

*Supplement of*

## **Phase state and viscosity of secondary organic aerosols over China simulated by WRF-Chem**

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## S1. Bulk diffusion coefficient of organic and water molecules within SOA particles.

The diffusion coefficient in the bulk ( $D_b$ ) is an important parameter determining the mass-transport and mixing rates. We calculate the  $D_b$  of organic molecules within SOA particles by the fractional Stokes–Einstein equation (Price et al., 2016; Evoy et al., 2019):

$$D_{b,\text{org}} = D_c \left( \frac{\eta_c}{\eta} \right)^\xi \quad (1)$$

where  $\eta$  is the viscosity of SOA particles. The fit parameter  $\xi$  is 0.93 (Evoy et al., 2019).  $\eta_c$  is the crossover viscosity at which the Stokes–Einstein equation and the fractional Stokes–Einstein equation predict the same diffusion coefficient. The value of  $\eta_c$  is  $10^{-3}$  Pa s (Evoy et al., 2019).  $D_c$  is the crossover diffusion coefficient:

$$D_c = \frac{kT}{6\pi R_{\text{diff}}\eta_c} \quad (2)$$

where  $k$  is Boltzmann constant ( $1.38 \times 10^{-23}$  J K $^{-1}$ ),  $T$  is the temperature (K), and  $R_{\text{diff}}$  is the hydrodynamic radius of the diffusing species, with a value of  $4 \times 10^{-10}$  m for organic molecules (Maclean et al., 2021).

The fractional Stokes–Einstein equation is also used to determine the diffusion coefficient of water (Price et al., 2016; Evoy et al., 2019; Evoy et al., 2020):

$$D_{b,\text{H}_2\text{O}}(\text{RH}, T) = D_0(T) \left( \frac{\eta_0(T)}{\eta(\text{RH}, T)} \right)^\delta \quad (3)$$

where  $D_0(T)$  is the temperature-dependent diffusion coefficient of water molecules in pure water, which can be calculated using the Stokes–Einstein equation (Price et al., 2016).  $\eta_0(T)$  is the temperature-dependent viscosity of pure water, obtained from the VTF equation in Maclean et al. (2021):  $\log(\eta_0(T)) = A + \frac{B}{T-T_0}$ . The values of  $A$ ,  $B$ , and  $T_0$  are  $-4.28$ ,  $152.87$  and  $173.06$ , respectively, obtained from fitting the temperature-dependent viscosities of water (Hallett, 1963; Crittenden et al., 2012) to the VTF equation.  $\delta$  is the fractional exponent and can be calculated by Eq. 4:

$$\delta = 1 - \left[ A_1 \exp \left( -B_1 \frac{R_{\text{diff}}}{R_{\text{matrix}}} \right) \right] \quad (4)$$

where  $A_1$  and  $B_1$  are coefficients with values of  $0.73$  and  $1.79$ , respectively (Evoy et al., 2020). The radius ( $R_{\text{diff}}$ ) of the diffusing molecule, i.e., the water molecule, is  $10^{-10}$  m. The radius of the matrix molecules ( $R_{\text{matrix}}$ ) is assumed to be  $4 \times 10^{-10}$  m, representing the size of organic molecules (Maclean et al., 2021).

## S2. Definitions of model performance statistics.

The mean bias (MB), normalized mean bias (NMB), root mean squared error (RMSE) and index of agreement (IOA) are calculated based on the equations below.  $P_i$  represents the simulated data, and  $O_i$  represents observed data.  $N$  is the number of the data pairs.  $\bar{O}$  is the mean value of the observed data:

$$MB = \frac{\sum_{i=1}^N (P_i - O_i)}{N}$$

$$NMB = \frac{\sum_{i=1}^N (P_i - O_i)}{\sum_{i=1}^N O_i} \times 100\%$$

$$RMSE = \sqrt{\frac{\sum_{i=1}^N (P_i - O_i)^2}{(N - 1)}}$$

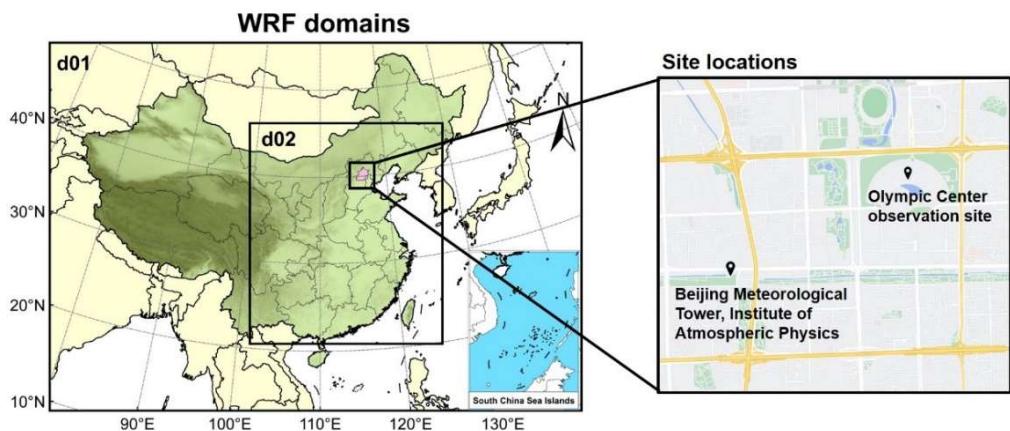
$$IOA = 1 - \frac{\sum_{i=1}^N (O_i - P_i)^2}{\sum_{i=1}^N (|P_i - \bar{O}| + |O_i - \bar{O}|)^2}$$

**Table S1.** Physical and chemical options in WRF-Chem used in this study.

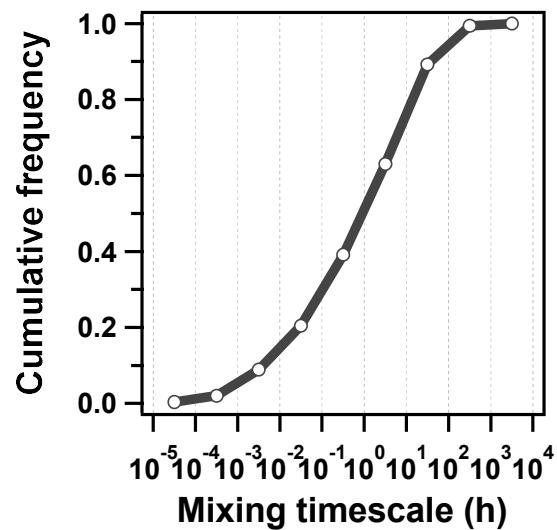
Physical/chemical schemes	Options
Advection scheme	Runge-Kutta 3rd order
Cloud microphysics	Lin et al. 1983 (Lin et al., 1983)
Long-wave radiation	RRTM
Short-wave radiation	Goddard
Surface layer	Revised MM5 Monin-Obukhov scheme
Land-surface model	Unified Noah land-surface model
Boundary layer scheme	YSU
Cumulus parameterization	Grell 3D
Photolysis scheme	Madronich F-TUV photolysis
Chemistry option	Updated MOZART-4 mechanism (Emmons et al., 2010)
Aerosol option	MOSAIC (Zaveri et al., 2008)

**Table S2.** Model performance statistics for simulated hourly mean RH,  $T$ , concentrations of PM<sub>2.5</sub> and PM<sub>2.5</sub> components at the IAP site.

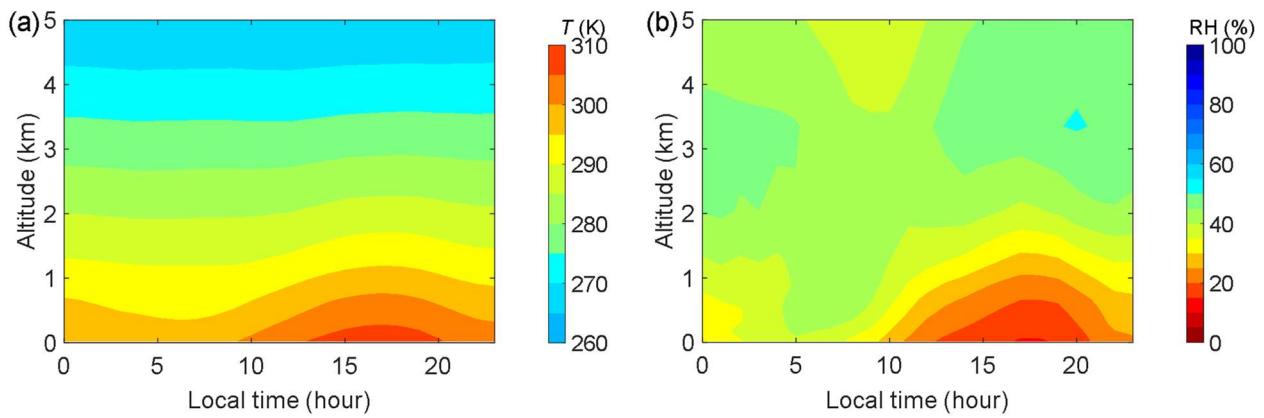
	Mean (observed)	Mean (simulated)	MB	NMB	RMSE	IOA
RH	40.60 %	29.63 %	-10.97 %	-27.01 %	14.90 %	0.87
$T$	299.48 K	301.29 K	1.81 K	0.60 %	2.84 K	0.93
PM <sub>2.5</sub>	52.05 $\mu\text{g m}^{-3}$	46.32 $\mu\text{g m}^{-3}$	-3.88 $\mu\text{g m}^{-3}$	-7.45 %	36.40 $\mu\text{g m}^{-3}$	0.64
NH <sub>4</sub> <sup>+</sup>	5.68 $\mu\text{g m}^{-3}$	3.71 $\mu\text{g m}^{-3}$	-1.90 $\mu\text{g m}^{-3}$	-33.43 %	5.33 $\mu\text{g m}^{-3}$	0.69
NO <sub>3</sub> <sup>-</sup>	8.71 $\mu\text{g m}^{-3}$	4.27 $\mu\text{g m}^{-3}$	-4.43 $\mu\text{g m}^{-3}$	-50.86 %	11.05 $\mu\text{g m}^{-3}$	0.70
SO <sub>4</sub> <sup>2-</sup>	8.73 $\mu\text{g m}^{-3}$	6.56 $\mu\text{g m}^{-3}$	-1.98 $\mu\text{g m}^{-3}$	-22.70 %	7.01 $\mu\text{g m}^{-3}$	0.70
SOA	11.03 $\mu\text{g m}^{-3}$	5.15 $\mu\text{g m}^{-3}$	-5.88 $\mu\text{g m}^{-3}$	-53.28 %	8.18 $\mu\text{g m}^{-3}$	0.49



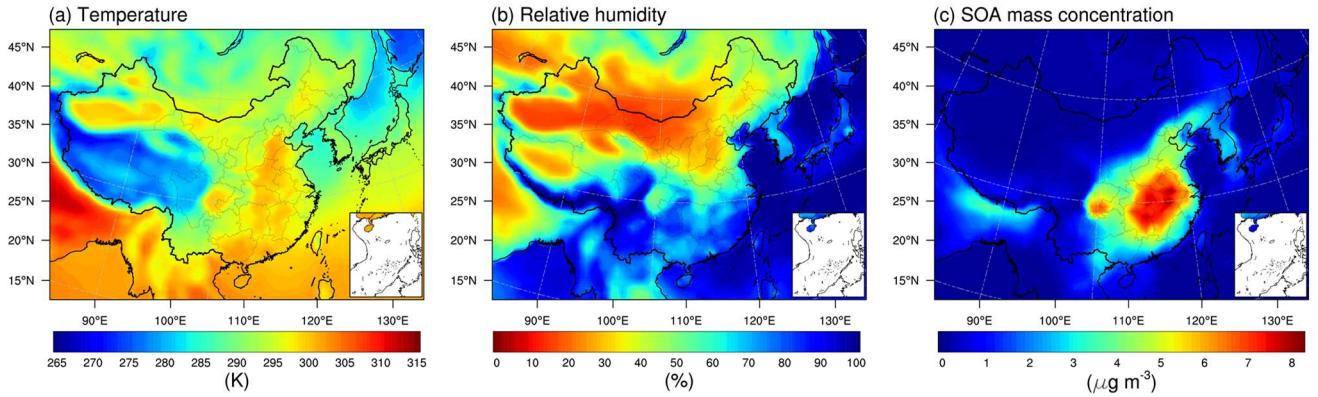
**Figure S1.** The WRF-Chem model domains and the observation sites. The map of the observation sites is adopted from © Google Maps.



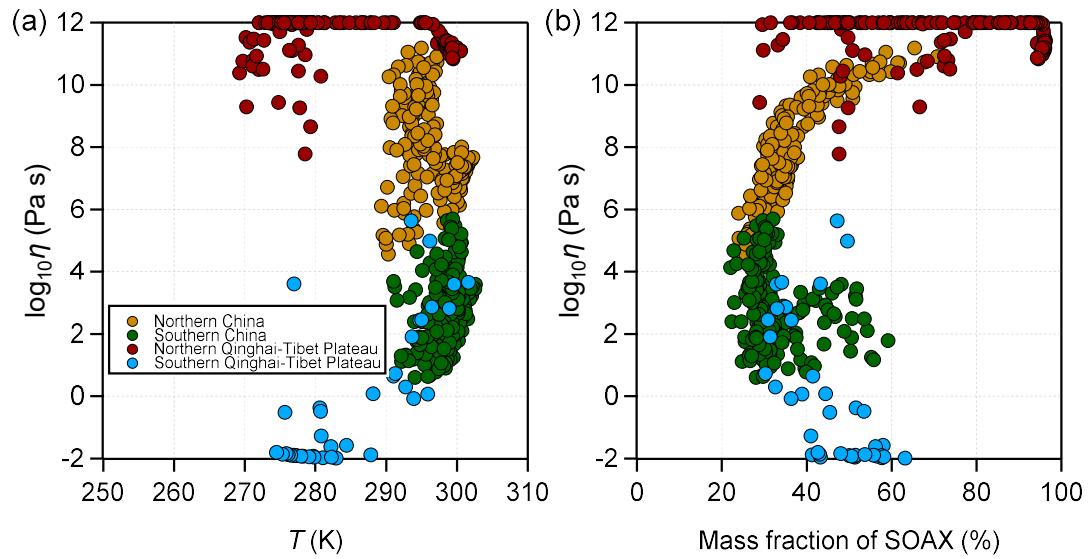
**Figure S2.** Cumulative distributions of mixing timescales of organic molecules within 200 nm SOA matrix at the IAP site.



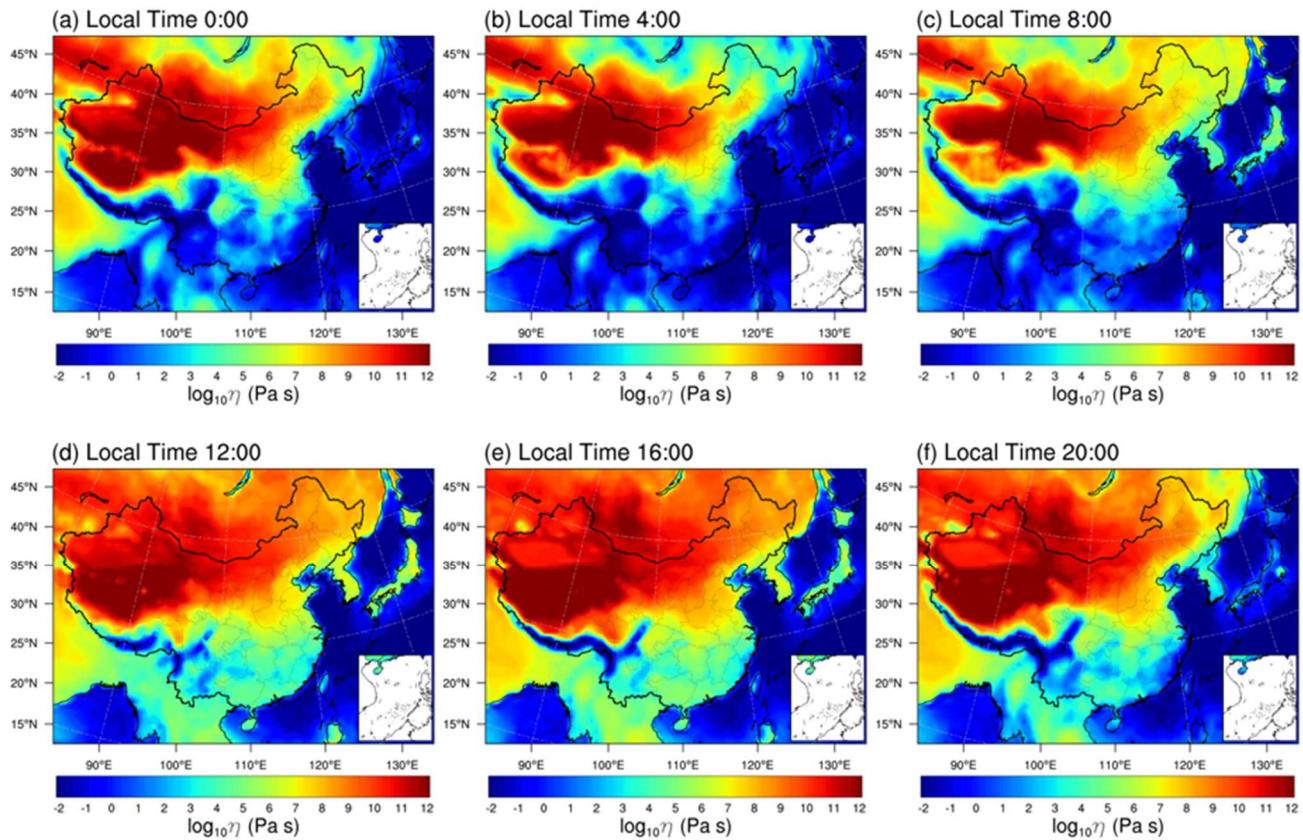
**Figure S3.** Median diurnal and vertical profiles of WRF-Chem predicted (a) temperature, and (b) relative humidity at the IAP site during May 20 – June 23 in 2018. Note: altitude is approximate and estimated from WRF-Chem pressure layers.



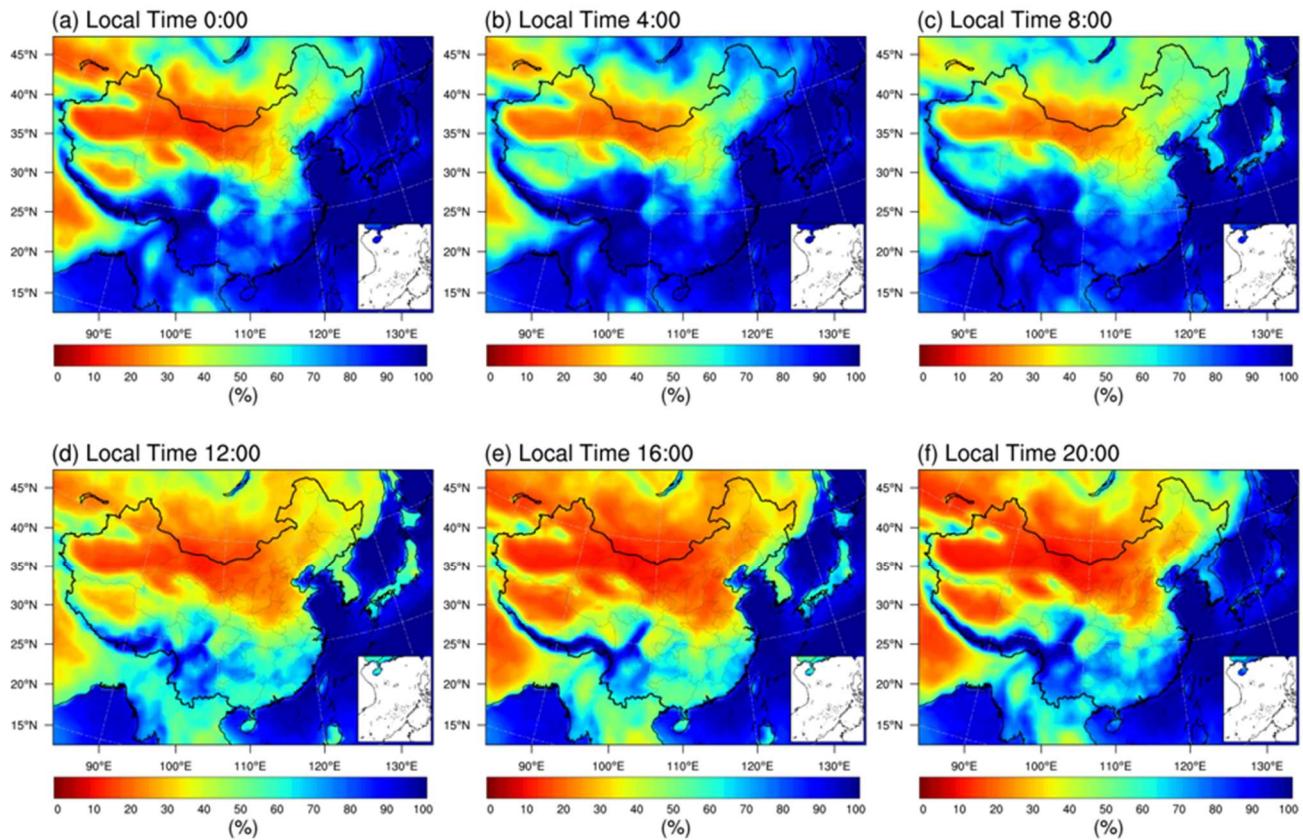
**Figure S4.** WRF-Chem predicted median surface values of (a)  $T$ , (b) RH, and (c) total SOA mass concentrations formed from VOC.



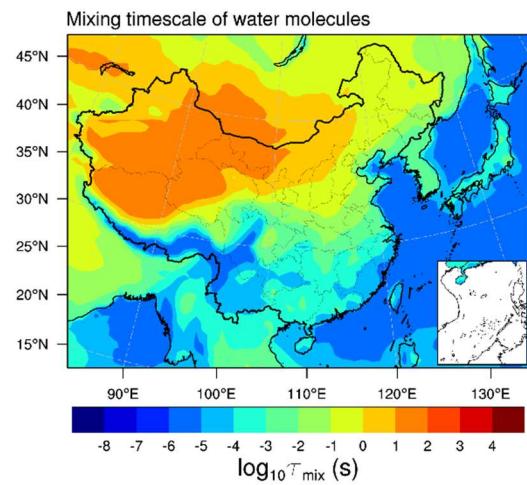
**Figure S5.** The median values of viscosity as a function of (a)  $T$  and (b) the mass fraction of SOAX ( $C^* = 0.1 \mu\text{g m}^{-3}$  at 298 K) calculated for selected regions in the northern China, southern China, northern Qinghai-Tibet Plateau, and southern Qinghai-Tibet Plateau as specified by white boxes in panel (a) during May 20 – June 23 in 2018.



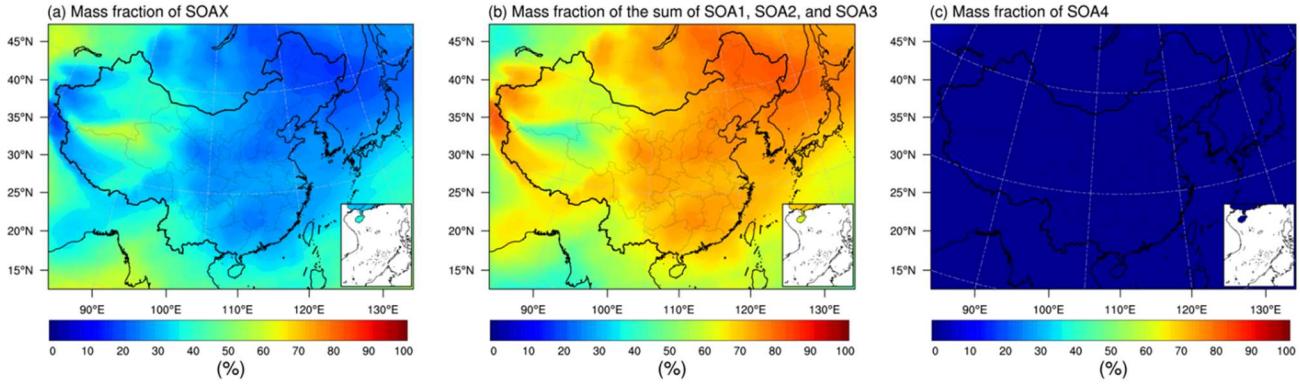
**Figure S6.** WRF-Chem predicted median surface values of viscosity at local time (hours in Beijing) during May 20 – June 23 in 2018.



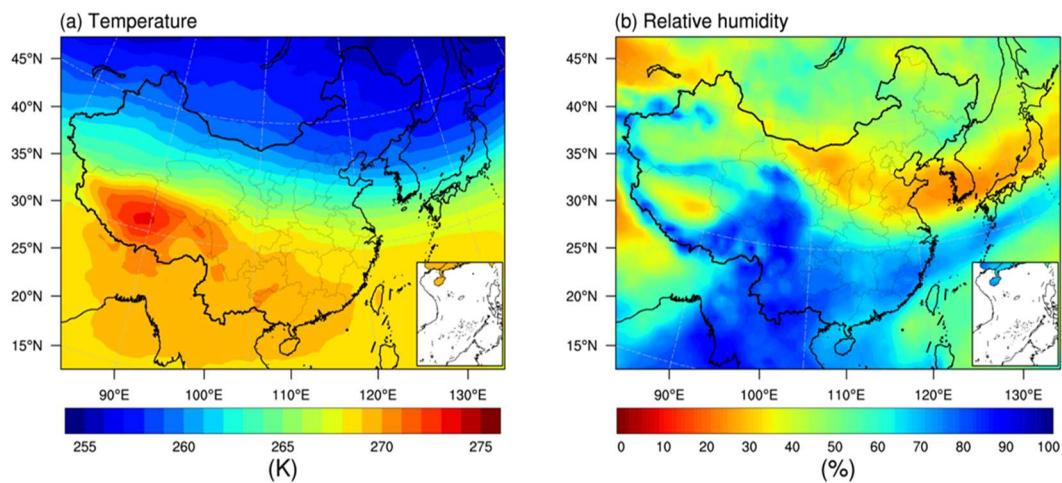
**Figure S7.** WRF-Chem predicted median surface values of RH at local time (hours in Beijing) during May 20 – June 23 in 2018.



**Figure S8.** WRF-Chem predicted median surface values of mixing timescales of water molecules in a 200 nm particle during May 20 – June 23 in 2018.



**Figure S9.** The predicted median values of mass fraction of (a) SOAX, (b) sum of SOA1, SOA2, and SOA3, and (c) SOA4 at 500 hPa during May 20 – June 23 in 2018 simulated in the base case (Table 1). SOAX, SOA1, SOA2, SOA3, and SOA4 represent the SOA with  $C^*$  of 0.1, 1, 10, 100, and  $1000 \mu\text{g m}^{-3}$  at 298 K, respectively.



**Figure S10.** The predicted median values of (a)  $T$  and (b) RH at 500 hPa during May 20 – June 23 in 2018 simulated in the base case (Table 1).

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