

Coevolving edge rounding and shape of glacial erratics; the case of Shap granite, UK

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Abstract

The size distributions and the shapes of detrital rock clasts can shed light on the environmental history of the clast assemblages and the processes responsible for clast comminution. For example, mechanical fracture due to the stresses imposed on a basal rock surface by a body of flowing glacial ice releases initial 'parent' shapes of large blocks of rock from outcrop, which then are modified by the mechanics of abrasion and fracture during subglacial transport. The latter processes produce subsequent generations of shapes, possibly distinct in form from the parent blocks. Lacking is a complete understanding of both the processes responsible for block shape changes and the trends in shape adjustment with time and distance away from the source outcrop. Field data on edge rounding and shape changes of Shap granite blocks (dispersed by Devensian ice eastwards from outcrop) are used herein to explore the systematic changes in block form with distance from the outcrop.

The degree of edge rounding for individual blocks increases in a punctuated fashion with the distance from the outcrop as blocks fracture repeatedly to introduce new fresh unrounded edges. In contrast, block shape is conservative, with parent blocks fracturing to produce self-similar 'child' shapes with distance. Measured block shapes evolve in accord with two well-known models for block fracture mechanics — 1) stochastic and 2) silver ratio models — towards one or other of these two attractor states. Progressive reduction in block size, in accord with fracture mechanics, reflects the fact that most blocks were transported at the sole of the ice mass and were subject to the compressive and tensile forces of the ice acting on the stoss surfaces of blocks lying against a bedrock or till surface. The interpretations might apply to a range of homogeneous hard rock lithologies.

Short Summary

Edge rounding in Shap granite glacial transported boulders is an irregular function of distance from the source outcrop in northern England, UK. Block shape is conservative, evolving according to block fracture mechanics — stochastic and silver ratio models — towards either of two attractor states. Progressive reduction in size occurs to blocks transported at the sole of the ice mass where the blocks are subject to the compressive and tensile forces of the ice acting against a bedrock or till surface.

Key words

Glacial erratics, erratic rounding, erratic shape, fracture, subglacial

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1 Introduction

50 The concentration, size, shape, and the degree of rounding of glacial ice-transported blocks of rock
51 may change with distance from the source outcrop. Spatial trends in concentration have been used
52 frequently to indicate preferred ice flow directions (Kujansuu & Saarnisto, 1990; Evans, 2007, Benn &
53 Evans, 2011, p. 675). Concentrated bands of ice-freighted erratics are referred to as ‘indicator plumes’,
54 ‘indicator trains’ or ‘indicator fans’, with concentrations dropping off rapidly outside of the plumes
55 due to ice-flow induced dispersion (Larson & Mooers, 2004). None-the-less, concentration is also
56 sustained by comminution, whereby blocks fracture, or abrade to form smaller blocks and fragments
57 through time and distance from the source outcrop. In contrast to dispersion, there has been less
58 focus on changes in size, shape, and edge-rounding with distance from source (Benn & Evans, 2011).
59 The changes in the shape of blocks are functions of the mechanical properties of the blocks, primarily
60 rock strength and structure, as well as the physical processes promoting comminution. A change in
61 block shape also represents a change in block size. To explore the controls on edge rounding and the
62 shape of erratics, dispersal from a well-known exposure of the Shap granite (Sg) in the UK was
63 examined in the present study. Improved understanding of process controls related to edge rounding
64 and fracture should shed light on the associated basal ice dynamics related to block form changes
65 generally. The two key issues are: 1) the relative importance of fracture mechanics in reducing block
66 size in contrast to edge-rounding and 2) whether edge-rounding and shape coevolve with distance
67 from the source outcrop.

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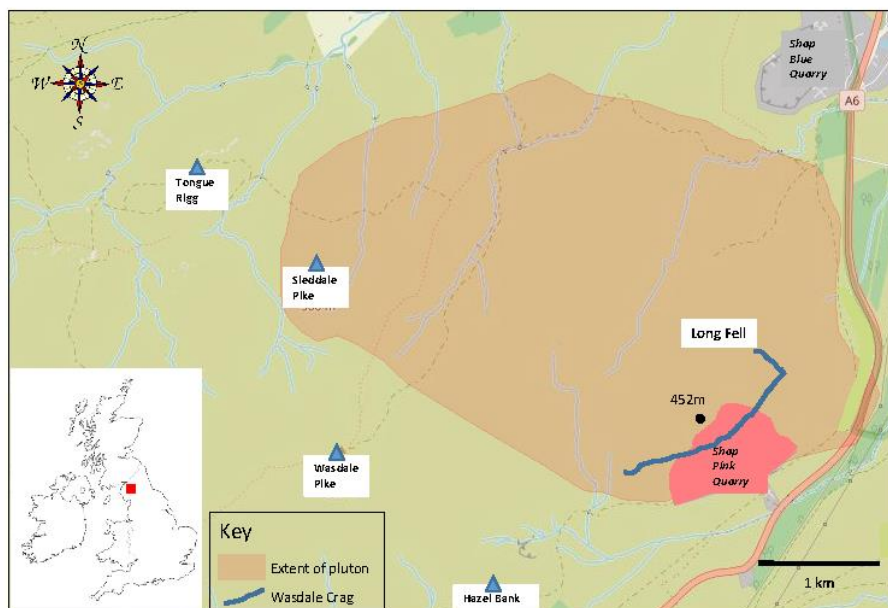
1.1 The Study Area and Context of the Study

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71 The exposure of the Sg pluton occupies a small area (c., 7 km²) in the eastern English Lake District (Fig.
72 1) defining a distinct, small, source area for granite blocks. The variation in the concentrations of Sg
73 blocks with distance from the pluton has been used as a key indicator of the directions of ice

74 movement across northern England (reviewed by Carling *et al.*, 2013) during the Dimlington Stadial
75 (c., 30 ka BP to 14.7 ka BP) within the overall period of the Devensian glaciation (c., 33 ka BP to 11.7
76 ka BP). Around the Late Glacial Maximum (LGM: 26.5 ka BP to 19 ka BP, Clark *et al.*, 2009), the region
77 was covered by ice, several hundred metres thick (Evans *et al.*, 2009), and Sg blocks were entrained
78 from the subglacial bedrock (Ugelvig *et al.*, 2016). Long Fell, on the eastern margin of the exposed
79 pluton, is a kilometre-scale *rôche moutonnée*, severely ice-plucked in the east and south-east at
80 Wasdale Crag (Fig. 1), with smooth, ice-planed surfaces occurring to the north, west and on the
81 summit (point 452m), indicating the erosional effects of moving ice and debris (Hallet, 1981). The
82 west to east change in the style of erosion, from smoothing to plucking, is consistent with ice in the
83 vicinity of the pluton moving predominately to the east in an early phase (c., 29-25 ka BP; Livingstone
84 *et al.*, 2012; Merritt *et al.*, 2019) of the Dimlington Stadial, and generally northwards across the pluton
85 subsequent to 22 ka BP, *i.e.* towards the end of the LGM (Livingstone *et al.*, 2012; Merritt *et al.*, 2019);
86 the latter supposition consistent with the W.S.W. to E.N.E. orientation of glacial striations on the
87 pluton (Nicholson, 1868).

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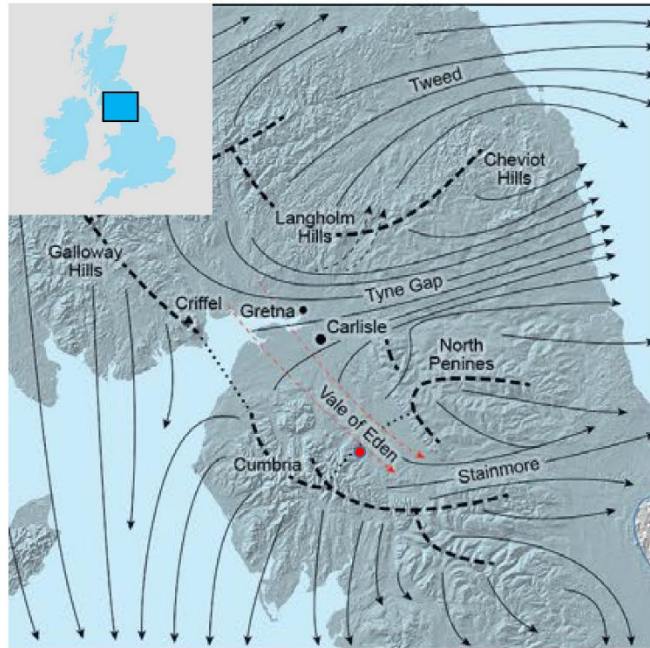
90 *Figure 1: Location of the Shap granite pluton. The central portion of the ice-plucked outcrop (Wasdale*
91 *Crag) crag has been destroyed by quarrying. Base map is from CC BY © OS Map Local data.*

92 [Approximate extent of the Shap Granite pluton outcrop from the British Geological Survey](https://www.bgs.ac.uk/map-viewers/geoindex-onshore/)
93 [\(https://www.bgs.ac.uk/map-viewers/geoindex-onshore/\)](https://www.bgs.ac.uk/map-viewers/geoindex-onshore/).
94

95 In terms of concentration, the dominant dispersal of Sg erratics, during the early phase of the
96 Dimlington Stadial (Stage I; 29-25 ka BP; Merritt *et al.*, 2019) was eastward (Carling *et al.*, 2013) within
97 sustained ice flow through the topographically controlled corridor of the Stainmore gap across the
98 north Pennines hills (Fig. 2A). The plume extended as far as the east coast of England; a distance more
99 than 100km (Fig. 3). Block size tends to diminish with distance, although examples of far-travelled
100 large blocks occur sparingly (Carling *et al.*, 2023). Due to shifting ice divides and competing ice
101 dispersal centres (Merritt *et al.*, 2019), subsequently two Sg plumes dispersed in southerly directions
102 until, in the late stadial, erratics briefly were dispersed northwards from the vicinity of the pluton
103 (Carling *et al.*, 2013) in accord with the ice movements reported by Livingstone *et al.* (2012). These
104 latter dispersal directions are not considered further herein. The focus solely is on those erratics the
105 final transport vectors ([direction and distance](#)) of which are [roughly](#) due east, defining a simple linear
106 direction over which changes in the nature of the erratic populations might be measured.

107
108 Less well understood than directions of travel and changes in concentration, is the process of edge-
109 rounding and shape changes of Sg blocks that accompany size reduction. The granite is an ideal choice
110 for study as the composition and texture is uniform (Grantham, 1928), mostly giving a massive,
111 unlayered, structure to individual blocks. Layering, such as found within sedimentary rocks, would
112 add complexity to the study of shape evolution, which ~~complexity~~ is avoided in this study. Hopkins
113 (1849) had commented briefly on the rounding of Sg blocks (density ~ 2.61 tonnes m^{-3}) as size reduces
114 towards the east coast, yet such rapid changes in form are seemingly at odds with the high strength
115 of the rock. The strength of Sg in compression exceeds 207 MPa (Holland, 1959;

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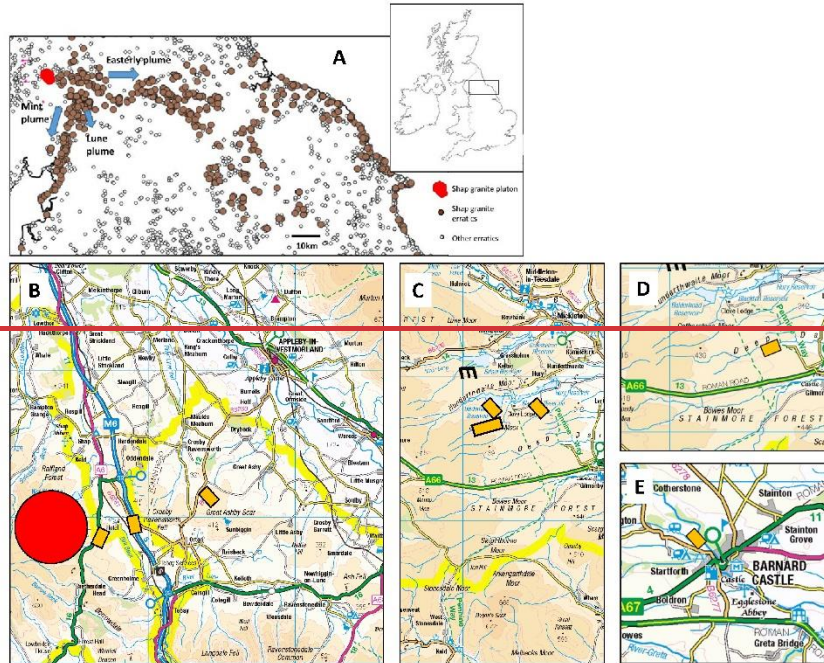


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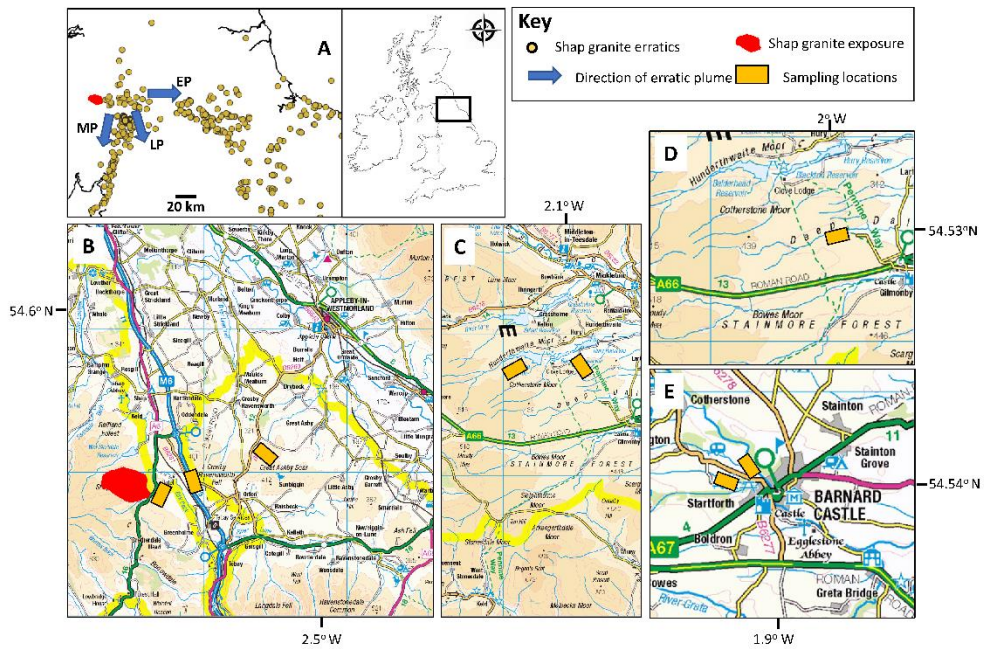
Figure 2: Reconstructed of Stage I (29-25 ka BP) of the last British-Irish Ice Sheet around the Solway Firth (from Merritt et al., 2019. Reproduced with permission) in northern England Stage (inset panel). Eastward ice flow through prominent topographic corridors occurs across the north Pennines. Broken and dotted lines refer to ice divides. Arrows indicate ice-flow vectors (dotted arrows indicate alternative ice-flow scenarios). Topography from NEXTMap digital elevation data. Shap granite erratic plume dispersed to the east from the pluton (red dot) chiefly over Stainmore (see Fig 3).

127 Day & Goudie, 1977; Goudie, 2006) such that the rock is considered ‘very strong’ (British Standards,
128 1981). Despite the rock strength, Hodgson (1870) had remarked on how seemingly rapid rounding of
129 granite might be aided by rock friability due to a high mica content associated primarily with biotite
130 (Firman, 1953). Biotite is soft compared with the large phenocrysts of feldspars and quartz (Firman,
131 1953) that dominate the granite composition. Nevertheless, there has been no investigation of the
132 changes in shape and rounding of Sg blocks with distance from the source; with very few granite blocks
133 visually maintaining significant mass over 10’s of km. A study of blocks exposed on the modern land
134 surface, away from major watercourses, should reveal rock-wear processes associated with glacial
135 transport as there has been negligible losses to Sg surfaces due to post-glacial subaerial weathering
136 (Wager, 1944; Parsons & Lee, 2005). The few weathered examples of blocks exhibit phenocrysts
137 standing proud (3-5mm) of the matrix, as the mica is readily subject to chemical weathering if buried

138 but the feldspars are not much altered (Wager, 1944). –Consequently, an hypothesis was proposed:
 139 ‘Sg ice-transported blocks would display systematic changes in edge-rounding and shape’; with an aim
 140 ‘to demonstrate if edge rounding and shape coevolve with distance to the east from the pluton’.



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143 *Figure 3: A) Spatial distribution of examples of Shap granite erratics within the study area,*
144 *northern England (inset), showing the early easterly-directed plume (EP) and, the later southerly*
145 *Mint and Lune plumes (MP & LP) and subsequent movement of some erratics northwards*
146 *relative to the source outcrop of Shap granite just east of the pluton. Sampling locations shown*
147 *Location of sampling sites (yellow rectangles) are indicative of the general sampling areas. B)*
148 *Wasdale Bridge, Haybanks, Blasterfield C) upper Teesdale; D) Levy Pool; E) Barnard Castle. See*
149 *main text for details. Base maps based on CC BY © OS 1:250 000 Scale Colour Raster™.*

150 Shape (and size) changes in a Shap granite block occur due to three predominant processes which
151 scale from effecting small areas of a block to larger areas:

152

153 1) abrasion, whereby grain-size fragments (e.g., phenocrysts) are ground-off the block surface
154 (Haldorsen, 1981; Benn & Evans, 2011) primarily by shear stresses associated with blocks
155 moving across a bedrock or till surface in the direction of basal ice motion, or by ice and till
156 moving over stationary blocks lodged against the substratum - this process can result in
157 distinct rounded surfaces on a block (Boulton, 1978; Hallet, 1979);

158

159 2) spallation, whereby flakes of rock are freed from the surface of the block (Olsen, 1983) due
160 to externally-derived and internally-derived tensile deviatoric stresses in the rock, both
161 imposed by the motion of the ice overburden, with the shear stresses acting on planes at less
162 than the block scale (Li *et al.*, 2018) – this process reduces block mass but results in localized
163 scarred surfaces;

164

165 3) fracture (Buscarnera & Einav, 2021) whereby the ‘parent’ block splits into substantial parts
166 (often two; here referred to as ‘child’ products). The propagating fissure ultimately may be
167 due to compression loading but, at the block surface, it is the result of a tensile stress (acting
168 on a plane at block scale) flexing the stoss surface of a brittle block lying on a hard basal surface,
169 leading to fissure development often transverse to the direction of basal ice motion (Morland
170 & Boulton, 1975; Hallet, 1996; Benn & Evans, 2011, p264). The tensile strength of a rock is

171 typically an order of magnitude less than the compressive strength (Li *et al.*, 2018). This
172 tripartite classification informed the Method.

173

174 To address the hypothesis, the focus of the study is abrasion and fracture, but observations on
175 spallation were obtained for completeness, with the latter results reported within Supplementary
176 Information. There is justification from studies of bedrock outcrop erosion by basal ice that both the
177 degree of abrasion of bedrock surfaces and the number of fracture events are related to time in
178 transport (Cohen *et al.*, 2006) and thus the distance erratics are moved.

179

180 **2 Method**

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182 Shap granite blocks were sampled along a west to east transect, starting from below Wasdale Crag. It
183 was assumed that all the sampled blocks were from the same population subject to basal traction
184 transport (*vis.* Boulton, 1978) for much of the transport histories; the population being a coarser
185 component of a ~~ledgement~~ subglacial traction till ~~till~~ (*sensu* Evans *et al.*, 2006) deposited during the
186 waning phase of the easterly phase of ice motion (Fig. 3A) (Hallet, 1979). Blocks ($L > c.$, 1.0 m) were
187 located by field walking. Locations sampled include Wasdale Old Bridge, Haybanks, Blasterfield, sites
188 near Barnard Castle in Teesdale and Levy Pool near Brough (Table S1), respectively 0.8 km, 3.5 km, 8.4
189 km, *c.*, 36 km and *c.*, 41 km from the Wasdale Crag outcrop (Fig. 3). The sites selected were known to
190 have sufficient erratics within defined areas for sampling. However, tTo obtain similar sample sizes,
191 the areas searched for the final two locations necessarily increased as the surface density of blocks
192 decreased eastwards. Examples of erratics were selected that were sitting on exposed bedrock or till
193 surfaces, so as not to be partially buried. Distance from the source outcrop is assumed to relate to
194 time in transport.

195 At each location, edge, and shape measurements and scar enumeration were made on thirty blocks
196 as briefly described below; the full procedure developed within Supplementary Information. The

197 sample size was found to be sufficient (Daniel, 1999; Conroy, 2018) for the aims of the project and,
198 moreover, interpretation of data trends became possible once the sample size $n > 30$ at each location.

199 These data were supplemented by a regional shape data compendium (Carling *et al.*, 2013). Changes
200 in block size with distance from the pluton are not considered herein using field data, as a statistically
201 significant sample size at each location would have to be prohibitively large to reflect the complete
202 size range of blocks. Rather block size changes are considered within a theoretical framework related
203 to shape changes. Blocks are considered as cuboids consisting of *faces* and *edges*.

204
205 In accord with 1) abrasion: edge rounding was measured after Wentworth (1923; Kirkbride, 1985). In
206 brief, each of the three most tightly rounded edges on the visible portion of each block was defined
207 by a chord (l), delimiting a segment of the block beneath each rounded edge, to give between 80 and
208 90 values for each location. Consideration of the height (h) of the segment in relation to the chord
209 length constrains the radius (r_c) of an inscribed circle beneath the rounded edge, which radius is a
210 measure of the degree of rounding:

211

$$212 \quad r_c = \frac{l^2}{8h} + \frac{h}{2} \quad (1)$$

213

214 The radius of curvature reduces as the chord length reduces towards zero and often a right-angle
215 corner occurs when r_c approaches 0. More rounded blocks have larger radii of curvature than less
216 rounded blocks as the sizes of the inscribed circles increase as edges become less sharp. In similar
217 fashion, the edge rounding was measured for joints bounding *in situ* Shap granite blocks constituting
218 the outcrop of Wasdale Crag. These latter data provide a base line of the degree of edge rounding of
219 blocks which have been subject to ice abrasion in place, but without subsequent transport.

220

221 To consider 3) shape changes by fracture: from initial field reconnaissance, blocks close to the source
222 often appear cubic, but polyhedrons occur sparingly - ranging from wedges to prisms. Further

223 from the source more ellipsoidal forms are evident. Consequently, to obtain an indication of the shape
224 of a cuboid or an ellipsoid block, the lengths of the three orthogonal axes: long axis (L); medium axis
225 (M) and the short axis (S) were recorded in the field – polyhedrons were not sampled – to give c., 30
226 values for each location. Consideration of the mechanics of shape changes also sheds light on the size
227 reduction process with distance. Fracture within individual blocks is sometimes associated with joints
228 and other block-scale planes of weakness. Yet, ice compressive force is the predominant mechanism
229 for significant progressive change in shape for homogeneous granite blocks, inducing tensile fracture
230 and block size reduction. Shape and size changes were examined either via a stochastic fracture model,
231 applicable to fracture at right-angles to either of the L , M or S axes (Domokos *et al.*, 2015) of ellipsoidal
232 blocks or, in accord with the silver ratio model applicable to cuboid blocks fracturing across the M -axis
233 alone (Buscarnera & Einav, 2021), as is explained in the Results.

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235 **3 Results**

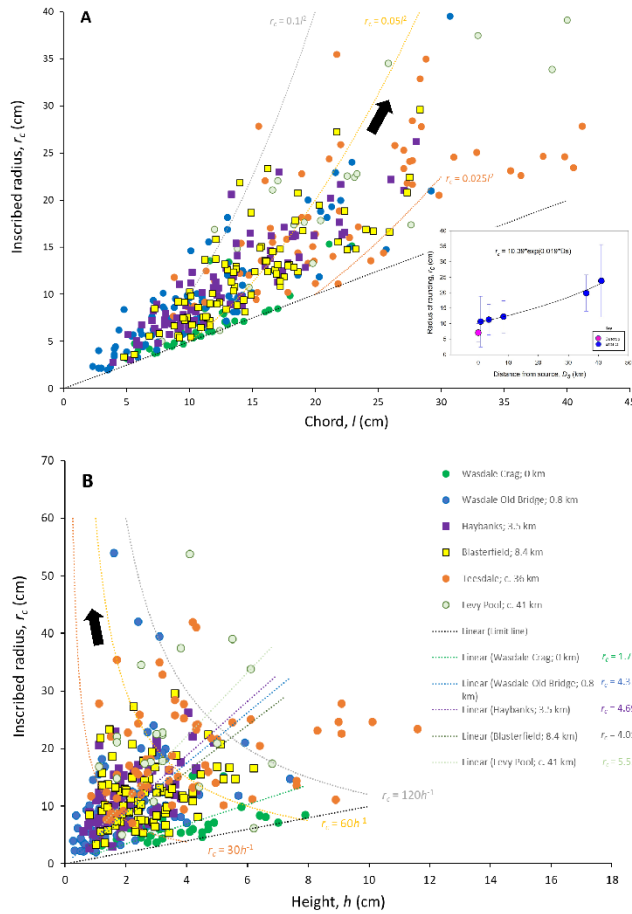
236 **3.1 Edge rounding**

237 As is evident from the form of equation 1, rounding is a positive function of the square of the length
238 of the chord of the segment, l , and an inverse function of the segment height, h (Fig. 4). As the
239 inscribed radius values are obtained from both the values of l and h (Equation 1), there is an element
240 of co-variance between the two axes in both panels A and B of Fig. 4. However, plotting the data in
241 this manner allows ready visualization of the trends of the radius data (r_c) relative to the variation in
242 the controlling parameters (l, h). Lower limits to data plotting positions occur in both panels equal to:
243 $r_c = l/2$ and $r_c = h$ respectively.

244 The joint rounding on the pluton is less developed in comparison with the rounding of edges of blocks
245 only 0.8km away at Wasdale Old Bridge (Fig. 4). Although the range in heights of the segments are
246 similar for both locations, the range in chord lengths for the pluton includes smaller values giving
247 overall ‘sharper’ average edge profiles for the pluton joints in contrast to the Wasdale Old Bridge

248 blocks. It is evident that any 'parent' blocks newly entrained from the outcrop will exhibit both lightly
249 rounded joint edges (glacially abraded when *in situ*) as well as sharp, fresh edges, the latter due to
250 fracture upon release from the outcrop. However, although the initial lightly rounded edges can be
251 further rounded with distance, fracture of entrained blocks introduces new 'sharp' edges as detailed
252 next.

253 Although as distance increases larger radii are more frequent, small radii also occur at distance (Fig.
254 4). It is unlikely that small radii can survive abrasive transport over several 10's of km from the pluton,
255 rather repeated fracture introduces new sharp edges and thus new small radii to different generations
256 of blocks. These new sharp edges begin to round far from the pluton. Although the plots of Fig. 4 are
257 developed considering singular data points from many blocks, if the trends are considered to
258 represent the rounding evolution that would occur for individual blocks, then the black arrows indicate
259 the general direction of edge rounding evolution (*i.e.*, Fig. 4 panel A: if h is constant and l is variable;
260 panel B: if l is constant and h is variable). The linear functions in Fig. 4B allow ready comparison
261 between locations such that, for any value of h , the degree of edge rounding is more pronounced with
262 distance from the pluton; specifically, the linear curves (green, blue, purple, and red) have increasing
263 values of the constant (*i.e.*, 1.71, 4.37, 4.69; 5.53 respectively). Similar linear functions for values of l
264 can be applied to Fig. 4A but, for the sake of clarity, these curves are not plotted. The detail of edge



265

266 *Figure 4: Trends in the values of the inscribed radius as a function of: A) chord length, and; B) segment*
 267 *height. Black arrows indicate the direction of travel of the hypothetical function for an individual block*
 268 *(see main text). Examples of hypothetical curves (brown, yellow and grey) for the trends in individual*
 269 *clast evolution are given for both $r_c \propto l^2$ and $r_c \propto h^{-1}$. Key in panel B also applies to panel A. Inset*
 270 *panel shows mean and s.d. of edge rounding as function of distance from outcrop.*

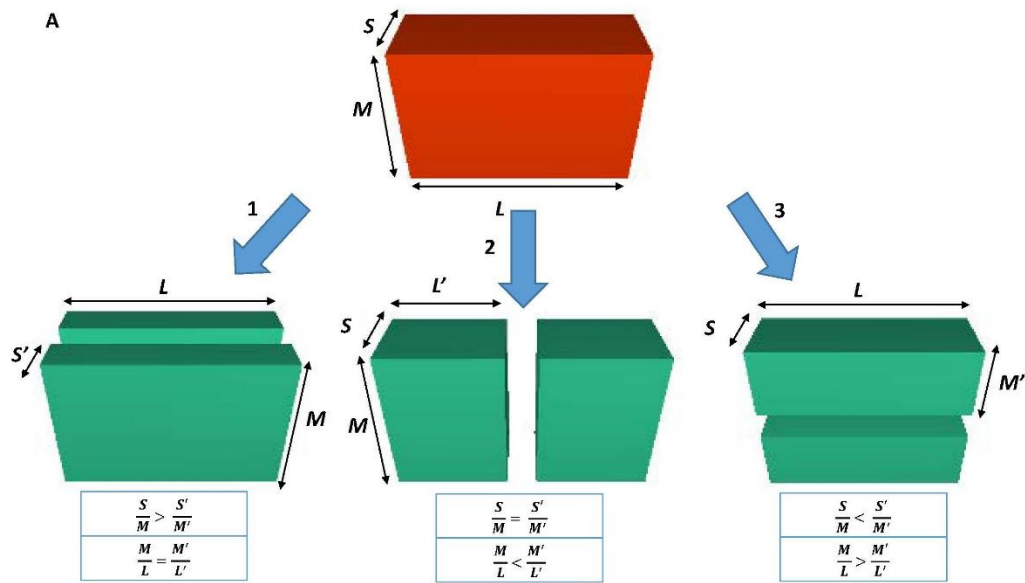
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272 rounding is considered within the Discussion, as edge-rounding of individual blocks is not a smooth
 273 function of distance from the source as might be inferred from the black arrows in Fig. 4 and from the
 274 inset figure of mean edge rounding with distance from the outcrop (Fig. 4 inset panel). The latter
 275 figure depicts an exponential increase in the mean radius of curvature with distance (D_s) from the
 276 source outcrop:

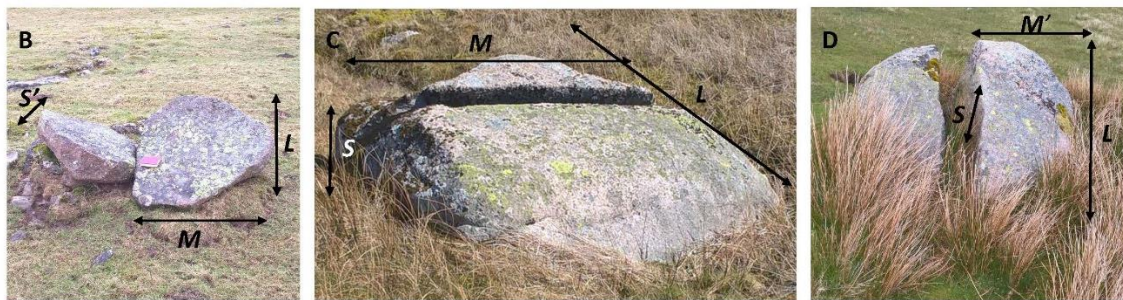
$$277 \quad r_c = 10.3881e^{(0.0194D_s)} \quad (2)$$

278 **3.2 Shape evolution**

279 In the context of natural hexahedrons, the *stochastic model* of progressive fracture due to the stress
280 of compression (Domokos *et al.*, 2015), describes the generation of ellipsoids with the orthogonal axes
281 length proportions: 2.32; 1.52: 1 (Fig. 5A), whereas the *silver ratio* progressive fracture model
282 (Buscarnera & Einav, 2021) describes the generation of cuboids with the edge length proportions: $\sqrt[3]{2^2}$;
283 $\sqrt[3]{2}$; 1, *i.e.*; 1.59: 1.26: 1 (Fig. 6A). In the former model, a fracture plane is orthogonal to any of the
284 three sides of a cuboid (enclosing the ellipsoid) and separates two pieces of equal mass. In the silver
285 ratio model, a fracture plane occurs orthogonal to the current longest axis, separating two pieces of
286 equal mass. In nature, deviation from these two models can occur such that shape self-similarity, in
287 terms of axial ratios, is not maintained necessarily upon successive fracture events if the subsequent
288 fracture is across an axis that differs from the previous fracture event. Fracture across the plane of
289 the short axis was observed in nature (Fig. 5B). However, systematic fracture across the plane of the
290 long axis (Fig. 5C) and across the medium axis (Fig. 5D; Fig. 6B) appeared predominant (*vis* Benn, 1992)
291 for the blocks observed in the field, in accord with both the stochastic and silver models. Given that
292 most blocks rest with the short axis vertical, fracture across the *L* or *M* axes is consistent with known
293 fracture mechanics, whereby the centre of an object is the location, under loading, of the maximum
294 in the tensile stress and the consequent nucleation point for fracture (Hiramatsu & Oka, 1966; Shipway
295 & Hutchings, 1993). From this point, a fracture line develops to the block edges (Man *et al.*, 2018)
296 transverse to the direction of tensile loading. For low values of static or dynamic loading, the rock
297 eventually ruptures into two parts (Man *et al.*, 2018). Thus, although a block on occasion might
298 fracture across an axis at variance with the two models above, there is a tendency for blocks to evolve
299 towards one or the other model. The system state attractors for these two models are shown in Fig.
300 7, wherein natural block shapes are considered. Importantly, compression and tensile fracture leads
301 in both models initially to uniquely defined anisotropic forms, although isotropic forms ($L = M = S$) can
302 occur in principle with progressive fracture if the fracture rule in each model is relaxed and varied.



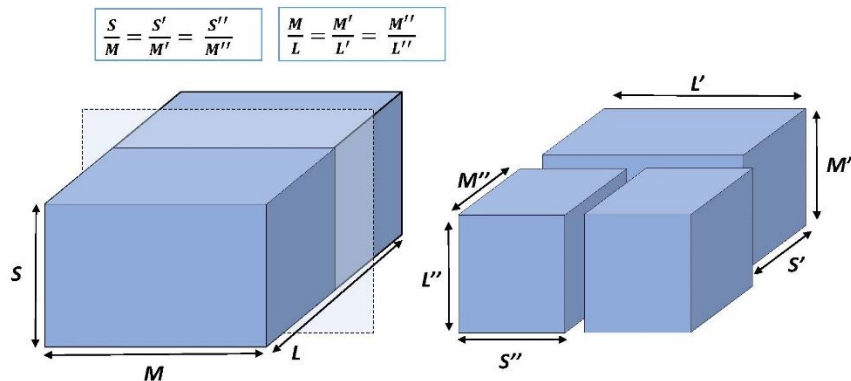
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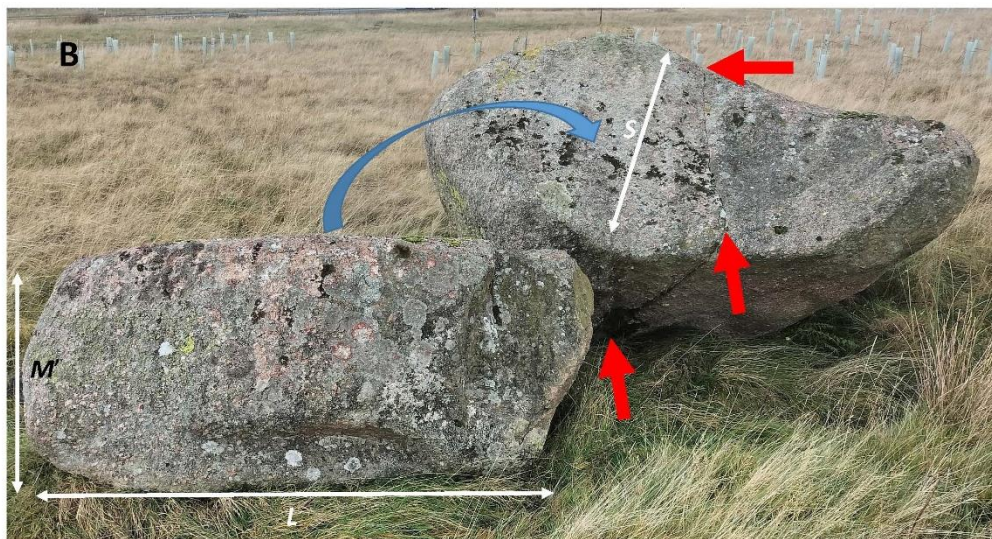
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305 *Figure 5: A) Schematic representation of the concept of the stochastic fracture model applied to a*
 306 *three-dimensional cuboid (enclosing an ellipsoid – see Fig. S1) subject to successive fracture given an*
 307 *assumed identical stress loading to the granite block at each fracture event. Fracture planes are*
 308 *orthogonal to a side and separate two pieces of equal mass. Shape self-similarity is not maintained*
 309 *upon successive fracture events. Three different fracture styles are possible within the model, as*
 310 *labelled 1, 2 and 3; B) Example of a well-rounded block split along a fracture plane consistent with*
 311 *model 1; C) Example of a well-rounded block split along a fracture plane consistent with model 2; D)*
 312 *Example of a well-rounded block split along a fracture plane consistent with model 3. The long axes*
 313 *are foreshortened in panels B, C and D.*

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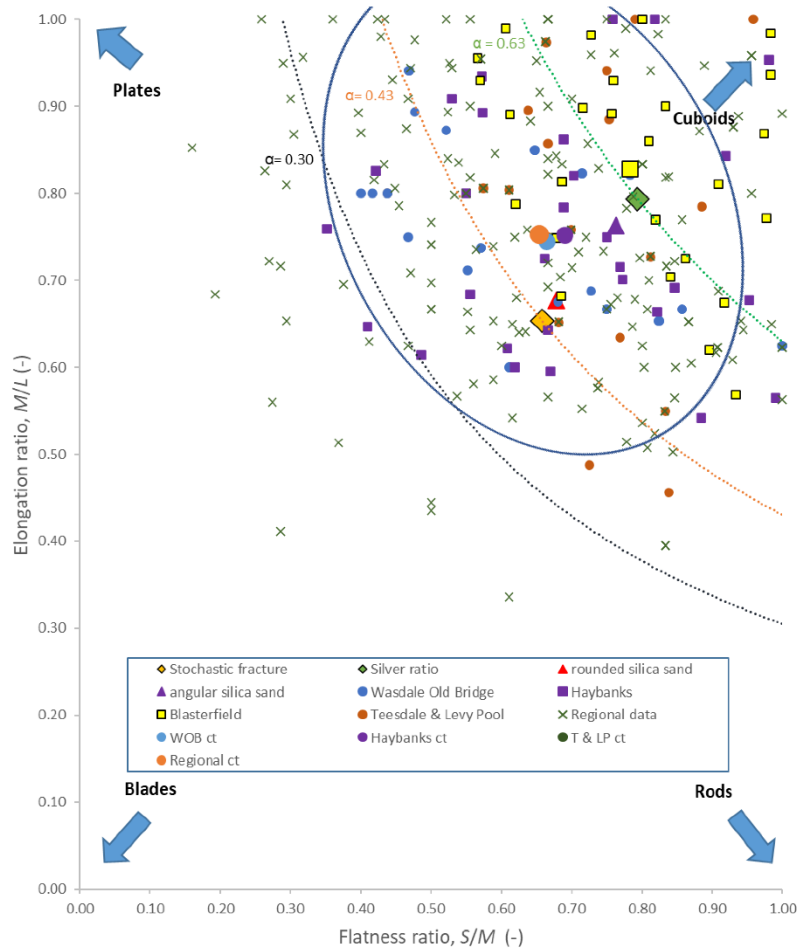


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316 *Figure 6: A) Schematic representation of the concept of the silver ratio model applied to a three-*
 317 *dimensional cuboid (– see Fig. S1) subject to successive fracture given an assumed identical direction*
 318 *of stress loading to the granite block at each fracture event. Fracture planes are orthogonal to the*
 319 *current long axis. Shape self-similarity is more closely maintained (in contrast to Fig. 5) upon successive*
 320 *fracture events; B) Example of silver ratio block. Block to left is approximately the same size as the*
 321 *block to the right and the lower surface (not seen) was originally on the top surface of the right-hand*
 322 *block with the exposed failure plane bisecting the M-axis alignment of the original parent block. The*
 323 *red arrows delineate a fracture plane, aligned with the M-axis of the right-hand block, which divides*
 324 *the right-hand block into two near-equal halves.*
 325



326

327 *Figure 7: The shape relationship for blocks in terms of the Zingg (1935) ratios. The system state*
 328 *attractors for stochastic fracture (gold diamond) and silver ratio (green diamond) are shown, as are*
 329 *the central tendency shapes for mechanically crushed silica sand grains that were initial sub-rounded*
 330 *or angular (Seo et al., 2021). Curves represent the trend in values of M/L and S/M for constant*
 331 *values of S/L . ct symbols represent the central tendency of each population. Oval is the 95% contour*
 332 *after Oakey et al., 2005.*

333

334 Within Fig. 7, the Zingg ratios (S/M and M/L) for the sampled locations are plotted together with a
 335 data set for the broader region (Regional data). Within Fig. 7, completely equant (isotropic) forms
 336 are absent and plate-like forms survive more readily than rods. Nonetheless, the central tendency of
 337 block shape within the regional data is $S/M = 0.65$ and $M/L = 0.75$; *i.e.*, roughly midway between the
 338 system state attractor for stochastic fracture and the silver ratio attractor. Lines of constant equal
 339 aspect ratios (S/L) are shown for the silver ratio model ($\alpha = 0.63$) and for the stochastic fracture model
 340 ($\alpha = 0.43$). Seo et al. (2021) showed that for homogeneous silica grains, fracture depended on initial

341 particle form (Fig. 7) with angular grains tending towards the silver ratio whilst rounded grains tended
342 towards stochastic fracture. If the fracture process is scale-invariant, then the size differences
343 between silica grains and the Shap blocks can be ignored, and one would expect the Shap granite (a
344 largely homogeneous lithology) to migrate across the diagram from silver to stochastic fracture as
345 cubic blocks become progressively more rounded and ellipsoidal. Blocks deviating from either model
346 (either too long or flat, *e.g.*, approaching $\alpha = 0.30$), will tend to fracture and migrate back towards $\alpha =$
347 0.43, as is especially evident in Fig. S6B. The central tendencies of the regional data and each of the
348 sampled locations are closely grouped between the central tendencies of the silver and stochastic
349 fracture. The exception is the Blasterfield location which lies closer to the silver ratio, but with
350 increased distance of transport, Teesdale & Levy Pool blocks are in accord with stochastic fracture.
351 Thus, it is evident that block fracture fluctuates between each model, with a trend for constant equal
352 aspect ratios close to $\alpha = 0.50$ (not plotted in Fig. 7).

353 Although Fig. 7 provides an impression of the spread of block shapes around a central tendency there
354 is no clear impression of the actual shape evolution as possible representative shapes can only be
355 selected arbitrarily from the data clouds. Further, only the cube (or sphere) limit point (*e.g.*, 1, 1 in
356 Fig. 7) is real. Limit points for rods and plates exist only through mathematical definition, because as
357 the rod and plate limit points are approached, rods become infinitely long and plates infinitely thin.
358 Thus, representative shapes need to be selected objectively. To solve this problem the procedure of
359 Oakey *et al.* (2005) was utilized to define representative shapes that define the 95% contour around
360 the central tendency of the regional data, represented by the blue oval in Fig. 7. With reference to the
361 position of the 95% contour in the blade quadrant, curve $\alpha = 0.30$ is selected to demarcate a lower
362 bound for common block ratios; with a few plate-like or rod-like blocks occurring in the lower portion
363 of the diagram.

364

365 **3.3 Size evolution**

366 The size distribution of the Shap granite blocks with distance from the pluton source has not received
367 detailed attention, although Carling *et al.* (2013) provide some general observations suggesting there
368 is size reduction with distance. In this study, the sample sizes were insufficient to demonstrate the
369 reduction in block size expected with distance from the source outcrop. However, controls on size
370 reduction are evident. Specifically, blocks greater than $L = 4\text{m}$ are rare (Carling *et al.*, 2013), the size
371 being controlled by the close joint spacing of the granite at source (Firman, 1953). With few
372 exceptions, large blocks ($L > 3.0\text{ m}$) do not occur beyond 7 km from the pluton, at which point medium
373 blocks ($2.5 > L > 1.5\text{ m}$) become scarce, with small blocks ($1.5 > L > 0.5\text{ m}$) and cobble-sized material
374 dominating with further dispersal (Carling *et al.*, 2013). These observations indicate that there was a
375 control on the upper size of blocks entrained from the pluton and fracture rapidly reduced block size
376 inducing a crude size-reduction down plume within just a few kilometres. This process was
377 accompanied by local deposition of abrasion and spallation debris as components of a subglacial
378 traction till ~~edgement~~ till. Nevertheless, the fracture mechanics that control block shape inevitably
379 control size evolution (Figs. 5 and 6). For example, fracturing a parent cube with 4m long edges and
380 its progeny across the L -axis, only six sequent fracture divisions are required to produce a 1 m cube,
381 as will be demonstrated in the Discussion.

382

383 **4 Discussion: The context of size and shape constraints**

384

385 The initial hypothesis proposed that Sg ice-transported blocks would display changes in edge-rounding
386 and shape with distance to the east from the pluton. As shown in the Results and elaborated below
387 edge-rounding does change with distance but block shape is conservative.

388

389 Space-time substitution is an underlying tenant of this study, in that the size and shape characteristics
390 of multiple individual blocks (an erratic plume), dispersing across the landscape, can reflect the

391 evolution of a single erratic block through time along the same general spatial trajectory. An adequate
392 number of sampled blocks are required for this analogy to hold because perturbations to the
393 population of erratics can occur during dispersal. For example, blocks can have been introduced to
394 the W-E trajectory of the study plume by N-S ice movements reworking blocks previously deposited
395 outside of the eastern-directed plume during periods of time after the main W-E ice flow. Also, for
396 the purposes of determining transport distance, a zero x-axis origin has been assumed to be the most
397 easterly outcrop of the pluton at Wasdale Crag. However, some blocks might have been sourced up
398 to a few kilometres to the west of Wasdale Crag. Despite these potential perturbations, which include
399 a small degree of subaerial weathering, the small sample sizes are sufficient to clearly demonstrate
400 systematic change in edge rounding due to ice transport as well as block shape evolution. Finally,
401 edge-rounding and shape are re-set to a degree for the children each time a parent block fractures,
402 so the process of rounding and shape adjustment is not a smooth function of distance from the
403 outcrop, as is explained below.

404

405 **4.1 A conceptual model of block edge rounding controls**

406

407 It should be acknowledged that this study has not considered abrasion of the faces of blocks but has
408 focussed on the edges which tend to abrade and round more rapidly than the associated faces
409 (Boulton, 1974). The edges of blocks still within the outcrop are sharp, albeit some are subject to a
410 slight degree of rounding in place (Fig. 4) from glacial wear, as well as a little post-glacial subaerial
411 weathering. Detached blocks close to the outcrop also tend to exhibit slightly ice-rounded edges, with
412 sharply angled joint planes characterising the other faces due to fracture release of the block from
413 outcrop. The increase in edge rounding with distance confirms the initial hypothesis.

414

415 Block edge rounding initially is constrained by the hardness of the Shap granite and the way it fractures
416 when first entrained at outcrop. The absence of significant edge rounding at the outcrop indicates

417 that blocks were entrained continually until the imposed stresses fell below that required to quarry
418 further blocks. Otherwise, edge rounding of entrained blocks is associated with basal traction
419 transport (Boulton, 1978; Hallet, 1979). Although the compressive strength of granite is high, the
420 tensile strength is an order of magnitude lower; possible as low as 4% of the compressive strength,
421 *i.e.*, 8 MPa (Anikoh *et al.*, 2015; Demirdag *et al.*, 2018; Engineering ToolBox, 2008; Yu *et al.*, 2018).
422 Thus, where compression is translated into flexure, the propensity of the block to elongate across the
423 axis of flexure leads readily to fracture of the brittle granite. This condition means that many blocks
424 close to source initially exhibited near right-angle edges (Fig. 4). Given this geometric constraint, radii
425 of edge curvature inevitable are small initially, approaching the limit: $r_c = l/2$ and $r_c = h$, and
426 increase with distance from the outcrop due to abrasion. However, fracture away from the outcrop
427 introduces new sharp edges (Figs. 4 & 7), such that larger radii characterizing an individual edge-
428 rounded block just before fracture are augmented by smaller radii. This change is reflected in the
429 scatter of radii values found with increased distance from the outcrop (Fig. 4). However, as block size
430 reduces, a condition is approached whereby the population of blocks are increasingly those which
431 resist fracturing (see section 'Block size controls) which should allow edge rounding to become more
432 persistent and thus more pronounced with distance. This condition may be approached in the case
433 of the examples from Teesdale (Fig. 4A) where it is evident that short chords become fewer with
434 distance as larger values of r_c begin to dominate the population. As blocks in transport can reorientate
435 within the ice flow, edge rounding has no effect on block shape, given the shape definition herein.
436 However, if blocks are not free to reorientate, a case not considered herein, the form of blocks can be
437 significantly affected by abrasion in place (Boulton 1974; Hallet, 1979).

438

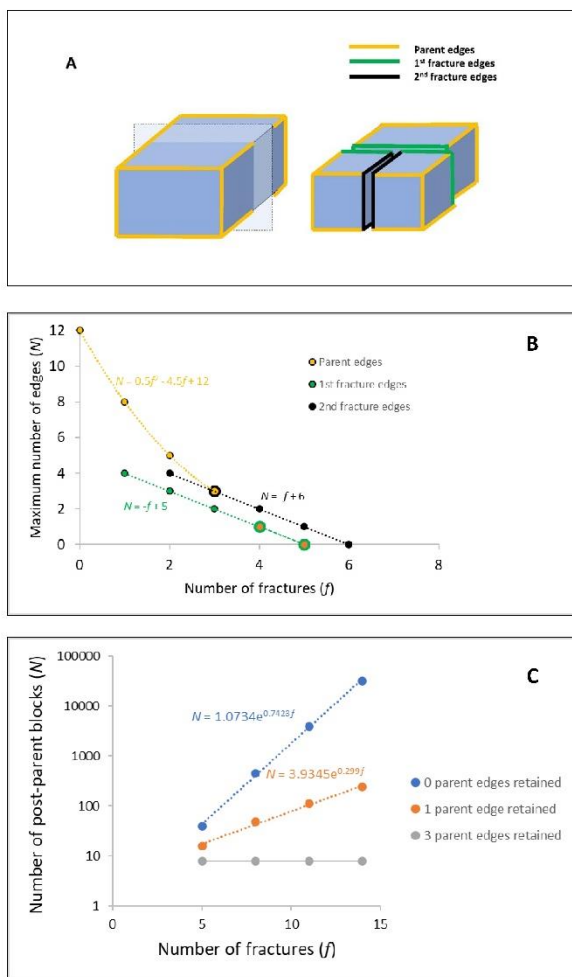
439 Although a positive exponential function (Equation 2) describes the increase in the mean edge
440 rounding with distance from the source outcrop (Fig. 4A inset panel), the function must eventually
441 transition to a negative function as abraded smaller blocks inevitably are characterized by smaller radii
442 of curvature. This latter condition was not recorded within the current study and sampling at greater

443 distances from the source would be required to determine if this transition occurs. A block (*e.g.*, 1 m
444 cube) subject to edge rounding equally on all 12 edges, as per Equation 2, would have lost about 4%
445 of its mass after 10 km and 9% after 40 km so, in contrast, fracture into two self-similar parts whereby
446 50% of mass is lost, is more significant than edge-rounding in terms of mass loss per block. The greater
447 significance of fracture is consistent with studies of ice erosion by quarrying versus abrasion of basal
448 bedrock surfaces (see references in Cohen *et al.*, 2006).

449

450 Rounding of individual blocks is not a steady process, as is evident from the data scatter in Fig. 4 and
451 is further illustrated in the following section. The process whereby the percentage of edges of
452 different generations are rounding with distance, or time, is shown schematically in Fig 8A, wherein
453 there are initially no more than 12 slightly rounded edges to a cube block newly released from outcrop
454 (see Supplementary Information for detail of the model). The model is simple but demonstrates the
455 complexity in edge rounding that must accompany successive fracturing of blocks. Fracturing the
456 block successively across the *L*-axis introduces new generations of fracture edges (sequent fractures
457 – Fig. 8B) at the same time as reducing the number of edges on each new block related to earlier
458 fracture events (see Supplementary Information for further detail). As the number of progeny blocks
459 increases exponentially for each fracture event (Fig. 8C), and each sibling can be further dissected
460 along one, two or three *M*-axes depending on block shape, a diagram including all fracture progeny
461 introduces unreasonable complexity, obscuring the key details. In Fig. 8A&B, for clarity, only one block
462 is followed through one to six sequent fractures, which reduces the number of data points for plotting
463 to a manageable number. The key point to illustrate is that the initial ‘parent’ block must be fractured
464 five times for one of the ensuing progenies to have lost all the initial 12 edges of the ‘parent’. The
465 total number of initial parent edges is relatively persistent because there are 12 edges to begin with
466 (Fig. 8). Contrarily, only four new edges (Fig. 8A) per block are produced on each fracture event. Thus,
467 in contrast to the curve for the initial parent edges, the 1st fracture edges can be lost in as little as four
468 fracture events depending on which sibling block is considered. The 2nd fracture edges are lost by a

469 total of five fracture events and so on, as more fractures occur adding new fracture edges. Relaxing
 470 the model to allow fracture across either the *M* or *S* axis (see Supplementary Information) only adds
 471 one or two fracture events to the process of edge extinctions. Thus, by introducing new edges at each
 472 fracture event, rounding of the block with distance or time is not a steady progression, with well-
 473 rounded edges being lost as blocks are split at the same time as new immature edges are added to a
 474 population of sub-mature edges. The model may not apply beyond some undetermined number of
 475 fracture events if there is a critical minimum block size that is less susceptible to fracture (as was noted
 476 above) and rounding then can become pronounced. Nonetheless, this model explains the presence
 477 of a ‘continuum’ from well-rounded edges to less-well-rounded edges on many individual blocks. The
 478 issue as to whether there is a minimum block size is considered in the next section.



479

480 *Figure 8: A) A regular block released from outcrop has 12 initial edges (Parent edges) all equally*
481 *rounded. Fracturing the block at right angles introduces four new edges (1st fracture edges) to each*
482 *of two sibling blocks, which edges are younger than the initial edges. A further fracture across the L-*
483 *axis is indicated by 2nd fracture edges; B) The maximum number of edges of each generation on a*
484 *block as a function of the number of fracture events, with only the parent edges and those edges*
485 *related to the first two fracture events plotted; C) The total number of blocks created at each fracture*
486 *event which retain 0, 1 or 3 of the original parent edges.*

487

488 The significant mean edge rounding, with distance from outcrop (Fig. 4A inset panel), indicates that
489 the blocks were transported within a mobile concentration of basal debris, in frequent block-to-block
490 contact and in contact with the bedrock, leading to abrasion before being deposited within a subglacial
491 traction till~~edgement till~~ (Hallet, 1979). If the distance travelled towards the east and south is not the
492 controlling factor, then the high degree of edge-rounding may be due to prolonged temporal transport,
493 with some material moving east, south, and then north again, extending the transport distances.
494 However, compatible with studies showing block modification after distances of only 0.4 km (Humlum,
495 1985; Lliboutry 1994; MacGregor *et al.* 2009), an alternative main explanation is preferred for the
496 easterly edge-rounding trend. Although Sg is mechanically strong in compression (Goudie, 2006) it is
497 susceptible to abrasion and tensile fracture for the following reason. The blocks contain large pink
498 phenocrysts set within a matrix of smaller mineral crystals. The large pink crystals are orthoclase
499 feldspar (Moh hardness 6 – 6.5). The other common minerals are glassy quartz (Moh hardness 7),
500 white plagioclase feldspar (Moh hardness 6) and black biotite mica (Moh hardness 2.5 – 3) (Caunt,
501 1986). ~~Weathered examples of blocks often exhibit phenocrysts standing proud (3–5mm) of the matrix,~~
502 ~~as the mica is readily subject to weathering (Wager, 1944).~~ Thus, the granular composition of the
503 granite with harder crystals adjacent to a soft mineral may aid rapid rounding by abrasion and facilitate
504 tensile fracture during glacial transport.

505 **4.2 Block shape controls**

506

507 Block shape is dependent on the initial controls exhibited at: 1) the outcrop of origin; and 2) the
508 subsequent transport history.

509

510 1) The primary control is the intersection of sub-vertical joints (Firman, 1953) in the granite with
511 horizontal expansion joint planes caused by unloading (Jahnes, 1943). Horizontal joints largely are
512 due to glacio-isostatic rebound and surface erosion (Westaway, 2009), leading to the release of the
513 residual stresses accumulated at depth (Berger & Pitcher, 1970). The resultant blocks initially tend to
514 be cubic. Where blocks lie within a few metres from the parent outcrop, the block faces tend to be
515 planar, although curved fractured surfaces occur occasionally, as do conchoidal fracture hollows on
516 otherwise planar surfaces. Curved fracture surfaces tend to occur in homogeneous granite due to
517 pressure unloading (Wang *et al.*, 2022), which will have occurred as ice erosion reduced the
518 overburden. Such joint-defined blocks within an outcrop are readily entrained by moving ice (Matthes,
519 1930; Morland & Boulton, 1975).

520

521 2) Although inhomogeneous blocks in traction may be envisaged as breaking down into multiple
522 fragments at each compressive event (Boulton, 1978), the largely homogeneous nature of the Sg
523 lithology leads to simple tensile fracturing, at each breakage event, whereby subsequent generations
524 of blocks exhibit shapes largely similar to the parent forms. Thus, there is a tendency for equant blocks
525 to persist, through time and distance, due to the tensile stresses associated with flexure across the
526 stoss surfaces reducing block mass in accord with either the silver model or the stochastic model. This
527 trend is indicated by the fact that stronger plate-like blocks occur less frequently away from the pluton
528 in contrast to the general absence at distance of the weaker rod-like blocks. Thus, cuboids progress
529 to form both cubes and cuboids such that the initial hypothesis is rejected.

530

531 **4.3 Block size controls**

532

533 Block size is dependent on the initial controls exhibited at: 1) the outcrop of origin; and 2) the
534 subsequent transport history.

535

536 1) The primary control is the presence of the frequent, well-developed joint planes within the pluton
537 (Firman, 1953; Caunt, 1986) which tend to define and delimit the range of the initial block sizes from
538 c., 0.5 m to 4 m. Fault planes are of sufficient rarity to be ignored. Joints are largely orthogonal: *i.e.*,
539 sub-vertical and near horizontal but oblique joints also occur.

540

541 2) Once in ice-transport, other controls on block disintegration may pertain. In the present case,
542 larger blocks close to the outcrop (< 0.8 km) often exhibit one (or more) intact or partially opened
543 failure plane(s) inherited from the outcrop structure. More commonly, with distance from the outcrop
544 (> 0.8 km), the planes of failure within individual blocks represent the directions of tensile and
545 compressive forces exerted by the ice on the blocks (and thus bear no relationship to structure or
546 composition), as appears to be the case where failure planes are aligned with the *L* or *M* axes. Fracture
547 occurred when the effective tensile stress exceeded the yield strength of the blocks. Glacial unloading,
548 and subsequent stress release, also may introduce planes of weakness within transported blocks.
549 Adopting the stochastic fracture mode or the silver ratio model for block shape changes indicates that
550 block volume effectively halves at each fracture event with consequent reduction in block size. This
551 conclusion has implications for the fractal evolution of erratic size distributions which, for brevity,
552 cannot be addressed within this paper.

553

554 Other small-scale planes of weakness can be attributed to spatial variations in the primary mineral
555 composition (Grantham, 1928; Parsons & Lee, 2005) leading to textural and grain-size variations which
556 can be visible rarely as parallel lineaments, and later hydrothermal alteration also induced
557 compositional and hence structural variations (Caunt, 1986). These weaknesses lead to loss of small
558 blocks and flakes from the larger parent blocks (see Supplementary Information) through spallation
559 rather than fracture. Spallation may be related to the state of stress within a deforming till layer

560 (LeBone Hooke & Iverson, 1995) rather than the tensile stress on the stoss side of a block which
561 accounts for block fracture.

562

563 **4.4 General considerations**

564

565 A significant question is whether flowing ice can generate significant stress to fracture the granite

566 blocks. If the thickness of the deforming ice layer at the basal boundary is small relative to the size of

567 the boulder, then the compressive force is likely to dominate. However, if the converse applies then

568 the tensile force likely will dominate. Herein, given that there is no information as to the thickness of

569 the deforming layer, the distinction is not considered because, in most cases, blocks will fracture at a

570 lower stress due to tension in contrast to compression. In a consideration of similar situations,

571 emphasis was placed on the compressive strengths of blocks (Boulton, 1978) relative to the normal

572 stresses due to a static ice load above a block. In the present examples, the tensile strength of the

573 stoss side of a block resisting flexure is more relevant for brittle fracture and for granite can be as low

574 as 8 MPa, which is a tensile stress readily applied by a modest (c., +100m thick)-yet dynamic ice cover

575 (Hallet, 1996). The distribution of compressive and tensile forces over the stoss side of a block

576 adjacent to the bedrock at the base of an ice mass will be complex and variable through space and

577 time (Hallet, 1979; Morland & Boulton, 1975; Ficker *et al.*, 1980; Cohen *et al.*, 2005). Yet, a simple

578 example below outlines the principles within the context of Shap granite erratics. Although a more

579 complex and complete appreciation of the stress environment of a boulder would be preferred, a

580 simple force balance is utilized instead. Simplicity is dictated by the absence of data to inform a more

581 complex model.

582

583 Setting the tensile stress at failure to 8 MPa and treating the rectangular block as subject to a critical

584 average driving force (τ_c) (Benn & Evans, 2011, p.114) due to ice flow, transverse and longitudinal

585 shear stresses arise of equal magnitude. Setting the fracture focus at half the block width in the

586 direction of loading, neglecting any water pressure variations (Cohen *et al.*, 2006) and deformation
587 within a basal till (LeBone Hooke & Iverson, 1995), and imposing the driving stress transverse to the
588 fracture plane, as little as 180 m thickness (H) of flowing glacial ice with an ice surface slope (α) of 1.5°
589 would be sufficient to induce fracture in the block:

590

$$591 \quad \tau_c = \rho_i g H \tan \alpha, \quad (3)$$

592

593 where ρ_i is the density of glacial ice and g is the acceleration due to gravity. The value of $H = 180$ m
594 pertains for a rectangular block with a surface area (A) defined by $L = 2$ m and $M = 2$ m (see
595 Supplementary Information for details). The effective instantaneous stress might be greater than as
596 given by Equation 3 (LeBone Hooke & Iverson, 1995) but for a block with $L = 3$ m, $M = 1$ m with the
597 long axis transverse to the ice flow the shear force maximum might be achieved with only 130 m of
598 ice cover (see Supplementary Information). To the east of the pluton the Last British Ice Sheet was
599 several hundred metres thick *c.*, 25-22 ka BP (Evans *et al.*, 2009), such that blocks would readily
600 fracture during full-glacial warm-based conditions where ice is flowing, as well as after the Late Glacial
601 Maximum when ice was thinning.

602

603 The smallest block sizes ($L < c.$, 1.0 m) present in the field were not considered, which means that the
604 sampled population was truncated at the finer end. Nevertheless, although in some rock-types, a
605 lower limit to block strength may be related to a minimum structural block size (Dreimanis & Vagners,
606 1971; Lim *et al.*, 2004; Domokos *et al.*, 2015) this is unlikely to pertain to granite which breaks-down
607 to grus at the scale of the phenocrysts. None-the-less, fracture and surface wear, to an initial block
608 population, tend to result in the observed block population consisting of those blocks which are
609 strongly resistant to further comminution (Moss, 1972; Tavares and King, 1998; Larson & Mooers,
610 2004; Pfeiffer *et al.*, 2022) which, in principle, enables some blocks to survive transport adjacent to
611 the sole of the ice for great distances before being deposited during the waning phase of the easterly

612 directed ice stream (Hallet, 1979). Thus, although there may be no lower effective block size, a
613 statistical increase in resistance to fracture of the block population with distance is likely evident as
614 witnessed by the increased rounding seen in the Teesdale population. The occasional far-travelled
615 large block, as noted in the Introduction, might be explained as being a statistically stronger example,
616 in contrast to the remainder of the population. Alternatively, large blocks can be cushioned within
617 the till body by smaller particles (Einav, 2007) thus avoiding fracture, or they can be transported
618 englacially, rather than basally, and consequently not subject to protracted abrasion and significant
619 compression whilst in traction. However, englacial blocks are more likely to be angular (Shilts, 1976;
620 Boulton, 1978) and might retain rugose faces.

621

622 Thus, although the reduction in plume parameters values, such as block size and concentration, are
623 commonly viewed as exponential functions of distance from the source (Shilts, 1976), such models
624 (*e.g.*, Fig. 4A inset panel) consider the sampled population as a whole and the inferences derived may
625 not apply to the transport history of individual blocks. Certainly, the reduction in edge rounding for
626 individual blocks is irregular with distance.

627

628 **5 Conclusions**

629

630 The hypothesis that granite blocks would display an increase in edge rounding with distance from the
631 source outcrop is confirmed, whilst the hypothesis that shape would evolve with distance is refuted.
632 Although the mean value for edge rounding for the whole block population increases exponentially
633 with distance, edge rounding on individual blocks is an irregular function mediated by block fracture
634 mechanics, as block size reduces (with shapes fluctuating between cuboids, slabs and rods) with
635 distance and new sharp edges are provided to partially edge-rounded blocks. Thus, edge rounding,
636 and shape coevolve as block size is reduced. Fracture transverse to block orientation is in accord with
637 the application of tensile stress which controls the process by which block form is conserved as block

638 size is reduced. Consideration of the orientation of the tensile fractures on blocks in the field might
639 be used to approximate the direction of ice flow at the time of fracture.

640

641 Overall, the results indicate that edge rounding is unlikely to be advanced if blocks continue to fracture.
642 Well-rounded blocks must represent blocks that have resisted splitting. In the case of exceptionally
643 large, rounded blocks, the rock mass likely is unusually homogeneous, lacking potential fracture lines.
644 However, smaller blocks are less likely to contain potential fracture lines and so fracture should
645 become less prevalent as blocks reduce in size, which then promotes edge rounding.

646

647 Future work should consider developing mathematical models that represent the function of edge
648 rounding as predicated by a model (*e.g.*, silver ratio) describing block size reduction. Similar studies
649 considering other lithologies (*e.g.*, stratified sedimentary rocks) likely would find different shape
650 evolution patterns in contrast to the cuboid central tendency displayed by the homogeneous granite,
651 with concomitant implications for edge rounding trends with time and distance.

652

653 **Author contribution**

654

655 PAC designed the study and conducted the field work, analysis, interpretation and drafting.

656

657 **Competing interests**

658

659 The author declares that he has no conflict of interest.

660

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662

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667 **Data Availability**

668 Basic data are available upon reasonable request from the author.

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