



1 **Quantifying the migration rate of drainage divides from**
2 **high-resolution topographic data**

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11 **Abstract**

12 The lateral movement of drainage divides is co-influenced by tectonics,
13 lithology, and climate, and therefore archives a wealth of geologic and climatic
14 information. Several methods have been proposed to determine the direction of
15 drainage-divide migration. However, how to quantify the migration rate of drainage
16 divides remains challenging. Here, we propose a new approach to calculate the
17 migration rate of drainage divides from high-resolution topographic data. The new
18 method is based on the cross-divide comparison of channel-head parameters,
19 including the critical upstream drainage area and the gradient of channel head, both of
20 which are used to calculate the normalized channel steepness at the channel head. We
21 then apply the new method to an active rift shoulder (Wutai Shan), and a tectonically



22 stable area (a mountain range in the Loess Plateau) in North China, to illustrate the
23 calculation of drainage-divide migration rates. The northward migration rates at the
24 Wutai Shan range from 0.10 to 0.13 mm/yr. The migration rates are approximately
25 zero at the mountain range in the Loess Plateau. This study demonstrates that the
26 migration rate of drainage divides can be determined more accurately once the cross-
27 divide differences in uplift rate are taken into account.

28 **Keywords**

29 Drainage divide; Migration rate; High-resolution topographic data; DEM; Channel
30 head

31 **1. Introduction**

32 The evolution of the Earth's surface is jointly controlled by tectonics, lithology,
33 and climatic conditions (e.g., [Molnar and England, 1990](#); [Whipple, 2009](#); [Bonnet,](#)
34 [2009](#); [Gallen, 2018](#); [Zondervan et al., 2020](#); [Bernard et al., 2021](#)). This provides a
35 basis for reconstructing the past tectonic ([Pritchard et al., 2009](#); [Kirby et al., 2012](#); [He](#)
36 [et al., 2021](#); [Shi et al., 2021](#); [Schildgen et al., 2022](#)) or climatic processes ([Tucker et](#)
37 [al., 1997](#); [Hancock et al., 2002](#)) through topography. The evolution of topography is
38 fundamentally coupled with changes in drainage systems, including river's vertical
39 and lateral movements ([Whipple, 2001](#); [Willett et al., 2014](#); [Zeng and Tan, 2023](#)).
40 Previous studies have extensively investigated how river channel profiles respond to
41 tectonic uplift ([Whipple, 2001](#); [Crosby and Whipple, 2006](#); [Pritchard et al., 2009](#);



42 Kirby et al., 2012; Goren et al., 2014), lithological difference (Duvall et al., 2004;
43 Safran et al., 2005; Forte et al., 2016), and precipitation perturbations (Schlunegger et
44 al., 2011; Bookhagen and Strecker, 2012). However, recent studies show that
45 widespread lateral movement of rivers (Clark et al., 2004; Deng et al., 2020; Zhao et
46 al., 2021; Zhou et al., 2022a) also interact with the adjustment of channel profiles
47 (Willett et al., 2014). Drainage-divide migration, therefore, may not only carry
48 information on geologic and/or climatic disturbance (Yang et al., 2019; Su et al.,
49 2020; He et al., 2021; Shi et al., 2021; Zeng and Tan, 2023) but also impact the
50 extraction of tectonic information from channel profiles (Goren et al., 2014; Ma et al.,
51 2020; Jiao et al., 2021). For this reason, the stability of drainage divides has drawn
52 more and more attention in recent years (e.g., Authemayou et al., 2018; Vacherat et
53 al., 2018; Chen et al., 2021; Shelef and Goren, 2021; Sakashita and Endo, 2023).

54 Drainage-divide migration is essentially controlled by the cross-divide
55 difference in erosion (Beeson et al., 2017; Dahlquist et al., 2018; Chen et al., 2021;
56 Zhou et al., 2022a). The erosion rates are routinely derived from geochronological
57 techniques, such as cosmogenic nuclides (e.g., ^{10}Be) concentration measurements
58 (Mandal et al., 2015; Struth et al., 2017; Sassolas-Serrayet et al., 2019), which can be
59 used to calculate the migration velocities of drainage divides (Beeson et al., 2017;
60 Godard et al., 2019; Hu et al., 2021). However, these techniques are usually based on
61 samples collected from an outlet that is several kilometers away from the drainage
62 divide and thus may not represent the erosion rates close to the drainage divide
63 (Sassolas-Serrayet et al., 2019). Besides, the high cost of sample testing makes it very



64 challenging to determine the drainage divide's motion by measuring the erosion rates
65 throughout the entire landscape. Hence, it would be ideal to find an accessible and
66 efficient method that can be applied to the entire landscape and cross-checked to make
67 full use of the ^{10}Be -derived erosion rates.

68 The advancement of remote sensing technology has promoted the development
69 of geomorphic analysis theory, making it possible to determine the drainage divide's
70 motion through topography analysis. For example, Willett et al. (2014) developed the
71 χ method to map the dynamic state of river basins. Forte and Whipple (2018)
72 proposed the cross-divide comparison of "Gilbert metrics" (including channel heads'
73 relief, slope, and elevation) to determine a drainage divide's motion. Others adopted
74 the comparison of slope angle or relief of the hillslopes across a drainage divide to
75 deduce its stability (Scherler and Schwanghart, 2020; Ye et al., 2022). Although these
76 geomorphic techniques are quantitative, so far, they could only determine the
77 migration direction of drainage divides. No rates have been obtained. Braun (2018)
78 raised a method that considers both alluvial and fluvial areas to calculate the
79 migration velocity of an escarpment (also a drainage divide). Zhou et al. (2022a)
80 developed a technique to calculate the migration rate through the cross-divide χ ratio
81 of high base-level channel segments. However, the channel-head parameter such as
82 the critical upstream area is an empirical value from previous studies, which may not
83 be applicable in specific natural areas and, therefore, could create great uncertainties
84 in the result of migration rates.

85 In this study, we choose a tectonically active area, i.e., the Wutai Shan in the



86 Shanxi rift system, and a tectonically inactive area, i.e., an unnamed mountain range
87 in the Loess plateau, to demonstrate how to quantify drainage-divide migration rates.
88 We use the aerial photography acquired by unmanned aerial vehicles (UAVs) and the
89 Structure from Motion (SfM) technology to obtain the high-resolution topography
90 data of these two areas. Based on the high-resolution data, we first identify the
91 position of the channel heads and extract their geomorphic parameters. We then
92 calculate the migration rates of the drainage divides using the channel-head
93 parameters. Moreover, we improve the method in Zhou et al (2022a) to adapt it to
94 areas where the elevations of outlets and channel heads are different across the
95 drainage divide. We apply these two methods in each case to calculate the drainage-
96 divide migration rates. This study aims to establish an approach to derive the
97 migration rate of drainage divides, at a high precision and low cost, based on
98 topographic analysis. Moreover, benefiting from the detailed tectonic research and the
99 high-resolution topographic data on the Wutai Shan, we attempt to quantify the
100 influence of the cross-divide difference in uplift rate on the drainage-divide migration
101 rate.

102

103 **2. Methods**

104 **2.1 Channel-head method**

105 According to the detachment-limited stream power model (Howard and Kerby,
106 1983; Howard, 1994), the channel's erosion rate (E) can be expressed as:



107
$$E = KA^m S^n \quad (1)$$

108 where K is the erosion coefficient, A is the upstream drainage area, S is the gradient of
109 the river channel, and m and n are empirical constants. Because of the mechanisms
110 such as erosion threshold (Howard and Kerby, 1983; Perron et al., 2008) or landslide
111 threshold (Burbank et al., 1996; Tucker et al., 1998), river channels (following Eq. 1)
112 emerge at a certain distance from the drainage divide. The region between the channel
113 head and the drainage divide is referred to as the hillslope area, where the erosion is
114 controlled by landslide, collapse, and diffusion processes (Stoke and Dietrich, 2006;
115 Stark, 2010; Braun et al., 2018; Dahlquist et al., 2018). The channel-head point is the
116 highest and the closest point to the drainage divide on a river channel (Clubb et al.,
117 2014). Therefore, the erosion rate at channel-head points (E_{ch}) can be described as:

118
$$E_{ch} = KA_{cr}^m S_{ch}^n \quad (2)$$

119 where E_{ch} is the erosion rate at channel-head points, A_{cr} is the critical upstream
120 drainage area of a channel-head point (Duvall et al., 2004; Wobus et al., 2006), and
121 S_{ch} is the channel-head gradient measured along the channel at the channel-head point.

122 To investigate the influence of the key parameters on the channel-head erosion
123 rate, we plot the curves of the channel-head erosion rate against the critical area based
124 on Eq. 2 for varying channel-head gradient and erosion coefficient (Fig. 1). The plots
125 show that the channel-head erosion rate (E_{ch}) increases monotonically with the critical
126 area (A_{cr}). When the critical area is invariant, the channel-head erosion rate also
127 increases with the channel-head gradient. A large erosion coefficient also creates a
128 high channel-head erosion rate. The results indicate that the side with a higher A_{cr} or



129 S_{ch} can have a higher erosion rate than the other side of the drainage divide and is
130 more likely to pirate the opposite drainage basin. Besides, high erosion coefficient can
131 amplify the drainage basins' erosion rate.

132 The drainage-divide migration is essentially controlled by the cross-divide
133 difference in erosion rates (Beeson et al., 2017; Dahlquist et al., 2018; Chen et al.,
134 2021). Furthermore, when one uses the cross-divide erosion rates at the channel heads
135 to calculate the erosion difference across the divide, one should also consider the
136 influence of differential uplift rates in these channel heads (Zhou et al., 2022a),
137 especially in the case of tectonic tilting uplift. The drainage-divide migration rate
138 (D_{mr}) can be obtained according to the cross-divide difference in erosion rate and
139 uplift rate (Zhou et al., 2022a):

$$140 \quad D_{mr} = \frac{\Delta E_{ch} - \Delta U_{ch}}{\tan\alpha + \tan\beta} \quad (3)$$

141 where ΔE_{ch} is the erosion rate difference between the two sides (annotated as α and β)
142 of the drainage divide ($\Delta E_{ch} = E_{cha} - E_{ch\beta}$), ΔU_{ch} is the cross-divide difference in rock
143 uplift rate ($\Delta U_{ch} = U_{cha} - U_{ch\beta}$), and $\tan\alpha$ and $\tan\beta$ are the gradients on both sides of
144 the drainage divide. Combining Eqs. 2 and 3, one can derive the equation of migration
145 velocity of drainage divides according to the parameters at the channel-head points:

$$146 \quad D_{mr} = \frac{K[(A_{cr}^m s_{ch}^n)_\alpha - (A_{cr}^m s_{ch}^n)_\beta] - \Delta U_{ch}}{\tan\alpha + \tan\beta} \quad (4)$$

147 The choice of α or β is arbitrary, and the positive direction of the migration velocity is
148 assigned as from the α to β side whereas the negative is the opposite. In this equation,
149 we assume the erosion coefficient is unchanged in the vicinity of a drainage divide. If
150 the exact K value is unknown, the drainage divide's unilateral erosion rate can be used



151 as a substitution:

$$152 \quad D_{mr} = \frac{E_{\alpha} \left[1 - \frac{(A_{cr}^m s_{ch}^n)_{\beta}}{(A_{cr}^m s_{ch}^n)_{\alpha}} \right] - \Delta U_{ch}}{\tan \alpha + \tan \beta} \quad (5)$$

153 or:

$$154 \quad D_{mr} = \frac{E_{\beta} \left[\frac{(A_{cr}^m s_{ch}^n)_{\alpha}}{(A_{cr}^m s_{ch}^n)_{\beta}} - 1 \right] - \Delta U_{ch}}{\tan \alpha + \tan \beta} \quad (6)$$

155 E_{α} and E_{β} are the erosion rates of the α to β side of drainage divide, respectively,

156 which can be derived through the cosmogenic nuclides (^{10}Be) concentration

157 measurements. The regional average erosion rate (\bar{E}) can also be used to calculate the

158 migration rate:

$$159 \quad D_{mr} = \frac{2\bar{E} \left[\frac{(A_{cr}^m s_{ch}^n)_{\alpha} - (A_{cr}^m s_{ch}^n)_{\beta}}{(A_{cr}^m s_{ch}^n)_{\alpha} + (A_{cr}^m s_{ch}^n)_{\beta}} \right] - \Delta U_{ch}}{\tan \alpha + \tan \beta} \quad (7)$$

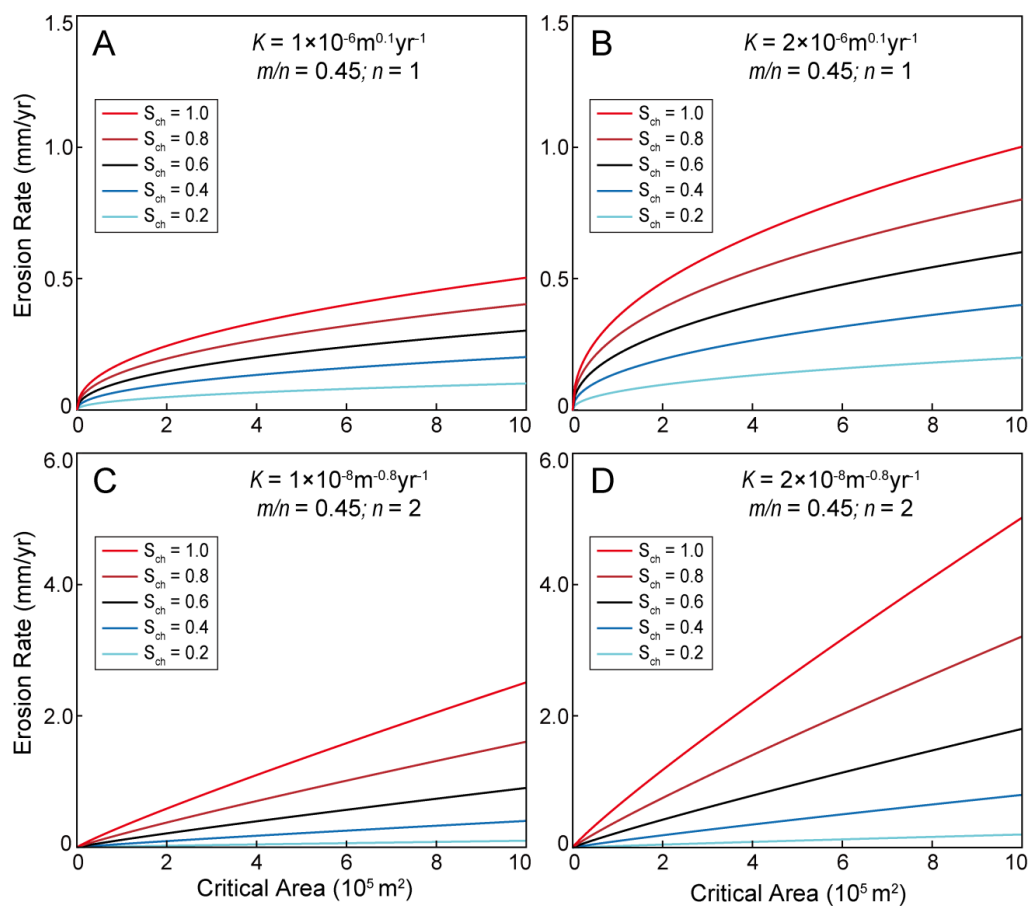
160 Based on Eqs. 4-7, the migration velocity of drainage divides can be estimated using

161 channel-head parameters combined with one of the erosion-related parameters

162 (erosion coefficient, erosion rate at one side of a drainage divide, or regional average

163 erosion rate).

164



165

166 **Figure 1.** Curves of the channel-head erosion rate (E_{ch}) against the critical area (A_{cr})

167 under different values of channel-head gradient (S_{ch}) and erosion coefficient (K). We

168 assume $m = 0.45$ and $n = 1$ in (A) and (B), and $m = 0.9$ and $n = 2$ in (C) and (D).

169

170 2.2 Channel-head-segment method

171 Zhou et al. (2022a) developed a method based on the cross-divide χ contrast of

172 channel-head segments to calculate the migration velocity of drainage divides. The

173 essence of the method is the cross-divide comparison of the channel-head segments'



174 steepness (k_{sn}) values. k_{sn} is a widely used index (Whipple et al., 1999; Wobus et al.,
 175 2006; Hilley and Arrowsmith, 2008; Kirby and Whipple, 2012) that is quantitatively
 176 related to erosion rate and erosion coefficient. Zhou et al. (2022a) proposed a cross-
 177 divide contrast of χ values, on behalf of the inverse of k_{sn} , which requires the same
 178 elevation of the channel heads and outlets across the drainage divide. Here, we release
 179 this restriction and make this method more applicable. When the regional erosion
 180 coefficient (K) is known and unchanged in the vicinity of the drainage divide, the
 181 drainage-divide migration rate can be estimated by the following equation:

$$182 \quad D_{mr} = \frac{K[k_{sn(\alpha)}^n - k_{sn(\beta)}^n] - \Delta U_{ch}}{\tan\alpha + \tan\beta} = \frac{K \left\{ \left[\frac{(z_{ch} - z_b)_\alpha}{\chi_\alpha} \right]^n - \left[\frac{(z_{ch} - z_b)_\beta}{\chi_\beta} \right]^n \right\} - \Delta U_{ch}}{\tan\alpha + \tan\beta} \quad (8)$$

183 where z_{ch} and z_b are the elevations of the channel heads and outlets, and χ is an
 184 integral function of channels' upstream area (A) to horizontal distance (x) (Perron and
 185 Royden, 2013; Willet et al., 2014). The drainage divide's unilateral erosion rate (E_α or
 186 E_β) can also be used as a substitution for the K value:

$$187 \quad D_{mr} = \frac{E_\alpha \left\{ 1 - \left(\frac{\chi_\alpha}{\chi_\beta} \right)^n \left[\frac{(z_{ch} - z_b)_\alpha}{(z_{ch} - z_b)_\beta} \right]^{-n} \right\} - \Delta U_{ch}}{\tan\alpha + \tan\beta} \quad (9)$$

188 or:

$$189 \quad D_{mr} = \frac{E_\beta \left\{ \left(\frac{\chi_\alpha}{\chi_\beta} \right)^{-n} \left[\frac{(z_{ch} - z_b)_\alpha}{(z_{ch} - z_b)_\beta} \right]^n - 1 \right\} - \Delta U_{ch}}{\tan\alpha + \tan\beta} \quad (10)$$

190 Alternatively, one can use the regional average erosion rate (\bar{E}) to calculate the
 191 migration rate:

$$192 \quad D_{mr} = \frac{2\bar{E} \left\{ \frac{\left[\frac{(z_{ch} - z_b)_\alpha}{(z_{ch} - z_b)_\beta} \right]^n - \left(\frac{\chi_\alpha}{\chi_\beta} \right)^n}{\left[\frac{(z_{ch} - z_b)_\alpha}{(z_{ch} - z_b)_\beta} \right]^n + \left(\frac{\chi_\alpha}{\chi_\beta} \right)^n} \right\} - \Delta U_{ch}}{\tan\alpha + \tan\beta} \quad (11)$$

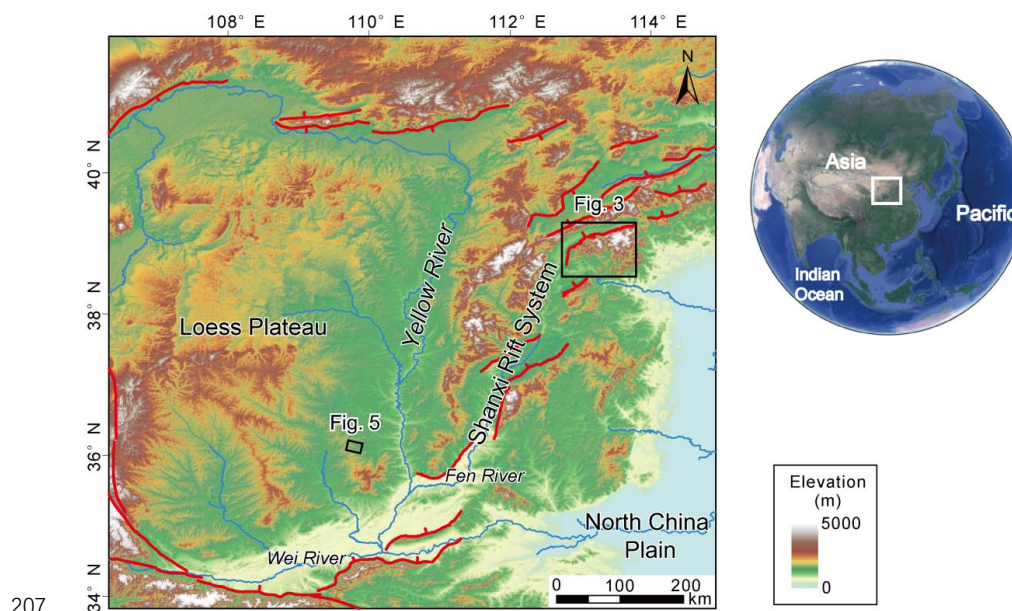


193 Based on Eqs. 8-11, the drainage-divide migration rate can be estimated using the χ
194 values of high-base-level channel segments combining with one of the erosion-related
195 parameters (erosion coefficient, erosion rate at one side of a drainage divide, or
196 regional average erosion rate).

197

198 **3. Application to natural cases**

199 We apply the new methods to two natural examples in North China, the Wutai
200 Shan, and the Loess Plateau (Fig. 2), to demonstrate how to calculate the drainage-
201 divide migration rates. We use UAV-acquired aerial photography and structure from
202 motion (SfM) photogrammetry to derive the sub-meter digital elevation model of the
203 two study areas. Based on the high-resolution topography data (sub-meter), we extract
204 the relevant parameters and calculate the drainage-divide migration rate using the two
205 methods above for each case. Analysis of the data is based on the Matlab toolbox
206 TAK ([Forte and Whipple, 2019](#)) and TopoToolbox ([Schwanghart and Scherler, 2014](#)).



207

208 **Figure 2.** Locations and tectonic background of the two nature cases in North China.

209 Red curves represent the main active faults. Black rectangles show the locations of the

210 two nature cases.

211

212 **3.1 Wutai Shan**

213 The Wutai Shan is a tilted fault block on the shoulder of the Shanxi Rift System

214 located in the central North China craton (Xu et al., 1993; Su et al., 2021). The tilting

215 uplift of the Wutai Shan is controlled by the Northern Wutai Shan fault (Fig. 3A), and

216 there is no active fault along the south edge of the Wutai Shan horst. The bedrock of

217 the Wutai Shan area is mainly metamorphic and igneous basement rocks (Clinkscales

218 et al., 2020; Zhou et al 2022a) and there is no obvious variation in rock erodibility and

219 precipitation in this area.



220 To derive the erosion coefficient of the Wutai Shan area, we calculate the
221 channel steepness values of this region and use the Kriging interpolation technique to
222 generate the k_{sn} distribution map (Fig. 3B). According to a low-temperature
223 thermochronology study of the Wutai Shan (Clinkscates et al., 2020), the erosion rate
224 of the sampling area (in the footwall block of the northern boundary fault of the Wutai
225 Shan) is about 0.25 mm/yr in the late Cenozoic. The average k_{sn} value of this area is
226 $\sim 80 \text{ m}^{0.9}$ (Fig. 3). According to the approach of previous studies (Kirby and Whipple,
227 2001; Kirkpatrick et al., 2020; Ma et al., 2020), the erosion coefficient is $\sim 3 \times 10^{-6}$
228 $\text{m}^{0.1} \text{yr}^{-1}$ in the Wutai Shan area.

229 We then apply the two above methods in this area to calculate the migration
230 velocity of the drainage divide in the Wutai Shan. We first randomly choose three
231 pairs of rivers (Fig. 4A) and make their slope-area plots (Figs. 4B, E, H) and the χ -
232 plots (Figs. 4C, F, I). According to the breaking point of the slope-area plot (Duvall et
233 al., 2004) and its corresponding position on the χ -plot, we can separate hillslope and
234 channel areas and mark the position of the channel heads on the plots and the
235 topography map (Fig. 4A). For the slope-area plots, we derive the value of critical
236 upstream drainage area (A_{cr}) according to the position of the channel heads. Because
237 the slopes of the channel-head points varies, we use the average slope of the hillslope
238 area as the value of channel-head gradient (S_{ch}). Moreover, for the χ -plots (Figs. 4C, F,
239 I), we obtain the elevations of outlets (z_b) and channel heads (z_{ch}) of the channel
240 segment, and the χ value according to the position of the channel-head points.

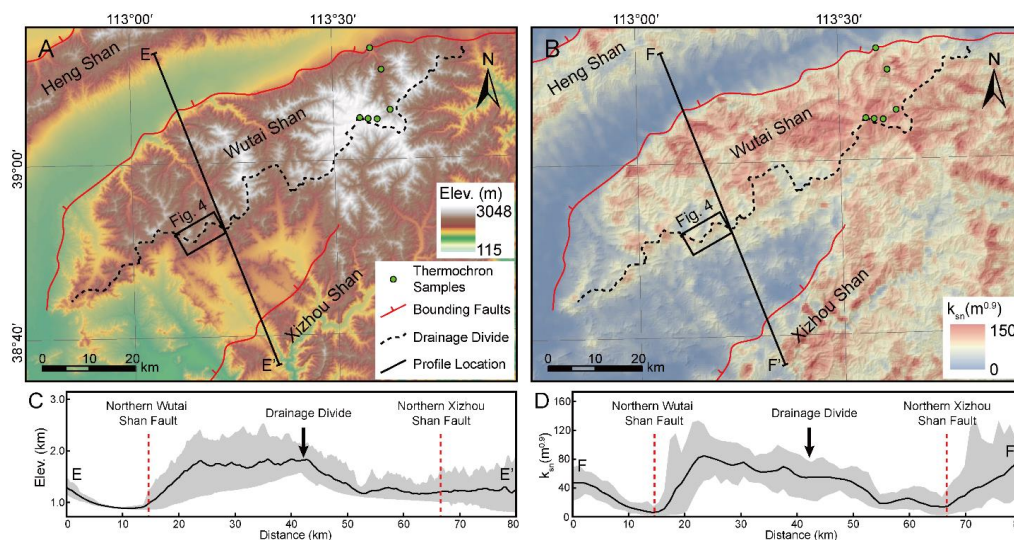
241 If we assume the rock uplift rate decreases linearly from 0.25 to 0 mm/yr from



242 northwest to southeast of the Wutai Shan horst (~40 km wide), the cross-divide uplift
243 difference in the channel-head points (ΔU_{ch}) (the distance along the normal direction
244 of the boundary fault is ~600 m) is ~0.004 mm/yr. The $\tan\alpha$ and $\tan\beta$ are in line with
245 the gradient of channel-head points (S_{ch}) on each side of the drainage divide (Figs.
246 4D, G, J). We assume $n = 1$ and $m = 0.45$ in the calculation following previous studies
247 (Wobus et al., 2006; DiBiase et al., 2010; Perron and Royden, 2013; Wang et al.,
248 2021). After determining these parameters, we adopt the channel-head (Eq. 4) and
249 channel-head-segment (Eq. 8) methods to calculate the migration rates. The required
250 data for calculation and the migration rates are shown in Table 1.

251 Both the slope-area plots (Figs. 4B, E, H) and the χ -plots (Figs. 4C, F, I) show
252 that distinct character of the rivers across the drainage divide. For the first site (Fig.
253 4D), the migration rates calculated by both the channel-head and channel-head-
254 segment methods are 0.12 mm/yr (northward). For the second site (Fig. 4G), the
255 migration rates derived from the two methods are 0.11 mm/yr and 0.13 mm/yr
256 (northward), respectively. For the third site (Fig. 4J), the migration rates are 0.12
257 mm/yr and 0.10 mm/yr (northward), respectively. The drainage divides of all three
258 points are predicted to migrate northward, which is consistent with previous result
259 inferred by the cross-divide contrast of slopes (Zhou et al., 2022b). Furthermore, the
260 migration velocities calculated by the two methods are comparable in all three sites.

261



262

263 **Figure 3.** (A & B) Topography and normalized channel steepness (k_{sn}) distribution of

264 the Wutai Shan horst and surrounding area. The black dashed curve shows the

265 location of the main drainage divide. Red curves show the main bounding faults. The

266 black straight lines show the location of the profiles E-E' and F-F'. Black rectangles

267 show the area of aerial photography (Fig. 4A). Green dots denote the locations of the

268 low-temperature thermochronology samples in Clinkscales et al. (2020). The

269 topography data (ALOS DEM, 12.5 m resolution) is downloaded from the Alaska

270 Satellite Facility (ASF) Data Search (<https://search.asf.alaska.edu>). The k_{sn} is

271 calculated using TopoToolbox (Schwanghart and Scherler, 2014) based on Matlab,

272 and the interpolation uses the Kriging method. (C) The topography swath profile

273 along E-E' in Fig. 3A. (D) The k_{sn} swath profile along F-F' in Fig. 3B. The red dotted

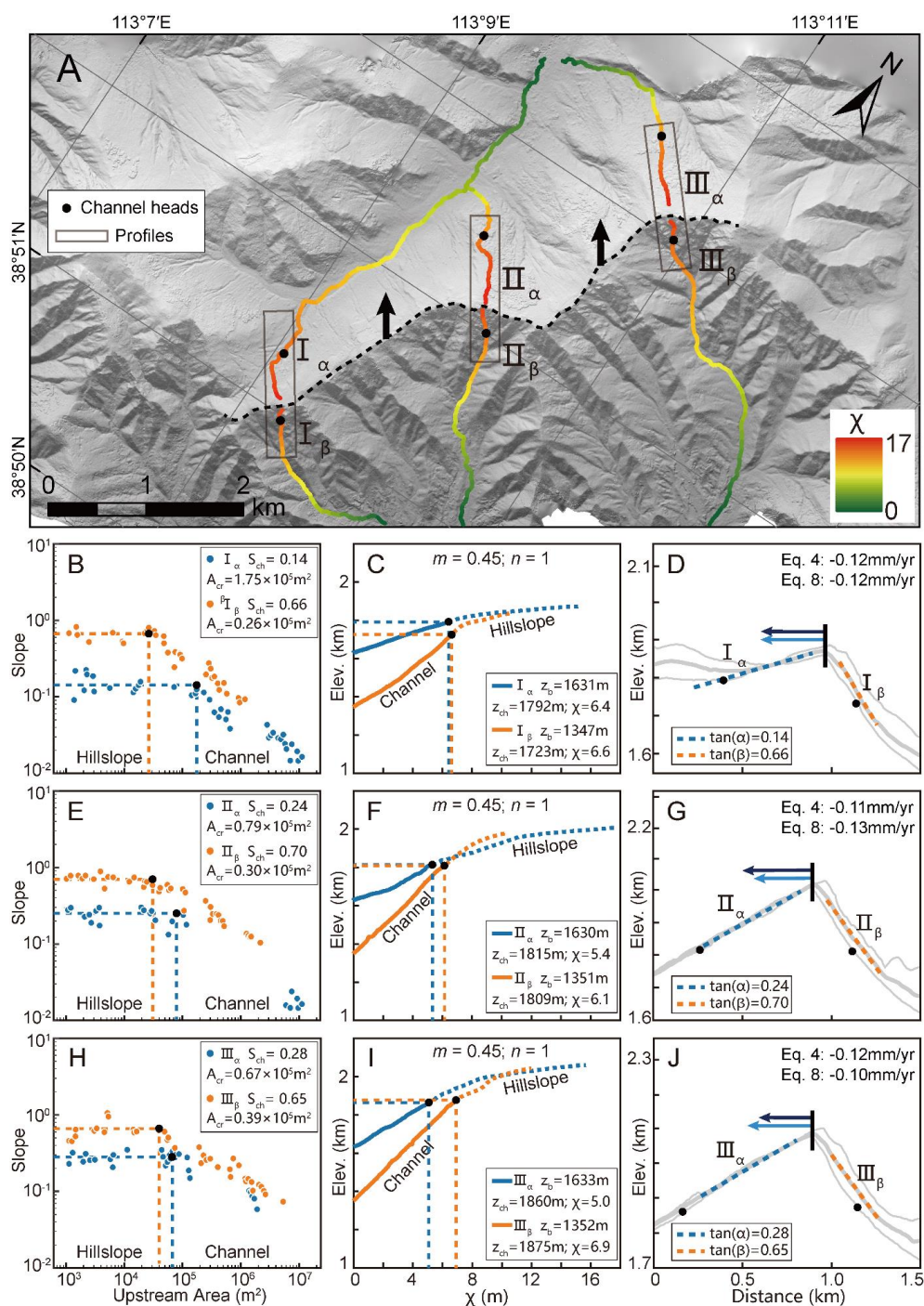
274 line shows the location of the main bounding faults and the black arrow shows the

275 location of the main drainage divide. Both swath profiles are 20 km wide (10 km on

276 each side).



277



278



279 **Figure 4.** Analytical results of the Wutai Shan. **(A)** High-resolution topographic map
280 (sub-meter) of the Wutai Shan. The black dashed curve shows the location of the main
281 drainage divide. Colored curves show the three pairs of selected channels used for
282 analysis. The black dots are the channel heads. Black rectangles show the location of
283 the cross-divide topography swath profiles. The black arrows show the direction of
284 drainage-divide migration **(B, E, H)** Slope-area plots of the three pairs of selected
285 channels. The blue and orange dots are the slope-area plots of the north (α) and south
286 (β) sides of the drainage divide respectively. The black dots represent the channel
287 heads. **(C, F, I)** χ -plots of the selected channels. The blue and orange curves are the χ -
288 plots of the north (α) and south (β) sides of the drainage divide respectively. The black
289 dots represent the channel heads. **(D, G, J)** Cross-divide topography swath profiles
290 with the drainage-divide migration rates. The locations of the profiles are in Fig. 4A.
291 The light and dark blue arrows are the drainage-divide migration rates calculated by
292 the channel-head (Eq. 4) and channel-head-segment (Eq. 8) method respectively.

293

294 **3.2 An unnamed mountain range in the Loess Plateau**

295 The Loess Plateau is hosted by the tectonically stable Ordos Block of the North
296 China craton (Yin, 2010 Su et al., 2021). It accumulates tens to hundreds of meters of
297 eolian sediments over the past 2.6 million years (Yan et al., 2014), draping preexisting
298 topography (Xiong et al., 2014). There is no active fault within the study area. The
299 lithology of the study site is mainly loess; there is little to no variation in rock



300 erodibility and precipitation within the area (Shi et al., 2020; Zhou et al., 2022b).

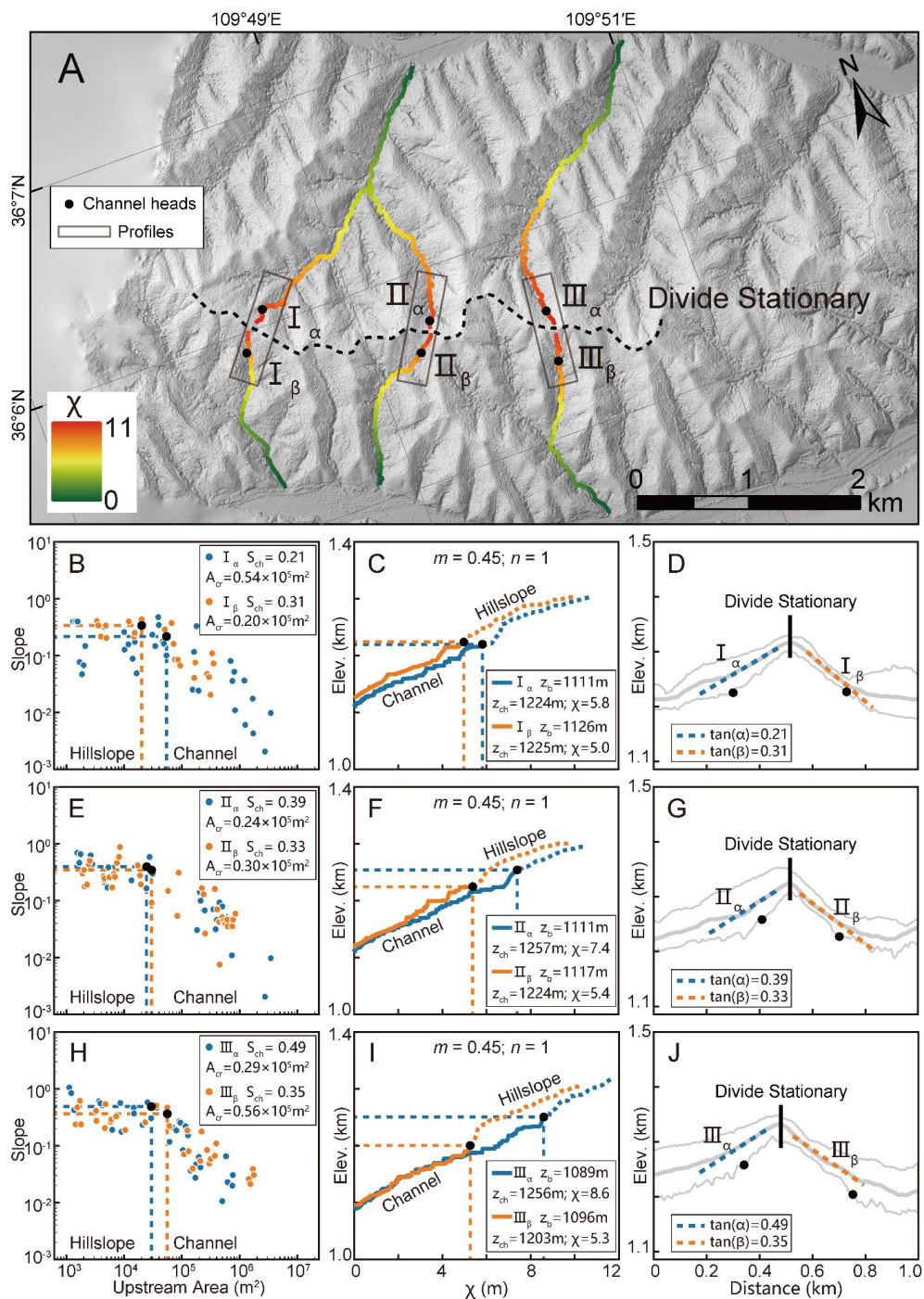
301 We apply the two methods in this area to calculate the drainage-divide migration
302 rate. Similar to the Wutai Shan case, we first randomly choose three pairs of rivers
303 and make their slope-area plots (Figs. 5 B, E, H) and the χ -plots (Figs. 5 C, F, I). Then
304 we mark the position of the channel-head points on the topography map (Fig. 5A),
305 slope-area plots, and χ -plots. According to its position, we derive the A_{er} values from
306 the slope-area plots (Figs. 5 B, E, H) and the χ values and the elevations of channel-
307 head segments' outlets (z_b) and heads (z_{ch}) from the χ -plots (Figs. 5 C, F, I). We also
308 acquire the average slope of the hillslope area and derive the S_{ch} , $\tan\alpha$, and $\tan\beta$
309 values.

310 The rate of soil erosion in the study area is about $500 \text{ t}\cdot\text{km}^{-2}\cdot\text{yr}^{-1}$ (Fu, 1989). If we
311 assume the density of Loess is $1.65 \text{ t}\cdot\text{m}^{-3}$, the average erosion rate here is about 0.3
312 $\text{mm}\cdot\text{yr}^{-1}$. Because there is no obvious unequal uplift in this region, we assume that
313 ΔU_{ch} is zero. We also assume $n = 1$ and $m = 0.45$ in the calculation. Then, we use the
314 methods of channel-head parameters (Eq. 7) and channel segments (Eq. 11) to
315 calculate the drainage-divide migration rates. The required data for calculation and the
316 migration rates are shown in Table 1.

317 All results of the three points show that the drainage-divide migration rate here is
318 close to zero, no matter which method is used in the calculation. The results show that
319 the drainage divide of the study site is in topographical equilibrium, which is
320 consistent with the inference in previous studies (Willett et al., 2014, Zhou et al.,
321 2022b).



322



323



324 **Figure 5.** Analytical results of a mountain range in the Loess Plateau. (A) High-
325 resolution topographic map (sub-meter). The black dotted curve shows the location of
326 the main drainage divide. Colored curves show the three pairs of selected channels
327 used for analysis. The black dots represent the channel heads. Black rectangles show
328 the location of the cross-divide topography swath profiles. (B, E, H) Slope-area plots
329 of the three pairs of selected channels. The blue and orange dots are the data of the
330 north (α) and south (β) sides of the drainage divide respectively. The black dots
331 represent the channel heads. (C, F, I) χ -plots of the selected channels. The blue and
332 orange curves are the χ -plots of the north (α) and south (β) sides of the drainage
333 divide respectively. The black dots represent the channel heads. (D, G, J) The cross-
334 divide topography swath profiles. The locations of the swath profiles are in Panel A.
335



336 **Table 1.** Channel’s parameters and the migration rates of the drainage divides of the
 337 two natural cases.

	No.	A_{cr} ($\times 10^6 \text{m}^2$)	S_{ch}	z_b (m)	z_{ch} (m)	χ	$\tan\alpha$	$\tan\beta$	ΔU_{ch} (mm/yr)	D_{mr} (mm/yr) (Channel-head method)	D_{mr} (mm/yr) (Channel-head- segment method)
Wutai Shan	Fig. 4 I $_{\alpha}$	1.75	0.14	1631	1792	6.4	0.14	0.66	~0.004	-0.12	-0.12
	Fig. 4 I $_{\beta}$	0.26	0.66	1347	1723	6.6					
	Fig. 4 II $_{\alpha}$	0.79	0.24	1630	1815	5.4	0.24	0.70			
	Fig. 4 II $_{\beta}$	0.30	0.70	1351	1809	6.1					
	Fig. 4 III $_{\alpha}$	0.67	0.28	1633	1860	5.0	0.28	0.65			
	Fig. 4 III $_{\beta}$	0.39	0.65	1352	1875	6.9					
Loess Plateau	Fig. 5 I $_{\alpha}$	0.54	0.21	1111	1224	5.8	0.21	0.31	0	0.02	-0.01
	Fig. 5 I $_{\beta}$	0.20	0.31	1126	1225	5.0					
	Fig. 5 II $_{\alpha}$	0.24	0.39	1111	1257	7.4	0.39	0.33			
	Fig. 5 II $_{\beta}$	0.30	0.33	1117	1224	5.4					
	Fig. 5 III $_{\alpha}$	0.29	0.49	1089	1256	8.6	0.49	0.35			
	Fig. 5 III $_{\beta}$	0.56	0.35	1096	1203	5.3					

338



339 4. Discussion

340 4.1 Location of channel heads

341 Willett et al. (2014) pioneered the use of cross-divide χ contrast to gauge the
342 horizontal motion of drainage divides. According to their method, drainage divides
343 are predicted to move toward the side with a higher χ value to achieve geomorphic
344 equilibrium. However, in a region with spatially variable uplift rates, lithology, or
345 precipitation, χ contrast may fail to reflect the drainage-divide migration (Willett et
346 al., 2014; Whipple et al., 2017; Forte and Whipple, 2018; Zhou and Tan, 2023). In the
347 tectonically active area, the cross-divide χ contrast can only be used in a small area
348 where rock type, precipitation, and uplift rate are nearly uniform (Willett et al., 2014).
349 Forte and Whipple (2018) proposed the Gilbert metrics to measure the stability of
350 drainage divides. Zhou et al. (2022a) combined the advantages of the χ and Gilbert
351 metrics methods, proposed to use the χ contrast with a high base level to calculate the
352 k_{sn} values at the channel heads on both sides of a drainage divide, and quantified the
353 migration rate of drainage divides at the eastern margin of Tibet.

354 To reduce the cross-divide difference in uplift rate, precipitation, and rock
355 strength, these methods should compare the parameters of points (slope, relief,
356 elevation, and k_{sn}) on both sides of the divide as closely as possible. As the hillslope
357 area (above the channel head) does not follow Eq. 1 (Stoke and Dietrich, 2006; Stark,
358 2010; Braun et al., 2018; Dahlquist et al., 2018)), the channel heads are the closest
359 point to the divide, following Eq. 1. Channel heads, therefore, are suitable for



360 measuring the drainage-divide stability with the parameters of the upstream drainage
361 area and channel gradient (Forte and Whipple, 2018; Zhou et al., 2022a; this study).
362 However, the location of the channel heads is usually based on empirical parameters,
363 which may introduce errors in the result of drainage-divide stability. In this study, we
364 advocate the use of high-resolution DEM to determine a more accurate position and
365 related parameters of the channel head, given that the use of UAVs to obtain the local
366 DEM has become highly efficient. We advance the theory to calculate the drainage-
367 divide migration rate based on the measured channel-head parameters. With the help
368 of the aerial photography of UAVs and the SfM techniques, one can obtain the sub-
369 meter resolution topography data of drainage divides (Figs. 4A & 5A) and get the
370 required parameters (including the exact locations of the channel heads across the
371 drainage divide) through topography analysis, which could improve the quantitative
372 research on the drainage-divide migration. Furthermore, the method provides a new
373 avenue to combine with catchment-wide ^{10}Be erosion rate or low-temperature
374 thermochronology data to calculate the migration rate, which has great potentials of
375 application in places where some variables are hard to be constrained.

376

377 **4.2 Cross-divide difference in uplift rate of the channel heads**

378 Although the channel heads across the divide are very close on the spatial scale of
379 an orogenic belt, differential uplift between the channel heads (ΔU_{ch}) could still exist,
380 especially in a tilting horst, such as the Wutai Shan. The cross-divide difference in



381 uplift rate could impact the calculation of the migration rate of drainage divides (Zhou
382 et al., 2022a). Although the differential uplift rate is usually small enough to be
383 ignored in some natural cases, its influence on the migration rate of drainage divides
384 should be taken into account theoretically (Zhou et al., 2022a).

385 In this study, we quantify the influence of cross-divide difference in rock uplift
386 rate (ΔU_{ch}) on the calculation of the migration rate of drainage divides at the Wutai
387 Shan, benefiting from the available tectonic and chronological research (Clinkscales
388 et al., 2020) and the newly obtained high-resolution topographic data. In the Wutai
389 Shan horst, ΔU_{ch} across the drainage divide is ~ 0.004 mm/yr. We estimated the
390 influence of ΔU_{ch} on the drainage-divide migration rate in the case study of the Wutai
391 Shan, which can reduce the error theoretically. If ΔU_{ch} is ignored, the drainage-divide
392 migration rate would decrease by $\sim 4\%$ in the Wutai Shan case. Although $\sim 4\%$ seems
393 to be negligible, such a ratio will increase if the mountain belt is narrower, the tilting
394 uplift is stronger, or the divide is closer to the steady state (i.e., the migration rate is
395 lower). In other words, the differential uplift may play a significant influence on the
396 measurement of drainage-divide stability in some situations. Consider an extreme
397 example: when the main drainage divide of a tilting mountain range (relatively narrow
398 in width) is at a steady state, the gradient, relief, and elevation of the channel heads
399 (collectively called “Gilbert metrics” (Forte and Whipple, 2018)) will show a
400 systematic cross-divide difference in theory. In this case, the drainage divide would be
401 considered unstable if ΔU_{ch} were neglected. Therefore, ΔU_{ch} should be taken into
402 account, either in a qualitative or a quantitative evaluation of the stability of drainage



403 divides using the parameters on the channel heads.

404

405 **5. Conclusions**

406 We have developed a new method to calculate the migration rate of drainage
407 divides based upon channel-head parameters. We have also improved the channel-
408 head-segment method in the previous study (Zhou et al., 2022a) to adapt the theory to
409 areas where the elevations of outlets and channel heads are different across the
410 drainage divide.

411 Using the high-resolution topographic data, we determined the exact locations of
412 the channel heads on both sides of the drainage divide and quantified the drainage-
413 divide migration rates in two natural cases (the Wutai Shan in the Shanxi Rift System,
414 and an unnamed mountain range in the Loess Plateau). The migration rates of the
415 study sites in the Wutai Shan are 0.10-0.13 mm/yr (moving north). The rates are close
416 to zero in the Loess Plateau.

417 Based on the locations of the channel heads and the uplift gradient of the
418 mountain, we calculated the cross-divide difference in uplift rate at the channel heads
419 (ΔU_{ch}), which is taken into account in the calculation of the drainage-divide migration
420 rate for the first time. If ΔU_{ch} is overlooked, the drainage-divide migration rate would
421 be underestimated. We suggest that ΔU_{ch} should be considered if one aims to assess
422 the stability of drainage divides based on the cross-divide difference in channel-head
423 parameters.



424

425 **Data availability.** The analysis of data is based on the Matlab toolbox TAK (Forte
426 and Whipple, 2019) and TopoToolbox (Schwanghart and Scherler, 2014). The
427 topography data (ALOS DEM, 12.5 m resolution) is downloaded from the Alaska
428 Satellite Facility (ASF) Data Search (<https://search.asf.alaska.edu/>).

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433 **Author contributions.** XT and CZ contributed to the design of research scheme.
434 CZ performed the geomorphic analyses. CZ, XT, and FS carried out field data
435 collection. CZ, XT, YL, and FS contributed to the text and reviewed the paper.

436

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