

Reviewer #3:

The presented manuscript describes how up to three different climatic states exist under the same forcing in a climate model of the Permian-Triassic paleogeography. Multistability is further shown to exist also when vegetation and carbon cycle feedbacks are activated and the existence of multiple stable states is proposed as an explanation for the observed high climate variability of the PTB, as well as discrepancies between numerical simulations and geological data. The authors use MITgcm, a coupled general circulation model with a coarse resolution that properly resolves the ocean circulation, but only has a relatively simple representation of atmospheric dynamics (e.g. only 5 vertical layers).

The manuscript is generally well-structured and easy to follow. The language and grammar probably need a revision. The finding of several (non-snowball Earth) stable climate equilibria at the time of the PTB is interesting and, to my knowledge, has not been shown before.

We thank the reviewer for this overall positive statement on the originality of our work, and we are willing to improve the language of our manuscript and to respond to the following criticisms.

However, I have a major concern about the validity of the findings, coming from some of the presented simulation results:

i.) The "hot" state has a global mean temperature of 30.9 °C at a CO₂ concentration of 320 ppm and a solar forcing that is ~ 2% weaker than the present-day forcing. To put this in other words, even though the CO₂ concentration is 20-25% lower than the modern values and the sun is 2% weaker than today (equivalent to roughly another halving of the CO₂ concentration), the global climate of the hot state is simulated to be approximately 16 °C warmer than the present-day climate. I am aware that a different continental distribution can lead to very different global mean temperatures, but this contrast to the present-day climate is so extreme that I am really wondering where this is coming from? An explanation for this extreme state is not given in the manuscript. In general, all three states ("cold", "warm" and "hot") have pretty high global mean temperatures. Is it because the land surface has a comparably low albedo value? Does the continental distribution lead to a much smaller cloud coverage? Or is there a very strong water vapour feedback in the MITgcm atmosphere component? A closer investigation of this aspect would, in my opinion, not just be interesting, but is actually crucial, as otherwise the validity of the model results is very questionable.

The reviewer is right saying that more details are needed on the physical mechanisms to explain the origin of the three different steady states and especially the hot one. The mean global air surface temperature of the cold state at 320 ppm, equal to 17.2 °C, is already larger than the present-day value. We have described in Section 3.1 many different quantities which characterise the ocean and atmosphere dynamics. For example, in the cold state the ocean circulation is completely different from the present-day one, with a single anti-clockwise overturning cell (Fig. 6f) and the absence of circumpolar currents (Fig. 10c) because of the presence of the Pangea continent. It is clear that the boundary conditions gives rise to crucial differences with the present-day climate, affecting the heat transport (Fig. 5) and the asymmetrical formation of sea ice in the two hemispheres.

In addition, alternative climatic states can be realised under the same boundary conditions and the same forcing. This is due to the fact that there are many nonlinear mechanisms acting between the climatic spheres (atmosphere, cryosphere, hydrosphere..) on a given time scale, and they can balance in different ways under the same forcing, as is well known in climate modelling (within the whole hierarchy of models, starting from the energy balance models towards the complex general circulation models). For example, multiple steady states have been obtained using different MITgcm setups in coupled-aquaplanet configurations (Ferreira et al., 2011; Brunetti et al., 2019; Ragon et al., 2022; Brunetti & Ragon, 2023; Zhu & Rose, 2023) or other models (Popp et al., 2016; Lucarini & Bódai, 2020), including high complexity models as IPCC-class models (Peltier & Vettoretti, 2014; Jackson & Wood, 2018; Malmierca-Vallet et al., 2023).

In a coupled aquaplanet (where the full nonlinear feedbacks between ocean, atmosphere and sea ice are taken into account over a millennial time scale), we investigated the role of cloud albedo (Brunetti et al., 2019) and indeed showed that the presence of the hot state depends on cloud reflection properties and on the amount of solar radiation that is allowed to enter at high latitudes (see also Ragon et al. (2022)).

Following the suggestion of the reviewer, we have analysed the cloud cover in the three steady states. It is larger in the hot state compared to the cold state in polar regions and on land (see Fig. 1a in this

response). The planetary albedo is 30% in the cold state, 29% in the warm state and 27% in the hot state, which are $\leq 30\%$, the present-day estimation (Goode et al., 2001). Thus, the energy absorbed into the atmosphere is generally larger than for present-day climate, and is larger in the hot state than in the cold one. At the same time, the atmospheric transmissivity of long-wave radiation is smaller in the hot state (0.50) than in the cold one (0.57), meaning that more thermal radiation is trapped within the atmosphere in the hot state. The combined effects of cloud feedback lead to more radiation to enter and stay into the atmosphere, the cloud feedback becoming dominant in the hot state, as also observed in the coupled-aquaplanet configuration (Brunetti et al., 2019). We suggest to add the analysis of the cloud cover in the three states in Section 3.1 of the manuscript.

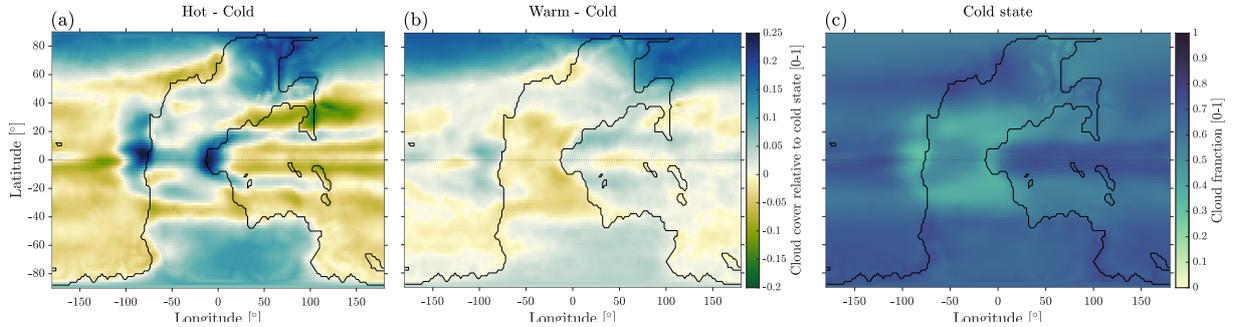


Figure 1: Cloud cover in (a) hot-cold; (b) warm-cold; (c) cold state.

ii.) The plot of global mean temperatures in Fig. 11 and the values in Tab. 5 highlight another extreme (maybe even unrealistic?) aspect of the simulated model results: the climate sensitivity seems to be extremely high. The slopes of the lines in Fig. 11 indicate that the climate sensitivity of this setup is 15-18 °C of warming per doubling of CO₂. An increase of just 8 ppm in the "warm" state led to a temperature increase of 1.45 °C (Tab. 5). If the modern climate would be anywhere near this sensitivity, humanity would be doomed already (we added ~ 140 ppm carbon to experience a comparable warming). The most recent IPCC estimate of modern climate sensitivity is 2.5-4 °C (likely range). Again, a different continental setup might explain some of the differences to the modern state, but the climate sensitivity in this study is so extreme that it requires a convincing explanation. Otherwise the model results cannot be viewed as reliable.

We agree that the equilibrium climate sensitivity of the three climatic states (from the slopes of the lines in Fig. 11) is quite large in comparison with the IPCC estimate obtained with CMIP-type models for present day. However, we need to consider that:

1. There is a spread in model results for the present-day climate, as summarised in Knutti et al. (2017), depending on model complexity and considered time scale.
2. The simulations of the present-day climate are tuned using many available observations. This is not possible of course for the Permian-Triassic period.
3. The atmospheric module is based on SPEEDY, the Simplified Parametrizations primitive-Equation DYNamics described in Molteni (2003) (see also the Appendix to that article on the web page of SPEEDY), with 5 vertical layers. It is important to consider that in the parameterization scheme for the longwave radiation, the infrared spectrum is partitioned into four regions: *i*) the 'infrared window' between 8.5 and 11 μm ; *ii*) the band of strong absorption by CO₂ around 15 μm ; *iii*) the aggregation of regions with weak/moderate absorption by water vapour; *iv*) the aggregation of regions with strong absorption by water vapour. Thus, the absorption of CO₂ is limited by the fact that only the largest absorption band is included in the infrared spectrum. This implies that the atmospheric CO₂ content is probably underestimated in our simulations, and that the range of CO₂ for the steady states can change when considering the full absorption bands. This also affects the equilibrium climate sensitivity of the MITgcm. We can include this more detailed description of the infrared spectrum in SPEEDY in Section 2.1 in the manuscript. The advantage of SPEEDY is that it requires one order of magnitude less CPU time than a state-of-the-art GCM at the same horizontal resolution, and is therefore suitable for studies on millennial time scale.
4. Despite this simplified atmospheric module, we have reproduced the present-day climate with our MITgcm setup (see Brunetti & V erard (2018) and additional comments below). Thus, we are confident that our model results are reliable, the main feedback mechanisms being properly described at

main order (within the limitations of low-resolution general circulation models (GCMs) and simplified parameterizations discussed above, typical of other Earth Models of Intermediate Complexity (EMICs)).

5. The simplified atmospheric module and the low spatial resolution likely affect the forcing range of stability, as we said above, but we expect that they have a small effect on the overall structure of the bifurcation diagram. The reason is that the presence of multiple steady states depends on the number of feedbacks included in the simulation on a given time scale and how they can balance between each other.
6. It is important to repeat our simulations with other models with different complexity (EMICs, CMIP-type GCMs, low-resolution GCMs, ...) in order to investigate the robustness of the alternative climatic states, as we state in the Conclusions (line 299). Other modellers of past climates have already shown their interest in the multistability framework that we propose in the present manuscript, and it is important to publish results obtained with different models. We are also involved in the Swiss National Science Foundation (SNSF) Sinergia Project n. 213539 where we plan to compare FOAM, PlaSim/cGENIE and MITgcm in future publications (at different time slices including present day). Some of the authors are also involved in TIPMIP, the Tipping Point Modelling Intercomparison Project.

iii.) I find it quite surprising that the deserts are smallest in the "hot" state. The authors claim that this is because there is more precipitation in that state. However, the annual mean surface air temperatures are 40-50 °C (daily temperature extremes should then be around 70-80 °C) in tropical and subtropical regions, where their model is simulating a vegetation cover of "forbland and dry shrubland". I am no expert in vegetation cover, but could any plant survive temperatures of >70 °C, even if it is just for a few hours a day? Additionally, even though there might be more precipitation in the hot state, this would probably be more localized in individual extreme events and not fall evenly. I see a potential discrepancy here, because the vegetation model is only fed with long-term monthly mean values, which don't capture this variability.

The annual mean surface air temperature (SAT) in the hot state (after convergence with BIOME4) is 32.4 °C (see Table 4), and not 40-50 °C. Seasonal precipitation and SAT for the hot and cold states are shown in Figs. 2, 3 in this response, respectively, while min/max/mean values of monthly averaged SAT and precipitation are shown in Fig. 4. Regions of null precipitation are the same along all the year in the cold state (Fig. 2, bottom panels), within 20 and 40 degLat, with mean SAT of the order of 40 °C (Fig. 3, bottom panels). These regions correspond to desert in the cold state (Fig. 12 in the manuscript). Regions of null precipitation have a much reduced extent depending on the season in the hot state (Fig. 2 in this response, upper panels), despite reaching higher temperature than in the cold state, the maximum being of the order of 60 °C (Fig. 4). This is why desert has less extent in the hot state, keeping also in mind that SAT is not the only driver of desert conditions, soil temperature and availability of water being crucial as well for the plant development (Wahid et al., 2007; Hatfield & Prueger, 2015).

The biome denoted as 'Forbland and dry shrubland' in Harrison & Prentice (2003) (the same classification that is used in Fig. 12 in our manuscript) contains tropical and temperate xerophytic shrubland (that is, shrubs adapted to dry periods), but also tropical and temperate forbland. Thus, this kind of biome is sufficiently general to appear in the hot state.

iv.) It is also quite unusual that the meridional overturning circulation (MOC) of the ocean is much stronger in the hot state, especially since there is a weakening of the MOC, when going from the cold to the warm state. Furthermore, in the hot state there seems to be a cell near the equator where the water transport is out of the bounds of the colorbar, i.e. has a transport of >100 Sv, which is extremely high and - to my knowledge - unrealistic for a supposed equilibrium state. Where is the energy that drives a constant massive ocean overturning coming from?

We have compared our results with those in Hülse et al. (2021) (see in particular Fig. 3 in that paper and lines 189-191 in our manuscript). They consider the Permian-Triassic paleogeography and different values of atmospheric CO₂ content. By increasing CO₂, the ocean overturning circulation changes structure: a single counter-clockwise overturning cell at low CO₂ (as in our cold state), which increases in intensity as a clockwise cell appears first at the North polar region (warm state) and then in the whole Northern hemisphere at high CO₂ (as in our hot state). This shows that the overall structure of the overturning cells in our simulations corresponds well to that in Hülse et al. (2021).

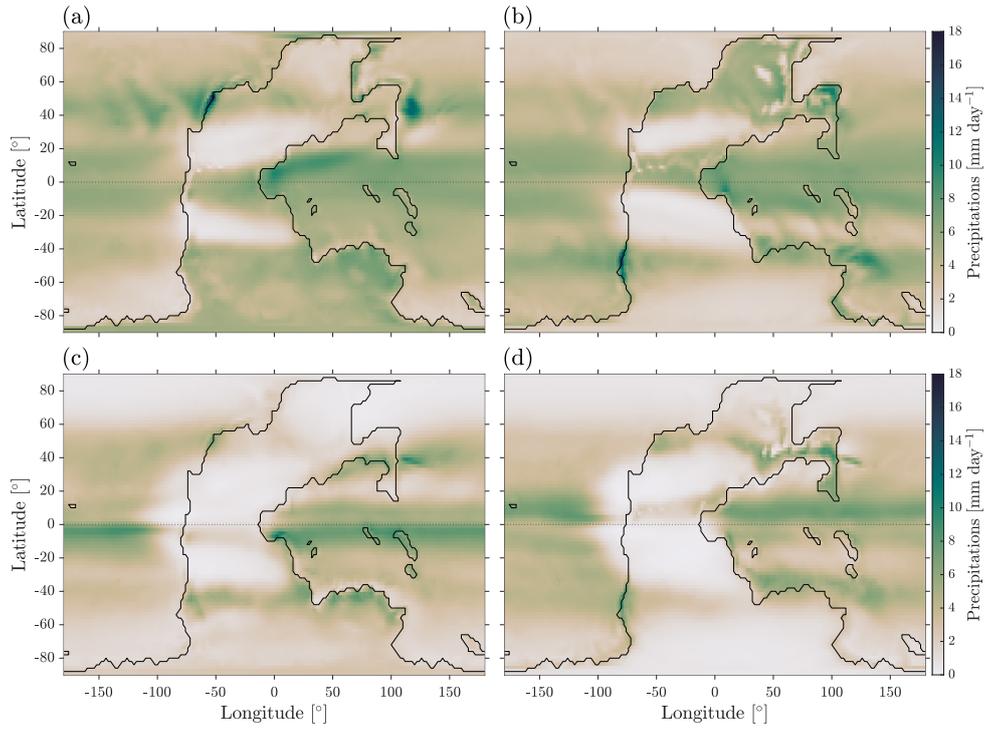


Figure 2: Seasonal (DJF: a,c; JJA: b,d) precipitation in hot (a-b) and cold (c-d) states when convergence with BIOME4 is attained.

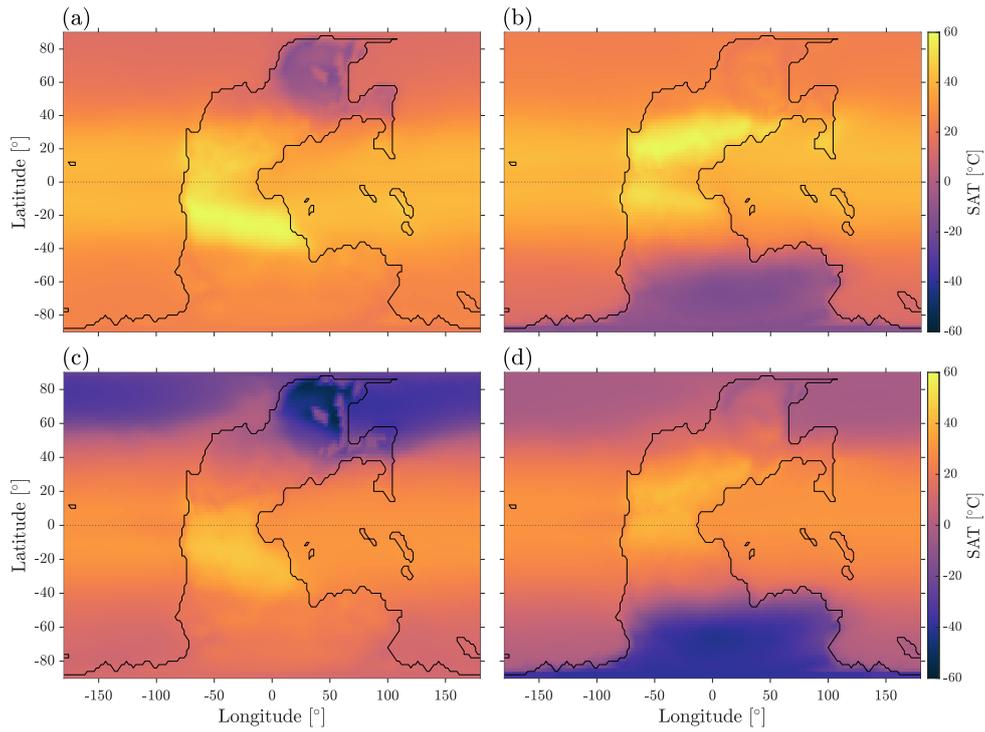


Figure 3: Seasonal (DJF: a,c; JJA: b,d) surface air temperature in hot (a-b) and cold (c-d) states when convergence with BIOME4 is attained.

Note that the intensity of local maximum of the overturning cell around 50S in the three attractors increases going from cold (19 Sv) to warm (25 Sv) and hot (33 Sv) (see Fig. 6 in the manuscript, bottom panels), this trend being in agreement with Hülse et al. (2021).

In order to investigate the reason why the overturning cell near the Equator is so intense in the hot state, we have performed a detailed study of the overturning circulation by first analysing the contribution of Tethys and Panthalassa. It turns out that the intense overturning cell is due to the circulation in

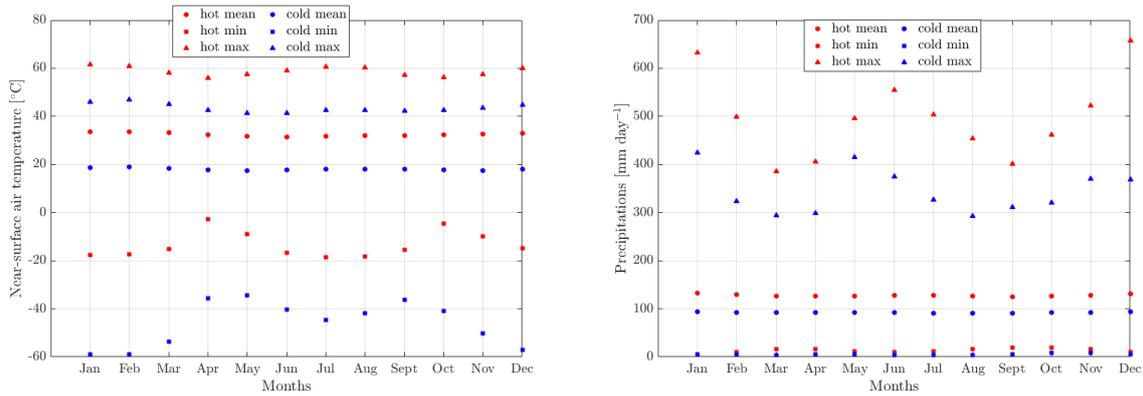


Figure 4: Monthly mean, minimum and maximum values of surface air temperature (left) and precipitation (right) for hot and cold states.

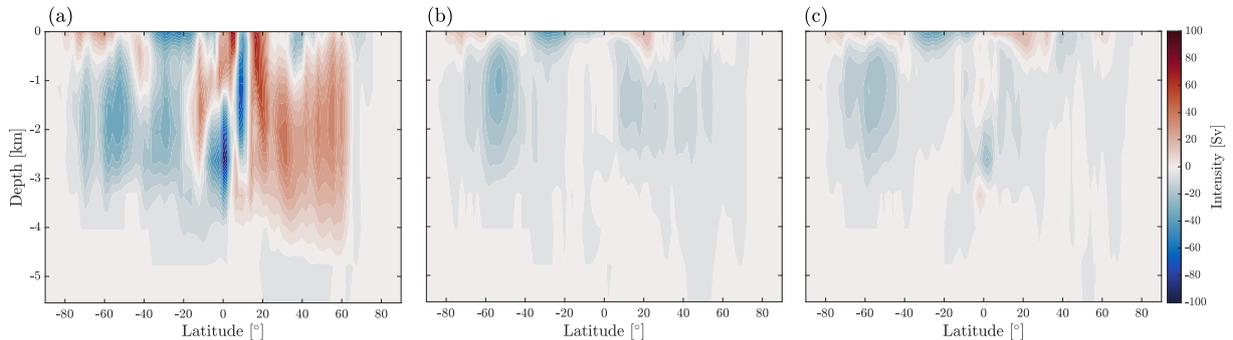


Figure 5: Residual-mean circulation in Panthalassa for the hot (a), warm (b) and cold (c) states.

Panthalassa because of the presence of equatorial oceanic ridges which can be seen in Fig. 1 in our manuscript on the west of Pangea. The overturning streamfunction in Fig. 6 (bottom panels) of the manuscript is calculated using the mean meridional velocity component. However, there is a turbulent component that is particularly strong near the west coast of Pangea at depth. Our preliminary results show that the residual-mean circulation, given by the sum of the mean part and the turbulent circulation (Danabasoglu et al., 1994; Ferreira et al., 2011) is much less intense (the intensity of the local maximum is of the order of 90 Sv), as can be seen in Fig. 5.

At this point, I am having a hard time believing the outcome of the simulation results, especially with respect to the high climate sensitivity and the generally unusual characteristics of the "hot" state. When seeing these results, my first guess would be that the whole "hot" state is a numerical artefact and that the atmosphere component of MITgcm is not doing a decent job here in general. In order to oppose my concern, the authors could present results of a reference simulation of 1850-today, to show that this version of MITgcm (with the necessary adaptations to the modern state) is able to get the historical warming roughly right (or one pre-industrial simulation and one with a more recent CO_2 concentration at 400 ppm, if that is easier).

A pre-industrial simulation obtained with MITgcm in a coupled atmosphere-ocean-sea ice-land configuration similar to the one used here has been published in Brunetti & V erard (2018) for $\text{CO}_2 = 326$ ppm and $S_0 = 342 \text{ W/m}^2$ (cf. in particular the setup denoted as Run4 in that paper). The simulation reproduces reasonably well the pre-industrial conditions, in particular the mean surface air temperature, the sea ice extent in the Arctic and Antarctic regions, the structure and maximal intensity of the overturning circulation, as expected by a low-resolution GCM (2.8° , 5 levels in the atmosphere, 15 in the ocean) with simplified atmospheric parametrizations. In addition, the TOA imbalance is quite low (-0.55 W/m^2), as well as the surface energy imbalance (0.04 W/m^2), assuring a small temperature drift of 0.009 K/century (Table 3 in Brunetti & V erard (2018)).

We have not a simulation at 400 ppm (the simulations in Brunetti & V erard (2018) were run with version MITgcm.c65q, while for changing the CO_2 content a more recent version is needed). Preliminary results with MITgcm.c67f show that the climate sensitivity may be large (without any particular effort of tuning to the present-day conditions). We plan to perform a detailed study of the climate sensitivity

and the complete analysis of the steady states for the present-day configuration in the context of the SNSF Sinergia Project that we mentioned above and just started in October 2023. However, this study requires time and is beyond the scope of the present manuscript.

Additionally, I really need to see a discussion of how the extreme and unusual results of the hot state can be explained physically. As the existence of the "hot" state at such low CO₂ concentrations is almost impossible in my eyes and given the other strange features mentioned above, I highly doubt the reliability of the presented results. Since the whole point of this manuscript is based on the existence of multistability, I have no other option than to suggest a rejection of the manuscript, unless the authors provide an elaborate and convincing explanation of why these extreme results are realistic.

We believe that our responses to all the previous points provide physical explanations for the existence of the hot state, in particular the analysis of the cloud feedbacks (point (i)), of the seasonal and monthly averages of surface air temperature and precipitation (point (iii)), and of the overturning circulation (point (iv)). All these detailed analyses improve the quality of our paper and we are grateful to the reviewer for this.

Moreover, we have explored the existence of multiple steady states in a coupled aquaplanet using the MITgcm in previous studies. We have shown in particular that the hot state depends on the amount of solar energy allowed to enter in the polar regions, thus on the cloud description (Brunetti et al., 2019); from a detailed analysis performed in Ragon et al. (2022), the hot state maximises not only the global temperature, but also the Material Entropy Production (MEP) due to the hydrological cycle (which represents the largest contribution to the total MEP), the total precipitation and the peak intensity in the water-mass transport. Other steady states maximise other quantities, each state being the result of a different balance between nonlinear feedbacks.

Finally, geological data suggest that climatic oscillations occurred in the Early Triassic, with temperature fluctuations of the order of ten degrees (see also a comment below, p. 7), from 'hot' to 'very hot' conditions. We believe that the multistability framework is particularly relevant for explaining such climatic oscillations.

Of course, the same procedure used in our manuscript should be repeated with other models of different complexity. However, the construction of the bifurcation diagram takes time. We believe that it is important to open the way, and show that it is feasible by providing to the scientific community a first detailed study (with all its limitations that we think we have honestly described) to start with.

Specific comments

- The language/grammar of the manuscript needs a revision. Very often I have the feeling that a "the" or similar article is missing (as an example in line 184 the sentence should be "In the hot state,...", right?).

We will correct this and similar errors. We shall give the final version of the manuscript to English speaking colleagues for a check.

- The whole discussion neglects the fact that there should be another stable climate: the snowball Earth. This should be mentioned at least once at some point.

We agree with the reviewer, and we will mention this possibility. However, we restricted our analysis to the steady states of relevance to the Early Triassic. We confirm that at least a colder climate exists: at the lower edge of the stable branches of both hot and cold states the system is attracted towards a colder state, as shown in Fig. B1 of the manuscript. A waterbelt state is present where the ice extends to $\sim 30^\circ$ latitude and the global mean surface air temperature is approx. -10°C (see Fig. 6 in this response). However, we have not investigated this state further since simulations require long CPU time while geological data exclude for the presence of snowball or waterbelt states in the Early Triassic (Sun et al., 2012; Romano et al., 2013; Goudemand et al., 2019; Widmann et al., 2020). Similarly, we did not search for steady states at global SAT below -10°C , but there is no reason to expect that no snowball exists.

- I would appreciate some more introduction as to why the Permian-Triassic Boundary is an important/interesting period to study? Right now the introduction is only about multistability and tipping points.

We propose to include the following paragraph in the Introduction (at line 40) to describe the climatic oscillations in the aftermath of the Permian-Triassic Boundary mass extinction and to provide the general context for our numerical simulations.

We are interested in the climatic oscillations observed at the Smithian-Spathian boundary in the Early Triassic, just after the Permian-Triassic boundary (PTB) mass extinction (~ 252 Ma), the most severe

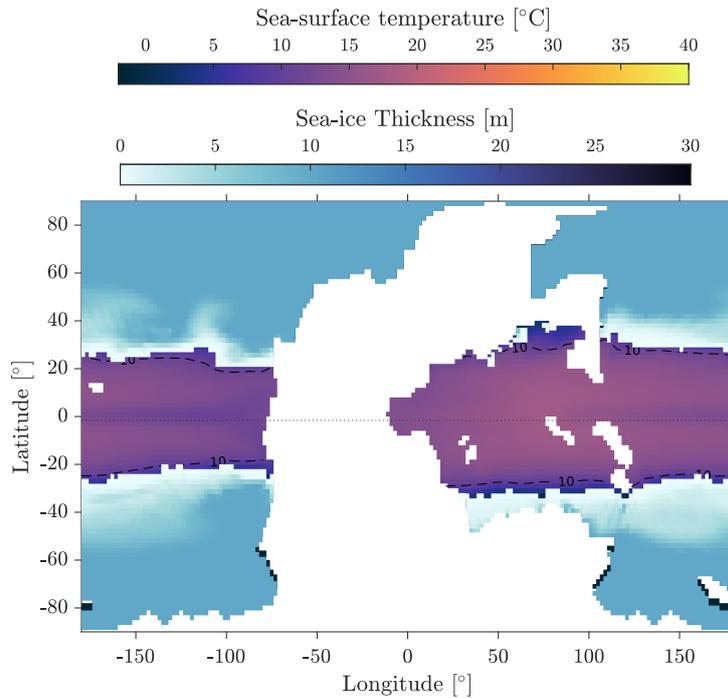


Figure 6: Sea-surface temperature and sea-ice extent in the waterbelt state at global mean SAT ~ -10 °C.

of the Phanerozoic Raup (1979); MacLeod (2014); Stanley (2016). As a consequence of the volcanic activity of the Siberian Large Igneous Province Campbell et al. (1992); Renne et al. (1995); Reichow et al. (2009), the global carbon cycle entered a perturbed state which persisted for nearly 5.4 Myr in the Early Triassic, until a new equilibrium state was reached in the Anisian Sun et al. (2012); Romano et al. (2013); Goudemand et al. (2019); Leu et al. (2019); Widmann et al. (2020). The observed fluctuations in the carbon isotope record Payne et al. (2004); Galfetti et al. (2007); Retallack et al. (2011) with successive diversification-extinction cycles of the nekton Orchard (2007); Brühwiler et al. (2010); Leu et al. (2019) and ecological crises of terrestrial plants Hermann et al. (2011); Schneebeli-Hermann (2020), are all indicative of the climatic changes which occurred in the Early Triassic, with variations in the global temperature of the order of 7-8 °C from the thermal maximum in the late Smithian to cold climates in early Spathian times Widmann et al. (2020).

However, despite the great effort of the scientific community to reconstruct such climatic oscillations in the aftermath of the PTB, large uncertainties remain in timing and causal relationships, implying that numerical modelling needs to consider a wide range of initial and boundary conditions for the simulation of such geological interval. In this context, ... [continuing at line 44]

- The model has no sea-ice dynamics, which would strongly impact individual climate states that have some sea ice. Given this shortcoming, also the small range in which the "warm" state exists is questionable.

We agree that the number of steady states and the extension of their stability region may depend on the configuration and the model setup. Indeed, feedback mechanisms acting on the same time scale could affect the balance between different processes, and thus the number of steady states. A sentence on this aspect can be added in the Conclusions of the manuscript, mentioning the role of sea ice dynamics, and also ocean dynamics, and relevant references (at line 300):

.... boundary conditions. In particular, including sea ice dynamics or different numerical implementations of thermodynamic sea ice Lewis et al. (2007); Voigt & Abbot (2012); Hörner & Voigt (2023), as well as considering a mixed-layer ocean or a fully dynamical one Poulsen et al. (2001); Pohl et al. (2014), may change the number of steady states, and reveal the source of possible biases.

This is also the reason why in the Conclusions (last paragraph, line 299) we call for the need of comparing different climate models. We can also specify that we use a *thermodynamic* sea ice in the abstract and the Conclusions (second paragraph, line 278) when we mention the MITgcm configuration.

- the choice of colors in the upper panel of Fig. 2, using darker colors for a higher albedo, seems odd. I would reverse the colorbar

We agree with this suggestion and we will reverse the colors.

- line 143: averaged over which time scale?

The average is computed over the last 100 yr of that part of the simulation (step 1 of the air-sea carbon exchange procedure).

- a short description of how the carbon cycle model works would be very helpful. Right now, I cannot judge whether this model is sufficient to provide a proper representation of the carbon cycle during the PTB

The procedure for including air-sea carbon exchanges is described in section 2.3 and it consists of two steps: 1) we estimate the distributions of oceanic tracers (DIC, dissolved inorganic phosphorous, alkalinity, phosphate and oxygen), which correspond to given values of atmospheric CO₂ content on the stable branch of the attractors. 2) These distributions are then used when the air-sea carbon exchanges are allowed. By construction, air-sea carbon exchanges vary the atmospheric CO₂ content of the order of 10 ppm (see Table 5). The advantage of including the option of CO₂ exchanges is to obtain the total (ocean + atmosphere) carbon content for each state, as reported in Table 5.

- lines 239-248: how do the plants survive these extreme temperatures in the warm state? Also, there is more carbon stored in vegetation in the hot state. This also means there is a lot of fuel for fires, which should occur very often given the extremely high temperatures. Is this self-consistent?

For the first question, see answer to point (iii).

We started to investigate the question of fires and possible geological signatures in collaboration with biochemists at the University of Lausanne. In order to have fires burning a large amount of biomass over long time scales (millennial), a season of vegetation development should be followed by a dry and hot one. This can indeed be the case in the tropical and subtropical regions of the hot state. However, the dominant biome in such regions is ‘forbland and dry shurland’, which has not a high biomass density (see Table D1 in our manuscript). Thus, the overall biomass content in the hot state can only slightly vary over millennial time scales.

- Figure captions could include more information to make the figures a bit more self-evident (e.g. Fig. 7-9)

We shall add such information.

- adding some contour lines in e.g. Fig. 3-4 would really help for readability

We thank the reviewer for this suggestion. Figures 3, 4, and also Fig. 9 (salinity distribution) in the manuscript can be modified as shown in Fig. 7, 8, 9 in this response, respectively.

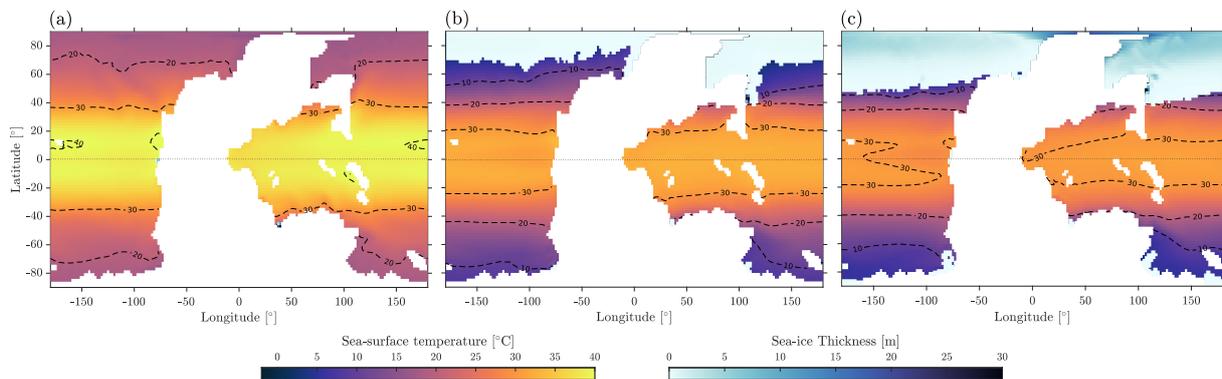


Figure 7: Sea-surface temperature and sea-ice thickness for (a) hot, (b) warm, and (c) cold states. White area corresponds to land.

- The first paragraph of the conclusion is rather a repetition of the introduction

Even if the content is similar, it is differently formulated. We think it is a useful summary of the main points and we would like to keep as it is.

- I don't understand the way that uncertainty in numbers is represented. For example in Tab.4: in the initial state of the hot state, the second iteration of the warm state and the fourth iteration of the cold state the uncertainty of SAT is much larger (9 instead of 1) than in the other states. Do these three cases actually have an uncertainty of 0.9°C and not 9°C? Otherwise the results seem to suggest some kind of instability. Do I understand those numbers correctly?

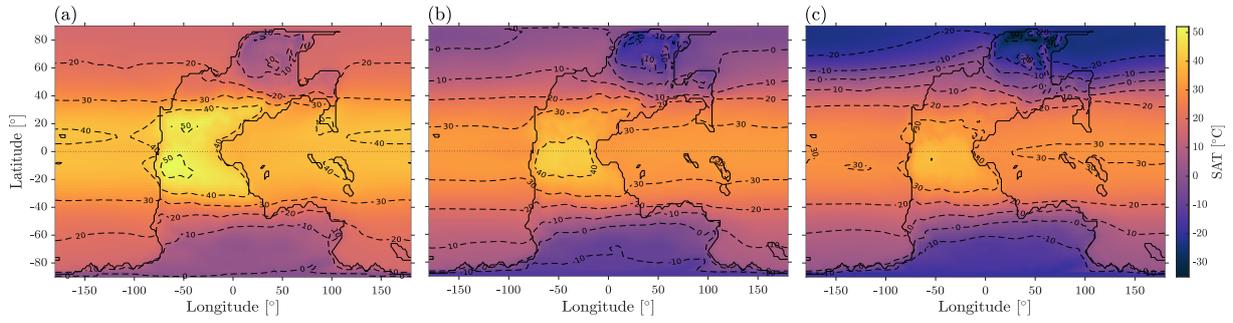


Figure 8: Near-surface air temperature for (a) hot, (b) warm, and (c) cold states.

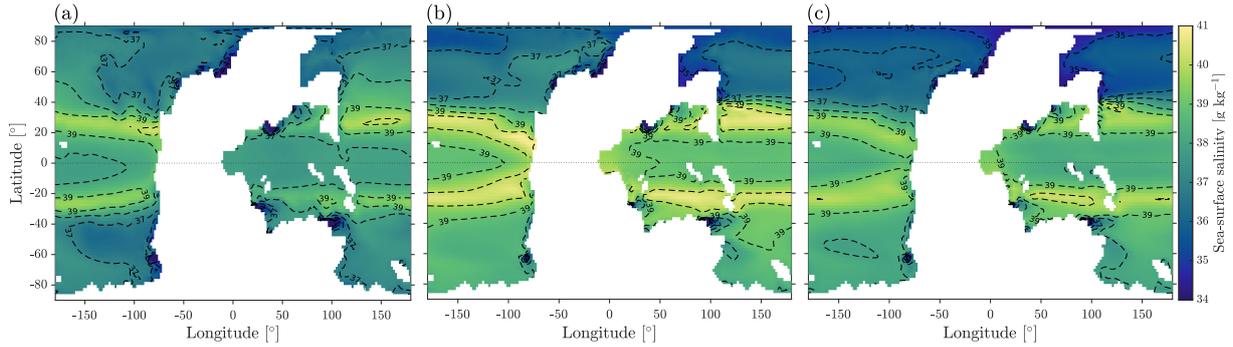


Figure 9: Sea-surface salinity of (a) hot, (b) warm, and (c) cold states. White area corresponds to land.

The number in parenthesis is the uncertainty associated to the last significant digit. For example, in the initial hot state, $30.92(9)^\circ\text{C}$ corresponds to $(30.92\pm 0.09)^\circ\text{C}$. This is a compact way to write uncertainties which is commonly used in physics and climate literature. While we expect that this compact form helps legibility, we are open to change to the extended form if required to do so.

- The river map in Fig. A1 could simply be added to Fig. 1. The Appendix A is then obsolete, as the content is also already mentioned in the model description section.

We agree with this suggestion.

- What about other greenhouse gases? Are they held fixed at some values? Which values were used?

The longwave radiation scheme in the atmospheric module (SPEEDY, Molteni (2003)) uses four spectral bands, as described in this response (point ii.3). The absorption by other greenhouse gases as methane is not included. This information can be added in section 2.1 when we mention the SPEEDY module.

Some technical corrections:

- labelling subfigures in Fig. 2 with (a) and (b)

We thank the reviewer for pointing this out.

- Fig. 10: It says that the line thickness varies with horizontal velocity, but it is not. Maybe make the thickness more sensitive to velocity or just drop the velocity scaling.

We agree that the variation in line thickness is not very visible. We can drop the velocity scaling.

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