

Firn air content changes on Antarctic ice shelves under three future warming scenarios

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Abstract. The Antarctic firn layer provides pore space in which an estimated 94 to 96 % of the surface melt refreezes or is retained as liquid water. Future depletion of firn pore space by increased surface melt, densification and formation of low-permeability ice slabs can potentially lead to meltwater ponding, hydrofracturing and ice shelf disintegration. Here, we investigate the 21st century evolution of total firn air content (FAC) and accessible FAC (i.e. the pore space that meltwater can reach) across Antarctic ice shelves. We use the semi-empirical firn model IMAU-FDM with an updated dynamical densification expression to cope with changing climate forcing. The firn model is forced by general circulation model CESM2 output for three climate emission scenarios (SSP1-2.6, SSP2-4.5 and SSP5-8.5), dynamically downscaled to 27 km horizontal resolution by the regional climate model RACMO2.3p2. To estimate accessible FAC, we prescribe a relationship between ice-slab thickness and permeability. In our simulations, ice shelves in the Antarctic Peninsula and Roi Baudouin ice shelf in Dronning Maud Land are particularly vulnerable to total FAC depletion (> 50 % decrease by 2100), even for low (SSP1-2.6) and intermediate (SSP2-4.5) emission scenarios. Especially in the high (SSP5-8.5) emission scenario, the formation of ice slabs further reduces accessible FAC on ice shelves with low accumulation rates (current rates < 500 mm w.e. yr⁻¹), including many East-Antarctic ice shelves and on Filchner-Ronne, Ross, Pine Island and Larsen C ice shelves. These results underline the potentially large vulnerability of low-accumulation ice shelves to firn air depletion through ice-slab formation.

1 Introduction

The Antarctic ice sheet (AIS) has been losing mass since at least 2002 (Shepherd et al., 2018; Rignot et al., 2019), contributing ~10 % to global average sea level rise since 1993 (Oppenheimer et al., 2019). This mass loss is mainly driven by enhanced iceberg calving and basal melting beneath ice shelves (Smith et al., 2020). Both reduce the buttressing effect of ice shelves, allowing tributary glaciers to accelerate, thereby increasing ice discharge into the ocean. In the Antarctic Peninsula, the warmest region of Antarctica, mass loss is also driven by surface melt. Here, extensive melt has led to meltwater ponding and subsequently to ice-shelf disintegration by hydrofracturing, after which mass loss from tributary glaciers has accelerated (Rignot et al., 2004; Banwell et al., 2013).

Not all ice shelves are susceptible to meltwater induced hydrofracturing. Firstly, surface melt typically only leads to meltwater ponding when the firn layer lacks sufficient pore space for meltwater to percolate in and refreeze. Currently, an estimated

25 94 to 96 % of the surface melt on the AIS is retained within the firn (Medley et al., 2022; Van Wessem et al., 2018). Secondly, meltwater induced hydrofracturing also requires sufficient tensile stress. Hydrofracturing, in turn, only induces mass loss if the ice shelf provides substantial buttressing. Currently, 60 % of the ice shelves (by area) both buttress upstream ice and are vulnerable to hydrofracturing if inundated by meltwater (Lai et al., 2020). Hence, to assess the future stability of ice shelves and predict mass loss from the AIS, it is important to estimate the future evolution of its firn layer.

30 Under future warming, we anticipate more surface melt and rainfall, faster firn densification and increased formation of low-permeability ice slabs (i.e. ice layers > 1 m thick) (Ligtenberg et al., 2014; MacFerrin et al., 2019; Kittel et al., 2021; Vignon et al., 2021). These processes decrease the firn air content (FAC) and consequently enable firn saturation and ponding by meltwater. On the other hand, snowfall is projected to increase (Kittel et al., 2021), adding pore space to the firn. Climate models have recently been used to assess the impacts of future climatic changes on Antarctica's firn. van Wessem et al. (2023)
35 estimate future melt ponding on ice shelves based on the exceedance of a melt-over-accumulation ratio (MOA) of 0.7. Gilbert and Kittel (2021) use runoff from climate models as an indicator of meltwater ponding.

Offline firn models forced by output of regional climate models are useful tools to simulate the transient evolution of the firn layer, and can therefore also be used to assess meltwater ponding onset. The main advantage of using a firn model instead of a climate model is the lower computational cost, which enables a higher vertical resolution, a proper initialization of the firn layer
40 and more extensive sensitivity tests. The disadvantage of using an offline firn model is that interaction with the atmosphere is not possible. In contrast to diagnostic studies that use MOA thresholds (e.g., van Wessem et al., 2023), firn models simulate transient changes of the firn layer, thereby accounting for the time it takes to adjust to new climatic conditions. Firn models have been used to simulate the current (1979 - present) AIS firn layer (Gardner et al., 2023; Keenan et al., 2021; Medley et al., 2022; Veldhuijsen et al., 2023a) and its evolution in response to climate change (Ligtenberg et al., 2014; Kuipers Munneke
45 et al., 2014a).

The densification equations used in semi-empirical firn models are often based on assumptions of constant accumulation and temperature (Arthern et al., 2010), but simulating future firn evolution requires densification expressions that allow for changing climatic conditions. Moreover, using only total FAC to assess the firn's meltwater buffering capacity overlooks the impact of near-surface ice slabs formed by meltwater refreezing. Ice slabs are common in Greenland (MacFerrin et al., 2019;
50 Culberg et al., 2021) and have locally been observed in Antarctica on Larsen C ice shelf (Hubbard et al., 2016). They impede vertical meltwater percolation to deeper firn, limiting the fraction of the FAC that is accessible for meltwater. To assess the meltwater buffering capacity of firn, it is therefore important to include the impact of ice slabs (henceforth the accessible FAC).

Here, we use the IMAU Firn Densification Model (IMAU-FDM) for Antarctica, which has previously been evaluated for the contemporary climate (1979-2020) (Veldhuijsen et al., 2023a). In this study, IMAU-FDM is driven by realizations of CESM2
55 of the scenarios SSP1-2.6, SSP2-4.5 and SSP5-8.5 for the period 1950-2100, dynamically downscaled to 27 km resolution with RACMO2.3p2. To allow for changing climatic conditions, we updated and evaluated the densification equation (Sect. 2). In Section 3 we parameterise the accessible FAC based on ice slabs and FAC. In Sections 4 and 5, we present and discuss the response of the AIS firn layer to future warming scenarios in IMAU-FDM and specifically focus on the evolution of total FAC, accessible FAC and runoff. We finish with conclusions in Sect. 6.

IMAU-FDM is a semi-empirical, 1D firn densification model that simulates the evolution of firn depth, density, temperature and liquid water content. Firn compaction is calculated based on the semi-empirical dry-snow densification equations of Arthern et al. (2010). Meltwater percolation is simulated using the bucket method, whereby each firn layer has a maximum irreducible water content that decreases with increasing density (Coléou et al., 1999). The meltwater can percolate through all layers in a single time step, and (partly) refreezes when it reaches a layer with a temperature below the freezing point. Once meltwater has saturated the lowermost firn layer beyond the maximum irreducible water content, we assume that it leaves the firn column as runoff instantaneously. Standing water and lateral runoff over ice layers are currently not considered. For further details of the model setup we refer to Veldhuijsen et al. (2023a) and Brils et al. (2022). Version 1.2A of IMAU-FDM (referred to as FDM v1.2A) has been extensively evaluated over Antarctica against in situ observations of firn density and temperature, and remote sensing altimetry measurements (Veldhuijsen et al., 2023a). In this study we update the model to version IMAU-FDM v1.2AD (referred to as FDM v1.2AD) by implementing a densification expression that is suitable for transient climate change experiments, as is described in the next section.

2.1 Densification expression

The rate of the dry-firn densification ($d\rho/dt$) in IMAU-FDM v1.2A is calculated using the semi-empirical equation of Arthern et al. (2010) in combination with a calibration factor (MO_*):

$$\frac{d\rho}{dt} = MO_* D \dot{b} g (\rho_i - \rho) e^{\left(\frac{E_c}{RT} - \frac{E_g}{RT_{ave}}\right)} \quad (1)$$

in which D is a constant, \dot{b} is the long-term average accumulation rate ($\text{kg m}^2 \text{ yr}^{-1}$), g is the gravitational acceleration, ρ_i is the density of bubble free ice (917 kg m^{-3}), ρ is the layer density (kg m^{-3}), T is the instantaneous layer temperature (K), T_{ave} is the long-term average surface temperature (K), R is the universal gas constant, and E_c and E_g are the activation energies for creep (60.0 kJ mol^{-1}) and grain growth (42.4 kJ mol^{-1}). The constant D has different values above (0.03) and below (0.07) the critical density level of $\rho = 550 \text{ kg m}^{-3}$ to represent two distinct densification mechanisms (Herron and Langway, 1980). The calibration factor MO_* depends on annual average accumulation and is defined separately for $\rho < 550 \text{ kg m}^{-3}$ (MO_{550}) and for $550 < \rho < 830 \text{ kg m}^{-3}$ (MO_{830*}). These calibration factors are based on the ratio of modelled and observed values of depths of critical density levels $\rho = 550 \text{ kg m}^{-3}$ (z_{550}) and $\rho = 830 \text{ kg m}^{-3}$ (z_{830}), where $z_{830*} = z_{830} - z_{550}$. MO_{550} and MO_{830*} were chosen as logarithmic and power-law functions, respectively, of the long-term average accumulation rate:

$$MO_{550} = \alpha - \beta \ln(\dot{b}) \quad (2)$$

$$MO_{830*} = \delta \dot{b}^{-\epsilon} + \phi \quad (3)$$

in which α , β , δ , and ϵ and ϕ are fit coefficients. Equations (1) to (3) use the long-term annual average accumulation rate (\dot{b}) as a proxy for overburden pressure, and Eq. (1) uses long-term annual average temperature (T_{ave}) in the grain growth part of the exponential term. To include the effect of a changing climate on firn densification, previous studies with IMAU-FDM used running average accumulation and temperature over the 40 years preceding each time step (Ligtenberg et al., 2014;

Kuipers Munneke et al., 2014a). Since there is a large spatial variation in firm age across the AIS, e.g. the firm age at the pore close off depth ranges from 20 to ~ 3200 years (Veldhuijsen et al., 2023a), the firm temperature and overburden pressure will change at different rates across the AIS in a warming future climate. In addition, the change in temperature and overburden pressure will also differ vertically within the firm column. Advection and conduction transport heat vertically, however firm has a relatively low thermal conductivity (0.2 to $2 \text{ W m}^{-1} \text{ K}^{-1}$, Calonne et al. 2019). For example, Muto et al. (2011) show that firm temperature throughout a firm column differs by about 1 K due to historical temperature trends in East Antarctica of 1 to 1.5 K over 50 years. So, using a running average of the accumulation and firm temperature is a crude approximation to capture the transient response of firm.

In this work, we aim to resolve this by replacing \dot{b} and T_{ave} in the densification equations (Eqs. 1 to 3), while staying as close as possible to FDM v1.2A. To do so, we revert to the complete transient, dynamical model of Arthern et al. (2010) for the evolution of firm density. Eq. (4) is derived from this equation by using several simplifying assumptions such as steady state accumulation. The equation is based on evolving squared grain size (r^2 , mm^2), and overburden pressure (σ , $\text{kg m}^{-2} \text{ s}^{-1}$), including the MO_* term:

$$\frac{d\rho}{dt} = \text{MO}_* k_c (\rho_i - \rho) e^{\left(\frac{E_c}{RT}\right)} \frac{\sigma}{r^2} \quad (4)$$

where k_c is a constant. The evolution of r^2 for one time step includes dry-snow metamorphism:

$$\frac{dr^2}{dt} = k_g e^{\left(-\frac{E_g}{RT}\right)} \quad (5)$$

where k_g is a constant. In case of refreezing, r^2 is calculated as the mass-weighted average of the solid firm grain size and refrozen liquid water grain size, under the condition that refreezing can only increase the grain size. The initial (0.03 mm) and refreezing (0.25 mm) grain sizes are taken from van Dalum et al. (2022). To determine MO_* (Eqs. 2 and 3), we replace \dot{b} in those equations by the local (layer) long-term mean accumulation rate (\dot{b}_{loc}) defined as:

$$\dot{b}_{loc} = \frac{\sigma}{gA}. \quad (6)$$

wherein A is the firm age. For updates in the layer merging and splitting approach we refer to Text S1.

2.2 Atmospheric forcing

IMAU-FDM is forced at the upper boundary with 3-hourly values of snowfall, sublimation, snowdrift erosion, 10-m wind speed, surface temperature, snowmelt and rainfall from the Regional Atmospheric Climate Model RACMO2, version 2.3p2, (RACMO2.3p2). This regional climate model is used to dynamically downscale ERA5 reanalysis data (Hersbach et al., 2020) for the contemporary climate (RACMO2.3p2-ERA5) and Community Earth System Model version 2 model output (CESM2, Danabasoglu et al. 2020) for future projections (RACMO2p3-CESM2) to 27 km resolution. RACMO2.3p2-ERA5 aims to provide an accurate description of past AIS weather (and climate) from 1979 - present, and has been thoroughly evaluated (van Wessem et al., 2023).

For future projections, van Wessem et al. (2023) used RACMO2.3p2 to dynamically downscale a historical CESM2 realization (1950-2014) and one realization of each of the low-, middle- and high-emission future (2015-2100) projection scenarios (SSP1-2.6, SSP2-4.5 and SSP5-8.5, respectively). CESM2 simulates the coupled interactions between the atmosphere-ocean-land components of the climate system at the global scale at 1 degree horizontal resolution (Danabasoglu et al., 2020), and has been thoroughly evaluated over the AIS (Gorte et al., 2020; Dunmire et al., 2022). The model has a relatively detailed representation of polar processes and is among the best CMIP6 models in representing the present Antarctic SMB (Gorte et al., 2020). The projected Antarctic warming in SSP5-8.5 (+7.7 °C) in CESM2 is stronger than the mean warming in CMIP6 models (+5 °C), which enables us to assess the AIS firn layer response to strong warming.

RACMO2.3p2-CESM2 time series of mean annual surface temperature, accumulation and surface melt over the AIS are shown in Fig. S1. Compared to RACMO2.3p2-ERA5 for the overlapping period (1979-2014) we find a temperature bias of -1.2 °C over the AIS, an accumulation bias of -7.6 mm w.e. yr⁻¹ (-4 %) and a snowmelt bias of -1.0 mm (-11 %). These biases can be explained by the cold bias in CESM2 (Dunmire et al., 2022). RACMO2.3p2-CESM2 has also been used by van Wessem et al. (2023) in their assessment of AIS meltwater ponding and compares well to meltwater lake volume observations of the Sentinel-2 satellite. Figure S2 shows the differences in mean annual surface temperature, accumulation and surface melt in the period 1979-2014 between RACMO2.3p2-CESM2 and RACMO2.3p2-ERA5. Accumulation and temperature in RACMO2.3p2-CESM2 are in general lower, except in Dronning Maud Land and Enderby Land. Temperatures are most notably lower on the Ross ice shelf and in West Antarctica. Surface melt is in general lower, except in Dronning Maud Land and on Larsen C ice shelf.

2.3 Experimental setup

The four IMAU-FDM versions used in this study differ by the dry-snow densification expression (non-dynamical or dynamical, Sect. 2.1) and the indirect atmospheric forcing (ERA5 or CESM2, Sect. 2.2). Abbreviations and characteristics of the IMAU-FDM versions used are listed in Table 1. FDM v1.2AD-C, the dynamical model indirectly forced by CESM2, is used to simulate future firn evolution over the AIS. FDM v1.2A-E and FDM v1.2AD-E are used for evaluation of the dynamical model over the current climate (Sect. 2.4) and FDM v1.2A-C to assess the impact of the dynamical model on future firn evolution (Sect. 4.5, tested for SSP5-8.5). FDM v1.2A-E provides firn characteristics over the AIS from 1979 - present and has been extensively evaluated (Veldhuijsen et al., 2023a). Details about the model initialization are given in Text S2.

2.4 In situ measurements

To calibrate and evaluate the firn model we compare the overlapping historical part (1979-2014) of the FDM v1.2A-E, FDM v1.2AD-E and FDM v1.2A-C simulations to in situ firn core density measurements (Fig. 1). We used 112 density profiles across the AIS, by combining multiple published datasets (van den Broeke, 2008; Schwanck et al., 2016; Bréant et al., 2017; Fernandoy et al., 2010; Montgomery et al., 2018; Fourteau et al., 2019; Olmi et al., 2021; Winstrup et al., 2019). Detailed information about the dataset is presented in Veldhuijsen et al. (2023a)

Table 1. Abbreviations and characteristics of IMAU-FDM versions used in this study.

Abbreviation	Forcing of RACMO2.3p2	Dry-snow densification	Period
FDM v1.2A-E ^a	ERA5	Arthern et al. (2010) (Eq. 1)	1979-2020
FDM v1.2A-C	CESM2	Arthern et al. (2010) (Eq. 1)	1950-2100
FDM v1.2AD-E	ERA5	Dynamical version (Eq. 4)	1979-2020
FDM v1.2AD-C	CESM2	Dynamical version (Eq. 4)	1950-2100

^aVeldhuijsen et al. (2023a)

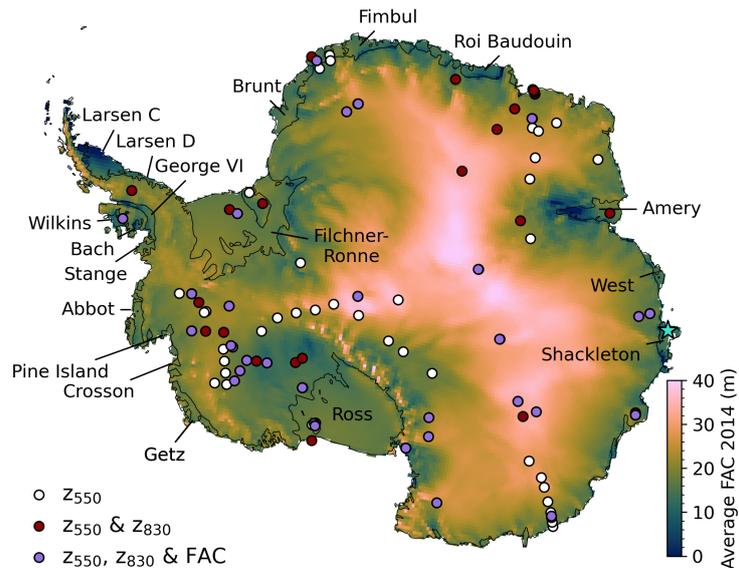


Figure 1. Map of Antarctica showing average firn air content (FAC) for 2014 from FDM v1.2AD-C. The circles indicate locations of in situ observations of the depth of critical density level $\rho = 550 \text{ kg m}^{-3}$ (z_{550}), the depth of critical density level $\rho = 830 \text{ kg m}^{-3}$ (z_{830}) and of firn air content (FAC). The blue star indicates the location of Fig. 3b. The names indicate the ice shelves referred to in the text.

2.5 Calibration

155 The densification equation of the non-dynamical model indirectly forced by ERA5 (FDM v1.2A-E) has been calibrated in Veldhuijsen et al. (2023a). To calibrate the dry-snow densification rate of the dynamical model versions, we first performed simulations for locations with firn density observations (Fig. 1), without MO corrections, i.e. in which the MO values are equal to 1. The resulting MO fits and statistics are shown in Fig. S3. All model versions yield similar R^2 values. The MO_{550} fits of the dynamical versions are steeper and higher than FDM v1.2A-E, due to a relatively low ratio of overburden pressure and grain size in the upper firn (above z_{550}). In addition, the CESM2 forcing alters the MO_{550} and MO_{830*} fits, due to differences in modelled accumulation rates and surface temperature.

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2.6 Performance of the dynamical densification model

We evaluate the performance of the dynamical model, FDM v1.2AD, by comparing it with FDM v1.2A and in situ observations. For the latter, we compare simulated to observed depths of the critical density levels $\rho = 550 \text{ kg m}^{-3}$ (z_{550}) and $\rho = 830 \text{ kg m}^{-3}$ (z_{830}), and FAC (Figs. 2a,b and c). Both versions indirectly forced by ERA5 yields similar root mean square error (RMSE) and bias, which indicates a similar performance of the updated dynamical firm model for the same forcing. The CESM forced run with the dynamical model yields slightly higher RMSE, indicating that the CESM2 forcing, which is not constrained by observations like ERA5, results in a slightly poorer performance.

The average absolute difference in FAC over the AIS between FDM v1.2AD-C and FDM v1.2A-E for the period 1979-2014 (the overlapping historical period) is 5.2 % (Fig. S4b). This is caused by a combination of the updated dry-snow densification expression and different climatic forcing. Conversely, the absolute FAC difference over the period 1979-2020 between FDM v1.2AD-E and FDM v1.2A-E, caused solely by the updated dry-snow densification expression, averages only 1 % (Fig. S4a). Over the grounded ice, the differences are even smaller (0.6 %), while they are higher in regions with high MOA, such as on Wilkins and Larsen C ice shelves, and around the grounding lines of e.g. Roi Baudouin and Amery ice shelves. The reason is that densification is enhanced in regions with high MOA (Fig. S4c), consistent with theoretical considerations that a MOA > 0.7 initiates depletion of pore space (Pfeffer et al., 1991; van Wessem et al., 2023). Overall, the results of the (non-)dynamical versions are similar over the historical period, which is as expected since there are no trends in accumulation and temperature, reducing the impact of the dynamical densification formulation. The difference in FAC evolution in response to future warming scenarios between the (non-)dynamical versions is discussed in Sect. 4.5.

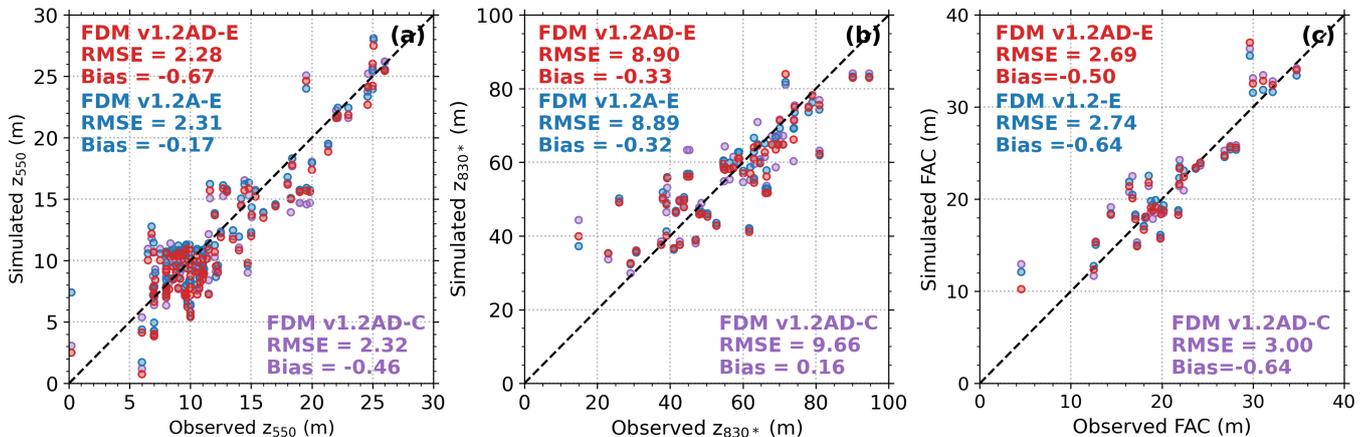


Figure 2. Simulated against observed (a) z_{550} , (b) z_{830^*} and (c) firm air content (FAC) for FDM v1.2AD-E, FDM v1.2A-E and FDM v1.2AD-C.

The dynamical FDM version (FDM v1.2AD-C) is used to simulate future FAC evolution to assess the vulnerability of ice shelves to meltwater ponding. However, meltwater refreezing can form ice slabs in firn, which can impede meltwater percolation to deeper layers, thereby reducing the firn's meltwater buffering capacity (Machguth et al., 2016; MacFerrin et al., 2019; Culberg et al., 2021). That is why in addition to FAC (henceforth referred to as total FAC), we also calculate accessible FAC.

185 To do so, we use ice layer thickness as a measure of their permeability. It is important to note that the calculation of accessible FAC is a post-processing step, and ice layers within the firn model itself are permeable for vertical liquid water movement.

Figure 3a shows relationships between ice layer thickness and permeability from several observational studies. A small-scale field experiment conducted in Greenland shows that ice layers of 0.12 m can still be completely permeable for liquid water (Samimi et al., 2020). On the other hand, in another small-scale field experiment in Greenland, ice lenses of only 0.03-0.05 m
190 have also been found to be partly impermeable (Clerx et al., 2022). Samimi et al. (2021) assume that ice layers thicker than 0.5 m act as impermeable barriers and prescribe a non-linear decrease in permeability between 0.1 and 0.5 m. These results also show that processes of meltwater percolation and refreezing occur at a small scale. Firn is therefore spatially heterogeneous (e.g., Samimi et al., 2020; Vandecrux et al., 2019), and on a larger horizontal scale, such as that of a FDM grid cell (27 km), ice layers can be discontinuous, allowing meltwater to still percolate through. For ice layers to be impermeable on the model-
195 resolved spatial scale, this requires at least a larger thickness than the ones found in the small-scale field experiments. Here, we also assume that lateral connectivity of ice layers increases with ice thickness.

Radar data and firn cores show that horizontally continuous > 1 m thick ice slabs typically develop on top of refrozen ice layers after extreme melt years. A radar study on Devon Ice Cap, Canada, revealed that an initially widespread ice layer that formed during an extreme melt year, thickened by between 0.5 and 4.5 m over the subsequent 5 years (Gascon et al., 2013).
200 Similarly, over time thickening ice layers of 1-2 m formed in Greenland following an extreme melt year (Culberg et al., 2021). While these large-scale radar observations do not give an exact relation between thickness and permeability, they do give an indication that ice layers thicker than 0.5 m are at least partly impermeable on a larger scale. In addition, firn temperature measurements in Greenland show that no percolation occurred through a 5.5 m thick ice slab even during an extreme melt year (Charalampidis et al., 2016). Based on these observations, we propose a relationship between ice layer thickness (z) and
205 permeability factor (Pf) (Fig. 3a), using a sigmoid function:

$$Pf = \frac{1 + b + (az)}{b + e^{(az)}} \quad (7)$$

in which a and b are tuning coefficients, for which we propose $a = 1.130$ and $b = 3.245$. We use a sigmoid function because it has a characteristic S-shaped curve, representing that at a large spatial scale thin ice lenses are permeable, while even very thick ice layers only approach complete impermeability.

210 Since exact observations that evaluate the permeability as a function of ice layer thickness at the regional scale are lacking, the relationship in Eq. (7) must be regarded as a rough estimate. In addition, the location of the observations have a larger surface slope (> 0.4 °) (Yi et al., 2005) than most Antarctic ice shelves (< 0.15 °) (Slater et al., 2018). The small surface slopes on ice shelves results in less lateral flow on top of refreezing layers, which may impact the permeability. Considering these

uncertainties, we test the sensitivity of our results to adjusted the values of a (1.119 and 1.250) and b (13.490 and 0.0594), indicated by the envelope of the black shaded surfaces in Fig. 3a. In addition, we also include total FAC, which represents full permeability.

To calculate the accessible FAC of a layer, its FAC is multiplied with the permeability factors of all overlying ice layers. E.g., if two distinct ice layers with $Pf = 0.5$ are overlying a firm layer, the FAC of that layer is multiplied twice by 0.5 to yield its accessible FAC. The sum of accessible FAC of the individual layers equals the firm accessible FAC. An ice layer can range from a single to numerous model layers. Impermeable ice layers are usually defined as having a density $> 830 \text{ kg m}^{-3}$ (the pore close-off density). Here, we use a threshold of $> 900 \text{ kg m}^{-3}$, which corresponds to the density of refreezing ice layers in the model. This choice limits the impact on the accessible FAC of changes in high-density non-refreezing layers in the deep firm. Figure 3b shows the impact of ice layer formation on accessible FAC for an example location in a high emission scenario (SSP5-8.5). As can be seen, ice layer formation from 2060 onwards depletes the accessible FAC compared to the total FAC. Henceforth, we refer to (a set of) ice layers that have a substantial impact on the accessible FAC as ice slabs.

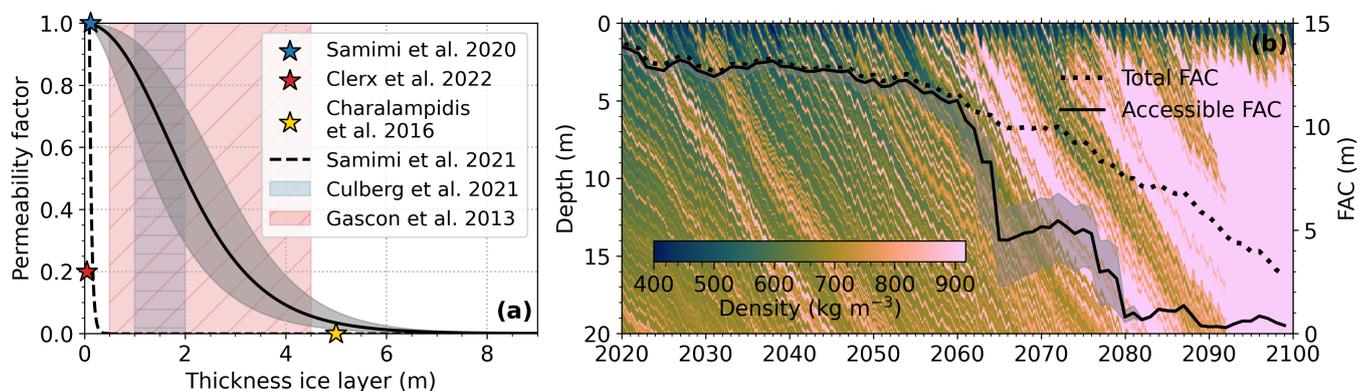


Figure 3. (a) Relations between the ice layer thickness and permeability factor, including results from in situ observations (stars), a previous estimate (dotted line), observed ranges of reduced permeability from radar observations (colored shaded surfaces) and a relationship proposed here (solid line) including tested sensitivity ranges (black shaded surface). (b) Example plot of simulated density including total firm air content (FAC) and accessible FAC (calculated using the proposed relationship from panel (a)) simulated with FDM v1.2AD-C for SSP5-8.5. The location is at Shackleton ice shelf and is indicated by the blue star in Fig. 1.

4 Results

4.1 Total and accessible firm air content in AD 2100

Using the updated firm model FDM v1.2AD, we project the firm evolution over the AIS for the period 1950-2100 driven by RACMO2.3p2-CESM2 for climate scenarios SSP1-2.6, SSP2-4.5 and SSP5-8.5. Figures 4a,b and c show the relative change of total FAC by 2100 compared to 2014. On average, FAC over the grounded ice decreases by -0.7, -1.1 and -2.3 % for scenarios

SSP1-2.6, SSP2-4.5 and SSP5-8.5, respectively. This implies that the effect of enhanced precipitation is weaker than the effect of firn warming. For ice shelves, FAC decreases by -16 %, -20 % and -42 % for scenarios SSP1-2.6, SSP2-4.5 and SSP5-8.5, respectively. For SSP1-2.6 and SSP2-4.5 we find a substantial FAC decrease on Larsen C (-70 % and -75 %), Wilkins (-59 and -58 %), Roi Baudouin (-67 and -81 %), George VI (-47 and -56 %) and Bach (-59 and -66 %) ice shelves. For SSP5-8.5, in addition we find a substantial FAC decrease for ice shelves in Dronning Maud Land, such as Fimbul ice shelf (-91 %), and elsewhere for Abbot (-76 %), Pine Island (-74 %), West (-83 %) and Shackleton (-76 %) ice shelves. FAC decrease on Ross and Filchner-Ronne ice shelves is more modest (-21 and -19 %).

Figures 4d, e and f show the relative change in accessible FAC by 2100 compared to 2014, and Figs. 4g, h and i show the difference between the total FAC change and accessible FAC change by 2100. The figures show that enhanced depletion of accessible FAC by ice layer formation mainly occurs over the ice shelves, and is limited over the grounded ice sheet, except for the region east of the Ross ice shelf under SSP5-8.5. For SSP1-2.6 the decrease of accessible FAC is accelerated compared to the total FAC on Larsen D ice shelf (from -46 to -65 %), but on average the difference over all ice shelves is limited (-16 vs -18 %), indicating limited ice layer formation. For SSP2-4.5 the depletion is accelerated on e.g. Amery (from 30 to -49 %), Larsen D (from -49 % to -68 %) and Fimbul (from -43 to -55 %) ice shelves. The average difference over all ice shelves under this scenario is limited as well (-19 vs -23 %). In contrast, for SSP5-8.5 the accelerated accessible FAC depletion is substantial (on average from -42 to -53 %), and especially pronounced on e.g. Amery (from -54 % to -92 %), Shackleton (from -76 to -94 %), Brunt (from -73 to -93 %) and Filchner-Ronne (from -18 to -33 %).

4.2 Climatic drivers of changes in firn air content

In this section, we link changes in FAC under SSP5-8.5 to various climate variables. Due to low temperatures in the interior ice sheet, 76 % of the AIS does not experience melt by the end of the century even in this strong warming scenario. Here, changes in FAC are solely driven by increasing firn temperature and changing accumulation rates. In 42 % of melt-free locations, FAC decreases by 2100, while in the remaining 58 %, FAC increases. In Fig. 5a we show the relative change in total FAC by 2100 compared to 2014 for non-melt locations as a function of temperature and accumulation change. For 4-6 °C warming an increase of at least 30 % accumulation is needed to compensate for the increased densification, whereas for > 8 °C warming, an increase of at least 70 % accumulation is required. Because of these compensating mechanisms, for most of the AIS the FAC remains relatively stable.

When we compare the change in FAC of the entire AIS to current climate conditions (1950-2014, Fig. 5b), we observe the largest relative decrease in FAC (-55 %) in currently warm regions (> -22 °C) receiving less than 1000 mm accumulation annually. For high-accumulation regions (> 1,000 mm w.e. yr⁻¹), such as parts of Getz ice shelf and the northwestern part of the Antarctic Peninsula, the decrease in FAC is notably smaller (-23 %). FAC also slightly decreases (-14 %) in colder regions (-34 and -24 °C) with low accumulation (< 100 mm w.e. yr⁻¹). Large differences over the period 2060-2100 between total FAC and accessible FAC mainly occur in current intermediate warm (-28 to -16 °C) and relatively dry (< 500 mm w.e. yr⁻¹) locations (-0.85 m) (Fig. 5c), and most prominently in regions with temperatures between -22 and -18 °C and accumulation rates between 100 and 400 mm w.e. yr⁻¹ (-1.6 m). We select this period as this is when total and accessible FAC start to

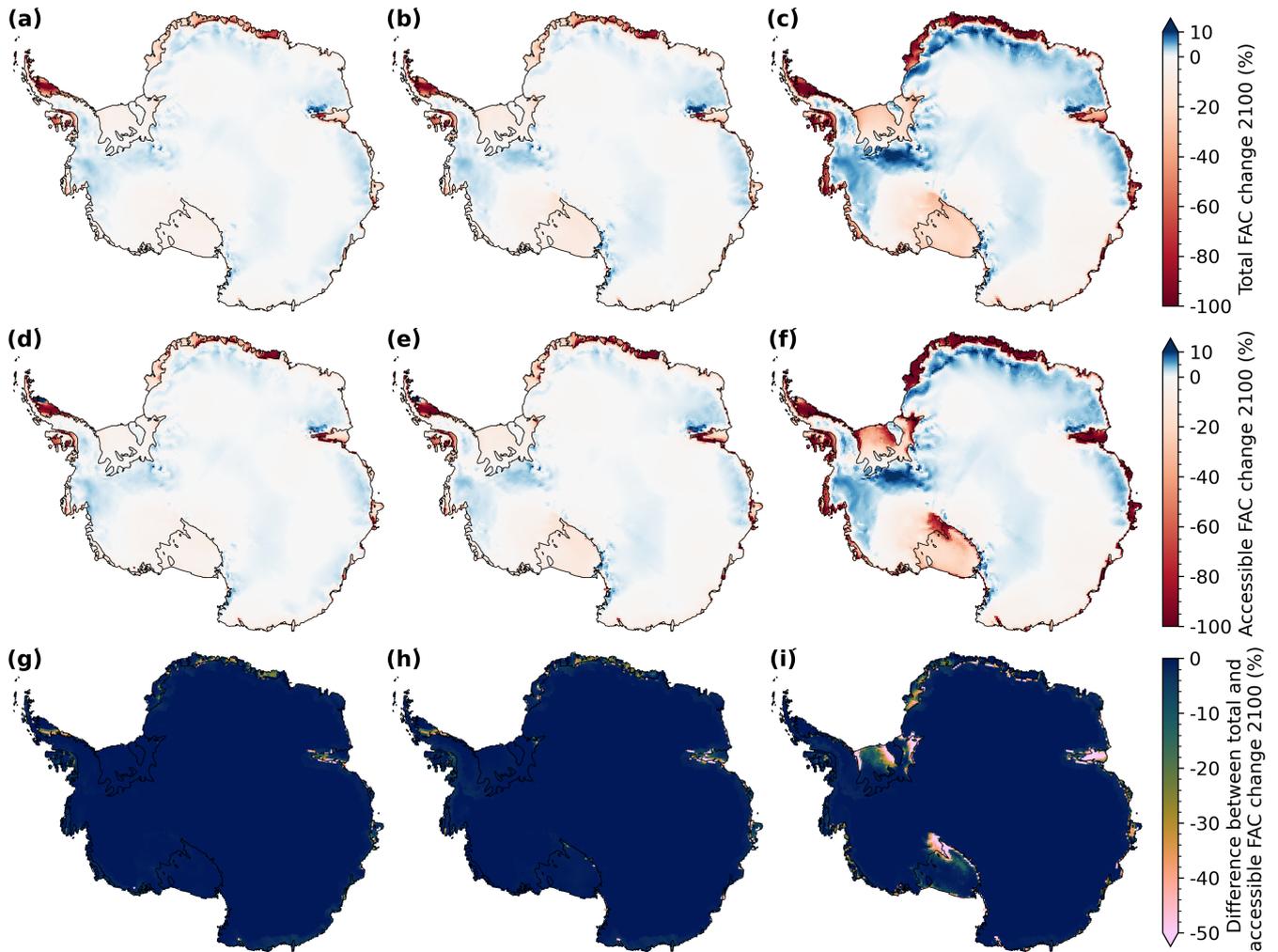


Figure 4. Relative change in total firm air content (FAC) (first row) and accessible FAC (second row) by 2100 compared to 2014 for (a,d) SSP1-2.6, (b,e) SSP2-4.5 and (c,f) SSP5-8.5. Please note the different scales for decreasing (red) and increasing (blue) FAC. (g,h,f) Difference between the total FAC change by 2100 (first row) and accessible FAC change by 2100 (second row).

265 diverge. For colder initial conditions, the projected melt is too weak to allow for ice lens formation, while for warmer locations, the firm layer is projected to completely disappear in 2090-2100. In the wettest locations ($> 600 \text{ mm w.e. yr}^{-1}$), the average differences are smaller (-0.59 m). The patterns in Fig. 5 are in general similar for SSP1-2.6 and SSP2-4.5, albeit with smaller magnitudes (Fig. S5).

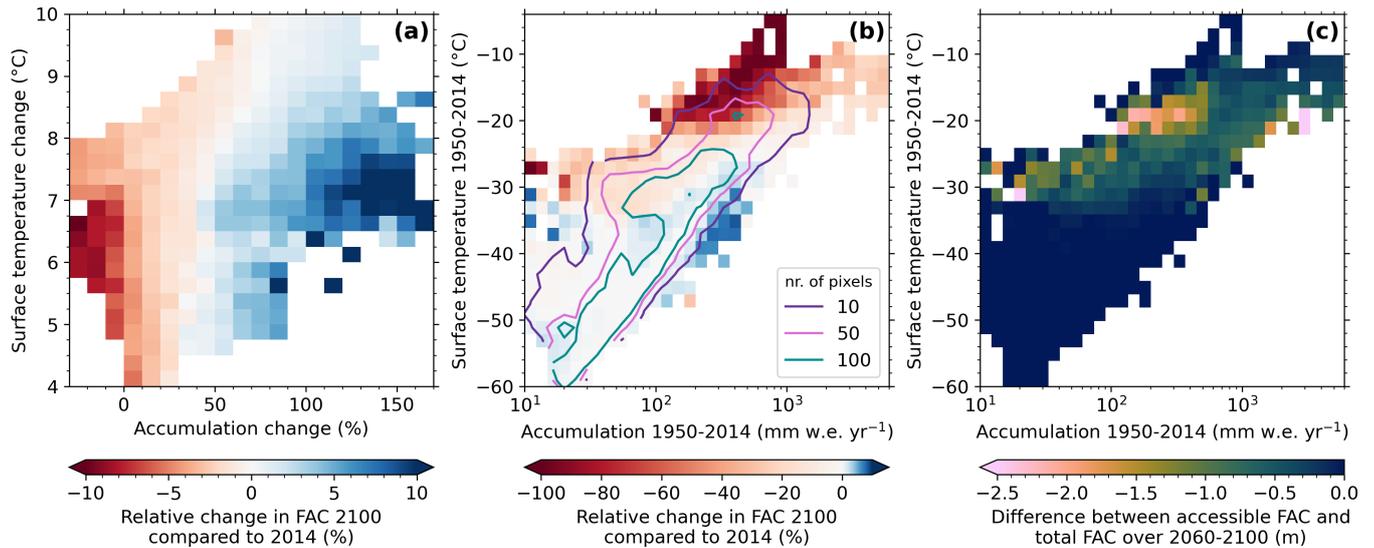


Figure 5. Relative change in total firm air content (FAC) by 2100 for SSP5-8.5 compared to 2014 (a) as a function of temperature change and accumulation change by 2100 compared to 2014 for locations that do not experience melt by the end of the century in SSP5-8.5 and (b) as a function of annual average accumulation and temperature (1950-2014) for the entire AIS. (c) Average difference between accessible FAC and total FAC (accessible FAC minus total FAC) in 2060-2100 for SSP5-8.5 as a function of annual average accumulation and temperature (1950-2014) for the entire AIS. Contour lines in (b) indicate the number of pixels per bin. Please note the different scales for decreasing (red) and increasing (blue) FAC in panel (b).

4.3 Temporal evolution of total and accessible firm air content, and runoff over ice shelves

270 Time series of total FAC, accessible FAC and runoff extent for 12 major ice shelves under SSP2-4.5 and SSP5-8.5 are shown in Fig. 6 (See Fig. S6 for SSP1-2.6). From 2020 onwards there is a gradual decrease in FAC on all ice shelves for all scenarios. An accelerated FAC depletion occurs around 2030 on Antarctic Peninsula (Larsen C, Wilkins and George VI) ice shelves and Roi Baudouin ice shelf, irrespective of the scenario. Further ahead, for SSP5-8.5 enhanced FAC depletion on Fimbul, Abbot, Pine Island and Shackleton ice shelves is projected around 2050-2060. Under SSP1-2.6 and SSP2-4.5 the Fimbul ice shelf also
 275 experiences enhanced FAC depletion around 2050-2060. By 2100, the Antarctic Peninsula ice shelves and the Roi Baudouin ice shelf are projected to retain less than 6 m FAC under SSP2-4.5. Under SSP5-8.5, FAC levels are anticipated to decrease by over 4 m across all ice shelves by 2100, resulting in less than 3 m of FAC remaining on the Roi Baudouin, Larsen C, Wilkins, Fimbul and Shackleton ice shelves.

Differences between the accessible and total FAC mainly occur under SSP5-8.5, and are most pronounced on Shackleton,
 280 Fimbul, Pine Island, Roi Baudouin, Amery and Filcher-Ronne ice shelves, where depletion is accelerated by up to 20 years and up to 5 m. These ice shelves have in common that they are currently relatively dry (< 500 mm w.e. yr⁻¹). On most ice shelves, the difference increases gradually. However, at Fimbul and Shackleton ice shelves, ice layer formation around 2060

results in a rapid depletion of more than 5 m (> 50 %) accessible FAC within 5 years. This coincides with an episode of high melt rates (25 % higher on Fimbul and 38 % higher on Shackleton compared to the previous and following 5 years). On the other hand, on the currently relatively warm (> -19 °C) and wet (> 600 mm w.e. yr⁻¹) Wilkins, Getz, Abbot and George VI ice shelves there remains little difference between accessible and total FAC, which corresponds with Fig. 5c. For SSP2-4.5 there is generally little difference between total FAC and accessible FAC, except for Roi Baudouin, Fimbul and Amery ice shelves (>1 m reduction in accessible FAC compared to total FAC after 2070).

The runoff extent is the areal fraction of the ice shelf where runoff is generated in a given year. Since ice layers are fully permeable for meltwater percolation in IMAU-FDM, the runoff time series are closely related to the total FAC time series, with some differences (Figs. 6e,f). For Wilkins, Abbot and George VI ice shelves the runoff extent is large compared to the FAC depletion (>50 % runoff extent with 5 m FAC), in contrast to Shackleton and Fimbul ice shelves, where the runoff extents are about 45 % with 2.5 m FAC. The reason for the high runoff extent on Wilkins, Abbot and George VI ice shelves is the combination of high accumulation and high melt rates. The high melt allows for saturation of a thick firn layer, which is maintained by high accumulation. In addition, runoff here also occurs year-round from firn aquifers, which are perennial subsurface bodies of liquid water, that become more ubiquitous in a warmer Antarctica (Bell et al., 2018).

For Wilkins ice shelf we see a quick increase from 0 to > 90 % runoff extent for both scenarios, which indicates limited spatial variation in firn state across the ice shelf. On the other hand, Larsen C, a larger ice shelf with large latitudinal extent and climate gradients, shows a gradual southward migrating increase in runoff extent. On average, 6 % and 25 % of the entire Antarctic ice shelf area experiences runoff in 2100 under SSP2-4.5 and SSP5-8.5, respectively, indicated by the black line.

4.4 Ice layer formation and its climatic drivers

In the previous sections, we showed that ice layer formation on some ice shelves causes enhanced depletion of accessible FAC. Figures 7a and b respectively show the maximum absolute difference and the corresponding relative difference between total FAC and accessible FAC over the period 1950-2100 for SSP5-8.5. The differences are highest on ice shelves in Dronning Maud Land and on the Amery, West, Shackleton, Ross and Filchner-Ronne ice shelves. In contrast, for Ross ice shelf the maximum difference is found near the grounding line, and for Filchner-Ronne ice shelf near the seaward edge. The differences are lowest in the Bellingshausen Sea region, on ice shelves such as Wilkins, George VI, Stange and Abbot, and on the Getz and Crosson ice shelves (< -3.9 m and < -47 %), which are among the warmest and wettest ice shelves of the AIS (> -19 °C and > 600 mm w.e. yr⁻¹). The absence of ice slabs under these conditions is also depicted in Fig. 5c.

In Figs. 7c to h we zoom in on FAC and accessible FAC time series for selected locations plotted together with accumulation, melt and associated MOA. At Amery, Shackleton and Filchner-Ronne ice shelves, we see that extreme melt seasons can cause a persistent reduction in accessible FAC (indicated by the grey shaded area). We define a melt season as extreme when the melt exceeds the 93rd quantile of the detrended time series. The 5-year running average MOA values for which this occurs on Amery, Shackleton and Filchner-Ronne are between 0.59-0.71. On Larsen C, where melt is more constant over the years, this occurs for a MOA of about 1.04. On the wetter Wilkins location, ice layer formation is limited, even though the firn layer becomes completely depleted and a MOA of 1 is exceeded. In addition, on the wetter Getz ice shelf location, ice layer formation

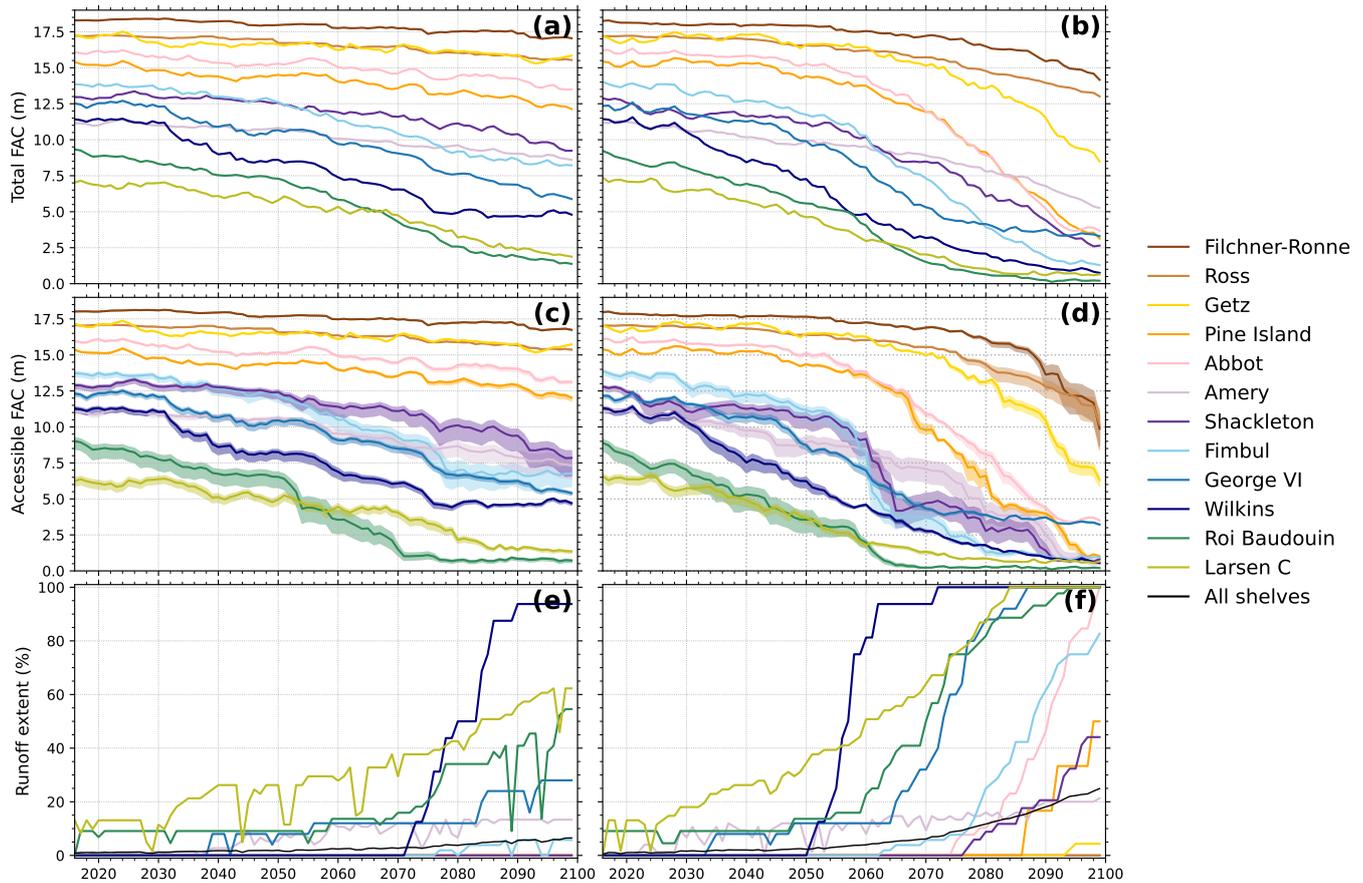


Figure 6. Time series of (a,b) total firm air content (FAC), (c,d) accessible FAC and (e,f) runoff extent of 12 ice shelves for (a,c,e) SSP2-4.5 and (b,d,f) SSP5-8.5 for the period 2015-2100. The shaded areas indicate the sensitivity to the relation between ice layer thickness and permeability factor shown in Fig. 3a.

is also limited as a MOA of 0.6 has not been reached, even though $> 50\%$ of the FAC has depleted. The general pattern of these figures is that melt-water blocking ice lenses are primarily formed in drier locations with considerable interannual variability in melt.

320 4.5 Impact of the dynamical densification model on future firm evolution

The change to a dynamical densification expression changes the temporal evolution of the firm. In this section and in Fig. 8, we quantify this effect by comparing FAC by 2080-2100 under SSP5-8.5 simulated by FDM v1.2A and by the dynamical model (FDM v1.2AD). We select the period 2080-2100 as the firm layer disappears in 2090 on some ice shelves (Fig. 6b). As shown in Sect. 2.1, both models include the effect that warmer snow densifies faster. However, in FDM v1.2A, the compensating effects

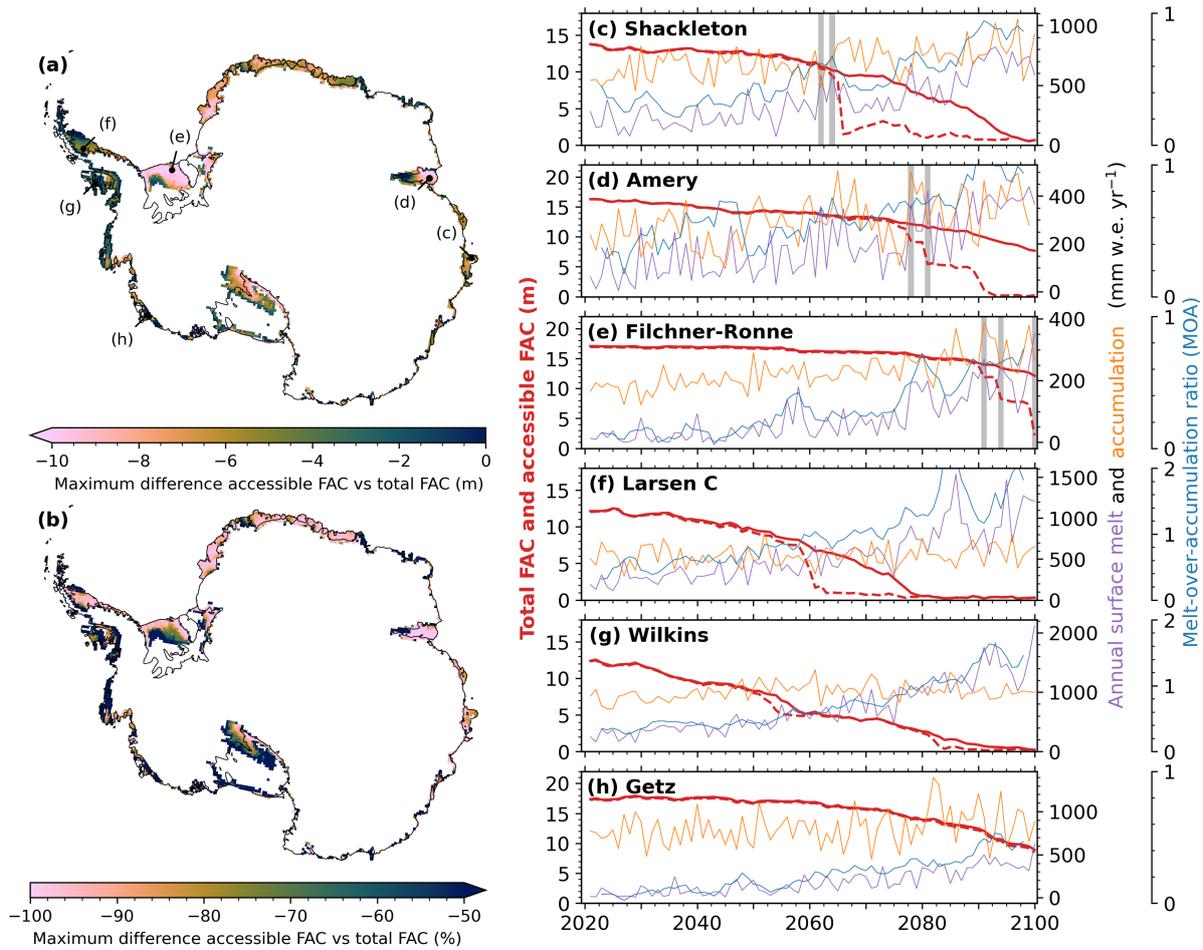


Figure 7. (a,b) The maximum (a) absolute and (b) corresponding relative difference between total firn air content (FAC) and accessible FAC (total FAC minus accessible FAC) from 1950-2100 for SSP5-8.5, shown for locations with at least 25 % accessible FAC depletion in 2100 compared to 2014. (c-h) Time series of total FAC (solid red line), accessible FAC (dashed red line), annual surface melt, annual accumulation and 5-year running average melt-over-accumulation ratio (MOA) ratio for individual grid points. The locations of the grid points are indicated in panel (a). The grey shaded areas indicate extreme melt seasons that cause persistent reduction in accessible FAC.

325 of enhanced grain growth, which makes snow stiffer, and enhanced accumulation, which increases the overburden pressure, are parameterised using 40 year running averages of temperature and accumulation.

High accumulation rates result in firn mostly younger than 40 to 100 years, and in such regions FDM v1.2A provides lower 2080-2100 FAC estimates than the dynamical model. This indicates that the effect of grain size growth, which slows down densification, is underestimated in FDM v1.2A in a transient climate for these locations. Figure 8b shows that these young firn
 330 locations are mostly found along the coasts of the Antarctic Peninsula and West Antarctica, such as Wilkins, Getz and George

VI ice shelves. Average end-of-century (2080-2100) FAC estimates of the dynamical model are 3.8 and 1.1 m higher in regions with a maximum firn age lower than 40 and 100 years, respectively.

For locations with older firn (> 100 years), the differences are smaller. This does not prove that the parameterisations of transient behavior are correct, but at least their errors balance out largely. Clear spatial patterns are visible in Fig. 8b. At the currently relatively dry Ross and Filchner-Ronne ice shelves (105 and 170 mm w.e. yr⁻¹ annual average accumulation, respectively) the dynamical model results in a quicker FAC depletion (-0.45 m and -0.41 m, respectively) compared to FDM v1.2A, due to a dominating effect of the increase in temperature (+8.1 °C and +8.4 °C, respectively) compared to accumulation (+10 % and +61 %, respectively) by 2080-2100 compared to 1950-2014.

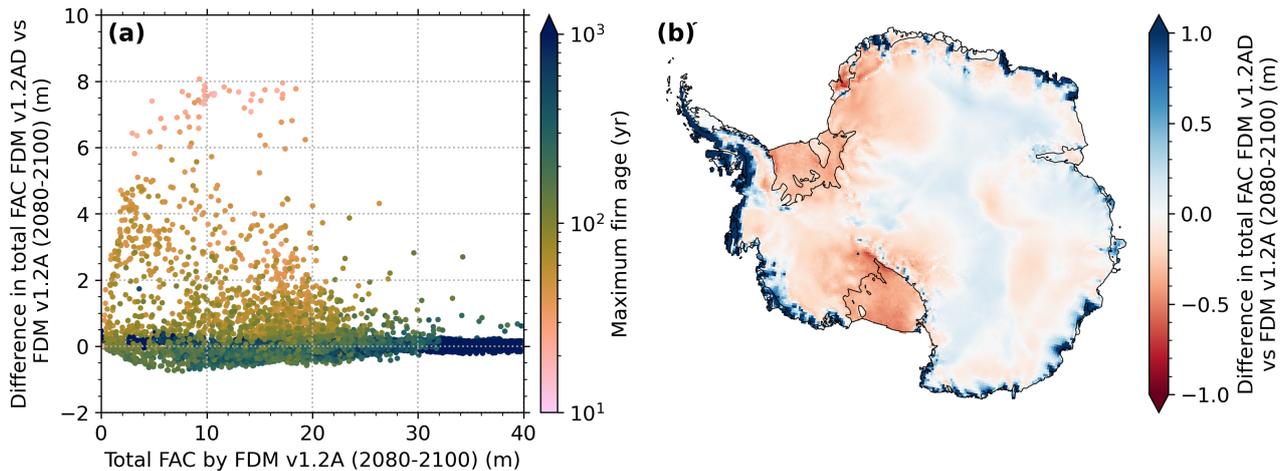


Figure 8. (a) Average total firn air content (FAC) difference between FDM v1.2AD-C and FDM v1.2A-C (FDM v1.2AD-C minus FDM v1.2A-C) against average FAC for FDM v1.2A-C for the period 2080-2100. The color indicates the maximum firn age (taken as the age at the critical density level $\rho = 830 \text{ kg m}^{-3}$) from FDM v1.2A-C (averaged over 1950-2014). (b) Average FAC difference between FDM v1.2AD-C and FDM v1.2A-C for the period 2080-2100.

5 Discussion

340 5.1 Firn air depletion

We use a firn model with an updated dynamical densification expression to simulate FAC over the AIS under future warming scenarios. We also estimate the impact of ice slabs on the accessible FAC. For the contemporary climate, the performance of the updated model is comparable to the non-dynamical model (Fig. 2). In a warming transient climate (here tested for SSP5-8.5), the Ross and Ronne-Filcher ice shelves in the updated model are more vulnerable to firn air depletion. On the other hand, high-accumulation ice shelves, such as Getz, Wilkins and George VI, are less vulnerable (Fig. 8).

The high vulnerability of Antarctic Peninsula ice shelves and Roi Baudouin ice shelf to total FAC depletion (> 50 % decrease in FAC by 2100 for all scenarios) aligns with previous studies (Gilbert and Kittel, 2021; Kuipers Munneke et al., 2014a; van Wessem et al., 2023). According to our results, enhanced FAC depletion on these ice shelves is expected to start around 2030 for all scenarios (Figs. 6, S6). For SSP5-8.5, we also find a substantial FAC depletion (> 74 % decrease) for ice shelves in
350 Dronning Maud Land, such as Fimbul, and elsewhere for Abbot, Pine Island, West and Shackleton ice shelves. Enhanced FAC depletion on these ice shelves is expected to occur around 2050-2060 for SSP5-8.5.

By including the effect of reduced permeability of ice slabs, our results reveal enhanced accessible FAC depletion under SSP5-8.5 on ice shelves with current accumulation rates < 500 mm w.e. yr⁻¹, mean annual temperatures < -16 °C and inter-annual variability in melt. Such ice shelves are mainly situated in East Antarctica, but also include the Ross, Filchner-Ronne, Larsen C and Pine Island ice shelves. Enhanced depletion starts around 2060-2070 for Shackleton, Fimbul and Pine Island
355 shelves (~ 4 °C AIS-wide average warming), and around 2080 for the colder Ross and Filchner-Ronne (~ 6 °C AIS-wide average warming). For SSP1-2.6 and SSP2-4.5 the accelerated accessible FAC depletion is limited to Larsen D, Fimbul, Amery and Roi Baudouin ice shelves. The formation of ice slabs thus increases the divergence between firn air depletion for the high emission scenario on the one hand, and for low- and intermediate emission scenarios on the other hand.

Our results suggest that extreme melt seasons can initiate ice-slab formation (Fig. 7), as observed in Greenland (Culberg et al., 2021). When ice layers that formed during an extreme melt season remain in contact with the surface hydrology, they concentrate new refreezing above their horizon, amplifying the contribution of even average subsequent melt seasons to ice-slab formation (Jullien et al., 2023). However, standing water on top of ice layers is not considered by IMAU-FDM, but an alternative positive feedback mechanism is captured: ice has a higher thermal conductivity, which contributes to more efficient
360 conductive cooling and thereby promotes the growth of ice layers and slabs (Vandecrux et al., 2020). The future accessible FAC on these ice shelves will depend on the frequency of future extreme melt events, and the timing of depletion is therefore less certain compared to non-ice slab regions where the depletion is mainly forced by the mean climate state and therefore more gradual.

Ice shelves where ice-slab formation under SSP5-8.5 is prevented have current accumulation rates > 600 mm w.e. yr⁻¹ and
370 mean annual temperatures > -19 °C, and are mainly situated in the Antarctic Peninsula and West-Antarctica, such as Wilkins, Stange, Abbot, Crosson and Getz ice shelves. High accumulation allows new pore space to regenerate FAC above the most recent refreezing layers. In addition, mild temperatures and more low-density fresh snow, both reducing the refreezing capacity per m³ of firn, prevent firn to reach the ice density. The projected increasing snowfall in Antarctica is thus not only important to counteract ice-sheet mass loss, but also to prevent ice-slab formation. This is in line with MacFerrin et al. (2019), who
375 found that ice slabs appear to be absent in regions of high accumulation (> 572 mm w.e. yr⁻¹) on the Greenland ice sheet. In contrast, high accumulation (>1,000 mm w.e. yr⁻¹) and mild (> -19 °C) conditions may lead to the formation of aquifers (Kuipers Munneke et al., 2014b; van Wessem et al., 2021), which aligns with the absence of extensive refreezing. Although firn aquifers do not have a depleted (accessible) FAC, the runoff from aquifers have the potential to cause hydrofracturing. Therefore, we will explore the future expansion of AIS aquifers in a forthcoming study.

380 The AIS ice-shelf-wide runoff extent in Fig. 6, 25 % by 2100 for SSP5-8.5, is substantially lower than reported by Gilbert and Kittel (2021), who estimate a runoff extent of 98 % by 2100 using the regional climate model MAR forced by the same CESM2 realisation. In MAR, liquid water reaching a firn layer with a density $> 830 \text{ kg m}^{-3}$ is converted to runoff, whereas in IMAU-FDM ice layers are completely permeable for meltwater percolation. Both models thus represent extremes in permeability assumptions, which explains the large difference. This also underlines the potentially large impact of ice slabs when estimating
385 the onset of meltwater ponding. Besides this, MAR also yields higher melt rates compared to RACMO2 for the same forcing (Carter et al., 2022), potentially caused by a more active snowmelt-albedo feedback. Differences in the initialization of the firn layer could also contribute to the discrepancy.

Extensive meltwater ponding is expected when accessible FAC is strongly depleted. Figure 6 shows that runoff is enhanced when total FAC (averaged over the ice shelf) roughly approaches 2.5 m for low-accumulation ice shelves, such as Roi Baudouin
390 ice shelf, and 5 m for high-accumulation ice shelves, such as Wilkins ice shelf. We expect that the accessible FAC thresholds for runoff generation are approximately similar. Based on these assumptions, Fig. 6 implies extensive melt ponding onset around 2060 on Roi Baudouin ice shelf for all scenarios. On Larsen C and Wilkins ice shelves meltwater ponding is expected around 2060 for SSP5-8.5 and around 2080 for SSP1-2.6 and SSP2-4.5. For these three ice shelves, meltwater ponding is thus expected to occur in the 21st century irrespective of the emission scenario. For SSP5-8.5 extensive meltwater ponding is
395 expected to occur on George VI around 2070, on Fimbul around 2075, and on Shackleton, Amery and Pine Island ice shelves around 2090. However, extensive meltwater ponding has already been observed on the northern George VI ice shelf (van Wessem et al., 2023), which suggests that our initial FAC estimates (Fig. 1) may be overestimated. On the other hand, locally observed meltwater ponding along the grounding lines of Amery and Roi Baudouin ice shelves is in line with our low initial FAC estimates there.

400 5.2 Limitations

FDM v1.2AD uses the bucket scheme to simulate vertical meltwater movement, which does not allow standing water over impermeable ice slabs, lateral meltwater movement, or preferential flow. Neglecting these processes has impacts on densification and ice layer formation. Verjans et al. (2019) found that a firn model using the bucket scheme produces similar density results as the more physically based Richards equation in a single domain for four locations on the Greenland ice sheet. Using the
405 Richards equation in a dual domain, which accounts for partitioning between matrix and fast preferential flow, simulated more ice layers, underestimated the FAC to a greater extent, but is better at reproducing density variability with depth. Using two firn models that use the bucket scheme, Thompson-Munson et al. (2023) simulated ice slabs in Greenland, and found that most ice slabs detected by IceBridge accumulation radar data in 2014 (MacFerrin et al., 2019) overlap with simulated ice slabs and ablation zones. On average, the observed ice slabs are located at slightly higher altitudes than the modelled ones. However, the
410 results are also strongly influenced by the densification equation and climatic forcing used (Verjans et al., 2019).

The densification scheme used in FDM v1.2AD (Eq. 4) is developed for dry-snow densification. The presence of liquid water may also impact the densification rate of firn; but due to a lack of physical understanding and available measurements, this effect has not been included. In line with this, the in situ observations used for calibration and evaluation of the model are

mainly (for 90 %) situated in non-melt regions. Equation (4) depends on initial grain size (taken here as 0.03 mm), which is a
415 poorly constrained parameter over the range of climates on ice-sheets. Fortunately, the model grain size is not very sensitive to
the initial value, since the growth rate is independent of the initial grain size, and the grain size quickly becomes magnitudes
larger (e.g. a growth rate of $0.0056 \text{ mm day}^{-1}$ for a firn layer of 250 K). Observed and modelled albedo evolution through
melt-refreezing cycles show that refreezing strongly increases the grain size (e.g., van Dalum et al., 2022). However, tests with
a different refreezing grain size (e.g. 0.4 mm instead of 0.25 mm) did not lead to very different results (Fig. S7). Again, this
420 process is poorly constrained by direct observations, hence the impact of refreezing on grain size, and subsequently on firn
compaction, remains uncertain. Firn compaction by horizontal divergence and strain softening is not included in the model,
therefore densification in high-strain and horizontal stretching areas, such as Pine Island and Thwaites ice shelves, is likely
underestimated (Horlings et al., 2021; Oraschewski and Grinsted, 2022).

Our outcomes of accessible FAC depend on ice-slab formation, which is a complex process to model. The current approach
425 (as a diagnostic post-processing step, rather than including it in the model) should be regarded as an exploratory study. We
present these results together with the total FAC and test the sensitivity to several ice layer thickness permeability relations. We
found that the timing and magnitude of accessible FAC depletion averaged over ice shelves is not very sensitive (< 10 years and
 < 1 m) to the thickness permeability relationships used (Figs. 3 and 6). Including the impermeability of ice layers interactively
within IMAU-FDM will be tested in future work.

430 The current view is that meltwater ponding weakens ice shelves, potentially leading to ice-shelf disintegration by hydrofrac-
turing (Banwell et al., 2013). However, Bell et al. (2017) found that when the ice surface slope is sufficiently steep, rivers can
form that transport liquid water laterally to the ocean, thereby preventing its destructive effects on ice shelves. FDM does not
include a liquid-water routing scheme to transport water laterally by streams and rivers.

Our results are furthermore limited by using only a single general circulation model (CESM2) and one model for dynamical
435 downscaling (RACMO2). Future work should address this by using an ensemble of Earth system models and other regional
climate models such as MAR (Kittel et al., 2021) and MetUM (Orr et al., 2021), which have different outcomes for melt (Carter
et al., 2022). The exact timing and amount of (accessible) FAC depletion will vary when using a different forcing dataset,
however the broad spatial variability among climatic regions and the dependency of ice layer formation on accumulation
should not be fundamentally different.

440 6 Conclusions

In this study, we explored future (accessible) FAC evolution over the AIS under various emission scenarios. Our main tool
is a firn model with an updated densification expression that allows for changing climatic conditions. Compared to the previ-
ous model version, the Ross and Filcher-Ronne ice shelves emerge as being more vulnerable to FAC depletion, while high-
accumulation ice shelves, such as Getz, Wilkins and George VI are less vulnerable. In our simulations, ice shelves in the
445 Antarctic Peninsula and Roi Baudouin ice shelf in Dronning Maud Land are particularly vulnerable to FAC depletion, also under
low (SSP1-2.6) and intermediate (SSP2-4.5) emission scenarios (> 50 % decrease in FAC by 2100). In the high (SSP5-8.5)

emission scenario all ice shelves experience considerable FAC depletion by 2100 (> 19 % decrease). The formation of ice slabs further reduces accessible FAC under SSP5-8.5, especially on low-accumulation ice shelves (current rates < 500 mm w.e. yr⁻¹) with a considerable interannual variability in surface melt. This includes many East-Antarctic ice shelves and Filchner-Ronne, Ross, Pine Island and Larsen C ice shelves. Under emission scenarios SSP1-2.6 and SSP2-4.5, ice-slab formation is limited to Larsen D, Roi Baudouin, Fimbul and Amery ice shelves. High accumulation rates (currently > 600 mm w.e. yr⁻¹) on Antarctic Peninsula and West Antarctic ice shelves, such as Wilkins, George VI, Getz, Abbot, Stange and Crosson ice shelves prevent the formation of ice slabs under all scenarios. These results highlight the potentially large vulnerability of low-accumulation ice shelves to firn air depletion through ice-slab formation.

455 *Code availability.* The code of IMAU-FDM v1.2AD is available on Zenodo (<https://doi.org/10.5281/zenodo.10723570>, Veldhuijsen et al. 2023b).

Data availability. The IMAU-FDM v1.2AD results (total firn air content and accessible firn air content) are available on Zenodo (<https://doi.org/10.5281/zenodo.10726834>, Veldhuijsen et al. 2023c).

460 *Author contributions.* SV and WJvdB defined the research goals and designed the study. SV updated the model, performed the simulations and analyzed the results. All authors contributed to discussions on the manuscript.

Competing interests. MRvdB is a member of the editorial board of journal The Cryosphere

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