

Estimating the refractivity bias of Formosat-7/COSMIC-II GNSS Radio Occultation in the deep troposphere

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Abstract

FORMOSAT-7/COSMIC-2 radio occultation (RO) measurements show promise for observing the deep troposphere and providing critical information on the Earth's planetary boundary layer (PBL). However, refractivity retrieved in the low troposphere can have severe biases under certain thermodynamic conditions. This research examines the characteristics of the deep tropospheric biases and presents methods for estimating the region-dependent refractivity bias using statistical regression models. The results show that the biases have characteristics that vary with land and oceans. With substantial correlation between local spectral width (LSW) and bias, the LSW-based bias estimation model can explain the general pattern of the refractivity bias, but with deficiencies in measuring the bias in the ducting regions and certain areas over land. The estimation model involving the relationship with temperature and specific humidity can capture the large biases associated with ducting. Finally, a minimum variance estimation that combines the LSW and temperature/water vapor models provides the most accurate estimation of the refractivity bias.

1 Introduction

Global Navigation Satellite System (GNSS) radio occultation (RO) observations have become a critical data source in atmospheric applications, particularly numerical weather prediction (NWP) (e.g., Healy, 2008; Rennie, 2010; Cucurull et al., 2007, 2017; Lien et al., 2021). Low-Earth-orbiting (LEO) satellites receive radio signals from GNSS transmitters, which bend due to atmospheric density changes. Information on the bending angle can be obtained with the GNSS RO technique, and then the atmospheric refractivity is further derived by Abel inversion. Since the RO technique measures the signal phase delay, it is not affected by clouds and rainfall. The RO profile is an all-weather observation with a high vertical resolution.

The RO observations, bending angle and refractivity, measure vertical gradients in atmospheric density, a function of temperature, moisture and pressure (Kuo et al., 2004). RO observations provide information on temperature (stratosphere and upper troposphere) and moisture (lower troposphere) with low noise and low systematic errors (biases), which makes them useful in atmospheric research (Eyre, 2008). Several GNSS RO missions, e.g., the FORMOSAT-3/Constellation Observing System for Meteorology, Ionosphere, and Climate (FS3/C), FORMOSAT-7/COSMIC-2 (FS7/C2), Meteorological Operational satellite (MetOp), Gravity Recovery And Climate Experiment (GRACE), Satellite de Aplicaciones Científico-C (SAC-C), X-band TerraSAR satellite (TerraSAR-X), Korea Multi-Purpose Satellite-5 (KOMPSAT-5), etc., have provided much RO data for NWP.

38 Many studies have illustrated the positive impact of assimilating RO observations, such as the operational forecast
39 systems at the European Centre for Medium-Range Weather Forecasts (ECMWF) (Healy, 2014), the
40 NCEP/Environmental Modeling Center (EMC) (Cucurull, 2007) and the Taiwan Central Weather Administration
41 (CWA) (Lien et al., 2021). Moreover, studies have been initiated recently to investigate the potential of
42 assimilating the large volume of commercial RO data from Spire, and the benefits can be identified in weather
43 forecasting (Bowler, 2020a). In addition to improving global NWP, studies have also confirmed that assimilating
44 RO observations improves severe weather prediction, particularly for tropical cyclones and heavy rainfall (e.g.,
45 Chen et al. 2020; 2021a,b, 2022; Chang and Yang, 2022; Yang et al., 2014).

46 As the successor of FS3/C, the FS7/C2 mission was launched in 2019 with support from the Taiwan
47 National Space Agency (TASA) and the United States National Oceanic and Atmospheric Administration (NOAA)
48 and National Science Foundation. The number of profiles obtained by FS7/C2 is approximately three times greater
49 than that of FS3/C since FS7/C has dense coverage over the tropics and subtropics (Chen et al., 2021c). Compared
50 with FS3/C, FS7/C2 has a higher signal-to-noise ratio (SNR), wider bandwidth, and a better open-loop (OL)
51 tracking model. These advantages enable the retrieval of more data from RO signals penetrating the moist
52 troposphere and having the ability to detect the planetary boundary layer (PBL) and superrefraction (SR) over the
53 top of the PBL (Schreiner et al., 2020; Sokolovskiy et al., 2024). Chen et al. (2021c) showed that the data
54 availability of the FS7/C2 RO profiles under 1km is five times greater than that of the FS3/C profiles over a six-
55 month range. Anthes et al. (2022) noted that the penetration rate of RO profiles is high even under extremely
56 moist conditions and near tropical cyclones. The ability to penetrate deep into the atmosphere makes RO
57 measurements ideal for studying the PBL. The PBL is directly influenced by any exchange of energy, momentum
58 and mass between Earth's surface and the atmosphere, and thus its characteristics are crucial for weather and
59 climate variabilities.

60 However, the use of GNSS RO in the lower atmosphere still has errors when radio rays pass through areas
61 with strong vertical or horizontal refractivity gradients. It is known since 1997 that negative biases in refractivity
62 exist in the lower troposphere, especially in the tropics (Rocken et al. 1997). The implementation of open-loop
63 tracking (Sokolovskiy, 2001) and the use of the holographic retrieval method largely reduce the negative
64 refractivity bias (REFB) in lower troposphere in earlier generation RO missions. The "radioholographic" methods
65 such as the canonical transform (CT) method (Gorbunov, 2001, 2002), Full Spectrum Inversion (FSI) (Jensen et
66 al, 2002) and Phase matching (PM) (Jensen et al, 2004) largely solve the multipath issue resulting from the "strong"
67 refractivity gradient. Still, negative REFB can arise in deep troposphere from multiple causes, as summarized
68 by Feng et al. (2020) and Wang (2020). A common cause (but not the only one) of negative biases in the lower
69 troposphere is ducting (Sokolovskiy 2003; Ao et al. 2003; Xie et al. 2010). When the vertical gradient of
70 refractivity $\partial N/\partial z$ exceeds a critical value of -157 N units per km (Lopez 2009), ducting occurs and rays are
71 trapped inside the ducting layer. In the presence of ducting, the singularity problem in the Abel transforms leads
72 to a non-unique inversion problem. Thus, the Abel inversion results in a negatively bias refractivity below the
73 ducting layers (Sokolovskiy, 2003). Feng et al. (2020) reported that climatological locations agree well with the
74 areas of high ducting frequency, mainly over the subtropical eastern oceans. Furthermore, there are non-ducting
75 related biases exist in the RO data. Error associated with low SNR in the complex moist lower troposphere may
76 cause negative biases in bending angles and refractivity. Another potential source is the propagation of radio

77 waves in a medium with random refractivity irregularities can also cause biases (Gorbunov et al. 2015). In regard
78 to the assimilation of RO data, quality control (QC) is applied to reject the RO data if the observation or the
79 corresponding backgrounds are suspected to be affected by superrefraction. The rejection rate is high below 2 km
80 due to the negative bias, which could also discard valuable information for data assimilation. To increase the value
81 of RO data in the lower atmosphere, this study aims to examine the characteristics of the REFBs with the FS7/C2
82 RO data in more detail and proposes methodologies to estimate them.

83 Previous research has demonstrated that the negative REFB in the ABL can be recognized and estimated
84 using canonical transform approximations (Sokolovskiy, 2003) and can be reconstructed in the presence of ducting
85 conditions (Xie et al., 2006). Based on Xie et al. (2006), Wang et al. (2017) developed an optimal estimation of
86 negative bias using precipitable water (PW) observations from Advanced Microwave Scanning Radiometer from
87 the EOS (AMSR-E) microwave radiometer satellite data. Wang et al. (2020) further proposed a bias estimation
88 algorithm by generating a candidate set of modeled ducting profiles. The one with the vertical gradient of the
89 reflected bending angle closest to the observed profile is taken as the bias-corrected profile. However, there are
90 some limitations with these methods, such that they only correct for ducting-related bias and the grazing signal of
91 the bending measurement is needed. For the RO observation error, the local spectral width (LSW), which measures
92 the uncertainty of the RO bending angle, has been used to indicate the quality of the individual RO profiles. The
93 LSW represents the errors caused by the nonspherical symmetry of refractivity in the moist troposphere
94 (Gorbunov, 2006; Sokolovskiy 2010). The LSW parameter has improved the use of RO observations in data
95 assimilation, including in the QC procedure (Liu et al., 2018) and dynamic estimation of RO error in the lower
96 troposphere (Zhang et al. 2023). Liu et al. (2018) showed that both uncertainties and biases were related to LSW.
97 Sjoberg et al. (2023) recently showed a strong statistical correlation between lower tropospheric uncertainties and
98 LSW. They also mentioned that they found a correlation between biases and LSW as well, but did not provide
99 details. Furthermore, Bowler (2020b) proposed estimating RO errors with information on mean temperatures
100 below 20 km. These results suggest that variations in LSW, temperature and humidity are related to the bias. Thus,
101 we developed statistical models that adaptively consider the biases associated within each RO profile using LSW
102 and temperature and water vapor.

103 We first investigate the characteristics of the FS7/C2 RO REFB and establish regression-based bias
104 estimation algorithms. Two types of algorithms are examined. One is based on the physical LSW parameter, and
105 the other is related to thermodynamic variables (temperature and water vapor). By comparing the results of the
106 estimated bias, we can identify how they link to the characteristics of each participating variable. Finally, a bias
107 correction method for the RO profile in the lower troposphere is proposed by combining the two error estimation
108 algorithms. We expect that this new algorithm can be used in different aspects such as improving the products of
109 temperature and moisture profiles retrieved from the refractivity in the moist lower troposphere (Chen et al. 2020),
110 definition of the PBL height (Xie, 2014), and the estimation of precipitable water vapor (Yeh et al. 2024).
111 Furthermore, for the DA systems that assimilate the RO refractivity, it is expected that the RO data in the deep
112 troposphere can be better exploited by using the bias estimation as a QC flag or assimilating the calibrated
113 refractivity profiles.

114 The remaining portions of this paper are organized as follows. Section 2 provides the data information and
115 methods for estimating the refractivity bias. Section 3 discusses the general characteristics of bias and its

116 sensitivities with respect to different variables and land/sea conditions. Section 4 presents the results of bias
117 estimation algorithms. Finally, the summary and conclusion are provided in Section 5.

118 **2. Data and methodology**

119 **2.1 GNSS RO FS7/C2 and ECMWF data**

120 This study uses the FS7/C2 RO atmospheric profiles (atmPrf) and wet products (wetPf2) processed by
121 the Taiwan Data Processing Center (TDPC). The study period is from 1st December 2019 to 29th February 2020,
122 before the FS7/C2 data were assimilated in the ECMWF analysis. All RO profiles are distributed between 45°S
123 and 45°N due to the low inclination orbits of the FS7/C2 satellites. A total of 244,853 profiles are selected with
124 the flag of “good data” during the periods, and only data below the height of 25 km are used to focus on the bias
125 characteristics in the troposphere. The data quality of the FS7/C2 constellation is improved compared to
126 FS3/COSMIC (FS3/C) due to the use of the advanced RO receiver and postprocessing with open-loop tracking.
127 Most of the profiles show a deeper penetration with depths below 1 km, and the penetration rate is 40% higher
128 than those of FS3/C (Chen et al., 2021c). Figure 1 shows the number of profiles that penetrate below 1.5 km above
129 the mean sea level (MSL) during the selected periods. The FS7/C2 data are mostly in tropical areas and have more
130 profiles penetrating below 1.5 km over oceans than over land.

131 The ECMWF atmospheric reanalysis (ERA5, [https://www.ecmwf.int/en/forecasts/access-forecasts/access-
132 archive-datasets](https://www.ecmwf.int/en/forecasts/access-forecasts/access-archive-datasets)) is used as the reference RO profiles. The hourly ERA5 reanalysis in the study period has a
133 horizontal resolution of 0.25 x 0.25 deg with 37 pressure levels, ranging from 1000 to 1hPa. The variable
134 geopotential, temperature and specific humidity are selected. Since the time of the RO data is precise in minutes,
135 we rounded the time of the RO profiles to the nearest hour. The ERA5 profiles are derived by interpolating the
136 reanalysis horizontally and vertically to the location and vertical levels of the RO atmPrf. The RO REFB is defined
137 as the difference between the FS7/C2 and the ERA5 RO observations at each level. This assumes that the ERA5
138 refractivities are close to truth. These biases are referred to as the real biases in this paper. Nevertheless, it is
139 possible that ERA5 may carry its own biases, which will not be discussed in this study.

140 For constructing the statistical models, the predictors are LSW, temperature (T), and specific humidity (Q).
141 The LSW, available in the atmPrf data, are calculated from the width of the spectrum during the RO processing
142 (Liu et al. 2018). The T and Q , available in the wetPf2 data, are computed from a one-dimensional variational
143 (1D-Var) retrieval algorithm using ECMWF 12-h forecast as the a priori (Wee et al. 2022).

144

145 **2.2 Statistical models for bias estimation**

146 Two polynomial regression models are developed to estimate the REFB using predictors associated with
147 different attributions of the observational error in GNSS RO data. The first model uses LSW/2 as the predictor,
148 and the other uses temperature (T) and specific humidity (Q) as the predictors. Liu et al. (2018) used a linear
149 function of LSW/2 to illustrate the FS3/C dynamic error variance in the bending angle and refractivity, and the
150 scaling factor 1/2 for LSW approximates the root mean square of random error of the bending angle (Liu et al.
151 (2018), assuming a Gaussian spectrum (Sirmans and Bumgarner 1975). Following Liu et al. (2018), we use the
152 variable LSW/2 and modify this relationship to a polynomial regression. The other bias estimation model is
153 established using the thermodynamic variables to emphasize the impact of the thermodynamic structure on REFB

154 in deep troposphere. The two polynomial regression models are referred to as the LSW and TQ estimators,
 155 respectively. The LSW represents the RO inversion uncertainty, and T and Q represent the impact of the
 156 thermodynamic structure on REFB within the ABL. Each of these variables is expected to partly explain the
 157 characteristics of the bias.

158 In each estimator, the order of the polynomial is optimized by using the metrics of R-squared and mean
 159 square error to assess the goodness of the fitting performance. The polynomial regression is performed with the
 160 training data, which is 80% of the total data, and the rest (20%) of the data is used for evaluating the regression
 161 performance. To derive a robust regression model, independent regression fitting is repeated five times by
 162 replacing the training/testing data with a different 80%/20% subsets of the data so that the testing data from five
 163 experiments eventually covers the whole data set. The regression model with the best fitting performance for both
 164 training and testing data is chosen as the optimal one. Given that our goal is to construct regional-dependent
 165 estimators to consider the spatial variation in the REFB, we group the RO refractivity profiles from 45°S to 45°N
 166 into 5°longitude x 3° latitude boxes (Figure 1), and the regression-based REFB estimators are built in each box.
 167 In total, there are 72 x 30 boxes. The boxes are defined by considering the number of available RO profiles below
 168 1.5km should be at least 10 profiles in each box for conducting the regression training and testing. With the 3
 169 months of data used in our study, choosing testing data lower than 20% of the total data results in a very coarse
 170 resolution of the boxes. On the other hand, choosing any number larger than 20% would sacrifice the amount of
 171 data that can train a reliable regression model. We note that all profile data below 1.5 km are used first (80% for
 172 training and 20% for testing) to determine the order of the LSW-based regression model and the optimal
 173 combination of the multi-variable (T and Q) regression model.

174 For the LSW estimator, a second-order polynomial is chosen based on the R-squared metric. Afterwards, a
 175 second-order polynomial regression is constructed for an individual box. Eq. (5) shows the formula of the LSW
 176 estimator in the i_{th} box

$$177 \quad u_i = \alpha_{i,1}x_i^2 + \alpha_{i,2}x_i + \alpha_{i,3} \quad (1)$$

178 where u_i , the predictand, is the REFB, x_i is the LSW/2, and $\alpha_{i,*}$ are the regression coefficients. Although the
 179 biases related to the signal tracking or multipath is much reduced after with the implementation of open-loop
 180 tracking and radio-holographic retrieval method, we expect that LSW can partially capture the biases inherited
 181 from bending angle.

182 A similar procedure is applied to derive a multivariable polynomial regression model with T and Q obtained from
 183 the 1D-Var analysis of the RO wet products (Wee et al. 2022) as the predictors. For consistency, the real REFB
 184 originally defined with the atmPrf, will be interpolated to the same levels of the wetPf2. No REFB, T and Q are
 185 collected if the T , Q profiles terminate above 1.5 km MSL. Before fitting, T and Q are standardized as

$$186 \quad \chi = \frac{x_i - \min(x_i)}{\max(x_i) - \min(x_i)} \quad (2)$$

187 where χ represents a normalized quantity ranging between 0 and 1 and x_i is the original value of Q or T in the i^{th}
 188 box. Given two variables, there are different combinations of order and interaction terms (multivariable
 189 polynomial function has the form of $\sum_{m=0}^M \sum_{l=0}^L b_{m,l} y^m z^l$, where m and l are the order of variable y and z ,
 190 respectively, and $b_{m,l}$ is the regression coefficient). For this application, the mean squared error is used to

191 determine the optimal fitting formula given that R-squared are comparable when higher order terms are included.
 192 The optimal multivariable polynomial regression model has the form:

$$193 \quad u_i = \beta_{i,1}y_i^2 + \beta_{i,2}y_i + \beta_{i,3}y_iz_i \quad (3)$$

194 where u_i is REFB, y_i is the normalized Q , z_i is the normalized T and $\beta_{i,*}$ are the regression coefficients.
 195 Considering the quadratic term of moisture is essential. The R-squared (MSE) value increases (decreases) from
 196 0.535 (37.044) with the y_i and y_iz_i terms to 0.732 (26.610) with the y_i^2 term.

197 We further apply the minimum variance estimation (MVE, Clarizia et al., 2014) to combine the results
 198 from the LSW and TQ estimators. This approach has the advantage of having a smaller RMS error than either the
 199 LSW or TQ estimation. The MVE is built to linearly combine the estimations so that the new estimation has the
 200 minimum error variance:

$$201 \quad u_{i,MVE} = \mathbf{m} \cdot \mathbf{u} \quad (4)$$

202 where \mathbf{u} is the vector of individual estimated refractivity bias and \mathbf{m} is the vector of combination coefficients. One
 203 of the advantages of this combination is that \mathbf{m} is derived considering the error covariance matrix of individual
 204 bias estimators.

$$205 \quad \mathbf{m} = \left(\sum_{i=1}^K \sum_{j=1}^K c_{i,j}^{-1} \right)^{-1} \mathbf{C}^{-1} \mathbf{1} \quad (5)$$

206 where $\mathbf{1}$ is a vector with all elements equal to one, K is the dimension of \mathbf{m} ($K = 2$ in our application), \mathbf{C}^{-1} is the
 207 inverse of the covariance matrix between the individual estimation errors and $c_{i,j}^{-1}$ are the elements of \mathbf{C}^{-1} .

208 The element of the error covariance matrix \mathbf{C} is expressed as $c_{i,j} = \langle (\mathbf{u}_i - \mathbf{u}_t)(\mathbf{u}_j - \mathbf{u}_t) \rangle$, where u_i and u_j is the
 209 i^{th} and j^{th} bias estimation, respectively, and u_t is the real bias.

210 **3 Characteristics of the refractivity bias**

211 **3.1 General characteristics of REFB**

212 Figure 2a shows the profile of the averaged REFB and its standard deviation from 0-25 km. RO data have
 213 significant biases in comparison to the ERA5 reference, especially in the low troposphere. The bias is evident
 214 below 5 km and is largest at the surface with an amplitude of approximately -11 N-units. Given the large variations
 215 in moisture and temperature in the low troposphere, the standard deviation below the 2 km height increases as the
 216 height decreases. Notably, although the total number of profiles quickly decreases below 5 km (Fig. 2b), there
 217 remain enough data for near-surface statistical evaluation, with about a 40% penetration rate at 0.5 km in reference
 218 to the total number of profiles at 10 km (Fig. 2c). The mean LSW (red line in Fig. 2a) also increases sharply as
 219 the height decreases, with two peaks, at the surface and near 2 km.

220 Figure 3a shows the latitudinal cross-section of the REFB. The largest values of REFB are below 5 km in the
 221 subtropics and tropics and slightly shifted to the Southern Hemisphere due to the austral summer. The opposite
 222 pattern, which has a high bias shifted to the Northern Hemisphere, is also seen with the data from June to August
 223 2020 (not shown). This result indicates the general dependence of the distribution of REFB on the seasonal

224 temperature and water vapor structure. Similar to the REFB pattern, large LSW occurs mainly in the tropics, tilting
225 toward the Southern Hemisphere with the maximum near the surface (Fig. 3b). This finding illustrates that LSW
226 variation can be related to the REFB to some extent. Moreover, other high LSW values are located a few
227 kilometers above the surface of the Southern Hemisphere. The increased LSW above 2 km could be caused by
228 common inversion layers in the troposphere of some oceans (Sokolovskiy et al. 2014). Another effect that could
229 be considered is the influence of convective clouds just above moist oceans (Yang et al., 2016). The large LSW
230 near the surface in Fig. 3b reflects the ability of FS7/C2 to penetrate deep into the moist troposphere of the tropics.
231 However, this surface maximum was not seen in the study of Zhang et al. (2023) using FS3/C data in August
232 2008.

233 3.2 Dependence on geography and thermodynamic conditions

234 We further examine the dependence of the REFB on land and oceanic thermodynamic conditions. Figure 4
235 compares REFB between land and ocean, together with its standard deviation (stdv) and LSW. Both REFB and
236 LSW below 4 km are somewhat larger over oceans, and the REFB extends to higher altitudes (Fig. 4c vs. 4d) with
237 a greater vertical gradient of REFB below 2 km. The magnitudes of mean REFB and stdv above 2 km are
238 comparable over land and ocean. The shape of the LSW profiles is different over oceans and land, with the second
239 peak value at 2 km more pronounced over oceans. Below 1.5 km, the shape of the REFB profile exhibits
240 characteristics as the LSW profiles, suggesting the potential of LSW as a predictor for estimating REFB.

241 Given the large REFB in deep troposphere, we focus on the regional variations in REFB averaged below 1.5
242 km. Figure 5a shows that the averaged value of negative REFB below 1.5 km is largest over the oceanic regions
243 near the western coasts of the South American and African continents. Small negative REFBs appear over the
244 tropical Pacific and land. There are small positive REFBs over the high mountain regions. The different behavior
245 of the REFB over ocean and land implies the impact of regional variability and the associated thermodynamic
246 structure in the lower troposphere. As shown in Fig. 5b-5d, high LSW occurrence is mainly located over the warm
247 equatorial regions of the Pacific, Atlantic and Indian Oceans. However, not all of the regions with high temperature
248 and moisture coexist with the regions with high LSW. Some exceptional regions can be seen, such as offshore to
249 the coast of Southwest Australia and offshore of Southwest Africa near the international data line. Fig. 5 suggests
250 that although LSW, temperature and specific humidity have certain cross-relationships, the characteristics of
251 thermodynamic conditions cannot fully explain the distribution of LSW. Therefore, an REFB estimation model,
252 which is based on only one variable, is not enough to explain REFB.

253 To further highlight the characteristics of REFB under different conditions, the REFB profiles are grouped
254 according to each profile's LSW, temperature and specific humidity averaged below 1.5 km for land and ocean
255 (Figure 6). As Xie (2014) reported, the 1.5 km MSL is the global mean PBL height calculated from the FS3/C
256 refractivity data. In general, it is evident that the negative REFB increases with increasing LSW below 4 km, as
257 shown in Fig. 3; however, the characteristics are different for land and ocean. Over land, the very high LSW does
258 not guarantee the occurrence of a large REFB in lower troposphere. Moisture and temperature likewise exhibit
259 the same linear relationship with negative REFB in the lower troposphere. However, negative REFBs also tend to
260 occur under conditions of low moisture over the ocean. Figure 6 reveals that the relationship between REFB and
261 LSW, T and Q under 1.5 km is dominantly linear; however, the REFB variations can be further explained by a

262 quadratic relationship with Q . It is noted that REFB at about 10 km increase with increasing LSW, T and Q over
263 both land and oceans, and even become weakly positive at high values of LSW, T and Q averaged below 1.5km.
264 In particular, RO profiles over land with large LSW below 1.5km has the largest positive REFB, nearly 8 N-unit,
265 aloft. Taking only the RO profiles penetrating 0.5 km will modify the characteristics of Figure 6 in two aspects.
266 First, the REFB below 10 km becomes positive for LSW/2 larger than 28%. Second, the REFB for cold
267 temperature shows negative at 15 km. The former feature is related to the early cutoff height in the tropical
268 occultation over central Africa (Sokolovskiy, 2010). The latter feature is attributed to the inversion associated with
269 the large-scale subsidence near the tropopause near mid-latitude. Sensitivity tests to address sampling issues will
270 be discussed in subsection 4.2.

271 **4 Results of bias estimation**

272 **4.1 General performance**

273 In this section, we present the estimation for REFB using the methods introduced in Section 2. As
274 mentioned, LSW/2, which represents the retrieval uncertainties of the bending angle and, hence, refractivity
275 uncertainties, is the predictor for the first bias estimation model. The T and Q retrieved from FS7/C2 RO data are
276 the predictors for the second estimator. Although the T and Q products retrieved from RO profiles using 1D-Var
277 retrievals may have errors, they still provide valuable information for REFB estimation through the training
278 process, as described in Section 2.

279 Figure 7 shows the relationship between the REFB and LSW/2 averaged below 1.5 km for the Southern
280 Hemisphere (SH) and Northern Hemisphere (NH). REFB is grouped every 2% of LSW/2, from 0 to 36%. The
281 solid and dashed lines show the LSW-based REFB estimates for ocean and land, respectively. Under 1.5 km, the
282 magnitude of the negative REFB as a function of LSW is larger over oceans than for land. Generally, as LSW/2
283 increases, the REFB becomes more negative below 1.5 km for both land and ocean. Although the relationship is
284 dominated by a linear trend, the quadratic term further improves the regression fitting. As shown in Table 1, the
285 correlations over ocean and land are robust (larger or close to 0.9) and similar with the training and testing data
286 in SH and NH. Compared to the REFB under the warm and moist condition of the austral summer in SH, the
287 REFB over NH is weaker but the relationship between LSW/2 and REFB is still strong over ocean and land,
288 except that the one over land has a somewhat stronger quadratic feature. Given this strong relationship, we expect
289 that the relationship during the boreal summer season will hold as well. However, the relationship between REFB
290 and LSW/2 is not present above 1.5 km, and there is little difference in REFB between land and ocean.

291 Figure 8 shows the result of the second bias estimator, which relates the REFB with normalized Q (y)
292 and product of normalized T and Q (yz) under 1.5 km. The TQ estimation over ocean and land captures the feature
293 where the REFB becomes more negative under moist conditions. Similar to the LSW estimator, the TQ estimator
294 shows a stronger dependence over the ocean. The multivariable regression has correlation coefficients equal to
295 0.79 and 0.72 for ocean and land in SH, respectively, and 0.75 and 0.69 in NH. In general, the REFB shows a
296 robust bi-linear relationship with y and yz , and the quadratic term (y^2) provides further adjustment. With a fixed
297 specific humidity, lower temperature results in larger negative REFB. In Fig. 8a, this result reflects the condition
298 over the cool SST (Fig. 5a and 5d), west of the coast of South America and South Africa. The relationship becomes

299 more linear in NH (Fig. 8a vs. 8c), i.e. less dependence to the quadratic term of specific humidity. For dryer
300 conditions, the TQ estimator tends to give neutral to positive REFB, especially over land (Fig. 8b and 8d) where
301 more data are in the dry condition and part of them are over the mid-latitude continent (Fig. 5c). Given a fixed TQ
302 value ($y_z=0.5$) in Fig. 8, Figure 9 shows the strong relationship between REFB and Q . Large negative REFB
303 corresponds to moist condition, but the negative amplitude is larger over the SH ocean with larger variation. The
304 relationship is more quadratic over ocean than over land and is most linear over the NH land. In Figure 8, a slightly
305 positive REFB is estimated for very cold and dry condition over ocean. In Feng et al. (2020), positive REFB is
306 identified in Bering Ocean at high latitude. While Fig. 8 qualitatively suggests the potential to capture such
307 positive REFB over high-latitude, whether the regional-dependent TQ estimator can be adequately applied to
308 estimate REFB in the polar or high-latitude regions is still an open question since the FS7/C2 data RO data used
309 in this study mostly distributed in the tropic to subtropic regions.

310 Figures 7 and 8 confirm that models with LSW/2 or TQ as predictors can estimate the REFB under 1.5 km, but
311 there are different sensitivities for ocean and land. In the next step, we further apply these regression methods
312 using the data in 5° longitude \times 3° latitude boxes within 45° N to 45° S to construct the region-dependent bias
313 estimation model.

314 Figure 10 shows the horizontal distribution of the mean real and estimated REFBs with the training and
315 testing data. Notably, there are some differences between the training and testing data (Fig. 10a vs. 10b), such as
316 the large REFB off the western coast of South American and coast of Australia. In comparison to the real REFB
317 distribution (Fig. 10a), the LSW-based REFB (Fig. 10c) captures the general pattern with larger biases over ocean
318 and lower biases over land in both the training and testing data. However, the LSW-based REFB is less capable
319 of capturing the large bias over the subtropical oceans off the west coast of South America and South Africa and
320 Australia. Those are expected to be the oceans that have a cold SST, where ducting occurs commonly due to the
321 frequent occurrence of inversion layers on top of the cool sea surface. Although the LSW-based REFB can also
322 represent a portion of the negative REFB in these regions in general, it is obvious that the values are
323 underestimated there. The LSW-based estimation exhibits good performance in estimating the negative REFB in
324 the Indian Ocean, where the pattern and magnitude of the estimated REFB are close to those of the real REFB. In
325 contrast to the LSW-based REFB, the TQ -based REFB represents the large negative REFB in the high-ducting-
326 occurrence regions well. Although the magnitude of the N -REFB offshore the coasts of South America and South
327 Africa is still underestimated, the pattern and amplitude of the negative REFB are much better represented in
328 comparison with the LSW-based estimation.

329 The TQ -based estimation (Fig. 10 e,f) captures the low bias pattern well, such as the tropical western
330 Pacific, western South America and Africa, while the LSW-based estimation overestimates the negative bias. The
331 similar pattern between the real and TQ -based estimated REFBs can be explained by the following two reasons.
332 The first reason is the ability to capture SST characteristics. For example, cold SST regions can result in a cool,
333 low moisture near-surface atmosphere (Fig. 5c and 5d) and impact the boundary layer. Second, the bias in the RO
334 refractivity profiles will be translated to the 1D-Var T and Q retrievals.

335 The final method, the MVE, combines the LSW and TQ estimations. As described in Section 2, the MVE
336 derives the optimal combination by considering the error correlation between the individual estimations. Notably,

337 the MVE approach requires knowledge of the error covariance matrix between two components (the matrix \mathbf{C} in
338 Eq. 5). The error correlation of the two REFB estimators is 0.294. A high error correlation indicates a dependency
339 between the two components and thus there is less benefit from using the MVE method. Although LSW is known
340 to have a relationship with temperature and water vapor, our results indicate that the error correlation between
341 two estimates is low enough that it is expected that the MVE can extract useful information from both estimations.
342 Compared to the LSW and TQ REFB estimation, the results of the MVE show a pattern closer to the real REFB
343 with both the training and testing data sets.

344 We next show the root-mean-square error (RMSE) between the real and estimated REFB in each box.
345 Figure 11 shows the contribution of each estimation in estimating bias for land and oceans and reflects the
346 representativeness of the mean REFB shown in Fig. 10. The LSW-based estimation exhibits high RMSE in the
347 cold SST regions and several ocean regions, such as the Southeastern Atlantic, Southeastern and North Western
348 Pacific Oceans, while the TQ estimation successfully mitigates this issue. On the other hand, the LSW-based
349 estimation performs better in the tropical Atlantic and Indian Oceans. With training and testing data, the large
350 RMSEs in the LSW or TQ estimation over the oceans are largely removed by the MVE method; however slight
351 degradation is observed over the continents of south America and middle Africa. With the testing data (the right
352 column in Fig. 11), the RMSEs are larger in individual estimations, as expected. In general, the MVE method
353 retains its advantage in the optimal estimation over ocean, with an RMSE smaller than that of either estimation.
354 Table 2 shows the global mean RMSE. The TQ method has a smaller RMSE compared to the LSW estimation.
355 The MVE method further improves the TQ method by 32% and 23.6% with the training and testing data,
356 respectively.

357 However, we also observed that the TQ -based REFB has larger RMSE in the ducting region in southeast
358 Pacific and Atlantic (Fig. 11e vs. Fig. 11f). This is attributed to an overestimated negative REFB (Fig. 10e vs.
359 10f) by the TQ estimator with a much moister near-surface condition in the testing data than those in the training
360 data. The overestimation of the testing data in the ducting regions suggests that more data is required to train the
361 statistical model applicable to a broader sets of temperature and moisture requires.

362 4.2 Sensitivity experiments

363 This subsection discusses the sensitivity of the REFB estimation to the penetration rate of the RO profiles
364 and investigates the impact of sampling error on constructing the LSW-based and TQ -based estimators. Two sets
365 of sensitivities are designed. For the first set of sensitivity, it is required that, in each box, at least 30 RO profiles
366 penetrate a certain level. For the second set of sensitivity, the REFB estimators are obtained for RO data from
367 different levels.

368 Figure 12 shows the REFB estimation with the testing data using different criteria of the penetration rate.
369 The estimators are obtained when there are at least 30 profiles whose minimum level is smaller than 1.5 or 0.5
370 km, respectively. The criteria are referred to as CT1 and CT2 in Fig. 12. As the criterion becomes more stringent,
371 more samples in the tropics are rejected and insufficient samples are available in the core of the ducting regions
372 and areas with latitudes higher than 30 degrees. For boxes with sufficient samples with the CT2 criterion, the
373 patterns of REFB, LSW, T and Q (the right column in Fig. 5) are very similar to the ones with an eased standard
374 criterion, but their amplitudes are generally higher. Nevertheless, the real REFB in Fig. 12a and Fig. 12b is very
375 similar to that in Fig. 10b using an eased criterion on sample number. This similarity is due to fact that the data

376 amount between 0.5 and 1.5 km is much more than that below 0.5km (Fig. 2b). However, the real REFB with
377 CT2 is larger in south Pacific and Atlantic. This reflects that the REFB quickly increases near the surface (Fig. 3a),
378 which can be emphasized after the RO profiles with early termination are removed. The LSW-based REFB with
379 strict criteria also captures the general pattern of real REFB, while the TQ -based REFB captures the large negative
380 REFB in the ducting regions well. The REFB estimation using the C2 criterion still show good ability in the
381 regions that the real REFBs are somewhat different between the C2 and standard criteria, such as Central and
382 northwestern Pacific. This good performance is attributed to the fact that the region-dependent regression models
383 can adapt to the changes in the training data in boxes.

384 Based on the results in Fig. 12, we separate the REFB estimation to different vertical levels, below 0.5
385 and between 0.5 and 1.5 km (Figure 13). As shown in Fig. 3b, the real REFB below 0.5 km is generally larger
386 than that between 0.5 and 1.5km, except for western Pacific and the ducting regions, west of south America and
387 south Africa. Below 0.5km, the penetration rate declines quickly, reducing the sample size. Nevertheless, it is
388 shown that both REFB estimators perform well in estimating the REFB as well, in particular that the TQ -estimator
389 is good at capturing the large REFB. Both estimators can even capture the large negative REFB in central southern
390 Pacific and south India, and the MVE REFB improves the TQ -based REFB in central Pacific ($150^{\circ}W$ to $150^{\circ}E$).
391 However, the TQ -estimator provides positive REFB estimation in the cold and dry condition north of Africa, while
392 a weak negative value is exhibited in the real REFB. While the TQ -estimator is very sensitive to the amplitude of
393 temperature and moisture, we emphasize that the regression model may not be reliable with a limited sampling
394 size in mid-latitude regions. Results of the REFB estimation between 0.5 and 1.5 km are very similar to Fig. 10.
395 This again confirms that the REFB shown in Fig. 10 is dominated by the data between 0.5 and 1.5 km.
396 Nevertheless, it is important that both REFB estimators can reflect not only the general characteristics and also
397 the differences at different vertical levels.

398 4.3 Estimating vertical profiles of refractivity bias

399 This section examines the performance of the REFB estimation methods and whether they can be used
400 for estimating the vertical profiles of REFB. The following three areas (indicated in Fig. 9a) with different REFB
401 characteristics are selected as examples: Area A is in the region of $0^{\circ} < Lat < 10^{\circ}N$ and $55^{\circ}E < Lon < 75^{\circ}E$, Area
402 B is in the region of $20^{\circ}S < Lat < 30^{\circ}S$ and $105^{\circ}W < Lon < 85^{\circ}W$, and Area C is in the region of $35^{\circ}S < Lat <$
403 $45^{\circ}S$ and $120^{\circ}W < Lon < 135^{\circ}W$. For each area, the estimated REFB at different levels are derived using the
404 estimation methods defined in the previous section. Figure 14a-c shows the mean of the real and estimated REFB
405 profiles in three areas with the testing data. We note that the results of the training and testing data are very
406 similar. In Area A, the mean negative REFB is large at the surface but gradually reverses to a positive bias at 3
407 to 5 km. In this case, the air below 2 km is very warm and moist over the Indian Ocean (Fig. 14d). The highly
408 humid condition gives a large LSW (Fig. 5b and 5c), and thus, the LSW method can have a good ability to
409 estimate bias in this circumstance, while the TQ method overestimates the negative REFB. In contrast, Area B
410 shows different patterns (Fig. 14b): the real negative REFB is even larger (-17 N units) at the surface, and the
411 negative bias at 2 km is still large compared to that in Area A. As shown in Fig. 14d, this characteristic is
412 associated with the inversion layer at 2 km over the cold SST region and large vertical moisture gradient, a typical
413 condition of ducting. While the LSW-based estimation underestimates the negative REFB with the existence of
414 the inversion layers this can be captured by TQ -based estimation. Nevertheless, the MVE method is always much

415 closer to the real REFB. In Fig. 14b Area B shows the improvement in the MVE than the TQ -based estimation,
416 while large RMSE remained in Area B with the MVE method in Fig. 11f. It should be noted that Fig. 11 is
417 calculated based on the difference the real REFB and estimated REFB of each profile “averaged” below 1.5 km,
418 where Fig. 14 groups the profiles with an interval of 500m. Therefore, the overestimation REFB below 1km with
419 the TQ -based estimator is alleviated with the average data used to construct Fig. 11.

420 For the box located offshore of north America with the mid-latitude cold and dry condition (Fig. 14c),
421 both estimators capture the general pattern of the vertical distribution of REFB but the amplitude below 1 km is
422 smaller than the real REFB. Nevertheless, the TQ -based REFB is much better represented compared to one from
423 the LSW estimator. Fig. 14 suggest that both estimators can be applied to estimate the vertical variations of REFB
424 in different regions. However, sample issues may be encountered in mid-latitude regions as discussed in section
425 4.2.

426 5. Conclusions

427 This study investigates the characteristics of refractivity bias (REFB) of FS7/C2 and its sensitivities to RO
428 measurement uncertainty (LSW) and thermodynamic conditions (temperature and moisture). Two bias estimation
429 models are constructed based on polynomial regression with the LSW, and temperature and specific humidity are
430 used as predictors in each estimation. The study period is December 2019-February 2020, with the ERA5
431 reanalysis data taken as the reference truth.

432 Similar to previous studies, the low-level FS7/C2 RO refractivity data of during the study period contain
433 significant biases when compared with ERA5. In general, the REFB below 1.5 km is negatively proportional to
434 LSW and exhibits a stronger dependency over ocean than over land. Additionally, REFB in the PBL has a strong
435 dependence on low-level temperature and moisture. While the majority of Pacific and Indian Oceans with warm
436 SSTs have significant negative REFBs, the largest negative REFB regions are near the cold SST regions off the
437 western coasts of South America and South Africa. Small and even positive REFBs are observed over South
438 America and South Africa.

439 Two REFB estimation models based on the polynomial regression approach are first applied to construct the
440 region-dependent mean REFB below 1.5 km. One estimation model uses a quadratic function of LSW. The other
441 uses the multivariable polynomial regression with temperature and specific humidity (TQ) as predictors, and the
442 moisture variable become emphasized after optimization. The estimation models are then applied to 72×30 boxes
443 from 45°S to 45°N . The minimum error variance (MVE) method is used to combine two REFB estimations. The
444 results show that the bias estimation models with either LSW or TQ have their own advantages in estimating
445 REFB. The LSW-based model shows the ability to capture the general pattern of the negative REFB but the
446 amplitude is significantly underestimated in the ducting areas. The TQ -based model has great performance in
447 representing the pattern and amplitude of REFB, particularly the large negative REFB in the ducting areas and
448 small REFB over most land regions. While the relationship between REFB and LSW below 1.5km is very strong
449 in a global sense, the TQ -based REFB shows its advantage in capturing the regional characteristics. The MVE
450 estimation successfully adopts the advantage from either LSW or TQ estimation and has the smallest RMSE,
451 particular over ocean.

452 Results of sensitivity tests show that the estimators at mid-latitude could be affected by the sampling issue
453 since requiring profiles penetrating 0.5 km cannot obtain sufficient samples to construct the regression models.
454 With the 3 months of data, the REFB estimation in tropic to subtropic regions remains similar with the RO profiles
455 penetrating below 1.5 or below 0.5km given that the amount of RO data between 0.5 and 1.5 km dominates.
456 Nevertheless, both the LSW and TQ estimation can capture the characteristics of REFB when the RO data are
457 separated to below 0.5 and between 0.5 and 1.5km. Such an ability allows the three REFB estimation models to
458 be applied to reconstruct the REFB vertical profiles for regions with distinct thermodynamic condition in deep
459 troposphere. Both the LSW and TQ estimations can well represent the vertical gradient of the mean REFB and
460 the MVE estimation gives an estimated REFB profile closest to the real REFB with the probability distribution
461 similar to the distribution of real REFB.

462 We should note some of the limitations of these REFB models. The temperature and moisture from the
463 ERA5 reanalysis may have bias. In addition, REFB may have more characteristics regarding smaller scales
464 spatiotemporally. We should also emphasize that the FS7/C2 RO data are mainly located in the tropic to subtropic
465 regions. Therefore, we need more data to justify whether the regression-based bias estimation is applicable in the
466 high-latitude regions. At last, predictors used in the statistical models may not be perfect to capture all attributions
467 of REFB. For future work, bias estimation models will be constructed at higher resolutions with more RO profiles
468 collected from the current FS7/C2 or other operational and commercial GNSS-RO satellites.

469 **Author contribution:** SY was in charge of the conceptualization of this study. SY and GP prepared the manuscript
470 with contributions from all co-authors. GP constructed the packages of bias estimation. SY and GP analyzed the
471 data. SY and GP wrote the manuscript draft; CC, SC, and CH reviewed and edited the manuscript. The authors
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473 improving the manuscript.

474 **Competing interests**

475 The authors declare that they have no conflict of interest.

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479 **Code and data availability**

480 The codes of the bias estimators used in this study are available at Github
481 (https://github.com/jiajia170801/bias_estimation_paper). The RO data is obtained from TDPC (TACC)
482 by https://tacc.cwb.gov.tw/data-service/fs7rt_tdpc/. The ECMWF reanalysis v5 (ERA5) data is
483 obtained from Copernicus server by [https://cds.climate.copernicus.eu/cdsapp#!/dataset/reanalysis-era5-
484 pressure-levels?tab=overview](https://cds.climate.copernicus.eu/cdsapp#!/dataset/reanalysis-era5-pressure-levels?tab=overview).

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623

624 **Table 1: Correlation coefficients between the mean real and estimated REFBs below 1.5 km over ocean and**
 625 **land in Southern Hemisphere (SH) and Northern Hemisphere**

Correlation coefficients	LSW based		<i>TQ</i> based	
	Ocean (SH/NH)	Land (SH/NH)	Ocean (SH/NH)	Land (SH/NH)
Training data set	0.94/0.96	0.9/0.92	0.79/0.75	0.72/0.69
Testing data set	0.93/0.96	0.89/0.87	0.71/0.68	0.70/0.63

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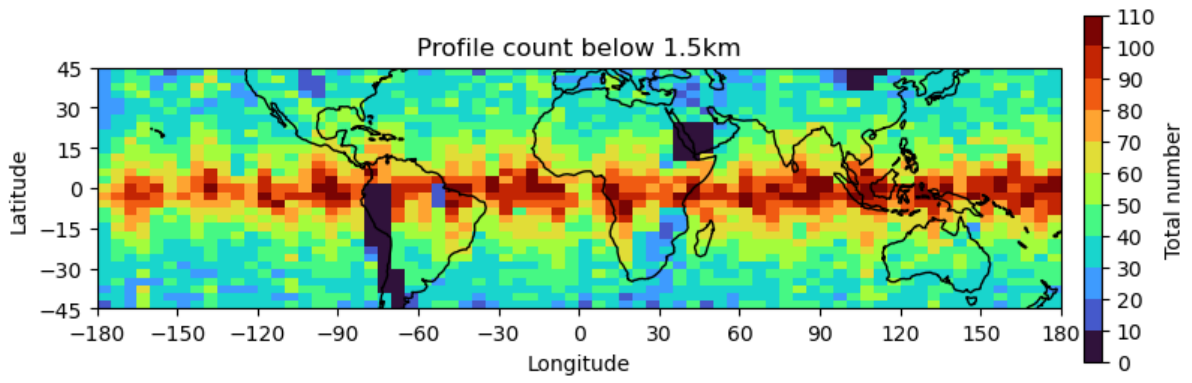
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628 **Table 2: Global mean RMSE of each REFB estimation in comparison to the real REFB below 1.5 km**

Global mean RMSE	LSW-based	<i>TQ</i> -based	MVE
Training data set	2.033	1.614	1.088
Testing data set	2.815	2.266	1.731

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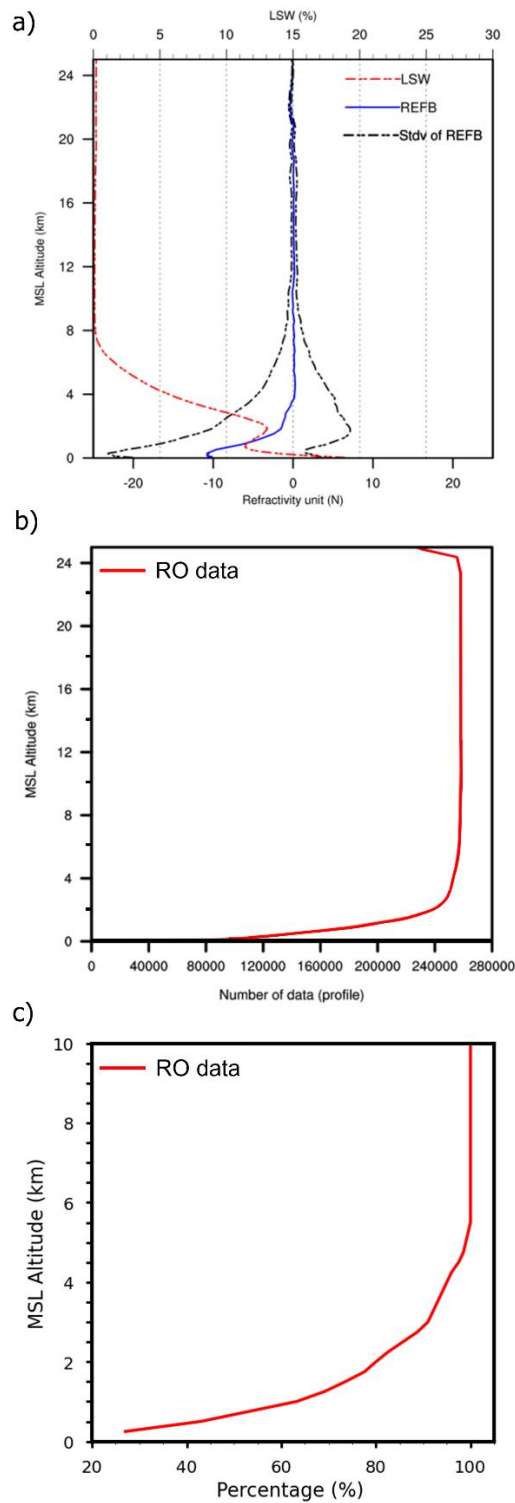


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632 **Figure 1: Number of FS7/C2 RO profiles below the 1.5 km height during the study period (unit: number of profiles).**

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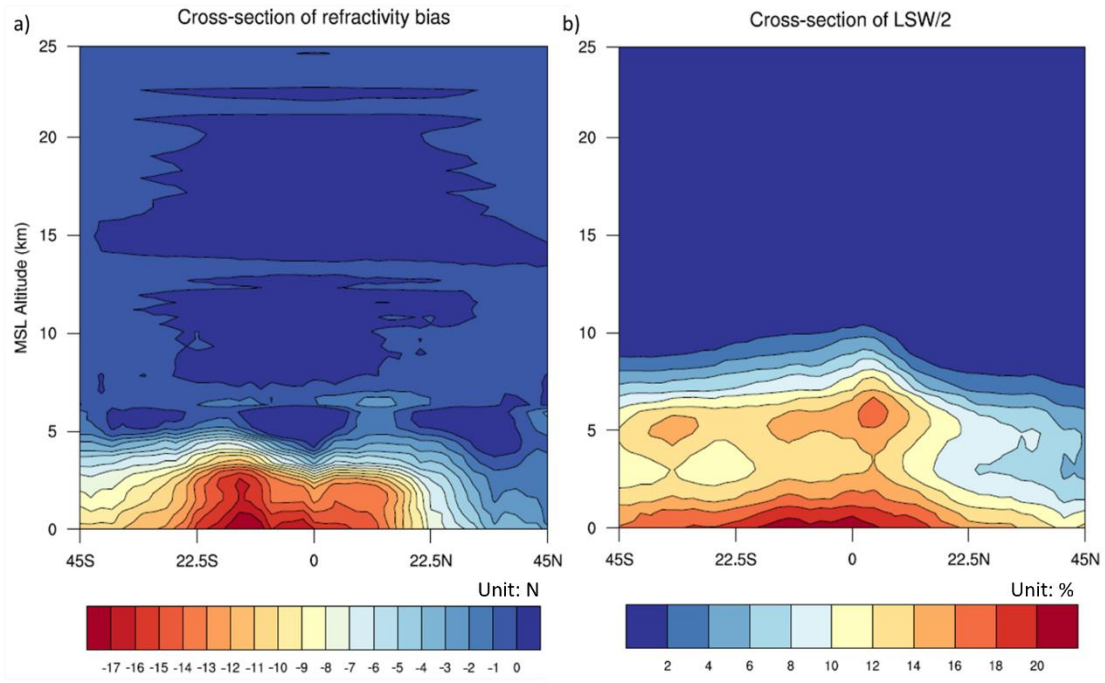
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636 **Figure 2: (a) Mean and standard deviation of REFB and mean LSW as a function of height. (b) The amount of available**
 637 **RO data, and (c) the percentage of profiles as a function of height in reference to the total number at 10 km. The RO**
 638 **data are from 1st December 2019 to 29th February 2020.**

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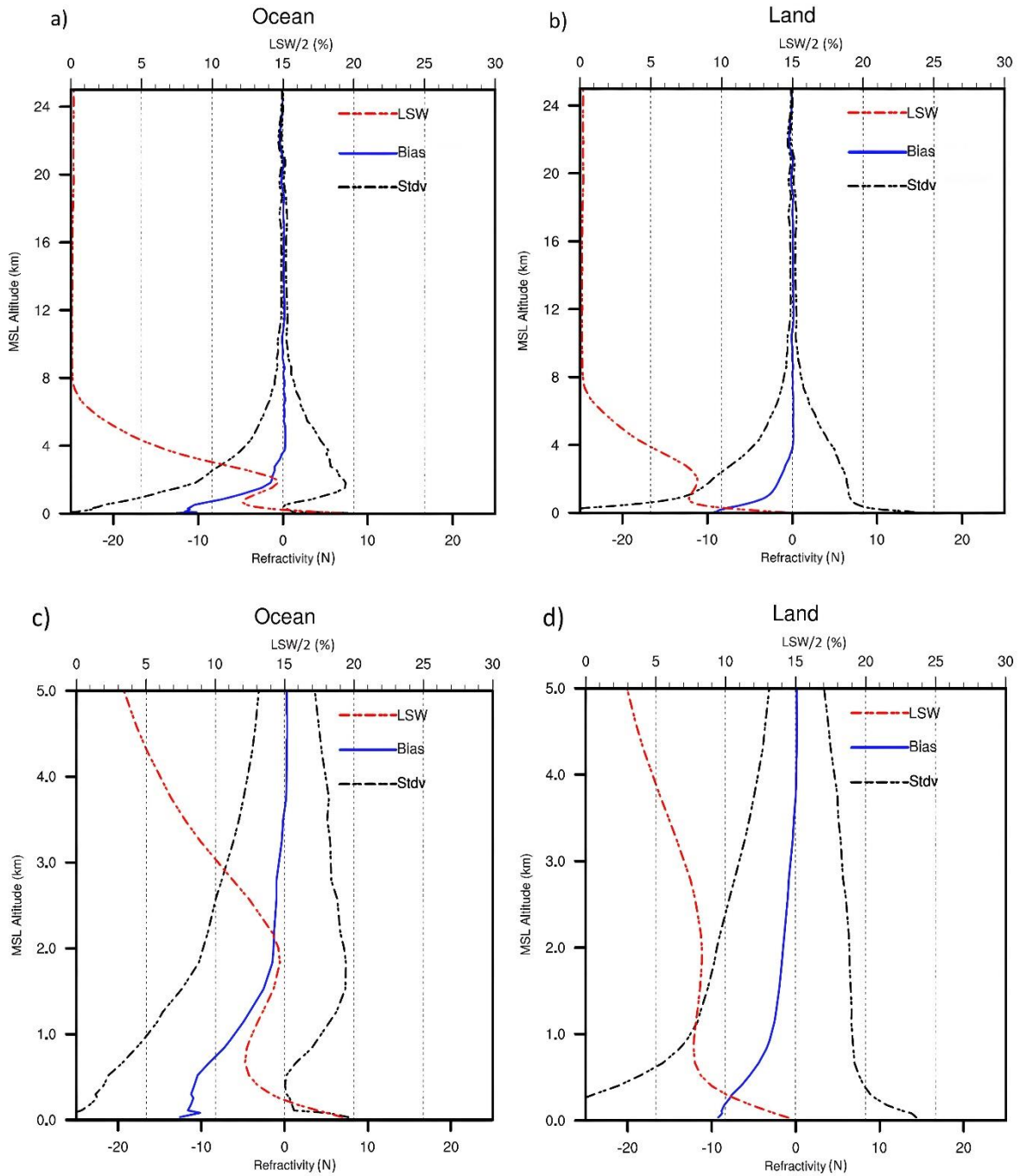
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Figure 3: The cross-sections of (a) zonal mean REFB and (b) mean LSW/2 from 1st December 2019 to 29th February 2020.



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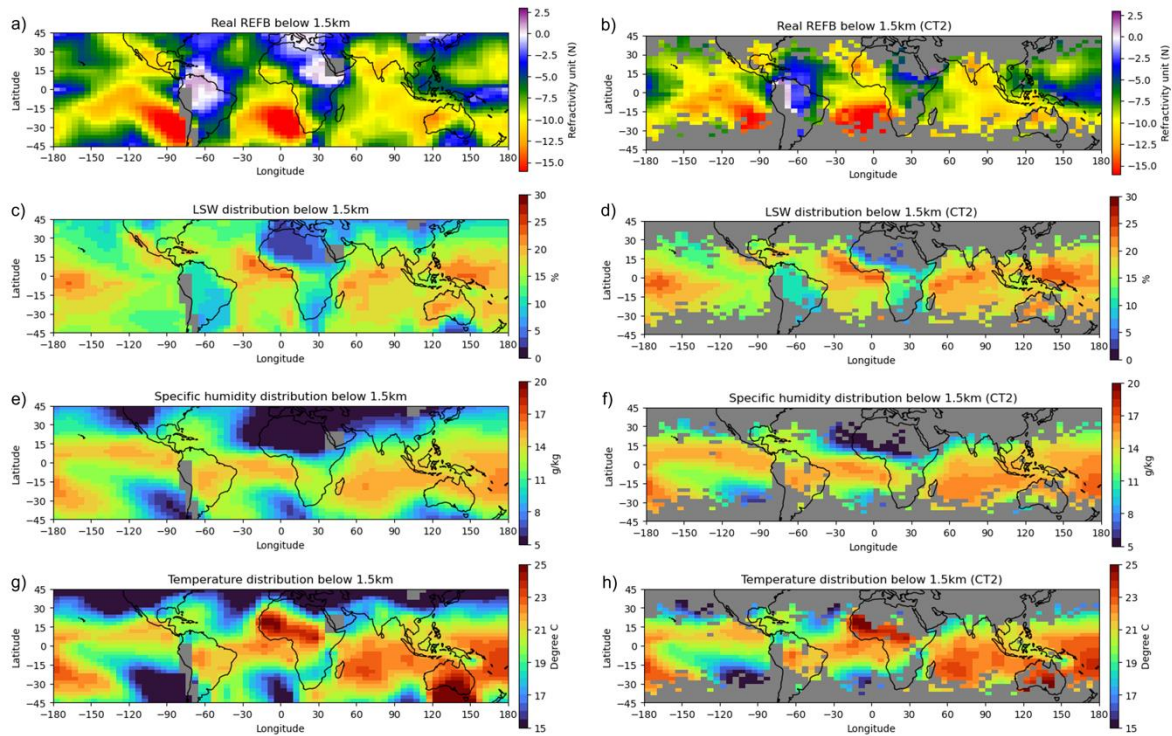
645

646 **Figure 4: (a) and (b) are vertical profiles of the mean and standard deviation of REF B, and mean LSW with altitudes**

647 **up to 25 km over ocean and land, respectively. (c) and (d) are the same as (a) and (b) except zoomed versions below 5**

648 **km.**

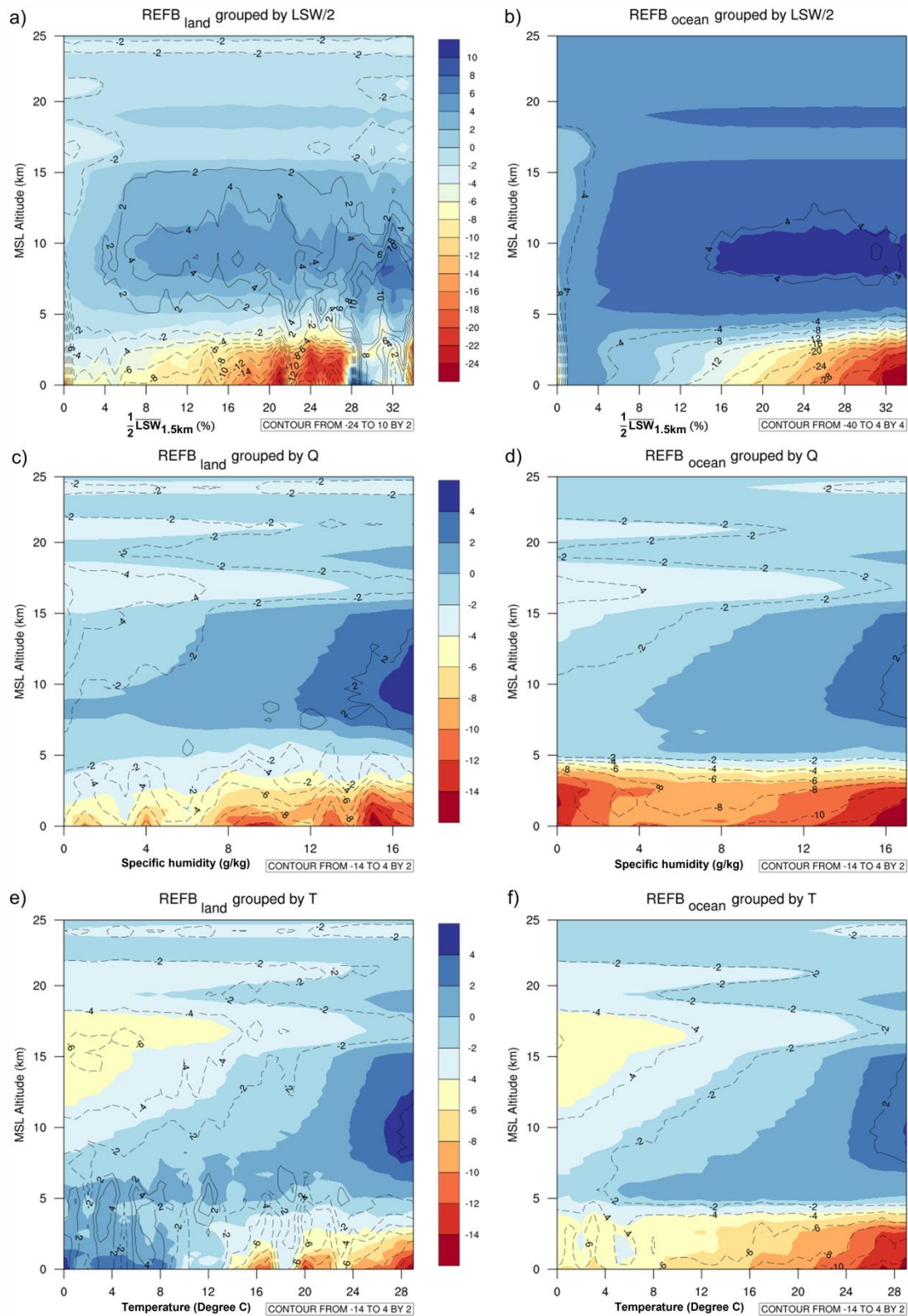
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650

651 **Figure 5: Horizontal distribution of (a) REFB (N units), (c) LSW (%), (e) specific humidity ($g\ kg^{-1}$), and (g) temperature**
 652 **($^{\circ}C$) during the study period. The values of REFB, LSW, specific humidity and temperature are averages over the**
 653 **lowest 1.5 km MSL of the atmosphere. (b), (d), (f) and (h) are the same as (c), (c), (e) and (g), but they are calculated**
 654 **with the criterion that at least 30 profiles penetrate below 0.5 km in each box.**

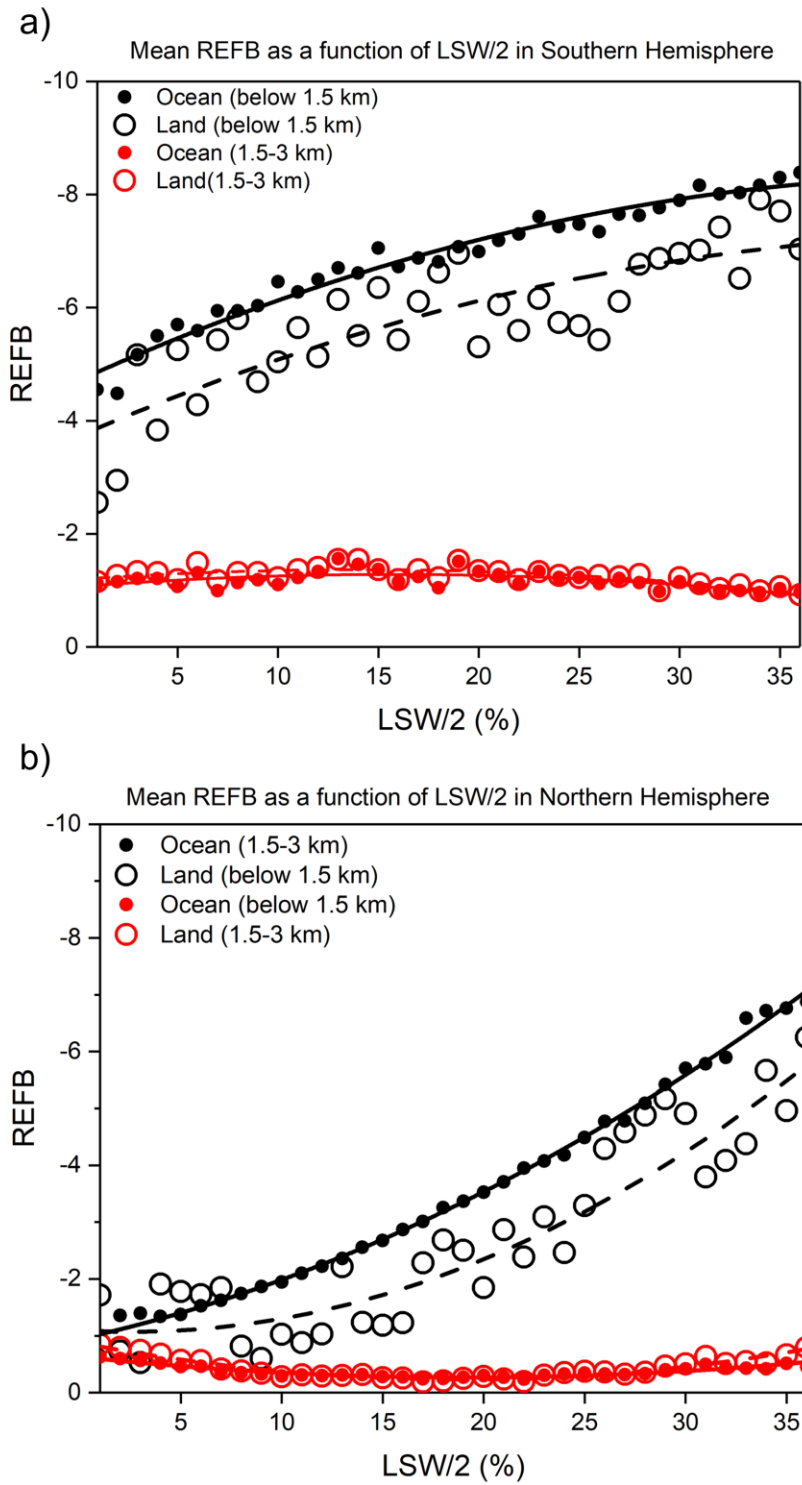
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657 **Figure 6: Refractivity bias as a function of height and average values over the lowest 1.5 km above MSL of (a) LSW/2,**
 658 **(c) specific humidity and (e) temperature over land. (b), (d) and (f) are the same as (a), (c) and (e), except over the ocean.**
 659 **The color shading shows the result using the RO profiles penetrating below 1.5 km while the contour uses the RO**
 660 **profiles penetrating below 0.5 km.**

661



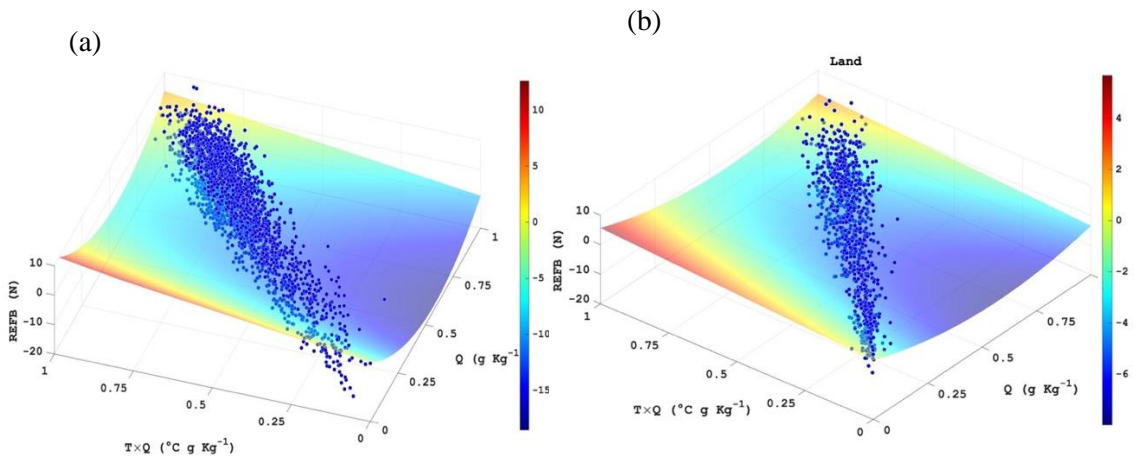
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663 **Figure 7: Relationship between LSW/2 and REFB. The solid and dashed lines represent the REFB computed from the**
 664 **statistical model for the ocean and land, respectively, as a function of LSW/2 (Southern Hemisphere only). LSW/2 and**
 665 **REFB are averaged below 1.5 km.**

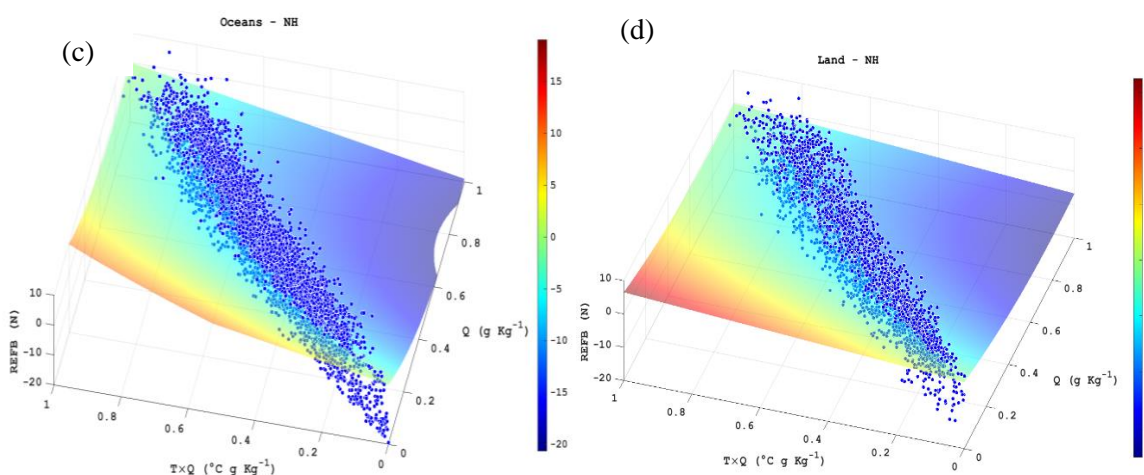
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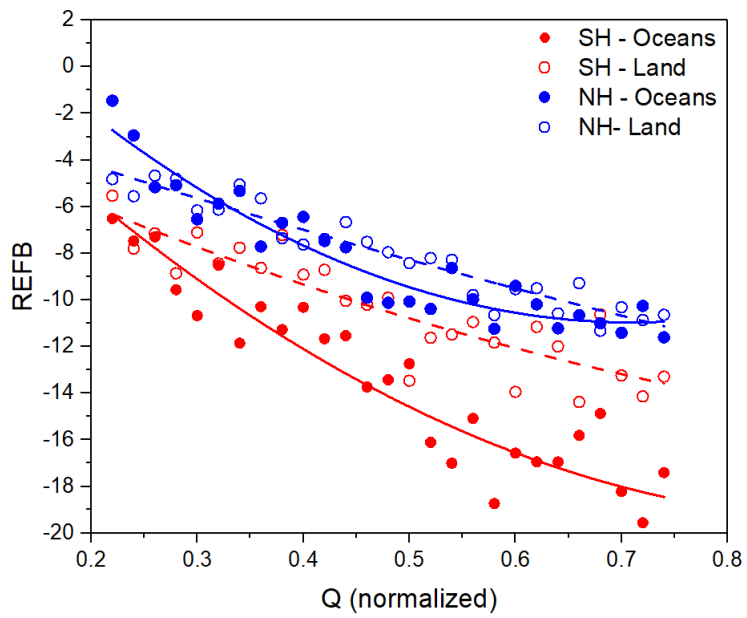
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671 **Figure 8: The relationship among REF B, normalized specific humidity, product of normalized temperature and**
672 **normalized specific humidity of a) oceans and b) land in the Southern Hemisphere. The scatters are the averaged values**
673 **of each profile below the lowest 1.5 km MSL. The surfaces show the model computed from statistical model (Eq. 3) as**
674 **the function of normalized specific humidity and product of normalized temperature and humidity. (c) and (d) are the**
675 **same as (a) and (b), but for the Northern Hemisphere.**

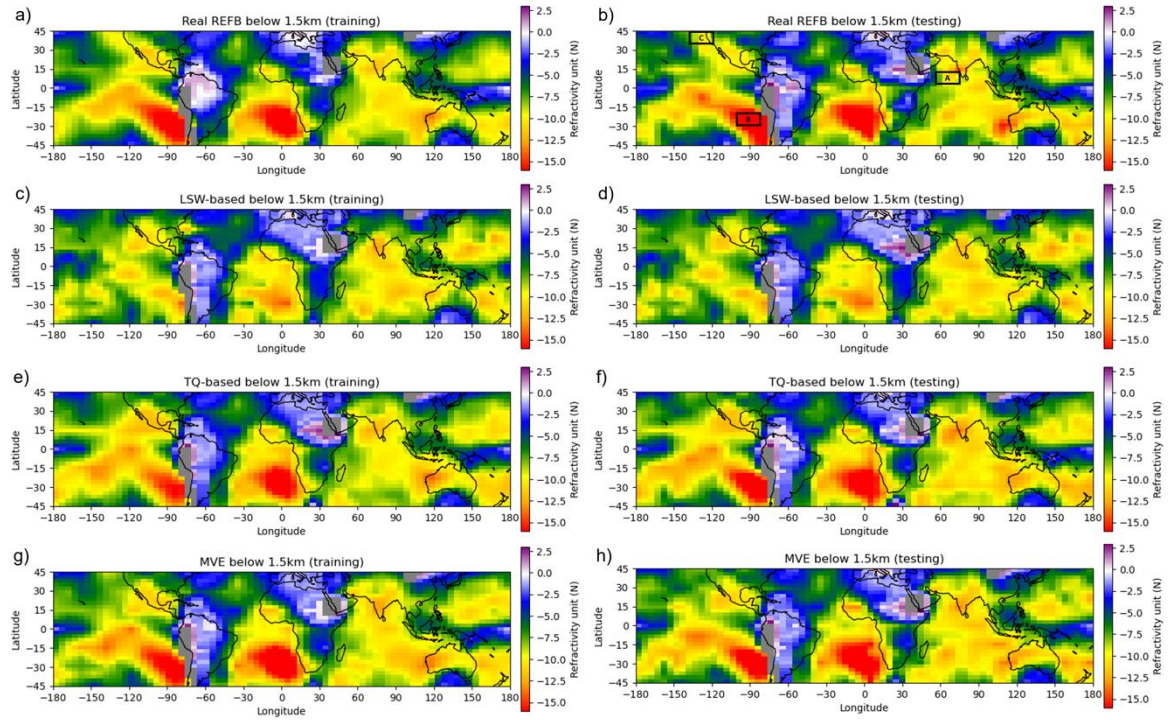
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678 **Figure 9: The relationship between REFB and normalized Q given a condition of normalized $TQ=0.5$.**

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680

681 **Figure 10: Horizontal distribution of refractivity bias and different estimated refractivity biases. The boxes denoted A**

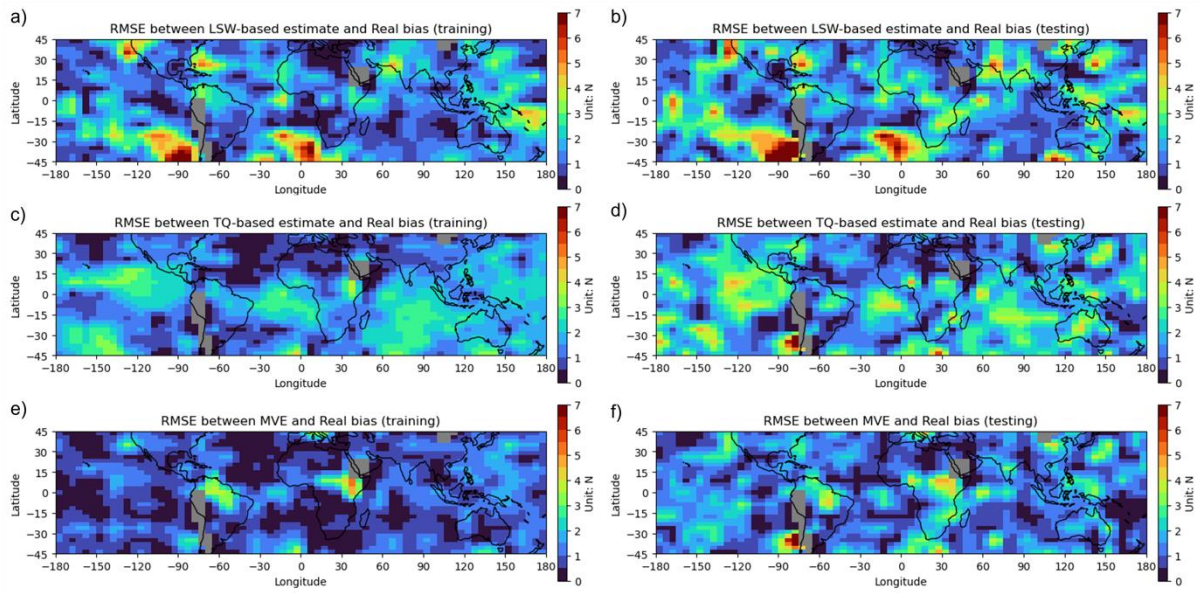
682 **and B are the example boxes used in Figures 12 and 13, respectively. All variables used to construct this figure are**

683 **averaged below 1.5km. Area A is in the region of $0^{\circ} < \text{Lat} < 10^{\circ}\text{N}$ and $55^{\circ}\text{E} < \text{Lon} < 75^{\circ}\text{E}$, Area B is in the region of 20°S**

684 **$< \text{Lat} < 30^{\circ}\text{S}$ and $105^{\circ}\text{W} < \text{Lon} < 85^{\circ}\text{W}$, and Area C is in the region of $35^{\circ}\text{S} < \text{Lat} < 45^{\circ}\text{S}$ and $120^{\circ}\text{W} < \text{Lon} < 135^{\circ}\text{W}$.**

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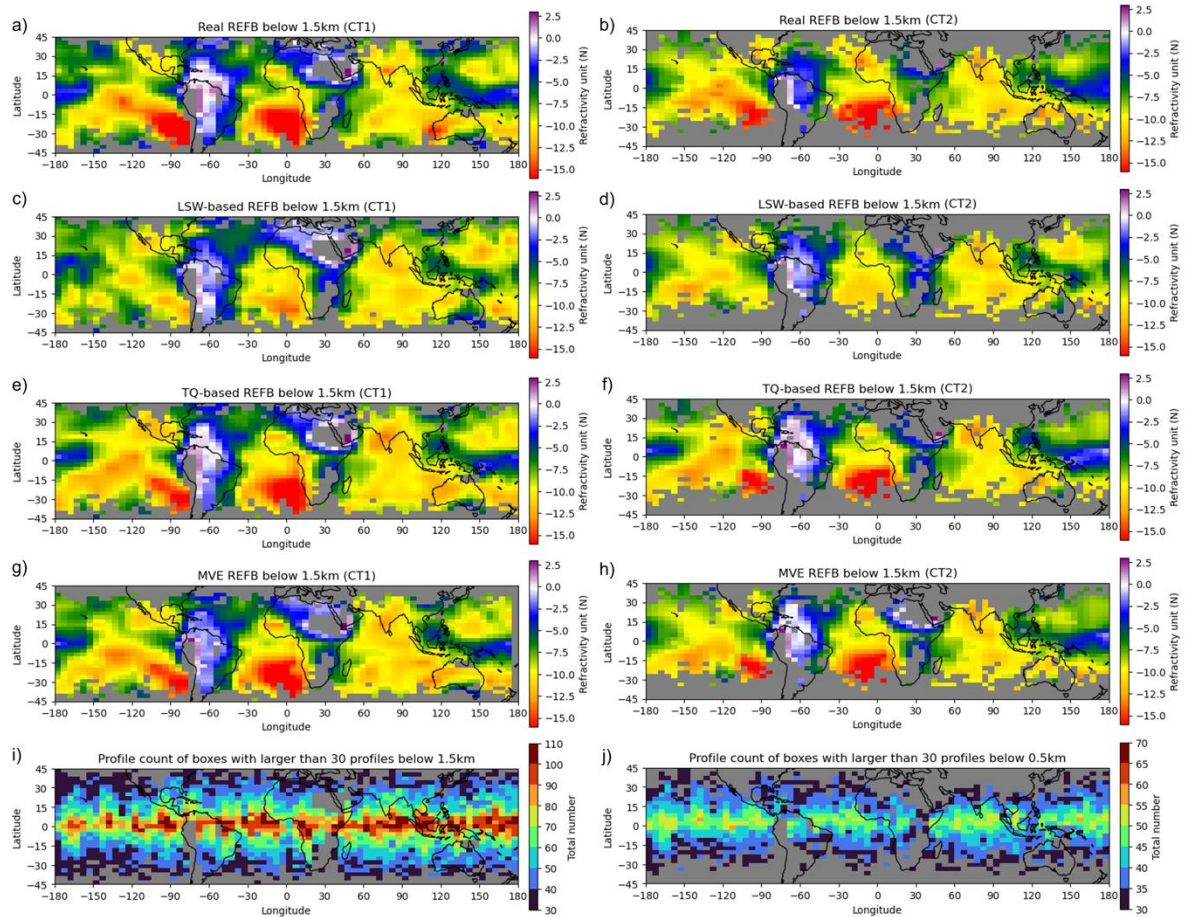
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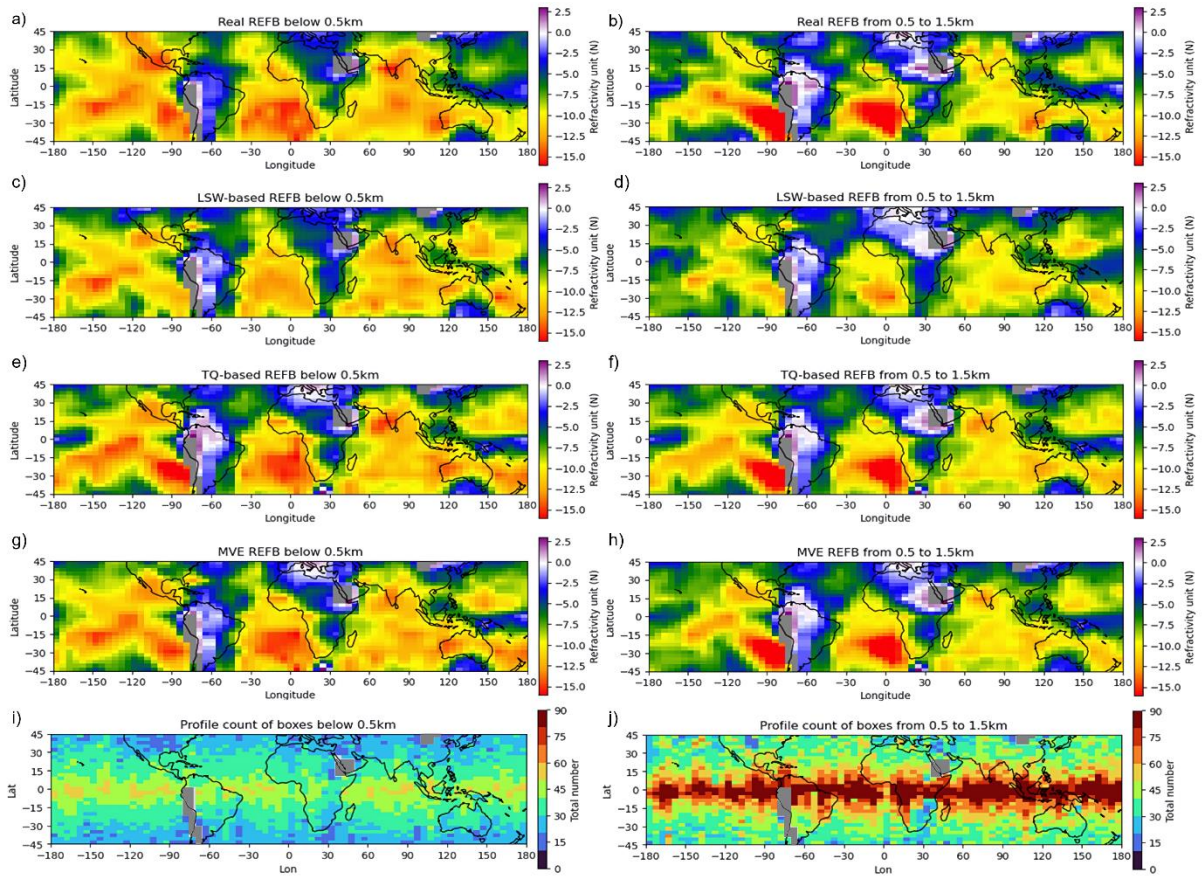
688 **Figure 11: Horizontal distribution of RMSE between the real REFB and estimated REFB by different methods with**
689 **training (left column) and testing (right column) data.**

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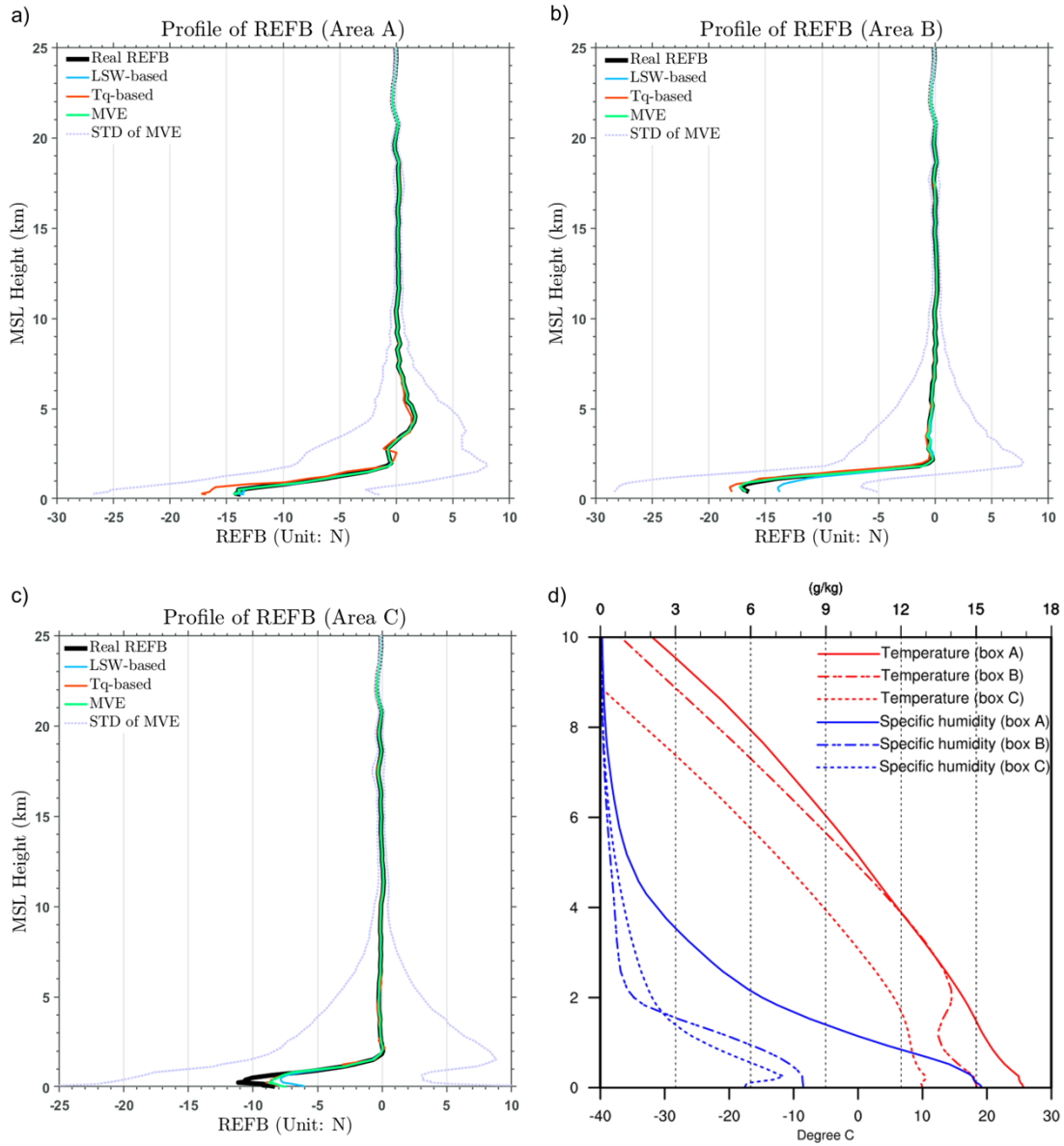
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692 **Figure 12:** The same as Fig. 10, but the calculation is done for RO data with different criteria (CT1 and CT2) of sample
 693 selection. CT1 requires at least 30 RO profiles penetrate below 1.5 km in each box, and CT2 is the same as CT2 except
 694 that the profiles penetrate 0.5 km. (i) and (j) are the horizontal distribution of the profile count with criterion CT1 and
 695 CT2, respectively.



696

697 **Figure 13: The same as Fig. 10, but the calculation is done for RO data from different levels. The left column uses the**
 698 **data below 0.5 km and the right column use the data between 0.5 and 1.5 km. (i) and (j) are the horizontal distribution**
 699 **of the profile count below 0.5km and between 0.5 and 1.5 km, respectively.**



700 **Figure 14: Profiles of refractivity bias (real and estimates) for two different areas selected in Fig. 10a. Boxes A, B and**
 701 **C are in ($0^\circ < \text{Lat} < 10^\circ\text{N}$, $55^\circ\text{E} < \text{Lon} < 75^\circ\text{E}$) and ($20^\circ\text{S} < \text{Lat} < 30^\circ\text{S}$, $105^\circ\text{W} < \text{Lon} < 85^\circ\text{W}$) and ($35^\circ\text{S} < \text{Lat} < 45^\circ\text{S}$**
 702 **and $120^\circ\text{W} < \text{Lon} < 135^\circ\text{W}$). (d) Profiles of temperature (red lines) and specific humidity (blue lines) averaged for**
 703 **Areas A (solid lines), B (long-dashed lines) and C (short-dashed line) shown in Fig. 10b.**

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