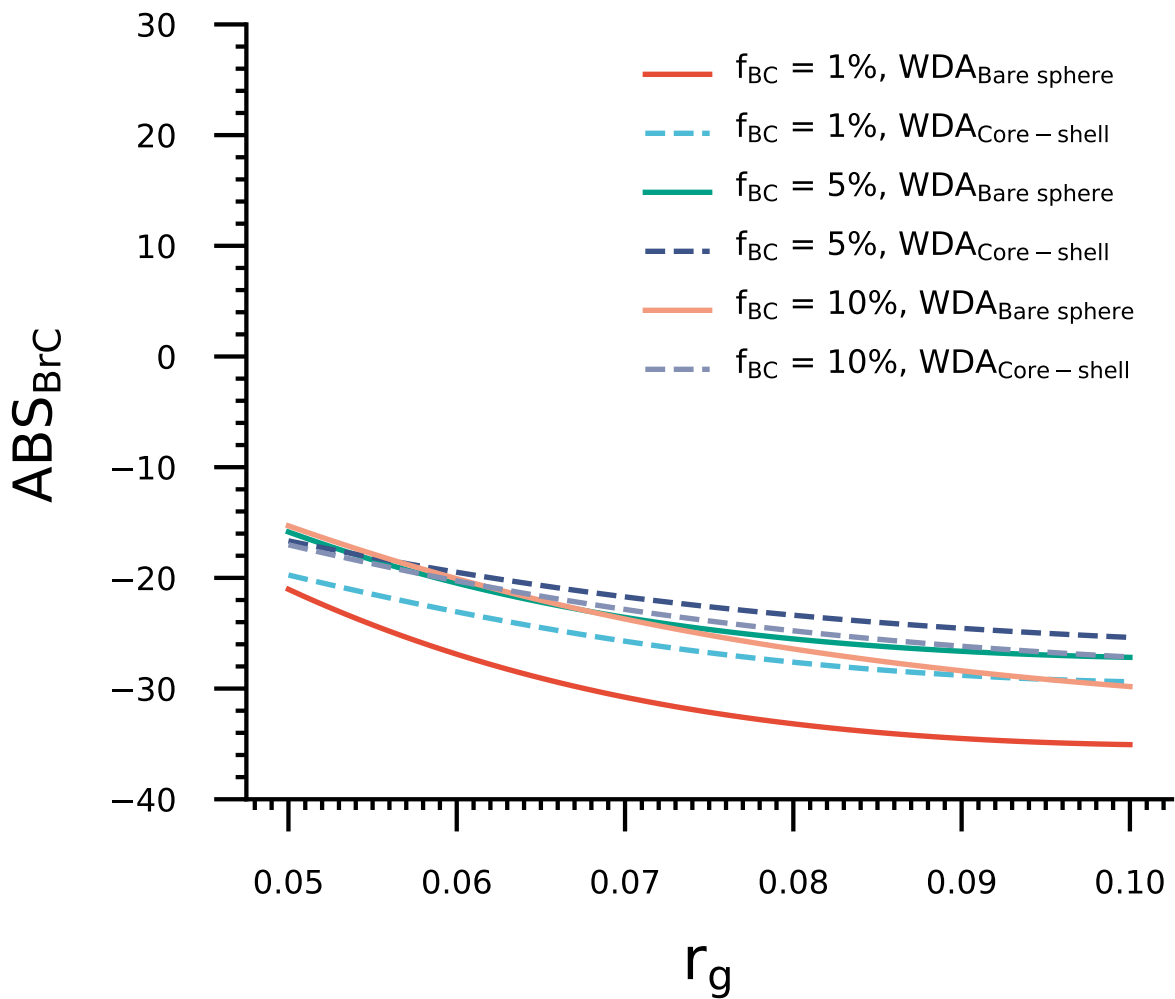
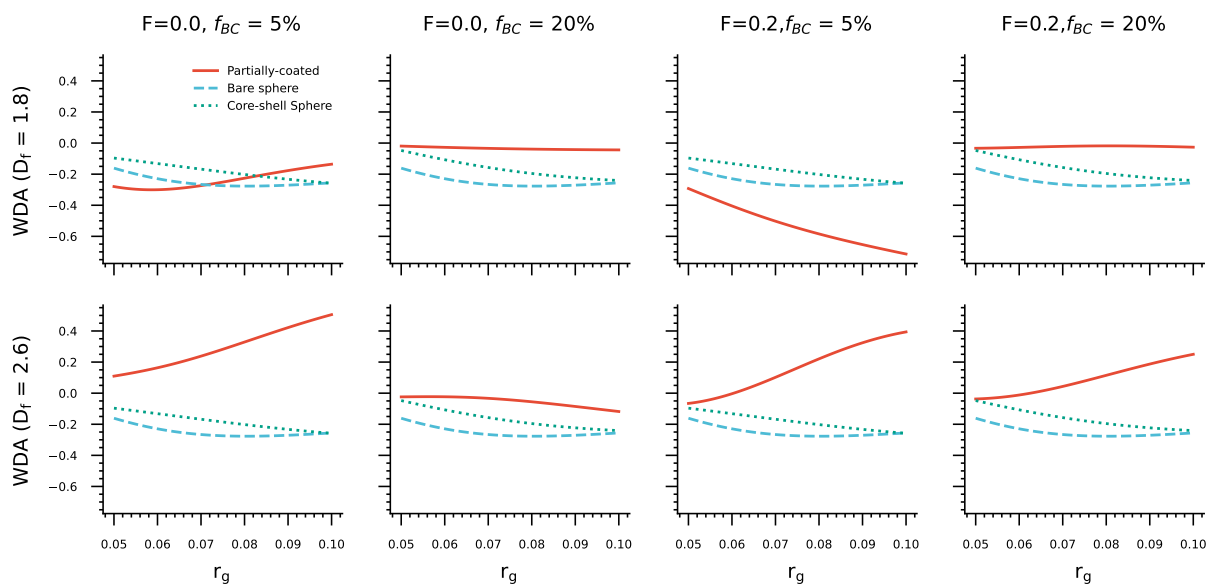


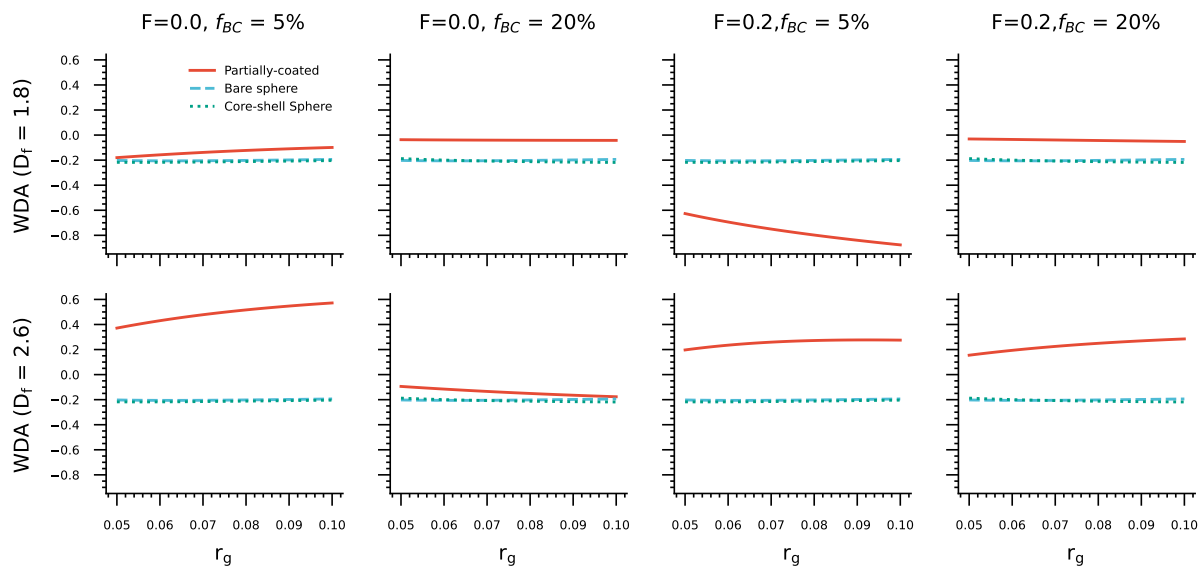
**Figure S1.** The variations of  $ABS_{BC}$  of fully coated BC ( $F = 1.0$ ) estimated based on the fixed AAE with the function of AAE and  $r_g$ , where the wavelength pair is 440 nm - 675 nm.



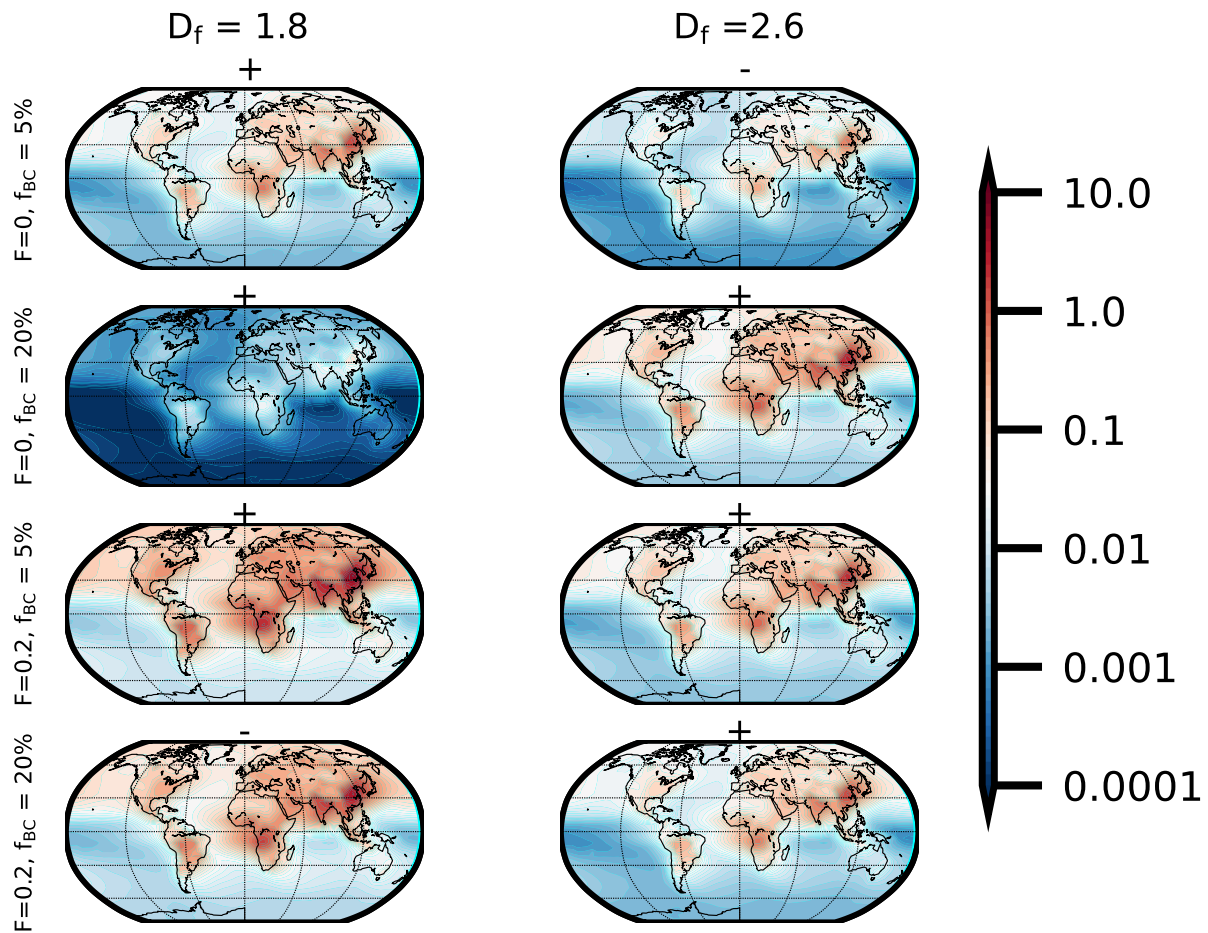
**Figure S2.** The variations of  $ABS_{BrC}$  estimated using the WDA method with  $r_g$  for fully coated BC ( $F = 1.0$ ).



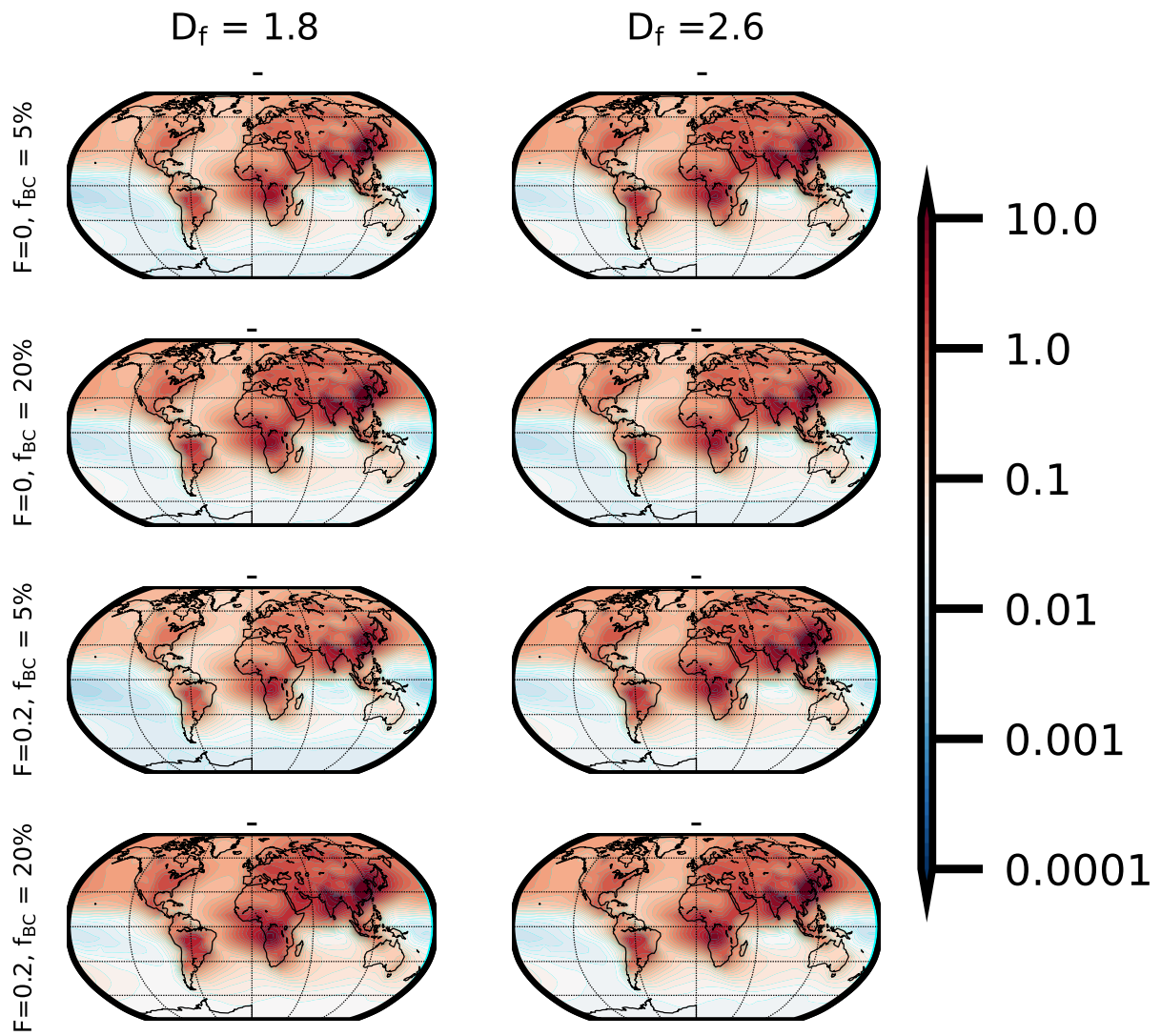
**Figure S3.** The variations WDA of BC with different morphologies with  $r_g$  at different mixing states, where  $\sigma_g = 1.4$ .



**Figure S4.** Similar to Figure S3, but for  $\sigma_g = 1.8$ .



**Figure S5.** The global distributions of BC AAOD that is attributed BrC based on the  $AAE_{440-675} = 1$  method, where negative sign means underestimation, and positive sign means overestimation.



**Figure S6.** Similar to Figure S5, but for but using the core-shell WDA method.