

1 **Solar FTIR measurements of NO<sub>x</sub> vertical distributions - Part 2:**  
2 **Experiment-based scaling factors describing the daytime variation of**  
3 **stratospheric NO<sub>x</sub>**

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9

10 **Abstract**

11 Long-term experimental stratospheric NO<sub>2</sub> and NO partial columns measured by means of solar Fourier-transform infrared  
12 (FTIR) spectrometry at Zugspitze (47.42° N, 10.98° E, 2964 m a.s.l.), Germany were used to create a set of experiment-based  
13 monthly scaling factors ( $SF_{\text{exp}}$ ). The underlying data set is published in a companion paper (Nürnberg et al., 2023) comprising  
14 over 25 years of measurements depicting the daytime variability of stratospheric NO<sub>2</sub> and NO partial columns in dependence  
15 of local solar time (LST). In analogy to recently published simulation-based scaling factors by Strode et al. (2022), we created  
16  $SF_{\text{exp}}$  normalized to  $SZA = 72^\circ$  for NO<sub>2</sub> and NO for every month of the year as a function of solar zenith angle (SZA). Apart  
17 from a boundary value problem at minimum SZA values originating in averaging over different times of the month, the  
18 obtained scaling factors  $SF_{\text{exp}}(\text{NO}_2)$  and  $SF_{\text{exp}}(\text{NO})$  in dependence of SZA represent very well the daytime behavior already  
19 shown in model simulations and experiments in the literature. This behavior is a well pronounced increase of the NO<sub>2</sub> and NO  
20 stratospheric partial column with the time of the day and a flattening of this increase after noon. In addition to the discussion of  
21  $SF_{\text{exp}}$ , we validate the simulation-based scaling factors  $SF_{\text{sim}}(\text{NO}_2)$  (Strode et al., 2022) and present simulation-based scaling  
22 factors for NO  $SF_{\text{sim}}(\text{NO})$ . The simulation-based scaling factors show an excellent agreement with the experiment-based ones,  
23 i.e. for NO<sub>2</sub> and NO the mean value of the modulus between experiment and simulation over all SZA and months is only  
24 0.02 %. We show that recently used model simulations can describe very well the real behavior of nitrogen oxide (NO<sub>x</sub>)  
25 variability in the stratosphere. Furthermore, we conclude that ground-based FTIR measurements can be used for validation of  
26 the output of photochemistry models as well as creating experiment-based data sets describing the daytime stratospheric NO<sub>x</sub>  
27 variability in dependence of SZA. This is a contribution to improved satellite validation and a better understanding of  
28 stratospheric photochemistry.

29

## 30 1 Introduction

31 The important role of NO<sub>2</sub> and NO in stratospheric photochemistry has been known for half a century (Crutzen, 1979). Both  
32 nitrogen oxides (NO<sub>x</sub>) are a product of the photolysis of N<sub>2</sub>O and are an important part of the ozone (O<sub>3</sub>)-destroying nitrogen  
33 catalytic cycle which controls the O<sub>3</sub> abundance in the stratosphere (Johnston, 1992). Additionally, industry and transportation  
34 are major sources of tropospheric NO<sub>x</sub> in the troposphere (Grewe et al., 2001). Especially in urban areas, it can serve as a  
35 precursor for e.g. O<sub>3</sub> or nitric acid (HNO<sub>3</sub>) and therefore promote smog events and directly affect human health (World Health  
36 Organization. Regional Office for Europe, 2003). Furthermore, NO<sub>2</sub> has the potential to cause significant radiative forcing  
37 during pollution events with highly elevated NO<sub>2</sub> concentrations in the troposphere (Solomon et al., 1999).

38 The monitoring and quantification of NO<sub>x</sub> total columns has been conducted since 1967 via different satellite missions (Godin-  
39 Beekmann, 2010; Rusch, 1973). For the observation of tropospheric pollution events (e.g. smog), therefore, the knowledge of  
40 the stratospheric contribution to the total column is crucial. One way to face this problem is the reference sector method, taking  
41 unpolluted total columns at a similar latitude (e.g. above the ocean) as a reference and subtract it from the total column (Richter  
42 and Burrows, 2002). The two main assumptions justifying this approach are the longitudinal homogeneity of the stratospheric  
43 column and negligible tropospheric columns over the ocean. However, due to the strong diurnal cycle of NO<sub>2</sub> and NO no time  
44 mismatch should occur between both columns.

45 One method for dealing with the problem of time and site mismatches when comparing different NO<sub>x</sub> columns is the use of  
46 ground-based Fourier-transform infrared (FTIR) measurements. This method can provide data from any time of the day during  
47 sun light hours, giving the opportunity to describe daytime NO<sub>x</sub> variabilities with a high precision, as done for NO<sub>2</sub> by  
48 Sussmann et al. (2005). For the first time, they found a reliable daytime NO<sub>2</sub> increasing rate of  $(1.02 \pm 0.12) \cdot 10^{14} \text{ cm}^{-2} \text{ h}^{-1}$   
49 derived from FTIR measurements at mid-latitudes. Additionally, the retrieved FTIR data can have a certain altitude resolution,  
50 which allows conclusions about NO<sub>x</sub> partial column variabilities, e.g. of the stratospheric columns (Zhou et al., 2021; Yin et  
51 al., 2019). In Part 1 of our two companion papers (Nürnberg et al., 2023) we used these advantages of ground-based FTIR  
52 measurements to retrieve stratospheric partial columns from long-term NO<sub>2</sub> and NO measurements above Zugspitze (47.42° N,  
53 10.98° E, 2964 m a.s.l.), Germany, yielding information on NO<sub>x</sub> daytime variability for every month of the year. This specific  
54 data set has the potential to improve satellite validation and can serve as a basis for the description of stratospheric NO<sub>x</sub>  
55 variabilities with high time resolution. However, the data from ground-based measurements can only be retrieved for the  
56 limited number and locations of existing sites.

57 A method without this site restriction describing stratospheric NO<sub>x</sub> concentrations with global coverage is the use of model  
58 data from three-dimensional global transport and photochemistry models. The latter are able to describe trace gas  
59 concentrations in dependence of altitude, latitude and longitude with a very good time resolution. In comparison to one-  
60 dimensional models describing only the vertical distribution of atmospheric trace gases (e.g. O<sub>3</sub>, NO<sub>2</sub>, NO) (Allen et al., 1984;  
61 Prather and Jaffe, 1990), three-dimensional models simulate transport fluxes in all three dimensions and are able to include  
62 nearly all feedback mechanisms of the real world (Mclinden et al., 2000; Chang and Duewer, 1979). Both types of models can  
63 account for daytime variabilities and have been used in the last decades for inter-satellite comparisons (Brohede et al., 2007;  
64 Dubé et al., 2020) as well as for satellite data validation (Bracher et al., 2005) and correction (Dubé et al., 2021; Wang et al.,  
65 2020). However, these studies differ from case to case and do not provide general global information about NO<sub>x</sub> variability.  
66 These global information should be site independent and can be applied to any satellite validation or correction all over the  
67 planet.

68 Here, a recent study of Strode et al. (2022) closed this gap by developing a set of simulation-based scaling factors ( $SF_{\text{sim}}$ ),  
69 which describe the daytime variability of NO<sub>2</sub>. A given  $SF_{\text{sim}}$  is a measure for the change of trace gas concentrations during  
70 the day normalized to a specific time (here sunrise or sunset).  $SF_{\text{sim}}$  are extracted from a three-dimensional model, which  
71 considers long-range transport, stratospheric and tropospheric chemistry as well as aerosol, radiation and transport. The  
72 generated monthly output is available for latitudes between -90° and 90° (1° steps) and altitudes between 6 km and 78 km

73 (0.5 km steps) for every time of the day given in solar zenith angle (SZA) values (Strode et al., 2022). This extensive research  
74 opens up the opportunity for the comparison, validation, and correction of remote and ground-based data products, by  
75 overcoming time or site mismatches.  
76 However, an observational counterpart, i.e. an analogous data set of experiment-based scaling factors describing the daytime  
77 increase of stratospheric NO<sub>x</sub> still does not exist, due to the lack of reliable long-term data comprising the full daytime NO<sub>2</sub>  
78 and NO variability. To close this gap, in this paper we create a set of experiment-based scaling factors ( $SF_{exp}$ ) in analogy to  
79 the simulation-based scaling factors published by Strode et al. (2002). On the one hand, this data set should serve as a general  
80 set of data describing the NO<sub>x</sub> daytime variability in dependence of SZA for the given latitude (47° N) of our observation site.  
81 On the other hand, we would like to use it to validate the recently published model data for  $SF_{sim}(NO_2)$  (Strode et al., 2022) as  
82 well as validate unpublished model data for  $SF_{sim}(NO)$  (Sarah Strode, personal communication, 2023). For this  $SF_{exp}$  data set  
83 we will use the observational results described in Part 1 of our set of two companion papers (Nürnberg et al., 2023), where a  
84 reliable long-term data set of NO<sub>2</sub> and NO partial columns above 16 km altitude above Zugspitze was created. As described  
85 above, these long-term data are retrieved from ground-based FTIR measurements and describe the daytime variability of  
86 stratospheric NO<sub>x</sub> within timesteps of minutes for every month of the year. The cut-off point at 16 km was chosen to avoid  
87 influences of variabilities near the tropopause and in the boundary layer upon the stratospheric partial column. Details are  
88 discussed in part 1. It is outside the scope of this work to describe with  $SF_{exp}$  the strong and fast photochemistry at sunrise and  
89 sunset.  
90 This paper (as Part 2 of our two companion papers) briefly describes in Sect. 2 the experimental set up and the resulting FTIR  
91 data taken from Part 1 (Nürnberg et al., 2023). In Sect. 3, the dependence on SZA for NO<sub>2</sub> and NO is shown and the resulting  
92 daytime variations presented in detail in Part 1 are discussed shortly, before the NO<sub>x</sub> partial columns (> 16 km) are converted  
93 into experiment-based scaling factors ( $SF_{exp}(NO_2)$  and  $SF_{exp}(NO)$ ) in Sect. 4. Finally, the resulting  $SF_{exp}$  are compared  
94 qualitatively and quantitatively to  $SF_{sim}$  retrieved from model simulations.

## 95 **2 FTIR data**

96 All data of this study are retrieved from long-term ground-based FTIR solar absorption measurements at Zugspitze, Germany  
97 (47.42° N, 10.98° E, 2964 m a.s.l.). The high-altitude observatory at Zugspitze is located in the German alps and can be  
98 considered as a clean site without strong influences from pollution events in the boundary layer. The used Bruker IFS 125HR  
99 spectrometer has operated continuously since 1995 at the Zugspitze. The experimental set-up and retrieval strategy are  
100 described in our part 1 companion paper (Nürnberg et al., 2023). As described in part 1, we used daily pressure and temperature  
101 profiles from the National Centers for Environmental Prediction (NCEP) interpolated to the measurement time. The  
102 temperature dependency of the data cannot be discussed in detail here, but it is very likely that the stratospheric temperature  
103 affects the NO<sub>x</sub> concentration and therefore also the observed diurnal cycle. The pollution filtered NO and NO<sub>2</sub> stratospheric  
104 partial columns (above 16 km altitude) derived in our part 1 study serve as a basis for the experiment-based scaling factors  
105 created now in this part 2) work. The data set comprises 6,213 NO and 16,023 NO<sub>2</sub> partial columns measured at the Zugspitze  
106 between 1995 and 2022.

## 107 **3 Experimental data**

### 108 **3.1 NO<sub>x</sub> stratospheric partial column dependence on SZA**

109 Figure 1 shows the NO<sub>2</sub> stratospheric partial columns (black symbols) taken from Nürnberg et al. (2023) for every month as a  
110 function of SZA. Note this is the same data as shown in our Part 1 (Fig. 3 therein), which had been therein plotted as a function  
111 of local solar time. The  $x$ -axis is interrupted for SZA values without observations in the respective month. Here, we define

112 SZA to be positive in the morning from sunrise ( $SZA = 90^\circ$ ) to local solar noon (respective minimum value dependent of the  
113 season) and to be negative in the afternoon between local solar noon and sunset ( $SZA = -90^\circ$ ).  
114 As already described and discussed in Part 1 of the two companion papers, the daytime increase of the  $\text{NO}_2$  stratospheric partial  
115 column follows for every month a linear behavior from sunrise to sunset. Briefly, this behavior reflects the photolysis of the  
116 reservoir species  $\text{HNO}_3$  and  $\text{N}_2\text{O}_5$  resulting in a consecutive increase of  $\text{NO}_2$  during daytime (Crutzen, 1970).  
117 Figure 2 shows in a similar way the  $\text{NO}$  stratospheric partial columns (black symbols) taken from the same work for every  
118 month in dependence of SZA (Nürnberg et al., 2023). Note this is the same data as shown in our Part 1 (Fig. 5 therein) as a  
119 function of local solar time. Briefly, the data show the typical daytime increase of stratospheric  $\text{NO}$  described in the literature  
120 via model calculations (Dubé et al., 2020; McLinden et al., 2000) or shown experimentally (Zhou et al., 2021; Rinsland et al.,  
121 1984) for every month. Here, the photolysis of the reservoir species  $\text{N}_2\text{O}$  leads to a well-pronounced increase of stratospheric  
122  $\text{NO}$  concentration in the morning (Crutzen, 1970). After local solar noon, the shift of the  $\text{NO}_2$ - $\text{NO}$  equilibrium, the increasing  
123 amount of  $\text{O}_3$  and the solar elevation dependency of the involved photochemical reaction lead to a strong flattening of the  
124 daytime  $\text{NO}$  curve in dependence of SZA in comparison to  $\text{NO}_2$ . This afternoon-effect is more pronounced in the summertime  
125 (mid row) than the rest of the year (Nürnberg et al., 2023).

#### 126 **4 Calculation of experiment-based scaling factors**

127 A set of experiment-based scaling factors ( $SF_{\text{exp}}$ ) analogous to the model-based scaling factors ( $SF_{\text{sim}}$ ) published by Strode et  
128 al. (2022) was created as follows: The mean values for  $2^\circ$  bins of SZA of the stratospheric partial column ( $> 16$  km) were  
129 calculated. In a next step, these mean values were normalized to  $SZA = 72^\circ$  (which is the only value being present in all  
130 monthly data sets) resulting in monthly  $SF_{\text{exp}}$  sets for  $\text{NO}_2$  and  $\text{NO}$  shown in Fig. 3 and Fig. 4, respectively. These data reflect  
131 the daytime variation of stratospheric  $\text{NO}_2$  and  $\text{NO}$  above Zugspitze, Germany. Values resulting from only one measurement  
132 point are shown in red without error bar.

133  $SF_{\text{exp}}(\text{NO}_2)$  (Figure 3, black and orange symbols) increases linearly throughout the day in each month, reflecting the increase  
134 in stratospheric  $\text{NO}_2$  concentration. There are two observations which can be pointed out here. First, the error bars in Fig. 3  
135 (i.e.  $\pm 2$  standard errors of the mean,  $\pm 2 \text{ SEM} = \pm 2 \sigma/\sqrt{n}$ ) are independent of the season and are very small, reflecting a low  
136 scattering within the  $2^\circ$  SZA bins and enough averaging data points  $n$ . Second, in spring and autumn, at local solar noon  
137 (minimum SZA), a significant increase in  $SF_{\text{exp}}(\text{NO}_2)$  is visible. This effect can be understood as a boundary value problem  
138 being due to the relatively fast change of SZA and of the  $\text{NO}_2$  stratospheric partial column (seasonal variation) during the  
139 spring and autumn months, respectively. Here, the combination of both the SZA and stratospheric partial column changes  
140 within one month end up with an increased averaged  $\text{NO}_2$  stratospheric partial column near the minimum SZA. The reason is  
141 that for SZA values below the minimum SZA at day 15 of each month, only partial columns from one half of the month can  
142 contribute to the average. Unfortunately, the stratospheric partial columns of this half deviate significantly from the monthly  
143 mean. Figure S1 in the supporting material illustrates this phenomenon using the  $\text{NO}_2$  partial column above 16 km altitude.  
144 Here, the first half (red symbols) and the second half (blue symbols) of April is split up into two datasets underlining the  
145 described boundary value problem. At low SZA values, only blue data points sum up to the averaged values, considering only  
146 the second half of the month. Consequently, the partial column and of course the scaling factor increases artificially (pointed  
147 out by the blue arrow in the figure). This effect leads us to the exclusion of these data points (Figure 3, orange symbols) below  
148 the minimum SZA reached at day 15 of the respective month. Another opportunity to face this problem would be the choice  
149 of a smaller time binning (e.g. 2 weeks, 10 days). However, this would i) worsen the comparability to the simulation-based  
150 scaling factors and ii) reduce the usable data base per time bin. The whole used data set of  $SF_{\text{exp}}(\text{NO}_2)$  can be found in the  
151 supporting material Table S1-S4.

152 For  $SF_{\text{exp}}(\text{NO})$  (Figure 4, black and orange symbols), the difference in daytime increase in comparison to  $\text{NO}_2$  is very well  
153 pronounced. Before local solar noon,  $SF_{\text{exp}}$  increases for every month linearly. After local solar noon, the described flattening  
154 of the increase is visible. Here, the NO stratospheric partial column stays almost constant within the scattering until sunset  
155 independent of the season. The  $\pm 2$  SEM error bars of  $SF_{\text{exp}}(\text{NO})$  shown in Fig. 4 are also very small, but more values are  
156 excluded (red symbols) due to the availability of only one measurement point within the corresponding  $2^\circ$  SZA bin. This  
157 reflects the lower data base of the NO retrieval, originating in the use of another spectral micro-window for analysis. However,  
158 the small error bars underline, that for most of the mean values, the data base is reliable. Near local solar noon for  $SF_{\text{exp}}(\text{NO})$   
159 a similar but even less pronounced effect can be seen, as described for  $\text{NO}_2$ . Here, the deviation from the visible trend at spring  
160 or autumn months is very small. However, for consistent data handling we will also exclude the respective values (orange  
161 symbols) for  $SF_{\text{exp}}(\text{NO})$  below the minimum SZA at each month 15<sup>th</sup>. The whole used data set of  $SF_{\text{exp}}(\text{NO})$  can be found in  
162 the supporting material Table S5-S8.

## 163 5 Model comparison of $\text{NO}_x$ scaling factors

164 In the previous section, we created experiment-based averaged monthly scaling factors  $SF_{\text{exp}}$  for  $\text{NO}_2$  and NO describing the  
165 daytime variation of stratospheric  $\text{NO}_x$  concentration above Zugspitze, Germany. Next, we will compare the discussed results  
166 for  $SF_{\text{exp}}$  to model-based scaling factors  $SF_{\text{sim}}$  for  $\text{NO}_2$  published by Strode et al. (2022) and for NO calculated from the same  
167 GEOS-GMI model simulation as the  $\text{NO}_2$  scaling factors. Details of the GEOS model simulation with GMI chemistry (Duncan  
168 et al., 2007; Strahan et al., 2007; Nielsen et al., 2017) are described in Strode et al. (2022) and refs therein. The model  
169 parameters and the analysis method can be found in the literature (Strode et al., 2022). The given scaling factors  $SF_{\text{sim}}(\text{NO}_2)$   
170 and  $SF_{\text{sim}}(\text{NO})$  are available for 146 levels between 6 km and 78.5 km altitude in a 0.5 km grid and are normalized to  
171  $\text{SZA} = 90^\circ$  (sunrise). For a better comparison of experiment and model, we calculated mean values for  $SF_{\text{sim}}$  which also  
172 represent the stratospheric partial column above 16 km altitude. In order to do so, for each model level  $z$ ,  $SF_{\text{sim}}(z)$  was weighted  
173 to the mean monthly partial column profile of the given  $\text{NO}_x$  retrieval at  $z$  and  $SF_{\text{sim}}(> 16 \text{ km})$  was obtained via averaging over  
174  $SF_{\text{sim}}(16 \text{ km})$  to  $SF_{\text{sim}}(78.5 \text{ km})$ . Furthermore,  $SF_{\text{sim}}(> 16 \text{ km})$  was normalized  $\text{SZA} = 72^\circ$  (rather than sunrise/sunset) as done  
175 for  $SF_{\text{exp}}$  in Sect. 4.

176  $SF_{\text{sim}}(\text{NO}_2)$  and  $SF_{\text{sim}}(\text{NO})$  are additionally shown in Fig. 5 and Fig. 6, respectively (red line). At first appearance,  $SF_{\text{exp}}$  (black  
177 symbols) and  $SF_{\text{sim}}$  (red line) fits together very well and the model data follow the experimental daytime variation for both  
178 species  $\text{NO}_2$  and NO.

### 179 5.1.1 Quantitative evaluation

180 For the quantitative evaluation of the model comparison, the residuals between experiment and model  $(SF_{\text{exp}} - SF_{\text{sim}})/SF_{\text{sim}}$  are  
181 calculated for  $SF(\text{NO}_2)$  and  $SF(\text{NO})$  and are shown in Fig. 7 and Fig. 8, respectively. Additionally, the mean bias per month is  
182 shown as a mean value over all SZA (red dotted line).

183 The residuals of  $SF(\text{NO}_2)$  (Figure 7) show over the whole year a very good agreement between experiment and model within  
184  $\pm 0.2\%$ , reflecting the high quality of the GEOS GMI simulation at midlatitudes. Only for a few months, significant differences  
185 between experiment and model are visible. For April, August and September, the morning increase of  $\text{NO}_2$  is less pronounced  
186 in the model, leading to a significant deviation from the experimental values and an underestimation of the experiment-based  
187 scaling factors  $SF_{\text{exp}}$  at noon. However, the experimental values describing the stratospheric  $\text{NO}_2$  variability can be also  
188 influenced by tropospheric variations, because the used  $\text{NO}_2$  partial column cannot be treated as completely independent of  
189 the tropospheric partial column (see Nürnberg et al. (2023)). Furthermore, the model data offer higher uncertainties during  
190 twilight which can lead to deviations from experiment (Alvanos and Christoudias, 2019).

191 Table 1 shows the mean bias (see also Figure 7, red dotted line) for every month calculated from the residuals shown in Fig. 7  
192 together with two times the SEM ( $2 \sigma/\sqrt{n}$ ). Unfortunately, due to the small values of 2 SEM of 0.0065 % to 0.0192 % for  
193 most of the months (except March, July, October, November), 2 SEM is smaller than the mean bias. Therefore, when taking  
194 2 SEM as a quantitative indicator,  $SF_{\text{exp}}$  and  $SF_{\text{sim}}$  agrees only in four months within the margin of error. However, when  
195 considering the mean deviation between experiment and model of below  $|0.068 \%$  per month, we can state that the model data  
196 published by Strode et al. (2022) reflect sufficiently well the experimental values retrieved from solar FTIR measurements at  
197 midlatitudes.

198 A very similar behavior can be obtained for  $SF(\text{NO})$  (Figure 8). With a maximum deviation of  $\pm 0.2 \%$  the agreement between  
199 experiment and model is very similar as seen for  $\text{NO}_2$ . However, it is remarkable, that for the months with highest SZA  
200 (January, February) the first data points after sunrise for which measurements exist (high SZA region) deviate significantly  
201 from zero. Comparing to Fig. 6, the experimental values in this region seem not to follow the continuous increase expected  
202 from model descriptions. Here, an error source of the experimental data can be the wide range in photochemical regimes along  
203 the line-of-sight of the FTIR slant column measurements at high SZA: high up in the atmosphere, the sun is already well above  
204 the horizon, so there has already been significant NO production, while lower down the atmosphere is still much darker and  
205 NO levels are still lower. The FTIR retrieval leads to an averaging over these effects because from the solar measurements NO  
206 slant columns along the line of sight are retrieved, and these are then converted to vertical column densities using a simple  
207  $\cos(\text{SZA})$  airmass correction.

208 Furthermore, the NO increase in the morning is more pronounced in the model, leading to a significant deviation from the  
209 experimental values and an overestimation of the experiment-based scaling factors  $SF_{\text{exp}}$  at noon. In the same manner as  
210 discussed before for  $\text{NO}_2$ , the experimental values describing the stratospheric NO variability can be influenced by tropospheric  
211 variations, because the used NO partial column cannot be treated as completely independent of the tropospheric partial column  
212 (see Nürnberg et al. (2023)). Consequently, the lower stratospheric partial column in the morning is more influenced by the  
213 tropospheric partial column than in the evening.

214 In the same way as done for  $\text{NO}_2$ , the mean bias (see also Fig. 8, red dotted line) and  $2 \sigma/\sqrt{n}$  (2 SEM) are calculated and are  
215 shown in Table 2 for the NO residuals. Here, a better agreement between experiment and model can be quantified. For six  
216 months (January, June, September, October, November, December) the mean bias is smaller than 2 SEM indicating an  
217 agreement between experiment and model within the error bars. Nevertheless, this observation not only reflects a better  
218 agreement between experiment and model but can be also explained with a higher scattering of the residuals leading to a higher  
219 SEM. This can be confirmed when comparing the values for 2 SEM given in Table 1 and Table 2. With a mean 2 SEM of the  
220 residuals over all months of 0.0096 % for  $\text{NO}_2$  and 0.0185 % for NO, respectively, the residual scattering with a similar  $n$  and  
221 a similar mean bias of 0.02 % is two times larger for NO.

222 In conclusion, the quantitative comparison of the experimental derived scaling factors  $SF_{\text{exp}}$  and the scaling factors derived  
223 from model simulations  $SF_{\text{sim}}$  for  $\text{NO}_2$  and NO showed very good agreement of both data sets with a mean bias between  
224 experiment and model of only 0.02 % over all months underlining the quality of the model data at midlatitudes and the  
225 reliability of the retrieved experiment-based scaling factors.

## 226 **6 Summary and Conclusions**

227 In this work, we reanalyzed an experimental long-term data set from solar FTIR measurements over 25 years of measurement  
228 at the Zugspitze (47.42° N, 10.98° E, 2964 m a.s.l.), Germany, published in a companion paper (Part 1, Nürnberg et al., 2023).  
229 We present for the first time experiment-based scaling factors  $SF_{\text{exp}}$  in dependence of the solar zenith angle (SZA) representing  
230 monthly daytime  $\text{NO}_2$  and  $\text{NO}$  variabilities in the stratosphere (> 16 km altitude) within timesteps of minutes.  $SF_{\text{exp}}$  is a  
231 measure for the variability of the  $\text{NO}_x$  partial column above 16 km altitude in comparison to local solar noon. We calculated  
232  $SF_{\text{exp}}$  from the time dependent monthly  $\text{NO}_x$  partial columns (published in Part 1) by averaging over SZA bins of 2° and a  
233 normalization to  $\text{SZA} = 72^\circ$ . The resulting values of  $SF_{\text{exp}}(\text{NO}_2)$  and  $SF_{\text{exp}}(\text{NO})$  reflect very well the expected daytime  
234 variability of  $\text{NO}_2$  and  $\text{NO}$  described in Part 1 (Nürnberg et al., 2023). Only the boundary values in spring and autumn months  
235 deviate significantly due to the relatively fast change of the minimum SZA during these months influencing the average value.  
236 Neglecting these values leads to two reliable experiment-based data sets for  $SF_{\text{exp}}(\text{NO}_2)$  and  $SF_{\text{exp}}(\text{NO})$ . Furthermore, we used  
237 these new experiment-based data sets to validate recently published simulation-based scaling factors  $SF_{\text{sim}}(\text{NO}_2)$  (Strode et al.,  
238 2022) and recently calculated simulation-based scaling factors  $SF_{\text{sim}}(\text{NO})$  from a global study representing a similar latitude  
239 (47 °N). Comparing experiment and model simulation, we find an excellent agreement for stratospheric  $\text{NO}_2$  and  $\text{NO}$  daytime  
240 variabilities with a mean bias of the modulus over all months and SZA of only 0.02 % with no significant deviating trends for  
241 boundary values. These results underline the quality of recent multi-dimensional model simulations of stratospheric trace  
242 gases, representing very well experimental data. Additionally, we showed, that ground-based FTIR measurements can provide  
243 reliable information about stratospheric  $\text{NO}_x$  variability within time steps of minutes, which can serve as a good basis for the  
244 validation of global model simulations and therefore can help to further optimize satellite validations.  
245 The analysis method of the retrieval of stratospheric  $\text{NO}_2$  and  $\text{NO}$  partial columns over Zugspitze, Germany, published in  
246 Part 1 of the two companion papers (Nürnberg et al., 2023) in combination with the generalization of this data by calculating  
247 unitless scaling factors  $SF$  and the validation of recently published model data in this paper (Part 2) can be seen as a strong  
248 tool for the further validation and correction of global model and satellite data. This approach can be taken for any ground-  
249 based FTIR spectrometer generating a global set of experiment-based stratospheric  $\text{NO}_2$  and  $\text{NO}$  partial columns or scaling  
250 factors  $SF_{\text{exp}}(\text{NO}_2)$  and  $SF_{\text{exp}}(\text{NO})$ .

### 251 **Data availability**

252 The presented calculated experimental factors  $SF_{\text{exp}}$  and the used partial columns in dependent of the SZA can be found in the  
253 supporting material of this paper. The used experimental data is published along in Part 1 of the two companion papers  
254 (Nürnberg et al., 2023). Any other data of interest underlying this publication can be obtained at any time from the  
255 corresponding author on demand. The simulated scaling factors for  $\text{NO}_2$  and  $\text{NO}$  are available at this website:  
256 [https://avdc.gsfc.nasa.gov/pub/data/project/GMI\\_SF/](https://avdc.gsfc.nasa.gov/pub/data/project/GMI_SF/)

### 257 **Author contributions**

258 PN optimized and performed the FTIR retrievals, made the scientific analysis, and wrote the manuscript. SAS performed the  
259 model simulations and processed the data for the comparison to experiment and supported editing of the manuscript. RS  
260 suggested this research, contributed to the design of the study, and supported editing of the manuscript.

### 261 **Competing Interests**

262 The contact author has declared that none of the authors has any competing interests.



263 **Acknowledgements**

264 Funding by the Federal Ministry of Education and Research of Germany within the ACTRIS-D project (grant no. 01LK2001B)  
265 is gratefully acknowledged. We acknowledge funding by the Helmholtz Changing Earth – Sustaining our Future research  
266 program within the Earth and Environment research field. SAS acknowledges support from NASA grant 80NSSC18K0711,  
267 the NASA Modeling, Analysis, and Prediction (MAP) Program, and computing resources from the NASA Center for Climate  
268 Simulation (NCCS) for the simulated scaling factors.

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**Table 1.** Calculated mean bias of residuals ( $[SF_{\text{exp}}-SF_{\text{sim}}]/SF_{\text{sim}}$ ) for every month between experiment and simulations for NO<sub>2</sub> and the standard error of the mean ( $\sigma/\sqrt{n}$ ) of this value.

Month	J (%)	F (%)	M (%)	A (%)	M (%)	J (%)	J (%)	A (%)	S (%)	O (%)	N (%)	D (%)
<b>mean bias</b>	-0.0230	-0.0257	-0.0024	0.0433	0.0118	0.0683	0.0060	0.0207	0.0414	-0.0062	0.0007	-0.0204
$2\sigma/\sqrt{n}$	0.0132	0.0092	0.0088	0.0082	0.0065	0.0096	0.0077	0.0093	0.0081	0.0072	0.0085	0.0192
<b>bias &lt; 2SEM ?</b>	No	No	Yes	No	No	No	Yes	No	No	Yes	Yes	No

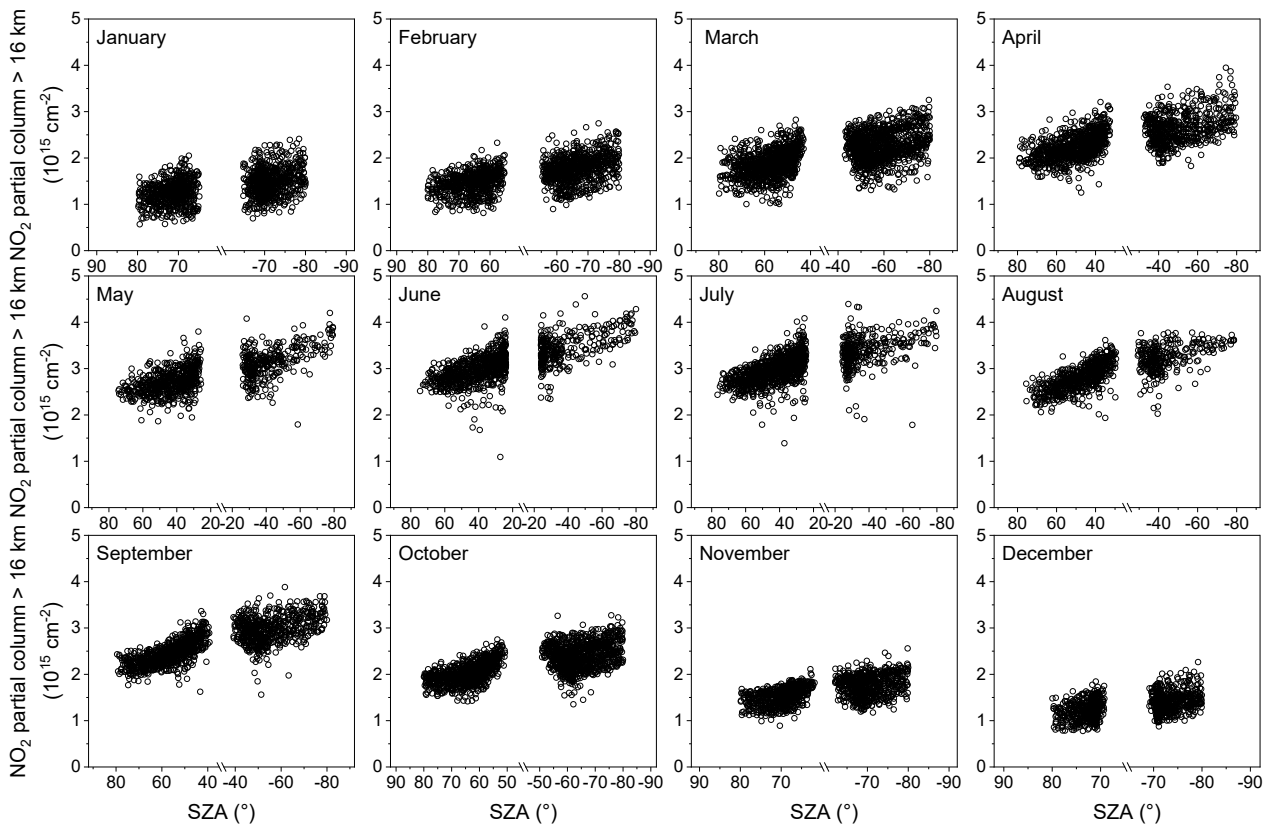
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**Table 2.** Calculated mean bias of residuals ( $[SF_{\text{exp}}-SF_{\text{sim}}]/SF_{\text{sim}}$ ) for every month between experiment and simulations for NO and 2 times the standard error of the mean ( $2\sigma/\sqrt{n}$ ) of this value.

Month	J (%)	F (%)	M (%)	A (%)	M (%)	J (%)	J (%)	A (%)	S (%)	O (%)	N (%)	D (%)
<b>mean bias</b>	-0.0045	-0.0592	-0.0220	-0.0269	-0.0714	-0.0046	-0.0889	-0.0767	-0.0068	-0.0118	-0.0096	0.0150
$2\sigma/\sqrt{n}$	0.0331	0.0236	0.0166	0.0110	0.0099	0.0160	0.0143	0.0102	0.0117	0.0138	0.0191	0.0425
<b>bias &lt; 2SEM ?</b>	Yes	No	No	No	No	Yes	No	No	Yes	Yes	Yes	Yes

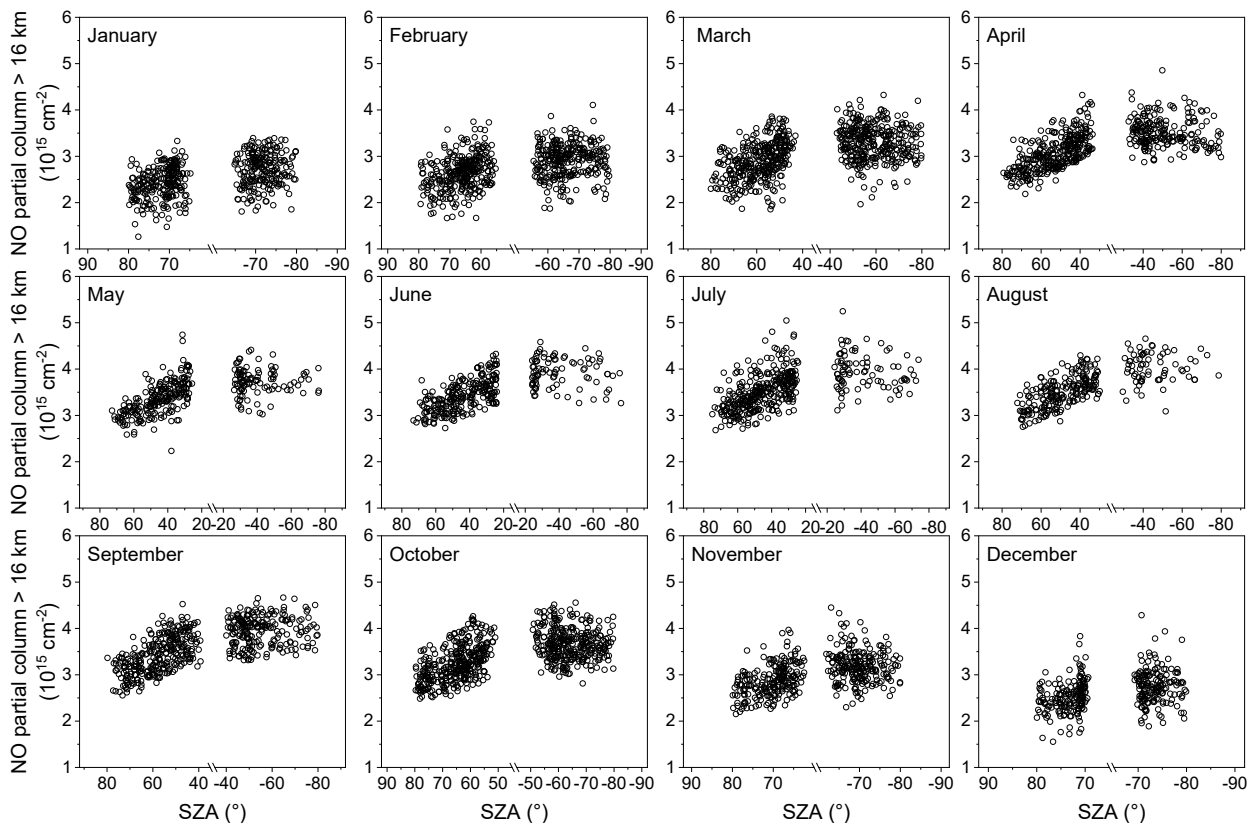
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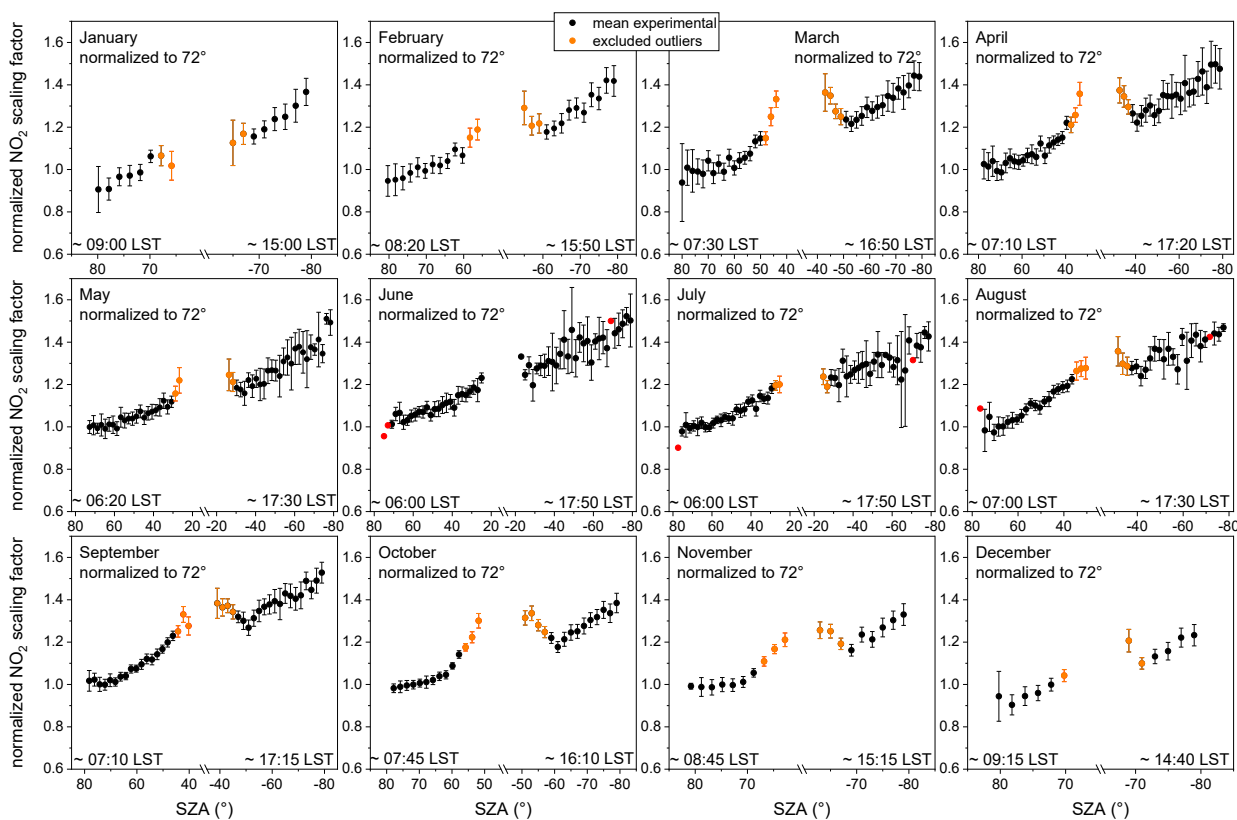
**Figure 1.** Retrieved NO<sub>2</sub> partial column above 16 km altitude measured at Zugspitze (black symbols) for every month in dependence of SZA.



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**Figure 2.** Retrieved NO partial column above 16 km altitude measured at Zugspitze (black symbols) for every month in dependence of SZA.



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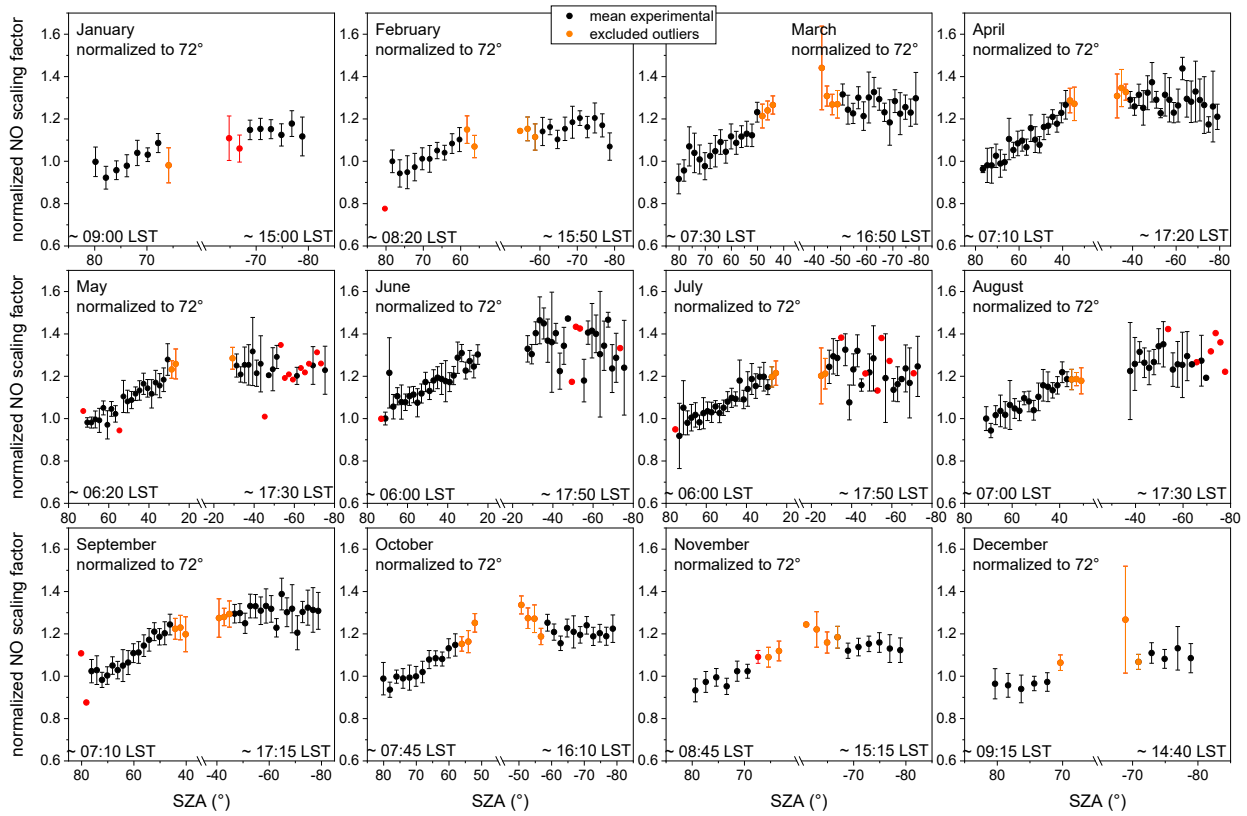
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**Figure 3.** Calculated normalized NO<sub>2</sub> scaling factors  $SF_{\text{exp}}(\text{NO}_2)$  above 16 km altitude measured at Zugspitze (black; orange symbols are excluded outliers) for every month in dependence of the SZA. The values represent the mean value within 2° SZA bins. The error bars represent two times the standard error of the mean ( $\pm 2 \sigma/\sqrt{n}$ ) value. Values resulting from only one measurement point are shown in red without error bar.



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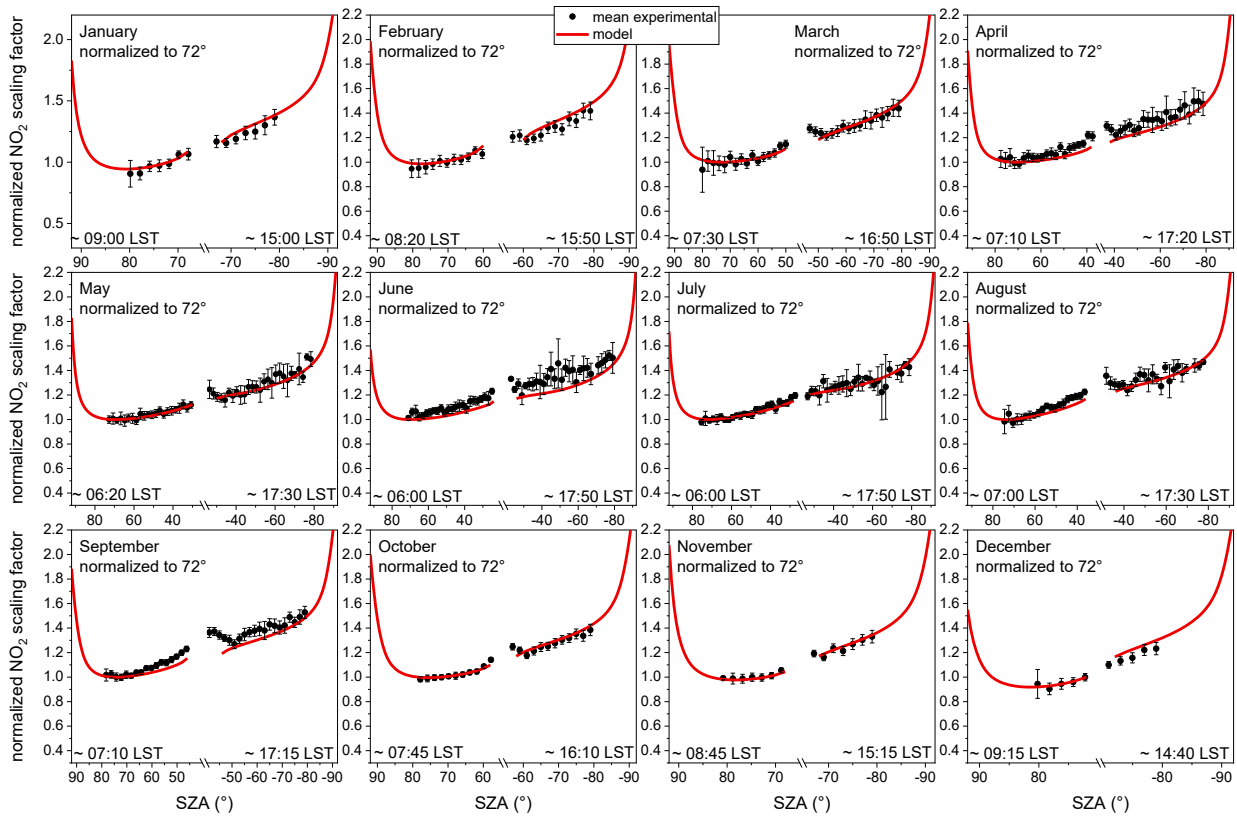
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**Figure 4.** Calculated normalized NO scaling factors  $SF_{\text{exp}}(\text{NO})$  above 16 km altitude measured at Zugspitze (black; orange are excluded outliers) for every month in dependence of SZA. The values represent the mean value within  $2^\circ$  SZA bins. The error bars represent two times the standard error of the mean ( $\pm 2 \sigma/\sqrt{n}$ ) value. Values resulting from only one measurement point are shown in red without error bar.



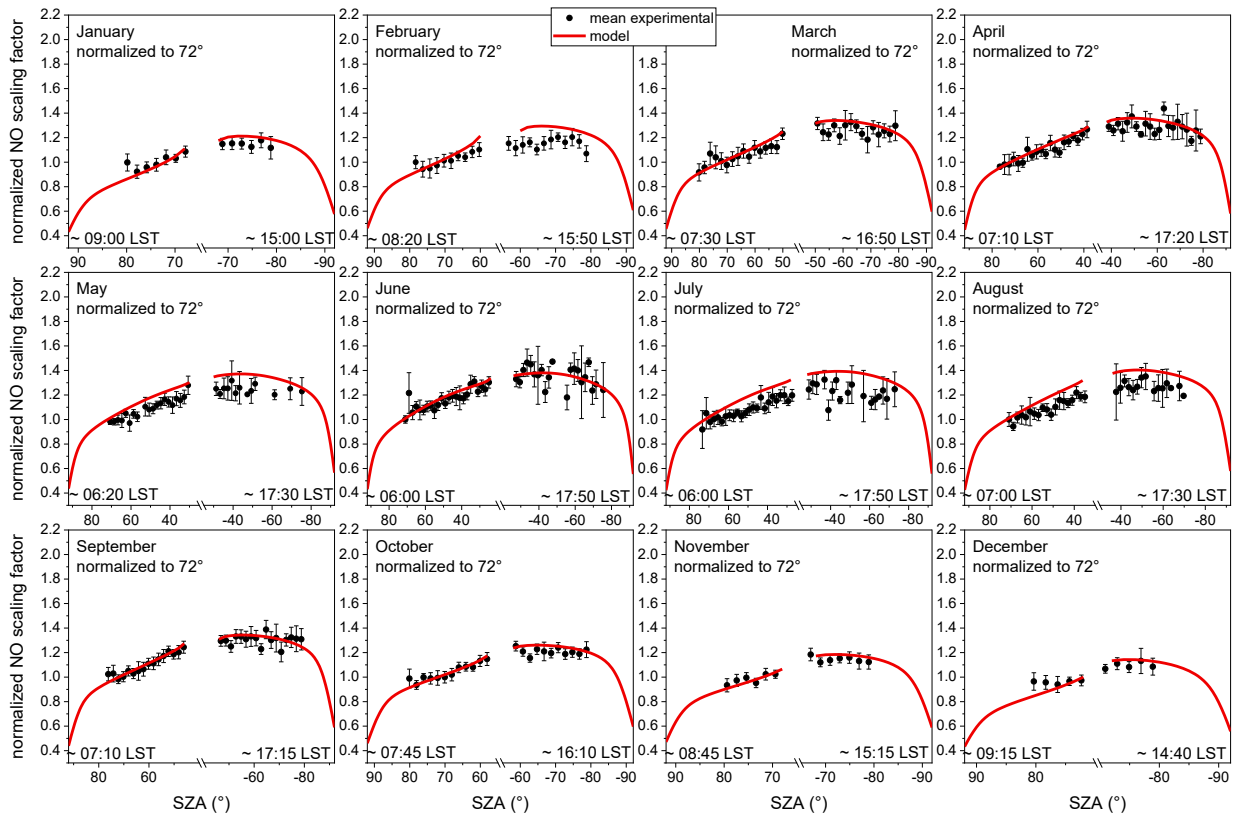
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**Figure 5.** Calculated normalized NO<sub>2</sub> scaling factors  $SF_{\text{exp}}(\text{NO}_2)$  above 16 km altitude measured at Zugspitze (black) and recalculated normalized NO<sub>2</sub> scaling factors  $SF_{\text{sim}}(\text{NO}_2)$  above 16 km altitude (red line) for every month in dependence of SZA. The experimental values represent the mean value within 2° SZA bins. The error bars represent two times the standard error of the mean ( $\pm 2 \sigma/\sqrt{n}$ ) value.



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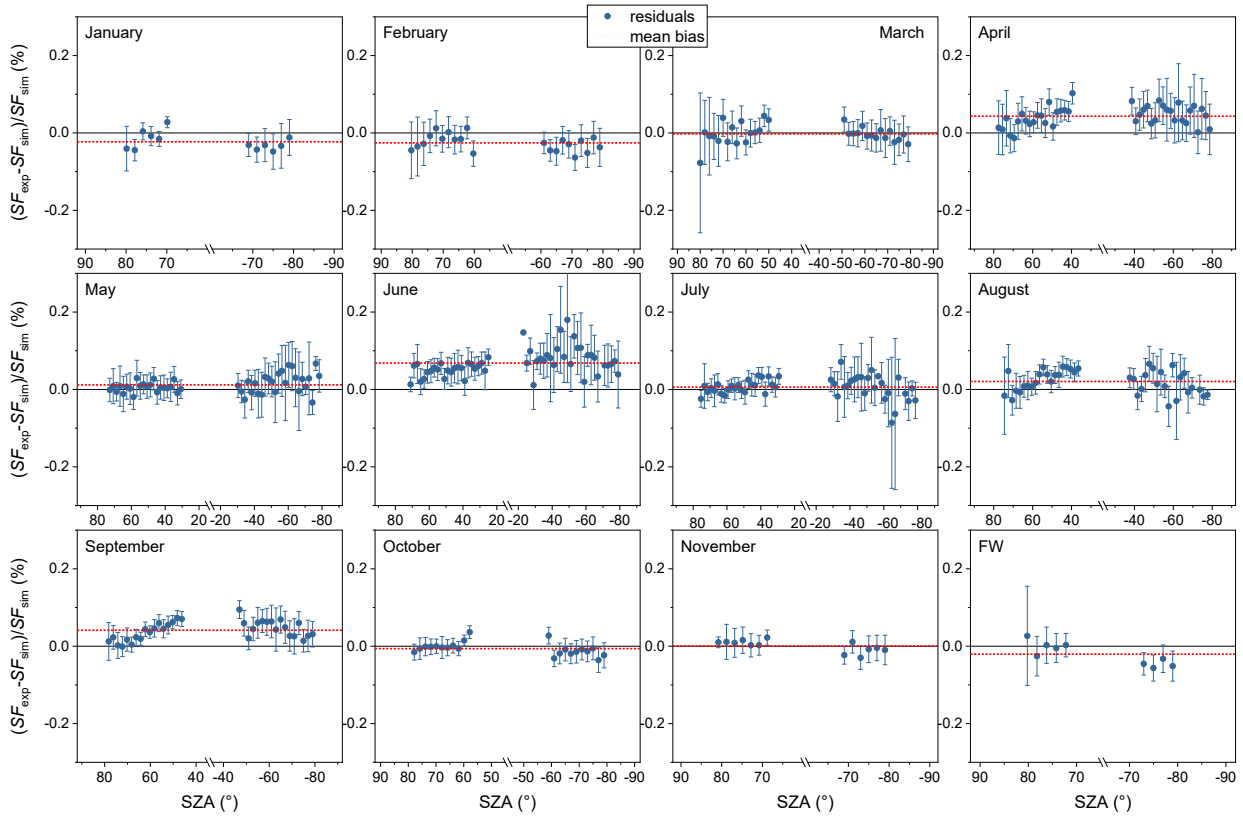
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**Figure 6.** Calculated normalized NO scaling factors  $SF_{\text{exp}}(\text{NO})$  above 16 km altitude measured at Zugspitze (black) and recalculated normalized NO scaling factors  $SF_{\text{sim}}(\text{NO})$  above 16 km altitude (red line) for every month in dependence of SZA. The experimental values represent the mean value within  $2^\circ$  SZA bins. The error bars represent two times the standard error of the mean ( $\pm 2 \sigma/\sqrt{n}$ ) value.





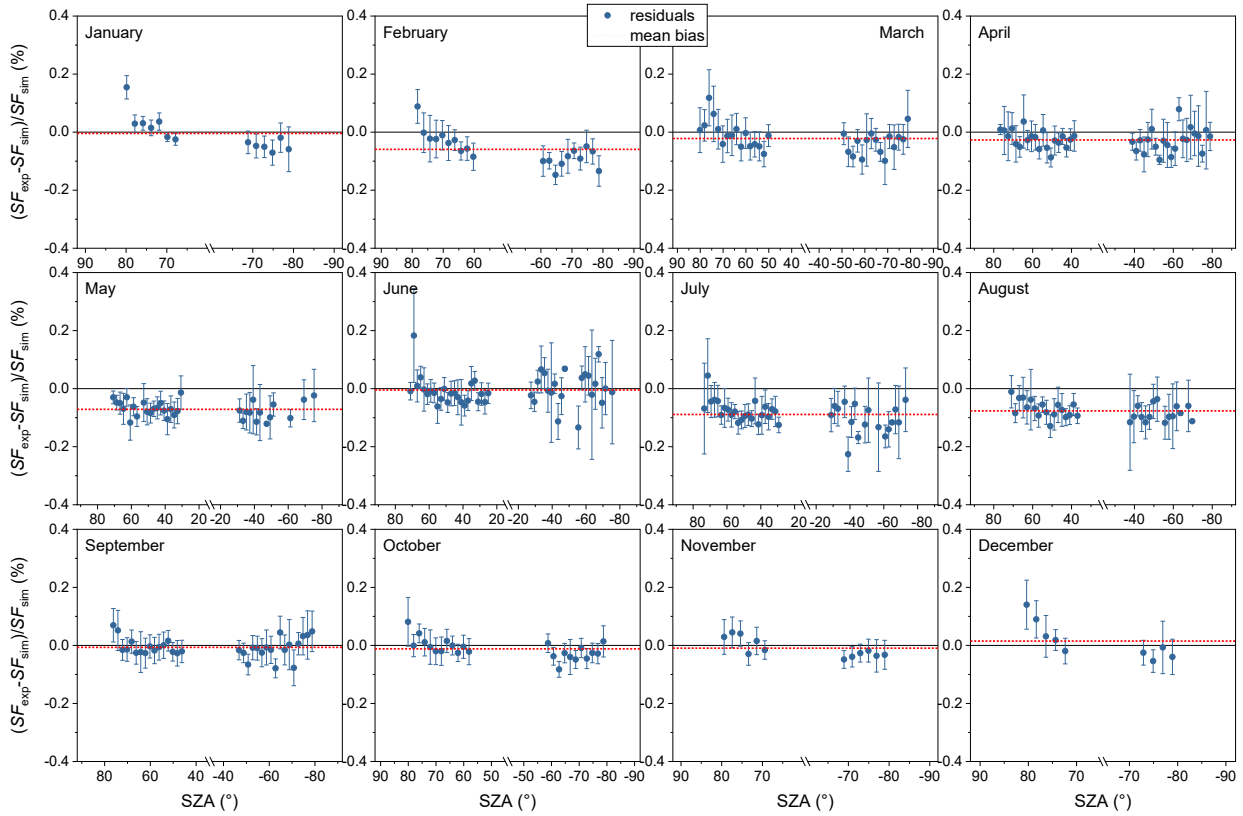
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**Figure 7.** Calculated residuals  $(SF_{exp}-SF_{sim})/SF_{sim}$  between the experimental normalized mean NO<sub>2</sub> scaling factors  $SF_{exp}$  and the simulated normalized NO<sub>2</sub> scaling factors  $SF_{sim}$  and interpolated to the respective SZA for every month in dependence of SZA. The error bars represent two times the propagated standard error of the mean ( $\pm 2 \sigma/\sqrt{n}$ ) of the experimental value. The mean bias over all SZA is shown in red.



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380 **Figure 8.** Calculated residuals ( $[SF_{\text{exp}}-SF_{\text{sim}}]/SF_{\text{sim}}$ ) between the experimental normalized mean NO scaling factors  $SF_{\text{exp}}$  and the simulated  
381 normalized NO scaling factors  $SF_{\text{sim}}$  and interpolated to the respective SZA for every month in dependence of SZA. The error bars represent  
382 two times the propagated standard error of the mean ( $\pm 2 \sigma/\sqrt{n}$ ) of the experimental value. The mean bias over all SZA is shown in red.