

# 1 Tipping points in coupled human-environmental system models: 2 a review

3 Isaiah Farahbakhsh<sup>1</sup>, Chris T. Bauch<sup>2</sup>, Madhur Anand<sup>1</sup>

4 <sup>1</sup>School of Environmental Sciences, University of Guelph, Guelph, N1G 2W1, Canada

5 <sup>2</sup>Department of Applied Mathematics, University of Waterloo, Waterloo, N2L 3G1, Canada

6 *Correspondence to:* Madhur Anand (manand@uoguelph.ca)

7 **Abstract.** Mathematical models that couple human behavior to environmental processes can offer valuable insights  
8 into how human behavior affects various types of ecological, climate and epidemiological systems. In many coupled  
9 human-environmental systems with tipping points, gradual changes to the human system can lead abruptly to  
10 desirable or undesirable new human-environmental states. We use snowball sampling to review the modelling of  
11 social processes—such as social norms and rates of social change—that are shown to drive tipping points, finding that  
12 many affect the coupled system depending on the system type and initial conditions. For example, tipping points can  
13 manifest very differently in input- versus output-limited systems. Some potential interventions, such as reducing  
14 costs associated with sustainable behavior, have intuitive results. However, their beneficial outcomes via less  
15 obvious tipping point behavior are highlighted. Of the models reviewed, we found that greater structural complexity  
16 can be associated with increased potential for tipping points. We review generic and state-of-the-art techniques in  
17 early warning signals of tipping points and identify significant opportunities to utilise digital social data to look for  
18 such signals. We conclude with an outline of challenges and promising future directions specific to furthering our  
19 understanding and informing policy that promotes sustainability within coupled human-environmental systems.  
20

21 **Non-technical summary.** Mathematical models that include interactions between humans and the environment can  
22 provide valuable information to further our understanding of tipping points. Many social processes such as social  
23 norms and rates of social change can affect these tipping points in ways that are often specific to the system being  
24 modelled. Higher complexity of social structure can increase the likelihood of these transitions. We discuss how data  
25 is used to predict tipping points across many systems.

## 26 1 Introduction to tipping points in coupled human-environmental systems models

27 Humans are facing environmental catastrophes of their own making, like climate change and biodiversity declines,  
28 at local and global scales and yet avoiding these catastrophes still poses complex challenges for sustainable behavior  
29 and policy interventions (Steffen et al., 2017). Traditionally, mathematical models of environmental systems have  
30 represented human impacts through fixed, static parameters or functions independent of the environment's current  
31 state (Binford et al., 1987; Bosch, 1971; Chaudhuri, 1986; Getz, 1980), and these models can be useful to inform  
32 optimal levels of sustainable extraction for short timescales. However, for longer timescales, where human dynamics

33 can evolve, it may be necessary to include human behavior endemically in the modelling framework to allow for  
34 human-environmental feedback to occur (Bauch et al., 2016; Innes et al., 2013; Lade et al., 2013; Schlüter et al.,  
35 2012). Coupled human-environmental system (CHES) models combine environmental (e.g., ecological,  
36 epidemiological, and climate) models with human behavior and population dynamics (Bury et al., 2019; Carpenter  
37 et al., 2009; Farahbakhsh et al., 2022; Innes et al., 2013; Lade et al., 2013; Phillips et al., 2020; Sethi and  
38 Somanathan, 1996). The human and environmental subsystems of the coupled system have two-way (positive and/or  
39 negative) feedback, such that changes in each subsystem influence one another. For example, in Innes (2013), the  
40 amount of forest cover influences the proportion of the population that conserves forest ecosystems. The inclusion of  
41 these feedbacks leads to increased diversity in the qualitative behavior of the system, such as whether the long-term  
42 dynamics converge to a sustainable or depleted environmental state, or cycle over time. Negative feedback promotes  
43 a return to equilibrium (Figure 1a) and can increase the system's capacity to respond to disturbances and adapt in  
44 ways that allow the system to maintain the function of social and ecosystem services, which is sometimes referred to  
45 as “resilience” (Folke, 2006).

46

47 Human-environmental negative feedback loops via processes such as public concern pressuring governments to  
48 introduce environmental legislation can be powerful and there are many historical examples of it occurring (Dunlap,  
49 2014; Grier, 1982; Mather and Fairbairn, 2000; Stadelmann-Steffen et al., 2021). Forest cover in Switzerland  
50 doubled, following an all-time low in the first half of the 19th century brought about by rapid population growth and  
51 early industrialisation. Wood shortages and floods led to public concern, triggering local regulation, the formation of  
52 the Swiss Forestry Society, and the first federal forestry law enacted in 1876 that in turn caused a recovery of forest  
53 cover (Mather and Fairbairn, 2000). Similarly, the bald eagle population in North America recovered significantly  
54 after the banning of DDT by the EPA in 1972. This was instigated by public outcry following the publication of  
55 Rachel Carson’s *A Silent Spring* in 1962 which linked DDT in the environment to low reproduction of birds and  
56 their declining population (Dunlap, 2014; Grier, 1982). In both cases, gradual recovery of the population was not  
57 brought about simply by governmental legislation. There were also strong movements in the public and scientific  
58 spheres, directly responding to perceived environmental risk which pressured governing bodies to enact immediate  
59 reform (Dunlap, 2014; Grier, 1982; Mather and Fairbairn, 2000). We interpret these two examples as negative  
60 feedback loops in a coupled human-environmental system because a decline in forest/eagle abundance stimulated a  
61 response by humans which led to the recovery of the environmental system (Figure 1a). These negative feedback  
62 loops are pervasive in the CHES models that we review here.

63

64 In contrast to negative feedback that promotes an eventual and often gradual return to equilibrium, tipping points  
65 describe a phenomenon in complex systems near an equilibrium where gradual changes in external conditions lead  
66 to abrupt and lasting shifts in the system state and characteristic behavior (also referred to as a “regime”). One way  
67 tipping points may occur is through nonlinear self-reinforcing mechanisms known as positive feedback loops, which  
68 amplify these gradual changes, propelling the system into a new stable state in ways that are often difficult to  
69 reverse. Such transitions have been extensively modelled using dynamical systems theory, where they exemplify a

70 type of “bifurcation” (Ashwin et al., 2012; Crawford, 1991; Dakos et al., 2008; Lenton et al., 2008). Additionally,  
71 many systems with tipping points exhibit alternative stable states, where the system has the potential to persist over  
72 long periods of time in one of multiple states under the same parameters (May, 1977; Lenton et al., 2008, Henderson  
73 et al. 2016). In many cases, a return to the system's previous state can be more difficult than anticipated, requiring  
74 additional effort rather than merely a return to parameters before the tipping point, a phenomenon known as  
75 hysteresis, which can make mitigation and adaptation efforts challenging.

76

77 Bifurcation theory has been applied to study tipping points in a vast number of environmental models (May and  
78 Oster, 1976; Brovkin et al., 1998; Ghil and Tavantzis, 1983; Wollkind et al., 1988); however, more recently,  
79 researchers have identified abrupt shifts in environmental systems for which bifurcation theory has yet to be  
80 explicitly applied (Dakos et al., 2019; Lenton, 2020, 2013). For example, during the mid-Holocene, the Sahara was  
81 much more humid than at present, showing evidence of shrub and savannah biomes as well as the expansion of  
82 lakes, an alternative stable state to what we know as its current desert state. It is hypothesised that around 5,000  
83 years ago, the gradual weakening of the North African Monsoon led to an abrupt decrease in vegetative cover, due to  
84 positive feedback between reduced surface albedo and precipitation, bringing the Sahara into a stable desert state  
85 (Hopcroft and Valdes, 2021; Pausata et al., 2020). In more dominantly human systems, many pivotal revolutions can  
86 also be framed as tipping points where gradual changes are reinforced by positive feedback loops, leading to a new  
87 political or technological stable state (Lenton et al., 2022). Social tipping points also occur in financial systems such  
88 as in the 2008 financial crisis. Here, the bankruptcy of Lehman Brothers led to a rise in public panic around the  
89 stability of markets, causing banks to increase their liquidity, amplifying the crisis in other economic sectors and  
90 leading to a global recession (Van Nes et al., 2016). These are just two of many examples illustrating how important  
91 tipping points are as a phenomenon, in both human and environmental systems, and coupling these systems using  
92 mathematical models could lead to further insights.

93

94 Since the beginning of the Anthropocene and with our growing awareness of human impacts on the environment,  
95 tipping points are increasingly being conceptualised within the context of coupled human-environmental systems  
96 (Bauch et al., 2016; Henderson et al., 2016; Lenton et al., 2022; Milkoreit et al., 2018). Tipping points can lead to  
97 highly beneficial or catastrophic outcomes for humans, especially when an environmental change occurs in the  
98 presence of social hysteresis. An example of detrimental tipping is in the forests of Kumaun and Garhwal in  
99 Northern India, where, prior to British colonisation, wood harvest was sustainably regulated through social norms  
100 and strict rules enforced by local village councils. When the British colonial government imposed their own rules on  
101 the use of forests, these social norms broke down. Eventually, protests led to British lumber restrictions being  
102 removed, but the system subsequently experienced rapid deforestation rather than a return to its previous levels  
103 under local management (Somanathan, 1991). This system has been modelled using a dynamical systems approach  
104 that allows for a quantitative understanding of the human drivers leading to the tipping points (Sethi and  
105 Somanathan, 1996). Contrasting this example, tipping points can also result in environmental change that is  
106 beneficial to humans and the environment. The rapid response of the international community to the hole in the

107 ozone layer has been interpreted by some as an example of a system undergoing tipping points caused by  
108 human-environmental feedback (Stadelmann-Steffen et al., 2021). First, there was a shift in public opinion regarding  
109 the use of CFC products, causing a change in behavioral norms and pressure on political institutions to follow suit.  
110 Then when policy was passed, industry shifted abruptly to producing CFC alternatives, which led to a tipping point  
111 in CFC emissions bringing about a new stable state of relatively low emissions globally (Andersen et al., 2013;  
112 Cook, 1990; Epstein et al., 2014; Stadelmann-Steffen et al., 2021).

113

114 Tipping points associated with social processes as described in the preceding paragraph can be conceptualised  
115 through positive feedback loops that capture a self-reinforcing process. In the case of social norms, this  
116 self-reinforcing process may correspond to peer pressure or conformism that reinforces the dominant opinion or  
117 belief. Depending on whether pro- or anti-mitigation opinions are currently dominant, this could lead to hysteresis  
118 (Figure 1b). The negative feedback loop that might normally regulate the CHES to exist in a state of intermediate  
119 environmental health and public support for sustainability (Figure 1a) could be overpowered by the positive  
120 feedback of social norms, leading the population to a state where either sustainability (or anti-sustainability) is  
121 strongly entrenched. If the conditions governing social learning or social norms move beyond a tipping point, the  
122 population may flip between these two norms, or alternatively it may move into a regime where social norms are  
123 instead dominated by the negative feedback loop, causing the population to exist in an interior state of partial  
124 sustainability. As such, negative feedback and positive feedback may be characteristic of any CHES and should be  
125 systematically studied.

126

127 This review aims to deepen our understanding of human drivers of tipping points in CHES models by exploring  
128 three crucial topics: the feedback loops and interactions between the human and environmental systems, the  
129 structural characteristics of the human system that influence tipping points, and the identification of early warning  
130 signals within human systems. By “human drivers”, we refer to the gradual changes in social parameters that elicit  
131 these non-linear tipping responses in either the environment, human system, or both. However, we also discuss  
132 aspects of social structure that may be conducive to tipping points. In the following sections we review CHES model  
133 literature found using Google Scholar with the keywords: ‘human environment system’ OR ‘socio-ecological  
134 system’ OR ‘social ecological system’ OR ‘human ecological system’ OR ‘human natural system’ combined with  
135 ‘tipping’ OR ‘regime shift’ OR ‘bifurcation’. Additional literature was found through a snowball approach using  
136 references from the sources found in this search as well as papers referencing these sources (Wohlin, 2014). The  
137 findings in this review highlight commonalities between the CHES models surveyed; however, some trends may be  
138 a result of both the dynamical models chosen and the relatively low diversity and volume of these models.

## 139 **2 Structures and processes in human systems that cause tipping points in CHES models**

140 In this section, we look at how social processes and structures cause tipping points. In order to have a better  
141 understanding of how these human drivers affect tipping, it is important to understand the basics of modelling

142 human systems. Within CHES models, various factors, such as economic incentives, environmental considerations  
143 and social pressures determine how individuals make decisions and interact with the environment. In most of the  
144 current modelling literature, individuals can choose between two behaviors (also referred to as opinions or  
145 strategies), one that is environmentally sustainable (also referred to as mitigation or cooperation) and another that is  
146 detrimental to the environment (also referred to as non-mitigation or defection). The perceived advantage of  
147 mitigation or non-mitigation relative to the current state of the human and environmental system can be quantified  
148 through a “utility function”. Common factors in the utility function are the rate of social learning, which determines  
149 the speed of human behavior change relative to environmental processes, social norms, which encourage the status  
150 quo or mitigation proportional to its frequency, cost of mitigation, which measures the economic cost of being a  
151 mitigator relative to a non-mitigator, and rarity-motivated valuation, which incentivizes mitigation as the  
152 environment approaches collapse (Bauch et al., 2016; Farahbakhsh et al., 2022; Tavoni et al., 2012). In most models  
153 that use social learning, individuals sample others in the population at a fixed rate and adopt a different behavior if  
154 the other behavior has a higher utility, with probability proportional to the difference in utility (Hofbauer and  
155 Sigmund, 1998; Schuster and Sigmund, 1983). This can also be formulated in a stochastic setting, where the  
156 probability of adopting a neighbor's behavior is a function of the difference in utility between behaviors (Schlag,  
157 1998). Most of the models reviewed in this paper use social learning to represent human behavioral dynamics. There  
158 are also CHES models that do not include social learning such as Motesharrei (2014) and Dockstader (2019) where  
159 the human population is influenced by its current size and the state of the environment; however, these are outside  
160 the scope of this paper.

161

162 Many human behaviors, such as resource extraction and pollution, have direct detrimental impacts on the  
163 environment; however, the severity of these impacts is often hard to predict. In many CHES models, small changes  
164 in parameters governing human behavior and social processes can lead to the abrupt collapse of sustainable states  
165 through tipping points that can cascade between the human and environmental systems (Bauch et al., 2016; Lade et  
166 al., 2013; Richter and Dakos, 2015; Weitz et al., 2016). Additionally, structural elements of the human system, such  
167 as the degree of choice and individual diversity, as well as how the social system is organised, can affect tipping.  
168 These heterogeneous model elements are often only accessible in agent-based models, where humans are  
169 represented as individual agents that follow a set of rules. CHES models do not always exhibit tipping points under  
170 realistic settings for the human system (Bury et al., 2019; Menard et al., 2021); however, in this review, we focus on  
171 models with tipping points.

## 172 **2.1 Coupling strength**

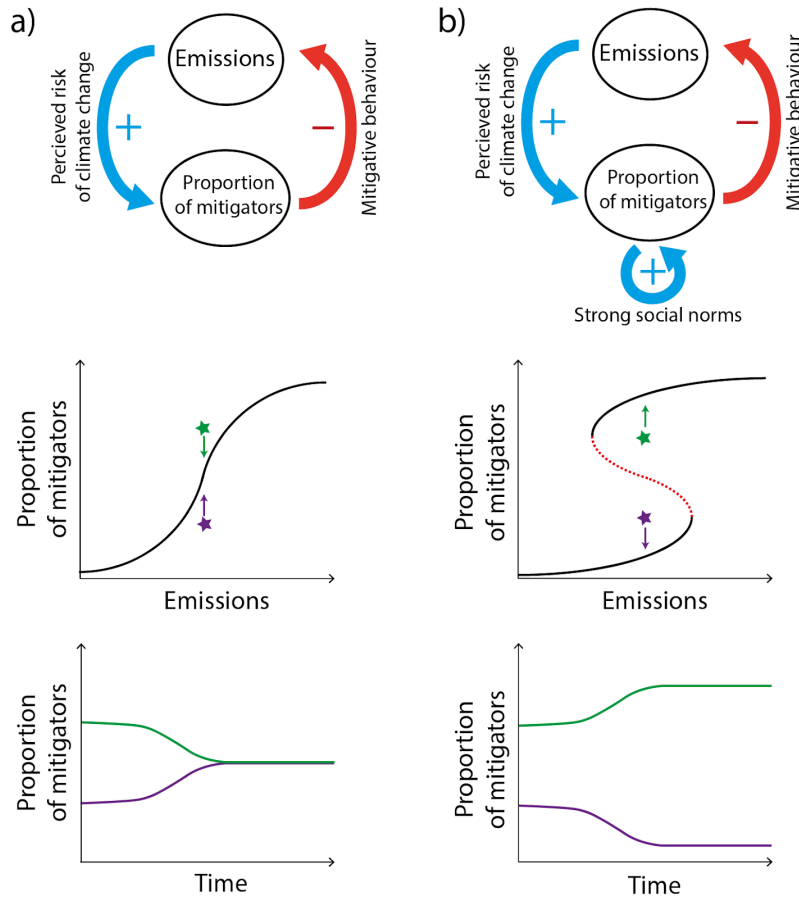
173 Coupling strength (how strongly the subsystems are coupled) can have a significant effect on the occurrence of  
174 tipping points in both systems, and the nature of these transitions often depends on whether systems are  
175 ‘input-limited’ or ‘output-limited’. In input-limited systems, humans extract from an environmental resource such as  
176 in forest and fishery models. Stronger coupling in input-limited models often leads to environmental collapse. A  
177 common social parameter representing the coupling strength in these systems is the extraction effort of humans,

178 which when increased past a critical threshold, leads to abrupt environmental collapse (Farahbakhsh et al., 2021;  
179 Richter and Dakos, 2015; Richter et al., 2013; Schlüter et al., 2016). For output-limited systems, where human  
180 activity increases levels of harmful outputs, such as pollution and climate models, coupling strength is instead  
181 represented by pollution rates. The influence of this coupling is less intuitive than extraction effort, for example, in  
182 lake pollution models as the pollution output of mitigators is decreased, pollution levels also decrease until a  
183 threshold is reached, heralding a detrimental tipping point where mitigation collapses and pollution then reaches a  
184 high level (Iwasa et al., 2010, 2007). This occurs because when the lake water is not very polluted, there is less  
185 incentive to be a mitigator and high-polluting behavior becomes a new norm. It is important to note that these  
186 models do not account for individuals valuing the environment in a healthy state, for example through the centering  
187 of ecosystem services, and the above example may be an artefact of this assumption. There is a need to shift both  
188 our relationship to the environment as well as the assumptions in our models so that inherent value in environmental  
189 systems is central in any decision-making, even when the environment is far from collapse. This fundamental  
190 valuing of the environment is present in many traditional indigenous belief systems, where relationships to the local  
191 natural environment are incorporated and prioritised in all aspects of life (Appiah-Opoku, 2007; Bavikatte and  
192 Bennett, 2015; Beckford et al., 2010; McMillan and Prosper, 2016).

## 193 **2.2 Rarity-motivated valuation**

194 Rarity-motivated valuation represents the extent to which humans increase their mitigative behavior in response to  
195 the environmental variable (e.g., forest cover, endangered species population size) nearing a depleted state. Model  
196 systems with rarity-motivated valuation often exhibit two tipping points at high and low levels, with a sustainable  
197 regime for intermediate values. High levels of rarity-motivated valuation lead to overshoot dynamics, however, this  
198 may not be true in empirical systems. In models, the sensitivity of human response to the abundance of the natural  
199 resource/population is represented by a ‘sensitivity’ parameter and there are often two critical thresholds in the  
200 sensitivity parameter that lead to tipping. Increasing the sensitivity parameter beyond the lower threshold induces a  
201 tipping point from a depleted to sustainable environmental equilibrium (Ali et al., 2015; Barlow et al., 2014; Bauch  
202 et al., 2016; Drechsler and Surun, 2018; Henderson et al., 2016; Lin and Weitz, 2019; Sun and Hilker, 2020; Thamp  
203 et al., 2018; Weitz et al., 2016). The second threshold exists at high values of the sensitivity parameter, where the  
204 sustainable equilibrium is destabilised by overshoot dynamics or a state of chaos in both the human and  
205 environmental systems. These dynamics are caused by the human system being too sensitive to changes in the  
206 environment, leading to extreme oscillations in both human behavior and the environment, which increases the  
207 likelihood of collapse in mitigation and the state of the environment (Bauch et al., 2016; Henderson et al., 2016).  
208 Rarity-motivated valuation can also be represented by a threshold in the state of the environment, below which  
209 humans shift towards sustainable behavior. In a common-pool resource model, lowering this threshold led to a series  
210 of tipping points that surprisingly resulted in a higher biomass equilibrium, although the trajectory to this state  
211 comes close to environmental collapse. This is in contrast to a high threshold, which leads to lower final biomass;  
212 however, the trajectory remains much farther from a depleted environmental state (Mathias et al., 2020). Similarly to  
213 high coupling in pollution models, one should be very careful to not interpret these results as stating “too much

214 conservation is detrimental to the environment”. They rest on model assumptions of a reactionary conservation  
 215 paradigm, where there is less value in conserving when the environment is in a healthy state.  
 216



**Figure 1: Negative feedback between the human and environmental subsystems, support convergence to the same equilibrium regardless of initial conditions (a). With strong majority-enforcing social norms, encouraging either mitigative or harmful behavior adds a positive feedback loop which makes the coupled system highly dependent on initial conditions (b). The top row shows the negative feedback loop between emissions and the proportion of mitigators, where (b) also includes the positive feedback of majority-enforcing social norms. In the middle row, equilibrium curves are plotted as a function of the maximum emissions of non-mitigators. Black solid lines represent stable equilibria and the red dotted line represents unstable equilibria. The green and purple curves in the bottom row are the trajectories for initial mitigation support and emission value given by the stars of the corresponding color in the upper row.**

217 **2.3 Social norms**

218 Introducing social norms can lead to alternative stable states and thus tipping points (Figure 1b), although the system  
 219 dynamics are highly dependent on both the type of social norms and initial conditions. Social norms are informal

220 rules emerging through social interaction that promote and discourage certain behaviors, especially around how  
221 humans relate to one another and the environment (Chung and Rimal, 2016). In models of small groups such as a  
222 community of fishers, they are often (rightly) assumed to support mitigative behavior by punishing those who  
223 violate norms by over-harvesting (Ostrom, 2000). However, at larger population scales, social norms can support  
224 either pro- or anti-mitigation behavior, on account of factors such as politicisation of actions relating to  
225 environmental, climate, and public health crises (Stoll-Kleemann et al., 2001; Van Boven et al., 2018; Latkin et al.,  
226 2022). Unlike a fisher for instance, a climate denier may not acknowledge themselves as a ‘defector’ who is harming  
227 a public good, but rather view the climate activist as ‘defecting’ against a free society. Thereby, social norms have  
228 the ability to encourage behavior that is harmful to both human and environmental well-being, over larger spatial  
229 and temporal scales (Bury et al., 2019; Latkin et al., 2022; Menard et al., 2021; Stoll-Kleemann et al., 2001; Van  
230 Boven et al., 2018).

231

232 Social norms can be represented as majority-enforcing, incentivizing the behavior of the majority, or  
233 mitigation-enforcing, such as sanctions, which only incentivize mitigation, relative to the proportion of mitigators in  
234 the current state of the system. In CHES models, increasing the strength of majority-enforcing norms leads to an  
235 increased number of regimes as well as bistable (more than one stable state) regimes (Figure 1b), made up of a  
236 single dominant behavior, which is highly dependent on the initial proportion of behaviors in a population (Ali et al.,  
237 2015; Barlow et al., 2014; Bauch et al., 2016; Bury et al., 2019; Phillips et al., 2020; Sigdel et al., 2017; Thampi et  
238 al., 2018). This occurs because these norms are indifferent to the type of behavior they enforce (i.e. sustainable vs  
239 harmful actions), and they act as a double-edged sword that reinforces the status quo through a positive feedback  
240 loop, where the dominant behavior becomes more prevalent (Figure 1b). On the other hand, increasing  
241 mitigation-enforcing social norms lead to a transition of the environmental system into a sustainable equilibrium  
242 (Chen and Szolnoki, 2018; Iwasa et al., 2010; Lafuite et al., 2017; Moore et al., 2022; Schlüter et al., 2016; Tavoni et  
243 al., 2012), sometimes through an intermediate regime of oscillatory dynamics (Iwasa et al., 2007). In a lake pollution  
244 model, along with decreasing the likelihood of environmental collapse, this increase in mitigation-enforcing social  
245 norms also led to the appearance of alternate stable states (Sun and Hilker, 2020). These findings show that stronger  
246 social norms lead to a greater number of tipping points; however, the trajectories brought about by these tipping  
247 points are highly dependent on the type of social norms (mitigation- or majority-enforcing) as well as the current  
248 dominant social behavior.

#### 249 **2.4 Cost of mitigation**

250 Reducing the cost of mitigation often leads to beneficial tipping points; however, these tipping points can depend on  
251 the rate of social change as well as social norms. Although it is intuitive that reducing costs or increasing economic  
252 incentives associated with mitigative action will have beneficial impacts on the environment, CHES models also  
253 show that this beneficial change can occur through tipping points (Bauch et al., 2016; Drechsler and Surun, 2018;  
254 Milne et al., 2021; Moore et al., 2022; Sigdel et al., 2017; Thampi et al., 2018). In coupled epidemiological models,  
255 where the environmental state is the proportion of infected individuals, mitigation cost is represented through the



256 economic cost or perceived risk of vaccination. Decreasing this cost leads to beneficial tipping points from a state  
257 with low pro-vaccine opinion and vaccine coverage to high pro-vaccine opinion and vaccine coverage (Phillips et  
258 al., 2020). Conversely, increasing this cost leads to a state of high infection and low vaccination. This detrimental  
259 tipping point occurs in the human system at lower levels of vaccination cost when majority-enforcing social norms  
260 are low, leading to widespread anti-vaccine opinion before the infection becomes endemic again (Phillips and  
261 Bauch, 2021). Decreasing profits of individuals engaging in non-mitigative behavior can also lead to an abrupt shift  
262 to a state of pure mitigators (Shao et al., 2019; Wiedermann et al., 2015); however, this transition can be dependent  
263 on a low rate of social change (Wiedermann et al., 2015). Other models demonstrate tipping in the other direction  
264 where increasing non-mitigators' payoff brings about a regime shift to pure non-mitigation and environmental  
265 collapse (Richter et al., 2013; Tavoni et al., 2012). Similarly, a common-pool resource model that uses machine  
266 learning in a continuous strategy space shows tipping to a depleted resource regime when the costs associated with  
267 harvesting are too low (Osten et al., 2017). An analog to mitigation cost is taxation rates, which resource users pay  
268 towards public infrastructure mediating resource extraction. In a model where individuals can choose to work  
269 outside of the system, pushing taxation rates to high or low levels tips a sustainable regime where institutions are at  
270 full or partial capacity to a collapse of institutions (Muneepeerakul and Anderies, 2020). In another model, only  
271 individuals with high extractive effort are subject to taxation, and increasing this taxation rate brings about a  
272 beneficial tipping point to a sustainable regime. However, the size of this sustainable region is smaller with multiple  
273 governance nodes evolving through social learning compared to a single taxing entity (Geier et al., 2019). However  
274 the cost of mitigation is represented, increasing the relative economic incentive of mitigation behavior has the  
275 potential to bring about beneficial tipping to a sustainable regime.

## 276 **2.5 Rates of social change and time horizons**

277 Human and environmental change often occur on different timescales and their relative rates of change play a major  
278 role in the long-term dynamics of the coupled system and whether or not tipping points will occur. Increasing the  
279 rate of social change (in most cases, social learning) leads to collapse in input-limited models due to overshoot  
280 dynamics. Whereas, in output-limited models, the impacts of the rate of social change are more model-specific. In  
281 both types of models, increasing the time horizon in decision-making is beneficial. In CHES models, these rates of  
282 change can be controlled by the rate of social learning which determines how frequently individuals interact and  
283 consequently, the pace of behavioral change within a population. Changes in the speed of the human system can  
284 have very different outcomes depending on the nature of human-environmental coupling. In input-limited models,  
285 increasing the speed of the human system relative to the environment often destabilises sustainable equilibria,  
286 leading to oscillations in both systems and, in many cases, the abrupt collapse of the environmental system. These  
287 overshoot dynamics occur as humans change their behavior too quickly to allow for the environment to stabilise. On  
288 the other hand, decreasing the relative speed of human dynamics usually brings about beneficial tipping points  
289 leading to a state of high forest cover (Figueiredo and Pereira, 2011), and supporting mitigators for a generalised  
290 resource (Hauert et al., 2019; Shao et al., 2019). These beneficial effects have also been observed in adaptive  
291 network models where individuals imitate their neighbors depending on the profitability of their strategies (Barfuss

292 et al., 2017; Geier et al., 2019; Wiedermann et al., 2015). The reduced speed of social change leads to beneficial  
293 outcomes as the resource is allowed more time to stabilise as decisions regarding extractive levels occur. Other  
294 relative rates of change can also significantly influence the existence of a sustainable regime. For example, in an  
295 agricultural land use model, increasing the speed of agricultural expansion and intensification relative to human  
296 population growth leads to the collapse of both the natural land cover and human population (Bengochea Paz et al.,  
297 2022).

298

299 In output-limited models, increasing the speed of social interaction is more model-specific. In some cases, such as  
300 forest-pest and climate systems, increasing the speed of the human system leads to better mitigation of  
301 environmental harms in the short term. However, long-term sustainability often requires additional social  
302 interventions such as reducing mitigation costs and increasing levels of environmental concern (Ali et al., 2015;  
303 Barlow et al., 2014; Bury et al., 2019). In lake pollution models, higher relative speeds of social dynamics can  
304 destabilise low-pollution equilibria, leading to oscillations and eventually a polluted state with no mitigation (Iwasa  
305 et al., 2010, 2007; Sun and Hilker, 2020). This is a similar phenomenon to the overshoot dynamics that occur when  
306 the human system is extremely reactive to the environment discussed in the case of rarity-motivated valuation;  
307 however, these outcomes are highly dependent on other social parameters. In a related model, with no social  
308 hysteresis, represented by mitigation-enforcing social norms, and strong environmental hysteresis, represented by a  
309 high phosphorus turnover rate, fast social dynamics could stabilise oscillations, leading to a low-pollution  
310 equilibrium (Suzuki and Iwasa, 2009). The emergence of oscillations under low rates of social learning, which was  
311 not observed in similar models is likely due to the environmental system being in a bistable state under strong  
312 hysteresis, such that even slow changes in the human system could tip the lake system into an alternative stable  
313 state.

314

315 When looking at relative rates of change in human and environmental systems, it is clear that the pace of the human  
316 system can be more readily influenced by interventions. This suggests an urgent need to further study the  
317 relationship between social and ecological timescales across a wide range of coupled systems to aid in sustainable  
318 policy-making decisions (Barfuss et al., 2017). Additionally in many models, the length of time horizons that  
319 humans take into account when deciding how they interact with the environment has a significant beneficial effect  
320 on conserving natural states and mitigating harmful action (Barfuss et al., 2020; Bury et al., 2019; Henderson et al.,  
321 2016; Lindkvist et al., 2017; Müller et al., 2021; Satake et al., 2007). A high degree of foresight in decision-making  
322 is a fundamental basis for many indigenous belief systems across the world. One manner in which this shows up is  
323 in land stewardship where care for the environment is prioritized as a means to ensure the health of many  
324 generations in the future (Appiah-Opoku, 2007; Beckford et al., 2010; Ratima et al., 2019).

## 325 **2.6 Social traits**

326 The inclusion and distribution of traits within agents can play a large role in determining the occurrence and types of  
327 tipping points within the coupled system, where ncreasing the modelled heterogeneity in social traits can lead to

328 more tipping and also promote sustainable outcomes. The majority of models discussed in the previous section only  
329 allow humans to choose between two strategies; mitigation and non-mitigation. The inclusion of additional  
330 strategies, determining how individuals interact with the environment and each other, can alter the potential for  
331 tipping points. For example, a common-pool resource model included a third strategy of conditional mitigation  
332 (Richter and Grasman, 2013). Under this additional strategy, agents act as mitigators until the number of  
333 non-mitigators reaches a certain threshold, where they then shift their behavior to non-mitigation. The addition of  
334 this third strategy alters tipping dynamics in opposite ways, depending on the value of maximum harvesting efforts.  
335 When efforts are high, the system is less prone to tipping; however, when they are low, tipping points are more  
336 likely to occur. This third strategy also affects tipping points by masking internal social dynamics, leading to more  
337 abrupt transitions, even when the system appears to be stable. This occurs when mitigators gradually change their  
338 strategy to conditional mitigators which can go unnoticed as their interaction with the environmental system does  
339 not change. However, when non-mitigation reaches high enough levels, there is a cascade of conditional mitigators  
340 choosing non-mitigation, in an example of herd behavior, which puts abrupt harvesting pressure on the resource.  
341 Another three-strategy model, where agents are partitioned by resource extraction rates, contrasts dynamics with and  
342 without the trait of environmental concern (Mathias et al., 2020). In the absence of this trait, the human system  
343 either tips to a state of high-extraction or low-extraction behavior, triggering either a detrimental or beneficial  
344 environmental tipping point, respectively. Including environmental concern leads to an increased number of  
345 cascading tipping points between both human and environmental systems. In a coupled agricultural model, where  
346 human traits include management strategies that respond to socio-economic and climate conditions, decreasing the  
347 diversity of these traits among agents in the system transitions the system from a sustainable state with high food  
348 production, landscape aesthetics and habitat protection to a state with low habitat protection (Grêt-Regamey et al.,  
349 2019). As there are relatively few models that explicitly compare the complexity of social traits and their effect on  
350 tipping points, it is difficult to say with certainty whether higher complexity will increase the likelihood of tipping  
351 points in all CHES and whether this is due to a higher dimensionality of the system. However, these commonalities  
352 are worth highlighting and will be put to the test with future CHES models and empirical work.

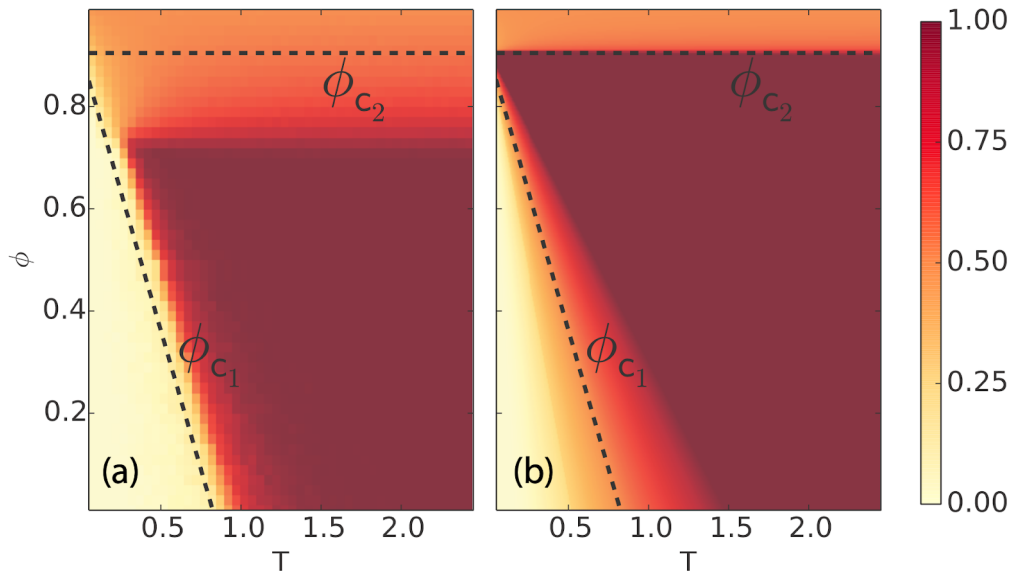
## 353 **2.7 Social networks**

354 In many agent-based CHES models, individuals are structured on a social network, where they usually only interact  
355 with others whom they share a link with. These models demonstrate how a higher number of connections in social  
356 networks increases the potential for tipping points, often through the emergence and growth of a bistable regime  
357 (Holstein et al., 2021; Sugiarto et al., 2017a, 2015). Additionally, the distributions of these connections play an  
358 important role. For example in networks with the same average number of connections, higher heterogeneity of  
359 connections among nodes leads to tipping points occurring earlier under certain social (Ising model) dynamics  
360 (Reisinger et al., 2022). The distribution of resources in human-environmental networks also affects the potential for  
361 abrupt environmental collapse. This often occurs in CHES network models where both human and environmental  
362 dynamics occur on a multi-layer network. Resource heterogeneity can be controlled through the distribution of  
363 carrying capacities or the amount of resource flow between nodes in the network, where higher flows lead to

364 homogeneous resource distributions. In both cases, increasing this heterogeneity can tip the system to a state of low  
365 extraction and high sustainability. Heterogeneity in carrying capacities increases the likelihood of sustainable  
366 harvesters extracting from a resource with a large capacity, which they can maintain at high levels, eventually  
367 convincing neighboring nodes to imitate their strategy (Barfuss et al., 2017). Heterogeneity through lower resource  
368 flows also leads to high-extraction nodes over-exploiting their resource and losing profits in the long run,  
369 de-incentivizing neighbors to imitate their behavior. Interestingly, optimal resource flow, which minimises the  
370 likelihood of resource collapse is found to be close to the critical threshold of resource flow, above which the  
371 coupled system collapses. As optimal resource flow decreases the likelihood of collapse by supplementing resources  
372 harvested at high levels, this confers an advantage to high resource extraction. Increasing past optimal levels leads to  
373 similar resource levels among high and low-extraction nodes, resulting in higher profits from high-extraction nodes,  
374 incentivizing the entire human system to eventually choose the high-extraction strategy (Holstein et al., 2021).

375

376 Heterogeneity of human interaction can be quantified through homophily, the extent to which alike individuals  
377 interact. Homophily can play a large role in the occurrence and behavior of tipping points in CHES models  
378 occurring on social networks, often having a detrimental effect on the environmental system. In a common-pool  
379 resource model with two distinct communities, increasing segregation by lowering the probability that agents in  
380 separate communities will have a link, softens the abruptness of a single detrimental tipping point compared to when  
381 the communities are well-mixed. This is due to the occurrence of multiple intermediate tipping points within each  
382 segregated community; however, increased segregation adds more hysteresis to the system increasing the difficulty  
383 of reversing this transition and returning to a sustainable state (Sugiarto et al., 2017b). In a public goods game  
384 modelling climate change mitigation, where humans are partitioned into rich and poor agents, a transition to group  
385 achievement of mitigation goals occurs at a lower perceived risk when there is no homophily and agents are  
386 influenced by others from both economic classes equally (Vasconcelos et al., 2014). Another human-climate model  
387 that included wealth inequality displayed an abrupt transition to lower peak temperature anomalies when homophily  
388 between economic classes approached zero (Menard et al., 2021).



**Figure 2: Mean proportion of nodes that are mitigators for network model (a) and ODE model (b).  $\phi$  is the rewiring probability and  $T$  is the time between social interactions.  $\phi_{c1}$  is the lower threshold and  $\phi_{c2}$  is the upper threshold, above which a fragmentation regime occurs. From (Wiedermann et al., 2015)**

389

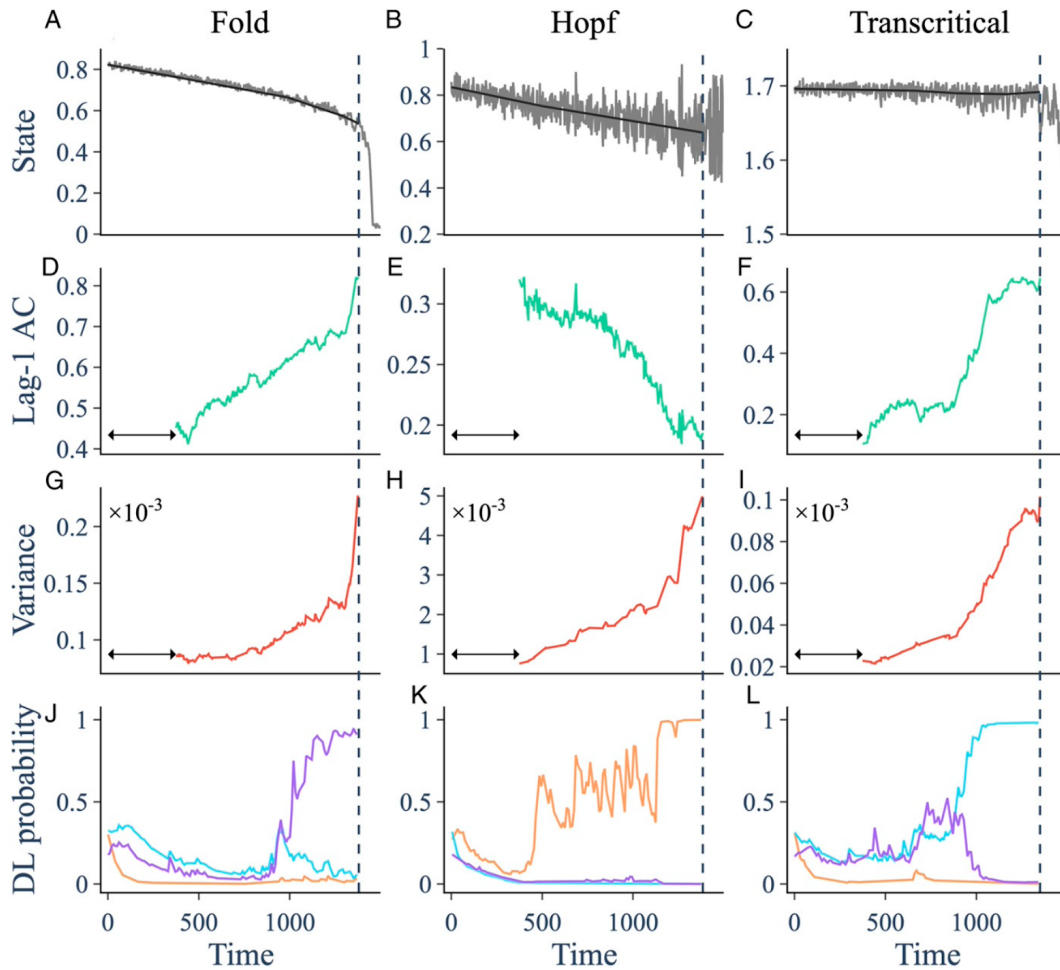
390 Social networks are rarely static and their ability to evolve over time is represented in adaptive network models  
 391 where agents can break existing social links and create new ones, a process called “rewiring”. Often this rewiring is  
 392 homophilic, meaning that agents are more likely to create a new social connection with others who share a similar  
 393 behavior. Common adaptive network CHES models have nodes representing a renewable resources stock with an  
 394 associated extraction level which can adopt a high extraction or low extraction level through imitating neighbors.  
 395 These models show that the level of homophilic rewiring can trigger regime shifts at both low and high levels,  
 396 where intermediate ranges correspond to a sustainable equilibrium. As agents can either choose to rewire or imitate  
 397 their neighbor, a low level of rewiring corresponds to a high speed of social interaction, which as discussed in  
 398 Section 2.5 can lead to detrimental tipping points. On the other hand, although high-rewiring leads to slower social  
 399 learning, it also brings about a fragmentation regime where social dynamics are dominated by homophily and the  
 400 network fragments into components based on strategy type, which makes widespread mitigation infeasible (Barfuss  
 401 et al., 2017; Geier et al., 2019; Wiedermann et al., 2015) (Figure 2). CHES models with social networks are still  
 402 relatively new and lack diversity in how they are formulated. For example, regarding the tipping points related to  
 403 rewiring social links, the lower threshold may be caused by increased social learning since in all models agents can  
 404 either rewire or imitate, but not both. There is still much to learn through isolating the effect of rewiring as well as  
 405 exploring a wide array of different model formulations of CHES on social networks.

### 406 3 Identifying early warning signals in the CHES

407 Although dynamical models can offer qualitative insight into potential trajectories of CHES resulting from specific  
408 interventions, it is more difficult to use them to generate precise and reliable predictions. Given the potential for  
409 severe environmental tipping points in the coming decades, it is extremely useful to be able to predict these abrupt  
410 shifts without complete mechanistic knowledge of the system. The ability to predict tipping points with limited data  
411 can allow policymakers to have more time preparing for future disasters, and given enough warning and political  
412 will, an opportunity to avoid them or mitigate their severity. Rapidly growing research in early warning signals  
413 (EWS) offers tools to monitor empirical time series data and warn of future tipping points that are likely to occur  
414 (Bury et al., 2021; Dakos et al., 2012, 2015, 2008; Kéfi et al., 2014; Lapeyrolerie and Boettiger, 2021). Although  
415 much of the work has been conducted on synthetic data, there are many studies that successfully predict historical  
416 tipping points in both empirical human and environmental time series data such as the 1987 Black Monday financial  
417 crash (Diks et al., 2019) as well as abrupt temperature shifts from paleoclimate datasets (Dakos et al., 2008).

### 418 **3.1 Recent advances for detecting early warning signals**

419 Much research has been done in the past few decades to develop tools for EWS using both empirical and synthetic  
420 time series data (Bury et al., 2021; Dakos et al., 2012, 2015, 2008; Kéfi et al., 2014; Lapeyrolerie and Boettiger,  
421 2021). Originally motivated by critical slowing down in bifurcation theory, where systems approaching a tipping  
422 point show a slower recovery to equilibrium under perturbations, generic EWS measure trends in this “slowing  
423 down” (Scheffer et al., 2009). The most commonly used methods compute the lag-1 autocorrelation and variance of  
424 the residuals from detrended time series data. Other widely used methods involve metrics such as skewness,  
425 measuring the asymmetry of fluctuations over time, and kurtosis, representing the likelihood of extreme values in  
426 the time series data. A phenomenon known as flickering occurs when there is sufficient noise to rapidly force the  
427 system between alternate stable states. In these cases, an increase in skewness and kurtosis is observed (Dakos et al.,  
428 2012). As lag-1 autocorrelation does not account for correlation beyond a single time step, power spectrum analysis  
429 has been used to look at changes in complete spectral properties, finding higher variations at low frequencies to  
430 commonly occur before a tipping point (Dakos et al., 2012; Scheffer et al., 2009). In spatial systems, many EWS are  
431 similar to those used in well-mixed systems, while also accounting for spatial variability. For example, Moran’s I is  
432 a spatial analog of lag-1 autocorrelation, which measures the correlation between neighboring nodes in a network  
433 (Kéfi et al., 2014).



**Figure 3: Generic EWS (second and third row) as well as deep learning EWS (bottom row) for time series generated by two ecological models exhibiting different types of bifurcations (top row); fold (left), Hopf (middle), and transcritical (right). As well as being more reliable, deep learning EWS can also distinguish between the type of bifurcation being approached. In the bottom row, the DL algorithm gives probabilities for the occurrence of fold (purple), Hopf (orange), or transcritical (blue) bifurcations. Image taken from (Bury et al., 2021).**

434 Numerous spatial ecological systems exhibit patterns in patchiness preceding a tipping point. For example, in  
 435 drylands, spotted vegetation patterns are hypothesised to be an EWS for the system approaching desertification  
 436 (Kéfi et al., 2014). Coupled human-epidemiological models also show that spatial properties in the distribution of  
 437 opinions on a social network offer potential EWS for the onset of disease outbreaks. Approaching this regime shift,  
 438 the number of anti-vaccine clusters increases, and very close to the transition point, these communities coalesce into  
 439 larger groups (Jentsch et al., 2018; Phillips et al., 2020). These clusters are quantified using a number of metrics,  
 440 such as an increase in modularity as well as the mean number, size, and maximum size of communities and  
 441 pro-vaccine echo chambers (Phillips and Bauch, 2021). This is also in agreement with previous work done in

442 percolation theory showing that phase transitions follow a breakup of connected components on the network  
443 (Newman, 2010).

444

445 One downside to the generic metrics discussed above is that they have the potential to fail in the presence of large  
446 amounts of noise where transitions can occur far from their analytically derived tipping point. A technique called  
447 dynamical network markers increases the dimensionality of the time series by transforming it from state variables to  
448 probability distributions of the mean and variance over a given window of time. This reduces the magnitude of noise  
449 in each dimension and in approaching a tipping point, one dominant group of variables will show a drastic increase  
450 in variance and correlation between other variables within that group. At the same time, the correlation between one  
451 variable in this dominant group and others outside the group will decrease. This technique has shown success with  
452 empirical data, such as predicting critical transitions in time series data for a eutrophic lake as well as the bankruptcy  
453 of Lehman Brothers (Liu et al., 2015), and flu outbreaks (Chen et al., 2019). Dynamical network markers have also  
454 been used on spatial systems such as those occurring on social networks through the use of hierarchical network  
455 representations. Here, networks are transformed into binary trees where leaves are the nodes from the original  
456 network and branches group nodes together at multiple resolutions. Through this hierarchical model, dynamical  
457 network markers use these multi-scale communities as the groups of variables that are analysed (Li et al., 2023).  
458 This spatial technique offers a novel method for predicting tipping points for CHES using human data occurring on  
459 complex social networks.

460

461 A very recent addition to the EWS toolkit uses concepts from statistical physics such as average flux, entropy  
462 production, generalised free energy, and time irreversibility to predict tipping points in a shallow lake model much  
463 earlier than generic methods such as autocorrelation and variance, showing promise for use in real-time monitoring  
464 (Xu et al., 2023). Additionally, the field of machine learning has motivated data-driven approaches to EWS which  
465 do not explicitly make use of any statistical metrics in the time series data. Instead, deep learning algorithms are  
466 trained on large synthetic datasets using models that have and have not approached tipping points. In the majority of  
467 cases, these algorithms have performed significantly better at predicting tipping points than generic EWS indicators  
468 when tested on empirical datasets that exhibit abrupt transitions (Bury et al., 2021; Deb et al., 2022) (Figure 3).  
469 Deep learning algorithms are also able to distinguish between different types of bifurcations as they are being  
470 approached which can offer vital information regarding the potential for catastrophic collapse in CHES.

### 471 **3.2 Social data for early warning signals**

472 In CHES models, the strength of EWS from environmental data has been shown to be muted compared to EWS  
473 from environmental systems not coupled to a human system (Bauch et al., 2016) or the same system with weak  
474 coupling between the human and environmental subsystems (Richter and Dakos, 2015). This is likely due to the  
475 effects of human behavior acting to mitigate variability in the environmental system, for example, rarity-motivated  
476 valuation creates a negative feedback loop where incentives to mitigate increase as the environment becomes further  
477 depleted, serving as a mechanism to avoid collapse. The muting of EWS provides a unique challenge for monitoring



478 tipping points in CHES using environmental data, especially as they occur more frequently in these coupled systems  
479 as discussed in Section 2. There are a small number of studies that have directly compared the strength and efficacy  
480 of EWS between various state or auxiliary variables in CHES models. In these studies, generic EWS from data in  
481 the human system were shown to be the only reliable indicators of the coupled system approaching a tipping point.  
482 Examples of human data used include the fraction of conservationists in a forest cover model (Bauch et al., 2016),  
483 average profits by resource harvesters and catch per unit effort common-pool resource models (Lade et al., 2013;  
484 Richter and Dakos, 2015). In agreement with generic methods, a state-of-the-art machine learning algorithm for  
485 EWS showed higher success in detecting tipping points generated from a coupled epidemiological model using  
486 pro-vaccine opinion in the human system compared to total infectious in the epidemiological system (Bury et al.,  
487 2021). It is possible that the state variable most sensitive to the forcing parameter may exhibit the strongest EWS, as  
488 seen in experimental work on tipping points in a lake food web. In this system, data from the species that had a  
489 direct trophic linkage to a driver of the tipping point (predators added to the food web) exhibited EWS earlier than  
490 those that were farther removed from the driver (Carpenter et al., 2014). If this is the case, human drivers of tipping  
491 points would most directly affect the human system, and EWS should still be stronger using social data.

492

493 The improved reliability of EWS from social data demonstrated through CHES models shows a significant promise  
494 for monitoring resilience in CHES through the analysis of socio-economic data. This confers a practical advantage  
495 as socio-economic data is often more frequently collected and readily available than environmental data (Hicks et  
496 al., 2016). Some examples of this are monitoring profits tied to resource extraction as well as using sentiment  
497 analysis on social media data, such as the number of tweets in a given area raising concern over the health of a  
498 coupled environmental system. Furthermore, citizen science not only generates environmental data but also provides  
499 social metadata through the participation of users who monitor specific areas. Leveraging existing platforms like  
500 CitSci.org, we can use this data to estimate trends in conservationist frequency over time (Wang et al., 2015). This  
501 approach allows for the implementation of real-time monitoring of environmental systems using data that is  
502 currently being generated, reducing the need for extensive knowledge or complex mechanistic models of the system.  
503 With the potential social data offers for use with EWS, it is important to note that much of the traditional social data,  
504 often conducted through national or regional surveys, do not provide fine-grained spatial or temporal resolution. On  
505 the other hand, novel methods that use social media data can solve the resolution issue, but may not accurately  
506 represent the population it is being used to model (Hargittai, 2020). These challenges may be addressed through a  
507 hybrid approach that uses hybrid time series generated from multiple types and sources of social data (Rosales  
508 Sánchez et al., 2017).

## 509 **4 Conclusion and future directions**

### 510 **4.1 Summary of main points**

511

512 From a wide range of examined theoretical models, we are able to gain insight into human drivers that lead to  
513 tipping points in CHES systems. Many social interventions, such as reducing mitigation costs and extractive effort,  
514 or increasing the time horizon in decision-making, lead to beneficial tipping points, regardless of the system  
515 modelled. The beneficial effect of these interventions is intuitive, however, non-linear responses manifested as  
516 tipping points may not be as evident. Mitigation costs can be reduced through subsidies for land preservation and  
517 green technology, and extraction effort through limits on land development and the expansion of protected natural  
518 areas (i.e. the Haudenosaunee-led protection of the Haldimand Tract) (Forester, 2021), and by increasing time  
519 horizons through passing long-term legislation that centers the well-being of human and environmental systems such  
520 as the Green New Deal (Galvin and Healy, 2020). These policy interventions become more difficult to implement at  
521 large scales, and models that are tailored to global coordination problems can give us insight into how institutions  
522 can work together to rapidly mitigate looming threats, such as the current climate crises we are facing (Karatayev et  
523 al., 2021).

524

525 Other human behaviors and social processes are much more nuanced and system-specific in how they affect tipping  
526 points. For example, models show that rarity-motivated valuation can act to detrimentally tip the environmental  
527 system into a depleted state when it crosses both an upper and (counterintuitively) a lower threshold value. This was  
528 illustrated most clearly in the example of forest cover in the paper by Bauch et al. (2016). Social norms, especially  
529 when majority-enforcing, increase the likelihood of tipping points through the emergence of bistable regimes that  
530 are made up of both sustainable and unsustainable environmental equilibria. The extent of coupling between the  
531 human and environmental system as well as the speed of social change relative to environmental change can have  
532 different effects depending on whether the model is input- or output-limited. Interventions related to human  
533 valuation and social norms are much more difficult to implement as they require a deeper mechanistic understanding  
534 of how to influence social dynamics and may also have ethical considerations.

535

536 The models we reviewed also show that greater structural complexity via the number and diversity of human traits  
537 as well as the number of social connections can increase the potential for tipping points and mask social dynamics  
538 making these transitions much harder to predict. The modelling literature has only explored a small sliver of the  
539 space of possible choices regarding assumed social structure and the types of environmental models coupled to  
540 them. For example, the vast majority of models only allow for a binary choice in human behavior and adaptive  
541 social networks have only recently been incorporated, with limited mechanisms of re-wiring and types of coupled  
542 environmental systems. Consequently, we still have much to learn on how shifting underlying social structures acts  
543 as a driver of tipping points. This is especially true in output-limited models which are important to improving our  
544 understanding of how our social structures affect pressing global issues such as pollution and climate change. Even  
545 if we include more diverse and realistic social structures and processes, CHES are composed of many non-linear  
546 feedbacks and contain high levels of uncertainty, and the reality is that we may not be able to have a complete  
547 mechanistic representation through models. EWS from empirical data show great potential in predicting tipping  
548 points without requiring a full understanding of the system being monitored. There have been many advances in

549 using state-of-the-art machine learning algorithms to provide accurate EWS from 1-D time series (Bury et al., 2021;  
550 Deb et al., 2022), and very recent work is now developing similar techniques to predict tipping points from spatial  
551 data (Dylewsky et al., 2022). As synthetic data from models have shown the value of EWS from social data, it is  
552 likely that applying these techniques to diverse and hybrid empirical social datasets can vastly improve our ability to  
553 predict tipping points caused by human drivers in the future.

#### 554 **4.2 Future work in CHES modelling**

555 There are many social phenomena that are not commonly included in CHES models, yet may be important in  
556 furthering our understanding of tipping points within these systems. We know that inequality in human systems  
557 plays a large role in individuals' risk perception and ability to engage in pro-environmental behavior (Gibson-Wood  
558 and Wakefield, 2013; Pearson et al., 2017; Quimby and Angelique, 2011; Rajapaksa et al., 2018) and have  
559 mentioned two CHES models that incorporate wealth inequality in a human-climate system (Menard et al., 2021;  
560 Vasconcelos et al., 2014). However, more studies explicitly investigating the role of inequality could offer some  
561 valuable insight into interventions that can be more effective in benefiting both the environment and the most  
562 vulnerable in human systems. This could be complemented by social biases where perceptions of risk are linked to  
563 an individual's socio-economic status, and detrimental environmental outcomes are experienced disproportionately by  
564 vulnerable communities as is commonly observed globally (Banzhaf et al., 2019; Boyce, 2007). Future models could  
565 allow for alternatives to the common modelling assumption where individuals act in their own self-interest, for  
566 example by incorporating other-regarding preferences into utility functions so that individuals value their neighbors'  
567 well-being along with their own (Dimick et al., 2018). These models could also look at grassroots redistribution of  
568 wealth allowing us to explore the effects of alternative social value systems on the environment (Tilman et al.,  
569 2018).

570

571 Stochasticity (noise), especially regarding drivers of tipping points can significantly affect system dynamics  
572 including when tipping points occur. Although many CHES models are deterministic, recent work has shown that  
573 increasing noise can lead to earlier tipping (Willcock et al., 2023), or in other cases, increase the duration of time the  
574 environmental system can persist before becoming extinct (Jnawali et al., 2022). These contradictory results warrant  
575 further work in understanding how different types of noise and their magnitude within drivers of tipping points  
576 affect the resilience of these systems. With stochasticity comes uncertainty, and in real-world systems, it is  
577 impossible to know with precision the extent of social change required to bring about a beneficial or avoid a  
578 detrimental tipping point. This uncertainty around our knowledge of system thresholds adds an additional challenge  
579 in both agreeing upon and following through with policy that promotes sustainable futures while taking into account  
580 potential tipping points. Experimental games have shown that high threshold uncertainty can promote the collapse of  
581 a shared resource, often through an increase in free-riding behavior (Barrett and Dannenberg, 2014, 2012). On the  
582 other hand, field experiments in fishing communities have shown that high uncertainty can promote cooperation and  
583 sustainable resource use (Finkbeiner et al., 2018; Rocha et al., 2020). Theoretical models show that increased  
584 uncertainty can lead to increased mitigative behavior if the shared resource is highly valued, however for low-valued

585 resources, increased uncertainty can deter mitigation, putting the persistence of the shared resource at risk (Jager et  
586 al., 2000; McBride, 2006). Uncertainty around thresholds is unavoidable, further motivating the need to offer  
587 additional incentives for mitigative action on institutional scales, rather than solely the threat of environmental  
588 collapse. In systems where uncertainty can promote mitigative action, increased communication and awareness  
589 campaigns around this threshold uncertainty could be useful to incorporate into policy.

590

591 This review has focused primarily on the effects of single drivers, however research on multiple co-occurring human  
592 drivers of tipping points, while more analytically challenging, could offer a holistic understanding of how these  
593 drivers interact. A recent study has shown that multiple drivers can both reduce the time until tipping or lead to a  
594 tipping point that would not occur with a single driver (Willcock et al., 2023) and there is already a large body of  
595 empirical work exploring the diversity of these drivers which can be used to inform future CHES models  
596 (Jaureguiberry et al., 2022; Maciejewski et al., 2019; Millennium Ecosystem Assessment, 2005). Finally, as the  
597 majority of the studies in modelling tipping points have focused on slow gradual changes in the driver, fast changes  
598 require further research as they can exhibit very different tipping behavior (Ashwin et al., 2012). CHES models  
599 ubiquitously exemplify the phenomenon of tipping points, which often occur through drivers in the human system.  
600 Although these models offer valuable insight in understanding key feedbacks and qualitative behavior, their  
601 predictive power is limited. Additionally, as many model findings can depend on the type of system modelled as  
602 well as assumptions in the model formulation, translating this work into policy remains a significant challenge.  
603 However, further work in both diversifying model systems and assumptions paired with research in universal  
604 real-time indicators of EWS shows considerable promise in both improving our understanding and predicting human  
605 drivers of tipping points in the environment.

606

607 **Author contribution.** I.F.: visualization, writing—original draft, writing—review and editing; C.T.B.: visualization,  
608 writing—original draft, writing—review and editing; M.A.: conceptualization, funding acquisition, supervision,  
609 visualization, writing—original draft, writing—review and editing.

610

611 **Competing interests.** The authors declare that they have no conflict of interest

612

613 **Funding.** This research was supported by the Natural Sciences and Engineering Council of Canada (Discovery  
614 grants to both M.A and C.T.B), the Canada First Research Excellence Fund (to M.A.) and in part by the  
615 International Centre for Theoretical Sciences (ICTS) for the program "Tipping Points in Complex Systems " (code:  
616 ICTS/tipc2022/9) in which M.A. and C.T.B. participated.

## 617 References

- 618 Ali, Q., Bauch, C. T., and Anand, M.: Coupled Human-Environment Dynamics of Forest Pest Spread and Control in  
619 a Multi-Patch, Stochastic Setting, *PLOS ONE*, 10, e0139353,  
620 <https://doi.org/10.1371/journal.pone.0139353>, 2015.
- 621 Andersen, S. O., Halberstadt, M. L., and Borgford-Parnell, N.: Stratospheric ozone, global warming, and the  
622 principle of unintended consequences—An ongoing science and policy success story, *J. Air Waste Manag.*  
623 *Assoc.*, 63, 607–647, <https://doi.org/10.1080/10962247.2013.791349>, 2013.
- 624 Appiah-Opoku, S.: Indigenous Beliefs and Environmental Stewardship: A Rural Ghana Experience, *J. Cult. Geogr.*,  
625 24, 79–98, <https://doi.org/10.1080/08873630709478212>, 2007.
- 626 Ashwin, P., Wieczorek, S., Vitolo, R., and Cox, P.: Tipping points in open systems: bifurcation, noise-induced and  
627 rate-dependent examples in the climate system, *Philos. Trans. R. Soc. Math. Phys. Eng. Sci.*, 370,  
628 1166–1184, <https://doi.org/10.1098/rsta.2011.0306>, 2012.
- 629 Banzhaf, S., Ma, L., and Timmins, C.: Environmental Justice: The Economics of Race, Place, and Pollution, *J. Econ.*  
630 *Perspect.*, 33, 185–208, <https://doi.org/10.1257/jep.33.1.185>, 2019.
- 631 Barfuss, W., Donges, J. F., Wiedermann, M., and Lucht, W.: Sustainable use of renewable resources in a stylized  
632 social–ecological network model under heterogeneous resource distribution, *Earth Syst. Dyn.*, 8, 255–264,  
633 <https://doi.org/10.5194/esd-8-255-2017>, 2017.
- 634 Barfuss, W., Donges, J. F., Vasconcelos, V. V., Kurths, J., and Levin, S. A.: Caring for the future can turn tragedy  
635 into comedy for long-term collective action under risk of collapse, *Proc. Natl. Acad. Sci.*, 117,  
636 12915–12922, <https://doi.org/10.1073/pnas.1916545117>, 2020.
- 637 Barlow, L.-A., Cecile, J., Bauch, C. T., and Anand, M.: Modelling Interactions between Forest Pest Invasions and  
638 Human Decisions Regarding Firewood Transport Restrictions, *PLoS ONE*, 9, e90511,  
639 <https://doi.org/10.1371/journal.pone.0090511>, 2014.
- 640 Barrett, S. and Dannenberg, A.: Climate negotiations under scientific uncertainty, *Proc. Natl. Acad. Sci.*, 109,  
641 17372–17376, <https://doi.org/10.1073/pnas.1208417109>, 2012.
- 642 Barrett, S. and Dannenberg, A.: Sensitivity of collective action to uncertainty about climate tipping points, *Nat.*  
643 *Clim. Change*, 4, 36–39, <https://doi.org/10.1038/nclimate2059>, 2014.
- 644 Bauch, C. T., Sigdel, R., Pharaon, J., and Anand, M.: Early warning signals of regime shifts in coupled  
645 human–environment systems, *Proc. Natl. Acad. Sci.*, 113, 14560–14567,  
646 <https://doi.org/10.1073/pnas.1604978113>, 2016.
- 647 Bavikatte, K. S. and Bennett, T.: Community stewardship: the foundation of biocultural rights, *J. Hum. Rights*  
648 *Environ.*, 6, 7–29, <https://doi.org/10.4337/jhre.2015.01.01>, 2015.
- 649 Beckford, C. L., Jacobs, C., Williams, N., and Nahdee, R.: Aboriginal Environmental Wisdom, Stewardship, and  
650 Sustainability: Lessons From the Walpole Island First Nations, Ontario, Canada, *J. Environ. Educ.*, 41,  
651 239–248, <https://doi.org/10.1080/00958961003676314>, 2010.
- 652 Bengochea Paz, D., Henderson, K., and Loreau, M.: Habitat percolation transition undermines sustainability in

653 social-ecological agricultural systems, *Ecol. Lett.*, 25, 163–176, <https://doi.org/10.1111/ele.13914>, 2022.

654 Binford, M. W., Brenner, M., Whitmore, T. J., Higuera-Gundy, A., Deevey, E. S., and Leyden, B.: Ecosystems,  
655 paleoecology and human disturbance in subtropical and tropical America, *Quat. Sci. Rev.*, 6, 115–128,  
656 1987.

657 Bosch, C. A.: Redwoods: A Population Model: Matrix methods may be used to model the growth, survival, and  
658 harvesting of California redwoods., *Science*, 172, 345–349, <https://doi.org/10.1126/science.172.3981.345>,  
659 1971.

660 Boyce, J. K.: *Inequality and Environmental Protection*, 2007.

661 Brovkin, V., Claussen, M., Petoukhov, V., and Ganopolski, A.: On the stability of the atmosphere-vegetation system  
662 in the Sahara/Sahel region, *J. Geophys. Res. Atmospheres*, 103, 31613–31624,  
663 <https://doi.org/10.1029/1998JD200006>, 1998.

664 Bury, T. M., Bauch, C. T., and Anand, M.: Charting pathways to climate change mitigation in a coupled  
665 socio-climate model, *PLOS Comput. Biol.*, 15, e1007000, <https://doi.org/10.1371/journal.pcbi.1007000>,  
666 2019.

667 Bury, T. M., Sujith, R. I., Pavithran, I., Scheffer, M., Lenton, T. M., Anand, M., and Bauch, C. T.: Deep learning for  
668 early warning signals of tipping points, *Proc. Natl. Acad. Sci.*, 118, e2106140118,  
669 <https://doi.org/10.1073/pnas.2106140118>, 2021.

670 Carpenter, S. R., Mooney, H. A., Agard, J., Capistrano, D., DeFries, R. S., Díaz, S., Dietz, T., Duraiappah, A. K.,  
671 Oteng-Yeboah, A., Pereira, H. M., Perrings, C., Reid, W. V., Sarukhan, J., Scholes, R. J., and Whyte, A.:  
672 Science for managing ecosystem services: Beyond the Millennium Ecosystem Assessment, *Proc. Natl.*  
673 *Acad. Sci.*, 106, 1305–1312, <https://doi.org/10.1073/pnas.0808772106>, 2009.

674 Carpenter, S. R., Brock, W. A., Cole, J. J., and Pace, M. L.: A new approach for rapid detection of nearby thresholds  
675 in ecosystem time series, *Oikos*, 123, 290–297, <https://doi.org/10.1111/j.1600-0706.2013.00539.x>, 2014.

676 Chaudhuri, K.: A bioeconomic model of harvesting a multispecies fishery, *Ecol. Model.*, 32, 267–279,  
677 [https://doi.org/10.1016/0304-3800\(86\)90091-8](https://doi.org/10.1016/0304-3800(86)90091-8), 1986.

678 Chen, P., Chen, E., Chen, L., Zhou, X. J., and Liu, R.: Detecting early-warning signals of influenza outbreak based  
679 on dynamic network marker, *J. Cell. Mol. Med.*, 23, 395–404, <https://doi.org/10.1111/jcmm.13943>, 2019.

680 Chen, X. and Szolnoki, A.: Punishment and inspection for governing the commons in a feedback-evolving game,  
681 *PLOS Comput. Biol.*, 14, e1006347, <https://doi.org/10.1371/journal.pcbi.1006347>, 2018.

682 Chung, A. and Rimal, R. N.: Social norms: A review, *Rev. Commun. Res.*, 4, 1–28,  
683 <https://doi.org/10.12840/issn.2255-4165.2016.04.01.008>, 2016.

684 Cook, E.: Global Environmental Advocacy: Citizen Activism in Protecting the Ozone Layer, *Ambio*, 334–338,  
685 1990.

686 Crawford, J. D.: Introduction to bifurcation theory, *Rev. Mod. Phys.*, 63, 991–1037,  
687 <https://doi.org/10.1103/RevModPhys.63.991>, 1991.

688 Dakos, V., Scheffer, M., van Nes, E. H., Brovkin, V., Petoukhov, V., and Held, H.: Slowing down as an early  
689 warning signal for abrupt climate change, 2008.

690 Dakos, V., Carpenter, S. R., Brock, W. A., Ellison, A. M., Guttal, V., Ives, A. R., Kéfi, S., Livina, V., Seekell, D. A.,  
691 van Nes, E. H., and Scheffer, M.: Methods for Detecting Early Warnings of Critical Transitions in Time  
692 Series Illustrated Using Simulated Ecological Data, *PLoS ONE*, 7, e41010,  
693 <https://doi.org/10.1371/journal.pone.0041010>, 2012.

694 Dakos, V., Carpenter, S. R., van Nes, E. H., and Scheffer, M.: Resilience indicators: prospects and limitations for  
695 early warnings of regime shifts, *Philos. Trans. R. Soc. B Biol. Sci.*, 370, 20130263,  
696 <https://doi.org/10.1098/rstb.2013.0263>, 2015.

697 Dakos, V., Matthews, B., Hendry, A. P., Levine, J., Loeuille, N., Norberg, J., Nosil, P., Scheffer, M., and De Meester,  
698 L.: Ecosystem tipping points in an evolving world, *Nat. Ecol. Evol.*, 3, 355–362,  
699 <https://doi.org/10.1038/s41559-019-0797-2>, 2019.

700 Deb, S., Sidheekh, S., Clements, C. F., Krishnan, N. C., and Dutta, P. S.: Machine learning methods trained on  
701 simple models can predict critical transitions in complex natural systems, 2022.

702 Diks, C., Hommes, C., and Wang, J.: Critical slowing down as an early warning signal for financial crises?, *Empir.*  
703 *Econ.*, 57, 1201–1228, <https://doi.org/10.1007/s00181-018-1527-3>, 2019.

704 Dimick, M., Rueda, D., and Stegmüller, D.: Models of Other-Regarding Preferences, Inequality, and Redistribution,  
705 *Annu. Rev. Polit. Sci.*, 21, 441–460, <https://doi.org/10.1146/annurev-polisci-091515-030034>, 2018.

706 Dockstader, Z., Bauch, C., and Anand, M.: Interconnections Accelerate Collapse in a Socio-Ecological  
707 Metapopulation, *Sustainability*, 11, 1852, <https://doi.org/10.3390/su11071852>, 2019.

708 Drechsler, M. and Surun, C.: Land-use and species tipping points in a coupled ecological-economic model, *Ecol.*  
709 *Complex.*, 36, 86–91, <https://doi.org/10.1016/j.ecocom.2018.06.004>, 2018.

710 Dunlap, T.: DDT: scientists, citizens, and public policy, Princeton University Press, 2014.

711 Dylewsky, D., Lenton, T. M., Scheffer, M., Bury, T. M., Fletcher, C. G., Anand, M., and Bauch, C. T.: Universal  
712 Early Warning Signals of Phase Transitions in Climate Systems,  
713 <https://doi.org/10.48550/ARXIV.2206.00060>, 2022.

714 Epstein, G., Pérez, I., Schoon, M., and Meek, C. L.: Governing the invisible commons: Ozone regulation and the  
715 Montreal Protocol, *Int. J. Commons*, 8, 337, <https://doi.org/10.18352/ijc.407>, 2014.

716 Farahbakhsh, I., Bauch, C. T., and Anand, M.: Best response dynamics improve sustainability and equity outcomes  
717 in common-pool resources problems, compared to imitation dynamics, *J. Theor. Biol.*, 509, 110476,  
718 <https://doi.org/10.1016/j.jtbi.2020.110476>, 2021.

719 Farahbakhsh, I., Bauch, C. T., and Anand, M.: Modelling coupled human–environment complexity for the future of  
720 the biosphere: strengths, gaps and promising directions, *Philos. Trans. R. Soc. B Biol. Sci.*, 377, 20210382,  
721 <https://doi.org/10.1098/rstb.2021.0382>, 2022.

722 Figueiredo, J. and Pereira, H. M.: Regime shifts in a socio-ecological model of farmland abandonment, *Landsc.*  
723 *Ecol.*, 26, 737–749, <https://doi.org/10.1007/s10980-011-9605-3>, 2011.

724 Finkbeiner, E. M., Micheli, F., Saenz-Arroyo, A., Vazquez-Vera, L., Perafan, C. A., and Cárdenas, J. C.: Local  
725 response to global uncertainty: Insights from experimental economics in small-scale fisheries, *Glob.*  
726 *Environ. Change*, 48, 151–157, <https://doi.org/10.1016/j.gloenvcha.2017.11.010>, 2018.

727 Folke, C.: Resilience: The emergence of a perspective for social–ecological systems analyses, *Glob. Environ.*  
728 *Change*, 16, 253–267, <https://doi.org/10.1016/j.gloenvcha.2006.04.002>, 2006.

729 Forester, B.: Haudenosaunee chiefs declare development moratorium across entire Haldimand Tract, *APTN News*,  
730 2021.

731 Galvin, R. and Healy, N.: The Green New Deal in the United States: What it is and how to pay for it, *Energy Res.*  
732 *Soc. Sci.*, 67, 101529, <https://doi.org/10.1016/j.erss.2020.101529>, 2020.

733 Geier, F., Barfuss, W., Wiedermann, M., Kurths, J., and Donges, J. F.: The physics of governance networks: critical  
734 transitions in contagion dynamics on multilayer adaptive networks with application to the sustainable use  
735 of renewable resources, *Eur. Phys. J. Spec. Top.*, 228, 2357–2369,  
736 <https://doi.org/10.1140/epjst/e2019-900120-4>, 2019.

737 Getz, W. M.: The ultimate-sustainable-yield problem in nonlinear age-structured populations, *Math. Biosci.*, 48,  
738 279–292, [https://doi.org/10.1016/0025-5564\(80\)90062-0](https://doi.org/10.1016/0025-5564(80)90062-0), 1980.

739 Ghil, M. and Tavantzis, J.: Global Hopf Bifurcation in a Simple Climate Model, 1983.

740 Gibson-Wood, H. and Wakefield, S.: “Participation”, White Privilege and Environmental Justice: Understanding  
741 Environmentalism Among Hispanics in Toronto, *Antipode*, 45, 641–662,  
742 <https://doi.org/10.1111/j.1467-8330.2012.01019.x>, 2013.

743 Grêt-Regamey, A., Huber, S. H., and Huber, R.: Actors’ diversity and the resilience of social-ecological systems to  
744 global change, *Nat. Sustain.*, 2, 290–297, <https://doi.org/10.1038/s41893-019-0236-z>, 2019.

745 Grier, J. W.: Ban of DDT and Subsequent Recovery of Reproduction in Bald Eagles, *Science*, 218, 1232–1235,  
746 <https://doi.org/10.1126/science.7146905>, 1982.

747 Hargittai, E.: Potential Biases in Big Data: Omitted Voices on Social Media, *Soc. Sci. Comput. Rev.*, 38, 10–24,  
748 <https://doi.org/10.1177/0894439318788322>, 2020.

749 Hauert, C., Saade, C., and McAvoy, A.: Asymmetric evolutionary games with environmental feedback, *J. Theor.*  
750 *Biol.*, 462, 347–360, <https://doi.org/10.1016/j.jtbi.2018.11.019>, 2019.

751 Henderson, K. A., Bauch, C. T., and Anand, M.: Alternative stable states and the sustainability of forests, grasslands,  
752 and agriculture, *Proc. Natl. Acad. Sci.*, 113, 14552–14559, <https://doi.org/10.1073/pnas.1604987113>, 2016.

753 Hicks, C. C., Crowder, L. B., Graham, N. A., Kittinger, J. N., and Cornu, E. L.: Social drivers forewarn of marine  
754 regime shifts, *Front. Ecol. Environ.*, 14, 252–260, <https://doi.org/10.1002/fee.1284>, 2016.

755 Hofbauer, J. and Sigmund, K.: *Evolutionary Games and Population Dynamics*, 1st ed., Cambridge University Press,  
756 <https://doi.org/10.1017/CBO9781139173179>, 1998.

757 Holstein, T., Wiedermann, M., and Kurths, J.: Optimization of coupling and global collapse in diffusively coupled  
758 socio-ecological resource exploitation networks, *New J. Phys.*, 23, 033027,  
759 <https://doi.org/10.1088/1367-2630/abe0db>, 2021.

760 Hopcroft, P. O. and Valdes, P. J.: Paleoclimate-conditioning reveals a North Africa land–atmosphere tipping point,  
761 *Proc. Natl. Acad. Sci.*, 118, e2108783118, <https://doi.org/10.1073/pnas.2108783118>, 2021.

762 Innes, C., Anand, M., and Bauch, C. T.: The impact of human-environment interactions on the stability of  
763 forest-grassland mosaic ecosystems, *Sci. Rep.*, 3, 2689, <https://doi.org/10.1038/srep02689>, 2013.



764 Iwasa, Y., Uchida, T., and Yokomizo, H.: Nonlinear behavior of the socio-economic dynamics for lake  
765 eutrophication control, *Ecol. Econ.*, 63, 219–229, <https://doi.org/10.1016/j.ecolecon.2006.11.003>, 2007.

766 Iwasa, Y., Suzuki-Ohno, Y., and Yokomizo, H.: Paradox of nutrient removal in coupled socioeconomic and  
767 ecological dynamics for lake water pollution, *Theor. Ecol.*, 3, 113–122,  
768 <https://doi.org/10.1007/s12080-009-0061-5>, 2010.

769 Jager, W., Janssen, M. A., De Vries, H. J. M., De Greef, J., and Vlek, C. A. J.: Behaviour in commons dilemmas:  
770 Homo economicus and Homo psychologicus in an ecological-economic model, *Ecol. Econ.*, 35, 357–379,  
771 [https://doi.org/10.1016/S0921-8009\(00\)00220-2](https://doi.org/10.1016/S0921-8009(00)00220-2), 2000.

772 Jaureguiberry, P., Titeux, N., Wiemers, M., Bowler, D. E., Coscieme, L., Golden, A. S., Guerra, C. A., Jacob, U.,  
773 Takahashi, Y., Settele, J., Díaz, S., Molnár, Z., and Purvis, A.: The direct drivers of recent global  
774 anthropogenic biodiversity loss, *Sci. Adv.*, 8, eabm9982, <https://doi.org/10.1126/sciadv.abm9982>, 2022.

775 Jentsch, P. C., Anand, M., and Bauch, C. T.: Spatial correlation as an early warning signal of regime shifts in a  
776 multiplex disease-behaviour network, *J. Theor. Biol.*, 448, 17–25,  
777 <https://doi.org/10.1016/j.jtbi.2018.03.032>, 2018.

778 Jnawali, K., Anand, M., and Bauch, C. T.: Stochasticity-induced persistence in coupled social-ecological systems, *J.*  
779 *Theor. Biol.*, 542, 111088, <https://doi.org/10.1016/j.jtbi.2022.111088>, 2022.

780 Karatayev, V. A., Vasconcelos, V. V., Lafuite, A.-S., Levin, S. A., Bauch, C. T., and Anand, M.: A well-timed shift  
781 from local to global agreements accelerates climate change mitigation, *Nat. Commun.*, 12, 2908,  
782 <https://doi.org/10.1038/s41467-021-23056-5>, 2021.

783 Kéfi, S., Guttal, V., Brock, W. A., Carpenter, S. R., Ellison, A. M., Livina, V. N., Seekell, D. A., Scheffer, M., Van  
784 Nes, E. H., and Dakos, V.: Early Warning Signals of Ecological Transitions: Methods for Spatial Patterns,  
785 *PLoS ONE*, 9, e92097, <https://doi.org/10.1371/journal.pone.0092097>, 2014.

786 Lade, S. J., Tavoni, A., Levin, S. A., and Schlüter, M.: Regime shifts in a social-ecological system, *Theor. Ecol.*, 6,  
787 359–372, <https://doi.org/10.1007/s12080-013-0187-3>, 2013.

788 Lafuite, A.-S., de Mazancourt, C., and Loreau, M.: Delayed behavioural shifts undermine the sustainability of  
789 social–ecological systems, *Proc. R. Soc. B Biol. Sci.*, 284, 20171192,  
790 <https://doi.org/10.1098/rspb.2017.1192>, 2017.

791 Lapeyrolerie, M. and Boettiger, C.: Teaching machines to anticipate catastrophes, *Proc. Natl. Acad. Sci.*, 118,  
792 e2115605118, <https://doi.org/10.1073/pnas.2115605118>, 2021.

793 Latkin, C. A., Dayton, L., Moran, M., Strickland, J. C., and Collins, K.: Behavioral and psychosocial factors  
794 associated with COVID-19 skepticism in the United States, *Curr. Psychol.*, 41, 7918–7926,  
795 <https://doi.org/10.1007/s12144-020-01211-3>, 2022.

796 Lenton, T. M.: Environmental Tipping Points, *Annu. Rev. Environ. Resour.*, 38, 1–29,  
797 <https://doi.org/10.1146/annurev-environ-102511-084654>, 2013.

798 Lenton, T. M.: Tipping positive change, *Philos. Trans. R. Soc. B Biol. Sci.*, 375, 20190123,  
799 <https://doi.org/10.1098/rstb.2019.0123>, 2020.

800 Lenton, T. M., Held, H., Kriegler, E., Hall, J. W., Lucht, W., Rahmstorf, S., and Schellnhuber, H. J.: Tipping

801 elements in the Earth's climate system, *Proc. Natl. Acad. Sci.*, 105, 1786–1793,  
802 <https://doi.org/10.1073/pnas.0705414105>, 2008.

803 Lenton, T. M., Benson, S., Smith, T., Ewer, T., Lanel, V., Petykowski, E., Powell, T. W. R., Abrams, J. F., Blomsma,  
804 F., and Sharpe, S.: Operationalising positive tipping points towards global sustainability, *Glob. Sustain.*, 5,  
805 e1, <https://doi.org/10.1017/sus.2021.30>, 2022.

806 Li, H., Li, X., Zhang, X., Zhao, C., and Wang, Z.: Detecting early-warning signals for social emergencies by  
807 temporal network sociomarkers, *Inf. Sci.*, 627, 189–204, <https://doi.org/10.1016/j.ins.2023.01.076>, 2023.

808 Lin, Y.-H. and Weitz, J. S.: Spatial Interactions and Oscillatory Tragedies of the Commons, *Phys. Rev. Lett.*, 122,  
809 148102, <https://doi.org/10.1103/PhysRevLett.122.148102>, 2019.

810 Lindkvist, E., Ekeberg, Ö., and Norberg, J.: Strategies for sustainable management of renewable resources during  
811 environmental change, *Proc. R. Soc. B Biol. Sci.*, 284, 20162762, <https://doi.org/10.1098/rspb.2016.2762>,  
812 2017.

813 Liu, R., Chen, P., Aihara, K., and Chen, L.: Identifying early-warning signals of critical transitions with strong noise  
814 by dynamical network markers, *Sci. Rep.*, 5, 17501, <https://doi.org/10.1038/srep17501>, 2015.

815 Maciejewski, K., Biggs, R., and Rocha, J. C.: Regime shifts in social-ecological systems, in: *Handbook on*  
816 *Resilience of Socio-Technical Systems*, edited by: Ruth, M. and Goessling-Reisemann, S., Edward Elgar  
817 Publishing, <https://doi.org/10.4337/9781786439376.00021>, 2019.

818 Mather, A. S. and Fairbairn, J.: From Floods to Reforestation: The Forest Transition in Switzerland, *Environ. Hist.*,  
819 6, 399–421, <https://doi.org/10.3197/096734000129342352>, 2000.

820 Mathias, J.-D., Anderies, J. M., Baggio, J., Hodbod, J., Huet, S., Janssen, M. A., Milkoreit, M., and Schoon, M.:  
821 Exploring non-linear transition pathways in social-ecological systems, *Sci. Rep.*, 10, 4136,  
822 <https://doi.org/10.1038/s41598-020-59713-w>, 2020.

823 May, R. M.: Thresholds and breakpoints in ecosystems with a multiplicity of stable states, *Nature*, 269, 471–477,  
824 <https://doi.org/10.1038/269471a0>, 1977.

825 May, R. M. and Oster, G. F.: Bifurcations and Dynamic Complexity in Simple Ecological Models, *Am. Nat.*, 110,  
826 573–599, <https://doi.org/10.1086/283092>, 1976.

827 McBride, M.: Discrete public goods under threshold uncertainty, *J. Public Econ.*, 90, 1181–1199,  
828 <https://doi.org/10.1016/j.jpubeco.2005.09.012>, 2006.

829 McMillan, L. J. and Prosper, K.: Remobilizing netukulimk: indigenous cultural and spiritual connections with  
830 resource stewardship and fisheries management in Atlantic Canada, *Rev. Fish Biol. Fish.*, 26, 629–647,  
831 <https://doi.org/10.1007/s11160-016-9433-2>, 2016.

832 Menard, J., Bury, T. M., Bauch, C. T., and Anand, M.: When conflicts get heated, so does the planet: coupled  
833 social-climate dynamics under inequality, *Proc. R. Soc. B Biol. Sci.*, 288, 20211357,  
834 <https://doi.org/10.1098/rspb.2021.1357>, 2021.

835 Milkoreit, M., Hodbod, J., Baggio, J., Benessaiah, K., Calderón-Contreras, R., Donges, J. F., Mathias, J.-D., Rocha,  
836 J. C., Schoon, M., and Werners, S. E.: Defining tipping points for social-ecological systems  
837 scholarship—an interdisciplinary literature review, *Environ. Res. Lett.*, 13, 033005,

838 <https://doi.org/10.1088/1748-9326/aaaa75>, 2018.

839 Millennium Ecosystem Assessment: Ecosystems and Human Well-being: Synthesis, Island Press, Washington, DC,  
840 2005.

841 Milne, R., Bauch, C., and Anand, M.: Local overfishing patterns have regional effects on health of coral, and  
842 economic transitions can promote its recovery, 2021.

843 Moore, F. C., Lacasse, K., Mach, K. J., Shin, Y. A., Gross, L. J., and Beckage, B.: Determinants of emissions  
844 pathways in the coupled climate–social system, *Nature*, 603, 103–111,  
845 <https://doi.org/10.1038/s41586-022-04423-8>, 2022.

846 Motesharrei, S., Rivas, J., and Kalnay, E.: Human and nature dynamics (HANDY): Modeling inequality and use of  
847 resources in the collapse or sustainability of societies, *Ecol. Econ.*, 101, 90–102,  
848 <https://doi.org/10.1016/j.ecolecon.2014.02.014>, 2014.

849 Müller, P. M., Heitzig, J., Kurths, J., Lüdge, K., and Wiedermann, M.: Anticipation-induced social tipping: can the  
850 environment be stabilised by social dynamics?, *Eur. Phys. J. Spec. Top.*, 230, 3189–3199,  
851 <https://doi.org/10.1140/epjs/s11734-021-00011-5>, 2021.

852 Muneeppeerakul, R. and Anderies, J. M.: The emergence and resilience of self-organized governance in coupled  
853 infrastructure systems, *Proc. Natl. Acad. Sci.*, 117, 4617–4622, <https://doi.org/10.1073/pnas.1916169117>,  
854 2020.

855 Newman, M. E. J.: *Networks: an introduction*, Oxford University Press, Oxford ; New York, 772 pp., 2010.

856 Osten, F. B. von der, Kirley, M., and Miller, T.: Sustainability is possible despite greed - Exploring the nexus  
857 between profitability and sustainability in common pool resource systems, *Sci. Rep.*, 7, 2307,  
858 <https://doi.org/10.1038/s41598-017-02151-y>, 2017.

859 Ostrom, E.: *Collective Action and the Evolution of Social Norms*, 2000.

860 Pausata, F. S. R., Gaetani, M., Messori, G., Berg, A., Maia De Souza, D., Sage, R. F., and deMenocal, P. B.: The  
861 Greening of the Sahara: Past Changes and Future Implications, *One Earth*, 2, 235–250,  
862 <https://doi.org/10.1016/j.oneear.2020.03.002>, 2020.

863 Pearson, A. R., Ballew, M. T., Naiman, S., and Schuldt, J. P.: Race, Class, Gender and Climate Change  
864 Communication, in: *Oxford Research Encyclopedia of Climate Science*, Oxford University Press,  
865 <https://doi.org/10.1093/acrefore/9780190228620.013.412>, 2017.

866 Phillips, B. and Bauch, C. T.: Network structural metrics as early warning signals of widespread vaccine refusal in  
867 social-epidemiological networks, *J. Theor. Biol.*, 531, 110881, <https://doi.org/10.1016/j.jtbi.2021.110881>,  
868 2021.

869 Phillips, B., Anand, M., and Bauch, C. T.: Spatial early warning signals of social and epidemiological tipping points  
870 in a coupled behaviour-disease network, *Sci. Rep.*, 10, 7611, <https://doi.org/10.1038/s41598-020-63849-0>,  
871 2020.

872 Quimby, C. C. and Angelique, H.: Identifying Barriers and Catalysts to Fostering Pro-Environmental Behavior:  
873 Opportunities and Challenges for Community Psychology, *Am. J. Community Psychol.*, 47, 388–396,  
874 <https://doi.org/10.1007/s10464-010-9389-7>, 2011.

875 Rajapaksa, D., Islam, M., and Managi, S.: Pro-Environmental Behavior: The Role of Public Perception in  
876 Infrastructure and the Social Factors for Sustainable Development, *Sustainability*, 10, 937,  
877 <https://doi.org/10.3390/su10040937>, 2018.

878 Ratima, M., Martin, D., Castleden, H., and Delormier, T.: Indigenous voices and knowledge systems – promoting  
879 planetary health, health equity, and sustainable development now and for future generations, *Glob. Health*  
880 *Promot.*, 26, 3–5, <https://doi.org/10.1177/1757975919838487>, 2019.

881 Reisinger, D., Adam, R., Kogler, M. L., Füllsack, M., and Jäger, G.: Critical transitions in degree mixed networks: A  
882 discovery of forbidden tipping regions in networked spin systems, *PLOS ONE*, 2022.

883 Richter, A. and Dakos, V.: Profit fluctuations signal eroding resilience of natural resources, *Ecol. Econ.*, 117, 12–21,  
884 <https://doi.org/10.1016/j.ecolecon.2015.05.013>, 2015.

885 Richter, A. and Grasman, J.: The transmission of sustainable harvesting norms when agents are conditionally  
886 cooperative, *Ecol. Econ.*, 93, 202–209, <https://doi.org/10.1016/j.ecolecon.2013.05.013>, 2013.

887 Richter, A., van Soest, D., and Grasman, J.: Contagious cooperation, temptation, and ecosystem collapse, *J. Environ.*  
888 *Econ. Manag.*, 66, 141–158, <https://doi.org/10.1016/j.jeem.2013.04.004>, 2013.

889 Rocha, J. C., Schill, C., Saavedra-Díaz, L. M., Moreno, R. D. P., and Maldonado, J. H.: Cooperation in the face of  
890 thresholds, risk, and uncertainty: Experimental evidence in fisher communities from Colombia, *PLOS*  
891 *ONE*, 15, e0242363, <https://doi.org/10.1371/journal.pone.0242363>, 2020.

892 Rosales Sánchez, C., Craglia, M., and Bregt, A. K.: New data sources for social indicators: the case study of  
893 contacting politicians by Twitter, *Int. J. Digit. Earth*, 10, 829–845,  
894 <https://doi.org/10.1080/17538947.2016.1259361>, 2017.

895 Satake, A., Leslie, H. M., Iwasa, Y., and Levin, S. A.: Coupled ecological–social dynamics in a forested landscape:  
896 Spatial interactions and information flow, *J. Theor. Biol.*, 246, 695–707,  
897 <https://doi.org/10.1016/j.jtbi.2007.01.014>, 2007.

898 Scheffer, M., Bascompte, J., Brock, W. A., Brovkin, V., Carpenter, S. R., Dakos, V., Held, H., Van Nes, E. H.,  
899 Rietkerk, M., and Sugihara, G.: Early-warning signals for critical transitions, *Nature*, 461, 53–59,  
900 <https://doi.org/10.1038/nature08227>, 2009.

901 Schlag, K. H.: Why Imitate, and if so, How? A Bounded Rational Approach to Multi-Armed Bandits, *J. Econ.*  
902 *Theory*, 78, 130–156, 1998.

903 Schlüter, M., Mcallister, R. R. J., Arlinghaus, R., Bunnefeld, N., Eisenack, K., Hölker, F., Milner-Gulland, E. J.,  
904 Müller, B., Nicholson, E., Quaas, M., and Stöven, M.: New horizons for managing the environment: A  
905 review of coupled social-ecological systems modeling, *Nat. Resour. Model.*, 25, 219–272,  
906 <https://doi.org/10.1111/j.1939-7445.2011.00108.x>, 2012.

907 Schlüter, M., Tavoni, A., and Levin, S.: Robustness of norm-driven cooperation in the commons, *Proc. R. Soc. B*  
908 *Biol. Sci.*, 283, 20152431, <https://doi.org/10.1098/rspb.2015.2431>, 2016.

909 Schuster, P. and Sigmund, K.: Replicator dynamics, *J. Theor. Biol.*, 100, 533–538,  
910 [https://doi.org/10.1016/0022-5193\(83\)90445-9](https://doi.org/10.1016/0022-5193(83)90445-9), 1983.

911 Sethi, R. and Somanathan, E.: The Evolution of Social Norms in Common Property Resource Use, *Am. Econ. Rev.*,

912 86, 766–788, 1996.

913 Shao, Y., Wang, X., and Fu, F.: Evolutionary dynamics of group cooperation with asymmetrical environmental  
914 feedback, *EPL Europhys. Lett.*, 126, 40005, <https://doi.org/10.1209/0295-5075/126/40005>, 2019.

915 Sigdel, R. P., Anand, M., and Bauch, C. T.: Competition between injunctive social norms and conservation priorities  
916 gives rise to complex dynamics in a model of forest growth and opinion dynamics, *J. Theor. Biol.*, 432,  
917 132–140, <https://doi.org/10.1016/j.jtbi.2017.07.029>, 2017.

918 Somanathan, E.: Deforestation, Property Rights and Incentives in Central Himalaya, *Econ. Polit. Wkly.*, 26,  
919 PE37-PE39+PE41-PE46, 1991.

920 Stadelmann-Steffen, I., Eder, C., Harring, N., Spilker, G., and Katsanidou, A.: A framework for social tipping in  
921 climate change mitigation: What we can learn about social tipping dynamics from the chlorofluorocarbons  
922 phase-out, *Energy Res. Soc. Sci.*, 82, 102307, <https://doi.org/10.1016/j.erss.2021.102307>, 2021.

923 Steffen, W., Crutzen, P. J., and McNeill, J. R.: 2. The Anthropocene: Are Humans Now Overwhelming the Great  
924 Forces of Nature?, in: 2. The Anthropocene: Are Humans Now Overwhelming the Great Forces of Nature?,  
925 New York University Press, 12–31, <https://doi.org/10.18574/nyu/9781479844746.003.0006>, 2017.

926 Stoll-Kleemann, S., O’Riordan, T., and Jaeger, C. C.: The psychology of denial concerning climate mitigation  
927 measures: evidence from Swiss focus groups, *Glob. Environ. Change*, 11, 107–117,  
928 [https://doi.org/10.1016/S0959-3780\(00\)00061-3](https://doi.org/10.1016/S0959-3780(00)00061-3), 2001.

929 Sugiarto, H. S., Chung, N. N., Lai, C. H., and Chew, L. Y.: Socioecological regime shifts in the setting of complex  
930 social interactions, *Phys. Rev. E*, 91, 062804, <https://doi.org/10.1103/PhysRevE.91.062804>, 2015.

931 Sugiarto, H. S., Chung, N. N., Lai, C. H., and Chew, L. Y.: Emergence of cooperation in a coupled socio-ecological  
932 system through a direct or an indirect social control mechanism, *J. Phys. Commun.*, 1, 055019,  
933 <https://doi.org/10.1088/2399-6528/aa9b0e>, 2017a.

934 Sugiarto, H. S., Lansing, J. S., Chung, N. N., Lai, C. H., Cheong, S. A., and Chew, L. Y.: Social Cooperation and  
935 Disharmony in Communities Mediated through Common Pool Resource Exploitation, *Phys. Rev. Lett.*,  
936 118, 208301, <https://doi.org/10.1103/PhysRevLett.118.208301>, 2017b.

937 Sun, T. A. and Hilker, F. M.: Analyzing the mutual feedbacks between lake pollution and human behaviour in a  
938 mathematical social-ecological model, *Ecol. Complex.*, 43, 100834,  
939 <https://doi.org/10.1016/j.ecocom.2020.100834>, 2020.

940 Suzuki, Y. and Iwasa, Y.: The coupled dynamics of human socio-economic choice and lake water system: the  
941 interaction of two sources of nonlinearity, *Ecol. Res.*, 24, 479–489,  
942 <https://doi.org/10.1007/s11284-008-0548-3>, 2009.

943 Tavoni, A., Schlüter, M., and Levin, S.: The survival of the conformist: Social pressure and renewable resource  
944 management, *J. Theor. Biol.*, 299, 152–161, <https://doi.org/10.1016/j.jtbi.2011.07.003>, 2012.

945 Thampi, V. A., Anand, M., and Bauch, C. T.: Socio-ecological dynamics of Caribbean coral reef ecosystems and  
946 conservation opinion propagation, *Sci. Rep.*, 8, 2597, <https://doi.org/10.1038/s41598-018-20341-0>, 2018.

947 Tilman, A. R., Levin, S., and Watson, J. R.: Revenue-sharing clubs provide economic insurance and incentives for  
948 sustainability in common-pool resource systems, *J. Theor. Biol.*, 454, 205–214,

949 <https://doi.org/10.1016/j.jtbi.2018.06.003>, 2018.

950 Van Boven, L., Ehret, P. J., and Sherman, D. K.: Psychological Barriers to Bipartisan Public Support for Climate  
951 Policy, *Perspect. Psychol. Sci.*, 13, 492–507, <https://doi.org/10.1177/1745691617748966>, 2018.

952 Van Nes, E. H., Arani, B. M. S., Staal, A., Van Der Bolt, B., Flores, B. M., Bathiany, S., and Scheffer, M.: What Do  
953 You Mean, ‘Tipping Point’?, *Trends Ecol. Evol.*, 31, 902–904, <https://doi.org/10.1016/j.tree.2016.09.011>,  
954 2016.

955 Vasconcelos, V. V., Santos, F. C., Pacheco, J. M., and Levin, S. A.: Climate policies under wealth inequality, *Proc.*  
956 *Natl. Acad. Sci.*, 111, 2212–2216, <https://doi.org/10.1073/pnas.1323479111>, 2014.

957 Wang, Y., Kaplan, N., Newman, G., and Scarpino, R.: CitSci.org: A New Model for Managing, Documenting, and  
958 Sharing Citizen Science Data, *PLOS Biol.*, 13, e1002280, <https://doi.org/10.1371/journal.pbio.1002280>,  
959 2015.

960 Weitz, J. S., Eksin, C., Paarporn, K., Brown, S. P., and Ratcliff, W. C.: An oscillating tragedy of the commons in  
961 replicator dynamics with game-environment feedback, *Proc. Natl. Acad. Sci.*, 113,  
962 <https://doi.org/10.1073/pnas.1604096113>, 2016.

963 Wiedermann, M., Donges, J. F., Heitzig, J., Lucht, W., and Kurths, J.: Macroscopic description of complex adaptive  
964 networks coevolving with dynamic node states, *Phys. Rev. E*, 91, 052801,  
965 <https://doi.org/10.1103/PhysRevE.91.052801>, 2015.

966 Willcock, S., Cooper, G. S., Addy, J., and Dearing, J. A.: Earlier collapse of Anthropocene ecosystems driven by  
967 multiple faster and noisier drivers, *Nat. Sustain.*, <https://doi.org/10.1038/s41893-023-01157-x>, 2023.

968 Wohlin, C.: Guidelines for snowballing in systematic literature studies and a replication in software engineering, in:  
969 *Proceedings of the 18th International Conference on Evaluation and Assessment in Software Engineering*,  
970 *EASE '14: 18th International Conference on Evaluation and Assessment in Software Engineering*, London  
971 England United Kingdom, 1–10, <https://doi.org/10.1145/2601248.2601268>, 2014.

972 Wollkind, D. J., Collings, J. B., and Logan, J. A.: Metastability in a temperature-dependent model system for  
973 predator-prey mite outbreak interactions on fruit trees, *Bull. Math. Biol.*, 50, 379–409, 1988.

974 Xu, L., Patterson, D., Levin, S. A., and Wang, J.: Non-equilibrium early-warning signals for critical transitions in  
975 ecological systems, *Proc. Natl. Acad. Sci.*, 120, e2218663120, <https://doi.org/10.1073/pnas.2218663120>,  
976 2023.