An improved and extended parameterization of the CO₂ 15 μ m cooling in the middle/upper atmosphere (CO2_cool_fort-1.0)

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Abstract. The radiative infrared cooling of CO_2 in the middle atmosphere, where it emits under non-Local Thermodynamic Equilibrium (non-LTE) conditions, is a crucial contribution to the energy balance of this region and hence to establishing its thermal structure. The non-LTE computation is too CPU time-consuming to be fully incorporated in climate models and hence

- 5 it is parameterized. The most used parameterization of the CO_2 15 μ m cooling for the Earth's middle and upper atmosphere was developed by Fomichev et al. (1998). The valid range of this parameterization with respect to CO_2 volume mixing ratios (VMR) is, however, exceeded by the CO_2 of several scenarios considered in the Coupled Climate Model Intercomparison Projects; in particular, the abrupt-4×CO₂ experiment. Therefore, an extension, as well as an update, of that parameterization is both needed and timely. In this work, we present an update of the parameterization developed by Fomichev et al. (1998), which
- 10 that parameterization that now covers CO_2 volume mixing ratios in the lower atmosphere from ~0.5 to over 10 times the CO_2 pre-industrial value of 284 ppmv (i.e., 150 ppmv to 3000 ppmv). Furthermore, it is improved by using a more contemporary CO_2 line list and the collisional rates that affect the CO_2 cooling rates. Overall, its accuracy is improved when tested against reference line-by-line calculations and by using measured global temperature profiles when tested for the reference temperature profiles as well as for measured temperature fields covering all expected conditions (latitude and season) of the middle atmo-
- 15 sphere. On average the errors The errors obtained for the reference temperature profiles are below 0.5 K day^{-1} for the presentday and lower CO₂ VMRs. The Those errors increase to $\sim 1-2 \text{ K day}^{-1}$ K day⁻¹ at altitudes between 100-120110-120 km for CO₂ concentrations of two to three times the preindustrial values. For very high CO₂ concentrations (four to ten times the preindustrial abundances) the those errors are below $\sim 1 \text{ K day}^{-1}$ for most regions and conditions, except at 110-120107-135 km where the parameterization overestimates them by $\sim 1.5\%$. 1.2%. These errors are comparable to the deviation of the non-LTE
- 20 cooling rates with respect to LTE at about 70 km and below, but are negligible (several times smaller) above that altitude. When applied to a large dataset of global (pole-to-pole and four seasons) measured temperature profiles temperature profiles measured by MIPAS (middle/upper atmosphere mode), the errors of the parameterization for the mean cooling rate (bias) are generally below 0.5 K day^{-1} , except between $5 \cdot 10^{-3} \text{ hPa}$ and $3 \cdot 10^{-4} \text{ hPa}$ ($\sim 85-9585-98 \text{ km}$), where they can reach biases of $1-2 \text{ K day}^{-1}$. However, for For single-temperature profiles, the cooling rate error (estimated by the root-mean-square
- 25 (RMS) of a statically significant sample) is about 1-2 K day⁻¹ below $5 \cdot 10^{-3}$ hPa (~85 km) and above $2 \cdot 10^{-4}$ hPa (~102 km).

In the intermediate region, however, it is between 2 and 7 K day⁻¹. For elevated stratopause events, it underestimates the the parameterization underestimates the mean cooling rates by 3-7 K day⁻¹ (~10%) at altitudes of $\frac{80-10085-95}{80-10085-95}$ km and the parameterized individual cooling rates show a large spread when compared to reference calculations. significant RMS (5–15 K day⁻¹). Further, we have also tested the parameterization for the temperature obtained by a high-resolution version

- of WACCM-X, which shows a large temperature variability and wave structure in the middle atmosphere. In this case, the mean (bias) error of the parameterization is very small, smaller than 0.5 K day⁻¹ for most atmospheric layers, reaching only maximum values of 2 K day⁻¹ near 5·10⁻⁴ hPa (~96 km). The RMS has values of 1–2 K day⁻¹ (~20%) below ~2·10⁻² hPa (~80 km), and smaller than 4 K day⁻¹ (~2%) above 10⁻⁴ hPa (~105 km). In the intermediate region between ~5·10⁻³ hPa and ~2·10⁻⁴ hPa (85–102 km), the RMS is in the range of 5–12 K day⁻¹. While these values are significant in percentage at ~5·10⁻³-5·10⁻⁴ hPa, they are very small above ~5·10⁻⁴ hPa (96 km). The routine is very fast taking (1.5–7.5)·10⁻⁵ s
 - depending on the extension of the atmospheric profile, the processor and the Fortran compiler.

1 Introduction.

Carbon dioxide is the major infrared cooler of the atmosphere from the lower stratosphere up to the lower thermosphere, at which height where emission by nitric oxide becomes important (López-Puertas and Taylor, 2001). However, the CO_2

- 40 infrared emissions in the ν_2 bands near 15 μ m that are responsible for the cooling, are in non-local thermodynamic equilibrium (non-LTE) above around 70 km (López-Puertas and Taylor, 2001). The computation of the cooling under those non-LTE conditions (see, e.g. López-Puertas and Taylor, 2001). Thus, in addition to the difficulty of computing the cooling rates in LTE, which requires the solution of the radiative transfer equation (RTE)which is , i.e., a non-local problemand requires a large amount of CPU time. Therefore, the solving the RTE , we have to calculate the non-LTE populations of the emitting
- 45 levels. Thus, the calculation of the non-LTE cooling rates requires the solution of the statistical equilibrium equations for all energy levels producing a significant emission and the corresponding RTE equations for all bands originating from them (see, e.g., Chapter 3 in López-Puertas and Taylor, 2001). Therefore, the exact calculation of non-LTE cooling rates in general circulation models (GCMs) or climate models that extend in height above the stratopause is impractical and virtually impractical and hence, efficient parameterizations of the CO₂ infrared cooling have been developed and to be implemented in
- 50 such models.

The most used parameterizations of the CO_2 15 μ m cooling for the Earth's middle/upper atmosphere was developed by Fomichev et al. (1998). That parameterization is applicable for a limited range of CO_2 abundances, up to double the preindustrial CO_2 concentration. Nowadays, however, with the rapid increase of the CO_2 concentration in the atmosphere, and its expected increase in the coming decades, climate model projections are being carried out in much higher CO_2 scenarios

55 (van Vuuren et al., 2011; O'Neill et al., 2016), that is, even quadrupling that even quadruples the pre-industrial CO₂ abundance (van Vuuren et al., 2011; O'Neill et al., 2016). For example, such scenarios are considered in the Coupled Climate Model Intercomparison Projects. Therefore, parameterizations coping with such large CO₂ concentrations are highly demanded. That is the aim of this work.; and that is precisely the purpose of our work. Several In addition to that of Fomichev et al. (1998)

, other parameterizations of the CO_2 15 μm cooling rates have been developed in the past. In the case of the Earth's at-

- 60 mosphere, it worth to mention: the comprehensive review of the early works reported by Fomichev et al. (1998), the summary presented in Sec. 5.8 of López-Puertas and Taylor (2001), and the more recent work of Feofilov and Kutepov (2012). Further, just before this work was submitted, a new parameterization has been developed that uses the Accelerated Lambda Iteration and Opacity Distribution Function techniques (Kutepov and Feofilov, 2023). For Mars and Venus atmospheres, where CO₂ is the most abundant species, the problem has been tackled in several studies, e.g.<u>López-Valverde et al. (1998, 2008)</u>,
- 65 López-Valverde et al. (1998); Hartogh et al. (2005); López-Valverde et al. (2008) and Gilli et al. (2017, 2021). In our case, we have the option of developing a completely new parameterization, to adapt other CO₂ parameterizations (as those cited above), or to extent and improve the parameterization of Fomichev et al. (1998). Attending mainly to practical reasons of promptness, we opted for the later.

The paper is structured as follows. A very basic description of the parameterization is presented in Sec. 2. Sec. 3 describes

- 70 the input atmospheric parameters used in the parameterization and required for calculating the reference cooling rates. In Sec. 4 we describe the calculations of the reference LTE and non-LTE cooling rates. The detailed description of the parameterization is presented in Sec. 5. The testing and accuracy of the parameterization against: (i) the reference cooling rates and for currently ; (ii) the measured temperature fields of the middle atmosphere of MIPAS; and (iii) the temperature profiles obtained by a high-resolution version of WACCM-X, are discussed in Sec. 6 and 7, 7 and 8, respectively. The previous cooling rate parameterization
- reterization was <u>commonly</u> used together with a parameterization of the CO_2 near-IR heating rates (Ogibalov and Fomichev, 2003) in <u>GCMs</u>. As we have extended the former to higher CO_2 volume mixing ratios (vmrs), and we do not plan to extend the latter to higher CO_2 vmrs in the near future, we assess in Sec. 9 that the the validity of the current near-IR heating parameterization <u>ean still be safely used with for high</u> CO_2 vmrsup to at least five times the pre-industrial values. In Sec. 10, we summarize the main conclusions of the study.
- 80 The relationship between pressure and geometrical altitude for the reference temperature profiles.

2 Framework of the parameterization

As discussed above, this parameterization is essentially based on that of Fomichev et al. (1998). For computing the CO_2 cooling rate, the atmosphere is divided into five regions (see Fig. 7): the LTE and four different non-LTE regions. The method and approximations for computing the cooling rates in those regions are described in detail in Sec. 5. The new parameterization

- has a finer grid and, because it has been developed to cover a larger range of CO₂ vmrs, the different boundaries of the non-LTE regions were revised and usually, in general, their upper boundaries were extended to upper altitudes. shifted to higher altitudes. The scheme consists of 83 levels in $x = \log(1000/p(hPa))$, covering from x = 0.125 to x=20.625 spaced by 0.125. The 0.25. The parameterization, however, can also be used for x > 20.625, where it uses the same scheme as for the NLTE4 region (see Sec. 5.4). The relationship between pressure and the geometrical altitude for the reference temperature profiles is shown
- 90 in Fig. S1. To a first approximation, the geometric altitude z below ~ 120 km is related to x by $z(\text{km}) \approx 7x$.

Figure 1. Input data used in the reference calculations. Panel a): The six temperature profiles used in the reference calculations up to the lower thermosphere (Fig. 7 shows them for the full range of pressures). MLE: midlatitude equinox (September, 40° N); TRO: tropics (June, equator); MLS: midlatitude summer (June, 40° N); MLW: midlatitude winter (June, 40° S); SAS: subarctic summer (June, 70° N); and SAW: subarctic winter (June, 70° S). For the entire altitude range see Fig. 7. A profile typical of an elevated stratopause event (ES, mean of MIPAS temperature measured for latitudes of 70° N– 90° N for 15 February 2009) is also shown for comparison and is discussed in Sec. 7.2. Panel b): CO₂ volume mixing ratio profiles used in this work for the entire altitude range. Solid lines: the profiles used in the reference calculations; dashed lines: intermediate profiles used to test the parameterization. Panel c): the $O(^{3}P)$ volume mixing ratio profiles. Here and in the following figures, the geometric altitude is approximate, corresponding to the pressure/altitude relationship of the MLE reference atmosphere.

The parameterization computes cooling rates for given inputs of temperature and concentrations of CO₂, O(^{3}P), O₂ and N₂ as a function of pressure. No specific grid is required and can be irregular. The routine interpoles the given parameters into its internal pressure grid. Possible cooling effects caused by temperature disturbances at vertical scales smaller than the internal grid of the parameterization, ≤ 1.75 km, (see, e.g. Kutepov et al., 2013) are not taken into account. That is, we assume

95 that the cooling induced by non-resolved gravity-waves propagating with a vertical wavelength of the order of/or smaller than ≤ 1.75 km would be taken into account in the GCMs by using an appropriate GW parameterization.

Further, the collisional deactivation (de)-activation of $CO_2(v_2)$ levels by the main atmospheric molecules (N₂ and O₂) and by $O({}^{3}P)$, can also be prescribed. To compute the different coefficients employed by the parameterization (see Sec. 5), reference LTE and non-LTE cooling rates are required (see Secs. 4.1 and 4.2). These are calculated for selected reference atmospheres , which are and described in the next section.

volume mixing ratio profiles used in this work. Solid lines: the profiles used in the reference calculations; dashed lines: those used to test the parameterization.

3 The reference atmospheres

3.1 Temperature

100

- 105 We used the same six pressure-temperature reference atmospheres as in Fomichev et al. (1998) for altitudes below ~120 km. Above this altitude, they were extended up to ~200 km with the empirical US Naval Research Laboratory Mass Spectrometer Incoherent Scatter Radar version 2.0 (MSIS2) model (Emmert et al., 2021) for medium conditions of solar activity, $F_{10.7}$ =103 sfu (June 2011) for all atmospheres except for MLE which was $F_{10.7}$ =142 sfu (September 2011). These six p-Tprofiles cover very well the envelope of the climatological zonal mean temperatures of the current middle atmosphere, e.g.
- 110 as measured by MIPAS from 2007 to 2012 (see Sec. 7). Of courseHowever, they do not cover the short scale temporal and spatial temperature variability (see , Fig. B1). The performance of the parameterization parameterization for such variability is addressed in Sec. 7. Further, the range of the six temperature profiles do not cover well the episodes of stratospheric warming with elevated stratopause. During these events, the altitude region of the typical stratopause, at about 50 km, is much colder,

being even 50 K colder than during normal conditions, and the altitude of the typical mesopause, near 85–90 km, is warmer by

115 a similar amount (see Fig. 1a, profile ES). For these conditions the temperature profile is nearly isothermal from the tropopause up to about 0.1 hPa and exhibits an inversion above, with a peak near the mesopause. We anticipate that for these <u>rare</u> conditions the error incurred by this parameterization can be significant (see Sec. 7.2).

We should also mention that the envelope of these reference atmospheres does not fully cover the predicted temperatures for the end of this century for projections with high CO_2 emissions. In particular, Whole Atmosphere Community Climate Model

- 120 (WACCM) simulations for this century under the RCP6.0 scenario (Marsh, 2011; Marsh et al., 2013; Garcia et al., 2017) yields zonal mean temperatures which are colder in the middle atmosphere. In order to cover such predictions, the envelope of the six *p*-*T* profiles assumed here would have to be widened by about -30 K in the upper stratosphere and by about -20 K in the mesosphere. The parameterization accuracy for such predicted temperatures has not been fully assessed in this work as we have considered only the projection of high CO₂ vmr profiles but not the corresponding predicted temperature fields. This will be the subject of future work.

3.2 CO_2 , $O(^3P)$, O_2 and N_2 abundances

The valid range of the parameterization of Fomichev et al. (1998) with respect to CO₂ volume mixing ratios is exceeded by the CO₂ concentration of several scenarios considered in the 6th Coupled Climate Model Intercomparison Project (CMIP6); in particular for the 4×CO₂ experiment. Several CO₂ scenarios have been proposed for the future. That is Thus, van Vuuren et al. (2011) proposed the scenario RCP2.6, which reaches tropospheric CO₂ values near 1000 ppmv by the end of the century. Likewise, Meinshausen et al. (2011) suggested the high CO₂ scenario of RCP8.5 (CMIP5) which has CO₂ concentrations of 2000 ppmv in the second half of the 23rd century; or even higher than 2000 ppmv (e.g., SSP5-8.5 in CMIP6, see O'Neill et al., 2016). Here we used a wide range of tropospheric CO₂ values ranging from about half of the pre-industrial (1851) value of 285 ppmv, to about ten times this value (see Fig. ?? 1b). The specific profiles were built from a WACCM run under

- the CMIP6 SSP5-8.5 scenario (Marsh, 2011; Marsh et al., 2013; Garcia et al., 2017). Global annual mean profiles of CO₂ were taken from WACCM simulations for years: 1851 (pre-industrial), CO₂ profile #2; 2014, CO₂ profile #3; 2050, CO₂ profile #4 (~2×pre-industrial); and 2099, CO₂ profile #6 (~4×pre-industrial). In addition, we set up , the low CO₂ profile (#1), by halving the pre-industrial profile #2, the intermediate CO₂ profile #5 (~3×pre-industrial profile) from the mean of WACCM outputs for 2050 and 2099, the high CO₂ profile #7 (~5×pre-industrial profile) by multiplying WACCM output for
- 140 2099 by a factor of 1.25, and the highest CO₂ profile #8 (\sim 10×pre-industrial profile) by multiplying WACCM output for 2099 by a factor of 2.7. In addition to those CO₂ vmr profiles, we also composed the intermediate profiles #9, #10 and #11, for testing the parameterization (see Sec. 6.2), which are shown in Fig. ?? 1b with dashed lines. Profiles #9 and #11 were obtained by multiplying WACCM outputs for the years of 2050 and 2099 by factors of 0.979 and 1.8, respectively. Profile #10 was calculated by weighting the WACCM annual mean for years 2050 and 2099 by 0.76875 and 0.256250, respectively. WACCM
- 145 provides the CO₂ vmr profiles up to about 130 km. Above that altitude, they were calculated by using a WACCM-X run for 2008, which provides CO₂ vmr up to near 500 km, and scaling them, in pressure levels, by the CO₂ value of the corresponding CO₂ profile at a pressure of $5 \cdot 10^{-6}$ hPa.

As discussed above, the parameterization requires the N₂, O₂ and O(${}^{3}P$) volume mixing ratio profiles for the six *p*-*T* reference atmospheres. They were taken from the MSIS2 model (Emmert et al., 2021) and are shown in Fig. S2.

150 4 Cooling rates for the reference atmospheres

We describe in this section the non-LTE cooling rates used as a reference. To compute the coefficients of the parameterization and the boundaries of the different layers they also require the calculations of the cooling rates in LTE, which are also described in this section. Further, we have assessed the accuracy of the LTE cooling rates by comparing them with those calculated by an independent code, the Reference Forward Model (RFM, Dudhia, 2017).



Figure 2. LTE cooling rates for the US standard temperature profile and the CO_2 vmr of Fomichev et al. (1998) computed by the GRANADA algorithm and the RFM code.

155 4.1 Reference LTE cooling rates

The LTE cooling rates have been computed using a modified Curtis matrix formulation (Funke et al., 2012). That formulation uses In that computation we used as the basis for the radiative transfer calculations (e.g., the optical depthsand transmittances, the transmittances and their differences) the Karlsruhe Optimised and Precise Radiative Transfer Algorithm (KOPRA, Stiller et al., 2002)code. Kopra. This code is a well-tested general-purpose line-by-line radiative transfer model that includes all the

160 known relevant processes for performing accurate radiative transfer calculations in planetary atmospheres. We used the CO₂ line list of HITRAN 2016 (Gordon et al., 2017) and the line shapes were modelled with a Voigt profile including the pressure and temperature dependencies of the Doppler and Lorentz halfwidths. The line mixing, although of little importance in this

case because the transmittances are integrated over a wide spectral range, was also taken into account (see Stiller et al., 2002)

. The flux transmittances were computed using a 10-point Gaussian quadrature. The wavenumber grid was 0.0005 cm⁻¹. The LTE cooling rates have been computed for the CO₂ bands associated with the vibrational states of the v₁v₂ mode manifold covering the spectral range from 540 cm⁻¹ to 800 cm⁻¹ in intervals of 10 cm⁻¹. All bands listed in HITRAN 2016 for the six most abundant isotopes in those spectral regions were included in the calculation. For reference, the accurate cooling rates computed assuming LTE conditions for the six *p*-*T* profiles and the reference eight CO₂ vmrs are shown in Figs. S3 and S4.

- In order to assure the accuracy of these LTE cooling rates we have compared them with those obtained with another very well tested and widely used radiative transfer code, RFM (Dudhia, 2017). This code has been used in many studies relevant to the MIPAS instrument (Fischer et al., 2008) and for the retrieval of MIPAS level 2 data obtained by the University of Oxford. It worth mentioning that RFM uses a classical Curtis matrix method (double flux transmittance differences) while we use the modified Curtis matrix method. Fig. 2 shows the results of the comparison for the US standard temperature profile and the CO₂ vmr of Fomichev et al. (1998). Here we used a common fine altitude grid of 0.5 km. We see that the agreement between
- 175 both codes is very good, with differences at most of the altitudes smaller than $0.1-0.2 \text{ K day}^{-1}$. Note that some of the major differences appear to be associated with small oscillations in the RFM results.

The same formulation has been used to calculate the Curtis matrices of all the CO₂ ν_2 bands which are required to compute the coefficients of the parameterization in the LTE region (see Sec. 5).

4.2 Reference non-LTE cooling rates

- 180 The reference line-by-line non-LTE cooling rates have been computed by using the GRANADA non-LTE code. The details of the method for solving the system of equations for CO_2 are given in Funke et al. (2012). In addition to the solution of the statistical and radiative transfer equations described in that work for the calculation of the non-LTE populations of the CO_2 levels, here, in order to compute accurate non-LTE cooling rates and to account for the overlapping between the different CO_2 ν_2 bands, we included an additional final iteration computing the radiation fields in all the bands by using the Lambda iteration
- 185 method. This algorithm shares the radiative transfer algorithm with KOPRA (Stiller et al., 2002). Thus, the details about the radiative transfer calculation related to KOPRA, e.g. line shape, spectroscopic data, wavenumber grid, <u>line mixing</u>, etc., given in the LTE Sec. 4.1 above, applies also to the non-LTE calculations described here.

For this case of non-LTE cooling rates, each ro-vibrational band contributes according to the non-LTE populations of their upper and lower levels. The non-LTE cooling rates calculated here comprise 16 ν_2 vibrational bands emitting/absorbing in 190 the 15 μ m region. That is, the fundamental ν_2 band, three first hot ν_2 bands and seven ν_2 second hot bands of the major CO₂ isotopologue, and the ν_2 fundamental bands of isotopologues ¹⁶O¹³C¹⁶O, ¹⁶O¹²C¹⁸O, ¹⁶O¹²C¹⁷O, ¹⁶O¹³C¹⁸O and ¹⁶O¹³C¹⁷O. The contribution of other weaker ν_2 bands arising from higher ν_2 levels, e.g. ν_2 =4, 5 or 6, are included in the calculation but have negligible contributions for the conditions of the Earth's atmosphere.

For the calculations of the non-LTE cooling rates, a collisional scheme and collisional rates are required. Although the 195 collisional rates affecting the $CO_2 v_2$ levels are an input parameter for the parameterization, here we have used, for the calculations of the reference cooling rates and for testing the parameterization, the collisional rates described in Funke et al. (2012).

Table 1. Main collisional proce	esses affecting the CC	0_2 vibrational leve	ls included in the	calculations of the	e non-LTE cooling	rates (extracted
from Table 5 of Funke et al., 20	012).					

No.	Process	Rate coefficient [†]
1a	$\operatorname{CO_2}^i(v_2) + \operatorname{N_2} \rightleftharpoons \operatorname{CO_2}^i(v_2 - 1) + \operatorname{N_2}$	$k \times 7 \times 10^{-17} \sqrt{T}$ +6.7×10 ⁻¹⁰ exp $(-83.8/T^{1/3})^{\ddagger}$
1b	$\operatorname{CO_2}^i(v_2) + \operatorname{O_2} \rightleftharpoons \operatorname{CO_2}^i(v_2 - 1) + \operatorname{O_2}$	$k \times 7 \times 10^{-17} \sqrt{T}$ +1.0×10 ⁻⁹ exp $(-83.8/T^{1/3})^{\ddagger}$
		$(k = 1, 3, 4.5, 6.75, 9, 12 \text{ for } v_2 = 1,, 6)$
1c	$\operatorname{CO}_2{}^i(v_2) + \mathbf{O} \rightleftharpoons \operatorname{CO}_2{}^i(v_2 - 1) + \mathbf{O}$	$3.5 \times 10^{-13} \sqrt{T}$ + $2.32 \times 10^{-9} \exp(-76.75/T^{1/3})$
2a	$\text{CO}_2{}^i(v_2, v_3) + \text{N}_2 \rightleftharpoons \text{CO}_2{}^i(v_2 + 2, 3 \text{ or } 4, v_3 - 1) + \text{N}_2$	$1.1 \times 10^{-15} + 1.14 \times 10^{-10} \exp(-72.3/T^{1/3}) +$
		$2.3 \times 10^{-40} T^9$
2b	$CO_2^{i}(v_2, v_3) + O_2 \rightleftharpoons CO_2^{i}(v_2 + 2, 3 \text{ or } 4, v_3 - 1) + O_2$	1.82×10^{-15} + $3.1 \times 10^{-11} \exp(-63.3/T^{1/3})$ +
		$2.0 \times 10^{-31} T^6$
2c	$CO_2^{i}(v_2, v_3) + O \rightleftharpoons CO_2^{i}(v_2 + 2, 3 \text{ or } 4, v_3 - 1) + O$	$2 \times 10^{-13} \ (T/300)^{1/2}$
3	$\operatorname{CO}_2^i(v_2, v_3) + \operatorname{CO}_2^i \rightleftharpoons \operatorname{CO}_2^i(v_2 + 1, v_3 - 1) + \operatorname{CO}_2^i(v_2 = 1)$	$3.6 \times 10^{-13} \exp(-1660/T + 176948/T^2)$
4	$\operatorname{CO}_2^i(v_2,v_3) + \operatorname{O}_2 \rightleftharpoons \operatorname{CO}_2^i(v_2+1,v_3-1) + \operatorname{O}_2(1)$	3×10^{-15}
5a	$\operatorname{CO_2}^i(v_2)$ + $\operatorname{CO_2}^i \rightleftharpoons \operatorname{CO_2}^i(v_2-1)$ + $\operatorname{CO_2}^i(v_2=1)$	See Table 6 in Funke et al. (2012)
5b	$CO_2^{i}(v_2)+CO_2^{j}(v_2') \rightleftharpoons CO_2^{i}(v_2-1)+CO_2^{j}(v_2'+1)$	$i=1; j=2-4; 2.35 \times 10^{-11}$
6	$CO_2^{i}(v_2, v_3) + N_2 \rightleftharpoons CO_2^{i}(v_2, v_3 - 1) + N_2(1)$	$5.0 \times 10^{-13} (300/T)^{1/2}$ for $v_2=0, 1, 3, 5, 7$
		$7.0 \times 10^{-13} (300/T)^{1/2}$ for $v_2=2, 4, 6$
7	$\operatorname{CO}_2{}^i(v_1v_2lv_3) + \operatorname{N}_2 \rightleftharpoons \operatorname{CO}_2{}^i(v_1'v_2'l',v_3) + \operatorname{N}_2$	5.4×10^{-13} for $v_2 = v'_2 = 0$ or $v_2 \& v'_2 \neq 0$
		8.1×10^{-13} for all other cases

[†] Rate coefficient for the forward sense of the process in cm³s⁻¹. [‡] This rate is taken as 10^{-15} cm³s⁻¹ for temperatures lower than 150 K (see Funke et al., 2012). *T* is temperature in K. *i* and *j* are different CO₂ isotopologues. *i*=1–6 except as noted. v_2 denotes equivalent $2v_1+v_2$ states, e.g., $v_2=2$ is the triad (10002, 02201, 10001).

They have been recently revised and used in the non-LTE retrieval of temperature from SABER and MIPAS measurements (García-Comas et al., 2008; García-Comas et al., 2023). The most relevant collisional processes concerning the populations of the levels emitting in the different ν_2 bands described above, and their rates, are listed in Table 1 for easier reference. We should note that these rates and their temperature dependencies are different from those used in the previous parameterization of Fomichev et al. (1998). The values are in general of very similar magnitude, except the k_0 rate (process 1c in Table 1) that has been considered here with its upper limit. That is, about a factor of two larger than in the parameterization of Fomichev et al. (1998). This rate coefficient is not well known, with uncertainties of the order of a factor of two (see, e.g., García-Comas et al., 2008). While laboratory measurements are in the range of 1.5 to $2 \cdot 10^{-12} \text{ cm}^3 \text{s}^{-1}$ the values derived from atmospheric observations are close to $6 \cdot 10^{-12} \text{ cm}^3 \text{s}^{-1}$. Although this rate can be chosen when using this parametarization parameterization, we have optimised it for the high-its larger value (see Table 1), as this value rate has been used in the most recent non-LTE

retrievals of temperature from SABER and MIPAS measurements. The effects of using half of this value on the cooling rates

are discussed in Sec. 6.2. In the comparisons shown in the next sections , however, we used consistently the collisional rates in Table 1 for the two parameterizations.

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The cooling rates near 15 μ m change very little with the illumination conditions. However, those cooling rates (or more strictly speaking, the flux divergence) of the CO₂ ν_2 bands computed by GRANADA under daytime conditions might be are affected by some emission from the relaxation and/or redistribution of the solar energy absorbed in the near-infrared bands (see, e.g. López-Puertas et al., 1990). As this absorption/heating is already taken into account by the NIR solar heating parameterization (see Sec. 9), all the non-LTE cooling rates computed here have been performed under for nighttime conditions.



Figure 3. The non-LTE cooling rates for the four reference atmospheres shown for altitudes up to the lower thermosphere. The cooling rates extended to the thermosphere are shown in Fig. S5. Note the different x-scales.

215 Contributions of the different bands to the cooling rates for the MLE atmosphere. That is, as the top/left panel of Fig. 4 but for the entire altitude range.

The results for the accurate, line-by-line non-LTE cooling rates computed for the six reference p-T profiles and the eight CO₂ vmrs are shown in Fig. 3 from the stratosphere up to the lower thermosphere, and in Fig. S5 for the upper part of the parameterization, i.e., above from 80 km to 200 km. We observe that the altitude distribution of the cooling rates depends very much on the temperature profile. This is the major difficulty in building the parameterization. A general common feature is the maximum near the stratopause because at these altitudes the non-LTE cooling rates do not differ significantly from those

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Figure 4. Contributions of the different CO₂ bands to the cooling rates for the six-four p-T references atmospheres and the contemporary CO₂ vmr #3 profile. Note the different x-scales.

in LTE and these are mainly driven by the high temperature of this region. Above the stratopause, the total non-LTE cooling rates depend very much on the contributions of the different bands, e.g., the v₂ fundamental band of the major isotopologue (FB), the contributions of the first and hot bands (Hots), and those of the v₂ fundamental bands of the five minor isotopologues.
225 These contributions are shown in Fig. 4 for the contemporary CO₂ vmr profile (#3) and the six four *p*-*T* profiles. The non-LTE cooling rates generally decrease with altitude above the stratopause, reaching a minimum near the mesopause for several *p*-*T* profiles, see, e.g., the TRO and MLS atmospheres in FigSAS and MLE atmospheres in Figs. 3 and 4. The cooling can be even negative, e.g. heating, for the very cold sub-arctic summer (SAS) mesopause, where heating can be of several K day⁻¹ (see bottom/left panel of Fig.43). Exceptional cases are the winter atmospheres (mid-latitude winter, MLW (not shown), and sub-arctic winter, SAW) where the mesopause is warmer and the cooling rates are large in this region. Above the mesopause, the cooling rate action because of the depletion of the vmr (see Fig. B1). At these altitudes, the cool-to-space is a very good approximation to the non-LTE cooling rate which, when expressed in K day⁻¹, is proportional to the CO₂ vmr, to the atomic oxygen density, [O], and to the temperature through exp(-*E*/*kT*) (see, e.g., See, 9.2 in López-Puertas and Taylor, 2001). As

altitude increases, the CO₂ vmr decreases and so does [O]. These two effects overcome the temperature increase leading to

a net cooling rate decrease. Note the significant contribution of the hot bands in the lower thermosphere (120–150 km, see Fig. B1), essentially due to the first hot band of the major isotopologue at these altitudes, which is about 10% of the total cooling(see Fig. B1).

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The dependence of the non-LTE cooling rates on the CO_2 abundances is illustrated in Fig. 3. We observe that in general, the cooling rate correlates very well with the CO_2 abundance, although that correlation is not always linearly and generally depends on altitude. This is true also for the cases where we have net heating for low CO₂ vmr, e.g. the subarctic summer (SAS) atmosphere between about 75 km and 95 km. For the MLE and MLS atmospheres, the cooling rate near \sim 90 km changes from net cooling to net heating for the largest CO₂ vmrs. Further, the very small cooling for the TRO p-T profile near 70 km remains very small even when the CO₂ vmr varies in a factor of 20. In the lower thermosphere, e.g. above around ~ 110 km, however, the dependency of the cooling rate on the CO_2 is very close to being linear (see Fig. S5).

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Figure 5. Non-LTE minus LTE cooling rates differences for the six-four p-T references atmospheres and the contemporary CO₂ vmr #3 profile. Differences for the higher CO₂ vmr #6 profile (\sim 4×pre-industrial) are shown in Fig. S6. The '*' symbol indicates the pressure level (in hPa) where the non-LTE–LTE difference reaches 5%. Note the different x-scales.

Altitude (left panel) and pressure level (right panel) of the deviation (>5%) of the non-LTE cooling rates from LTE values for the six p-T references atmospheres and the eight vmr profiles.



Figure 6. Effect of the k_0 collisional rate (or, equivalently, the O(${}^{3}P$) concentration) on the non-LTE cooling rates for the six four p-T references atmospheres and the contemporary CO₂ vmr #3 profile. Note the different x-scales.

A comparison of the non-LTE and LTE cooling rates for the six p-T reference atmospheres for CO₂ vmrs #3 (current vmr) and #6 (four times the preindustrial value) are shown in Figs. 5 and S6. This comparison is useful from a physical point of view 250 and it is required necessary in order to establish the boundaries of the different atmospheric regions of the parameterization (see Sec. 5). We first observe (Fig. 5) that the altitude of the departure of the cooling rate from LTE to non-LTE (considered as the altitude where the non-LTE–LTE difference is larger than 5%) depends on the temperature profiles profile, and ranges from pressures of $5.2 \cdot 10^{-2}$ hPa (~72.5 km) for the sub-arctic summer (SAS) atmosphere to $1.2 \cdot 10^{-2}$ hPa (~78.7 km) for the tropical (TRO) atmosphere. A similar figure plot but for the higher CO₂ profile #6 ($\sim 4 \times \text{pre-industrial}$) is shown in Fig. S6. 255 An overview of the altitude/pressure level of the deviation from LTE of the cooling rate from LTE is shown in Fig. B2 for the six p - T profiles and the eight CO₂ vmr profiles. We see that the lower altitude (higher pressures) occur for the sub-arctic summer (SAS) and sub-arctic winter (SAW) reference atmospheres. It is also evident that this altitude increases with the CO_2 vmr, except for the SAS and SAW cases for which it is nearly independent of the CO_2 vmr. That is expected as, for a more abundant CO_2 atmosphere, the 15 μ m bands become optically thicker and fewer collisions are sufficient for keeping the emitting levels in LTE. Fig. B2 suggests that for higher CO_2 vmrs, the LTE to non-LTE transition region (see Fig. 7) could be 260



be conservative as and placed it at the lowest altitude for any p - T or CO₂ vmr profile. This Thus, it has been taken at x = 9.875($p = 5.14 \times 10^{-2}$ hPa, $z \approx 70$ km) which, except for the SAW atmosphere and with the lowest CO₂ profile, is fulfilled fulfils the LTE to non-LTE transition region for all p - T and CO₂ vmr profiles.

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For completeness, Fig. B3 shows an example of the comparison of non-LTE and LTE cooling rates including the thermosphere for the six p-T profiles and the current CO₂ values. This shows the enormous difference between LTE and non-LTE cooling rates (being non-LTE values much smaller) in the thermosphere.

The atomic oxygen concentration is an input to the parameterization and plays a crucial pointing role in determining the CO₂ infrared cooling. The region where it is important also plays a crucial role when As a consequence, it is very important in establishing the different non-LTE regions of the parameterization (Fomichev et al., 1998). To identify the atmospheric regions where it is important, we have perturbed-performed a calculation by dividing the k_0 collisional rate by a factor of two. We recall that perturbing this rate is equivalent to perturbing, which is almost equivalent to change the O(³P) concentration -by the same factor. Fig. 6 shows this effect for the six four p-T profiles considered for and considering the current CO₂. Generally, it is most important above around 10^{-3} hPa (~95 km). However, for the sub-arctic summer (SAS) and sub-arctic winter (SAW) atmospheres it is also important down to $5 \cdot 10^{-3}$ hPa (~85 km). The fact that its importance starts being significant at different

atmospheric levels for the different p-T profiles poses an additional difficulty in the development of the parameterization.



Figure 7. Atmospheric regions considered in the parameterization. $x_{b,i}$ represents the boundaries of the layers; $x_{b,1} = 9.875$, $x_{b,2} = 12.625$; $x_{b,3} = 16.375$, and $x_{b,4} = 19.875$. The temperature profiles used in the reference calculations are also shown as a reference.

5 The parameterization

Essentially, we follow here the parameterization developed by Fomichev et al. (1998). A brief description of the method including the most important features and equations is given in this section.

The atmosphere is divided into five different regions (see Fig. 7) where different approaches are used for calculating the cooling rates. These regions are qualitatively the same regions as those defined by Fomichev et al. (1998) but their altitude extensions (except for the LTE region) have been significantly revised, mainly as a consequence of the ample range of CO₂ abundances for which this parameterization is developed. In fact, their upper boundaries have been moved upwards (except for LTE), resulting in the following ranges: LTE from the lower boundary at LTE: x =0 up to x_{b,1} 0–9.875 (z = 9.875)
(z ≈ 0-≈70 km); NLTE1: from x_{b,1} to x_{b,2} x=12.625 -9.875-12.625 (z ≈70-87 km); NLTE2: from x_{b,2} to x_{b,3} x=16.375 12.625-16.375 (z ≈ 87-109 km); NLTE3: from x_{b,3} to x_{b,4} x = 19.875-16.375-19.875 (z ≈ 109-180 km); and NLTE4: for

 $x > 19.875 \ (z \gtrsim 180 \text{ km}).$

The lowermost (LTE) and the uppermost (NLTE4) regions are the most straightforward and also the regions where the errors are in general smaller. The most difficult parts are the transition regions from LTE to non-LTE, where: (i) several bands contribute to the cooling with different source functions and their relative contributions depend very much on the actual temperature profiles (see Fig. 4); and (ii) the exchange of radiation between layers is significant and different for the different considered bands. Further, although most of the radiative excitation at a given layer is produced by the absorption of photons travelling downwards can also contribute significantly. This is the case, for example, for the stronger fundamental band near the mesopause. (iii) The Further, the cooling above around 90 km depends also on the collisions with atomic oxygen. This effect can be accurately taken into account in the upper non-LTE regions where

all bands become optically thin, however it is very difficult to represent it properly between around the mesopause and a few tens km above, where the atomic oxygen concentration varies largely and the exchange of radiation between layers is still important.

5.1 The LTE region

300 The parameterization in the LTE region is based on the Curtis matrix method. The cooling rate $\epsilon_i^t(\nu)$ at a given pressure level x_i , in a spectral region ν , and for a particular temperature profile t, is given by

$$\epsilon_i^t(\nu) = \sum_{j=0}^{j_{\rm CM}} \mathcal{A}_{i,j}^t(\nu) \varphi_j^t(\nu) \underbrace{+ v_i^t(\nu) \varphi(T_{\rm surf}^t, \nu)}_{\text{surf}, \nu},\tag{1}$$

where the indices i, j refer to pressure levels x_i and x_j , and the sum is extended over the pressure levels x_j ranging from the lower boundary, $x_j = 0$, until $x_{j_{CM}} = 13.875$. This upper boundary of the Curtis matrix $\frac{x_{j_{CM}}}{x_{j_{CM}}} = 13.875$, has been selected to 305 minimize the error in the lowest non-LTE region, NLTE1 (see more details in Sec. 5.2 below). $\mathcal{A}_{i,j}^t(\nu)$ is the modified Curtis matrix (slightly different from its usual definition, see, e.g. López-Puertas and Taylor, 2001). The last term factor $\varphi_i^t(\nu)$ in

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 $\varphi_j^t(\nu) = \exp(-h\nu/(k_B T_j^t)) \exp[-h\nu/(k_B T_j^t)],$

where h is the Planck constant, k_B is the Boltzmann constant, and T_j^t is the temperature of the p-T profile t at level x_j . The 310 Similarly, $\varphi(T_{surf}^t, \nu)$ corresponds to the exponential part of the Planck function for the surface temperature T_{surf}^t . The $v_i^t(\nu)$ term accounts for the absorption at level i times the transmission from the surface up to level i at ν , so that $v_i^t(\nu)\varphi(T_{surf}^t,\nu)$ accounts for the heating rate due to the absorption of the radiation from the surface (or lower boundary). The cooling rate is calculated in the spectral range from 540 to 800 cm⁻¹ divided into frequency intervals, ν , 10 cm⁻¹ wide. Those LTE cooling rate profiles have been calculated for each of the six p-T reference atmospheres and the eight CO₂ vmrs profiles.

315 In the parameterization, the Curtis matrix is expressed with an explicit temperature dependence by

$$\mathcal{A}_{i,j}^t(\nu) = \mathbf{a}_{i,j}^t(\nu) + \mathbf{b}_{i,j}^t(\nu) \,\varphi_i^t(\nu),$$

where the matrix coefficients $\mathbf{a}_{i,j}^t(\nu)$ and $\mathbf{b}_{i,j}^t(\nu)$ are given by

$$\mathbf{a}_{i,j}^{t}(\nu) = \mathcal{A}_{i,j}^{t}(\nu) \frac{S_{0}(\nu)}{S_{0}(\nu) + [S_{1}(\nu) + S_{2}(\nu)] \varphi_{i}^{t}(\nu)},$$

320 $\mathbf{b}_{i,j}^t(\nu) = \mathcal{A}_{i,j}^t(\nu) \frac{S_1(\nu) + S_2(\nu)}{S_0(\nu) + [S_1(\nu) + S_2(\nu)]\varphi_i^t(\nu)},$

and $S_0(\nu)$, $S_1(\nu)$, and $S_2(\nu)$ are the band strengths of the fundamental, first hot and second hot bands, respectively, in the ν -interval. In this way, the temperature dependence, mainly caused by the band strength of the first and second hot bands, is carried out in $\varphi_i^t(\nu)$. Those matrix coefficients are calculated for each spectral interval ν . We obtain the coefficients for the entire spectral region of the CO₂ 15 μ m bands by summing over all the ν -intervals and weighting with the ν -dependency of the $\varphi_i^t(\nu)/\varphi_i^t(\nu_0)$ factor, e.g.

$$\frac{\mathbf{a}_{i,j}^{t}}{\mathbf{b}_{i,j}^{t}} \equiv \frac{\sum_{\nu} \mathbf{a}_{i,j}^{t}(\nu) \varphi_{j}^{t}(\nu)}{\varphi_{j}^{t}(\nu_{0})}$$

$$\frac{\mathbf{b}_{i,j}^{t}}{\mathbf{b}_{i,j}^{t}} \equiv \frac{\sum_{\nu} \mathbf{b}_{i,j}^{t}(\nu) \varphi_{j}^{t}(\nu) \varphi_{i}^{t}(\nu)}{\varphi_{j}^{t}(\nu_{0}) \varphi_{i}^{t}(\nu_{0})}$$

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$$\mathbf{a}_{i,j}^{t} = \frac{\sum_{\nu} \mathbf{a}_{i,j}^{t}(\nu) \varphi_{j}^{t}(\nu)}{\varphi_{j}^{t}(\nu_{0})}, \quad \text{and} \quad \mathbf{b}_{i,j}^{t} = \frac{\sum_{\nu} \mathbf{b}_{i,j}^{t}(\nu) \varphi_{j}^{t}(\nu) \varphi_{i}^{t}(\nu)}{\varphi_{j}^{t}(\nu_{0}) \varphi_{i}^{t}(\nu_{0})}$$

with $\nu_0 = 667.3799 \text{ cm}^{-1}$ being the frequency of the fundamental band of the major isotopologue.

Next, we define global $\mathbf{a}_{i,j}$ and $\mathbf{b}_{i,j}$ matrix coefficients, to be used for any input temperature profile, as weighted averages of the $\mathbf{a}_{i,j}^t$ and $\mathbf{b}_{i,j}^t$ for the six reference p-T profiles. We introduce a set of normalized weights ξ_i^t , altitude-dependent, for each temperature profile so that:

$$\mathbf{a}_{i,j} = \sum_{t} \xi_i^t \mathbf{a}_{i,j}^t \quad \text{and} \quad \mathbf{b}_{i,j} = \sum_{t} \xi_i^t \mathbf{b}_{i,j}^t.$$
(3)

(2)

335 Analogously to the matrix coefficients
$$\mathbf{a}_{i,j}^{t}(\nu)$$
 and $\mathbf{b}_{i,j}^{t}(\nu)$ we define the corresponding vector coefficients for the surface
flux, $a_{\operatorname{surf},i}^{t}(\nu)$ and $b_{\operatorname{surf},i}^{t}(\nu)$, so
 $v_{i}^{t}(\nu) = a_{\operatorname{surf},i}^{t}(\nu) + b_{\operatorname{surf},i}^{t}(\nu)\varphi_{i}^{t}(\nu)$, with
 $a_{\operatorname{surf},i}^{t}(\nu) = \frac{v_{i}^{t}(\nu) S_{0}(\nu)}{S_{0}(\nu) + [S_{1}(\nu) + S_{2}(\nu)]\varphi_{i}^{t}(\nu)}, \qquad b_{\operatorname{surf},i}^{t}(\nu) = \frac{v_{i}^{t}(\nu) [S_{1}(\nu) + S_{2}(\nu)]}{S_{0}(\nu) + [S_{1}(\nu) + S_{2}(\nu)]\varphi_{i}^{t}(\nu)},$

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$$\boldsymbol{u}_{\mathrm{surf},i}^{t} = \frac{\sum_{\nu} \boldsymbol{a}_{\mathrm{surf},i}^{t}(\nu) \varphi(\boldsymbol{T}_{\mathrm{surf}}^{t},\nu)}{\varphi(\boldsymbol{T}_{\mathrm{surf}}^{t},\nu_{0})}, \qquad \boldsymbol{b}_{\mathrm{surf},i}^{t}(\nu) = \frac{\sum_{\nu} \boldsymbol{b}_{\mathrm{surf},i}^{t}(\nu) \varphi(\boldsymbol{T}_{\mathrm{surf}}^{t},\nu) \varphi_{i}^{t}(\nu)}{\varphi(\boldsymbol{T}_{\mathrm{surf}}^{t},\nu_{0}) \varphi_{i}^{t}(\nu_{0})},$$

$$a_{\text{surf},i} = \sum_{t} \xi_i^t a_{\text{surf},i}^t \underset{\sim}{\text{and}} b_{\text{surf},i} = \sum_{t} \xi_i^t b_{\text{surf},i}^t.$$

$$(4)$$

In this way, the cooling rate ϵ_{i} , at a pressure level x_i , ϵ_i , for a given input temperature profile T_{inp} , is calculated in the parameterization by:

The weights ξ_i^t are obtained by minimising the cost function $\chi(x_i)$ at each pressure level x_i , given by the sum of the square of the differences of the reference line-by-line-LTE cooling rates, ϵ_{ref}^t , (see Sec. 4.2) and those computed by the parameterization by using Eq. (5), $\epsilon_{par,i}^t$, for each p-T profile t by using Eq. (5), e.g.,

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$$\chi(x_i) = \sum_t \eta^t \left\{ \epsilon_{\mathrm{ref},i}^t - \epsilon_{\mathrm{par},i}^t \right\}^2,$$

or, in more detail, by

The normalized coefficients η^t were introduced originally for considering different fractions of the area of the Earth ascribed to each *p*-*T* reference profile. Thus, in the previous parameterization they were taken equal to 0.05 for the subarctic (winter and summer) profiles, 0.1 for the mid-latitude (winter and summer) profiles, 0.4 for the tropical profile, and 0.3 for the midlatitude equinox *p*-*T* profile. In this study, we have explored different options including the original coefficients and a uniform weighting for the six *p*-*T* profiles and we found a smaller χ for the latter, e.g., $\eta = 1/6$ for all profiles. Hence, that was included in this version.

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In that way, we have parameterized the cooling rates as a function of temperature. The cooling rates depend also on the CO₂ vmr profiles (see Fig. 3). The parameterization incorporates the dependence on the CO₂ abundance by calculating $\mathbf{a}_{i,j}$ and $\mathbf{b}_{i,j}$ for a generic CO₂ profile by assuming a linear interpolation in $\frac{\log(\mathbf{a}_{i,j}/\text{VMR}(x_i))}{\log[\mathbf{a}_{i,j}/\text{VMR}(x_i)]}$ and $\log[\mathbf{b}_{i,j}/\text{VMR}(x_i)]$ from the adjacent CO₂ vmr profiles. Thus, the $\mathbf{a}_{i,j}$ and $\mathbf{b}_{i,j}$ coefficients of Eq. 5 3 have been calculated (and are provided) for the eight CO₂ vms shown in Fig. 221b.

5.2 The NLTE1 region: The transition from LTE to non-LTE

- This region is difficult to parameterize because we have several bands contributing to the cooling (see Fig. 4) and their relative contributions depend significantly on both the temperature structure and the CO_2 vmr profile. Note that, at certain levels, the cooling induced by the weaker hot bands is larger than that of the stronger fundamental band. We should also note that the contribution of the first hot bands at high altitudes, ~110–150 km is not negligible (5–10%, Fig. B1). This contribution is accounted for in the parameterization by implicitly assuming that it is produced by the fundamental band of the main 270 instance (see below and Sec 4.2).
- 370 isotopologue (see below and Sec 4.2).

The lower boundary of this region, e.g. the LTE-to-NLTE1 transition, occurs, depending on the temperature profile, at altitudes from \sim 70 km up to \sim 85 km (0.08 hPa to 0.004 hPa, see Fig. B2), taking place a few kilometers lower for the subarctic summer atmosphere and the lowest CO₂ VMR. This transition region occurs at higher altitudes for larger CO₂ vmrs, i.e., the atmosphere becomes optically thicker and fewer collisions are enough to keep the levels in LTE. However, since we need to

represent also the low CO₂ vmrs, we decided to conservatively set up this region at rather low altitudes, $x_{b,1} = 9.875$ (~70 km), the same <u>level</u> used in the previous parameterization.

The upper limit of this region was set up in the previous parameterization at the pressure levels where collisions with $O({}^{3}P)$ start affecting significantly the cooling rates. Again, that pressure level depends on the temperature profile (and also on the $O({}^{3}P)$ concentration), being lower, at ~0.004 hPa ($x \approx 12.4$), for the subarctic summer and winter conditions (see Fig. 6). Here, we have taken the upper boundary of $x_{b,2} = 12.625$ (≈ 87 km), slightly higher than the 12.5 value assumed in the original parameterization.

In this region we followed, as in Fomichev et al. (1998), the matrix approach discussed in Sec. 5.1 above. Thus the , Eq. 5 was used but with corrected modified $\mathbf{a}_{i,j}^{\prime t}$ and $\mathbf{b}_{i,j}^{\prime t}$ coefficients that account for the non-LTE corrections. For each p-T profile, t, we define:

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$$\mathbf{a}_{i,j}^{\prime t} = \mathbf{a}_{i,j}^{t} \left[\epsilon_{(\text{ref,nlte}),i}^{t} / \epsilon_{(\text{ref,lte}),i}^{t} \right]$$
 and
 $\mathbf{b}_{i,j}^{\prime t} = \mathbf{b}_{i,j}^{t} \left[\epsilon_{(\text{ref,nlte}),i}^{t} / \epsilon_{(\text{ref,lte}),i}^{t} \right],$

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where $\epsilon_{(ref,lte)}^{t}$ and $\epsilon_{(ref,nlte)}^{t}$ are the reference LTE and non-LTE cooling rates, respectively. Then, the general $\mathbf{a}_{i,j}'$ and $\mathbf{b}_{i,j}'$ coefficients were calculated by following the same procedure as for the LTE region. That is, by weighting the *p*-*T*-specific $\mathbf{a}_{i,j}'$ and $\mathbf{b}_{i,j}'$ coefficients with a set of altitude-dependent weights $\xi_i'^{t}$ and minimizing the total cost function $\chi(x_i)$ (see Sec. 5.1). In this way, we obtain:

$$\begin{aligned} \mathbf{a}_{i,j}' &= \sum_{t} \xi_{i}'^{t} \, \mathbf{a}_{i,j}^{t} \left[\epsilon_{(\text{ref,nlte}),i}^{t} / \epsilon_{(\text{ref,lte}),i}^{t} \right] \quad \text{and} \\ \mathbf{b}_{i,j}' &= \sum_{t} \xi_{i}'^{t} \, \mathbf{b}_{i,j}^{t} \left[\epsilon_{(\text{ref,nlte}),i}^{t} / \epsilon_{(\text{ref,lte}),i}^{t} \right], \end{aligned}$$

and the cooling rates are computed by using Eq. 5 but replacing $\mathbf{a}_{i,j}$ and $\mathbf{b}_{i,j}$ by $\mathbf{a}'_{i,j}$ and $\mathbf{b}'_{i,j}$, respectively, i.e.,

This procedure, while producing a perfect match for a single atmosphere by construction, generates irregularities for other atmospheres at some levels, e.g., when using $\mathbf{a}_{i,j}^{\prime t}$ for atmosphere t' at points where $\epsilon_{(ref, Ite),i}^{t}$ is close to zero. We observed that the irregularities were significantly mitigated by reducing the dimensions of the Curtis matrix from 83×83 to 55×55, where i = 55 corresponds to $x_{CM} = 13.875$ ($\mathbf{p} = 9.422 \times 10^{-4}$ hPa, $z \approx 94$ km). That is, by placing x_{CM} slightly above the x_{b2} boundary boundary between the NLTE1 and NLTE2 regions. Errors induced in the LTE cooling rates by the matrix reduction are negligible (smaller than 0.05 K day⁻¹ at the upper boundary).

5.3 The NLTE2 and NLTE3 regions: The recurrence formula with/without correction

The parameterization in the NLTE2, NLTE3 and NLTE4 regions is based on the recurrence formula proposed by Kutepov and Fomichev (1993). This approach is valid when the cooling rate is dominated by the fundamental band and also the absorption of radiation coming from the layers above the layer at work can be neglected (Kutepov and Fomichev, 1993; Fomichev et al., 1998). Those The boundaries of these regions are then adapted to the applicability of that approach. The NLTE3 boundaries were chosen to embrace the region where those conditions are fulfilled to a large degreein the NLTE3 region. In the layers below, i.e., in the NLTE2 region, however, that formula is not accurate and requires a correction term that accounts to account

- 410 for the absorption of radiation coming from the layers above and for the cooling of bands other than the fundamental of the main isotopologue. This The recurrence formula is also the basis for the calculation of the cooling rate in the NLTE4 region (see Sec. 5.4)but, but it is simplified because the exchange of photons within the layers of this region with the layers below can be neglected.
 - We Further, we should emphasise that the dependence of the cooling rate on the CO_2 vmr in these regions is mainly twofold.
- 415 On one hand, its direct dependence (see Eq. 7 below), and also through the escape function which depends on the CO₂ column above a given layer (see FigFigs. S7).

and <u>S8</u>). We discuss below the boundaries of the NLTE2 and NLTE3 layers and the expressions that are used for the cooling rates in these regions. First, we describe, i.e., the recurrence formulation, then the correction that is applied in the NLTE2 region.

- The lower boundary of the NLTE2 region is limited from below by the layers set up at the layer where the cooling rate obtained by the corrected recurrence formula is better more accurate than that given by the non-LTE-corrected Curtis matrix approach . This layer has been chosen (used in NLTE1). This has been set up at $x_{b,2} = 12.625$ (≈ 87 km), which is very similar to the value in the original parameterization of $x_{b,2} = 12.5$ (≈ 85 km). Its upper limit The upper boundary of the NLTE2 region is set up at the layers pressure level where the recurrence formula does not need to be corrected to yield an accurate estimation
- 425 of the cooling rate. In this work, it has been set up at $x_{b,3} = 16.375 \ (\approx 109 \text{ km})$, which is significantly higher than the value of $x_{b,3} = -14 \ (\approx 93 \text{ km})$ set up in the previous parameterization. The main reason for this is that for the higher CO₂ vmr's vmrs used here, the atmosphere becomes optically thicker; hence, the absorption of radiation of the layer above needs to be taken into account also at lower pressures.

The Thus, the cooling rates in the NLTE2 and NLTE3 regions are calculated by:

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$$\epsilon(x_i) = \kappa_F \frac{\text{VMR}(x_i)[1 - \lambda(x_i)]}{M(x_i)} \tilde{\epsilon}(x_i), \tag{7}$$

where $\kappa_F = 2.55520997 \times 10^{11}$ is a constant that depends on the Einstein coefficient of the fundamental band (*A*), on ν_0 and on the units of ϵ (Fomichev et al., 1998)¹, VMR(*x*) is the CO₂ vmr, M(x) is the mean molecular weight, $\lambda(x_i) = A/[A + l_t(x_i)]$, $\lambda(x_i) = A/[A + l_t(x_i)]$ where $l_t(x_i) = k_{N2} [N_2] + k_{O2} [O_2] + k_O [O]$, k_{N2} , k_{O2} and k_O are the collisional rate constants with N₂, O₂ and O(³*P*) (see Table 1), and [N₂], [O₂] and [O(³*P*)] are the concentrations of the respective species. Note that the collisional rates depend on x_i through their temperature dependencies.

The escape probability function L(u) represented as function of the column at a given layer, u(x), for several and vmr profiles. They have been calculated with the GRANADA code. The right panels show the differences with respect to the values used in the previous parameterization (a single profile for all atmospheres). The columns as a function of altitude are shown in Fig. S8.

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 $\tilde{\epsilon}$ at level x_i , $\tilde{\epsilon}(x_i)$, is obtained by the recurrence formula

$$[1 - \lambda(x_i)(1 - D_i)] \tilde{\epsilon}(x_i) = [1 - \lambda(x_{i-1})(1 - D_{i-1})] \tilde{\epsilon}(x_{i-1}) + D_{i-1}\varphi_{i-1} - D_i\varphi_i$$
(8)

starting from the lower boundary at $x_i = x_{b2}$, where, using Eq. (7),

$$\tilde{\epsilon}(x_{b2}) = \frac{M(x_{b2})}{\kappa_F \operatorname{VMR}(x_{b2}) \left[1 - \lambda(x_{b2})\right]} \epsilon(x_{b2}) \tag{9}$$

and $\epsilon(x_{b2})$ is obtained by Eq. (6). The D_i coefficients above are given by

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$$D_i = (d_{i-1} + 3d_i)/4$$
 and $D_{i-1} = (3d_{i-1} + d_i)/4$ (10)

where

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$$d_{i} = \begin{cases} \alpha(x_{i}, u) L(u) & \text{if } x_{b2} \le x_{i} \le x_{b3}. \\ L(u) & \text{if } x_{i} \ge x_{b3}. \end{cases}$$
(11)

L(u) is the escape function which mainly depends on the CO₂ column, u, above a given level x_i . However, the temperature of the layers above. The temperature of those layers affects this function as it influences the line shape of the CO₂ lines and

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hence the probability of photons escaping to space. This is reflected in Fig. S7shows the calculations of a, which shows L(u) as a function of the CO₂ column for the six p-T reference atmospheres and a single CO₂ vmr profile (#3); and for the MLE atmosphere and the eight, current vmr). The dependence of L(u) with the CO₂ vmr profiles -is shown in Fig. S7. In our calculations, we have used for L(u) the average of this function for the six p-T reference atmospheres.

¹Note that this constant has been changed from its value of 2.63187×10^{11} in Fomichev et al. (1998) to the actual value used in the distributed code and guoted here of $2.55520997 \times 10^{11}$.

The $\alpha(x_i, u)$ parameter entering in Eq. 11 for (11) and needed in the NLTE2 region, has been computed by minimizing the following cost function at each point x_i :

$$\chi(x_i) = \sum_{t} \eta^t \left[\epsilon_{\text{ref}}^t(x_i) - \epsilon_{\text{par}}^t(\alpha, x_i) \right]^2$$

After performing some sensitivity tests, we used uniform weighting for the different reference atmospheres (η^t = 1/6 for all atmospheres), rather than the area-weighting used in the previous parameterization. Other tests were performed to determine the optimal upper boundary for the α correction: extending the region upwards reduces the error in the x-x=16-19-16-19
region, but results in a spurious jump at the uppermost boundary, which is avoided with a lower x_{b3} = 16.375if using a lower x_{b3} of 16.375. It is worth noting that α above x x = 14.5 goes takes values below unity, thus decreasing the escape in the region. For the fit of the optimal α, the parameterized value of ε(x_{b2}) is considered as starting point rather than the reference value.

In the NLTE3 region, we used the same method as in region NLTE2, except that no correction for the L(u) function is applied, i.e., $\alpha(x_i, u) = 1$.

465 5.4 The NLTE4 region

The recurrence formula used in the NLTE2 and NLTE3 regions described above is also valid in the uppermost region, NLTE4 , but, in this case, region but, as the CO_2 bands are so optically thin here, the exchange of radiation within the layers of this region can be neglected and the recurrence formula is reduced to a simpler expression. Namely, a cooling-to-space term and an additional term that accounts for the absorption of the radiation emitted by the layers below the boundaryof this NLTE4

470 regionits boundary. Thus, in this region, the cooling rate is calculated for this region is computed by using Eq. (7) but with a simple expression for $\tilde{\epsilon}(x_i), \tilde{\epsilon}(x_i) = \Phi(x_{b3}) - \varphi(x_i)$, that gives a smooth transition to the cooling to space approximation, e.g.,

$$\epsilon(x_i) = \kappa_F \frac{\text{VMR}(x_i) \left[1 - \lambda(x_i)\right]}{M(x_i)} \left[\Phi(x_{b3}) - \varphi(x_i)\right],\tag{12}$$

where $\Phi(x_{b3})$ is obtained from the boundary condition

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$$\Phi(x_{b3}) = \tilde{\epsilon}(x_{b3}) + \varphi(x_{b3})$$
 (13)

and using the recurrence formula in Eq. (8).

6 Testing the parameterization for the reference atmospheres

The parameterization has been tested against the accurate line-by-line cooling rates calculation for the references reference cooling rates calculated for the reference atmospheres (the six p-T profiles and the eight CO₂ VMR profiles) (see next section),

480 and for intermediate CO_2 vmrs and for the k_0 collisional rate (Sec. 6.2). Further, it has been verified for measured temperature profiles that exhibit a large variability (Sec. 7) - and for the temperature profiles obtained by a high-resolution version of WACCM-X (Sec. 8).

6.1 Accuracy of the parameterization for the reference atmospheres

In this section, we discuss the accuracy of the current parameterization for the assumed references reference atmospheres. The

- 485 non-LTE models used in both the original (Fomichev et al., 1998) and in the current parameterizations are different. Hence we expect some differences not just caused by the parameterization itself but possibly also by the different non-LTE models. Figure 8 shows the cooling rates of this parameterization compared to those of the previous parameterization and to those obtained by the accurate, line-by-line (reference) non-LTE modelthe reference ones, for a contemporary CO₂ vmr profile (#3in Fig. ??) and the six *p*-*T* profiles. The comparison for lower CO₂ profiles are shown in Figs. S9 and S10, and S11, and
- in Figs. <u>\$12511</u>–S15 for high CO₂ vmrs. We should clarify that to make the comparison meaningful the three sets of cooling rates shown here include the same updated collisional rates (Table 1). Note , however, that these rates are different from those used in the previous parameterization (Fomichev et al., 1998). The new parameterization also supports the previous collisional rates but it has <u>ben been optimized</u> for the new ones , <u>see in</u> Table 1. As expected, larger differences are obtained in the region between 10⁻² hPa (~80 km) and 2·10⁻⁵ hPa (~120 km) and are more marked for the sub-arctic summer (SAS) and sub-arctic winter (SAW) atmospheres.

The differences are more clearly illustrated in Figs. 9 and S16, where we show the mean and the RMS (root mean square) standard deviation of the differences for the eight for lowest and four highest CO_2 VMR profiles, respectively. The improvement of the new parameterization is noticeable (compare blue and red lines). In general, the cooling rates of the current parameterization are more accurate than in the previous one for most of the regions and temperature structures. We observe that the <u>terrors</u> errors (e.g., the differences with respect to the line-by-line reference non-LTE cooling rates) of the new pa-

- rameterization (red curves) are very small overall. They are below ~0.5 K day⁻¹ for the current and lower CO₂ abundances (see Fig. 9). For higher CO₂ concentrations, between about two and three times the pre-industrial values, the largest errors are ~1–2 K day⁻¹, and are located near 100–120110–120 km (see Fig. 9 and top/left panel in Fig. S16). The quoted values refer to the mean of the differences although they are larger for the individual *p*-*T* atmospheres. The spread of these values is larger 505 in the region of 10⁻² hPa (~80 km) to 10⁻⁴ hPa (~105 km), where the RMS reach values between -2 K day⁻¹ to +2 K day⁻¹
- 505 in the region of 10^{-2} hPa (~80 km) to 10^{-4} hPa (~105 km), where the RMS reach va (Fig. 9).

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For the very high CO₂ concentrations (four, five and ten times the pre-industrial abundances) the errors are also very small, below $\sim 1 \text{ K day}^{-1}$ for most regions and conditions; except in the $\frac{107-140107-135}{107-135}$ km region where we found maximum positive bias of $\sim 4 \text{ K day}^{-1}$, $\sim 5 \text{ K day}^{-1}$, and $\sim 16 \text{ K day}^{-1}$ for the 4×, 5× and 10× the pre-industrial CO₂ vmr profiles (see

510 Fig. S16). Those maximum errors in the cooling rates for the different vmrs are however comparable when expressed in relative terms, all about 1.2%. It is also notable the significantly large spread (large RMS) significant RMS in the region of \sim 80–120 km; clearly, the region which is more difficult to parameterize, particularly for such a large range of CO₂ abundances.

That increase of the differences of the new parameterization with respect to the reference calculations for the very high CO_2 vmrs near 110 km, seems to be related to the transition region from NLTE2 to NLTE3 (see Fig. 7). It looks like the cooling in

515 the lower part of the NLTE3 region requires also the α correction correction by the α factor for high CO₂ vmrs. This suggests that for higher CO₂ vmrs the parameterization would be more accurate if this transition altitude is risen. Such a rise, however,



Figure 8. Comparison of the cooling rates of the current and previous parameterizations with respect to reference non-LTE cooling rates for the present-day CO_2 vmr profile #3 and the six p-T reference atmospheres. Note that the latter cooling rates are hardly visible in the left panels of the figures. See Figs. S9 and S10 for lower CO_2 concentrations, and Figs. S11–S15 for higher CO_2 vmrs.



Figure 9. Mean of the cooling rates differences of the current and previous parameterizations with respect to the reference cooling rates for the four lowest CO_2 vmr profiles. The shaded areas show the standard deviation of the differences between the six p-T atmospheres. Detailed comparisons for each p-T profile are shown in Fig. 8 above, and in Figs. S9, S10 and S11 in the supplement.

would worsen the cooling below this boundary. This manifests the difficulty of obtaining very accurate cooling rates for a large range of CO_2 vmr with this method.

Comparison of the cooling rates of the current and previous parameterizations with respect to reference non-LTE cooling
 rates for the present-day vmr profile #3 and the six reference atmospheres. Note that the latter are hardly visible in the left panels of the figures. See Figs. S9 and S10 for lower concentrations, and Figs. S11–S15 for higher vmrs.

Global mean of the cooling rates differences of the current and previous parameterizations with respect to the reference line-by-line (LBL) cooling rates for the four lowest vmr profiles. The shaded areas show the standard deviation of the differences between the six atmospheres. Detailed comparisons for each profile are shown in Fig. 8 above, and Figs. S9, S10, and S11

525 in S1. Global mean of the cooling rates differences of the current parameterization with respect to the reference non-LTE cooling rates for the four highest vmr profiles (#5–8) considered in this work. The shaded areas show the differences (standard deviation) spread between the six p-T atmospheres. Detailed comparisons for each p - T profile are shown in Figs. S12–S15.

6.2 Assessment of the cooling rates for intermediate CO_2 vmrs and for the k_0 collisional rate

The aim of the parameterization is to be used for any CO₂ vmr input profile in the range of the profiles #1 and #8 of Fig. ??

530 <u>1b</u> and any plausible value for the k_0 rates discussed in Sec. 4.2. In this section we demonstrate that the parameterization also works is also very accurate for CO₂ vmrs that fall between the reference profiles used for its development and also when using different k_0 values. In particular, we show results for the intermediate CO₂ vmr profiles #9, #10 and #11 (see Fig. ??1b) and the k_0 collisional rate used in the reference calculations divided by a factor of two.

Comparison of the cooling rates of the current and previous parameterizations with respect to accurate cooling rates for the 535 intermediate vmr profile #9 (see Fig. ??) and the six reference atmospheres.

Figure B4 shows the results of the calculation for the intermediate CO_2 vmr profile #9, which is between the current CO_2 vmr value and that projected for 2050 (two times the pre-industrial value). We can observe similar features to the calculations for the adjacent reference contemporary CO_2 vmr profile (#3) (see Fig. 8), although the differences are slightly larger because we are using a larger the CO_2 vmr profile is larger. The distinctions are more clearly seen in Fig. 10 where we show the

- 540 mean and the RMS standard deviation of the differences for the six p-T profiles. The patterns in the differences, as well as their values and spreads, are very similar to those described above in Sec. 6 for the CO₂ vmr-reference profiles. The major differences appear between 105 and 140135 km, reaching maximum values of 1, 2 and 109 K day⁻¹ for the vmr profiles #9, 10 and 11, respectively. Again, as we observe, we observe that the new parameterization is more accurate at practically all altitude levels. Further, the maximum values of the standard deviations of the differences for the various p-T profiles also resemble
- very much those discussed before, reaching maximum values of about 2 K day^{-1} , 3 K day^{-1} , and almost 1015 K day^{-1} for the respective CO₂ vmr profiles. Note that although these values are larger for higher CO₂ vmrs, they are very similar when expressed in percentage.

As the $CO_2(v_2)$ - $O(^3P)$ collisional rate, $k_{CO_2-O}k_O$, is still uncertain nowadays by almost about a factor of two (García-Comas et al., 2012) (see, e.g., García-Comas et al., 2012) and we intend that this parameterization be also used used also for rates different of the

- nominal value, we have tested its accuracy for its lowest likely value. Fig. B shows the results of decreasing the collisional rate $k_{CO_2-O} k_O$ by a factor of two for the CO₂ vmr profile #3 (current value) and the six *p*-*T* profiles. The errors incurred when using this rate are slightly larger than for the nominal rate. We see that for the reduced rate, the differences are generally below 1 K day⁻¹, but can have values up to 2 K day⁻¹ near 90 km for the mid-latitudes summer and mid-latitudes winter atmospheres; and between ~8085 km and 100 km for the sub-arctic summer conditions. The improvement with respect to the
- previous parameterization is not that large for this case (see Fig. 11); only below 70 km and near 90 km, mainly caused by the significant difference incurred by the previous parameterization for the sub-arctic winter atmosphere (see bottom/right panel in Fig. B). The smaller differences between both versions of the parameterizations for the reduced k_0 are likely caused because the previous one was optimized for this lower reduced rate.

Testing the effect of the (v_2) - collisional rate on the parameterization. Comparison of the cooling rates of the current and 560 previous parameterizations with respect to the reference cooling rates for the current vmr abundance (profile #3, see Fig. ??) and the six *p*-*T* reference atmospheres when reducing the collisional rate by a factor of two.



Figure 10. Mean of the cooling rates differences of the current parameterization with respect to the reference cooling rates for the intermediate CO_2 vmr profiles (#9–11). The shaded areas show the differences <u>spread</u> (standard deviation) spread between the six p-T atmospheres. Note the different scales of the *x*-axis. Detailed comparisons for each p-T profile are shown in Figs. B4, S17 and S18.



Figure 11. <u>Global mean Mean of the cooling rates differences of the current parameterization with respect to the accurate (reference) cooling rates for the results in Fig. B. The shaded areas show the differences spread (standard deviation) spread between the six p-T atmospheres.</u>

6.3 Performance of the parameterization

In Table 2 we list some examples of the time taken for executing the parameterization for two processors, two compilers and three atmospheric intervals. It is noticeable the better performance (up to a factor of 5 faster) when using the Intel Fortran

565 Compiler Classic (ifort) with respect to the gfortran. We did not test the ifort compiler in the second processor, which suggests that the times obtained with ifort and processor #1 could be improved in a factor of 2.7. We did not try other more modern Fortran compilers like ifx which could even run the parameterization even faster. It is worth also mentioning that if the atmosphere is cut in the first 50 km, the execution is about 1.76 faster. This is because in the lower region, where the cooling occurs in LTE conditions, the calculation involves the Curtis matrix and operations of the coefficient matrices *a* and *b*

570 are required. Reducing this region, e.g. starting near 50 km where LTE still prevails, makes the parameterization significantly faster. Reducing the atmosphere at the upper layers, however, hardly decreases the computation time. Thus if using a processor of type 2, with an *ifort* compiler for an atmosphere in the range of 50–270 km, the calculation of a cooling rate profile could be as low as 0.015 ms, and with still margin of improvement if using modern Fortran compilers like *ifx*.

 Table 2. An example Performance of the MIPAS nighttime temperature profiles (15 February 2009) used for verifying the parameterization accuracy. Note the large variability of the temperature profiles.

Processor Type, Specs.	Compiler	Input atmosphere (# levels, Altitude range)	Time (ms)
1, x86_64 64-bit AMD EPYC 7742 2.245 GHz	ifort	273, 0–550 km	0.074
1, x86_64 64-bit AMD EPYC 7742 2.245 GHz	ifort	185, 50–550 km	0.042
1, x86_64 64-bit AMD EPYC 7742 2.245 GHz	ifort	<u>162, 50–270 km</u>	0.041
1, x86_64 64-bit AMD EPYC 7742 2.245 GHz	gfortran	273, 0–550 km	0.360
<u>1,</u> x86_64 64-bit AMD EPYC 7742 2.245 GHz	gfortran	<u>185, 50–550 km</u>	0.204
1, x86_64 64-bit AMD EPYC 7742 2.245 GHz	gfortran	<u>162, 50–270 km</u>	<u>0.197</u>
2, x86_64 64-bit Intel Core i7 4.2 GHz	gfortran	273, 0–550 km	0.133
2, x86_64 64-bit Intel Core i7 4.2 GHz	gfortran	<u>185, 50–550 km</u>	0.077
2, x86_64 64-bit Intel Core i7 4.2 GHz	gfortran	<u>162, 50–270 km</u>	0.073

7 Testing the parameterization for the MIPAS measured temperatures

575 7.1 Solstice and equinox conditions

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We have compared the cooling rates estimated by the parameterization with those calculated accurately by the line-by-line (LBL) model the reference ones for realistic, e.g. measured, temperature profiles that present a large variability and very changing vertical structure (see e.g. Fig. B1). Specifically, we compared them for the p-T profiles measured by the MIPAS instrument (García-Comas et al., 2023) for five full days of measurements (about 2500 profiles) with global latitude coverage and covering two days for solstice (14 January and 13 June) and two days for equinox conditions (25 March and 21 September) for 2010. Further, we compare the results for the temperatures of 15 February 2009 when a strong stratospheric warming τ followed by an elevated stratopause event τ -occurred in the Northern polar hemisphere τ (see Sec. 7.2). The comparison is carried

out for the MIPAS measurements taken only during nighttime conditions, as the MIPAS non-LTE cooling rates for daytime, obtained simultaneously with the temperature inversion, include also the fraction of the 15 μ m cooling which is produced by

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the relaxation of the solar energy absorbed by CO_2 near-IR bands, which is not accounted for in this parameterization (see Sec. 9). The zonal mean of the temperatures, CO_2 vmrs and $O({}^{3}P)$ abundances for those conditions are shown in Figs. B2, S19 and S20, respectively.

MIPAS zonal mean nighttime temperatures for 14 January 2010 (Northern winter hemisphere, top/left), 25 March 2010 (Northern spring hemisphere, top/right), 13 June 2010 (Northern summer hemisphere, bottom/left) and 21 September 2010 590 (Northern fall hemisphere, bottom/right).



Figure 12. Zonal mean of the differences in the cooling rates of the old parameterization (left column) and the new one (right column) with respect to the reference cooling rates obtained for MIPAS temperatures for 14 January 2010 (solstice) and 25 March 2010 (equinox). Similar figures for 13 June 2010 (Northern summer hemisphere) and 21 September 2010 (Northern fall hemisphere) are shown in Fig. B3.

The results are presented in Fig. 12 for the zonal mean of the differences for two days one day of solstice and two days one day of equinox conditions and in Fig. 13 as the global mean difference for all latitudes for each of the four individual days.

Mean of the differences in the cooling rates of the old parameterization (blue) and the new one (red) with respect to the LBL accurate cooling rates obtained for MIPAS temperatures for 14 January and 13 June 2010 (solstice, left panels), and 25 March and 21 September 2010 (equinox, right panels).

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Figure 13. Zonal mean-Mean (solid lines) and RMS (dash lines) of the differences in the cooling rates of the old parameterization (left columnblue) and the new one (right columnred) with respect to the LBL reference accurate cooling rates obtained for MIPAS temperatures for 14 January and 13 June 2010 (solstice, left panels), and 25 March 2010 (equinox), 13 June 2010 (Northern summer hemisphere) and 21 September 2010 (Northern fall hemisphereequinox, right panels).

RMSs of the differences in the cooling rates of the old parameterization (in blue) and the new one (red) with respect to the LBL accurate cooling rates obtained for MIPAS temperatures for 14 January and 13 June 2010 (solstice, left panels), and 25 March and 21 September 2010 (equinox, right panels).

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In general, the new parameterization is slightly more accurate. For example, the deviations of the cooling rates from the reference LBL calculations in the altitude range of 105–115 km are larger in the old parameterization (about 2 K day⁻¹) than in the new onefor which they are negligible, which are negligible in this region. Also, the differences with respect to the reference calculations are larger in the altitude range of 80–95 km for solstice conditions, and at altitudes of 80–100 km for equinox conditions (see Fig. 13).

Overall, the errors in mean profiles of the cooling rates of the new parameterization for one day of measurements are 605 below 0.5 K day⁻¹, except in the region between $5 \cdot 10^{-3}$ hPa and $3 \cdot 10^{-4}$ hPa (~85–95 km), where they can reach values of $1-2 \text{ K day}^{-1}$. This region is the most difficult to parameterize because several bands contribute to the cooling rate and they are very sensitive to the temperature structure of the middle atmosphere (e.g., even outside this region). Note also that this is precisely the region where the standard deviation RMS of the differences of the cooling rate with respect to the reference ones are largest, reaching values of up to 6 K day⁻¹ (see Fig. **??**13).



Figure 14. As Fig. 12 but for the MIPAS temperatures taken on 15 February 2009 when a major elevated stratopause event occurred.

610 7.2 Elevated stratopause conditions

The comparison of the cooling rates estimated by the old and new parameterizations with respect to the reference LBL calculations for 15 February 2009, a day with a pronounced and unusual elevated stratopause event (see the zonal mean temperatures in Fig. B4) are shown in Fig. 14. Similar features as for the other conditions shown above can be appreciated, except in the polar winter region. The mean of the differences and the standard deviations for all the profiles at latitudes northernmost of

- 50° N are shown in Fig. 15. The differences are significantly larger than for other latitudes in the 80–95 km altitude region. Both parameterizations underestimate the cooling in that atmospheric region. The new parameterization has, however, a better performance above about 80 km, but in the strat-warm/elevated stratopause region (80–100 km) it still underestimates the cooling by 3–7 K day⁻¹ (~10%).
- It seems clear that part of this underestimation is caused by the fact that such atypical temperature profiles (see Sec. 3.1) were not considered in the parameterization. However, its inclusion would not solve the problem as in the calculations of the coefficients a trade-off of the weighting of the different p-T reference atmospheres has to be chosen (see Secs. 5.1 and 5.2). Thus, it might ameliorate the inaccuracy for these elevated-stratopause events but would worsen the accuracy for other general situations. This manifests the difficulty/limitation of this method to provide accurate non-LTE cooling rates for all temperature structures (gradients) that we might find in the real atmosphere. Nevertheless, we have to keep in mind that these situations are
- 625 sporadic and limited to high polar regions. Hence they should not impact significantly the accuracy of the cooling rates of this parameterization in global multiyear GCM simulations.



Figure 15. Mean (solid) and RMS (dash) of the differences in the cooling rates of the old parameterization (in blue) and the new one (red) with respect to the reference cooling rates obtained for MIPAS temperatures for 15 February 2009 for latitudes northernmost of 50°N.

- The MIPAS nighttime temperature zonal mean for 15 February 2009, used for verifying the parameterization accuracy for stratospheric sudden warming and elevated stratopause conditions. Note the location of the stratopause in the Northern polar region.

Testing the parameterization for WACCM-X high-resolution temperatures 630 8

In addition to those tests above, we have also tested the parameterizations for the temperature structure obtained by a high-resolution version of the WACCM-X model (Liu et al., 2024). This version of WACCM-X has a fine grid of $0.25^{\circ} \times 0.25^{\circ}$ in latitude × longitude and a vertical resolution of 0.1 scale heights (\sim 0.5 km) in most of the middle and upper atmosphere, transitioning to 0.25 scale heights in the top three scale heights². With such a fine grid the model itself can internally generate gravity waves thus providing temperature profiles with a vertical structure very similar to that measured by high vertical resolution lidars of the mesosphere 635 and lower thermosphere. Some examples of p-T profiles of the model exhibiting those vertical features and the latitudinal and longitudinal variabilities are shown in Fig. S23 of the supplement. Further, the model spans from the surface up to nearly $600 \text{ km} (\sim 5 \cdot 10^{-10} \text{ hPa})$ which is ideal for testing the parameterization. In addition to the pressure-temperature profiles of the model, their $O({}^{3}P)$ O₂, and N₂ vmr profiles have been used. A contemporary CO₂ vmr (profile#3) was included in these calculations.

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The parameterization has been tested for a total of 225 temperature profiles. They have been selected from the model output for January conditions at four latitudes: 20°N, 40°N, 60°N, and 70°N of the Northern (winter) hemisphere and two additional latitudes, 60°S, and 70°S of the Southern (summer) hemisphere. For each latitude, 36 profiles corresponding to longitudes from 0° to 360° every 10° were selected. A few p-T profiles are shown in the left column of Fig. 16, and all the profiles for latitudes

²We recall that the Δx grid of the parameterization is 0.25.

645 20°N, 60°N, 70°N and 70°S are shown in Fig. S23 in the supplement. We should note that those temperature structures very much resemble those measured by lidar instruments.

The results for a few representative p-T profiles are shown in Fig. 16. A few more examples are shown in Figs. S24-S26 in the supplement. In general, the results are very similar to those obtained for the MIPAS temperatures. The parameterization works very well below $\sim 5 \cdot 10^{-3}$ hPa (~ 85 km), with differences generally smaller than 1–2 K day⁻¹. In the upper regions,

- 650 above $\sim 2 \cdot 10^{-4}$ hPa (~ 105 km, not fully shown in Fig. 16 because of the small scale chosen to highlight the differences in the region of larger differences) it also works very well. In this region, the cooling rate differences are slightly larger than near the $\sim 5 \cdot 10^{-3}$ hPa (~ 85 km), generally below 5 K day⁻¹, but they are much smaller in relative terms since the cooling rates at high altitudes are very large (in the order of 100–300 K day⁻¹). In the intermediate region, between $\sim 5 \cdot 10^{-3}$ hPa and $\sim 2 \cdot 10^{-4}$ hPa, the algorithm still reproduces the reference calculations rather well but not as well as in the other regions. The cooling rate
- 655 differences can reach up to $10 \text{ K} \text{ day}^{-1}$ in a few isolated levels of some individual profiles which can represent up to about 20%. It is noticeable though that while the differences can be significant, the profile shape of the reference and parameterised calculations are very similar (see middle panels in Fig. 16).

To have a global perspective, we have plotted in Fig. 17 the mean of the differences for all the p-T profiles together with their RMS (root-mean-square). We see that the mean (bias) of the parameterization is very small, practically below 1.5 K day⁻¹ anywhere and below 0.5 K day⁻¹ for most of the atmospheric layers. The RMS, a representative error of individual profiles, is also small at levels below $\sim 2 \cdot 10^{-2}$ hPa (~ 80 km) with values of 1–2 K day⁻¹ ($\sim 20\%$) and above 10^{-4} hPa (~ 105 km), with values smaller than 4 K day⁻¹ ($\sim 2\%$). In the intermediate region, between $\sim 5 \cdot 10^{-3}$ hPa and $\sim 2 \cdot 10^{-4}$ hPa, the RMS however is significant, with most values in the range of 5–12 K day⁻¹. While these values are significant in percentage at $\sim 5 \cdot 10^{-3} - 5 \cdot 10^{-4}$ hPa, they are very small above $\sim 5 \cdot 10^{-4}$ hPa.

665 9 Discussion: The use of this parameterization with a previous CO₂ solar NIR heating rates parameterization

Some of the GCM models use the parameterization of the CO_2 15 μ m cooling together with that of the CO_2 near-infrared (NIR) heating of Ogibalov and Fomichev (2003). Hence, as we are updating the former for larger CO_2 abundances, and the update on the NIR heating parameterization for the large CO_2 abundances is out of the scope of this work, we investigate if the latter is still valid for the large CO_2 abundances. For that purpose, we compute CO_2 NIR heating rates with the parameterization of

- 670 Ogibalov and Fomichev (2003) and with the GRANADA model for the large CO_2 concentrations for the six p-T reference atmospheres. We should note that the non-LTE models used in both parameterizations are different and hence we expect some difference not just caused by the parameterization itself but by the differences between the underlying non-LTE model in the NIR heating parameterization and GRANADA. The CO_2 NIR heating rates of GRANADA were calculated with the rate coefficients and photolysis rates described in Funke et al. (2012) but updated with those described in Jurado-Navarro et al.
- 675 (2015, 2016) and also with those described below. In particular, the J_{O3} rate used in these calculations is ~10% smaller than in Jurado-Navarro et al. (2015) below 100 km, and thus leads to an $[O(^1D)]$ of ~10% smaller below 90 km, but is very similar near 100 km. Above ~100 km, the J_{O2} coefficient used in the present calculations is about 40% smaller, than in Jurado-Navarro



Figure 16. As FigComparison of cooling rates of the parameterization and the reference calculations for high-resolution WACCM-X temperature profiles. 12 but The left column shows the panels for the MIPAS temperatures taken on 15 February 2009 when a major elevated stratopause event occurred pressure temperature profiles, with two profiles (black and red) in each panel. The middle column shows the reference cooling rates (solid) and the cooling rate from the parameterization (dotted) for the corresponding p-T profiles. The right column shows the differences of the parameterized cooling and the generate calculation. The different rows are results for p-T profiles at different latitudes.



Figure 17. Mean (left) and RMS (right) of the differences in the cooling rates of the old-parameterization (in blue) and the new one (red) with respect to the LBL accurate reference cooling rates obtained for MIPAS temperatures for 15 February 2009 considering only latitudes northernmost of 50° Nthe WACCM-X high-resolution temperature profiles.



Figure 18. Solar NIR heating rates for the tropical atmosphere and a SZA of 44.5° computed by the solar NIR heating parameterization of Ogibalov and Fomichev (2003) and those obtained in the updated GRANADA model (see text). The right panel shows the differences in the heating rates of the parameterization minus those computed in GRANADA.

et al. (2015), leading to a similar reduction in $[O(^1D)]$. Further, we updated the following collisional rates. The rate coefficient of N₂ + O(¹D) \rightarrow N₂(1) + O, has been increased by a factor of 1.08, and the collisional deactivation of N₂(1) with atomic oxygen (which has an important role in the heating rates, see, e.g. López-Puertas et al., 1990), has been updated from a value of 4.5 × 10⁻¹⁵ (T/300)^{1.5} cm³s⁻¹ to 4.3 × 10⁻¹⁵ (T/300)^{2.9} cm³s⁻¹.

The results of the comparison are shown in Fig. 18 for the tropical atmosphere and an intermediate solar zenith angle (SZA) of 44.5°. The region of most importance for the CO₂ NIR heating rates is that comprised between 0.1 and 0.01 hPa (Fomichev et al., 2004). In this region, the differences between the algorithm of Ogibalov and Fomichev (2003) and GRANADA are in the range of $+0.2 \text{ K/day-K} \text{ day}^{-1}$ to $-0.5 \text{ K/day-K} \text{ day}^{-1}$ for CO₂ vmrs up to five times the pre-industrial CO₂ profile, e.g., about 10 to 15%. Hence, given that they have been computed with very different non-LTE models and the significant effect that

parameters like the CO₂ vmr above ~ 90 km, the collisional rate between N₂(1) and O(${}^{3}P$), the O(${}^{3}P$) concentration itself, and the rate of exchange of CO₂ v_3 quanta with N₂(1) have on these solar heating (see, e.g. López-Puertas et al., 1990), these differences are reasonable. Hence the new CO₂ cooling rate parameterization reported here can be safely used together with the CO₂ solar NIR heating parameterization of Ogibalov and Fomichev (2003) for CO₂ vmrs up to five times the preindustrial

 CO_2 profile.

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10 Summary and Conclusions

An improved and extended parameterization of the CO₂ 15 μm cooling rates of the Earth's middle/upper atmosphere has been developed. It follows essentially the same method of the parameterization of Fomichev et al. (1998). The major novelty is
its extended range of CO₂ abundances, ranging from CO₂ profiles with tropospheric values close to half of the pre-industrial

- value to ten times that value. This extension of CO_2 profiles can still be safely applied to the parameterization of the CO_2 nearinfrared heating of Ogibalov and Fomichev (2003) up to at least five times the pre-industrial CO_2 values, which is normally combined with this cooling rates parameterization.
- Other improvements or updates are as follows. It has an extended and finer vertical grid, increasing the number of levels from eight to 83. The CO₂ line list has been updated, from HITRAN 1992 to HITRAN 2016. Although the collisional rate coefficients affecting the CO₂ v_1 and v_2 levels are input parameters for the parameterization, in this version we have used more contemporary collisional ratesvalues, e.g., as currently used in the non-LTE retrieval of temperature from CO₂ 15 μ m emissions of SABER and MIPAS measurements (García-Comas et al., 2008; García-Comas et al., 2023). The rate coefficients are in general of very similar magnitude, except for the collisional deactivation of CO₂(v_1 , v_2) levels by atomic oxygen, which
- is now larger by <u>approximately</u> a factor of approximately two, e.g. close to its upper accepted accepted upper limit. As a consequence of the larger range of CO₂ vmr profiles, the different NLTE layers for computing the cooling rates have been significantly revised. For example, it is worth mentioning that the lowermost altitude of the cooling-to-space approximation (the uppermost NLTE layer) has risen from \sim 110 km up to 160–170 km.

The new parameterization has been thoroughly tested against line-by-line LTE and non-LTE cooling rates for: (i) the six p-T reference atmospheres; (ii) the two most important input parameters (aside temperature), the CO₂ ymr profiles and the

collisional rate of $CO_2(v_1, v_2)$ by atomic oxygen; and (iii) for realistic measured temperature fields of the middle atmosphere (about 5000–2500 profiles), including an episode of strong stratospheric warming with elevated stratopausea very elevated stratopause; and iv) for the temperature profiles (225 profiles) obtained by a high-resolution version of WACCM-X, capable of generating internally gravity waves and hence with temperatures showing a large variability and pronounced vertical wave

715 <u>structures</u>. Further, to illustrate the improvements, <u>such comparisons the comparisons of points (i) to (iii)</u> have also been performed for the previous parameterization.

For the reference pressure-temperatures temperatures profiles, the errors of the new parameterization (mean of the differences in the cooling rates with respect to line-by-line reference calculations for the six p-T atmospheres), are below 0.5 K day⁻¹ for the current and lower CO₂ vmrs. For higher CO₂ concentrations, between about two and three times the preindustrial values, the largest errors are ~1–2 K day⁻¹, and are located near 100–120110–120 km. For the very high CO₂ concentrations

- values, the largest errors are $\sim 1-2$ K day⁻¹, and are located near 100-120110-120 km. For the very high CO₂ concentrations (from four to ten times the pre-industrial abundances) the errors are also very small, below ~ 1 K day⁻¹, for most regions and conditions; except in the 110-120107-135 km region where the parameterization overestimates them in a few K day⁻¹, $\sim 1.512\%$. For these reference atmospheres, the new parameterization has a better performance for most of the atmospheric layers and temperature structures.
- From the testing of the parameterization for realistic current temperature fields of the middle atmosphere as measured by MIPAS, we found that, in general, the new parameterization is slightly more accurate. In particular, in the 105–115 km range, the previous parameterization overestimates the cooling rate by 1.5 K day^{-1} , while the new one is very accurate. However, in the other height regions the difference is not so dramaticimportant. The new parameterization has a better performance in the 80–95 km altitude region. Overall, the errors in the global-mean profiles (about 1000 profiles bias) of the cooling rates of
- 730 the new parameterization, calculated for four different atmospheric conditions with about 500 profiles in each of them, are below 0.5 K day^{-1} , except between $5 \cdot 10^{-3} \text{ hPa}$ and $3 \cdot 10^{-4} \text{ hPa}$ (~85–95 km), where they can reach biases of $1-2 \text{ K day}^{-1}$. That region is the most challenging to parameterize because several CO₂ 15 μ m bands contribute to the cooling rate and they depend very much on the temperature structure of the whole middle atmosphere (e.g., even outside this region).
- For single-temperature profiles, the cooling rate error (characterised by the RMS of the difference between the reference and the parameterized cooling rates) is about $1-2 \text{ K} \text{ day}^{-1}$ below $5 \cdot 10^{-3} \text{ hPa}$ (~85 km) and above $2 \cdot 10^{-4} \text{ hPa}$ (~100 km). In the intermediate region, however, it is significant, between 2 and 7 K day⁻¹. We have further tested the parameterization against very rare and demanding situations, such as the temperature structures of stratospheric warming events with elevated stratopause. In these situations, however, the parameterization underestimates the cooling rates by 3–7 K day⁻¹ (~10%) at altitudes of 80–100 km, and the individual cooling rates show a significant RMS (5–15 K day⁻¹).
- 740 This parameterization has In addition, we have also tested the parameterization for the temperature structure obtained by a high-resolution version of WACCM-X, with temperatures showing a large variability and pronounced vertical wave structure. The mean (bias) error of the parameterization is very small, smaller than 0.5 K day⁻¹ for most atmospheric layers, and below 1.5 K day⁻¹ for almost any altitude from the surface up to 200 km. The RMS of the differences in the cooling rates from the parameterization and the reference model is similar to that obtained for MIPAS temperatures, with values of 1–2 K day⁻¹ (~20%) below ~2·10⁻² hPa (~80 km), and smaller than 4 K day⁻¹ (~2%) above 10⁻⁴ hPa (~105 km). In the
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intermediate region, between $\sim 5 \cdot 10^{-3}$ hPa and $\sim 2 \cdot 10^{-4}$ hPa, they are slightly larger than for MIPAS with values in the range of 5–12 K day⁻¹. These values, while they are significant in relative terms at $\sim 5 \cdot 10^{-3} - 5 \cdot 10^{-4}$ hPa, they are very small in percentage above $\sim 5 \cdot 10^{-4}$ hPa.

As has been shown, this parameterization has some limitations (see Secs. 6and 7.2). To, 7.2 and 8). In order to be able to

- apply specific approximations for the cooling rates, it has been designed for fixed atmospheric regions where specific radiative transfer regimes prevail. Thus, its extension to a very large range of CO_2 abundances inevitably causes a loss of accuracy for extreme cases at specific atmospheric layers. A possible solution for future updates could be to use different extensions of the non-LTE regions (i.e. Fig. 7) for different abundances of CO_2 . Likewise, this parameterization (like the original one) was devised for being used in GCMGCMs, that is to produce accurate global cooling rates , cooling rates globally e.g., for when
- 755 considering all expected temperature profiles covering the different latitudinal and seasonal conditions. Thus, the ability of the parameterization for computing accurate cooling rates for specific and very different temperature gradients of the middle atmosphere is limited. The most critical region is between individual temperature profiles with large temperature gradients in the $5 \cdot 10^{-3}$ hPa and (~85 km) to $3 \cdot 10^{-4}$ hPa (~85–9595 km). From the comparison for realistic measurements we have found that, although the mean cooling rates are accurate, the standard deviation of the parameterized cooling rates is large
- 760 (~6region is limited. On the contrary, it is extremely fast. The routine takes only 15) in that region. As another example, see See: *µs* of CPU time for calculating a profile in the range of 50 7.2, we have shown that the parameterization underestimates the cooling rates in that atmospheric region (and the standard deviation is even larger) for elevated stratopause events. One may think that this is caused because such extreme temperature profiles were not considered in the reference atmospheres. But, if so, the degree of improving the accuracy would depend on the chosen weighting factors for each reference atmosphere.
- 765 Thus, its inclusion might give more accurate cooling rates for elevated stratopause episodes but would worsen the accuracy for other general situations. km to 270 km in a machine with an Intel Core i7 4.2 GHz processor if compiled with ifort. This is more than 6600 times faster than the best option of the NLTE15μmCool-E v1.0 routine recently reported by Kutepov and Feofilov (2023). To conclude, parameterizations overcoming those limitations but retaining the goodness of this approach that speed are highly desirable to be developed in the future.
- 770 *Code availability.* The code is available at https://zenodo.org/doi/10.5281/zenodo.10849969. The parameterization is also available as a Python routine for calculating cooling rates for specific purposes at https://zenodo.org/doi/10.5281/zenodo.10547026. Note that the Python version is much slower than the Fortran version and it is not recommended for use in GCMs.

Appendix A: Notes and recommendations for using the parameterization

Appendix B: , and abundances

The routine source code is written in Fortran 90 and is available at https://zenodo.org/doi/10.5281/zenodo.10849969. It has been devised for being implemented in General Circulation Models although it can also be used for other purposes, e.g., to compute the CO_2 15 μ m cooling rate for a given reference atmosphere. The code is organized in a library (in directory source/modules/) that can be included in a more complex GCM model. The subroutine to be called is CO2_NLTE_COOL, inside module file co2cool.f90.

- 780 (top), (middle) and (bottom) volume mixing ratio profiles for the respective atmospheric conditions used in the references calculations. The following inputs are required (in order) by CO2_NLTE_COOL:
 - Atmospheric profiles as a function of pressure for temperature and four VMRs of CO₂, O, O₂, and N₂.
 - 1ev0: the index of the given pressures so that p(1ev0) is the maximum pressure level (lower boundary) to be considered for calculating the heating rate. Heating rates will be calculated from that pressure up to the minimum pressure specified in the pressure array. E.g., if p is given in the range of 10^3 hPa to 10^{-6} hPa (or 10^{-6} hPa to 10^3 hPa)
 - and p(1ev0) = 1 hPa, the heating rate will be calculated in the range of 1 hPa to 10^{-6} hPa.
 - surf_temp: surface temperature (if set to a negative value, the temperature of the maximum pressure level will be used).
 - hr: heating rate. This is an input/out array with the same dimension of pressure. It will be calculated only at pressures in
 - the range of p(lev0) (max. pressure considered) to the minimum specified pressure (minimum(pressure)). Note that we have used thoroughly this paper the term "cooling rates", e.g., the hr values with changed sign.

Appendix B: LTE cooling rates for the reference atmospheres

- Units are: temperature in K, pressure in hPa, vmrs in mol/mol (not ppm), heating rate in K day⁻¹.
- Input profiles can run either from ground to top of the atmosphere (decreasing pressures) or reverse (top to ground with increasing pressures). The pressure grid can be irregular.
- Important notes:

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calculations in the LTE region. 1) Pressure levels should include the surface pressure (near 10^3 hPa), even if the 15 μ m cooling is to be calculated only at lower pressure levels (higher altitudes), i.e., p (lev0) $\leq 10^3$ hPa.

2) If $15 \,\mu m$ cooling shall be calculated only in the non-LTE regime, it is recommended to set up the lower boundary,

800 p (lev0), close to the limit of the LTE/non-LTE transition, e.g. near 1 hPa. In this way, more time-consuming calculations in the LTE region will be avoided.

The LTE cooling rates for the reference atmospheres shown up to the lower thermosphere. Note the different x-scales. The cooling rates extended up to the thermosphere are shown in Fig. S4 below.

The LTE cooling rates for the reference atmospheres. As in Fig. S3 but covering the thermosphere. The output is expressed 805 as the heating rate in units of K day⁻¹ on the given input grid in the range of p(lev0) to the minimum specified pressure.

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Appendix B: Non-LTE cooling rates for the reference atmospheres for the entire altitude range.

To compile the routine follow these steps:

- Edit the Makefile and change the Fortran compiler to your preferred choice (e.g., gfortran, ifort, etc.),

- From this folder, run make.

810 Non-LTE cooling rates for the reference atmospheres covering the thermosphere. Those for the lower altitudes are shown above in Fig. 3. The cooling rates for the volume mixing ratio profiles used to test the parameterization are also shown (dashed lines). The compilation produces a test program run_cool (see below) and a module library file lib/libco2_cool.a.

Appendix B: Non-LTE-LTE cooling rate differences.

A test program, source/main.f90, is also provided to test the parameterization on individual profiles. Its input file 815 input.dat has a fixed format. Do not change the number of commented lines!

- First input at line 9: n_lev, lev0, T_surf.

- Starting from line 12:

- 6 atmospheric profiles are read (n_lev rows are expected).

The output heating rates are written in the output.dat file.

820 Non-LTE-LTE cooling rates differences for the six p-T references atmospheres (as in Fig. 5) but for the vmr profile #6 (4× the pre-industrial values). The '*' symbol indicates the pressure level (in hPa) where the non-LTE-LTE difference reaches 5%. Note the different x-scales.

Non-LTE-LTE cooling rates differences for the six-references atmospheres and the vmr profile #3 (as in Fig. 5) but including the thermosphere.

825 Appendix B: The column amounts.

To test main.f90, two input/output files are provided: input_test.dat and input_test2.dat with their corresponding output_test.dat and output_test2.dat output files. The first computes the heating in the full pressure range provided; the second only at pressures smaller than ~1 hPa. To test the routine follow these steps:

The column amount u as a function of altitude z for several and the current vmr profile, #3 (left), and for the eight vmr profiles
considered and the mid-latitude equinox (MLE) profile. They have been used in the representation of the escape probability

function L(u) in Fig. S7. _ cp input_test.dat input.dat

_./run_cool

- Check that the results in output.dat are consistent with output_test.dat

- The same procedure can be done for test2.

835 Appendix B: Cooling rate differences of the current and previous parameterizations with respect to accurate cooling rates for the reference atmospheres

We show in this section a comparison of the cooling rates of the current and previous parameterizations with respect to accurate cooling rates. The routine is supplied with the collisional rates described in this paper (see Table 1). Nevertheless, they can be changed by the user. They are prescribed in the constants.f90 module. - The rates are defined in the form $z = a\sqrt{T} + b \exp(-qT^{-1/3})$.

The coefficients are specified as follows:

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- for CO₂-O: a_zo, b_zo, g_zo (default: $3.5 \times 10^{-13}, 2.32 \times 10^{-9}, 76.75$)

- for CO₂-O₂: a_zo2, b_zo2, g_zo2 (default: 7.0×10⁻¹⁷, 1.0×10⁻⁹, 83.8)

- for several-CO₂vmr profiles for the six *p*-*T* reference atmospheres.Note that similar figures $-N_2$: a_zn2, b_zn2, g_zn2 (default: 7.0×10⁻¹⁷, 6.7×10⁻¹⁰, 83.8).

The most likely rate to be changed is k_0 , probably by using smaller values. We tested a collisional k_0 rate two times smaller than used in the development of the parameterization and found that its accuracy did not change significantly (see Sec. 6.2).

Although the parameterisation is specifically developed for the CO₂ vmr profile #3 are shown in the main text (Fig. 15 $\$\mu$ m non-LTE region, it also works for the LTE region, but the user should be cautious that other important cooling rates in the LTE

region, such as those of O_3 and H_2O , are not included. We recommend that the GCM users utilise their radiation scheme in the LTE region and this parameterization in the non-LTE region (e.g., above ~ 50 or 60 km).

Comparison of the cooling rates of the current and previous parameterizations with respect to accurate cooling rates for the vmr profile #1 for the six *p*-*T* reference atmospheres. Boundaries of the parameterization. About the lower boundary (maximum pressure) see notes above. About the upper boundary (minimum pressure), there is in principle no limitation but

- 855 we recommend setting it up as high as the upper lid of your model. There is a large number of GC and CC models with upper lid at $\sim 10^{-2}$ hPa (or ~ 80 km). This parameterization can be used for such models to compute the CO₂ non-LTE cooling rates between ~ 50 km and ~ 80 km. We note that under these circumstances, the cooling rates near the upper lid might not be accurate, as the contribution of the layers above the upper lid is not considered. This, however, is not a limitation of the parameterization itself, but an intrinsic limitation of this kind of models. There is no restriction either about the upper limit of
- 860 the upper boundary, provided it is physically meaningful. That is, it can be placed at altitudes as high as 500 km or higher. Comparison of the cooling rates of the current and previous parameterizations with respect to accurate cooling rates for the vmr profile #2 for the six *p*-*T* reference atmospheres.

Comparison of the cooling rates of the current and previous parameterizations with respect to accurate cooling rates for the vmr profile #4 for the six p-T reference atmospheres.

865 Appendix B: Additional figures



Comparison of the cooling rates of the current parameterization with respect to accurate cooling rates for the vmr profile #5 for the six p.T reference atmospheres. The results of the previous parameterization are not shown because this profile is beyond its applicability limits.

Figure B1. Contributions of the different CO_2 bands to the cooling rates for the MLE p-T atmosphere. That is, as the left panel of Fig. 4 but for the entire altitude range.



Figure B2. Comparison—Altitude (left panel) and pressure level (right panel) of the cooling rates deviation (\geq 5%) of the current parameterization with respect to accurate non-LTE cooling rates from LTE values for the vmr profile #6 for the six p-T reference references atmospheres . The results of and the previous parameterization are not shown because this eight CO₂ profile is beyond its applicability limits vmr profiles (see Fig. 1b): #1, half of pre-industrial; #2 pre-industrial; #3, present day; #4, ~2×pre-industrial); #5, ~3×pre-industrial; #6, ~4×pre-industrial; #7, ~5×pre-industrial; and #8, ~10×pre-industrial.



Figure B3. Comparison of the <u>Non-LTE-LTE</u> cooling rates of the current parameterization with respect to accurate cooling rates differences for the six p-T references atmospheres and the present day CO₂ vmr profile #7 for the six p-T reference atmospheres3 (as in Fig. The results of 5) but including the previous parameterization are not shown because this profile is beyond its applicability limits thermosphere.



Figure B4. Comparison of the cooling rates of the current parameterization and previous parameterizations with respect to accurate cooling rates for the intermediate CO₂ vmr profile #8 for 9 (see Fig. 1b) and the six p-T-p-T reference atmospheres. The results of the previous parameterization are not shown because this profile is beyond its applicability limits.





As Fig. B4 but Comparison of the cooling rates of the current and previous parameterizations with respect to the reference cooling rates for the higher intermediate present day CO₂ vmr abundance (profile #11 (3, see Fig. ??1b). Note that and the results of six p-T reference atmospheres when reducing the previous parameterization are not shown as the profile used here is beyond its applicability limits nominal collisional rate in Table 1 by a factor of two.

Figure B5. As Fig. B4 but for Testing the higher intermediate effect of the CO_2 vmr profile #10 (see Fig. ?? v_2)-O(³P) collisional rate on the parameterization.

As Fig. B4 but Comparison of the cooling rates of the current and previous parameterizations with respect to the reference cooling rates for the higher intermediate present day CO₂ vmr abundance (profile #11 (3, see Fig. ??1b). Note that and the results of six p-T reference atmospheres when reducing the previous parameterization are not shown as the profile used here is beyond its applicability limits nominal collisional rate in Table 1 by a factor of two. 45

Appendix C: Quantities used in the calculation of the accurate and parameterized cooling rates for the MIPAS temperatures

We show in this appendix the vmr and abundances used in the calculations of the accurate and parameterized cooling rates. The LBL accurate cooling rates are also shown.



Figure B1. Zonal mean An example of the MIPAS nighttime vmrs temperature profiles (15 February 2009) used in for verifying the calculation parameterization accuracy. Note the large variability of the cooling rates temperature profiles.



Figure B2. Zonal MIPAS zonal mean nighttime <u>vmr used in the calculation of the cooling rates</u>temperatures for 14 January 2010 (Northern winter hemisphere, top/left), 25 March 2010 (Northern spring hemisphere, top/right), 13 June 2010 (Northern summer hemisphere, bottom/left) and 21 September 2010 (Northern fall hemisphere, bottom/right).



Figure B3. Zonal mean <u>LBL accurate of the differences in the cooling rates of the old parameterization (left column) and the new one (right column) with respect to the reference cooling rates obtained for the MIPAS nighttime temperature fields considered in this work temperatures for 13 June 2010 (Northern summer hemisphere) and 21 September 2010 (Northern fall hemisphere).</u>



Figure B4. Zonal The MIPAS nighttime temperature zonal mean of the vmr for 15 February 2009 (topsee also Fig. B1), abundance (middle) and the LBL accurate cooling rates (bottom) used for verifying the parameterization accuracy under stratospheric sudden warming and elevated stratopause conditions (15 February 2009). Note the high altitude location of the stratopause in the Northern polar region.

- 870 *Author contributions.* MLP performed the LTE and non-LTE reference calculations, participate in the adaptation of the original parametarization, wrote the manuscript and had the final editorial responsibility for this paper. FF led (together with BF) the adaptation of the original parametarization of Fomichev et al (1998), wrote the code of the new parameterization, performed all the tests of the parameterization and calculated the cooling rates of the previous and new parameterizations presented here. VF made a critical contribution for the adaptation of its original algorithm and to its update. BF co-led the adaptation of the original parametarization and designed the accuracy tests. DM
- 875 provides the CO2 abundances and advise on the development of the parameterization for its use and implementation in climate models. All the authors contributed to the discussions, and provided text and comments.

Competing interests. The authors declare that they have no conflict of interest.

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References

885

- Dudhia, A.: The Reference Forward Model (RFM), Journal of Quantitative Spectroscopy and Radiative Transfer, 186, 243 – 253, ISSN 0022-4073, https://doi.org/http://dx.doi.org/10.1016/j.jqsrt.2016.06.018, http://www.sciencedirect.com/science/article/pii/ S0022407316301029, satellite Remote Sensing and Spectroscopy: Joint ACE-Odin Meeting, October 2015, 2017.
- Emmert, J. T., Drob, D. P., Picone, J. M., Siskind, D. E., Jones, M., Mlynczak, M. G., Bernath, P. F., Chu, X., Doornbos, E., Funke, B., Goncharenko, L. P., Hervig, M. E., Schwartz, M. J., Sheese, P. E., Vargas, F., Williams, B. P., and Yuan, T.: NRLMSIS 2.0: A Whole-Atmosphere Empirical Model of Temperature and Neutral Species Densities, Earth and Space Science, 8, e2020EA001 321, ISSN 2333-5084, https://doi.org/10.1029/2020EA001321, 2021.
- 890 Feofilov, A. and Kutepov, A.: Infrared Radiation in the Mesosphere and Lower Thermosphere: Energetic Effects and Remote Sensing, Surveys in Geophysics, 33, 1231–1280, https://doi.org/10.1007/s10712-012-9204-0, 2012.
- Fischer, H., Birk, M., Blom, C., Carli, B., Carlotti, M., von Clarmann, T., Delbouille, L., Dudhia, A., Ehhalt, D., Endemann, M., Flaud, J. M., Gessner, R., Kleinert, A., Koopmann, R., Langen, J., López-Puertas, M., Mosner, P., Nett, H., Oelhaf, H., Perron, G., Remedios, J., Ridolfi, M., Stiller, G., and Zander, R.: MIPAS: an instrument for atmospheric and climate research, Atmos. Chem. Phys., 8, 2151–2188, 2008.
 - Fomichev, V. I., Ogibalov, V. P., and Beagley, S. R.: Solar Heating by the Near-IR CO2 Bands in the Mesosphere, Geophysical Research Letters, 31, ISSN 1944-8007, https://doi.org/10.1029/2004GL020324, 2004.
 - Fomichev, V. L., Blanchet, J.-P., and Turner, D. S.: Matrix parameterization of the 15 μm CO₂ band cooling in the middle and upper atmosphere for variable CO₂ concentration, J. Geophys. Res., 103, 11505–11528, ISSN 0148-0227, 1998.
- 900 Funke, B., López-Puertas, M., García-Comas, M., Kaufmann, M., Höpfner, M., and Stiller, G. P.: GRANADA: a Generic RAdiative traNsfer AnD non-LTE population Algorithm, J. Quant. Spectrosc. Radiat. Transfer, 113, 1771–1817, https://doi.org/10.1016/j.jqsrt.2012.05.001, 2012.
- Garcia, R., Smith, A., Kinnison, D., de la Camara, A., and Murphy, D.: Modification of the gravity wave parameterization in the Whole Atmosphere Community Climate Model: Motivation and results, Journal of the Atmospheric Sciences, 74, 275–291, https://doi.org/10.1175/JAS-D-16-0104.1, 2017.
- García-Comas, M., López-Puertas, M., Marshall, B., Wintersteiner, P. P., Funke, B., Bermejo-Pantaléon, D., Mertens, C. J., Remsberg, E. E., Gordley, L. L., Mlynczak, M., and Russell, J.: Errors in SABER kinetic temperature caused by non-LTE model parameters, J. Geophys. Res., 113, D24106, https://doi.org/10.1029/2008JD010105, 2008.
- García-Comas, M., Funke, B., López-Puertas, M., Bermejo-Pantaleón, D., Glatthor, N., Clarmann, T. v., Stiller, G. P., Grabowski, U., Boone,
 C. D., French, W. J., Leblanc, T., López-González, M. J., and Schwartz, M.: On the Quality of MIPAS Kinetic Temperature in the Middle Atmosphere, Atmos. Chem. Phys., 12, 6009–6039, https://doi.org/10.5194/acp-12-6009-2012, 2012.
 - García-Comas, M., Funke, B., López-Puertas, M., Glatthor, N., Grabowski, U., Kellmann, S., Kiefer, M., Linden, A., Martínez-Mondéjar, B., Stiller, G. P., and von Clarmann, T.: Version 8 IMK/IAA MIPAS temperatures from 12–15 μm spectra: Middle and Upper Atmosphere modes, Atmos. Meas. Tech., submitted, 2023.
- 915 Gilli, G., Lebonnois, S., González-Galindo, F., López-Valverde, M. A., Stolzenbach, A., Lefèvre, F., Chaufray, J. Y., and Lott, F.: Thermal Structure of the Upper Atmosphere of Venus Simulated by a Ground-to-Thermosphere GCM, Icarus, 281, 55–72, ISSN 0019-1035, https://doi.org/10.1016/j.icarus.2016.09.016, 2017.
- Gilli, G., Navarro, T., Lebonnois, S., Quirino, D., Silva, V., Stolzenbach, A., Lefèvre, F., and Schubert, G.: Venus Upper Atmosphere Revealed by a GCM: II. Model Validation with Temperature and Density Measurements, Icarus, 366, 114432, ISSN 00191035, https://doi.org/10.1016/j.icarus.2021.114432, 2021.
- Gordon, I. E., Rothman, L. S., Hill, C., Kochanov, R. V., Tan, Y., Bernath, P. F., Birk, M., Boudon, V., Campargue, A., Chance, K. V., Drouin, B. J., Flaud, J. M., Gamache, R. R., Hodges, J. T., Jacquemart, D., Perevalov, V. I., Perrin, A., Shine, K. P., Smith, M. A. H., Tennyson, J., Toon, G. C., Tran, H., Tyuterev, V. G., Barbe, A., Császár, A. G., Devi, V. M., Furtenbacher, T., Harrison, J. J., Hartmann, J. M., Jolly, A., Johnson, T. J., Karman, T., Kleiner, I., Kyuberis, A. A., Loos, J., Lyulin, O. M., Massie, S. T., Mikhailenko, S. N., Moazzen-Ahmadi, N.,
- 925 Müller, H. S. P., Naumenko, O. V., Nikitin, A. V., Polyansky, O. L., Rey, M., Rotger, M., Sharpe, S. W., Sung, K., Starikova, E., Tashkun, S. A., Auwera, J. V., Wagner, G., Wilzewski, J., Wcisło, P., Yu, S., and Zak, E. J.: The HITRAN2016 molecular spectroscopic database, Satellite Remote Sensing and Spectroscopy: Joint ACE-Odin Meeting, October 2015, 203, 3–69, 2017.
- Hartogh, P., Medvedev, A. S., Kuroda, T., Saito, R., Villanueva, G., Feofilov, A. G., Kutepov, A. A., and Berger, U.: Description and Climatology of a New General Circulation Model of the Martian Atmosphere, Journal of Geophysical Research: Planets, 110, ISSN 2156-2202, https://doi.org/10.1029/2005JE002498, 2005.
- Jurado-Navarro, A. A., López-Puertas, M., Funke, B., García-Comas, M., Gardini, A., Stiller, G. P., and von Clarmann, T.: Vibration-vibration and vibration-thermal energy transfers of CO₂ with N₂ from MIPAS high resolution limb spectra, Journal of Geophysical Research, p. 2015JD023429, 2015.

Jurado-Navarro, A. A., López-Puertas, M., Funke, B., Garcia-Comas, M., Gardini, A., González-Galindo, F., Stiller, G. P., Clarmann, T. V.,

- 935 Grabowski, U., and Linden, A.: Global distributions of CO2 volume mixing ratio in the middle and upper atmosphere from daytime MIPAS high-resolution spectra, Atmospheric Measurement Techniques, 9, 6081–6100, https://doi.org/10.5194/amt-9-6081-2016, 2016. Kutepov, A. and Feofilov, A.: New Routine NLTE15µmCool-E v1.0 for Calculating the Non-LTE CO 2 15 Mm Cooling in GCMs of Earth's
 - Atmosphere, Preprint, Solar-terrestrial science, https://doi.org/10.5194/gmd-2023-115, 2023.
- Kutepov, A. A. and Fomichev, V. I.: Application of the Second-Order Escape Probability Approximation to the Solution of the NLTE
 Vibration-Rotational Band Radiative Transfer Problem, Journal of Atmospheric and Terrestrial Physics, 55, 1–6, 1993.
- Kutepov, A. A., Feofilov, A. G., Medvedev, A. S., Berger, U., Kaufmann, M., and Pauldrach, A. W. A.: Infra-Red Radiative Cooling/Heating of the Mesosphere and Lower Thermosphere Due to the Small-Scale Temperature Fluctuations Associated with Gravity Waves, in: Climate and Weather of the Sun-Earth System (CAWSES), edited by Lübken, F.-J., pp. 429–442, Springer Netherlands, Dordrecht, ISBN 978-94-007-4347-2 978-94-007-4348-9, https://doi.org/10.1007/978-94-007-4348-9_23, 2013.
- 945 Liu, H.-L., Lauritzen, P. H., and Vitt, F.: Impacts of Gravity Waves on the Thermospheric Circulation and Composition, Geophysical Research Letters, 51, e2023GL107453, ISSN 1944-8007, https://doi.org/10.1029/2023GL107453, 2024.
 - López-Puertas, M. and Taylor, F. W.: Non-LTE radiative transfer in the Atmosphere, World Scientific Pub., Singapore, 2001.
 - López-Puertas, M., López-Valverde, M. A., and Taylor, F. W.: Studies of Solar Heating by CO2 in the Upper Atmosphere Using a Non-LTE Model and Satellite Data, Journal of Atmospheric Sciences, 47, 809, 1990.
- 950 López-Valverde, M. A., Edwards, D. P., López-Puertas, M., and Roldán, C.: Non-Local Thermodynamic Equilibrium in General Circulation Models of the Martian Atmosphere 1. Effects of the Local Thermodynamic Equilibrium Approximation on Thermal Cooling and Solar Heating, Journal of Geophysical Research, 103, 16799–16812, https://doi.org/10.1029/98JE01601, 1998.
 - López-Valverde, M. A., López-Puertas, M., and González-Galindo, F.: New Parameterization of CO₂ Cooling Rates at 15 μm for the EMGCM, ESA Rep. ESA Rep., ESA, 2008.
- 955 Marsh, D. R.: Chemical-Dynamical Coupling in the Mesosphere and Lower Thermosphere, in: Aeronomy of the Earth's Atmosphere and Ionosphere, vol. 2, pp. 3–17, Springer, Dordrecht, iaga special sopron book edn., 2011.
 - Marsh, D. R., Mills, M. J., Kinnison, D. E., Lamarque, J.-F., Calvo, N., and Polvani, L. M.: Climate Change from 1850 to 2005 Simulated in CESM1(WACCM), Journal of Climate, 26, 7372–7391, https://doi.org/10.1175/JCLI-D-12-00558.1, 2013.
- Meinshausen, M., Smith, S. J., Calvin, K., Daniel, J. S., Kainuma, M. L. T., Lamarque, J.-F., Matsumoto, K., Montzka, S. A., Raper, S. C. B.,
 Riahi, K., Thomson, A., Velders, G. J. M., and van Vuuren, D. P.: The RCP Greenhouse Gas Concentrations and Their Extensions from 1765 to 2300, Climatic Change, 109, 213, ISSN 1573-1480, https://doi.org/10.1007/s10584-011-0156-z, 2011.
 - Ogibalov, V. P. and Fomichev, V. I.: Parameterization of Solar Heating by the near IR CO2 Bands in the Mesosphere, Advances in Space Research, 32, 759–764, https://doi.org/doi: 10.1016/S0273-1177(03)80069-8, 2003.
- O'Neill, B. C., Tebaldi, C., van Vuuren, D. P., Eyring, V., Friedlingstein, P., Hurtt, G., Knutti, R., Kriegler, E., Lamarque, J.-F., Lowe,
- 965 J., Meehl, G. A., Moss, R., Riahi, K., and Sanderson, B. M.: The Scenario Model Intercomparison Project (ScenarioMIP) for CMIP6, Geoscientific Model Development, 9, 3461–3482, ISSN 1991-9603, https://doi.org/10.5194/gmd-9-3461-2016, 2016.
 - Stiller, G. P., von Clarmann, T., Funke, B., Glatthor, N., Hase, F., Höpfner, M., and Linden, A.: Sensitivity of trace gas abundances retrievals from infrared limb emission spectra to simplifying approximations in radiative transfer modelling, J. Quant. Spectrosc. Radiat. Transfer, 72, 249–280, 2002.
- 970 van Vuuren, D. P., Edmonds, J., Kainuma, M., Riahi, K., Thomson, A., Hibbard, K., Hurtt, G. C., Kram, T., Krey, V., Lamarque, J.-F., Masui, T., Meinshausen, M., Nakicenovic, N., Smith, S. J., and Rose, S. K.: The Representative Concentration Pathways: An Overview, Climatic Change, 109, 5–31, ISSN 0165-0009, 1573-1480, https://doi.org/10.1007/s10584-011-0148-z, 2011.