The Pareto effect in tipping social networks: from minority to majority

Jordan Everall[1], Fabian Tschofenig[24], Jonathan F. Donges[32,43], Ilona M. Otto[1]

[1]Wegener Center for Climate and Global Change, University of Graz, Austria
[2]Department of Environmental Systems Sciences, University of Graz, Austria
[32]Potsdam Institute for Climate Impact Research (PIK), Member of the Leibniz Association, Potsdam, Germany
[43]Stockholm Resilience Centre, Stockholm University, Stockholm, Sweden
[4]Department of Environmental Systems Sciences, University of Graz, Austria

Correspondence to: Jordan Everall (jordan.everall@uni-graz.at)

Abstract. How do social networks tip? A popular theory is that a small minority can affect network, or trigger population-wide change. This effect is roughly consistent with the properties of the Pareto principle, a semi-quantitative law which suggests that, in many systems, 80% of effects are produced by only 20% of the causes. In the context of the transition to net-zero emissions, this vital 20% can be a critical instigator of social tipping, a process which can rapidly accelerate the process of changing social norms. In this work, we asked whether the Pareto effect can be observed in social systems by conducting a literature review, placing a focus on social norm diffusion and complex contagion via social networks. By collecting simulation and empirical results of social tipping events from a wide range of disciplines and a large parametric space, we recognised shared behaviour across studies. By analysing the compiled dataset, we show general support for the existence of a tipping point at around 25% of the total population in susceptible social systems. Near this critical mass, a high likelihood exists for a social tipping event, where a large majority is then quickly "tipped". Our findings indicate slight variations between modelling and empirical results, with average tipping points at 24% and 27%, respectively. Additionally, we show a range of critical masses where social tipping is possible; these values lie between 10% and 43%. Finally, we also provide practical advice for facilitating norm changes under conditions of uncertainty, in difficult social norm transitions, and when social groups are resistant to change.

1 Introduction

Nonlinear dynamical systems, under which social tipping processes (social tipping) can be considered, have been studied comprehensively by both natural (Strogatz, 2019) and social scientists over the last century. Famous examples are Granovetter (1973), who showed that a select minority can alter the macro scale information flow in certain social network structures, and

Schelling (1971), who demonstrated that a slight individual racial preference can lead to completely segregated neighbourhoods. Some contemporary authors have focussed on rapid shifts in smoking behaviour (Nyborg et al., 2016) and the "critical mass phenomenon", whereby the participation of a minority (25-30%) in a collective event can engage the remaining majority (Andreoni et al., 2021; Centola et al., 2018). As recognition of the close coupling between social and physical systems characteristic of the Anthropocene has increased (Lenton, 2020; Steffen et al., 2018), so has research on social tipping processes in the context of climate and global environmental change, since these can act as mechanisms of rapid societal transformation (Constantino et al., 2022; David Tàbara et al., 2018; Lenton, 2020; Nyborg et al., 2016; Otto et al., 2020b; Westley et al., 2011). This new area of tipping scholarship is centred around deliberately bringing about social change through targeted action on tipping elements at "sensitive intervention points" (Farmer et al., 2019) or at moments of opportunity that trigger a tipping point. It is important to note that the definitions of tipping points in a Socio-Ecological Systems (SES) context are not uniform. In section 2.1 of this paper, we provide a concise summary as a guide for understanding these definitions in the context of this work.

New research in this sector can be broken down into analyses and analytical frameworks. Key examples of the former are seen in Otto et al. (2020), who identified several concrete societal tipping elements and timescales through expert elicitation, while Farmer et al. (2019) and Lenton (2020) also indicated critical points for intervention in financial, energy, resource and governance systems, to name a few. Frameworks refer more generally to processes, phases, and conceptualisations of "radical" socioecological transitions (Feola, 2015). More recent work (Winkelmann et al., 2020) proposed a framework that includes a more detailed description of social tipping mechanisms and explicitly incorporated critical elements such as social network properties (e.g. polarisation, clustering, and modularity), agency, temporospatial scales, and dynamics like social contagion and network adaptation. Much of this work emphasises the existence or identification of social tipping points, the need to trigger them, and their value in the sustainability transition. Many theories specific to modelling social tipping in social-environmental systems as opposed to general social systems have been proposed (Lade et al., 2017; Müller-Hansen et al., 2017; Schwarz et al., 2020; Schwarz and Ernst, 2009), and a body (Andersson et al., 2020; Frei et al., 2023; Geier et al., 2019; Schleussner et al., 2016; Schunck et al., 2021) of recent empirical work in the fields of statistical physics, network science, and computational social science also acknowledges their applications to the SES transformation.

One theme critically discussed in recent literature is the prediction of social tipping points, and whether social tipping is possible at large scales in complex social-ecological systems (Bentley et al., 2014). It is largely understood that any general tipping point is difficult to predict due to the system's complexity, heterogeneity, and dependence on context (Bentley et al., 2014; Constantino et al., 2022; Winkelmann et al., 2020). In some circumstances, these points may not even exist (Ferraz de Arruda et al., 2023). Despite this, evidence for tipping seems to exist, or at least for tipping as it is conceptualised in network theory (Guilbeault et al., 2018), across and between societies, scopes, and organisms (Dodds and Watts, 2004). A significant

number of overlaps or co-occurrences observed in empirical and modelling results for social contagion processes from various disciplines confirm this (Andreoni et al., 2021; Centola et al., 2018; Wiedermann et al., 2020; Xie et al., 2011). While it is highly unlikely that the employed methods will ever be quantitatively used to predict tipping points across systems, the results obtained can be used to identify a range of scenarios where tipping is more likely.

Tackling the questions surrounding social tipping processes becomes much easier when social networks are studied, and network science methods are used. These are critical tools for understanding and studying social tipping processes (Granovetter, 1978; Watts and Dodds, 2007; Watts and Strogatz, 1998). Naturally, we do not have to view the system(s) through this lens, and many other approaches are viable (Eker et al., 2019). However, it is useful to do so, as social interactions—a fundamental part of social processes—can be well represented in these networks (Berner et al., 2023; Guilbeault et al., 2018; Sayama et al., 2013; Smaldino, 2023). Some of the tipping literature acknowledges this (Constantino et al., 2022; Smith et al., in preparation; Winkelmann et al., 2020), but, to our knowledge, no literature solely presents a network-based perspective. The conducted literature review enabled us to determine how previous findings and the social tipping concept can be complemented by network theory. Ideally, this will improve our understanding of this perspective and advance methodological approaches. While we limited our scope to social networks, we also limited the scope of what we recognised as social tipping in this article. Social tipping processes can lead to high-level changes in the socio-techno sphere, for example, by reducing EV battery costs, or the legislative sphere by changing how climate change is integrated in school curricula. We did not consider this level of abstraction in this work and focussed solely on social tipping in terms of the change in and transfer of norms, values, or behaviours between people. Although this work is slightly removed from the sustainability and climate change context where social tipping is usually discussed, we and several others (Constantino et al., 2022; Holme and Rocha, 2023; Smith et al., in preparation; Winkelmann et al., 2022) believe that the insights provided by studying a network, and by taking a complex contagion-centred approach are necessary to better understand higher-level tipping in sectors that are crucial for social transformations.

Firstly, beginning from this point, we quantified general trends in the social tipping literature in several disciplines. Undertaking such a task can be prohibitively difficult due to the complexity of the dataset when compiled across disciplines, the inconsistency of term usage, and the general complexity of social tipping, where many confounders are present (Milkoreit, 2023). This task is made especially difficult when intending to include a quantitative analysis, where variables such as critical mass and tipping thresholds (macroscopic and individual) have different dimensions. To ensure robust results, we took a conservative approach towards the data collected and focussed on identifying the marginal effects of individual factors where many explanatory variables were involved. We also provide a range of social tipping thresholds, instead of a single macroscopic threshold. Thus, in this work, we focused on establishing the upper limit of the societal critical mass required to trigger a social tipping event, even in difficult-to-tip systems. Secondly, we wanted to determine whether the Pareto effect exists in susceptible social systems. The Pareto effect is roughly consistent with the principle that 80% of an effect can be

attributed to 20% of the causes (Pareto, 1971). Although this is used arguably only as a general term for non-linear effects in various systems, in the context of this research, it specifically denotes the ability of a small minority of people (i.e. roughly 20%) to trigger system-wide change, influencing roughly 80% of the population. This is a well-known term in many spheres (Dunford et al., 2014); thus, it can be used to communicate relatively technical knowledge to a non-scientific audience. Lastly, we wanted to bridge the conceptual and terminological gap between the network science and social tipping literature. By analysing the literature identified in our initial database search, we could systemically identify several critical factors influencing tipping processes in a subset of social systems. With these as our guide, we qualitatively reviewed each factor and synthesised the existing information from the relevant literature, reporting the results in section 2. In the next steps, we then limited our analysis to literature which explicitly incorporated networks in a formal sense and included only those that reported empirical results. Finally, we relate our findings to social tipping in a concrete and applicable fashion in section 4.3. Our goal was to verify the existence of a Pareto effect in social tipping processes, conduct a broad-scope quantitative review of factors influencing social tipping processes, and ultimately to define a realm of possibility where tipping is most likely to occur.

2 Narrative Literature review of tipping in social networks

2.1 What is social tipping?

The terms and definitions used in the interdisciplinary field of social tipping research are quite inconsistent. Mixed meanings occur: Terms are appropriated for different contexts, and in the process, slightly changes occur in their meanings (Milkoreit, 2023). It is easier to begin by describing the characteristics of social tipping where the literature on the topic is more consistent (Hodbod et al., 2024; Milkoreit, 2023; Milkoreit et al., 2018; Winkelmann et al., 2022). Even here, the terms *social tipping points* and *social tipping processes* are easily conflated, although the former is strictly a feature of the latter. Four primary characteristics of social tipping processes in the context of social-ecological systems are nonlinearity (abruptness), positive feedback as a change mechanism, multiple stable states, and limited reversibility. The definitions provided below were included because they reference or have some or all these characteristics.

In this paper, we use published definitions as much as possible, but we define or re-define specific terms where necessary for the purposes of our analysis and for improved clarity.

Tipping refers to a phenomenon where a relatively small change or intervention in a system leads to a large change (or to large changes) on a macroscopic level (Milkoreit, 2023). The term *tipping point* originated from social science research on racial segregation patterns (Grodzins, 1957) and was used to refer to thresholds for the racial composition of neighbourhoods in the U.S. in the 1950s. When these thresholds were crossed, people with the minority skin colour started to feel uncomfortable and tended to move out. More recently, the term was popularised by Gladwell's (2000) book on trends in human behaviour and consumption, as well as technology change. The definition of *tipping elements* originated, however, in work on the Earth's climate system (Lenton et al., 2008). Since these terms were established, they have been broadly used in various scientific

disciplines in the natural (Holland et al., 2006; Scheffer et al., 2012; Dakos and Bascompte, 2014) and social sciences (Grodzins, 1957; Milkoreit et al., 2018; Schelling, 1971; Winkelmann et al., 2022). Our unit of analysis in this article i.e networks of social agents capable of undergoing non-linear changes are consistent with existing definitions of *social tipping elements* in this body of work. A

A formal definition of the term *social tipping* was proposed by Otto, Donges et al. (2020). These authors stated that social tipping involves a discontinuous state transition in the underlying system, i.e. it is more than a rapid continuous change (triggering phase). The emergence of the new state, however, can be gradual (manifestation phase). A more mathematical definition of social tipping using a criticality framework was recently introduced by (Winkelmann et al. (2022). under which . These authors argued that a tipping threshold is reached when the system reachesa critical state, where a comparably small intervention can trigger a significant system change over time, known as a *tipping event*. This definition and approach have been expanded by others (Smith et al., in preparation). This criticality-centered definition of social tipping differs significantly from the definition of social tipping *minority tipping* introduced in this paper. Rather than focussing on criticality, wewe introduce simple criteria (Box 1) for the shift from a minority to a majority, which we explain further later in the paper. Lastly, the term *spillovers*, as used for example by

Berger et al., (2021), and Efferson et al., (2020) is a useful framework for social tipping, particularly in the context of exogenous changes to a social system, i.e. interventions. A spillover is an indirect systemic effect produced by an endogenous response to an intervention on a single or few individuals. This is larger than the effect of the intervention itself.

,we describe aconducted to examine inority-induced social tipping, interpreted as being limited ,assumed that had redwere In this article, we present a quantitative analysis of minority-induced social tipping, focusing on cases where early adopters of a new norm comprise less than 50% of the population. For our quantitative results (Fig. 4, Fig. 5), we operationalize social tipping as instances that meet the criteria for a social tipping event as defined in Box 1, specifically where the fraction of adopters of a norm transition from a minority ($f_0 < 0.5$) to a majority ($f_\infty > 0.5$). However, we relax this constraint in section 2 to discuss a wider evidence base. and refer to the broader definition by (Milkoreit (2023), as described above. Figure 1a shows the stricter definition as a shaded blue social tipping zone, a scenario in which a minority group of actors have convinced a majority group to adopt another social norm. This is also what is referred to as a contagion event, or a cascade in network theoretic terms (Box 1). Figure 1a also depicts a characteristic feature of social tipping, i.e. its non-linearity, a non-linear increase in a system state variable for a given increase in a system control parameter, or a state variable itself (Strogatz, 2019). This non-linearity in social systems implies that a marginal effect of norm adoption, e.g. one individual adopting a new norm, can have a large effect on the final fraction of people adopting this new norm after a social tipping event. Figure 1a demonstrates this under the assumption that the exemplary social system can undergo a social tipping process. In this example,

165 alternative norm adoption by ~20% of the population leads to a steady state alternative norm adoption of around ~80%, demonstrating the theoretical Pareto or minority tipping effect.
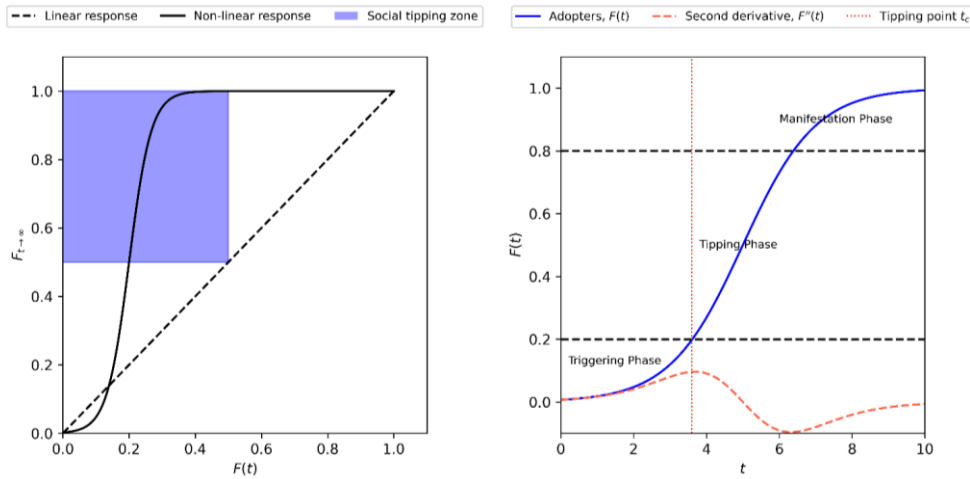
Figure 1: (a) The line denoted "Non-linear response" characterises the predicted steady state behaviour of a social system in response to an increasing fraction of individuals adopting an alternative norm, $F(t)$. Social tipping as defined for the purposes of our
170 quantitative analysis is depicted as the blue-shaded region. (b) In blue, the evolution of the alternative norm adopter fraction over time is predicted in a social system undergoing a social tipping event. The tipping threshold is defined as the adopter fraction at the maximum of its second derivative, the tipping point t_c, shown here as a purple horizontal line. We use these two definitions as a conceptual base for our review, and its methodology.

A fundamental idea of social tipping (and tipping in general) is the idea of non-linearity, or a non-linear increase in a system
175 state variable for a given increase in a system control parameter. A useful and intuitive concept of "spillovers" to depict this comes from Efferson et al., 2020. A spillover is an indirect systemic effect produced by an endogenous response to an intervention on a single, or few individuals. This is larger than the effect of the intervention itself. In this sense, an increase in a system control parameter or the actions of a single individual would be an intervention, and the non-linear response in the system the spillover. The term spillover is intuitive when considering dynamical social systems. If we plot the steady state
180 value of the state variable $F(\lambda)$ as $t \to \infty$ against a given value of the critical parameter $\lambda(t)$, and shade the region above $F(\lambda) = \lambda(t)$, this shaded area represents the domain where the system exhibits a nonlinear response, specifically where $F(\lambda) > \lambda$. We depict this concept in Fig. 1 below, where the blue shaded area is a "spill" over the reference line.

185 Figure 1: (a) Depiction of the zone of non-linear outcomes based on the critical parameter value λ, denoted by "Tipping zone" and shown in blue. An exemplary cumulative distribution function depicts the Pareto effect where roughly a 20% change in a

system control parameter results in an 80% change in the system state at equilibrium. (b) A possible time evolution of the fraction of adopters of a new norm in a social system undergoing a tipping event. We use these two concepts as a conceptual base for our review, and its methodology.

190 Although this is a general example, if λ represents the proportion of actors engaged in one social norm, and $F(\lambda)$ the final fraction as the time of the system approaches infinity, the shown Pareto CDF depicts a scenario in which a minority of actors have convinced a large majority to switch to another social norm. This is also what is referred to as a contagion event, or a cascade in network theoretic terms. Another way to view social tipping which will be employed in our analysis further on, is to look at the number of people as a fraction of the social system who have adopted a certain norm over time. A tipping

195 pointThe tipping point then can be identified as the point in time where the fraction of norm adopters $F(t)$ has the most potential to induce a social tipping eventchange. How do we define this point? One way is to refer to the concept of criticality introduced previously. Smith et al., (n.d). define this criticality as the probability that the state of a complex adaptive system at a given point in time undergoes a tipping process or a path bifurcation. We conceptualise this simply for the purposes of our analysis by using the second derivative of the state variable, $F(t)$. The maximum value of this second derivative is the point

200 where the acceleration in the rate of norm adoption is the greatestthe point where marginal norm adoption produces the greatest acceleration in the change of norm adoption. We assume this is the point most likely to lead to a social tipping event, if it is possible within the given social system. Jin and Yu (2021) also adopted this measure to classify the tipping threshold of a networked social system under complex contagion conditions, classified as the chance of tipping based on a perturbation or marginal (individual) norm change. In Figure 1b, we plot this fraction $F(t)$. We apply the language from Otto, Donges et al.

205 (2020) here to illustrate these stages.

Box 1: Key Terms

Social tTipping event

Assuming a social system where an agent can adopt norm states *a* or *b* at a given time, this pertains to the steady state fraction of individuals who have adopted norm *a*. The condition which is satisfied by a tipping event is defined as:

$$M(0) < 0.5 \text{ (indicating that norm } a \text{ starts in the minority) and } \lim_{t \to \infty} M(t) > 0.5$$

(norm *a* becomes the majority). Where $M(t)$ is the fraction of norm *a* adopters at a given time.

Network cascade

Analogous to a tipping event but on a network: A change in the behaviour of individuals (nodes) in a population (network) due to a herd-like behaviour through imitation of others. Subject to the *cascade condition*: An innovator or seed node has to be attached to a vulnerable cluster of nodes who become adopters, which after a percolation (spreading) process must occupy a fixed fraction (here > 0.50) of a finite network (Watts, 2002).

Tipping threshold point - Macroscopic

Given a social system, refers to the point t_c $c(t)$ in the trajectory of $F(t)$, where $F(t)$ represents the fraction of individuals in a social system who have adopted a certain norm at time t, whereafter a rapid and non-linear increase occurs in $F(t)$. Also referred to as a tipping point. We conceptualise this as the maximum of the second derivative. See Figure 1.b for a graphical example.

Critical MassTipping threshold – Macroscopic,

The fraction of individuals $F(t)$ in a social system who have adopted a certain norm at the time where the macroscopic tipping point threshold is reached, represented as $F(t_c) = \lambda F(c) = \lambda$.

Threshold fraction - Individual Threshold

Given a node *i* in a social network: The fraction ϕ of network neighbours *k* of node *i* sharing a common state, after which exceeded, node *i* also changes their state (Granovetter, 1978).

Box 1: ~~Some K~~key terms which are helpful for understanding the concepts presented in this article. Definitions may be similar to those in other works but have been slightly changed to apply to our analysis.

2.2 Networks and tipping

Social processes are governed by relationships among people. The spatial and temporal sum of these connections constitute social networks. In this sense, the network structure is fundamental to flows that occur via a social network and critically affects tipping processes (Dodds and Watts, 2004). A formal description of networks is usually the mathematical concept of a graph. In their simplest form, networks consist of nodes and links (Berner et al., 2023). Thus, a network N can be fully described by the tuple $N = (V, E)$, where V is the set of all nodes, and E is the set of all links. Here, nodes can be people, animals, or molecules, and the links can be Facebook interactions, mating relationships, or bonds. Before giving specific examples of networks, it is important to distinguish adaptive, temporal, and static networks. Intuitively, the first two change their structures over time, while the latter does not (Holme, 2015).

Adaptive networks and temporal networks both shape, and are shaped by dynamic processes that occur in them, but the topology of the former takes precedence over the temporality or timing of events (Berner et al., 2023; Holme, 2015). Considering that all social networks are predicated on social interaction and constantly change, for all intents and purposes, static networks are either representations of aggregated social interactions or network processes, such as rewiring, over a period of time (time-aggregated networks). They can also represent a static slice of a network at a fixed time point. A concrete example of a social network would be attendees of a conference and their interactions. In this case, each user is a node, and conversations between attendees are represented as links (contacts) between them, forming a human proximity network (Donges et al., 2021; Holme, 2015). The sum of all conversations taking place in the conference period or a snapshot of those currently conversing (e.g. at 15:00 on a Friday afternoon) would then be a static representation. A temporal or adaptive representation is more difficult to visualise but could be created by plotting the average degree (number of node links) of the graph against time (Holme, 2015) . In this work, we consider all three types of networks (i.e. adaptive, temporal, and static), but the majority are either static or adaptive networks. Most of the literature, and especially those examples involving modelling, use archetypal network-topologies representing commonly occurring real-world networks and their properties. One example is small world networks: These display properties such as high local clustering of nodes and short path lengths, which are often featured by real-world biological, ecological, and social systems (Telesford et al., 2011; Watts and Strogatz, 1998). A figure and reference for the most common network topologies appearing in our review appears in Fig. 2.

Small-World   Barabási-Albert   Erdős-Rényi   Regular Random   Clustered Lattice
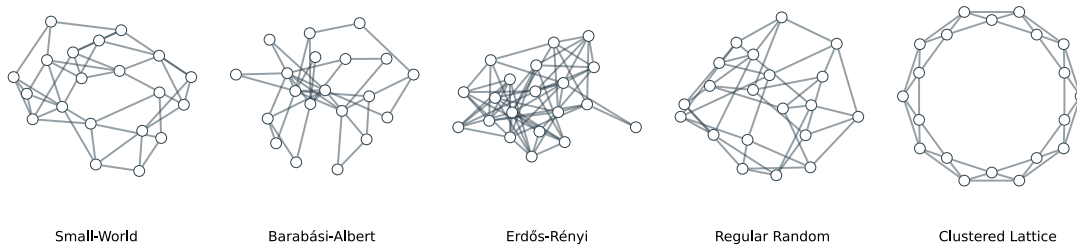
Figure 2: A visual representation of the most common network topologiesypes identified in our literature review.

Table 1: A description of network characteristics for the network topologies shown in Fig 2.

Network tType	Clustering	Average pPath lLength	Degree dDistribution
Small-World	High	Short	Varies
Barabási-Albert	Low	Short	Scale-free (Power law)
Erdős-Rényi	Low	LowVaries	Binomial/Poisson
Regular Random	Low	Long	Uniform
Clustered Lattice	High	Long	Uniform

Table 1: A description of network characteristics for the networks shown in Fig 2.

For the purposes of this work, which was carried out to view social tipping through the lens of network theory, we can generalise social tipping as a contagious spreading process or cascade via a complex network (Guilbeault et al., 2018; Watts, 2002). A definition is given in Box 1.This spreading process can involve behaviours, opinions, knowledge, or social norms (Christakis and Fowler, 2007; Nyborg et al., 2016; Schleussner et al., 2016). The mechanism leading to contagious spreading processes via networks is classified in two main ways: simple contagion and complex contagion (Guilbeault et al., 2018). In the former, an agent can be "infected" by one exposure to another contagious agent, whereby an agent usually requires multiple exposures from different sources in the latter (Centola and Macy, 2007). A notable requirement for the propagation of complex contagion is the presence of wide bridges (Guilbeault and Centola, 2021; Reisinger et al., 2024). A bridge forms a link between two otherwise disconnected subcomponents of a network. This can be a single link between two nodes, *a* and *b*. One dimension of this bridge is its length, which is the shortest path between these two nodes. Another is its width, which is the number of ties it contains. The latter is critical, because it facilitates the requisite multiple exposures of nodes as the contagion travels from node *a* to node *b*, and thus of node *b* itself. A wide bridge thus forms a network structure that facilitates the spread of complex contagions through multiple, reinforced connections between two neighbourhoods in the network. Using the language of systems dynamics, the control parameters we are observing in this study relate to network properties or the properties of agents embedded in the network, for example thresholds, or even the adopting fraction itself at any given time, and the steady

~~system state variable is the fraction of individuals who have adoptIn particular, where we are interested in finding the point of critical mass which facilities a tipping event or; the rate of change of cooperation with respect to the current level of cooperation or adoption, we can use Centola's 2013 definition of a tipping point:~~

~~"The gap between zero cooperation and the level of cooperation at which the growth of participation becomes self-sustaining."~~

260 In the rest of this article, we will use the term *social tipping* to refer to a network cascade,~~s cascade and social tipping interchangeably,~~ implying that these terms have the same meaning when discussing social opinion and norm dynamics in networks. Exceptions to this usage occur when we cite specific literature, where we prefer to distinguish between these terms as originally defined. ~~We consider social behaviour to be an expression of the adherence or adoption of the norm, and use the terms interchangeably.~~ An important distinction regarding thresholds should be made between the system level macroscopic

265 tipping threshold and individual agent thresholds~~, or threshold fractions~~. Whereas the former is defined as shown in Fig 1b and as described in Box 1 as the tipping ~~point~~ threshold along a ~~time series~~trajectory, the latter refers to the conditions in an agent's immediate social network required for one agent to change their opinion (Watts, 2002). ~~The difference is important as~~ In the most realistic cases, the mean individual threshold will neither equal nor reliably predict a given macroscopic threshold (Wiedermann et al., 2020) .

270 **2.3 The role of network structure and attributes**

In this section, we examine the effects of network traits or properties on social tipping processes in some well-known network topologies. Not all networks are the same, and the topology can vary based on the social domain (Efferson et al., 2020), social group (Christakis and Fowler, 2008), or social process (Bellotti et al., 2023) represented by the network. For example, financial networks display more inequality in degree distribution than a reference small world network (Leo et al., 2016), homophilous

275 networks spread health innovation behaviour more effectively than unstructured networks (Centola, 2011), and bursty network interactions can allow contagion events in networks which are otherwise difficult to tip (Karimi and Holme, 2013). Network topology can vary over time or can be shaped by social processes, such as those occurring in temporal and adaptive dynamical networks (Berner et al., 2023). This topological change can then affect the social processes, which leads to feedback loops. As such, topology and dynamics in networks are often confounded when trying to explain why they change and evolve (Shalizi

280 and Thomas, 2011). It can be difficult to address the role of network structure when most of the networks discussed in this work are essentially adaptive dynamical networks, i.e. they have constantly evolving structures. Due to this consideration, we address how a given static topology affects cascade dynamics near a certain time point.

By focusing on well-known network topologies, problems related to terms used in different fields can be avoided, for example,

285 where certain network types are ubiquitous, for example, Erdős-Rényi, Barabási Albert (Albert and Barabási, 2002), or Watts-Strogatz (Watts and Strogatz, 1998) networks (Telesford et al., 2011). A broad base of evidence exists for the existence of

common relationships between topology, cascade size, and frequency. For example, evidence from game theory-based(Ohtsuki et al., 2006), ecology-based (Martin et al., 2020), as well as social contagion-based models (Centola, 2011, 2013), all show that a structured network positively affects the magnitude and rate of contagion spread compared to unstructured networks. This finding contrasts with the "strength of weak ties" concept described by Granovetter (1973) and others (Watts and Strogatz, 1998). One way to interpret these contradicting results is to consider that they depend on network size. Centola (2013) demonstrated how weak ties are mildly helpful in contagion spread in small systems, but strong ties and clustered networks are required to produce successful critical mass phenomena in larger systems. Where social tipping to promote sustainability plays out on a global scale, a prerequisite for any mobilisation effort, therefore, is the existence of homophilic, interconnected, and trusting networks. Although this is generally the case (Guilbeault et al., 2018), Efferson et al. (2020) showed how homophily can be detrimental to spillovers in the context of policy interventions when they are too large. This implies that attempts to facilitate norm change exogenously may interact with homophily in detrimental ways once the intervention becomes too strong. Clustering, more specifically, increases the likelihood of repeated exposures to a contagion source and locks the information within a community (Fink et al., 2016). This second aspect is fundamental for reaching a critical mass (Centola, 2010) and halting the dispersion of a social contagion for long enough that a percolating cluster can form (Box 1). Overall, complex contagion requires a network to have communities which are sufficiently built up but are also connected through wide bridges. This allows ideas to reinforce themselves from within, but also offers enough connectivity so these similar clusters can connect at some point (Chiang, 2007). This idea is a fundamental one in our world as we know it, characterised by increasingly highly connected global networks; the information supply is higher than ever, and so is the noise (Bak-Coleman et al., 2021). Contagion or information about it tends to die out after more than three network steps (Airoldi and Christakis, 2024; Christakis and Fowler, 2007, 2008; Fowler and Christakis, 2008), indicating that some fundamental laws govern network structures which are compatible with the stickier cascades we have to deal with.

2.4 The role of an actor's preference and heterogeneity

Successful emergent social tipping processes fundamentally require consecutive individuals or agents to be susceptible to change. Many terms are used to conceptualise this susceptibility. In models of norm change or opinion spread across disciplines, such susceptibility is often operationalised implicitly or explicitly as a threshold (Centola, 2013; Efferson et al., 2020; Granovetter, 1978; Guilbeault et al., 2018; Watts, 2002). A threshold quantifies the point at which an agent will change their behaviour; thus, it governs the magnitude and rate of social tipping in a population. In the real world, this susceptibility varies individually (Efferson et al., 2020) and depends heavily on the type of normative change (Berger et al., 2021; Guilbeault et al., 2018). In other words, both individual thresholds and their governing distributions are heterogeneous. Macroscopic or social-group-level threshold distributions are also emergent, meaning that their shape is not visible or predetermined, but arises due to the unique set of interactions occurring among microscopic actors (Wiedermann et al., 2020). This property makes prediction exceedingly difficult, especially with regard to highly polarised or controversial issues. Wiedermann et al. (2020) successfully demonstrated how agents seeded with very narrowly distributed individual thresholds can produce a different

system level distribution. Some models and experiments show the significant effects different threshold distributions have on both cascade speed and magnitude (Andreoni et al., 2021; Berger et al., 2021; Dodds and Watts, 2004; Karsai et al., 2016). Efferson et al. (2020) demonstrated how this effect is also robust to changes in network topology, intervention types, and several other factors. Individuals with high thresholds or even untippable or "immune nodes" regarding a given spreading event can severely hinder or prevent a cascade process (Karsai et al., 2016; Wiedermann et al., 2020). This potential effect is magnified when these nodes occupy key positions in a network, for example, as the first contacts for an innovator or a seed node for a potential network contagion (Reisinger et al., 2024). Optimally, this first contact network should consist of individuals who have typically lower thresholds than normal to enable cascades (Nishioka and Hasegawa, 2022). Efferson et al. (2020) also specifically showed that, under some conditions (where a positive response to an intervention is guaranteed), targeting resilient nodes with policy interventions is more effective than relying on endogenous processes such as tipping or spillovers to evoke norm change.

Thresholds are influenced by several often co-dependent, and some examples are: payoffs or switching incentives (Centola et al., 2018), tension (Berger et al., 2021), and jointness of supply (Centola, 2013). These terms all refer to a switching payoff or the cost of norm adoption (abandonment) but are expressed differently. This payoff depends on the network density, social context, and type of norm change (Berger et al., 2021; Constantino et al., 2022; Efferson et al., 2020). Perhaps confusingly, these terms are also used in some models to refer to implicit thresholds, for example, in Andreoni et al. (2021), where tipping thresholds are set by changing miscoordination penalties or by increasing the personal benefit of change. Conversely, explicit thresholds are used to operationalise these same concepts. Examples are seen in Berger et al. (2021), and Efferson et al. (2020), where different threshold distributions are used to represent different social preferences and tension related to a specific dilemma. Based on this example, Fig. 3 displays several general distributions which may represent preferences via tipping thresholds for certain socio-ecological dilemmas.
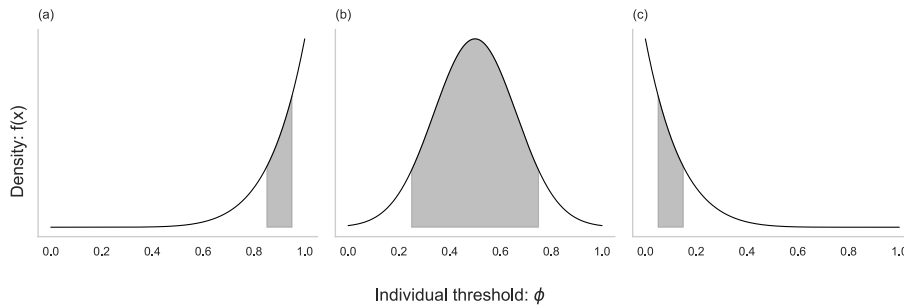
Figure 3: Illustrative ~~threshold fraction~~individual threshold **(ϕ) distributions for a population. These indicate** the susceptibility towards **changing a specific behaviour or norm in reference to some current social dilemmas surrounding pro-environmental behaviour. Here, (a) could represent a decision to become vegan, (b) to ride a bike to work, and (c) to recycle rubbish and waste. The shaded area represents different strategies for choosing members of a network, i.e. the seeds, to try and promote endogenous norm change via a network or to cause social tipping.**

All meat and animal product consumption would correlate with a left-skewed distribution (a), meaning that the mean threshold is high, and tipping is difficult (Peattie, 2010a). In this situation, most people would only change their dietary habits when a vast majority, i.e. around 70%, consume food differently (Fig. 3b). Intuitively such a dynamic makes the existence of any minority tipping dynamic unlikely, as a majority (> 0.50) have likely already adopted the alternate norm. Another is car usage reduction, the controversial and polarised nature of which may be represented by a bi-modal distribution. In this case, the willingness to drive less is very low in one-half of the population and very high in the other half. Regardless of the nomenclature used, several sources show that the successful adoption of a cascading norm or behaviour is highly contingent on the perceived individual benefits, regardless of the magnitude of the cascade (Berger et al., 2021; Centola et al., 2018; Centola, 2013).

2.5 The role of agency and inequalities

In this section, we ask how individuals and groups can intentionally influence the adoption of new patterns of behaviour (Kaaronen and Strelkovskii, 2020) and induce abrupt changes in social conventions and public opinion (Centola et al., 2018; Galam and Cheon, 2020). Specifically, how does the agency of individuals and groups transform the social structure, understood as the collective prescriptions and constraints on human behaviour (Granovetter, 1985; Robb, 2014). The social structure is composed of a rule system that constitutes the "grammar" for social action. This is used by the actors to structure and regulate their transactions with one another in defined situations or spheres of activity (Otto et al., 2020a). Burns and Flam (1987, p.26) pointed out that the complex and multidimensional normative network is not given but is a product of human action, stating, 'human agents continually form and reform social rule systems'. However, what agency do individuals have to change the social structure? Human agency is understood as the ability to shape one's life, and a few aspects can be distinguished. Individual agency is reflected by individual choices and the ability to influence one's own life conditions and chances. This individual agency varies strongly within a society based on the individual's age, gender, income, education, personal health status, position in social networks, and other factors. Collective agency refers to situations in which individuals pool their knowledge, skills, and resources and act in concert to shape their future. Everyday agency refers to consumer and daily choices, and strategic agency refers to the capacity to affect wider system change (Otto et al., 2020a).

In a network-theoretic sense, agency can be seen as the ability of a node to control or initiate processes in a network. Where structural properties of a network or a node such as centrality or degree strongly influence this ability (Korkmaz et al., 2018), we can use these structural measures as a proxy for a node's agency. Structural properties, while generally a good indication of a node's influence, are only one aspect. The agency of a particular node also depends on the specific dynamics in a given network and the context. This was clearly demonstrated by Guilbeault and Centola (2021), who showed that standard centrality

measures, while suitable for predicting (the social influence of seed nodes under conditions of simple contagion dynamics, fail under complex contagion conditions. Social influencers, who in colloquial terms have high degrees of agency as per our definition above, have been the subject of much contentious debate in several areas dealing with research on social change (Constantino et al., 2022; Han et al., 2020; Hodas and Lerman, 2014; Nielsen et al., 2021; Nishioka and Hasegawa, 2022; Nyborg et al., 2016; Paluck et al., 2016; Paluck and Shepherd, 2012; Watts and Dodds, 2007). Taking an intuitive view of social influencers and their presence in the era of social media platforms such as TikTok and Instagram could lead one believe that they might dramatically shape social opinion and information. However, in the world of complex contagion, which depends on nodes' proximity to wide bridges rather than node degree, they may be surprisingly ineffective (Guilbeault and Centola, 2021; Watts and Dodds, 2007). In fact, "normal" people may be the most cost-effective instigators of change, especially as the volume of information reaching us increases more and more (Bakshy et al., 2011; Fink et al., 2016; Hodas and Lerman, 2014). How does change take place in situations where individuals and groups have different and conflicting interests? Centola (2021) pointed out the role of so-called change agents, who bring innovative solutions into their communities, advocate change, build networks of early adopters, and play pivotal roles in coordinating the new equilibrium and restructuring institutions.

2.6 The role of processes, time, theme, and scale

Temporal processes have a large effect on social tipping dynamics. Due to the interdependence of processes, network structure, and agent state variables, these can be difficult to analyse as mentioned in section 2.3. Some sources claim that temporal processes can be more important than network topology or can simplify some aspects of complex spreading (Hodas and Lerman, 2014; Karimi and Holme, 2013). In the former study, the duration over which interactions occur strongly affects cascade magnitude and success. To highlight the difficulty of making general statements about these systems, the duration length shows the opposite effect, depending on whether a fractional or absolute threshold is used in the cascade model. The information transmission rate or burstiness can be conducive to complex contagion (Karimi and Holme, 2013), but it has been shown to slow down simple contagion (Karsai et al., 2011). Information about the social norm landscape, both globally (norm average) and locally (close contacts), strongly influences the decision to abandon an old norm or to adopt a new norm (Bergquist and Dinerstein, 2020; Leviston and Uren, 2020; Pieters et al., 1998). This information may pertain to the prevalence of a social norm in society and is very important when the perceived risk or change is high (low payoff). This may happen, for example, when a person decides to abandon a behavioural norm but faces the penalty of alienation from their close social group. When this agent knows that there is global support for an alternative norm despite the group norm, they may be more encouraged to switch regardless. Andreoni et al. (2021) provided evidence for this in a behavioural experiment, where the participants were provided with information about other players' preferences, which were not directly linked to increased contagion size. Jin and Yu (2021) also showed a similar effect by taking a modelling approach. This is a key factor when considering something like pro-environmental behavioural norm changes, like eating less meat (Leviston and Uren, 2020), where the risk of alienation is high. Information frequency or regularity and clarity are then crucial for ensuring cascade events

~~are~~social tipping events are noticed by people in a social network, essentially increasing the fraction of people available to engage ~~with a cascade~~in norm change. Irregular or delayed belief update times, as well as unclear information, dampen social tipping effects and prevent the formation of a critical mass, as people become risk-averse when provided with poor information (Berger et al., 2021; Peattie, 2010b). As a caveat, when the information density (i.e. the frequency of providing information over time) becomes too low, social contagions may fail to infect a person, as the person does not attach enough importance to the information or does not notice the signal (Hodas and Lerman, 2014). This can also be thought of as a poor signal-to-noise ratio. Fink et al. (2016) identified this as one factor making nodes with a high in-degree, common with social influencers, more difficult social contagion targets than others. They are overwhelmed with noise. To a lesser extent, the noise created by our highly interconnected digital global network may make complex contagion generally difficult through these mediums (Bak-Coleman et al., 2021; Hodas and Lerman, 2014).

We established earlier that norms and opinions spread differently from, e.g. viruses and memes, and that these can be roughly separated into complex and simple contagions, respectively. This simple dichotomy hints at a fundamental principle: that every type of contagion may spread differently. Indeed, as an example, in their long-term study of a network of 12,067 people over 32 years, Christakis and Fowler (Christakis and Fowler 2007, 2008 Fowler and Christakis, 2008) showed that the spread of happiness depends more on a person's geographical proximity to a potential contagion source than the spread of healthy eating behaviour. Smoking behaviour transfers very easily to one's spouse, but not obesity or happiness. Finally, educated people in the USA will have more influence over the smoking behaviour of others, but, in another study on rural communities in India, local elders and knowledge holders only had a marginal effect on the spread of malaria-prevention behaviour (Bellotti et al., 2023). Norms related to controversial topics such as politics, or social movements in response to socio-political issues show large marginal effects after continued exposure to a norm holder, showing that repeated exposure is critical for opinion change (Fink et al., 2016; Romero et al., 2011). This unique variation in spreading behaviour based on content can make it even more difficult to make predictions. All of these studies still report repeated exposure and social proximity as leading predictors of norm spread between people, supporting arguments for the use of complex social contagion models, even in unfamiliar contexts or under conditions of uncertainty.

3. Data and Methods

3.1 Data collection

To identify literature on social tipping in networks from various disciplines, several broad search terms and strings were initially used, as the disciplines employ different nomenclature. Where we explicitly focussed on networks, we included this in every search string. A literature search was conducted in the Web of Science, as well as in Google Scholar, for the period of 01/01/2001 - 20/09/2023. Search terms used were ("complex contagion" AND "social networks"~~", "network"*, "networks"* AND ("complex contagion" OR "norm diffusion"~~), ("norm diffusion" OR "complex contagion") AND "social networks". We

identified 33 studies using modelling, observational, or experimental methods to study complex contagion in human networks, and that mentioned or referred to empirical results in their abstracts. Another 27 were discovered by examining the reference lists of the initially identified literature and by using comprehensive review articles recently conducted on complex contagions (Guilbeault et al., 2018; Holme and Rocha, 2023). Of the 60 studies identified, 21 were had to be discarded because these still only investigated simple contagionclude rather than complex contagion models, or complex contagion-like phenomena. We then analysed the final list of the literature in stages. In stage 1, key empirical results were elucidated and coded into a database. In stage 2, we evaluated these key results and relevant theory (synthesised in section 2). We also looked for finding overlaps and examples of agreement between fields. In this section, we also draw on literature cited in the references of the primary literature to bridge knowledge gaps and to supplement our synthesis. This material was not included in the dataset but can be found in the references. The number of pieces of literature considered in these stages was $N = 42$. In stage 3, we filtered the literature so that only those with quantitative results allowing analyses of tipping thresholds were kept. At the end of stage 3, we were left with $n = 124$ articles. A summary of the literature used in stage 1 is displayed in Table 4, and the results are shown in Fig. 4. Stage 3 results are displayed in Fig. 5.

Stage 1 involves classifying key results in terms of how they influence social tipping icascades n networks. Concretely, we applied two criteria: the effect on the rate and magnitude of the social tipping eventcascade. Here, the rate refers to the change in the fraction of adopters of an alternative norm per unit time after a tipping point, and the magnitude, the final fraction of norm adopters. We compared these to a baseline scenario, which was defined as the trajectory with the lowest rate and magnitude in a modelling ensemble or from experimental results. A simple grading system was used to simplify the data collection process, shown in Table 2. Where many of these effects displayed non-monotonic behaviour, we coded them accordingly; these are represented on the x-axis in Fig. 5 as "+/-". Results which could not be quantitatively graded were marked as having a positive or negative impact on social tippingthe cascade likelihood. A positive (or negative) impact was interpreted as an increase (or decrease) in the probability, speed, or magnitude of a social tippingcascade event. Where similar terms showed conceptual or mechanistic agreement, and were used in the same context, i.e. the study evaluated a particular aspect of their effect, we grouped these under an umbrella term. Examples are terms used to describe rewiring (process), an awareness of other people's preferences (process), and weak network ties (structure). All of these can increase the distribution of information through the network to agents and are classified under the umbrella term *global information*. This is shown in Fig. 4a. A glossary of the terms and their meanings can be found in Appendix A, Table A1. Fig. 4b shows the magnitude due to incomplete data for the rate, but this was included for the classification in Figure 4a. A link to the full dataset can be found in the Data/Availability section.

Table 2: Categories of grouping terms based on a percent change in the magnitude of a social tipping event compared to a baseline scenario.

Percent change	Positive/Negative Impact (+/-)

0-30%	1
30-60	2
> 60%	3

~~Table 2: Categories of grouping terms based on a percent change to the magnitude of a tipping event compared to a baseline scenario.~~

3.2 Intercomparison of tipping data from models and experiments

480 To quantitatively compare tipping data across compatible literature sources, we obtained nine modelling data sets and five experimental datasets either by contacting the respective authors, retrieving published data, or re-running simulations based on software cited in the articles. For literature where none of these things were possible, trajectories or data were extracted directly from articles using optical character recognition (OCR) or other graphical techniques. The models evaluated included complex contagion-like dynamics, regardless of the technical implementation. This meant that, even if the models did not

485 explicitly use a contagion model, the social spreading dynamics included a threshold-like mechanism of contagion, where agents needed multiple different exposures to be infected. As mentioned in section 2.1, we conducted this review primarily to identify the macroscopic tipping threshold, as this allowed us to bound our analysis and compare units more easily across studies, as most of the literature reporting qualitative results includes time series. This was helpful, because the parameter dimensionality can be very high and its overlap low. Assuming a time evolution for the fraction of adopters of an alternative

490 norm $F(t)$ ~~in a given~~in each dataset is present, we calculated the tipping threshold ~~, c(t)~~λ from each. ~~This is considered to be the point where a sufficient fraction of agents in a social network sharing the same state value has been achieved in order to facilitate a rapid cascade (defined as over 50%) of state value changes over the rest of the susceptible network population. We refer to the critical mass at the tipping threshold c(t) as λ(t).~~ We drop the time dependency in notation going forward for brevity. We found ~~the critical threshold λ c(t)~~as defined in section 2.1, i.e. the fraction of adopters ~~point in the trajectory of~~

495 $F(t)$ ~~F(t), the fraction of adopters of an alternative norm~~ where the criticality (see section 2.1) in the system is the highest. ~~More concretely we assume this to be the point in F(t)~~ at the point, where the second derivative reaches its maximum: $F(t_c)$. This can be expressed:

$$\lambda = F(t_c) = max_t(F''(t)). \tag{1}$$

Where trajectories are non-continuous, as in experimental results, finite difference methods were employed to estimate λ. Whe

500 re we were also interested in identifying microscopic or individual level thresholds, ~~(threshold fractions),~~ we have collected ranges of mean individual thresholds where a cascade event is possible (Appendix B1).

4 Results

Below, we summarise the main mechanisms which affect social tipping success as identified by parsing the qualitative results from the literature. A table of terms is provided with network abbreviations.

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Table 3: A summary of network topology abbreviations for Table 4.

Term	Abbreviation
Clustered lattice	CL
Erdős–Rényi ~~network~~	ER
Regular random ~~network~~	RRN
Small world ~~network~~	SW
Holme-Kim ~~network~~	HK
Scale-free	SF
Watts-Strogatz	WS
Power-law	PL
Barabási–Albert ~~model~~	BA
~~Scale free~~	~~SF~~
~~Small world network~~	~~SW~~
~~Erdős–Rényi~~	~~ER~~

Table 4: A summary of network topology, the key and supplementary mechanisms which were identified ~~as~~to havinge an impact on social tipping events.
~~Table 3: A summary of network topology abbreviations for Table 4, below.~~

510

Citation	Method†	Network t~~T~~opology	N*	Key m~~M~~echanisms	Supplementary m~~M~~echanisms
Andreoni et al. (2021)	Mixed – modelling, experimental (online)	Complete network	10 – 20	Switching payoffs; switching threshold;	Personal preferences; public awareness of preferences; Timescale
Amato et al. (2018)	Observational (large-scale data)	Empirical (conversation network)	~Millions	Policy (institutional intervention); committed activists	Informal institutions
Centola et al. (2018)	Mixed – modelling, experimental (online)	Complete network	25	Coordination payoffs; committed minority size	Individual memory length; population size
Centola (2013)	Modelling	CL, RRN	1000	Jointness of supply (coordination payoff); homophily	network structure
Baronchelli et al. (2006)	Modelling	Complete network	10,000	System size	Scaling relations
Xie et al. (2011)	Modelling	ER, BA, complete network	500	Network topology	Immune nodes; critical minority size
Castilla-Rho et al. (2017)	Mixed – modelling, observational (real-world)	Grid	630 (673)	"zealots" - rule followers; group norm enforcement (pressure to conform)	Network connectedness, average degree; group size
Paluck et al. (2015)	Experimental (real-world)	Empirical (school)	~431	Characteristics of seeds; out-degree of seeds	Zealots
Wiedermann et al. (2020)	Modelling	ER	100,000	Switching threshold distribution; fraction of acting individuals	Average degree

Citation	Method[†]	Network tTopology	N*	Key mMechanisms	Supplementary mMechanisms
Karsai et al. (2016)	Mixed – modelling, observational (large-scale data)	Empirical (skype)	100,000 (510 million)	Immune nodes; switching thresholds	Constant flow of innovators
Watts, Duncan J. (2002)	Modelling	SF	10,000	Influence of seed nodes	Degree/threshold heterogeneity Switching threshold
Faribi & Holme (2013)	Modelling	Empirical (internet community), ER	113 – 35,564	Network temporality	
Nishioka & Hasegawa (2022)	Modelling	ER, empirical (Ffacebook)	100,000	Switching thresholds; influence of seed nodes	Clustering; network typology
Lacopini et al. (2022)	Modelling	Empirical (various),	327	Social influence of seed nodes; stubbornness	Higher order network structures
Krönke et al. (2020)	Modelling	ER, BA, WS, Empirical (various)	16 – 1024	Clustering; reciprocity	Network topology
Karsai et al. (2014)	Mixed – modelling, observational (large-scale data)	Empirical (skype) SFSkype), SF	100,00 (≤ 663 million)	Neighbour service adoption rate, GDP; press liberty	Network topology
Barash et al. (2012)	Modelling	Lattice, PL, SW	40,000	Long-range-ties; influence of seed nodes	Network topology
Bakshy et al. (2011)	Observational	Empirical (Ttwitter)	54,890 – 4 million	Social influence (spreader); url type (e.g. blog/forum, news)	Content categories; interest; feeling

Citation	Method[†]	Network Topology	N*	Key Mechanisms	Supplementary Mechanisms
Han et al. (2020)	Modelling	PL, Empirical	10,000	Preferential contact of nodes (small vs large degree); information transmission	Population size; mean degree
Jin & Yu (2021)	Modelling	ER, BA, HK, lattice, SW, RRN	10,000	Global information; information sources	Network topology
Zhu et al. (2019)	Modelling	ER, ER-SF, SF-SF	10,000	Network heterogeneity	Threshold distribution
Efferson et al. (2020)	Modelling	Homophilus, complete, RRN	100, 500	Switching threshold heterogeneity; coordination/switching payoff	Cultural identity; group norm
Hisashi et al. (2006)	Modelling	Lattice, SF, RRN, C	100, 500	Ratio of payoff to degree; network topology	Population size
Min & San Miguel (2023)		ER	100,000	Rewiring probability; network "plasticity"	Average degree
Watts and Dods (2007)	Modelling	RRN, Homophilic	10,000	Social influentials, network structure (groups)	Network density; network degree distribution
Damon Centola (2010)	Mixed – modelling, experimental (online)	CL, SW	98 – 144	Homophily; network topology; exposure count	Clustering
Damon Centola (2011)	Mixed – modelling, experimental (online)	Clustered lattice, ER, SF, SW	72	Homophily; network topology	Node centrality
Gizem et al. (2018)	Modelling	Lattice, SW, ER	769 – one million	Network structure; social influence (key nodes)	Clustering; degree distribution
Okada et al. (2022)	Modelling	Lattice, SW, RRN	100 – 1,600	Network structure; trust; density	Polarization

Citation	Method†	Network Topology	N*	Key Mechanisms	Supplementary Mechanisms
Ehret et al. (2022)	Experimental (online)	Complete network	35	Group identity, pay-offs	Preference distribution; population heterogeneity
Hodas et al. (2014)	Observational (large-scale data)	Empirical (Twitter, Digg)	140,000, 170,000	Social influentials; information density	Clustering; intensity of exposure
Belloti et al. (2023)	Observational (real-world)	Empirical (villages; northern India)	1530	Frequency of exposure to contagion; household exposure; trust	Weak ties; social influentials
Christakis & Fowler (2008)	Observational (real-world) – smoking	Empirical (friendship)	12,067	Trust; social proximity; social tie strength/type	**Social influentials (education); clustering**, physical proximity
Fowler & Christakis (2008)	Observational (real-world) – happiness	Empirical (friendship)	12,067	Trust; social proximity; social tie strength/type	Physical proximity
Christakis & Fowler (2007)	Observational (real-world) – obesity	Empirical (friendship)	12,067	Trust; social proximity; social tie strength	Household contacts, gender
Centola & Baronchelli (2015)	Mixed – Modelling, Experimental (online)	Lattice, RRN, Complete network	24, 48, 96	Network topology, network connectivity, competing norms	Network size
Bond et al. (2012)	Observational (large-scale data)	Empirical (Facebook)	61 million	Social tie strength; geographic proximity	Weak ties
Fink et al. (2015)	Observational (large-scale data)	Empirical (Facebook)	55,070	Hashtag type, thresholds, clustering	Adoption payoffs, external topic coverage (e.g. news media)
Airoldi & Christakis (2024)	Experimental (real-world)	Empirical (villages; Honduras)	24,702	Seed node selection/influence; type of norm	Education; social proximity
Tschofenig et al. (2024)	Modelling	BA	5000	Threshold distribution, seed size	Clustering, network topology

Citation	Method†	Network tTopology	N*	Key mMechanisms	Supplementary mMechanisms
Reisinger et al. (2024)	Modelling	SF, CL, SWN, RRN, empirical (Facebook)	1000 – 7057	Wide bridges, contagious components	Network topology

*Figure in Brackets refers to population size of observational data (where available) as opposed to the population size of agents or nodes in a model.
†Modelling here refers strictly to agent-based or simulation modelling as opposed to statistical models or analyses of observational data.

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Contradictions regarding several factors were commonly observed in the literature, which was expected given the nature of complex contagion on complex adaptive systems. To estimate the degree of heterogeneity, we counted $N = 36$ different network topologies, and $N = 22$ different population sizes across the scope of the reviewed articles. Several variables showed non-monotonicity within models and experiments, which are designated by the "+/-" symbol in Fig 4a. Some of the most
520   divergent findings are related to homophily, temporal dynamics of network processes, and network size. These are reflected in Fig 4, where several studies show either positive or negative impacts on social tipping. Despite differences of opinion expressed in the sources, overall, slightly more positive support for homophily appeared in the literature, as well as a strong positive effect on tipping cascade size under certain circumstances. Social influence, which was mentioned along with social influencers quite frequently in the articles, is shown to have a positive and effect on contagion success and magnitude, as shown in Fig. 4a and 4b. It is important to note, however, that the term *social influence* is not the same as *social influencer*.
525   Factors pertaining to social influencers are multiple and include a high in-degree, which is associated with a reduction in infection probability from a cascade for the reasons mentioned in section 2.6. Broad agreement across the literature was seen that trust and clustering have strong positive effects on cascade magnitude, as well as on overall success. Taken together, clustering, social proximity, and trust were identified as consensus factors in the literature review, based on the signs of their
530   effects. These factors all increase the frequency or number of exposures to close contagion contacts and thus help satisfy the fundamental requirements of complex contagion spread.

Conflicting results should not be seen as arguments or weights for the absolute effect of a factor, but rather as a tendency, or the probability of an effect to influence contagion. This pluralistic approach is necessary, as most of the differences shown in
540   Figure 4 are due to strong contextual factors influencing the dynamics of the system in question.
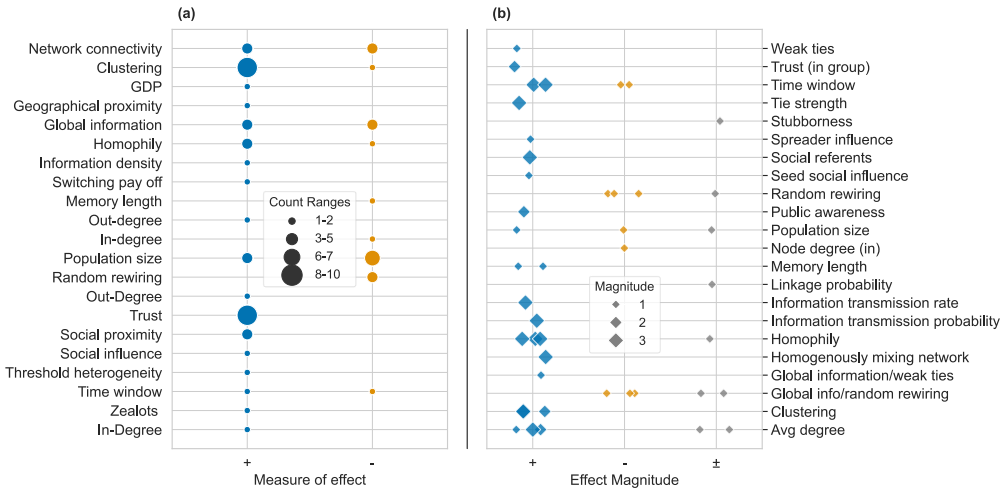
Figure. 4: (a) Frequently cited factors influencing complex contagion events in social networks. Summary based on *n* = 95 observations in *N* = 39 studies. Some concepts have been harmonised interdisciplinarily where compatible. Factors with a sample size of 1 are not shown here to aid visibility but can be found in the SI. Population size, global information, and temporal structure show high disagreement across the literature and depend on the context of spreading processes. Trust is a key factor. (b) Factors influencing the magnitude of contagion events in social networks. Values for the literature with more discernible data on effects, *n* = 50. Magnitudes are defined as per Table 2 and range from 0-100% impact on cascade magnitude. The relationship is displayed as an increasing value of the listed factor, set against a baseline scenario.

Our analysis of critical mass sizes and the steady state adopter fraction as per Fig. 5 shows that a critical mass of individuals who have adopted a norm exists in susceptible social systems; above this critical mass, the fraction of adopters rapidly increases. This is observed at approximately 25% of the total population size (modelling: 24%, empirical: 28%) when considering only social tipping events, and 21% when considering all results. This conforms to theoretical predictions for social tipping processes, and it may seem unsurprising that modelling results also replicate this. However, empirical results (i.e. categorising observational and experimental results) are in general agreement with the modelling results, as well as with each other. Empirical results tend to demonstrate sharper thresholds and non-linearity, verging on discontinuity. We also see this effect continuing across timescales. For
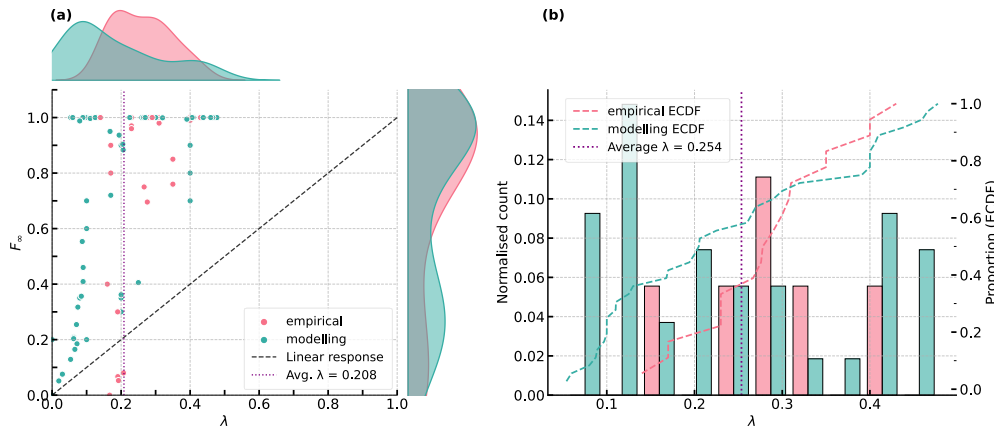
Figure 56: (a) The critical mass sizetipping threshold λ and the steady state adopter fraction F_∞, ϕ **Here, we show** $n = 8687$ **modelling and empirical results from** $N = 13$ **papers on**of **complex contagion in social networks. The bimodal distribution of steady states as shown by the** y **axis marginal distribution, shown on the right, supports theoretical predictions for the non-linearity of social tipping processes. After a critical mass of** ~ 255% **in susceptible populations has been reached, the fraction of norm adopters converges quickly to a fully tipped state (** $F_\infty \approx 1\phi \approx 1$ **). (b) The distribution of tipping thresholds. Here, we classify only social tipping events, i.e.** $F_\infty >$ ϕ 50% **of the population, numbering** $n = 59$. **The empirical cumulative distribution function (ECDF) demonstrates that 95% of critical masses conducive to tipping are <** 0.4 **of the fraction of the population.**

~~example~~example, the results shown in Fig. 5 in Amato et al. (2018) have a timescale ranging over centuries, while the behavioural experiments from Centola (2018) and Andreoni (2021) have timescales of days to weeks. This implies a scale invariance in the tipping dynamics with respect to time. Several trajectories do not display social tipping, and some, e.g the cluster of red points at the bottom left of Fig. 5a, do not even demonstrate a positive non-linear response ($F_\infty > \lambda$), even though the tipping point occurs at a fraction of ~ 0.25 or lower. This indicates some systems are not able to see global tipping even if a rapid change in norm adoption occurs in a small fraction of the population. The slightly bimodal distribution in the critical mass size of modelling results (teal) seen along the top margin of Fig. 5 is likely a result of using different modelling approaches to model complex contagion. Some models inherently feature non-linear but continuous transitions to the tipped state, such as the analytical approximation methods of Granovetter's tipping threshold model (Xie et al., 2011), whereas numerical methods tend to show discontinuities. Certain functional forms representing tipping are also responsible, for example, system dynamics models using normal forms to model social tipping (Kroenke et al. 2022). These normal forms may inherently feature certain dynamics, such as discontinuous bifurcations. Several models seem to show a bias toward very low critical mass sizes, which is not replicated in the empirical studies. This may suggest that the dynamics or assumptions of these models are not realistic. They provide overly optimistic predictions of the potential for a critical mass to tip a system. It should be noted that, in a large majority of models, the initial seed node or first adopter of an alternative norm was normally taken to be one person or a very small fraction, i.e. < 5% of the total population. Fig. 5b demonstrates the range in which social tipping is most likely to occur:

0-44% of the population $ECDF^{-1}(0.95)$, where the value for empirical data is 40% and for modelling data is 46%, respectively. This implies that values above this threshold involve dynamics that are too linear to be considered social tipping or that there is no critical mass at which the system tips for a given system state (i.e. even at critical masses above this range, no social tipping dynamic is possible). More importantly, 36% of empirical and 56% of modelling tipping events occur before or at the critical mass of 25% of individuals. Although not included in Fig. 5 due to not being in time series, results from Airoldi and Christakis (2024) who intervene in a population to induce social contagion, showed large increases in the behavioural adoption for certain treatments when the targeted fraction reached 20-30% of the population. As previously mentioned, several concepts identified in the literature repeatedly appeared across multiple papers, with consistent supporting evidence across different disciplines. In Table 5, we synthesise some higher-level takeaways in more general and less technical language.

Table 5: Key characteristics affecting social tipping processes on networks as identified by their frequency in the literature.

Key Concept~~Concept~~characteristic	Findings	Implications	References
High-profile individuals (social influencers)	Influencers may increase the possibility of a cascade under certain circumstances, but this effect is marginal, and can be polarising. Attempts to leverage these actors are often not cost- or resource-effective. Outcomes are also unpredictable. Moreover, these nodes can often hinder cascades, as they may face lower payoffs or even penalties for changing (politicians, public figures, etc.)	To maximise efficiency, interventions or campaigns attempting to influence or effect behavioural change should not rely solely on highly visible or renowned social actors. Using a random selection of actors or following heuristics based on phenomena such as the friendship paradox may be more successful when contentious social changes are ongoing.	(Airoldi and Christakis, 2024; Bakshy et al., 2011; Bellotti et al., 2023; Centola et al., 2018; Efferson et al., 2020; Guilbeault and Centola, 2021; Hodas and Lerman, 2014; Watts, 2002; Watts and Dodds, 2007)
Frequency of exposure	People require repeated exposures to an alternative norm to change. Despite the	New or uncertain contexts, for example, norms related to climate change or when the causal	All

Key Concept~~characteristic~~	Findings	Implications	References
	complexities which may surround the relationship between exposure and response, the number of exposures over a certain period is by far the most robust predictor.	mechanism of norm change is unknown, require a careful strategy. Any intervention should focus on repeated exposure and ensure that information about the desired norm reaches people. It should also focus on ensuring information is not lost in noise, i.e. by avoiding overwhelmed channels such as social media.	
Trust	The strength of social connection heavily mediates the spread of contagion between individuals. This is not always the same as social proximity but is often correlated with it.	Trusted information sources are more effective at changing norms in their social networks than untrusted sources. This relationship is more severe for controversial or important norm changes. When considering these issues, or intervention potentials, trusted individuals related to the target group should be identified and leveraged for change.	(Bellotti et al., 2023; Christakis and Fowler, 2007, 2008; Fowler and Christakis, 2008; Iacopini et al., 2022; Nishioka and Hasegawa, 2022; Okada et al., 2022; Watts and Dodds, 2007)O
Network structure	Structured networks are more conducive to social tipping under complex contagion conditions. Although this varies with size, structural traits such as homophily and clustering allow a seed to amplify itself or gain a critical	Tight-knit, trusting, and close communities are necessary to allow a sufficient build-up of momentum for social change. This becomes more important with more controversial norm changes or those which provide a lower personal reward, or even a penalty.	(Bellotti et al., 2023; Centola, 2013; Okada et al., 2022; Reisinger et al., 2024; Watts and Dodds, 2007)

Key Concept~~Concept~~characteristic	Findings	Implications	References
	mass size to initiate a successful cascade.		
Type and context of norm change	Contagion dynamics differ substantially with the type of norm change, as well as the context. For example, educated people have a stronger influence on maternal health behaviour, as well as on smoking habits, but in some circumstances, village elders or knowledge holders only have a marginal influence over health behaviour, where the household is most important. Behaviour and knowledge norms spread differently in a population, even considering the same concept. Group identity and individual psychology may reduce the effects of exogenous attempts to promote norm change, e.g. policies. Different people's response to change differs depending on these circumstances.	Different societal norm changes require different solutions. These relationships should be explicitly studied on a per norm basis, e.g. consumption, flying, or driving behaviour. Policy interventions should rely on this knowledge. With regard to a given intervention target, fast behavioural adoption can still occur even if attitudes and knowledge are slower to change.	(Airoldi and Christakis, 2024; Bastos et al., 2013; Bellotti et al., 2023; Christakis and Fowler, 2007, 2008; Efferson et al., 2020; Fink et al., 2015; Fowler and Christakis, 2008; Hodas and Lerman, 2014; Romero et al., 2011)
Personal Preferences and	Personal preferences for a specific norm can affect cascade success in a	Understanding the distributions of preferences in terms of changing norms needs to be considered	(Efferson et al., 2020; Fahimipour et al., 2022;

Key Concept~~Concept~~characteristic	Findings	Implications	References
Heterogeneity	population. Not limited to how strongly different fractions of a population feel towards a certain norm, it also relates to the distribution of these feelings. For example, increasing the variance of this preference distribution tends to reduce norm spread.	when mass-scale changes in social norms are attempted. This is most relevant for governance personnel and policymakers. Intervention strategies can target groups with preferences that are more likely to facilitate the endogenous spread of norms.	Karsai et al., 2016; Wiedermann et al., 2020)

595 ~~Table 5: Critical mechanisms affecting social tipping processes on networks as identified by their frequency in the literature.~~

5.0 Discussion and Conclusion

Although complex contagion dynamics i~o~n networks are generally not amenable to reductionist methods of analysis (Shaliz & Thomas, 2011), our results show a broad level of agreement with the literature we reviewed regarding variables that affect the success of contagion. Clustering and structure in network topology dominate among these, as well as a high degree of trust
600 between social connections (Fig. 4). These factors are also critical in instances where norm change is difficult, payoffs for switching norms are low, social pressure from the in-group exists, or the norm is connected to social identity (Efferson, 2020). These things are now more relevant than ever in a time when some of our existing societal norms no longer fit the purpose of living in harmony with our planet and her boundaries (Otto et al., 2020b). A particularly relevant issue is the strong tie of group identity to problematic behavioural norms, which stymie the endogenous spread of social norms even after a targeted
605 intervention (Efferson et al., 2020; Ehret et al., 2022). In the light of climate change, these behavioural norms could correspond to things such as driving a large car, flying, or eating meat (Peattie, 2010a). Social tipping points research in SES calls for leveraging social tipping points to promote rapid societal change (Milkoreit, 2023; Winkelmann et al., 2020), but it does not address whether tipping is even possible with respect to certain behavioural norms or to the dynamics required for particularly recalcitrant or sensitive behavioural norms. Our review shows clearly that each norm change is highly dependent on the social
610 context, distribution of individual preferences, and heterogeneity. It also shows that a high variance in the distribution of personal preferences (social polarisation) is detrimental to changing social norms, which is an increasingly pressing issue (Frei et al., 2023).

Despite these considerations, we observed a clear non-linear trend when we investigated the critical mass required to induce tipping in a social network (Fig. 5). More concretely, we display evidence that a critical mass of around 25% of the population can precipitate a population-wide social tipping event. This finding is in line with existing speculations about critical mass estimates (Centola et al., 2018). The reason for this is not addressed in detail here, but recent analytical work (Karimi and Oliveira, in preparation) suggests that, under a 25% threshold, homophily limits the interaction potential of minorities, resulting in a "homophily trap". Not all social systems we analysed demonstrated social tipping (Fig. 5a), even when they displayed a rapid change in the fraction of norm adopters around 25%. This highlights that the 25% threshold identified in this paper is highly dependent on the state of the social system. This reflects existing claims about the conditionality of social tipping (Winkelmann et al., 2022). However, For the purposes of this study, our results answer our research question: They support the existence of a Pareto effect in social tipping dynamics. Although this finding should not be generalised to all realms of social norms and social systems to all realms of social norms and social systems, it is a helpful indicator and target to aim for if policymakers would like to push or monitor wide-scale social change. A notable case is the increasing popularity of vegetarianism in Germany. Figures currently show the vegetarian population to be at around 10% (Statista, 2023), which is within the range for social tipping, as shown by Fig. 5b. This case also demonstrates an increasing rate of change. A more generalizable result of our analysis is shown in Fig. 5b, which gives an estimate of the lower and upper ranges where tipping may occur.

The good agreement between empirical evidence and modelling results identified in this work supports the predictive power of models when used to investigate complex social contagion processes. This is particularly positive as considering the fact that each of the modelling results shown in Fig. 5 used different types and forms of models. These ranged from equation-based modelling to system dynamics and agent-based modelling using probabilistic approaches.

These modelling approaches must be empirically validated before they can be included in high-level or integrated modelling frameworks, which generally requires reliable heuristics which can be scaled up to an aggregate level, such as in IAMs (Trutnevyte et al., 2019). To introduce social complexity into larger models (Donges et al., 2020), the validation across modelling approaches may guide less computationally intensive models without losing accuracy. An example is the sigmoid norm adoption curve, as shown in Fig. 1b. This type of function is commonly used in system dynamics models to govern the rates of norm adoption, where the location of the inflection point is an important driver of large-scale social change in some contexts (Eker et al., 2019). There are several avenues to compare this norm adoption curve across methodological approaches, particularly from the network models or norm adoption time series analysed in this work. As a first approximation, this function could be parametrized using the data provided in this analysis (Fig. 5). More broadly, these norm adoption curves can be analytically derived from agent-based network models using approximation methods (Wiedermann et al., 2020), or reconstructed using time series from social media data, e.g. online service adoption (Karsai et al., 2016).

A key issue affecting this analysis was the small sample size, particularly with respect to the tipping point results discussed in section 4. The dimensionality, heterogeneity, and scale of variables relating to complex contagion in social networks across disciplines is such that it becomes prohibitively more difficult to process, categorise, and harmonise the findings across disciplines. In this sense, our work should be considered as an agenda-setting narrative review and by no means as an exhaustive survey of the literature. Further research would ideally gather more evidence for the existence of a Pareto effect by performing more rigorous statistical analyses and using a larger sample size. However, by identifying critical factors for successful social contagion in a broad pool of literature, this paper provides guidance and indicates where future research on related topics should occur. For example, research could be conducted in areas where agreement within the discipline is lacking, e.g. for factors like network connectivity, population size, and/or global information (see Fig. 4). We also only considered a one-dimensional aspect of social tipping, namely its reliance on critical mass as a time-dependent variable. Additionally, we neglected multistability, and assumed that there was no intermittent or regressive behaviour of the system once it had been tipped, which is a substantial issue to consider (Ferraz de Arruda et al, 2023). Although we attempted to cover most common network topologies, we decided that multi-layer networks were mostly beyond the scope of this review due to the added complexity normally associated with these approaches. Higher level network structures have a non-trivial effect on contagion dynamics (De Domenico, 2023; Zhang et al., 2023), and the field of social tipping and social contagion would generally benefit from a comparison between these structures and typical or single-layer network structures. The application of the second derivative to characterize tipping points serves as a useful initial approximation. However, its efficacy is contingent upon integration with additional criteria, such as those delineated in the definition of a social tipping event (Box 1). Future research should prioritize two avenues: (1) providing a robust theoretical justification for the use of the second derivative in this context, and (2) replicating the analysis using alternative frameworks, such as the criticality approach discussed in section 2.1. These efforts would serve to validate or refine the current methodology and potentially offer new insights into the dynamics of social tipping points.

Finally, our investigation was necessarily bound to the domain of social networks, and we did not consider performing alternative mapping between social entities. Many of the reviewed models are not always integrated into broader SES systems; either energy use, emissions, or environmental behaviour are absent. Future research should be directed towards reconciling or refining this gap between conceptual frameworks and integrated modelling, where more generic tipping dynamics are included in an SES model. Recent global SES models or World-Earth Models (WEMs) which explicitly simulate social dynamics on a micro scale (Donges et al., 2020), as well as contributions from ecological economics (Lamperti et al., 2018), are good starting points. This work has laid the foundation for further inroads.

Our macroscopic approach towards measuring tipping thresholds provides concrete critical mass ranges required to facilitate social tipping events via social networks. Where causality was deemed important, we supplemented this more approximate range with an investigation of the factors contributing to social tipping. Our focus on complex contagion and recalcitrant norm change means that our recommendations aid the navigation of inherently difficult societal transitions, such as the one to net-zero. On the flipside, in situations where the norm change is minor and possible, our range of tipping thresholds provides a concrete, empirically supported target for policymakers, encouraging the spread of easier-to-swallow sustainable norm change in social groups.

Code/Data availability

All data and code used to run the analysis, produce the figures, and harmonise the data_sets can be found on https://github.com/foroveralls/pareto_tipping.

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Author contributions

J.E, I.M.O, and J.F.D. developed the conceptual framework. J.E performed the literature review, data analysis, developed the figures, and led the writing of the manuscript with contributions from I.M.O, J.F.D, and F.T.

Conflict of interest statement

At least one of the (co-)authors is a member of the editorial board of *Earth System Dynamics*.

Appendix A

Term	Explanation
Avg degree	**The average number of connections per node in the network.**
Clustering	**The degree to which nodes in a network tend to cluster together.**
Degree heterogeneity	**The variability in the number of connections that nodes in the network have.**
Density	**The proportion of actual connections to the number of possible connections within the network.**
Geographical proximity	**The closeness in geographical location between nodes in a network.**
Global info/random rewiring	**The availability of global information in the network and the formation of random connections.**
Global information/weak ties	**The role of weak ties in providing access to global information.**
Homogenously mixing network	**A network where nodes are equally likely to connect with each other.**
Homophily	**The tendency of individuals to associate and bond with similar others.**
In-group conformity	**The tendency of individuals to conform to the norms and behaviours of their respective groups.**
Information transmission probability	**The likelihood of information being successfully transmitted in a pairwise interaction between between connected nodes in thethe network.**
Information transmission rate	**The rate at which information is transmitted through thethe network.**
Jointness of supply	**The extent to which the supply of a good, service, or benefit or service is shared among individuals.**
Lattice	**A structured network topology where each node is connected to its nearest neighbors.**
Linkage probability	**The probability of a connection forming between two nodes in the network.**
Memory length	**The amount of past information that nodes in the network retain.**
Network size	**The number of nodes in the network.**
Node degree (out)	**The number of outgoing connections from a node.**
Node degree (in)	**The number of incoming connections to a node.**

Term	Explanation
Population size	The total number of individuals within a given population or network.
Public awareness	The level of knowledge and awareness among the public or nodes in the network.
Random rewiring	The process of randomly rearranging connections within the network.
Seed degree (out)	The number of outgoing connections from the initial or seed nodes.
Seed social influence	The level of influence exerted by the seed nodes.
~~Social influence of seed nodes~~	~~The extent to which seed nodes can influence the norms and behaviours of other nodes in the network.~~
Social proximity	The closeness of nodes in the network based on geodesic distance (path distance)~~social relationships~~.
Social referents	Influential individuals or nodes within the network that serve as reference points for others.
Spreader influence	The ability of specific nodes, termed spreaders, to propagate information or norms efficiently within the network.
Structure	The arrangement of nodes and connections within the network.
Stubbornness	The resistance of nodes to change their state or adopt new norms and behaviours.
Threshold heterogeneity	The diversity in the thresholds that nodes have for adopting new norms or behaviours.
Tie strength	The intensity or closeness of the relationships between connected nodes.
Time window	The specific period considered for observing and analysing the dynamics of the network.
Trust	The level of confidence shared by nodes ~~nodes share~~ regarding the choice of their norms
Trust (in group)	The level of trust that individuals have within their respective groups or clusters in the network.
Weak ties	The connections between nodes that are not very strong or close.
Zealots	Highly committed or fervent nodes in the network that actively ~~propagate, or~~propagate or resist the propagation of specific norms or beliefs.

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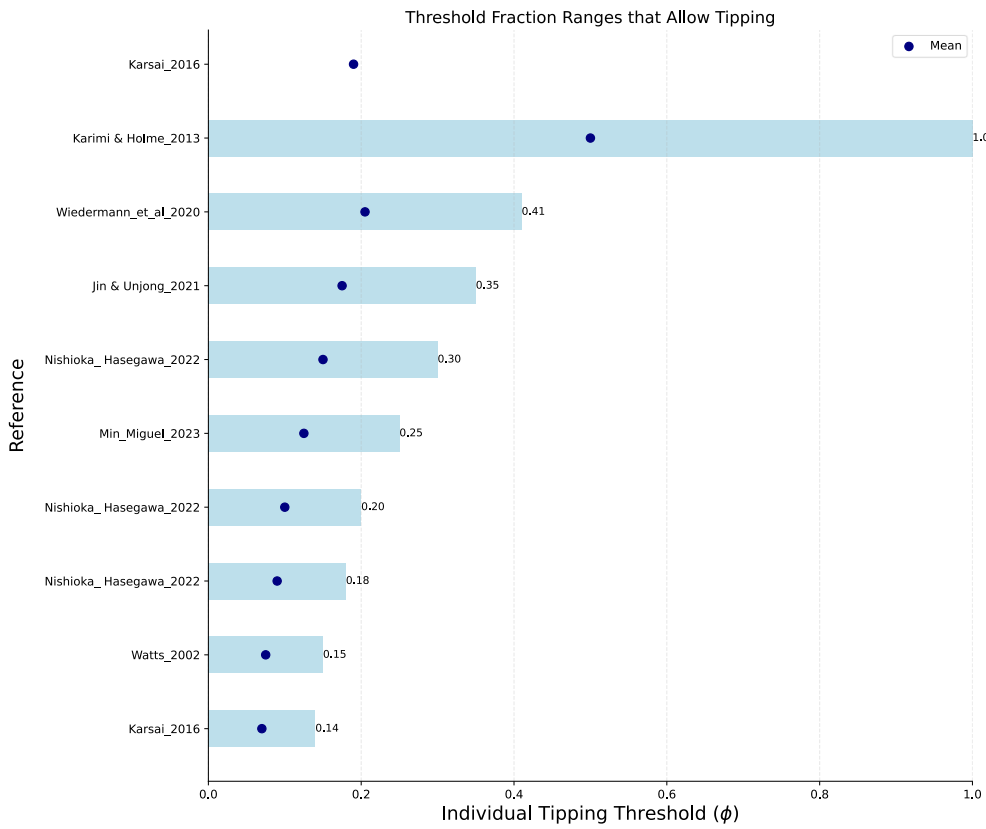
Figure B1: A range of individual tipping thresholds which allow for a social tipping event in a given population.

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