a dense measurement  
357 network. I cannot offer any temporal correlation length scale for this work, but I am not quite sure  
358 about adopting the 1-hr length scale.

359 Since Turner et al. (2020) have dense measurement data, a spatial correlation length scale and a  
360 temporal correlation length scale are imposed on the off-diagonal components of the measurement  
361 error covariance matrix. The effect of the dense measurement data is taken into account by including  
362 the spatial correlation length.

363 Meanwhile, as you note, the temporal correlation length is uncertain. We have added inversion  
364 analyses using different temporal correlation lengths to the sensitivity analysis (in Section 4.3).

365

366 L448: Which period does Figure 12a represent? Is it the average of the hourly posterior fluxes during  
367 the study period?

368 Figure 12a (Figure 11a in the revised manuscript) represents the single average emission fluxes  
369 optimized using all data during the campaign period. As described above, this has been clarified in  
370 Section 3.5 in the revised manuscript.

371

372 L470-471: Related to Equation 1, how many scaling factors were used/solved? Is this value of “0.856”  
373 just the average of many scaling factors? A simple average of many scaling factors would not work,  
374 though.

375 The scaling factor and the spatially resolved anthropogenic emission fluxes were each solved as single  
376 averages during the campaign period. We have added the following sentence to Section 3.5: “Similarly,  
377 a single average scaling factor for the large point sources was optimized from the data over the entire  
378 campaign period.”

379

380 L512-513: Can the author offer further discussion on the difference between this study and Pisso et  
381 al.?

382 We have added the following sentences: “Pisso et al. (2019) and this study use comparable Lagrangian  
383 transport models to calculate atmospheric transport; however, there are several differences, including  
384 the type of observational data (in-situ vs. column), the prior emission fluxes (EDGAR vs. ODIAC),  
385 the meteorological fields for driving the transport model (ERA-Interim vs. WRF based on GPV-MSM),  
386 and the spatial resolution of emission estimates (20 km × 20 km vs. 3 km × 3 km). Our sensitivity

387 analysis shows that changing the prior fluxes, meteorological field, and emission estimation resolution  
388 to roughly match Pissot et al. (2019) did not produce a result substantially different from the emission  
389 estimation result of the reference inversion. We thus concluded that the improved accuracy of emission  
390 estimates in our study may be due to the use of columns as observational data. Column data are less  
391 susceptible to the effect of PBL height changes that are difficult to simulate in transport models and  
392 have information on a larger area of emissions due to the difference in wind direction at each altitude.”  
393

394 L535: With “forward simulation,” as pointed out above, how is footprint-based (backward is assumed  
395 unless explicitly stated) inversion possible?

396 In the revised manuscript (Section 4.2), we have added an explanation that the forward simulations  
397 correspond to calculating the  $XCO_2$  values from the footprints and the surface  $CO_2$  fluxes using  
398 Equations (2) to (4).  
399

400 L540: The mismatch between predictions and observations could be due to local sources not included  
401 in the prior, not necessarily due to transport error. Do you have evidence that there was a clear transport  
402 error? For  $CH_4$ , EDGAR is generally not as good as regional inventories. I see both  $CO_2$  and  $CH_4$   
403 measurements are significantly higher later in the afternoon (from Figure S3). It seems that the  $CO_2$   
404 and  $CH_4$  sources are correlated. It may be the transport model didn’t capture the afternoon winds. Any  
405 evidence for that?

406 We have no clear evidence to suggest that there was an error in the transport (e.g., wind speed and  
407 direction do not substantially differ from the measurements; simulated PBL heights do not take  
408 extreme values). On the other hand, as you pointed out, the mismatch between the prior simulations  
409 and the observation on 3 March 2016 may be attributable to a short-term local source not included in  
410 the prior fluxes.

411 We have revised the sentence as follows: “As described in Sect. 4.2, in some cases, the simulations  
412 failed to reproduce the diurnal variation and to capture the plume from nearby large point sources,  
413 possibly because of the transport modeling error or the short-term local sources not included in the  
414 prior fluxes (Figs. 8d and S6).”  
415

416 Referee #2

417 The authors developed an inversion scheme to infer the anthropogenic carbon dioxide emissions in  
418 the Tokyo Metropolitan Area from observations of three ground based remote sensing sites. One of  
419 which is a TCCON site.

420

421 The authors obtained the background by subtracting the simulated CO<sub>2</sub> enhancement (from the  
422 footprint and surface flux) from the observed XCO<sub>2</sub> values at the Tsukuba COCCON site for the  
423 forward modeling. To assess the biosphere, they spatially downscaled the terrestrial biospheric model  
424 VISITc to simulate the biogenic influence and found the influence to the enhancements to be small.  
425 The authors infer the meteorological surface interaction using WRF-STILT with a spatial resolution  
426 of 1km. The Bayesian inversion scheme inverts for spatially resolved emissions, separated into point  
427 and area-sources for the more than two months period with a total of approximately 6.5 degrees of  
428 freedom. The authors also compared 12 different model configurations.

429

430 The authors report total carbon dioxide emissions for the study area and compare it to several literature  
431 reports and find good agreements within the reported uncertainties. The scientific value is to be rated  
432 as high, since emission estimates from observations still remain a tough challenge and needed to  
433 confirm or refine reported emission inventories. The paper is written in a clear, structured style.  
434 However, some details need improvements.

435

436 We thank you for your careful reading of our paper and for providing many valuable comments. We  
437 have added descriptions related to the potential weaknesses that you raise and revised our manuscript  
438 according to your comments. Please see our specific responses below.

439

440 Potential weaknesses are:

441 1. The authors conduct inversion in log-space, and therefore negative emissions are suppressed, which  
442 is not very realistic. The biogenic model needs to be perfect, so that we can be sure that there are no  
443 “negative emissions”.

444 This study does not optimize total (anthropogenic + biogenic) fluxes, but only anthropogenic fluxes.  
445 Because the magnitude of the biogenic fluxes (negative fluxes during the daytime) in the Tokyo  
446 Metropolitan Area (TMA) in February and March is more than an order of magnitude smaller than the  
447 anthropogenic fluxes and their differences among four models are small (with a standard deviation of  
448 0.09 ppm), the biogenic fluxes were fixed at the prior values. Therefore, it is reasonable to constrain  
449 the anthropogenic fluxes (nonpoint or area sources) to positive values by the inversions in log-space.  
450 In the revised manuscript, we have made it clear that only “anthropogenic” emissions are optimized.

451

452 2. DOFS of 6.49 implicates that solution tend to stick to the a-priori, given that the dimension of the  
453 state vector is rather large ( $m = 1921$  or  $481$  or  $121$ ).

454 As you suggested below, we have investigated how the degrees of freedom for signal (DOFS) change  
455 when the prior uncertainties are increased by a factor  $\sim 1.5$  and  $2$ . Although the DOFS increase with  
456 the prior uncertainty, we found that their changes are not very large (please see our response below).  
457 However, a DOFS of  $\sim 6.5$  would be useful for evaluating emissions from administrative divisions. In  
458 the present study, the focus was on emissions for each administrative division rather than smaller-scale  
459 individual emissions, and we compared the estimated emissions aggregated with the administrative  
460 boundaries with the reported administrative emissions.

461

462 3. The authors assumed that all the sites have the same background air. It is not always true, when  
463 considering the transport time that the air needed to travel from upwind to downwind especially when  
464 the distance between the sites are big ( $\sim 60$  km).

465 The background values used in the simulation and the inverse analysis are specified as the  $XCO_2$   
466 measurements at Tsukuba minus the STILT-calculated  $XCO_2$  enhancements ( $\Delta XCO_2$ ) at Tsukuba.  
467 These background values correspond to the concentrations at the boundary of the TMA defined in this  
468 study, and we think it is appropriate to consider the background to be common to the observation sites  
469 within the relatively small TMA. The  $XCO_2$  values for urban sites other than Tsukuba are represented  
470 as the sum of the background and the  $\Delta XCO_2$  calculated in consideration of fluxes and atmospheric  
471 transport within the TMA.

472

473 4. The definition of background is confusing. The authors have two definitions of background in the  
474 paper, i.e. 5 percentile value of TCCON station at Tsukuba and observed  $XCO_2$  from Tsukuba  
475 COCCON site subtracted with simulated  $CO_2$  enhancement.

476 In the revised manuscript, the 5-percentile value of the Tsukuba TCCON site has been referred to as  
477 the “baseline”. The “background” is now used only in the simulations. We note that the Tsukuba  
478 COCCON data were not used to estimate emissions but used only to correct  $XCO_2$  values observed  
479 by the other spectrometers.

480

481 I would appreciate if the authors could comment on their thoughts on the potential weaknesses and/or  
482 discuss it in the paper, before the acceptance.

483 We have added the discussion regarding the limitations and possible improvements from both the  
484 measurement and simulation sides in Section 5 (L601-605 and L579-583, respectively).

485 Briefly stated, from the measurement side, one limitation is the number of measurements. More  
486 instruments and longer time series would probably increase our sensitivity and thus the DOFS. More  
487 instrument locations would also help to constrain the background. Another limitation from the

488 simulation side is the difficulty of accurately modeling the wind fields. As we saw for 3 March 2016,  
489 we had mismatches possibly due to imperfect wind fields. To better constrain wind fields and PBL,  
490 additional wind lidar observations would be useful.

491

492 Detailed comments:

493 L 15: Suggestion: "We conducted ..." --> "In order to infer a top down emission estimate, we  
494 conducted..."

495 We have made this revision.

496

497 L17: I thought that you deployed 3 EM27SUN spectrometers, please clarify.

498 As described in Section 2, the SN63 EM27/SUN arrived in Tsukuba in the middle of the campaign,  
499 and sunlight measurements were not performed during the entire campaign period (i.e., only from  
500 March to April 2016). To avoid any misunderstanding that the three EM27/SUNs were used for  
501 emission estimates, we would like to keep this description here. For clarification, we have added the  
502 following sentence in Section 3.4: "In the following simulations and inverse analyses, only the  
503 TCCON data were used as the measurement data at Tsukuba, since the SN63 EM27/SUN  
504 measurements started in the middle of the campaign (as described in Sect. 2)."

505

506 L 22: "nonpoint source" --> I would suggest the term "area source" (29 occurrences)

507 We have made these revisions.

508

509 L 26: "emission fluxes at > 3km" To my understanding, the WRF-STILT resolution is 1km, please  
510 clarify.

511 We have added the following description in Section 3.4: "For area source emissions, however, we re-  
512 gridded the original footprints to a spatial resolution of  $0.025^\circ \times 0.025^\circ$  to degrade the spatial  
513 resolution for the inverse analysis. First, the area source emissions were summed for each  $0.025^\circ \times$   
514  $0.025^\circ$  grid cell. Then, individual footprints for the  $0.025^\circ \times 0.025^\circ$  grid were derived by dividing the  
515 sum of the nine XCO<sub>2</sub> contributions for the  $0.0083^\circ \times 0.0083^\circ$  grid by the emissions for the  $0.025^\circ \times$   
516  $0.025^\circ$  grid."

517

518 L 31: Please add your final emission number for the study area, or at least the scaling factor with the  
519 according uncertainty to the abstract and if feasible, compare it to the literature references.

520 We have revised the last two sentences of the abstract as follows: "The prior and posterior total CO<sub>2</sub>  
521 emissions in the TMA are  $1.026 \pm 0.116$  and  $1.037 \pm 0.054$  Mt-CO<sub>2</sub> d<sup>-1</sup> at the 95% confidence level,  
522 respectively. The posterior total CO<sub>2</sub> emissions agreed with emission inventories within the posterior  
523 uncertainty, demonstrating that the EM27/SUN spectrometer data can constrain urban-scale monthly

524 CO<sub>2</sub> emissions.”  
525  
526 L 87: Suggestion: "when the daily sunshine duration in this region is high" --> "during the high-  
527 insolation period" for clarity and specificity.  
528 We have revised the sentence as follows: “when the proportion of clear days is high”  
529  
530 L 93: "city center" --> "city-center"  
531 We have made this revision.  
532  
533 L101: "ASL" --> "a.s.l." (standard abbreviation, multiple occurrences)  
534 We have made this revision.  
535  
536 L107: " and is now continuously operated " --> " and has since been continuously operated "  
537 We have made this revision.  
538  
539 L116: "interval of approximately 1 min" --> "interval of about 1 minute"  
540 We have made this revision.  
541  
542 L130: What is the integration time for determining sigma? If it is 1 min, it might be useful to also  
543 report the 15 min values as you did for comparing the observations with the forward simulations.  
544 An integration time of 15 min was used. We have added the following sentence: “Each of the  
545 EM27/SUN data points was averaged per 15-min bin.”  
546  
547 L132: you scale the TCCON to EM27, would it not make more sense to scale EM27 to TCCON, since  
548 TCCON is considered as standard.  
549 It is certainly common to scale EM27/SUN data to TCCON data. However, the Tsukuba TCCON  
550 XCO<sub>2</sub> data have a slightly larger scatter than the other EM27/SUN data used in this study, and this  
551 made the variation in the TCCON XCO<sub>2</sub> data at a high solar zenith angle somewhat ambiguous. To  
552 derive an airmass-dependent correction factor (ADCF) for the SN44 EM27/SUN, we used the SN63  
553 EM27/SUN data as the reference, which were validated using co-located aircraft measurements  
554 (Ohyama et al., 2020).  
555 We note that, in analyses where measurements at one site are used as part of the background for  
556 measurements at other sites, the differences between them (enhancements above the background)  
557 rather than the absolute values of the concentration are particularly important. Which instrument is  
558 used as the reference has little effect on the emission estimates. In fact, in the case where the SN44  
559 EM27/SUN XCO<sub>2</sub> data corrected for the airmass dependence and the SN38 EM27/SUN XCO<sub>2</sub> data



560 were scaled to the original TCCON data, the relative change in the total TMA CO<sub>2</sub> emissions is less  
561 than 0.1%.

562

563 Ohyama, H., Morino, I., Velazco, V. A., Klausner, T., Bagtasa, G., Kiel, M., Frey, M., Hori, A., Uchino,  
564 O., Matsunaga, T., Deutscher, N. M., DiGangi, J. P., Choi, Y., Diskin, G. S., Pusede, S. E., Fiehn, A.,  
565 Roiger, A., Lichtenstern, M., Schlager, H., Wang, P. K., Chou, C. C.-K., Andrés-Hernández, M. D.,  
566 and Burrows, J. P.: Validation of XCO<sub>2</sub> and XCH<sub>4</sub> retrieved from a portable Fourier transform  
567 spectrometer with those from in situ profiles from aircraft-borne instruments, *Atmos. Meas. Tech.*, 13,  
568 5149–5163, <https://doi.org/10.5194/amt-13-5149-2020>, 2020.

569

570 L135: Maybe mention the altitudes of the stations somewhere in the text.

571 The altitudes of each station are described in the first paragraph of Section 2.

572

573 L142: unit wrong → ppm/(mol/m<sup>2</sup>/s)

574 We have made this revision.

575

576 L145: Since you use the exact same altitudes as T.S.Jones et al., 2021 uses, you can add a citation here.

577 The paper by Jones et al. (2021) has been cited here.

578

579 L154: "multiplied by anthropogenic and biogenic fluxes" --> "multiplied with spatially resolved  
580 emission inventories for anthropogenic and biogenic fluxes separately"

581 We have made this revision.

582

583 L155ff: "The change ... over all grid cells." --> "The change ... over all grid cells and serves for the  
584 forward modeling."

585 We have made this revision.

586

587 L150ff: "We then aggregated the footprints in each grid over the STILT run time." It is not clear what  
588 you mean by "aggregate". If it is meant as an introduction into the following sentence I would suggest  
589 to move the line break before this sentence.

590 We have moved the position of the line break and revised the sentences as follows: "The hourly  
591 footprints calculated over the STILT run time (24 h) at a given time were weighted by temporal  
592 correction factors of CO<sub>2</sub> emissions (described in Sect. 3.3) and aggregated in each grid cell. From the  
593 summed footprints at each altitude, we then calculated the pressure-weighted column-average  
594 footprint, taking account of the column-averaging kernel of the EM27/SUN spectrometer (Rodgers  
595 and Connor, 2003; Jones et al., 2021)."

596

597 L243: please break down this long sentence into at least two shorter ones

598 We have revised the sentence as follows: “Specifically, hourly net ecosystem exchange (NEE) data  
599 from the Vegetation Integrative Simulator for Trace gases (VISIT) model, referred to as VISITc, were  
600 adopted as the biogenic CO<sub>2</sub> flux data. The NEE data were combined with green vegetation fraction  
601 (GVF) data to downscale them.”

602

603 L248: "the original VISIT" --> "the initial VISIT"

604 We have made this revision.

605

606 L251: Gaussian T382 Grid --> please explain shortly, give reference or just state something like  
607 "operate on exactly the same grid" in order to make your point.

608 We have revised the sentence as follows: “The VISITc model operates on the same grid as the CFSR  
609 data (i.e., approximately 0.31° × 0.31°).”

610

611 Section 3.3 in general: Multiple sentences are very long; consider breaking them into shorter pieces  
612 for a better understanding.

613 We have made this revision.

614

615 L257: How you can downscale VISITc product from 0.31 \* 0.31 deg. to 1 km x 1 km using 4 km  
616 resolution GVF data? I am not sure whether you have the high-resolution information necessary to  
617 achieve this goal.

618 The effective spatial resolution of the downscaled biogenic fluxes is about 4 km, although the biogenic  
619 flux data were generated on a 1 km x 1 km grid to be consistent with the footprints. To avoid  
620 misunderstanding, we have revised the sentence as follows: “to better characterize the spatial  
621 distribution of biogenic CO<sub>2</sub> fluxes, we spatially downscaled the hourly VISITc NEE data using GVF  
622 data from the Visible Infrared Imaging Radiometer Suite (VIIRS) sensor onboard the Suomi National  
623 Polar-orbiting Partnership satellite (VIIRS Global Green Vegetation Fraction). The GVF data are  
624 produced with an approximately 4-km spatial resolution on a daily basis from the past 7 days of VIIRS  
625 observations (Ding and Zhu, 2018).”

626 In addition, we have added the following sentence: “We note that the effective spatial resolution of the  
627 downscaled biogenic fluxes is about 4 km, although they were generated on a 1 km x 1 km grid.”

628

629 L267: "DXCO<sub>2</sub> values measured" This statement is confusing, since DXCO<sub>2</sub> values are derived from  
630 the forward model as described in the referenced section 3.1

631 In the revised manuscript, we have modified the forward model that calculates XCO<sub>2</sub>. We have revised

632 the sentence as follows: “XCO<sub>2</sub> measurements at a given location are quantitatively related to the  
633 presumed surface CO<sub>2</sub> fluxes via the forward model  $H$ ”

634

635 L268: "H, representing atmospheric transport" --> To my understanding it is the forward model.

636 We have removed “representing atmospheric transport”.

637

638 L273: Is it correct, that you have the logarithmic of a scaling factor (unitless) as well as an emission  
639 value (in mole/area/time) in the state vector  $x$ ? Please clarify.

640 The scaling factor is linear, not logarithmic. We have added the following sentence: “On the other  
641 hand, the scaling factor for the large point source emissions was optimized at linear scale.”

642

643 L279: Inverting in the log-space introduces a strong bias to positive emissions. Negative emissions  
644 are not necessarily non-physical, especially in case of CO<sub>2</sub>, because biospheric activity might be  
645 stronger than assumed. Did you try to invert in linear space? Negative emissions could serve as a  
646 sanity check here.

647 The inversion in linear space was only tried at the initial stage. In the present study, we do not estimate  
648 total (anthropogenic + biogenic) fluxes, but only anthropogenic fluxes. The negative emissions for the  
649 anthropogenic sources could cause large uncertainty in their emission estimates. In addition, in  
650 February and March in the TMA, the magnitude of the biogenic fluxes (negative fluxes during the  
651 daytime) is more than an order of magnitude smaller than the anthropogenic fluxes (Table 4 and Figure  
652 S5) and their differences among four models are small (with a standard deviation of 0.09 ppm) (Section  
653 4.2). Therefore, it is reasonable to constrain the anthropogenic fluxes to positive values by the  
654 inversions in log-space.

655 In the revised manuscript, we have revised the sentence to make it clear that “anthropogenic area  
656 source” emissions are optimized as follows: “because the area source emissions from each grid cell  
657 differ by a couple of orders of magnitude, and the optimization of area source emissions at linear scale  
658 might lead to unphysical negative posterior emissions.”

659

660 L331: "sources, large point sources" --> "sources, strong point sources" to separate from the spatial  
661 meaning of "large"

662 In the revised manuscript, we have defined “large point sources” as point sources with large emissions  
663 (the first paragraph of Section 2).

664

665 L311ff: It is not very clear in the text what XCO<sub>2</sub><sup>{Diff}</sup> means and how it separates from (DXCO<sub>2</sub>).

666 We have revised the sentence as follows: “To characterize the diurnal variation in XCO<sub>2</sub> at each  
667 observation site, we examined the diurnal variation in XCO<sub>2</sub> enhancements (XCO<sub>2</sub><sup>Enh</sup>) above the daily

668 XCO<sub>2</sub> baseline.”

669 Additionally, in the revised manuscript, “ΔXCO<sub>2</sub>” is used for only representing XCO<sub>2</sub> enhancements  
670 calculated from the forward model.

671

672 L315: It is a bit confusing here, because you define another background (5 percentile value of the  
673 Tsukuba TCCON site) than the one you use for the forward modeling. What XCO<sub>2</sub><sup>{Diff}</sup> is actually  
674 used for? Just to look into temporal fluctuation?

675 To avoid confusion with another “background” used in the simulations, the 5-percentile value of the  
676 Tsukuba TCCON site has been referred to as the “baseline” in the revised manuscript. XCO<sub>2</sub><sup>Enh</sup>  
677 (XCO<sub>2</sub><sup>Diff</sup> in the initial manuscript) values were calculated using only the observed XCO<sub>2</sub> values to  
678 examine the temporal fluctuation at each site. These XCO<sub>2</sub><sup>Enh</sup> confirmed that using XCO<sub>2</sub>  
679 measurements at Tsukuba as background in the simulations would be valid (please see also the next  
680 response).

681

682 L312: Please explain the reasons to use Tsukuba as a background site.

683 We have added the following sentence in Section 3.4: “We assumed that the XCO<sub>2</sub> values at Tsukuba  
684 approximately represent background air, as there are lower CO<sub>2</sub> emissions around Tsukuba (Fig. 3)  
685 and the XCO<sub>2</sub> values observed at Tsukuba were systematically lower than those at the other urban  
686 sites, which can be seen from the XCO<sub>2</sub> values in Fig. 2a.”

687

688 L314ff and L355: How many days (or observations of the n=654 observations) were replaced by  
689 CarbonTracker?

690 We have added the following description: “For days when measurements at Tsukuba were not  
691 available (16, 17, 27, and 28 February and 23 March)”

692

693 L359: you averaged the data in 15 mins. Why is it optimal or in another word, why no drift of the  
694 sensor is integrated? You could refer to: <https://acp.copernicus.org/articles/16/8479/2016/acp-16-8479-2016.pdf>, section 3.1, where the optimal integration time is determined by using Allan analysis.

695 We have added the following sentences in Section 2: “Chen et al. (2016) derive an optimal integration  
696 time of 10 to 20 min, based on the Allan variance of two sets of EM27/SUN data from side-by-side  
697 measurements. However, they used a shorter integration time of 5 min to derive the EM27/SUN  
698 differences between upwind and downwind of local emission sources. In the present study, we found  
699 that it is difficult for the XCO<sub>2</sub> simulation to accurately reproduce the times at which point source  
700 plumes are observed (Sect. 4.2), and a comparison of the simulations and observations at short time  
701 intervals is not beneficial. Thus, we adopted an integration time of 15 min for the EM27/SUN data.”

702  
703

704 L370: You talked about the model-observation discrepancy, forward modeling vs. observation is  
705 mainly given by the errors in the WRF-STILT, what about the background error?

706 In this case, the background is represented as the Tsukuba TCCON  $XCO_2$  data minus the  $\Delta XCO_2$   
707 simulations at Tsukuba (i.e.,  $XCO_2^{Tsukuba}_{TCCON} - \Delta XCO_2^{Tsukuba}_{STILT}$ ). If this background value in the late  
708 afternoon became larger by  $\sim 4$  ppm, the simulation would agree with the observation. Considering the  
709 uncertainty in the  $XCO_2^{Tsukuba}_{TCCON}$  data and the magnitude of the  $\Delta XCO_2^{Tsukuba}_{STILT}$  data (Figure S5c), we  
710 believe that the effect of the background on the model-observation discrepancy would be small.  
711 Meanwhile, as pointed out by Referee #1, short-term local sources not included in the prior fluxes  
712 could contribute to the discrepancy. Therefore, we have revised the sentence as follows: “However,  
713 we cannot rule out the possibility that short-term local sources not included in the prior fluxes may  
714 cause the discrepancy between the prior simulations and the observations. Therefore, we attribute this  
715 large model–observation discrepancy to errors in the WRF-STILT model, or to the short-term local  
716 sources not included in the prior fluxes, or both.”

717

718 L445: you are looking into the model-observation mismatch for the inverse modeling framework.  
719 However, in your inversion you assume the same background for all sites. The background influence  
720 is canceled out in the forward model. Why you need to take the uncertainty of the background into  
721 account?

722 Indeed, Equation (7) in the initial manuscript seems to indicate that the background is canceled out.  
723 In the revised manuscript, the equation has been modified to represent how the urban  $XCO_2$   
724 measurements are simulated. Equations (2) to (4) in the revised manuscript make it clear that  
725 background (i.e., Tsukuba TCCON minus Tsukuba STILT) is included in the simulation.

726 We note that this change is mathematically identical (with just a movement of the  $XCO_2^{Tsukuba}_{TCCON}$  term),  
727 resulting in the same inversion results.

728

729 L455: It is not exactly clear what the authors mean with “upward” and “downward”

730 We have revised the sentence as follows: “the emissions from the central TMA region became smaller  
731 than the prior values, and the emissions from the other regions became larger than the prior values.”

732

733 L470: With 6.5 degrees of freedom the model has not enough freedom to scale the sources individually.  
734 What happens if you provide an intentionally much uncertain a-priori (e.g. Factor 2 higher).

735 When the prior uncertainties are increased by a factor  $\sim 1.5$  and 2 (i.e., 120% and 170% of the prior  
736 emissions, respectively), the degrees of freedom for signal (DOFS) are 8.35 and 10.18, respectively.

737 Although the DOFS increase with the prior uncertainty, they still seem insufficient to resolve the  
738 sources individually. We note that the case with 120% uncertainty is included in the sensitivity analysis.

739 In addition, the DOFS for all sensitivity analyses have been added to Table 5.

740

741 L475ff: Table 5: Please add the degrees of freedom and the Bayesian Information Criterion (BIC) to  
742 this list. The latter is a helpful number to tell which of the models could be a better choice.

743 The DOFS have been added to Table 5. In addition, we calculated the BIC according to Rayner (2020)  
744 (Table R1). With coarser spatial resolution (cases #7a and #7b), the BIC becomes smaller (i.e., a better  
745 model) due to the substantial decrease in the  $m \log(n)$  term of the BIC. According to this parameter,  
746 the worse the spatial resolution, the better the inverse model. We acknowledge that there are a variety  
747 of ways to optimize the grids for spatially resolved emission flux estimates, and we intend to consider  
748 this in future studies.

749

750 Rayner, P.: Data assimilation using an ensemble of models: a hierarchical approach, Atmos. Chem.  
751 Phys., 20, 3725–3737, <https://doi.org/10.5194/acp-20-3725-2020>, 2020.

752

753 Table R1. Bayesian information criterion (BIC) for the different meteorological data, prior emission  
754 data, prior uncertainty ( $\sigma_a$ ), spatial correlation length of  $S_a$  ( $l_s$ ), temporal correlation length of  $S_s$  ( $l_t$ ),  
755 and spatial resolution of the inversion domain ( $r_s$ ).

Case	Meteorological data + prior emission data	$\sigma_a$ (%)	$l_s$ (km)	$l_t$ (h)	$r_s$ (°)	BIC
#0	WRF/MYJ + ODIAC	85	10	1	0.025	11932
#1	WRF/MYJ + ODIAC (LPS fixed)	85	10	1	0.025	11958
#2a	WRF/MYNN25 + ODIAC	85	10	1	0.025	11912
#2b	WRF/YSU+topo + ODIAC	85	10	1	0.025	11890
#2c	ERA5 + ODIAC*	85	10	1	0.025	11719
#3a	WRF/MYJ + ODIAC	50	10	1	0.025	11937
#3b	WRF/MYJ + ODIAC	120	10	1	0.025	11927
#4a	WRF/MYJ + ODIAC	85	5	1	0.025	11933
#4b	WRF/MYJ + ODIAC	85	20	1	0.025	11932
#5a	WRF/MYJ + ODIAC	85	10	0.5	0.025	11854
#5b	WRF/MYJ + ODIAC	85	10	2	0.025	12161
#6	WRF/MYJ + EDGAR	95	14	1	0.025	12752
#7a	WRF/MYJ + ODIAC	75	16	1	0.05	3324
#7b	WRF/MYJ + ODIAC	65	25	1	0.1	1138

756 \*Data from Sodegaura on 23 March 2016 were excluded.

757

758 L494ff: The statement appears reasonable. However, referenced Fig. S6 does not appear to have a  
759 connection to this statement.

760 The reference to Figure S6 (Figure S7 in the revised manuscript) has been changed to the sentence  
761 describing EDGAR as follows: “case #5, EDGAR version 6 ( $0.1^\circ \times 0.1^\circ$  spatial resolution) without  
762 large point source correction used as the prior estimate (Fig. S7)”

763

764 L497ff: The sentence is very long. Please reformulate.

765 We have revised the sentence as follows: “Although the number of grid cells with a spatial resolution  
766 of  $0.05^\circ$  and  $0.1^\circ$  was equivalent to or lower than the number of measurement data points, respectively,  
767 the total DOFS slightly decreased (to 5.84 for  $0.05^\circ$  and 5.05 for  $0.1^\circ$ ). This was due to the changes in  
768 the prior uncertainty and the spatial correlation length.”

769

770 L526: I thought a third EM27/SUN is also deployed at Tsukuba site.

771 As described in our response above, since the solar measurements with the SN63 EM27/SUN were  
772 not used for emission estimates, we would like to keep this description here. For clarification, we have  
773 added the following sentence in Section 3.4: “Note that in the following simulations and inverse  
774 analyses, only the TCCON data were used as the measurement data at Tsukuba, since the SN63  
775 EM27/SUN measurements started in the middle of the campaign (as described in Sect. 2).”

776

777 L553: Again here is 3km resolution mentioned. To my understanding it is 1km. If not correct please  
778 explain the reasons.

779 We have added the following description in Section 3.4: “For area source emissions, however, we re-  
780 gridded the original footprints to a spatial resolution of  $0.025^\circ \times 0.025^\circ$  to degrade the spatial  
781 resolution for the inverse analysis. First, the area source emissions were summed for each  $0.025^\circ \times$   
782  $0.025^\circ$  grid cell. Then, individual footprints for the  $0.025^\circ \times 0.025^\circ$  grid were derived by dividing the  
783 sum of the nine XCO<sub>2</sub> contributions for the  $0.0083^\circ \times 0.0083^\circ$  grid by the emissions for the  $0.025^\circ \times$   
784  $0.025^\circ$  grid.”

785

786 L915: “sigma\_a” for prior uncertainty instead of “sigma\_e”.

787 We have made this revision.

788

789 General model description:

790 lack of overview and strict separation of description of the inversion methodology, model setup details  
791 and results

792 We have refined the sentence structures in the revised manuscript. Specifically, we have moved the  
793 description of the simulation conditions in Section 4.2 (L331-342 in the initial manuscript) and the  
794 description of the construction of the prior error covariance matrix and measurement error covariance  
795 matrix in Section 4.2 (L387-412) to the Methodology section. Additionally, the descriptions of the

796 background (L349-357 and L375-382) have been combined and moved to the Methodology section.  
797 The remaining part of Section 4.3 (L413-446) has been merged with Section 4.2, and Section 4.3 has  
798 been removed.  
799