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Supplementary Information

2 **The role of lithospheric thermal structure in the development of lateral**

3 **heterogeneous of the continental collision system**

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Table S1. Parameter list of the numerical experiments

Material	Units	Sub-lithospheric	Continental	Continental	Lithospheric			
Parameters		Mantle	upper	lower	Mantle	Sediment	Oceanic	Weak
			Crust	Crust			Crust	Zone
Thickness	km	-	25	10	85, 88	4	8	80
Thermal	$\text{m}^2 \text{s}^{-1}$	$9.89 \cdot 10^{-7}$	$1.21 \cdot 10^{-6}$	$1.15 \cdot 10^{-6}$	$9.87 \cdot 10^{-7}$		$1.21 \cdot 10^{-6}$	$1.21 \cdot 10^{-6}$
Diffusivities(κ)								
Heat	J	1250	750	750	1250	750	750	750
Capacity (C_p)	$\text{kg}^{-1} \text{K}^{-1}$							
Density(ρ)	kg m^{-3}	3370	2800	2900	3370	3000	3000	3300
Thermal								
expansivity(α)	K^{-1}	$3 \cdot 10^{-5}$	$2.7 \cdot 10^{-5}$	$2.7 \cdot 10^{-5}$	$3 \cdot 10^{-5}$	$2.7 \cdot 10^{-5}$	$2.7 \cdot 10^{-5}$	$2.7 \cdot 10^{-5}$
Angle of internal	$^\circ$	30	30	30	30	2	2	2
friction(ϕ)								
Cohesion (C)	Pa	$20 \cdot 10^6$	$20 \cdot 10^6$	$20 \cdot 10^6$	$20 \cdot 10^6$	$10 \cdot 10^6$	$10 \cdot 10^6$	$10 \cdot 10^6$
Flow Law ^a	-	dry olivine(diff/disl)	wet quartzite	wet anorthite	dry olivine(diff/disl)	gabbro	gabbro	gabbro

Visc.prefactor (A*) ^b	Pa ⁻ⁿ S ⁻¹	2.37·10 ⁻¹⁵ /6.52·10 ⁻¹⁶	8.57·10 ⁻²⁸	7.13·10 ⁻¹⁸	2.37·10 ⁻¹⁵ /6.52·10 ⁻¹⁶	1.0·10 ⁵⁰ /1.12·10 ⁻¹⁰	1.0·10 ⁵⁰ /1.1	1.0·10 ⁵⁰ /1.1
Stress exponent (n)	-	1/3.5	1/4.0	1/3	1/3.5	1/3.4	1/3.4	1/3.4
Activation Energy (E)	J mol ⁻¹	375·10 ³ /530·10 ³	0/223·10 ³	0/345·10 ³	375·10 ³ /530·10 ³	497·10 ³	497·10 ³	497·10 ³
Activation Volume (V)	m ³ mol ⁻¹	4·10 ⁻⁶ /18·10 ⁻⁶	0/0	0/0	4·10 ⁻⁶ /18·10 ⁻⁶	0/0	0/0	0/0
Grain size exponent(m)	-	3/-	1/-	1/-	3/-	1/-	1/-	1/-
Radioactive heating production (H)	W m ⁻³	0	varies	varies	0	0	0	0

10 ^a Flow law are taken from *Hirth and Kohlstedt* [2003] for dry olivine, *Gleason and Tullis* [1995] for wet quartzite, *Rybacki et al.* [2006] for wet anorthite, *Wilks and*

11 *Carter* [1990] for gabbro.

12 ^b The viscosity prefactor, A*, is scaled from uniaxial experiments for plane strain as in *Ranalli* [1995] and *Tetreault and Buiter* [2012].

Table S2. List of the numerical experiments

Mode name	$T_{\text{pro_moho}} (\text{°C})$	$T_{\text{retro_moho}} (\text{°C})$	$H_{\text{pro-uc}} (\text{W m}^{-3})$	$H_{\text{retro-lc}} (\text{W m}^{-3})$	$H_{\text{pro-lc}} (\text{W m}^{-3})$	$H_{\text{pro-lc}} (\text{W m}^{-3})$	Collision Patterns
m1	450	450	$1.0 \cdot 10^{-6}$	$1.0 \cdot 10^{-6}$	$4.0 \cdot 10^{-7}$	$4.0 \cdot 10^{-7}$	I
m2	450	500	$1.0 \cdot 10^{-6}$	$1.0 \cdot 10^{-6}$	$4.0 \cdot 10^{-7}$	$4.0 \cdot 10^{-7}$	I
m3	450	550	$1.0 \cdot 10^{-6}$	$1.0 \cdot 10^{-6}$	$4.0 \cdot 10^{-7}$	$4.0 \cdot 10^{-7}$	I
m4	450	600	$1.0 \cdot 10^{-6}$	$1.0 \cdot 10^{-6}$	$4.0 \cdot 10^{-7}$	$4.0 \cdot 10^{-7}$	I
m5	500	450	$1.0 \cdot 10^{-6}$	$1.0 \cdot 10^{-6}$	$4.0 \cdot 10^{-7}$	$4.0 \cdot 10^{-7}$	II
m6	500	500	$1.0 \cdot 10^{-6}$	$1.0 \cdot 10^{-6}$	$4.0 \cdot 10^{-7}$	$4.0 \cdot 10^{-7}$	I
m7	500	550	$1.0 \cdot 10^{-6}$	$1.0 \cdot 10^{-6}$	$4.0 \cdot 10^{-7}$	$4.0 \cdot 10^{-7}$	I

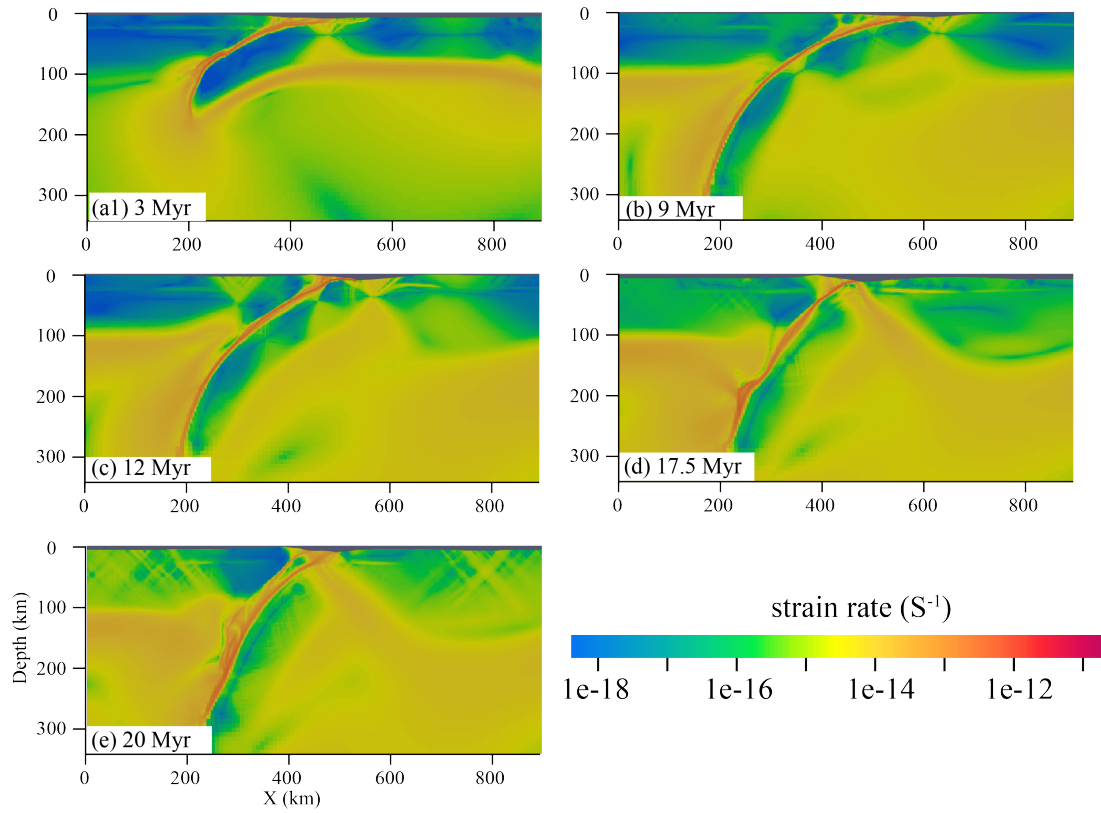
m8	500	600	$1.0 \cdot 10^{-6}$	$1.0 \cdot 10^{-6}$	$4.0 \cdot 10^{-7}$	$4.0 \cdot 10^{-7}$	I
m9	550	450	$1.0 \cdot 10^{-6}$	$1.0 \cdot 10^{-6}$	$4.0 \cdot 10^{-7}$	$4.0 \cdot 10^{-7}$	I
m10	550	500	$1.0 \cdot 10^{-6}$	$1.0 \cdot 10^{-6}$	$4.0 \cdot 10^{-7}$	$4.0 \cdot 10^{-7}$	II
m11	550	550	$1.0 \cdot 10^{-6}$	$1.0 \cdot 10^{-6}$	$4.0 \cdot 10^{-7}$	$4.0 \cdot 10^{-7}$	I
m12	550	600	$1.0 \cdot 10^{-6}$	$1.0 \cdot 10^{-6}$	$4.0 \cdot 10^{-7}$	$4.0 \cdot 10^{-7}$	I
m13	600	450	$1.0 \cdot 10^{-6}$	$1.0 \cdot 10^{-6}$	$4.0 \cdot 10^{-7}$	$4.0 \cdot 10^{-7}$	I
m14	600	500	$1.0 \cdot 10^{-6}$	$1.0 \cdot 10^{-6}$	$4.0 \cdot 10^{-7}$	$4.0 \cdot 10^{-7}$	II
m15	600	550	$1.0 \cdot 10^{-6}$	$1.0 \cdot 10^{-6}$	$4.0 \cdot 10^{-7}$	$4.0 \cdot 10^{-7}$	I
m16	600	600	$1.0 \cdot 10^{-6}$	$1.0 \cdot 10^{-6}$	$4.0 \cdot 10^{-7}$	$4.0 \cdot 10^{-7}$	I

m17	450	500	$1.5 \cdot 10^{-6}$	$1.0 \cdot 10^{-6}$	$4.0 \cdot 10^{-7}$	$4.0 \cdot 10^{-7}$	II
m18	450	500	$2.0 \cdot 10^{-6}$	$1.0 \cdot 10^{-6}$	$4.0 \cdot 10^{-7}$	$4.0 \cdot 10^{-7}$	II
m19	450	500	$3.0 \cdot 10^{-6}$	$1.0 \cdot 10^{-6}$	$4.0 \cdot 10^{-7}$	$4.0 \cdot 10^{-7}$	II
m20	450	500	$4.0 \cdot 10^{-6}$	$1.0 \cdot 10^{-6}$	$4.0 \cdot 10^{-7}$	$4.0 \cdot 10^{-7}$	II
m21	450	500	$1.0 \cdot 10^{-6}$	$1.5 \cdot 10^{-6}$	$4.0 \cdot 10^{-7}$	$4.0 \cdot 10^{-7}$	II
m22	450	500	$1.5 \cdot 10^{-6}$	$1.5 \cdot 10^{-6}$	$4.0 \cdot 10^{-7}$	$4.0 \cdot 10^{-7}$	II
m23	450	500	$2.0 \cdot 10^{-6}$	$1.5 \cdot 10^{-6}$	$4.0 \cdot 10^{-7}$	$4.0 \cdot 10^{-7}$	II
m24	450	500	$3.0 \cdot 10^{-6}$	$1.5 \cdot 10^{-6}$	$4.0 \cdot 10^{-7}$	$4.0 \cdot 10^{-7}$	II
m25	450	500	$4.0 \cdot 10^{-6}$	$1.5 \cdot 10^{-6}$	$4.0 \cdot 10^{-7}$	$4.0 \cdot 10^{-7}$	II

m26	450	500	$1.0 \cdot 10^{-6}$	$2.0 \cdot 10^{-6}$	$4.0 \cdot 10^{-7}$	$4.0 \cdot 10^{-7}$	I
m27	450	500	$1.5 \cdot 10^{-6}$	$2.0 \cdot 10^{-6}$	$4.0 \cdot 10^{-7}$	$4.0 \cdot 10^{-7}$	II
m28	450	500	$2.0 \cdot 10^{-6}$	$2.0 \cdot 10^{-6}$	$4.0 \cdot 10^{-7}$	$4.0 \cdot 10^{-7}$	II
m29	450	500	$3.0 \cdot 10^{-6}$	$2.0 \cdot 10^{-6}$	$4.0 \cdot 10^{-7}$	$4.0 \cdot 10^{-7}$	II
m30	450	500	$4.0 \cdot 10^{-6}$	$2.0 \cdot 10^{-6}$	$4.0 \cdot 10^{-7}$	$4.0 \cdot 10^{-7}$	II
m31	450	500	$1.0 \cdot 10^{-6}$	$3.0 \cdot 10^{-6}$	$4.0 \cdot 10^{-7}$	$4.0 \cdot 10^{-7}$	I
m32	450	500	$1.5 \cdot 10^{-6}$	$3.0 \cdot 10^{-6}$	$4.0 \cdot 10^{-7}$	$4.0 \cdot 10^{-7}$	II
m33	450	500	$2.0 \cdot 10^{-6}$	$3.0 \cdot 10^{-6}$	$4.0 \cdot 10^{-7}$	$4.0 \cdot 10^{-7}$	II
m34	450	500	$3.0 \cdot 10^{-6}$	$3.0 \cdot 10^{-6}$	$4.0 \cdot 10^{-7}$	$4.0 \cdot 10^{-7}$	II

m35	450	500	$4.0 \cdot 10^{-6}$	$3.0 \cdot 10^{-6}$	$4.0 \cdot 10^{-7}$	$4.0 \cdot 10^{-7}$	II
m36	450	500	$1.0 \cdot 10^{-6}$	$4.0 \cdot 10^{-6}$	$4.0 \cdot 10^{-7}$	$4.0 \cdot 10^{-7}$	II
m37	450	500	$1.5 \cdot 10^{-6}$	$4.0 \cdot 10^{-6}$	$4.0 \cdot 10^{-7}$	$4.0 \cdot 10^{-7}$	II
m38	450	500	$2.0 \cdot 10^{-6}$	$4.0 \cdot 10^{-6}$	$4.0 \cdot 10^{-7}$	$4.0 \cdot 10^{-7}$	II
m39	450	500	$3.0 \cdot 10^{-6}$	$4.0 \cdot 10^{-6}$	$4.0 \cdot 10^{-7}$	$4.0 \cdot 10^{-7}$	II
m40	450	500	$4.0 \cdot 10^{-6}$	$4.0 \cdot 10^{-6}$	$4.0 \cdot 10^{-7}$	$4.0 \cdot 10^{-7}$	II
m41	450	500	$1.0 \cdot 10^{-6}$	$1.0 \cdot 10^{-6}$	$2.0 \cdot 10^{-7}$	$4.0 \cdot 10^{-7}$	II
m42	450	500	$1.0 \cdot 10^{-6}$	$1.0 \cdot 10^{-6}$	$6.0 \cdot 10^{-7}$	$4.0 \cdot 10^{-7}$	II
m43	450	500	$1.0 \cdot 10^{-6}$	$1.0 \cdot 10^{-6}$	$2.0 \cdot 10^{-7}$	$2.0 \cdot 10^{-7}$	II

m44	450	500	$1.0 \cdot 10^{-6}$	$1.0 \cdot 10^{-6}$	$4.0 \cdot 10^{-7}$	$2.0 \cdot 10^{-7}$	II
m45	450	500	$1.0 \cdot 10^{-6}$	$1.0 \cdot 10^{-6}$	$6.0 \cdot 10^{-7}$	$2.0 \cdot 10^{-7}$	II
m46	450	500	$1.0 \cdot 10^{-6}$	$1.0 \cdot 10^{-6}$	$2.0 \cdot 10^{-7}$	$6.0 \cdot 10^{-7}$	II
m47	450	500	$1.0 \cdot 10^{-6}$	$1.0 \cdot 10^{-6}$	$4.0 \cdot 10^{-7}$	$6.0 \cdot 10^{-7}$	II
m48	450	500	$1.0 \cdot 10^{-6}$	$1.0 \cdot 10^{-6}$	$6.0 \cdot 10^{-7}$	$6.0 \cdot 10^{-7}$	II

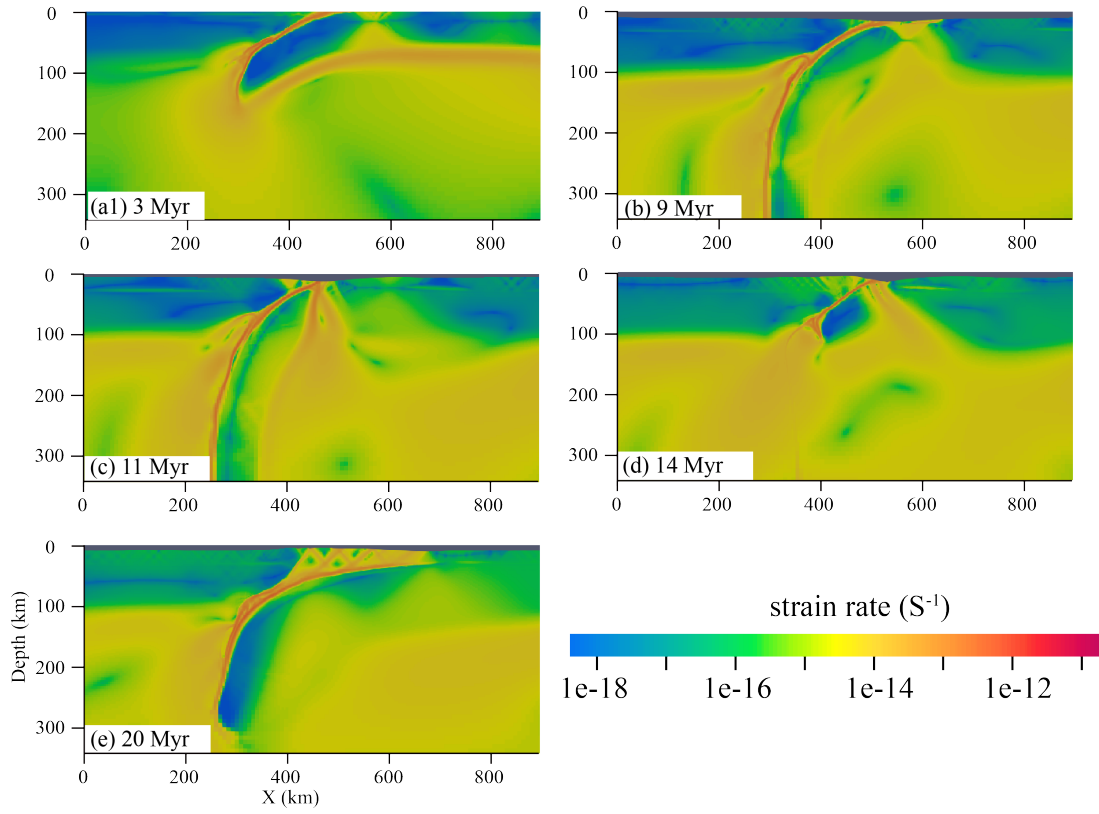


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Figure S1. Strain rate for Model m2 at selected model times.

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Figure S2. Strain rate for Model m7 at selected model times.

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