

A landslide runout model for sediment transport, landscape evolution and hazard assessment applications

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Abstract

We developed a new rule-based, cellular-automaton algorithm for predicting the hazard extent, sediment transport and topographic change associated with the runout of a landslide. This algorithm, which we call MassWastingRunout (MWR), is coded in Python and implemented as a component for the package Landlab. MWR combines the functionality of simple runout algorithms used in landscape evolution and watershed sediment yield models with the predictive details typical of runout models used for landslide inundation hazard mapping. An initial Digital Elevation Model (DEM), a regolith depth map, and the location polygon of the landslide source area are the only inputs required to run MWR to model the entire runout process. Runout relies on the principle of mass conservation and a set of topographic rules and empirical formulas that govern erosion and deposition. For the purpose of facilitating rapid calibration to a site, MWR includes a calibration utility that uses a Bayesian Markov Chain Monte Carlo algorithm to automatically calibrate the model to match observed runout extent, deposition and erosion. Additionally, the calibration utility produces empirical probability density functions of each calibration parameter that can be used to inform probabilistic implementation of MWR. Here we use a series of synthetic terrains to demonstrate basic model response to topographic convergence and slope, test calibrated model performance relative to several observed landslides, and briefly demonstrate how MWR can be used to develop a probabilistic runout hazard map. A calibrated runout model may allow for region-specific and more insightful predictions of landslide impact on landscape morphology and watershed-scale sediment dynamics, and should be further investigated in future modelling studies.

1. Introduction

Over geologic timescales, landslides and their runout shape the topographic expression of mountain ranges and channel networks (e.g., Campforts et al., 2022; Korup, 2006; Larsen and Montgomery, 2012; Montgomery and Dietrich, 1988). Over more pragmatic engineering and environmental risk management timescales, landslides and their runout can inundate and destroy infrastructure (e.g., Kean et al., 2019) but also support numerous ecosystem

35 benefits, including carbon and nutrient transport from hillslopes to channels and the creation of riparian habitat (Benda
36 et al., 2003; Bigelow et al., 2007; Goode et al., 2012). Therefore, explicit representation of landslide runout is a
37 necessary component of: (1) landslide inundation hazard assessments, with emphasis on inundation extent and flow
38 depth (e.g., Frank et al., 2015; Han et al., 2015); (2) watershed sediment yield models, with emphasis on the
39 mobilization, deposition and type of sediment carried by the landslide (e.g., Bathurst and Burton, 1998;
40 Istanbuluoglu, et al., 2005); and (3) landscape evolution models, with emphasis on topographic change prediction
41 (e.g., Tucker and Bras, 1998; Istanbuluoglu and Bras, 2005; Campforts et al., 2022);

42 Landslide runout processes can be generalized into three phases: initiation, erosion, and deposition. After a landslide
43 initiates, it may break apart and flow as a relatively dry debris slide, or it may mix with surface runoff to become a
44 debris flow. The mobility of the mass wasting material and resulting erosion/deposition pattern often varies as a
45 function of runout topography and initial relief and size of the landslide (Iverson, 1997). Mobility may also be
46 impacted by substrate liquefaction (Hung and Evans, 2004) and landslide basal cataclasis (Shaller et al., 2020). As
47 the runout material moves downslope, flow depth varies as a function of channel width (Kean et al., 2019), which in
48 turn impacts erosion rates (Schürch et al., 2011). Theoretical, field and laboratory observations indicate that erosion
49 rates may also depend on the moisture content of the channel bed (Iverson, 2012; McCoy et al., 2012), flow grain size
50 (Egashira et al., 2001) and granular stress within the flow (Capart et al., 2015). The slope at which deposition begins
51 is controlled by the grain-to-water ratio and friction angle of the slide material (Takahashi, 2014; Major and Iverson,
52 1999; Zhou et al., 2019) but the friction angle of the material may vary as a function of the grains in the flow and
53 fluidization of the flow material (Hutter et al., 1996). Lateral levees often form along the edges of the flow (Major,
54 1997; Whipple and Dunne, 1992; Shaller et al., 2020) and deposition at the distal end of the flow may occur as layered
55 accretion (Major, 1997) or as the emplacement of a single, massive deposit (Shaller et al., 2020). If the water content
56 of the runout material is high enough, as the solid fraction of the distal end of the flow compresses, the water is
57 squeezed out and may continue as an immature debris flow (sensu Takahashi, 2014) or intense bedload (sensu Capart
58 & Fraccarolo, 2011), extending the runout distance (e.g., Shaller et al., 2020).

59 Landslide inundation hazard models aim to accurately predict the runout extent and/or flow depths of a runout event
60 and may include some or most of the above processes in the model. Example models include: (1) site-specific-
61 empirical/statistical models that use simple geometric rules and an estimate of the total mobilized volume (initial
62 landslide body + eroded volume) or a growth factor (e.g., Reid et al., 2016); (2) detailed, continuum-based mechanistic
63 models, which conceptualize the runout process as a single-phase or multiphase flow using the depth-integrated
64 Navier-Stokes equations for an incompressible, free-surface flow (i.e., shallow water equations; Frank et al., 2015;
65 Han et al., 2015; Iverson and Denlinger, 2001; Medina et al., 2008) and often (though not always) require pre-
66 knowledge of the total mobilized volume (e.g., Barnhart et al., 2021; Han et al., 2015); (3) reduced or appropriate
67 complexity flow-routing models (e.g., Murray, 2007) that use rule-based abstractions of the key physical processes
68 that control the flow (Clerici and Perego, 2000; Guthrie and Befus, 2021; Gorr et al., 2022; Han et al., 2017, 2021;
69 Horton et al., 2013; Liu et al., 2022) and are typically implemented using just the initial landslide location and volume
70 but often rely on heavy, site specific parameterization and; (4) hybrid modelling approaches that combine mechanistic

71 models with empirical and reduced complexity approaches (D'Ambrosio et al., 2003; Iovine et al., 2005; Lancaster et
72 al., 2003; McDougall and Hungr, 2004).

73 For landscape evolution and watershed sediment yield applications (herein collectively referred to as watershed
74 sediment models, WSMs), the runout model must be scalable in both space and time, and capable of modelling the
75 entire runout process given an internally modelled initial landslide body (e.g. Tucker and Bras, 1998; Doten et al.,
76 2006; Campforts et al., 2022). As such, computationally efficient and parsimonious reduced complexity runout models
77 that evolve the terrain and transfer sediment are often preferred in WSMs, however with simplifications that can
78 restrict model ability to accurately replicate observed inundation extent or depositional patterns. Such simplifications
79 include omitting debris flow erosion and bulking in runout channels, limiting flow to only a single cell in the steepest
80 downstream direction, and assuming debris flows only occupy the width of a single cell (e.g., Tucker and Bras, 1998;
81 Istanbuloglu and Bras, 2005) or link of a channel network (Benda and Dunne, 1997).

82 We developed a new, reduced complexity landslide runout model, called MassWastingRunout (MWR), that bridges
83 the scalable functionality of WSMs with the predictive accuracy of landslide inundation hazard models, without the
84 computational overhead of a detailed mechanistic representation of the runout process, or difficult parameterization
85 typical of other models. MWR models landslide runout starting from the source area of the landslide, making it easily
86 compatible with WSMs that internally determine the initial landslide body size and location. MWR tracks sediment
87 transport and topographic change downstream, and evolves the attributes of the transport material, making it suitable
88 for sediment yield studies. MWR can be calibrated by adjusting just two parameters (S_c and q_c , described in Section
89 2) and is augmented with a Bayesian Markov Chain Monte Carlo (MCMC) calibration utility that automatically
90 parameterizes model behavior to observed runout characteristics (e.g., erosion, deposition, extent). MWR also
91 includes a built-in utility called MWR Probability, designed for running an ensemble of simulations to develop
92 probabilistic landslide runout hazard maps, making MWR suitable for hazard assessment applications.

93 In this paper, we present the conceptualization and numerical implementation of the MWR model (Section 2), describe
94 the calibration utility and its probabilistic implementation (Section 3) and demonstrate basic model response to
95 topographic convergence and slope on a series of synthetic terrains (Section 4). Event-scale applications to replicate
96 observed runout extent, sediment transport, and topographic change at four topographically and geologically unique
97 field sites (see Figure 1) are discussed (Section 5). We test MWR's predictive ability using the parameterization of
98 one site to predict runout hazard at a nearby site and show a brief example of Monte Carlo model runs to determine
99 runout probability from initial landslide source areas defined by an expert-determined potentially unstable slope or a
100 hydrologically-driven landslide hazard model (Section 6). We conclude with a short summary of MWR model
101 performance and suggest how a calibrated MWR can be incorporated into WSMs.



102

103 **Figure 1:** Example landslides used to evaluate calibrated MWR performance: (a) Cascade Mountains, WA: a large debris avalanche
 104 over steep, broadly convergent terrain (photo credit: Stephen Slaughter). (b) Black Hills, WA: large debris flows over a broadly
 105 convergent, gently sloped valley (photo credit: Stephen Slaughter). (c) Rocky Mountains, CO: a moderate sized debris avalanche
 106 over a steep, unconfining divergent hillslope. (d) Olympic Mountains, WA: small debris flows in steep, highly convergent
 107 channels. Image scale varies with depth, but approximate scale of the image is indicated at the location of the scale bar.

108 **2. Description of the MassWastingRunout model**

109 **2.1 Overview of the cellular-automaton modelling approach**

110 MWR is coded as a discrete cellular automaton (CA) model. CA models apply a set of equations or rules (deterministic
 111 or probabilistic) to individual cells of a grid to change the numerical or categorical value of a cell state (e.g., Codd,
 112 1968). In earth sciences, CA models are widely used to model everything from vegetation dynamics (e.g., Nudurupati
 113 et al., 2023) to lava flows (e.g., Barca et al., 1993) to geomorphic transport, in which gravitationally directed erosion

114 and depositional processes modify a digital elevation model (DEM) representation of a landscape (e.g., Chase, 1992;
115 Crave & Davy, 2001; Murray & Paola, 1994; Tucker et al., 2018). Existing CA-based landslide runout models include
116 models by Guthrie and Befus (2021), D’Ambrosio et al. (2003) and Han et al. (2021). In all of these models, runout
117 behavior is controlled by topographic slope and rules for erosion and deposition but conceptualization and
118 implementation differ.

119 In MWR, mass continuity is central to model conceptualization. Of the wide range of landslide runout processes
120 described in the introduction, MWR explicitly represents erosion, deposition, and flow resistance due to debris size
121 and vegetation. Material exchange between the runout material and underlying terrain as well as flow resistance
122 determines runout extent and landscape evolution. Model rules are designed such that they can be parameterized from
123 field measurements. Finally, in MWR, most computations occur only at the location of moving debris, in a manner
124 analogous to the “mobile” cellular automaton implementation of Chase (1992).

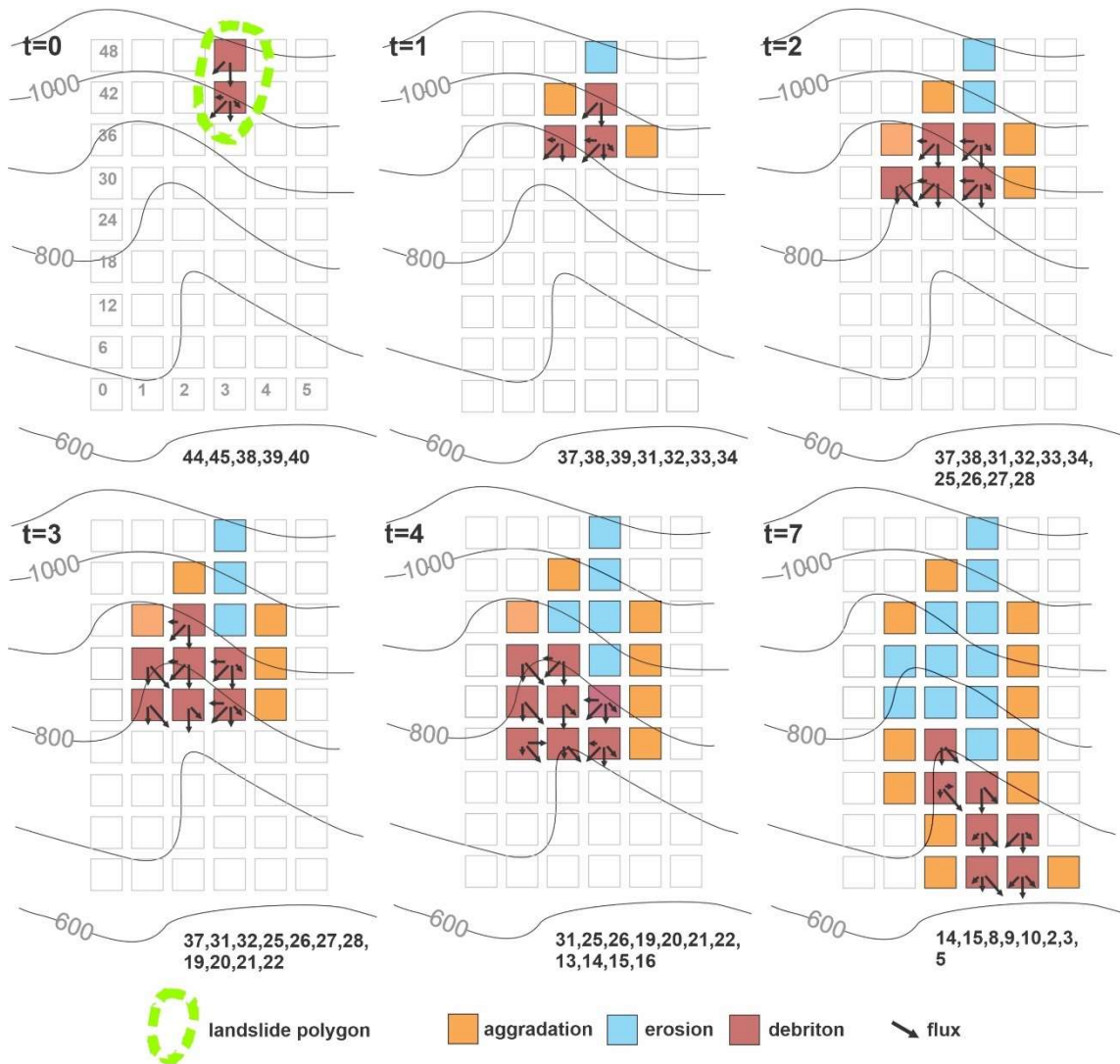
125 Chase (1992) modelled precipitation-driven surface erosion by randomly placing single packets of precipitation on a
126 DEM, which then moved from higher elevation to lower elevation grid cells, eroding and transporting sediment as a
127 function of the slope between the cells. The individual packets of precipitation were referred to as precipitons. In
128 MWR, since we route the downslope progression of debris from a specified mass wasting source area, we refer to
129 these packets of debris as “debritons”. The debritons represent debris flux, here defined as a volume of debris
130 transferred per model iteration per grid-cell area, [$\text{m}^3/\text{m}^2/\text{iteration}$] and are equivalent to the flow depth in the cell.

131 The present implementation of the MWR algorithm is coded in Python and developed as a component of the Landlab
132 earth surface modeling toolkit (Barnhart et al., 2020; Hobbey et al., 2017). MWR uses the Landlab raster model grid,
133 which consists of a lattice of equally sized, rectangular cells. Topographic elevation, derived topographic properties
134 like slope and curvature, and other spatially varying attributes such as regolith depth and grain size, are recorded at
135 nodes in the center of each cell (see Figure 5 of Hobbey et al., 2017). In the subsequent sections we describe the model
136 theory. All parameters and variables used in the theory are listed in the Notation section.

137 **2.2 Mobilization of the initial mass wasting source material (Algorithm 1):**

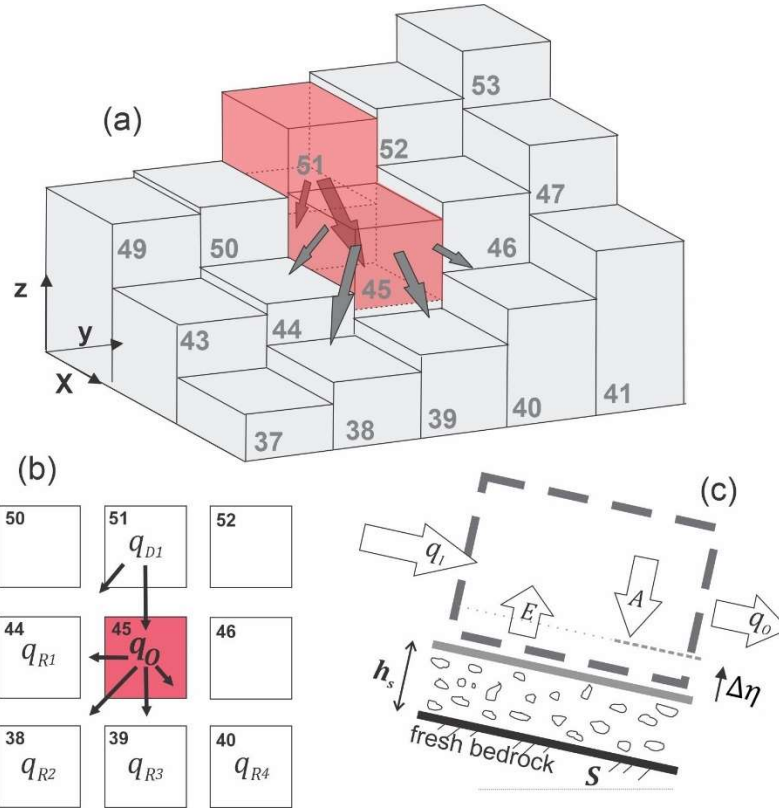
138 To initiate MWR, the user provides maps of initial topography, regolith depth, and the location and depth of the mass
139 wasting source material (e.g., the initial landslide body). Each raster model grid node in the mass wasting source
140 material is designated as a debriton (Figure 2, iteration $t = 0$) with a magnitude equal to the mass wasting source
141 material depth and basal elevation equal to the initial topography minus the mass wasting source material depth. The
142 basal elevation can be thought to represent the rupture or slip surface of the source material and the redistribution
143 (flux) of each debriton to its downslope nodes (receiver nodes) is determined as a function of the slope of the slip
144 surface. At the lowest-elevation debriton of the source material, flux to its downslope nodes is determined using the
145 surface slope of the initial DEM (see flow direction of lowest node in Figure 3a). This implementation helps to ensure
146 that the lowest-elevation debriton in the mass wasting source material moves downslope and movement of upslope
147 debritons are impacted by the geometry of the mass wasting source material. For example, the receiver nodes of the
148 lowest-elevation debriton in the landslide illustrated in Figure 2 (iteration $t = 0$, detailed in Figure 3a) would be
149 identified as those among the eight neighboring nodes whose initial topographic elevation was less than the initial

150 topographic elevation of the node while for the debriton at node 51, the receiver nodes would be identified as those
 151 among the eight neighboring nodes whose topographic elevation is less than the topographic elevation of the terrain
 152 underlying the debriton (the slip surface).



153

154 **Figure 2.** Illustration of initial mass wasting release and runoff down a steep, convergent slope. Variable t indicates model iteration
 155 (not time). Notice how the flow elongates and widens as the model progresses and the number of receiver nodes (numbers listed at
 156 bottom of each panel) and quantity of mobilized material increase. -



157

158 **Figure 3.** (a) Three-dimensional illustration of iteration $t = 0$ in Figure 2, showing initial source material nodes (represented by red
 159 cells) and flux towards downslope nodes. (b) Distribution of q_0 to downslope nodes 38, 39, 40 and 44; (c) illustration of mass
 160 continuity applied to any node that receives a debriton.

161 2.3 Flow routing and rules for erosion, deposition and resistance (Algorithm 2)

162 Algorithm 2 is essentially the runout model. It determines how each debriton traverses and modifies the landscape.
 163 After receiver nodes from the first model iteration are determined in Algorithm 1 (iteration $t=0$), Algorithm 2 is
 164 repeatedly implemented until all material has deposited (i.e., there are no debritons). Each debriton moves one grid
 165 cell per model iteration, the larger the landslide size, the more iterations necessary to evacuate the landslide slip
 166 surface. As each debriton moves, it may erode or aggrade the landscape, impacting the movement of any upslope
 167 debritons. As is common with other reduced complexity models (e.g., Guthrie and Befus, 2021), we assume that
 168 inertial effects have negligible impact on flow behavior (i.e., the kinematic flow approximation) and the downslope
 169 redistribution of a debriton or flux to each of a node's i -th receiver nodes (q_{R_i}) is determined as a function of
 170 topographic slope (slope of terrain under the debriton). We do this using the Freeman (1991) multiple flow direction
 171 algorithm:

$$172 \quad q_{R_i} = q_0 \frac{S_i^a}{\sum_{i=1}^{Nr} S_i^a} \quad (1)$$

173 where q_0 is the total out-going flux from the node and has units of depth [m] per model iteration, Nr is the number
 174 of receiving nodes, i is the index for each receiver node (e.g., $i = 1, 2 \dots Nr$) and S_i is the underlying topographic
 175 slope to the i -th receiver node (Figure 3b). The Freeman (1991) multiple flow direction algorithm is a commonly used

176 approximation for two-dimensional flow, and in this implementation it is handled by a pre-existing Landlab flow-
 177 routing component. The exponent a controls how material is distributed to downslope nodes, with higher values
 178 causing narrower flow (Holmgren 1994). In a braided river cellular-automaton model, Murray and Paola (1997) used
 179 an approximation for turbulent shallow water flow to justify $a = 0.5$ (which is the exponent on the slope factor in
 180 channel friction laws). For our application, we found MWR provided a closer fit to observed mass wasting runout if
 181 $a = 1$, suggesting that the material behavior is more similar to linear-viscous shear flow than to wall-bounded turbulent
 182 shear flow (e.g., as the runout debris flows downslope, it tends to spread less than shallow, turbulent water). The total
 183 incoming flux (again, in units [m] per model iteration) towards a given node (q_I), is determined by summing the flux
 184 from each of the node's donor nodes:

$$185 \quad q_I = \sum_{j=1}^{Nd} q_{D_j} \quad (2)$$

186 Where Nd is the number of donor nodes, and q_{D_j} is the flux from node D_j (the j -th donor node, $j = 1, 2, \dots, Nd$; Figure
 187 3b).

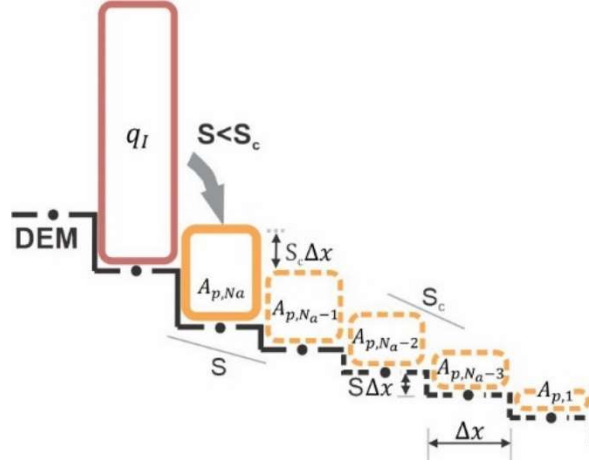
188 As noted by Tucker and Hancock (2010), the flow depths calculated from two-dimensional flow approximations like
 189 (1) can be influenced by the choice of grid-size used to represent the terrain. Additionally, as simplified multi-
 190 directional flow models like (1) neglect the pressure and momentum forces in the movement of flow, they can result
 191 in inaccurate flow width and depth estimates, depending on terrain slope and convergence. Rengers et al. (2016) noted
 192 these limitations when using a kinematic wave approximation of the shallow water equations, as this approximation
 193 lacks a pressure term that facilitates the spreading of the modelled water surface. While the topographic controls on
 194 mass conservation are adequately represented by (1), our model bears such limitations when calculating flow depth
 195 and width. Additionally, in our model, flow depth is used to determine a depth-dependent erosion rate. As such, in
 196 order to avoid unrealistically high flow depths (and erosion rates), we constrain flow depth to an upper limit as:

$$197 \quad h = \min(h_{max}, q_I) \quad (3)$$

198 Where h_{max} is an effective upper limit to flow depth, that in practice can be approximated as the maximum observed
 199 flow depth, as inferred from field indicators or assigned based on expert judgement (See Section 5) and h is the
 200 corrected flow depth used to calculate flow shear stress. This correction allows erosion rates to vary with flux but
 201 prevents unreasonably large values. This flow depth correction does not violate the conservation of mass and runout
 202 mass balance, as h is only used to calculate flow shear stress.

203 To determine aggradation (A) at a node, we use a critical slope (S_c) constraint that permits computationally-rapid
 204 distribution of q_I over multiple nodes. Critical slope constraints or rules are common to many reduced complexity and
 205 landscape evolution models. Chen et al. (2023) showed that when flow inertia can be ignored, S_c can be approximated
 206 from the surface slope of observed deposits. Several landscape evolution models use a S_c -based nonlinear, nonlocal
 207 aggradation scheme (e.g., Campforts et al., 2020; Carretier et al., 2016) but when this rule is implemented with the
 208 debris framework described above, unreasonably tall deposits result when q_I is large and slope at the node (S) \ll
 209 S_c . To resolve this problem, aggradation depth can be limited to $A \leq S_c \Delta x$, (where Δx grid cell length), but we found
 210 that this constraint results in long deposits that parallel the underlying slope when q_I is large. Instead, MWR computes

211 the aggradation depth at a node assuming that the aggradation will spread over N_a nodes until all of q_I is deposited
 212 and that the surface slope of the overall deposit will be equal to S_c , as shown in Figure 4 and described as follows.



213
 214 **Figure 4.** Illustration of aggradation rule used in MWR when q_I is assumed to spread over 5 nodes ($N_a = 5$). Solid yellow box
 215 indicates aggradation amount at a given node. Dashed yellow boxes and lines indicate the geometry of assumed the aggradation
 216 beyond the node. Dots along DEM surface are nodes.

217 Aggradation at a node is determined as:

$$218 \quad A = \begin{cases} 0, & S \geq S_c \\ \min(A_{p,N_a}, q_I), & S < S_c \end{cases} \quad (4)$$

219 Where S is the steepest slope to the node's eight neighbouring nodes, A_{p,N_a} is a potential aggradation depth necessary
 220 to form the beginning of the overall deposit that: (1) begins at the node and spreads over N_a consecutive nodes; (2)
 221 has a total volume equal to $q_I \Delta x^2$; (3) a surface slope equal the critical slope S_c and; (4) an underlying topographic
 222 slope equal to the steepest slope at the node and assumed constant over the N_a consecutive nodes of deposition. From
 223 these assumptions, we can analytically define A_{p,N_a} and N_a as a function of q_I , S_c and S as follows:

224 First, q_I , calculated from (2), can be used to calculate $A_{p,i}$ by expressing q_I as the sum of the N_a deposits that make
 225 up the overall deposit as:

$$226 \quad q_I = \sum_{i=1}^{N_a} A_{p,i} \quad (5)$$

227 where $A_{p,i}$ is the i -th deposition amount in the overall deposit and $i = 1$ is the last node of deposition ($A_{p,1}$; see Figure
 228 4). Since we assume the deposit slope and underlying topographic slope are uniform, the deposition amount at any of
 229 the N_a nodes can be determined from $A_{p,1}$ as:

$$230 \quad A_{p,i} = A_{p,1} + (i - 1)\Delta x(S_c - S) \quad (6)$$

231 From (6) we can re-write (5) as a function of $A_{p,1}$ and rearrange to define $A_{p,1}$ as a function of q_I :

$$232 \quad A_{p,1} = \frac{1}{N_a} q_I - \frac{N_a - 1}{2} \Delta x(S_c - S) \quad (7)$$

233 Substituting (7) into (6) and solving for $i = N_a$, we get an expression for A_{p,N_a} :

$$234 \quad A_{p,N_a} = \frac{1}{N_a} q_I + \frac{N_a - 1}{2} \Delta x (S_c - S) \quad (8)$$

235 Equation (8) can be rearranged into a quadratic equation and solved for N_a as:

$$236 \quad N_a = \frac{-A_{p,1} + \frac{1}{2} \Delta x (S_c - S) \pm \sqrt{\left(A_{p,1} - \frac{1}{2} \Delta x (S_c - S)\right)^2 + 2 \Delta x (S_c - S) q_I}}{\Delta x (S_c - S)} \quad (9)$$

237 We use (8) to solve for A_{p,N_a} and (9) to solve for N_a assuming $A_{p,1} = 1/2 \Delta x S_c$ and rounding the positive solution to
 238 the nearest integer. When implemented using a single debriton, released on a two-dimensional hillslope as illustrated
 239 in Figure 4, the debriton deposits over N_a nodes at a uniform slope equal to S_c . When implemented on an actual three-
 240 dimensional terrain, the interaction between multiple debritons in multiple directions creates a complex deposit whose
 241 slope changes with S_c .

242 To determine erosion depth (E) [m/iteration], we constrain E to the lesser of a potential erosion depth, h_e , and local
 243 regolith depth, h_r :

$$244 \quad E = \min(h_r, h_e) \quad (10)$$

245 where h_e is computed as a function of the basal shear stress of the flow, τ [Pa], (Equations 12 and 13) and the critical
 246 shear stress (τ_c) of the regolith at the node [Pa]:

$$247 \quad h_e = k(\tau - \tau_c)^f \quad (11)$$

248 The coefficient k is an erodibility parameter [m/Pa^f]. Stock and Dietrich (2006) showed that k encapsulates substrate
 249 properties. If h_e is used to represent erosion over geomorphic time scales, with repeated debris flow occurrences in a
 250 single model iteration, k becomes associated with debris flow length and frequency (Perron, 2017). In our application
 251 since we are modelling the erosion associated with a single runout event, as represented by the downslope movement
 252 of the debritons, the coefficient k therefore needs to scale h_e on the order of the average erosion depth caused by a
 253 single debriton. Using this logic, k can be computed using the observed average erosion depth and an estimated length
 254 of the runout material that caused the erosion. Further details on how we determine k from observed runout are
 255 included in the Appendix. The exponent f controls the non-linearity of h_e with shear stress. Many authors (Chen &
 256 Zhang, 2015; Frank et al., 2015; Shen et al., 2020) use a value of 1 for f but field measurements by Schürch et al.
 257 (2011) (see their Figure 3) suggest that f may be less than 1 if τ is assumed to vary linearly with flow depth,
 258 particularly at flow depths greater than 3 meters.

259 MWR includes two options for defining τ : (1) a quasi-static basal shear stress approximation or (2) a grain-size-based
 260 shear stress approximation. The quasi-static basal shear stress approximation (e.g., Takahashi, 2014) is defined as:

$$261 \quad \tau = \rho g h \sin \theta \quad (12)$$

262 where ρ is the density of mass wasting material (grain and water mixture) [kg/m³], g is gravity [m/s²], h is the adjusted
 263 flow depth described in (3) and θ is the topographic slope ($\tan^{-1}(S)$) measured in degrees.

264 The grain-size-based shear stress approximation is defined using an empirical formula by Bagnold (1954):

$$265 \quad \tau = \sigma \tan \varphi \quad (13)$$

266 Where σ is normal stress [Pa], φ is the collision angle between grains, measured from the vertical axis (See Bagnold,
 267 1954), with a value of $\tan \varphi$ typically equal to 0.32. Stock and Dietrich (2006) defined σ as:

$$268 \quad \sigma = \cos \theta v_s \rho_s D_s^2 \left(\frac{du}{dz} \right)^2 \quad (14)$$

269 Where v_s is the volumetric solids concentration, ρ_s is density of the solids [kg/m³], u is flow velocity [m/s], z is depth
 270 below the flow surface [m], du/dz is the shear strain rate [1/s] and D_s is the representative grain size [m]. Stock and
 271 Dietrich (2006) suggested that D_s corresponds to a small percentile of the coarsest fraction of the runout material (D_{88}
 272 to D_{96}) and they approximated du/dz as:

$$273 \quad \frac{du}{dz} = \frac{u}{h} \quad (15)$$

274 Solely for the purpose of computing du/dz , we approximate velocity at a node using a grain-size dependent empirical
 275 formula for debris flow velocity by Julien and Paris (2010) as:

$$276 \quad u = 5.75u^* \log \left(\frac{h}{D_s} \right) \quad (16)$$

277 Where u^* is shear velocity ($\sqrt{gh \tan \theta}$). Substituting (16), (15), (14) and (13) into (11) yields a grain-size dependent
 278 approximation for h_e that mimics the non-linear erosion response to flow depth in Schürch et al. (2011). Additionally,
 279 this form of τ is advantageous because it permits landslide-driven erosion rates to scale with landslide grain size,
 280 which can vary by lithologic region (e.g., Roda-Boluda et al., 2018). As will be shown in Section 5, we obtained
 281 reasonable model calibration at multiple sites by defining D_s from the coarser grain sizes observed in the field at
 282 existing runout-deposits, road-cuts and tree-throw pits.

283 Once A [m] and E [m] have been determined, total out-going flux per iteration, q_o [m] is determined as (see Figure
 284 3c):

$$285 \quad q_o = \begin{cases} q_l - A + E, & q_l \geq q_c \\ 0, & q_l < q_c \end{cases} \quad (17)$$

286 Where q_c is a threshold flux for deposition. When $q_l < q_c$, q_l deposits and q_o becomes zero. The threshold flux q_c
 287 conceptually represents the flow depth below which flow resistance is large enough to cease the forward momentum
 288 of the flow, whether in the form of internal friction or friction due to vegetation and obstructions (e.g., large clasts or
 289 logs). The density and water content of q_l , A , and E are treated as uniform and surface runoff, such as channelized
 290 stream flow or hillslope-infiltration-excess runoff, that might mix with q_l , A , or E is ignored. Once q_l , A , q_o and E
 291 have been determined, change in elevation at a node ($\Delta\eta$) is calculated as:

$$292 \quad \Delta\eta = A - E \quad (18)$$

293 Attributes (e.g., grain size, organic content or any other attribute that is transferred in the flow) of the debriton and
 294 regolith are updated using a volumetric-weighted average approach. First, for each regolith attribute being tracked by
 295 the model, the attribute value delivered to a node from its donor nodes (ξ_D) is determined as:

$$296 \quad \xi_D = \frac{\xi_D \cdot q_D}{q_l} \quad (19)$$

297 where \mathbf{q}_D is a vector containing all q_{D_j} sent to the node, ξ_D is a vector containing the incoming attribute values for
 298 each q_{D_j} , and q_I is the sum of incoming flux from donor nodes defined by (2).

299 Second, the attribute value sent from a node to its receiver nodes (ξ_R) is determined as:

$$300 \quad \xi_R = \frac{\xi_{t-1}E + \xi_D(q_I - A)}{q_o} \quad (20)$$

301 where ξ_{t-1} is the attribute value at the node before any aggradation (i.e., the previous iteration attribute value). Finally,
 302 the attribute value at the node, updated to account for erosion and aggradation (ξ) is:

$$303 \quad \xi = \frac{\xi_{t-1}(h_r - E) + \xi_D A}{A + h_r - E} \quad (21)$$

304 Regolith thickness (h_r) and topographic elevation (η) are updated at a node as:

$$305 \quad \eta = \eta_{t-1} + \Delta\eta \quad (22)$$

$$306 \quad h_r = h_{r,t-1} + \Delta\eta \quad (23)$$

307 Where η_{t-1} and $h_{r,t-1}$ are the topographic surface elevation and regolith thickness at the node from the previous
 308 model iteration. After regolith thickness and topographic elevation have been updated for each debriton, the multi-
 309 direction slope of the DEM, which is needed for implementing Equation (1) the next model iteration, is recomputed.
 310 As the DEM is updated following each model iteration, topographic pits or flat topography may form. These features
 311 have no slope or slope inwards and obstruct debriton movement. To allow a debriton to pass an obstruction, we rely
 312 on a simple work-around: upon encountering the obstruction, the debriton is directed to itself and some portion of the
 313 debris is deposited based on (4). At the end of the model iteration, the node elevation and slope are updated. During
 314 the next iteration, if the remaining mobile debris is no longer obstructed, it moves to its downslope node(s). If the
 315 node is still obstructed, it is again sent to itself until either all material has deposited or the elevation of the node
 316 exceeds that of its neighbour nodes, allowing the debriton to move downslope.

317 **3. Calibration and MWR probability**

318 **3.1 Calibration utility**

319 MWR includes an adaptive, Bayesian Markov Chain Monte Carlo (MCMC) calibration algorithm described by Coz
 320 et al. (2014) and Renard et al. (2006). The MCMC algorithm is implemented as a utility for MWR and identifies a
 321 single set of parameters that best match MWR output to an observed landslide runout dataset. The observed runout
 322 dataset can consist of a single or multiple landslides. Depending on user input, MWR simultaneously or sequentially
 323 models runout from each landslide source area in one model run. To use the calibration utility, the user provides an
 324 initial (prior) guess of the parameter values and their respective probability distribution functions (PDF) that calibrate
 325 the MWR to a specific site. Then, the calibration utility randomly selects a set of trial parameter values (Λ) from the
 326 prior PDFs and runs MWR using Λ . Once the model has completed the run, the algorithm evaluates the posterior
 327 likelihood of the parameter set ($L(\Lambda)$) as the product of model ability to replicate observed runout (described below)
 328 and the prior likelihood of the parameter set. After the first $L(\Lambda)$ has been determined, the utility selects a new set of

329 parameters (Λ_{t+1}) by jumping some distance (described below) from each parameter in Λ space. Depending on the
 330 value of $L(\Lambda_{t+1})$, the algorithm either stays at Λ or moves to Λ_{t+1} . This Markov process is repeated a user-specified
 331 number of times. Jump direction is random, but the algorithm is adaptive because the jump distance changes depending
 332 on if $L(\Lambda_{t+1}) > L(\Lambda)$ occurs more than a user specified threshold value. For a detailed description of the algorithm
 333 see Coz et al., (2014).

334 The $L(\Lambda)$ index is estimated as the product of the prior probability of the selected parameter values, $p(\Lambda)$, and three
 335 other performance metrics as:

$$336 \quad L(\Lambda) = p(\Lambda) * \Omega_T * \frac{1}{\Delta\eta_E^2} * \frac{1}{Q_{sE}^2} \quad (24)$$

337 where Ω_T is the Lee-Salle index (Heiser et al., 2017) for evaluating model planimetric fit and $\Delta\eta_E$ and Q_{sE} are new
 338 dimensionless indices, proposed for this study (described below). The index $\Delta\eta_E$ is the volumetric error of the
 339 modelled topographic change over the entire model domain normalized by the observed total mobilized volume (initial
 340 landslide body + erosion volume). The index Q_{sE} is the mean-cumulative sediment transport error along the modelled
 341 runout path normalized by the observed mean cumulative flow. Larger values of Ω_T and smaller values of $\Delta\eta_E$ and
 342 Q_{sE} indicate modelled runout more closely fits observed. Note that we add a value of 1 to Ω_T and use the squared-
 343 reciprocal values of $\Delta\eta_E$ and Q_{sE} in (24) so that the magnitude of $L(\Lambda)$ is always equal to or greater than zero and
 344 increases with improved fit. The metric Ω_T is written as:

$$345 \quad \Omega_T = \frac{\alpha - \beta - \gamma}{\alpha + \beta + \gamma} + 1 \quad (25)$$

346 where α , β and γ are the areas of matching, overestimated and underestimated runout extent, respectively.

347 The index $\Delta\eta_E$ is determined as:

$$348 \quad \Delta\eta_E = \sqrt{\frac{\sum_{i=0}^p [(\Delta\eta_{oi} - \Delta M_i) \Delta x^2]^2}{V^2}}. \quad (26)$$

349 Where V is observed total mobilized volume and p is the number of nodes in the area made up of the matching,
 350 overestimated and underestimated areas of runout extent and $\Delta\eta_{Mi}$ and $\Delta\eta_{oi}$ are the modelled and observed
 351 topographic change [m] at the i -th node within that extent.

352 To calculate Q_{sE} , we first determine the cumulative sediment transport volume (Q_s) at each node, j along the runout
 353 profile, in a manner similar to the flow volume/mass balance curves in Fannin and Wise (2001) and Hungr and Evans
 354 (2004):

$$355 \quad Q_s = -\Delta x^2 \sum_{i=1}^{u_j} \Delta\eta_{i,j} \quad (28)$$

356 where $\Delta\eta_{ij}$ is the topographic change [m] at the i -th node located upstream of node j , and u_j is the total number of all
 357 nodes located upstream of j . Q_s is computed for both the observed and modelled runout path (Q_{sO} and Q_{sM}
 358 respectively) and Q_{sE} of a runout is determined as:

$$Q_{sE} = \sqrt{\frac{\frac{1}{r} \sum_{j=1}^r (Q_{sO} - Q_{sM})^2}{Q_{sO}^2}} \quad (29)$$

Where r is the number of nodes along the center line of the runout path, and $\overline{Q_{sO}}$ is the observed mean cumulative flow.

As will be detailed in Section 5, field estimates for S_c and q_c vary over the length of the runout path. To account for the heterogeneity of S_c and q_c , we estimate prior distributions of potential S_c and q_c values from field/remote sensing measurements. Then, from model calibration to a DEM-of-Difference (pre-runout DEM subtracted from the post-runout DEM; DoD) using the calibration utility, we find single values of S_c and q_c that allow the modelled DoD to replicate the observed DoD.

We run the calibration utility using a single Markov chain of 2000 repetitions. At most sites, the model converged relatively quickly on a solution and we therefore didn't account for burn-in or evaluate convergence (e.g., Gelman et al., 2021) and considered 2000 repetitions adequate. Future implementations of the calibration utility may include multiple chains, burn-in and a check for convergence. As a final note, many debris flow runout models are evaluated using Ω_T or variations of Ω_T alone (e.g., Gorr et al., 2022; Han et al., 2017) and the MWR calibration utility can also be run solely as a function of Ω_T . However, we found that calibration based on Ω_T (i.e., runout extent) alone results in high parameter equifinality (e.g., Beven 2006); multiple parameter sets result in an equally calibrated model as evaluated by Ω_T . As such, we recommend calibrating debris flow/landslide runout models to an observed DoD. If repeated lidar is available, a DoD can be obtained from before and after scans of the observed runout event. Alternatively, a DoD can be created by hiking the observed runout event and mapping field-interpreted erosion and deposition depths. Additional details on how we prepared DoDs for multiple sites are included in the Supplementary Material.

3.2 Mapping landslide runout hazard

MWR includes an additional utility called MWR Probability that produces landslide runout probability maps. MWR Probability repeatedly runs MWR a user specified Np times, each repetition with a different, randomly sampled parameter set from the posterior parameter PDFs produced by the calibration utility. MWR Probability includes three options for specifying the initial mass wasting source material: (1) a user-provided landslide source area polygon(s) based on field and/or remote sensing observations; (2) a user-defined hillslope susceptible to landslides (e.g., potentially unstable slope), where landslide area and location are randomly selected within, but no larger than the hillslope; this option is useful when the extent of a potential landslide is unknown; and (3) a series of mapped landslide source areas within a watershed, as determined by an externally run Monte Carlo landslide initiation model (e.g., Hammond et al., 1992; Strauch et al., 2018); this option is useful for regional runout hazard applications. If using Option 1, modelled runout probability represents uncertainty in MWR parameterization. If using Option 2 or 3, modelled runout probability reflects uncertainty in both MWR parameterization and landslide location and size.

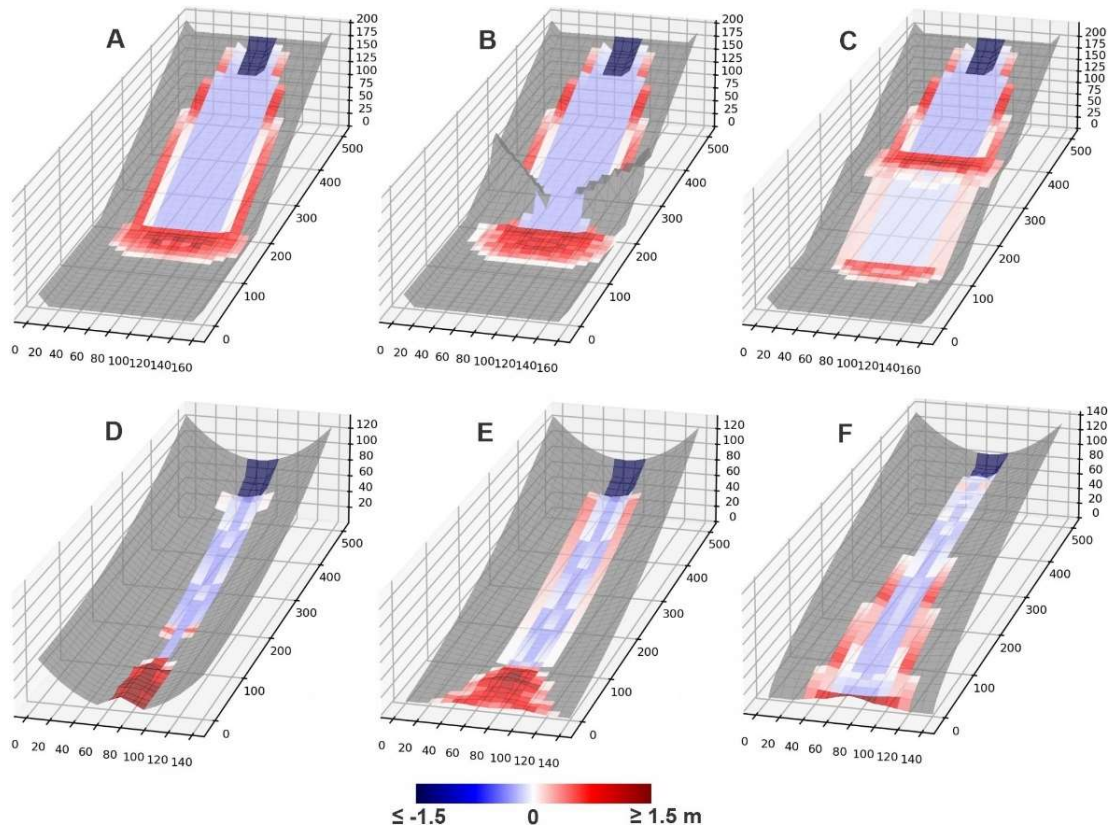
392 For all three run options, each model iteration begins with the same initial topography. After Np model simulations,
393 Np different versions of the post-runout landscape are created and, probability of runout at each node is determined
394 as:

$$395 \quad P(\Delta\eta) = \frac{\text{num}(|\Delta\eta| > 0)}{Np} \quad (30)$$

396 where $\text{num}(|\Delta\eta| > 0)$ is the number of times topographic elevation at a node changes as a result of erosion or
397 deposition from the Np model runs. Probability of erosion or aggradation can be determined by replacing the
398 numerator in (30) with $\text{num}(\Delta\eta < 0)$ or $\text{num}(\Delta\eta > 0)$ respectively.

399 **4. Basic model behavior**

400 We evaluate basic model behavior using a series of virtual experiments. The virtual experiments consist of six
401 synthetic terrains including: (A) a planar slope that intersects a gently sloped plane ($S = 0.001$); (B) a planer slope
402 with a constriction, that intersects a gently-sloped plane; (C) a planar slope that has a bench mid-slope and then
403 intersects a gently-sloped plane; (D) a concave up, uniform-convergence slope; (E) a concave up, variable-
404 convergence slope that widens (convergence decreases) in the downslope direction; (F) a convex up, variable-
405 convergence slope that widens (convergence decreases) in the downslope direction. On each terrain, a 30-meter wide,
406 50-meter long and 3-meter deep landslide is released from the top of the terrain. All six terrains are covered by a 1-
407 meter thick regolith and use the same parameter values ($S_c = 0.03$, $q_c = 0.2$ m, $k = 0.01$, $D_s = 0.2$ m). Each terrain is
408 represented using a 10-m grid. Experiment results are shown in Figure 5.



409

410 **Figure 5.** Shaded, 3-D visualizations of model response to six different synthetic terrains, colored according to the DoD of the
 411 final runout surface. Shading is to scale. Red indicates a positive change in the elevation of the terrain (aggradation) and blue
 412 indicates a negative change (erosion). The 3-D visualization of the DoD is exaggerated by a factor of 5 to make visible in figure.
 413 Grid size is 10 meters.

414 On Terrain A, the landslide spread as it moved downslope and formed levees along the edge of the runout path. The
 415 width of the spread was a function of the multiple flow direction algorithm and resistance along lateral margins of the
 416 runout as represented by q_c . At the slope break at the base of the slope, the material deposited at an angle controlled
 417 by S_c . On Terrain B, the flow initially eroded and deposited identical to the first but near the slope break, the
 418 topographic constriction forced flow depth to increase and exceed q_c , minimizing the formation of levees (because
 419 $q_o > q_c$) and resulted in a slightly larger deposit at the base of the slope. On Terrain C, landslide runout was again
 420 initially identical to the runout on Terrain A; however, upon intersecting the mid-slope bench, most of the runout
 421 material deposited. A small, thinner portion did continue past the bench but eroded at a lower rate than the initial slide
 422 upslope of the bench. Upon intersecting the flat surface at the base of the hillslope, the runout material deposited.
 423 On Terrain D, the landslide and its runout were confined to the center of convergent terrain and only deposited once
 424 the slope was less than S_c . The slide never widened because the uniformly convergent channel shape prevented
 425 spreading and the narrower flow width maintained a higher flow depth, which prevented the formation of levees. On
 426 Terrain E, the landslide again deposited once slope was less than S_c but because topographic convergence of Terrain
 427 E decreases in the downslope direction, as the runout material moved downslope, the deposit spread more than on
 428 Terrain D, which caused thinner flow and deposition along margins of the runout path. On the final terrain, Terrain F,

429 slope is always greater than S_c so deposition was limited to levees along the edge of the flow that formed as the runout
430 spread in response to decreasing convergence.

431 MWR model behavior can be summarized as follows. The displacement and deposition of landslide material predicted
432 by MWR responds to topography in a reasonable manner: Flow width increases as convergence decreases (e.g, Terrain
433 F), which in turn reduces flow depth. Lower flow depths cause lower erosion rates and reduce aggradation extent.
434 Conversely, modelled flow depth increases when convergence increases (e.g., Terrain B). Where the flow encounters
435 broadly convergent or planer slopes, lateral levee deposits form, a common feature of landslides reported in the
436 literature and at sites reported here (see Section 5) that detailed mechanistic models can struggle to reproduce (e.g.,
437 Barnhart et al., 2021).

438 We do not attempt to compare MWR modelled flow with the output of shallow-water-equation based models or
439 observed granular flows (e.g., Medina et al., 2008; McDougall and Hungr, 2004; Iverson and Denlinger, 2001; Han
440 et al., 2015). The cellular automaton representation in MWR does not model the time-dependent evolution of debris
441 flow velocity and depth, and conceptually moves debris instantaneously at each iteration, as driven by changes in the
442 evolving topographic elevation field. Because of that, only the final outcome (modelled runout extent, sediment
443 transport and topographic change) of MWR can be compared with other models or observed runout, which we do in
444 the next section. Also, as described in Section 2.3, behaviour of the multiple flow direction algorithm does vary with
445 grid size. Using a coarser or finer grid, without adjusting model parametrization, could potentially change the runout
446 patterns shown in Figure 5.

447 **5 Model Validation**

448 **5.1 Overview**

449 In this section, we demonstrate the ability of a calibrated MWR to replicate observed runout extent, sediment transport
450 and topographic change at field sites located in the western USA and summarize model calibration results with an
451 evaluation of MWR calibration relative to terrain attributes of the observed runout paths. Note that simply calibrating
452 a model to match field data does not constitute a satisfactory test of model predictive ability (Iverson, 2003). Strategic
453 testing, which involves calibrating the model to one site or period of time and then running the calibrated model at a
454 separate site or period of time (Murray, 2013), is a better indicator. Two of our validation sites, the Cascade Mountains
455 and Olympic Mountains sites, include two separate landslides and subsequent runout and we test model predictive
456 ability at these sites in Section 6.

457 Calibrated model performance is demonstrated at the following field sites (see Figure 6a for locations and observed
458 runout extent): (1) two runout events over the same hillslope in the Cascade Mountains (Washington state [WA],
459 USA): a large debris avalanche in 2009 (Cascade Mountains, 2009) and a moderately-sized debris flow in 2022
460 (Cascade Mountains, 2022) that inundated and flowed within a first-to-second order channel until perpendicularly
461 intersecting a narrow river valley several hundred meters below the landslide (Figure 1a); (2) debris flows in the Black
462 Hills (WA) sourced from a small failure along the toe of a deep-seated landslide (Black Hills, South) and a moderately-
463 sized debris avalanche from a large road fill (Black Hills, North) that flowed several kilometers along a relatively

464 wide, broadly convergent channel before stopping (Figure 1b); (3) a single, moderately-sized debris avalanche in the
 465 Rocky Mountains (Rocky Mountains), the majority of which flowed several hundred meters over a broadly convergent
 466 to divergent hillslope in Colorado (Figure 1c); and (4) a 30-year chronology of small landslides and subsequent debris
 467 flows in the Olympic Mountains (WA) in steep, highly convergent channels that flowed well over a kilometer and
 468 coalesced into a single runout deposit in a dendritic, channelized watershed (Olympic Mountains; Figure 1d). All
 469 landslides initiated during heavy rainfall or rain-plus-snowmelt storm events (WRCC, 2022; NRCS, 2022; Table 1)
 470 but their runout varied in terms of erosion rate, grain size (Figure 6b), depositional behavior (Figure 6c) and the
 471 topographic convergence of the underlying terrain.

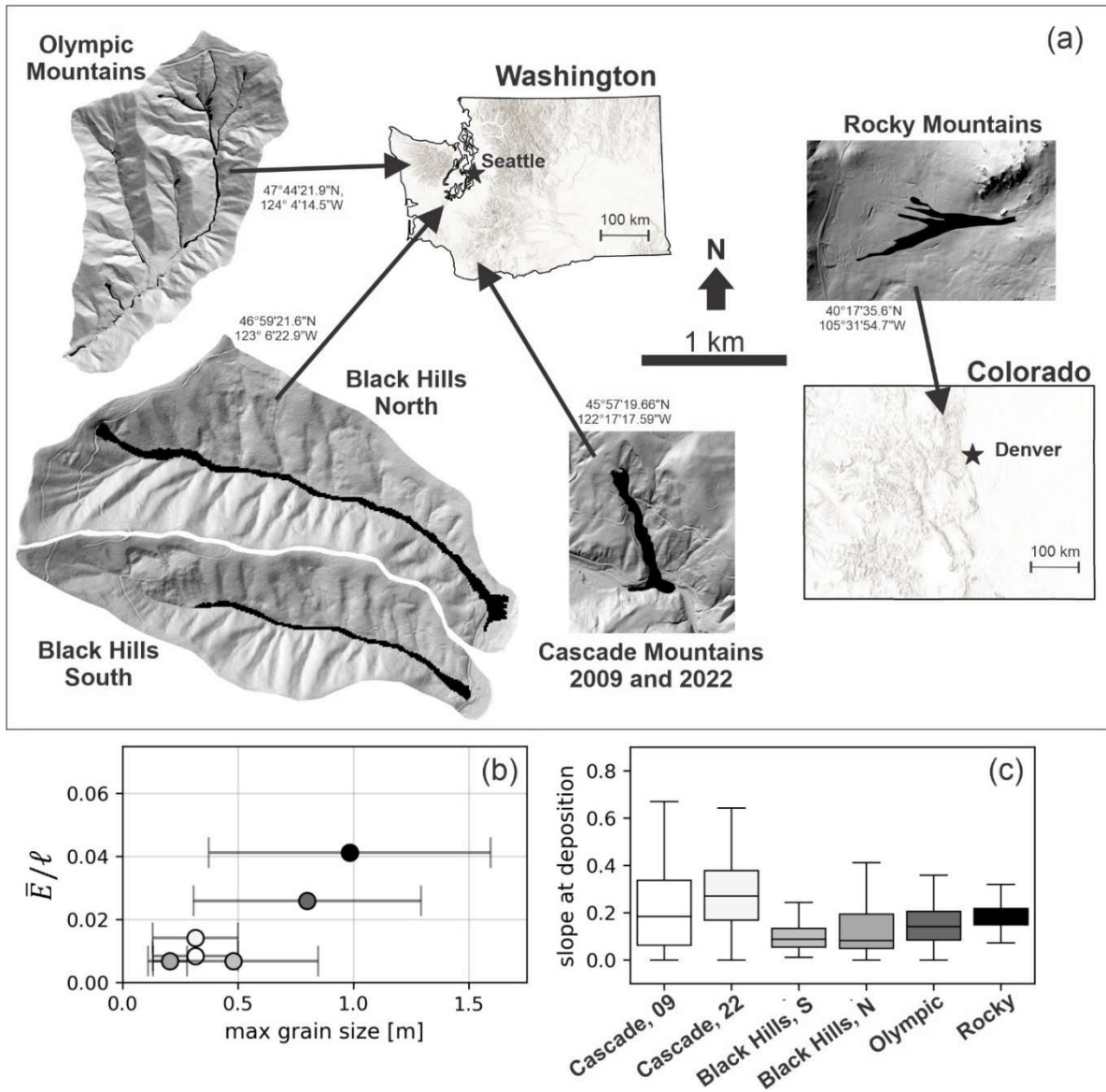
472 **Table 1.** Landslide and runout characteristics

site	Cascade Mountains 09	Cascade Mountains 22	Black Hills, south	Black Hills, north	Rocky Mountains	Olympic Mountains
initial landslide body length., ℓ [m] ^a	185	55	80	75	40	45
initial landslide body width [m] ^a	86	53	13	69	25	15
initial landslide body depth [m] ^a	6.9	7.5	1.4	3.6	4.6	1.5
initial landslide body vol. [m ³] ^a	110,000	22,000	1,500	18,500	4,600	1025
2-day cumulative precipitation + snowmelt [mm]	120+85	140+75	205+5 0	205+5 0	193+0	100 - 220 + ?
maximum grain size [m]	0.316	0.316	0.48	0.206	0.984	0.8
slope range of positive-net deposition [%]	1 - 15	1 - 15	<1 - 10	<1 - 8	16 - 25	5 - 15
average flow depth in scour zone [m]	4	2	2	3	3	3
average channel slope in scour zone [m/m]	0.25	0.25	0.15	0.15	0.4	0.3
average channel width in scour zone [m]	45	20	25	35	55	10
length of erosion, [m]	600	340	1210	1345	360	2550
erosion area, A_e [m ²]	28,400	6,600	22,800	52,400	20,800	28,900
erosion volume, $\sum E \Delta x^2$ [m ³] ^b	44,547	5,125	12,332	26,815	34,275	33,725
average erosion per unit length of runout debris, \bar{E}/ℓ , [m/m]	0.0085	0.014	0.0068	0.0068	0.041	0.026
k	0.020	0.034	0.017	0.020	0.076	0.051
growth factor, [m ³ /m]	74.2	15.1	10.2	19.9	95.2	13.2
average observed $ \Delta\eta $ [m]	2.4	2.2	0.53	0.63	0.89	1.4
total erosion volume / total mobilized volume ^c	0.29	0.19	0.89	0.59	0.88	0.97

473 ^a for the Olympic Mountains site, width and depth are average values and length and volume are defined as the
 474 average cumulative value upstream of each runout path

475 ^b excludes landslide volume

476 ^c total mobilized volume = initial landslide body + erosion volume



477

478 **Figure 6** (a) Landslide locations in Washington and Colorado states. Coordinates next to each site are WGS84. Shaded DEMs of
 479 each site are shown at the same scale. (b) Observed average erosion rate per unit landslide length (\bar{E}/ℓ) relative to the observed
 480 average-maximum grainsize. Error bars indicate standard deviation. (c) Underlying topographic slope of observed deposition.

481 5.2 Model setup and field parameterization

482 Each model was set up on a 10-meter grid representation of the pre-event DEM with either a uniform or spatially
 483 varying regolith thickness (detailed for each site in the Supplementary Material). The length (ℓ) and area of the initial
 484 mass wasting source material (e.g., the initial landslide body) was interpreted from a combination of Lidar DEM, air-
 485 photo and field observations. The average depth of the initial landslide body was measured in the field or from the
 486 DoD. The volume of the initial landslide body was determined as the area times the average depth. An average width
 487 was determined as the area divided by the length. At the Olympic Mountains site, where the observed runout pattern
 488 formed as a result of multiple landslides, (see Supplementary Material), landslide depth and width values listed in

489 Table 1 are average values and landslide length, area and volume values are the average cumulative value upstream
490 of each runout path. At all locations, we use Equation (13) to approximate shear stress. We field-surveyed each site,
491 noting the maximum flow depth (inferred from initial landslide body volume and height of scour marks and width of
492 channel in erosion zone), typical deposition and erosion depths and the size of the largest grains in the runout deposits.
493 We estimated parameter values from these field and remote observations (See Table 1). A site-specific value for k
494 was determined as a function of the observed average erosion depth (determined as total erosion volume divided by
495 the erosion area, \bar{E}) relative to the length of the runout debris, which we approximated as the length of the initial
496 landslide body (ℓ). Further details are described in the Appendix.

497 The volume of the initial landslide body ranged in volume from 400 to 110,000 m³ across sites. At all sites, erosion
498 and subsequent entrainment added to the total mobilized volume (initial landslide body + erosion volume), but the
499 contribution was highly variable. The erosion volume divided by the total mobilized volume was as low as 0.19 at the
500 Cascade Mountains, 2022 landslide to as high as 0.97 at the Olympic Mountains landslides (Table 1).

501 The average maximum grain size varied from 0.2 m at the Black hills sites to nearly 1 m at the Rocky Mountains Site
502 (Figure 6b, Table 1). Values of \bar{E}/ℓ ranged from 0.007 to 0.041 [m/m] with the highest rate occurring at the Rocky
503 Mountains landslide and the lowest at the Black Hills sites. Details on grain-size samples and data collected in the
504 field are described in the Supplementary Material. In terms of growth factors (average volumetric erosion per unit
505 length of the erosion-dominated region of the runout path, Hungr et al., 1984; Reid et al., 2016) values ranged from
506 10 m³/m at the Black Hills South site to 95 m³/m during the Rocky Mountains landslide (Table 1).

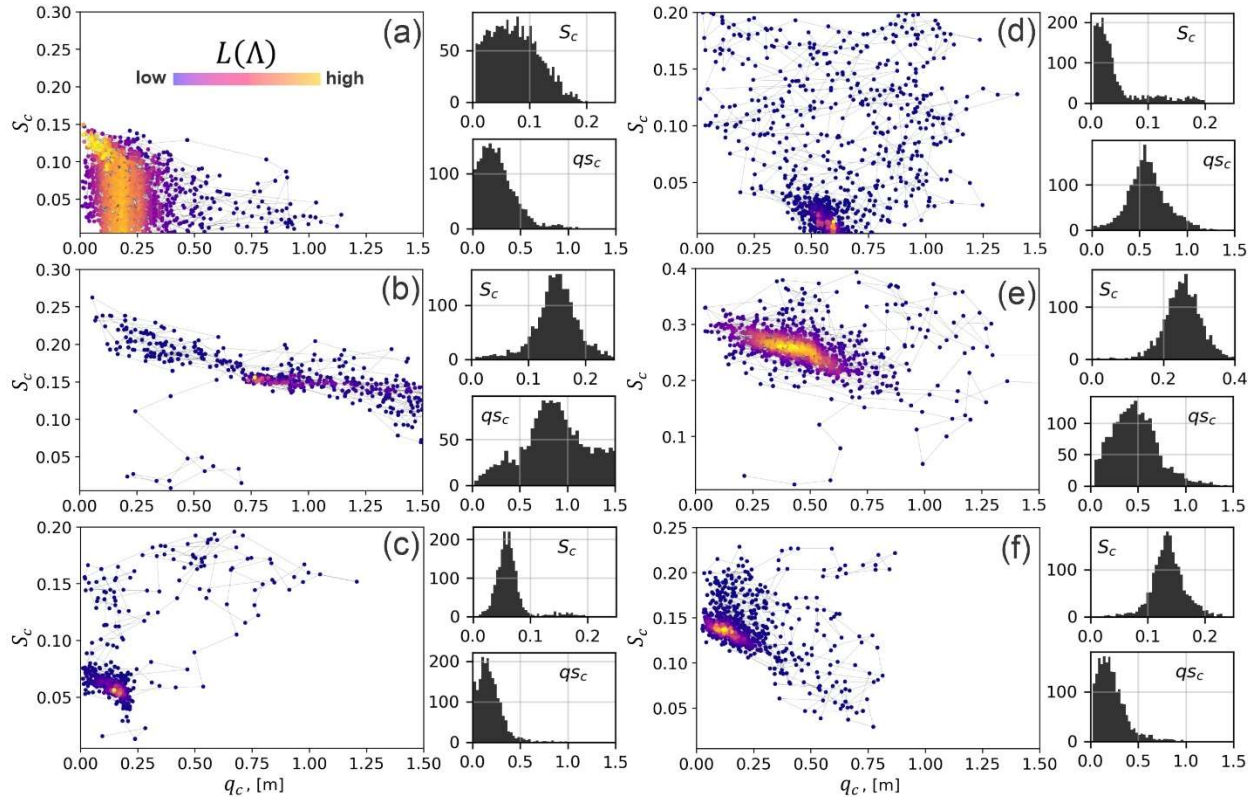
507 The median values of topographic slopes at which observed deposition occurred (i.e., $\Delta\eta > 0$, inferred from the DoD)
508 ranged between 0.1 and 0.3 across sites, while deposition was also observed in much steeper (>0.4) slopes, and much
509 flatter slopes at some sites (Figure 6c) (Table 1). The slope of channel reaches where net deposition (cumulative
510 erosion and deposition; e.g., Guthrie et al., 2010, inferred from field observations) was positive tended to be lowest at
511 the Black Hills site ($<1\%$ to 10%) and highest at Rocky Mountains site (16% to 25%).

512 We defined uniform prior distributions of S_c and q_c and then used the calibration utility to find the best-fit parameter
513 values (parameter values corresponding to the highest $L(\Lambda)$). Minimum and maximum values of S_c were initially
514 estimated from the range of observed slope of areas of positive-net deposition (Table 1). Minimum and maximum
515 values of q_c were set as 0.01 to 1.75, which roughly represents the range of minimum observed thickness of debris
516 flow termini in the field at all of the validation sites. For the purpose of implementing the calibration utility, we
517 prepared a DoD of each site. The DoD was determined either from repeated lidar or field observations as detailed in
518 the Supplementary Material.

519 **5.3 Calibration and model performance**

520 Markov chains, colored according to the likelihood index, $L(\Lambda)$ are plotted in the S_c - q_c domain, along with
521 histograms of sampled S_c and q_c values for each landslide in Figure 7. Each Markov chain includes 2000 model
522 iterations. The runtime for 2000 model iterations depended on model domain, landslide size and number of landslides
523 modeled but varied from roughly 1.5 for the Cascade Mountains, 2022 landslide to 6 hours for the Olympic Mountains

524 landslides on a 2016 2.1 GHz Intel Core Xeon, 32 GB memory desktop. The chains show a wide array of sampling
 525 patterns and parameter ranges but broadly speaking, at all sites, the algorithm jumped within S_c - q_c space towards
 526 higher $L(\Lambda)$, to form bell-shaped posterior distributions for each parameter. Depending on the landslide type, the
 527 calibration algorithm converged on different S_c - q_c pairs. For example, at the Cascade Mountains site, the calibration
 528 utility converged to smaller q_c and S_c values for the 2009 event (Figure 7a), which permitted thinner flows over lower
 529 slopes and effectively made the 2009 modelled runout more mobile relative to the 2022 modelled runout (Figure 7b).
 530 At the Rocky Mountains site (Figure 7e), a relatively high q_c value helps control lateral extent of the modelled runout
 531 that in the observed runout was controlled by standing trees (see Supplementary Material).



532
 533 **Figure 7.** MWR calibration results for (a) Cascade Mountains, 2009; (b) Cascade Mountains, 2022, (c) Black Hills, South; (d)
 534 Black Hills, North; (e) Rocky Mountains and; (f) Olympic Mountains. Each result shows a scatter plot of the sampled S_c and q_c
 535 values, colored by their relative $L(\Lambda)$ value. Line between points indicates jump direction. Note y-axis scale differs between
 536 plots. To the right of each scatter plot are histograms of the iterated S_c and q_c parameters, which can be normalized to represent
 537 an empirical PDF of the possible S_c and q_c values that calibrate MWR to the site. Histogram y-axis is count and x-axis is S_c or
 538 q_c , as indicated on the histogram.

539 Profile plots of modelled Q_s and maps of the modelled planimetric runout extent, colored to indicate where the runout
 540 matched (α), overestimated (β) or underestimated (γ) the observed runout are shown in Figure 8. Values of Ω_T we
 541 obtained with MWR are comparable or higher than reported values of Ω_T in the literature that used a variety of models
 542 (Gorr et al., 2022; Barnhart et al., 2021; Note, to compare Ω_T values to those studies, subtract 1 from values reported
 543 in this study). Across the sites, the volumetric error of the model, $\Delta\eta_E$, ranges between 6% and 15% (median 9.1%)
 544 of the total mobilized volume from the observed DoD. An overall <10% volumetric error is reasonable considering
 545 the low number of parameters required to calibrate MWR and that empirical estimates of total mobilized volume used

546 to run other runout models can vary by as much of an order of magnitude (e.g., Gartner et al., 2014; Barnhart et al.,
547 2021). Model performance in predicting cumulative sediment transport along the runout profile was within similar
548 error ranges. Except for the Rocky Mountains site where MWR consistently modelled wider-than-observed flow, the
549 mean-cumulative sediment transport error along the runout profile (Q_{sE}) were limited to 5%-19% of the mean
550 cumulative flow determined from the observed DoD.

551 MWR generally successfully replicates observed sediment transport along the runout path via model parameterizations
552 that are unique to each landslide. For example, the profile plots of Q_s at the Cascade Mountains site (Figure 8a and
553 8b) show that during the 2009 landslide, all of the runout material flowed past the first 750 meters of the runout path.
554 During the 2022 landslide, material began to deposit just down slope of the initial landslide scar, as both observed and
555 modelled Q_s reverse slope, indicating loss in downstream volume flux. Model comparisons in the Cascade Mountains
556 site were limited to the upper 750 m of the hillslope because a large portion of the runout material was lost to fluvial
557 erosion in the valley (see Supplementary Material).

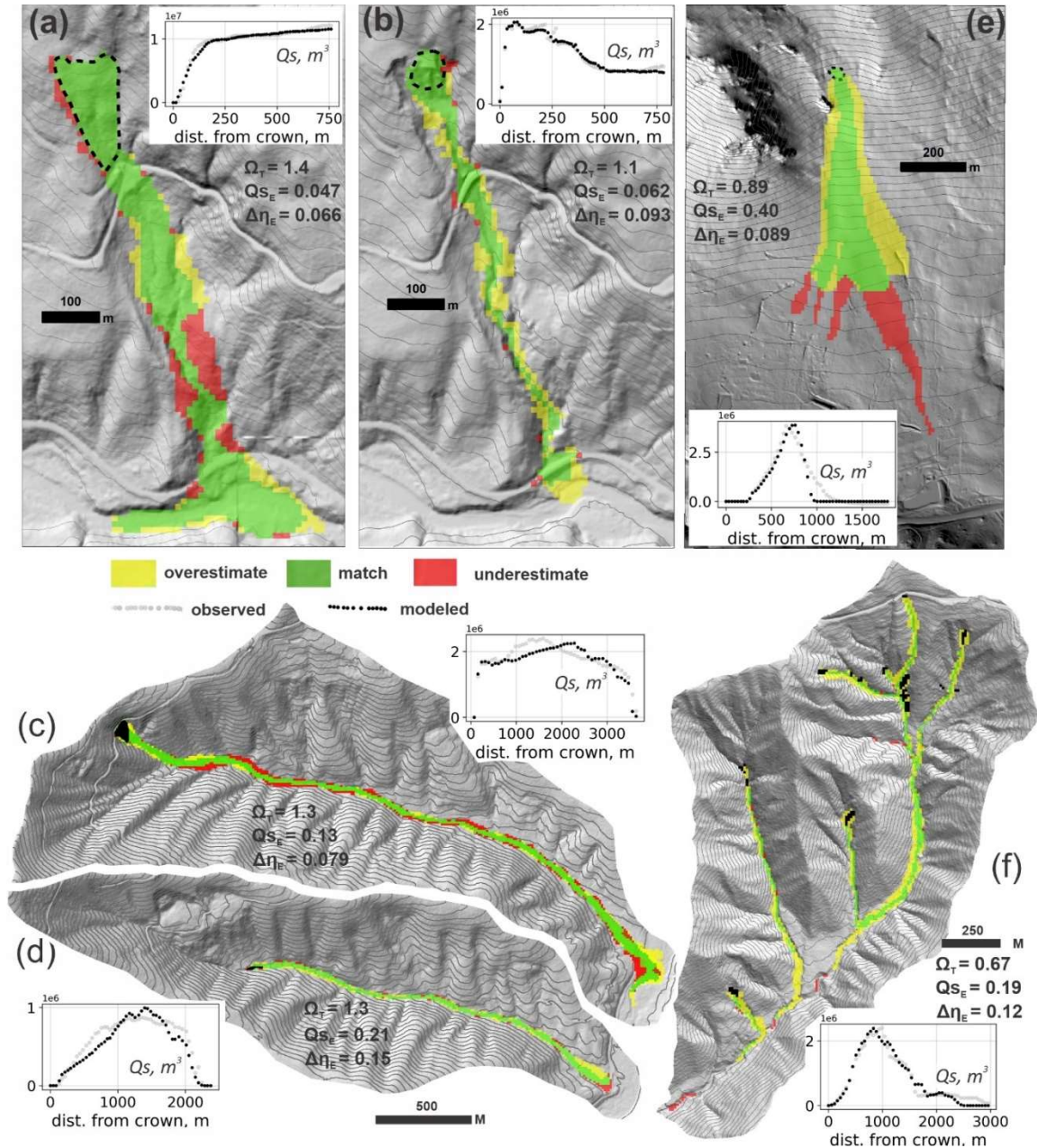
558 MWR also successfully replicates the observed sediment transport patterns at the Olympic Mountains site (profile plot
559 of Q_s in Figure 8f) and to a lesser degree, the Rocky Mountains site (Figure 8e). This finding is notable, because at
560 the Olympic Mountains site, observed runout extent and sediment depositional pattern were heavily impacted by
561 woody debris. Similarly, at the Rocky Mountains site, the width of the runout appeared to be restricted by trees. (See
562 Supplementary Material).

563 Using a fixed cell size of 10-m might have impacted model performance in some areas. MWR tended to over-estimate
564 the runout width for small landslides like the Olympic Mountains and Cascade Mountains, 2022 sites (yellow zones
565 in Figures 8f and 8b), likely because of the 10-m grid size used to represent the terrain. A 10-m DEM is generally
566 accepted as a good balance between model detail and computational limitations (e.g., Horton et al., 2013). However,
567 for small landslides, the 10-m grid is close to the size of the channels that controlled observed runout (see Figure 1d)
568 and may not have accurately represented the terrain. Modelled flow was less topographically-constrained and tended
569 to flow over a wider area of the terrain than observed in the more confined and smaller channels within the axis of the
570 runout valleys.

571 Because MWR does not have an explicit representation of flow momentum, it may show poor performance in regions
572 of the runout path where flow momentum is the primary control on runout extent. For example, at the Cascade
573 Mountains, 2009 slide, MWR underestimates the slope-perpendicular flow over a bench (large red zone in Figure 8a).
574 Review of model behavior for this slide (Figure 9) shows how MWR successfully mimics diverging flow around a
575 broad ridge upslope of the bench (iteration $t=28$ in Figure 9), but afterwards continues to follow topographic slope
576 and converges too rapidly into a narrow ravine along the west edge of the bench (iteration $t=40$ in Figure 9; compare
577 to runout scar in air photo and underestimated region on topographic bench in Figure 8a). At the Rocky Mountains
578 site, in addition to standing trees, the forward momentum of the runout material may have also restricted lateral spread
579 of the observed runout. Modelled runout is consistently too wide.

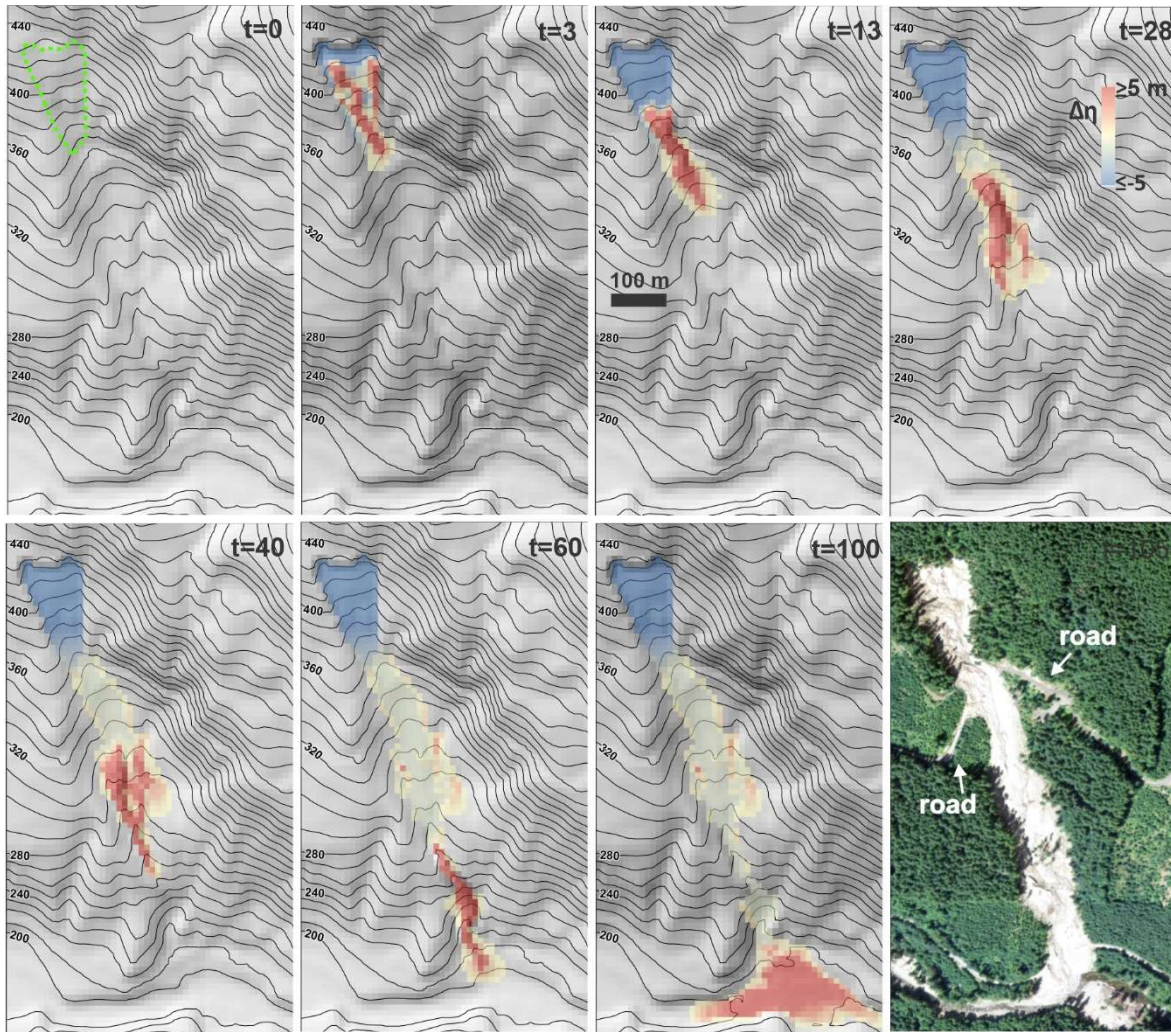
580 Overall, calibration was best at the Cascade Mountains, 2009 landslide (values of Ω_T are highest and values of $\Delta\eta_E$
581 and Q_{sE} are lowest) and poorest at the Rocky Mountains and Olympic Mountains sites (Values of Ω_T are lowest and
582 Q_{sE} and $\Delta\eta_E$ are highest). At both the Rocky Mountains and Olympic Mountains sites, because we lacked repeat lidar,

583 we created the DoD from a map of field estimated erosion and deposition depths and estimated the pre-event DEM.
 584 The lower calibration scores may indicate that field estimated DoDs were not as accurate as those determined via lidar
 585 differencing. Another source of uncertainty that we have not addressed in our study is regolith thickness. At most
 586 sites, we used a uniform thickness. As regolith thickness limits maximum erosion depth (i.e., Equation 10) using a
 587 spatially accurate regolith thickness may improve model performance. Finally, except for the Rocky Mountains site,
 588 where topography was unusually planar and the model seemed to consistently over-estimate flow width, at most sites,
 589 MWR does not appear to have a strong systematic bias in modeled output, which suggests that MWR may not have
 590 any structural weaknesses. In the next section, we evaluate model performance relative to runout path topography.



591
 592 **Figure 8.** Calibrated model performance as indicated by maps of modeled runout extent, profile plots of observed and modeled
 593 cumulative sediment transport along the centerline of the runout path (Q_s , see Equation 28) and reported values of Ω_T , $\Delta\eta_E$ and

594 Q_{SE} . Y-axis label for profile plots of Q_s indicated on plot. In all maps, up is north except in (e), north is towards the left. (a)
 595 Cascade Mountains, 2009; (b) Cascade Mountains, 2022; (c) Black Hills, North; (d) Black Hills, South; (e) Rocky Mountains; (f)
 596 Olympic Mountains.



597
 598 **Figure 9.** Illustration of modeled runout of the Cascade Mountains, 2009 landslide beginning from the initial movement of the
 599 landslide body to final deposition in the river valley that demonstrates MWR response to topography. Note how the landslide slip
 600 surface directs the initial flow. Topography lines reflect the underlying terrain, which is updated after each iteration. Air photo in
 601 last panel shows observed runout extent. Note that upper road is not part of the observed landslide runout path.

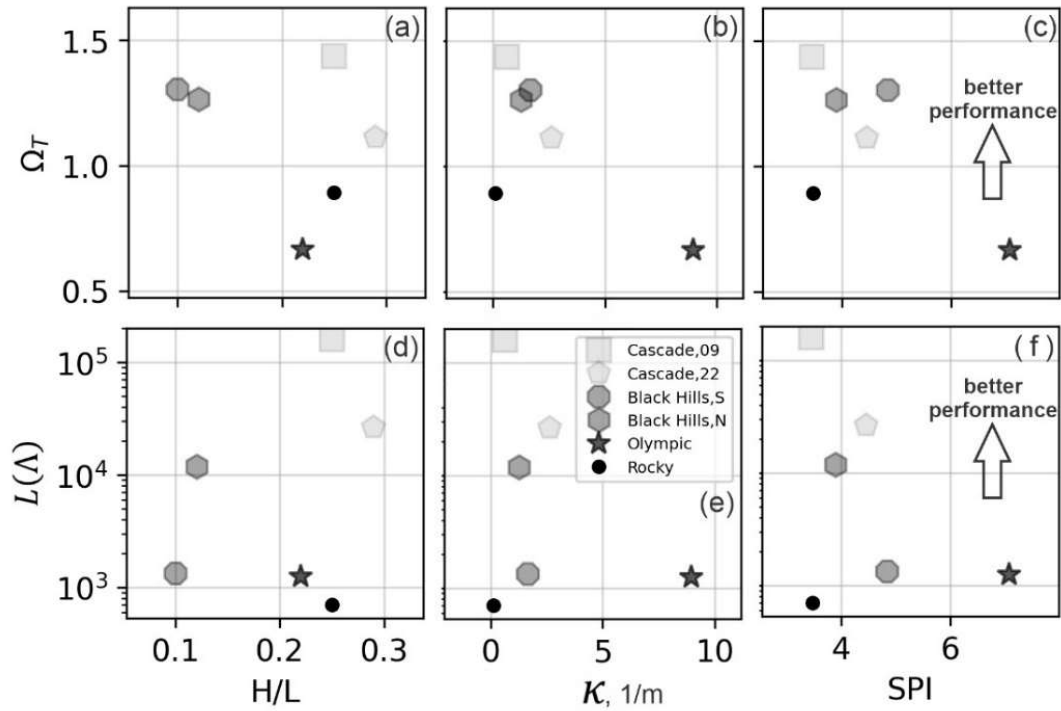
602 Model behavior at the Rocky Mountains site suggests that MWR performance may systematically vary with
 603 topography (e.g., it may not perform as well on planar hillslopes). To check for systematic model variation, we
 604 compared model performance with three topographic indices described by Chen & Yu (2011). The indices are
 605 computed from the terrain in the observed runout extent and include the relief ratio (H/L), mean total curvature (κ)
 606 and the mean specific stream power index (SPI). The index H/L equals the average slope of the runout path (or
 607 relative relief), determined as the total topographic relief of the runout (measured from the center of the landslide to
 608 the end of the runout path) divided by the horizontal length of the runout and indicates the mobility of the runout.
 609 Index κ represents topographic convergence, which is the second derivative of the terrain surface, with increasingly
 610 positive values of index κ reflecting growing topographic convergence and concave-up channel profile (e.g.,

611 Istanbuluoglu et al., 2008). The index SPI is determined as the natural log of the product of the contributing area and
612 slope. Indices κ and SPI are computed at each node in the runout extent and model performance is compared to the
613 mean value.

614 Comparison of model performance with respect to the topographic indices in Figure 10 shows: slightly improved
615 model performance over runout paths that are less convergent (lower SPI and κ values) and on steeper terrain (higher
616 H/L) but neither trend is significant. The latter finding appears to be mostly a result of how well modelled sediment
617 transport and topographic change (Q_{sE} and $\Delta\eta_E$) replicated observed, as there does not appear to be a trend in Ω_T with
618 H/L and the two best performing models (both Cascade Mountains landslides) had the lowest (best) Q_{sE} values and
619 low $\Delta\eta_E$ values. Both findings are likely impacted by the grid size we used to represent terrain. As noted above, at all
620 sites we used a 10-m grid, but at some sites 10-m doesn't quite capture the relief of channelized topography that
621 controlled observed runout, leading to modelled runout that was considerably wider than observed and causing low
622 Ω_T value (this is especially true at the Olympic Mountains site, Figure 10a, b and c). Also, it is important to note that
623 these indices were calculated for the extent of the observed debris flows and may not represent the topographic form
624 that controlled the model.

625 In summary, using the calibration utility, we showed how MWR can be calibrated to a range of different landslide
626 types and runout terrains. To a certain degree, though calibration, MWR can be parameterized to compensate for
627 deficiencies in the DEM or processes not explicitly represented in the model (momentum, woody debris). While model
628 performance at the Rocky Mountains site suggests MWR may not perform as well on planar hillslopes, a relationship
629 between model performance and topography was not eminent. This finding is likely a result of the contributions of
630 numerous factors other than the terrain form, such as the DEM resolution, the quality of the DoD and importance of
631 processes not explicitly included in the model that also impact performance.

632



633
 634 **Figure 10.** Illustration of model calibration, as reflected by the posterior parameter likelihood $L(\Lambda)$ and planimetric fit (Ω_T)
 635 relative to topographic indices. There is no strong trend between the topographic indices and calibration performance. Note,
 636 curvature values are scaled by a factor of 100.

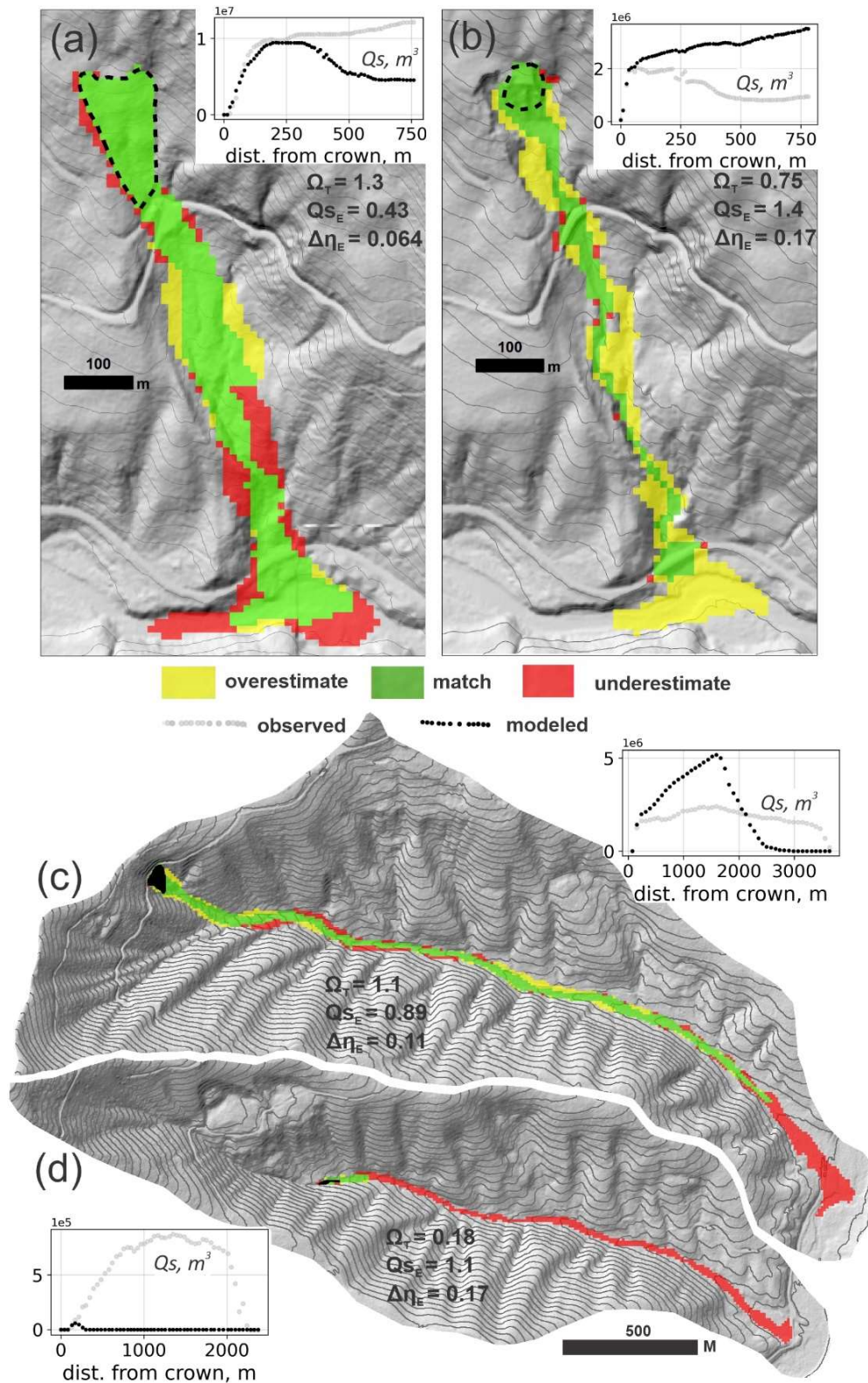
637 6 Discussion

638 6.1 Strategic testing of MWR for hazard mapping applications

639 Having demonstrated model response to topography and calibrated performance for a variety of landslides and runout
 640 terrains, we now strategically test MWR using the Cascade Mountains and Black Hills sites. Since both of these sites
 641 include two separate landslides, we can thus test model performance by swapping best-fit model parameters at each
 642 site, rerunning the models and comparing results with the original, calibrated results. At the Cascade Mountains site,
 643 the 2009 and 2022 landslides originated on the same hillslope (Figure 8a and 8b). At Black Hills site, the two landslides
 644 occurred on different hillslopes but in adjacent east-west oriented watersheds (Figure 8c and 8d).

645 As shown in Figure 11, at three of the landslides (both Cascade Mountains landslides and the Black Hills, North
 646 landslide), when the best-fit parameters from the other landslide are used to predict runout, the accuracy of modelled
 647 runout planimetric extent drops but resultant Ω_T values can still be as high or higher than values reported in other
 648 studies (compare to equivalent Ω_T values in Gorr et al., 2022 and Barnhart et al., 2021). In terms of modelled sediment
 649 transport and topographic change, swapping best-fit parameters has a more substantial effect. At the Cascade
 650 Mountains, 2009 landslide, using the 2022 best-fit parameter values causes about half of the modelled runout material
 651 to prematurely deposit on the hillslope, reducing the amount of sediment that reaches the valley floor (Q_{SE} increases
 652 by a factor of nine; Figure 11). Using the Cascade Mountains, 2009 parameter values on the Cascade Mountains, 2022

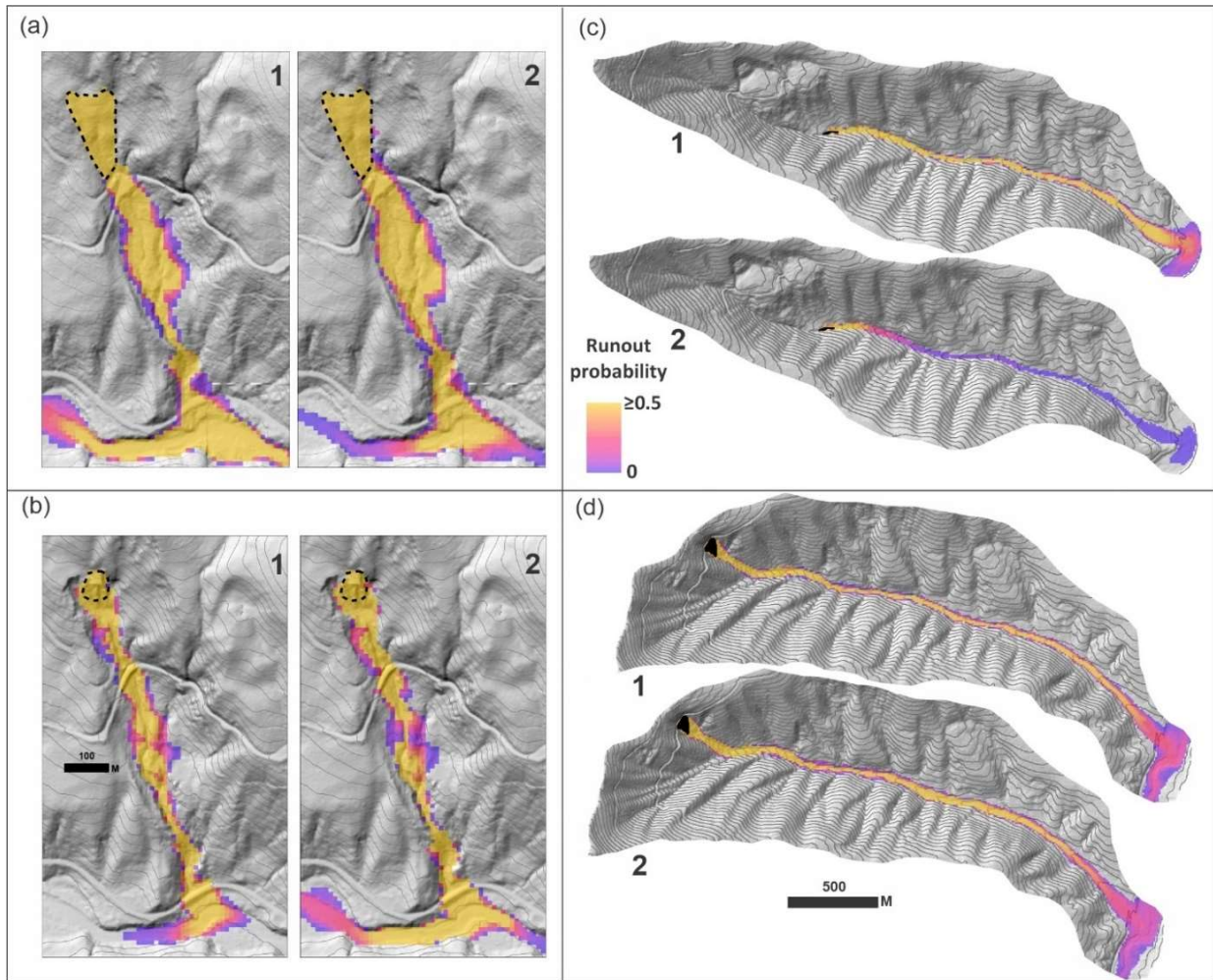
653 landslide (Figure 11b) increases modelled runout extent and results in nearly four times the entrainment and transport
654 of sediment to the valley floor, causing Q_{sE} to increase by a factor of 20 and $\Delta\eta_E$ by 83%. At the Black Hills site,
655 using the South basin best-fit model parameters at the North basin causes Q_{sE} and $\Delta\eta_E$ increase by 83% and 39%
656 respectively (Figure 11c). Unlike the other three landslides, swapping best-fit parameters at the Black Hills, South
657 landslide results in both large sediment transport and runout extent error because the North landslide best-fit
658 parameters applied to the South landslide causes the model to entrain too little and stop prematurely (Figure 11d).
659
660



661

662 **Figure 11.** Model performance using the neighboring landslide parameter values, as indicated by modeled runout extent, profile
 663 plots of Q_s , reported values of Ω_T , $\Delta\eta_E$ and Q_{sE} . Compare with Figure 8. (a) Cascade Mountains, 2009; (b) Cascade Mountains,
 664 Black Hills, North; (d) Black Hills, South

665 As landslide hazard models often forecast hazard probabilistically, an alternative test to simply swapping the best-fit
 666 parameters is to swap parameter PDFs determined from the calibration utility and compare probability of runout at
 667 each model node (Equation 30). As shown in Figure 12, similar to the first test, at three of the landslides, using the
 668 parameter distribution associated with the neighbouring landslide results in relatively minor changes in whether runout
 669 is likely to occur versus not occur (probability of runout $\geq 50\%$; Figures 12a, 12b and 12d) but at the Black Hills South
 670 landslide, swapping parameter PDFs causes a large change in runout probability (Figure 12c).
 671



672 **Figure 12.** Model tests by swapping parameter PDFs and comparing runout probability at the (a) Cascade Mountains, 2009; (b)
 673 Cascade Mountains, 2022; (c) Black Hills, South and; (d) Black Hills, North sites. (1) runout using parameter distributions of the
 674 site and (2) runout using parameter distributions of the neighboring site.
 675
 676

677 The results of these two tests suggest that site-specific calibration may be needed to accurately predict runout behavior
 678 using MWR, especially when the user aims to apply MWR to sediment yield analyses; however, we suspect that this
 679 finding is a consequence of testing the model at sites with very different landslide types and runout processes. At sites
 680 like the Cascade Mountains and Black Hills sites, which consisted of different landslide processes including small,
 681 confined debris flows to large, unconfined debris avalanches, MWR may need to be calibrated to each type of landslide
 682 and predictive applications might involve applying the appropriate parameter set based on landslide type.

683 Although the need for calibration of MWR may limit model transferability across sites, this limitation holds true for
684 most physics-based models. Barnhart et al. (2021) compared the ability of three different detailed-mechanistic models
685 to replicate an observed post-wildfire debris-flow runout event in California, USA. All three models used a shallow-
686 water-equation-based approach that conserved both mass and momentum, representing the flow as either a single
687 phase or double phase fluid. All models gave comparable results in simulating the event, suggesting that there may
688 not be a “true” best model. Despite the high level of detail and processes explicitly included in each model, all models
689 were sensitive to and required an estimate of the total mobilized volume, and the ability to replicate observed runout
690 ultimately depended on calibration of the parameters used to characterize debris flow properties.
691 Finally, in regions where landslide processes are relatively uniform (like the Olympic Mountains site),
692 parameterization determined through calibration to one landslide might be transferable across sites. Additionally, as
693 noted in Section 3.1, we found numerous parameter combinations allowed MWR to match observed runout extent.
694 This finding suggests that if the project aim is limited to an evaluation of runout extent, model calibration to the site
695 may not be as critical and parameter values from calibration to nearby landslides or even globally-available repeated
696 DEMs and airphotos that show the slope of past landslide deposits (for S_c) and how thick their frontal lobes are at the
697 point of deposition (for q_c), might be sufficient.

698 **6.2 MassWastingRunout probability applications**

699 In this section we briefly demonstrate how to determine runout probability from a probabilistically determined
700 landslide hazard map or a specific, potentially unstable slope using MWR. The first application may be appropriate
701 for watershed- to regional-scale runout hazard assessments. The second application is an example hazard assessment
702 for a potentially unstable hillslope. Both applications are demonstrated at the Olympic Mountains site where landslide
703 size and type tended to be relatively uniform and parameter PDFs determined through calibration may therefore
704 represent typical runout processes in the basin.

705 **6.2.1 Runout probability from a landslide hazard map**

706 To determine runout probability from a landslide hazard map, we ran MWR Probability using Option 3, reading a
707 series of mapped landslide source areas created by an externally run Monte Carlo landslide initiation model. For the
708 landslide initiation model, we used LandslideProbability (Strauch et al., 2018), an existing component in Landlab that
709 computes landslide probability by iteratively calculating Factor-of-Safety (FS : ratio of the resisting to the driving
710 forces) at each node on the raster model grid Np times from randomly selected soil (regolith) hydrology properties
711 (e.g., soil depth, saturated hydraulic conductivity) soil strength (friction angle, cohesion) and recharge rates
712 (precipitation input rate minus evapotranspiration and soil storage). Landslide probability at a node is defined as the
713 number of times $FS < 1$ divided by Np .

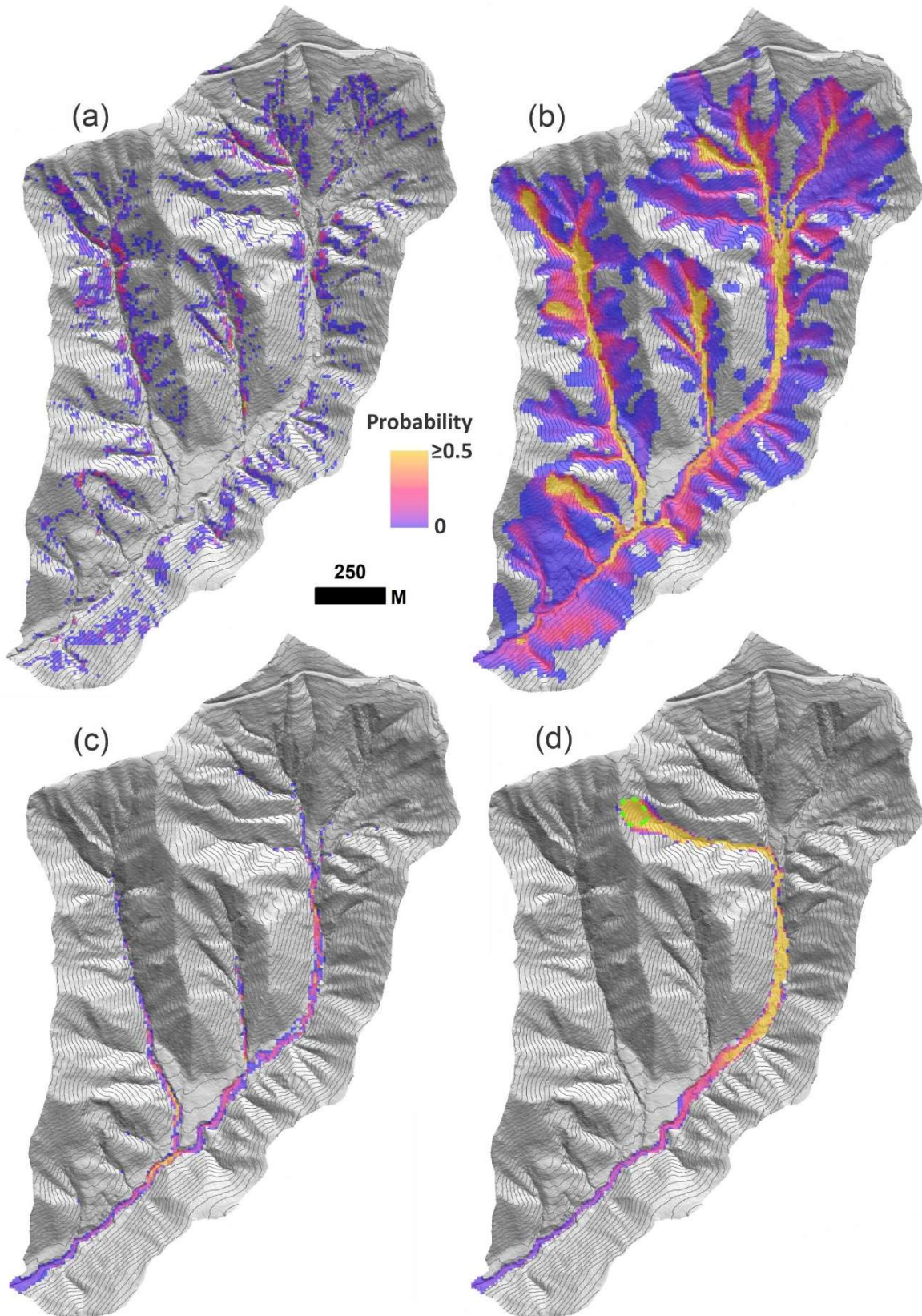
714 We first ran LandslideProbability using a 50-year precipitation event (WRCC, 2017) to determine landslide
715 probability (Figure 13a) over the entire Olympic Mountains model domain and create the series of Np FS maps.

716 Details on the LandslideProbability setup are included in the Supplementary Material. We then read the series of FS
717 maps into MWR Probability, treating all nodes with $FS < 1$ as a landslide source, and ran MWR Np times. Each
718 iteration, MWR read a new FS map and randomly selected a new set of parameter values from S_c - q_c parameter PDFs
719 created by the calibration utility.

720 Runout probability, which reflects MWR parameter uncertainty and uncertainty in the initial landslide size and
721 location caused by a 50-year precipitation event, is illustrated in Figure 13b and shows that the probability of runout
722 is high in many of the second order channels but low at the basin outlet. As discussed in Section 3, the probability of
723 aggradation or erosion caused by the runout can be determined by adjusting the numerator of Equation (30). As an
724 example, the probability of deposition greater than 1 meter is shown in Figure 13c.

725 **6.2.2 Runout probability for a specific, potentially unstable slope**

726 When field evidence or other data indicate that a specific hillslope may be potentially unstable, but the exact area of
727 a potential landslide on that slope is unknown, MWR can be used to generate a hazard estimate that takes into account
728 the uncertainty in the landslide area. For this application, MWR Probability is run using Option (2), which requires a
729 polygon representing the extent of the potentially unstable slope. We designated a 0.6 ha, convergent hillslope in the
730 headwaters of the Olympic Mountains site as a potentially unstable slope (Figure 13d). For each model repetition, a
731 landslide area can form anywhere within the potentially unstable slope and is at least as large as a user defined
732 minimum size but no larger than the potentially unstable slope. This example shows that, given uncertainty in the
733 landslide size and location, and uncertainty in MWR parameterization, if a landslide were to initiate on the potentially
734 unstable slope, the probability of the runout reaching the basin outlet is less than 5%.



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736
737

Figure 13. Olympic Mountains site: **(a)** Landslide probability, $P(FS \leq 1)$. **(b)** Corresponding runout probability, $P(\Delta\eta)$. **(c)** Probability of deposition greater than 1 m and **(d)** Runout probability for the potentially unstable slope (green-dashed polygon).

738 7.0 Concluding remarks

739 In this study, we described, calibrated and tested MassWastingRunout (MWR), a new cellular-automaton landslide
740 runout model that combines the functionality of simple runout algorithms used in WSMs (landscape evolution and
741 watershed sediment yield models) with the predictive detail typical of runout models used for landslide inundation
742 hazard mapping. MWR is suitable for hazard assessment and WSM applications. MWR is implemented in Python as
743 a component for the Landlab earth surface modelling toolkit and is designed for probabilistic landslide hazard
744 assessments, sediment transport and landscape evolution applications. MWR includes a Markov Chain Monte Carlo
745 calibration utility that determines the best-fit parameter values for a site as well as empirical Probability Density
746 Functions (PDF) of the parameter values. MWR also includes a utility called MWR Probability that takes the PDF
747 output from the calibration utility to determine runout probability.

748 Results indicate that despite its simple conceptualization, MWR shows skill in modeling the final runout extent,
749 sediment transport and topographic change associated with a landslide. MWR needs only the location and geometry
750 of an initial landslide source area to model the entire runout process. When compared to other models capable of
751 replicating observed landslide inundation patterns, the strength of MWR lies in its use of field-inferable parameters,
752 its ability to internally estimate the total mobilized volume (initial landslide body + erosion volume) and its relatively
753 parsimonious model design.

754 MWR can be calibrated to a site using just two parameters (critical slope, S_c , and a threshold flux for deposition, q_c)
755 and the MWR calibration utility enables the user to calibrate the model for a watershed within several hours on a
756 standard desktop (Section 5.3). Although the predictive power of MWR hinges on calibration—a common requirement
757 for mechanistic models—its reliance on two calibration parameters serves to constrain model uncertainty. Site-specific
758 calibration may be needed when MWR is used for sediment yield analysis, but if the aim is limited to mapping runout
759 extent, it may be possible to infer parameterization from nearby landslides or possibly from globally available repeated
760 DEMs and air photos that show where past mass-wasting flows have stopped (for S_c) and how thick their frontal lobes
761 are at the point of deposition (for q_c). Nonetheless, as a rules-based, cellular-automaton model, MWR is not designed
762 to accurately simulate flow depth. For accurate flow depths or debris flow impact forces, a detailed-mechanistic
763 modeling approach should be used.

764 MWR shows a rich set of intuitive responses to topographic curvature and slope (Section 4). When calibrated to the
765 runout of six different observed landslides, the volumetric error of MWR, $\Delta\eta_E$, ranged between 6% and 15% (median
766 9.1%) of the observed total mobilized volume. Except for the Rocky Mountains site where MWR consistently
767 modelled wider-than-observed flow, the cumulative flow error along the runout profile (Q_{sE}) were limited to 5%-19%
768 of the mean cumulative flow determined from the observed DEM-of-Difference (DoD). These are considered
769 acceptable levels of performance given that the total mobilized volume of many debris flow models assume an order
770 of magnitude range of confidence. A notable finding of this paper is that at most sites, MWR modeled runout did not
771 have any strong systematic bias in predictions (toward unrealistically short or wide flows, for example), which
772 suggests that MWR is structurally sound. However, MWR may underperform compared to mechanistic models when
773 flow momentum is the primary driver of runout extent. (e.g., in areas of slope-perpendicular flow).

774 In this study we showed how to couple MWR with LandslideProbability to map debris flow hazard when landslide
775 initiation location is uncertain. As a component of the Landlab earth surface modelling toolkit, MWR is designed to
776 be compatible with other models and thus relatively easy to integrate into a WSM. An example WSM that incorporates
777 MWR might include models for landslide initiation, hillslope diffusion and fluvial incision to investigate the role of
778 landslides and their runout on long-term landscape evolution. Future studies will explore large-scale application in
779 landscape evolution or sediment yield models, and characterize model parameters for different geologic and
780 hydroclimatic conditions. The use of a calibrated runout model in WSMs might allow for region-specific and more
781 insightful predictions of landslide impact on landscape morphology and watershed-scale sediment dynamics.

782

783 **Appendix A - Determination of k**

784 The average erosion depth caused by the observed runout (\bar{E}) can be determined from the DoD as the total erosion
785 volume ($\sum E\Delta x^2$) divided by the erosion area (A_e):

$$786 \quad \bar{E} = \frac{\sum E\Delta x^2}{A_e} \quad (\text{A1})$$

787 where $\sum E\Delta x^2$ and A_e exclude the initial landslide body volume and area, areas of deposition ($\Delta\eta > 0$) and areas
788 with no change in elevation ($\Delta\eta = 0$). In terms of the debris flow conceptualization used in MWR, \bar{E} can also be
789 written as a function of the mean number of times a debris flow would need to pass over a grid cell (\bar{n}) multiplied by an
790 average erosion depth per debris flow (\bar{h}_e) to equal \bar{E} as:

$$791 \quad \bar{E} = \bar{n}\bar{h}_e \quad (\text{A2})$$

792 An estimate for \bar{n} can be determined from the average length of the runout material divided by the cell width:

$$793 \quad \bar{n} = \frac{\ell}{\Delta x} \quad (\text{A3})$$

794 At most sites, we approximate the average length of the runout material simply as the mapped landslide length (ℓ).
795 As the debris flows move down slopes in excess of S_c , they entrain material, split, and spread, and the runout material
796 tends to lengthen. Using the initial landslide length to represent the runout length thus represents a minimum value
797 for \bar{n} and if needed, the numerator of (A3) can be multiplied by a coefficient to better match runout length.

798 Combining (A2) and (A3), \bar{h}_e can be defined as the average erosion rate per unit length of runout debris (\bar{E}/ℓ) times
799 the cell width:

$$800 \quad \bar{h}_e = \frac{\bar{E}\Delta x}{\ell} \quad (\text{A4})$$

801 Rewriting equation (11) as a function of the average shear stress in the erosion-dominated reaches of the runout path
802 ($\bar{\tau}$) and assuming $\tau_c \cong 0$, debris flow erodibility parameter k can be estimated as:

$$803 \quad k = \frac{\bar{h}_e}{\bar{\tau}f} \quad (\text{A5})$$

804 To solve for k , we estimated $\bar{\tau}$ from field-approximated debris flow depth and channel slope measurements in the
805 erosion-dominated reaches of the runout path (Table 1). We used (13) to define $\bar{\tau}$. For D_s , we used the average
806 maximum grain size observed over the whole runout path. If τ is defined as a function of grain-collision dependent
807 shear stress approach (13) and k is determined as a function of f , as in (A5), the impact of f on model behavior is
808 relatively small.

809 Notation

810	q_{R_i}	[m]	debris flux from a node to each of the node i -th receiver nodes
811	i		variable used to represent count or index in Equations 1, 5 and 28
812	q_O	[m]	the total out-going debris flux
813	Nr		the number of receiving nodes of node n
814	S_i		the underlying topographic slope ($\tan \theta$) to each of the node i -th receiver nodes
815	a		exponent in (1) that controls how flow is distributed to downslope nodes
816	q_I	[m]	The total incoming flux
817	Nd		number of donors nodes to a node
818	q_{D_j}	[m]	the flux from node D_j (the j -th donor node)
819	j		variable used to represent count or index in Equations 2 and 29
820	h	[m]	flow depth at node, adjusted to be no more than h_{max}
821	h_{max}	[m]	the maximum observed flow depth
822	A	[m]	aggradation depth
823	S_c		critical slope
824	S		steepest slope to the node's eight neighbouring nodes
825	Δx	[m]	cell length
826	$A_{p N_a}$	[m]	potential aggradation depth that forms a deposit that spreads over N_a consecutive
827	$A_{p,i}$	[m]	i -th deposition amount in the deposit illustrated in Figure 4
828	N_a		number of nodes $q_{S_n^i}$ is assumed to spreads over
829	E	[m]	erosion depth
830	h_r	[m]	regolith depth
831	h_e	[m]	potential erosion depth
832	θ	[°]	topographic slope used to determine shear stress, equal to $\tan^{-1}(S)$
833	τ	[Pa]	basal shear stress
834	τ_c	[Pa]	critical shear stress of the regolith
835	k		erodibility parameter in (11)
836	f		exponent, controls the non-linearity of h_e in (11)
837	ρ	[kg/m ³]	density of runout material
838	σ	[Pa]	normal stress at basal surface
839	φ		tangent of collision angle between grains, measured from the vertical axis
840	v_s		volumetric solids concentration
841	ρ_s	[kg/m ³]	density of solids
842	D_s	[m]	characteristic particle diameter
843	u	[m/s]	depth average flow velocity
844	z	[m]	depth below the flow surface
845	u^*		shear velocity
846	g	[m/s ²]	acceleration due to gravity
847	$\Delta\eta$	[m]	change in elevation at node
848	\mathbf{q}_D		a vector containing all q_{D_j} sent to the node
849	ξ_D		a vector containing the incoming attribute values for each q_{D_j}
850	ξ_D		attribute value delivered to the node
851	ξ_R		attribute value sent to receiver nodes

852	ξ		attribute value at node
853	η	[m]	topographic elevation
854	Λ		parameter set
855	$L(\Lambda)$		likelihood of parameter set
856	$p(\Lambda)$		prior probability of parameter set
857	Ω_T		the Lee-Salle index for evaluating model planimetric fit
858	α	[m ²]	modelled area of matching extent (compared to observed runout extent)
859	β	[m ²]	modelled area of overestimated extent
860	γ	[m ²]	modelled area of underestimated extent
861	$\Delta\eta_E$		volumetric error of the modelled topographic change relative to the observed total
862			mobilized volume, fraction.
863	V	[m ³]	observed total mobilized volume
864	p		the number of nodes in the modelled runout extent
865	$\Delta\eta_{Mi}$	[m]	the modelled topographic change [m] at the i -th node within the runout extent
866	$\Delta\eta_{Oi}$	[m]	the observed topographic change [m] at the i -th node within the runout extent
867			
868	Q_{sE}		mean-modelled-cumulative flow error along the runout path relative to the observed
869			mean cumulative flow, fraction.
870	$\Delta\eta_{ij}$	[m]	topographic change [m] at the i -th node located upstream of node j
871	u_j		total number of all nodes located upstream of node j
872	r		the number of nodes along the center line of the runout path
873	Q_s	[m ³]	the cumulative debris flow volume at each node, j along the center line of the runout path
874	Q_{sO}	[m ³]	the observed cumulative debris flow volume (Q_s) at each node, j
875	Q_{sM}	[m ³]	the modeled cumulative debris flow volume (Q_s) at each node, j
876	$\Delta\eta_{ij}$	[m]	the topographic change [m] at the i -th node located upstream of node j
877	u_j		the total number of all nodes located upstream of j
878	$\overline{Q_{sO}}$	[m ³]	the observed mean cumulative flow
879	$P(\Delta\eta)$		
880	E/ℓ	[m/m]	average erosion per unit length of runout debris
881	$P(\Delta\eta)$		probability of runout, expressed as the probability that the elevation of a node changes
882	$num()$		number of
883	Np		number Monte Carlo iterations used to determine probability
884	A_e	[m ²]	erosion area of the observed or modeled runout
885	\bar{E}	[m]	average erosion depth caused by the runout
886	$\sum E\Delta x^2$	[m ³]	the total erosion volume
887	\bar{n}		mean number of times a debriton would need to pass over a grid cell multiplied by an
888			average erosion depth per debriton to equal \bar{E}
889	\bar{h}_e	[m]	average erosion depth per debriton
890	ℓ	[m]	length of runout debris, approximated as the length of the initial landslide body
891	H/L		the total topographic relief of the runout (measured from the center of the landslide to the
892			end of the runout path) divided by the horizontal length of the runout
893	κ	[1/m]	mean total curvature
894	SPI		mean specific stream power index
895	FS		Factor-of-Safety, ratio of the resisting to the driving forces acting on a hillslope
896			

897 **Code availability**

898 MassWastingRunout and several tutorial notebooks area available at: <https://github.com/landlab/landlab>

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910 **Competing interests**

911 The contact author has declared that none of the authors has any competing interests.

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