

Bayesian multi-proxy reconstruction of early Eocene latitudinal temperature gradients

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Abstract

Accurately reconstructing large-scale palaeoclimatic patterns from sparse local records is critical for understanding the evolution of Earth's climate. Particular challenges arise from the patchiness, uneven spatial distribution, and disparate nature of palaeoclimatic proxy records. Geochemical data typically provide temperature estimates via transfer functions derived from experiments. Similarly, transfer functions based on the climatic requirements of modern taxa exist for some fossil groups, such as pollen assemblages. In contrast, most ecological and lithological data (e.g. coral reefs and evaporites) only convey information on broad climatic requirements. Historically, most large-scale proxy-based reconstructions have used either geochemical or ecological data, but few studies have combined multiple proxy types into a single quantitative reconstruction. Large spatial gaps in existing proxy records have often been bridged by simple averaging, without taking into account the spatial distribution of samples, leading to biased temperature reconstructions. Here, we present a Bayesian hierarchical model to integrate ecological data with established geochemical proxies into a unified quantitative framework, bridging gaps in the latitudinal coverage of proxy data. We apply this approach to the early Eocene climatic optimum (EECO), the interval with the warmest sustained temperatures of the Cenozoic. Assuming the conservation of thermal tolerances of modern coral reefs and mangrove taxa, we establish broad sea surface temperature ranges for EECO coral reef and mangrove sites. We integrate these temperature estimates with the EECO geochemical shallow marine proxy record to model the latitudinal sea surface temperature gradient and global average temperatures of the EECO. Our results confirm the presence of a flattened latitudinal temperature gradient and unusually high polar temperatures during the EECO, which is supported by high-latitude ecological

32 data. We show that integrating multiple types of proxy data, and adequate prior information, has the
33 potential to enhance quantitative palaeoclimatic reconstructions, improving temperature estimates from
34 datasets with limited spatial sampling.

35 **Keywords**

36 Palaeoclimate, latitudinal temperature gradients, temperature proxies, Eocene, sampling bias, Bayesian

37 **Introduction**

38 Understanding the long-term evolution of Earth's climate system and contextualising contemporary global
39 warming relies on accurate reconstructions of past climates (Royer et al., 2004; Burke et al., 2018; Tierney
40 et al., 2020). Recent advances in the synthesis of palaeoclimatic data (e.g. Veizer and Prokoph, 2015; Hollis
41 et al., 2019; Song et al., 2019; Grossman and Joachimski, 2022; Judd et al., 2022) are offering
42 unprecedented insights into the complex and dynamic nature of the Earth's climate system, yet a
43 fundamental challenge remains: the proxy record of past climates is spatially incomplete and afflicted by
44 imperfect preservation and uneven sampling (Judd et al., 2020; Jones and Eichenseer, 2022; Judd et al.,
45 2022).

46 Acknowledging the assumptions and limitations inherent in geochemical temperature proxies, such as
47 experimentally derived calibrations, influences from seasonality, dissolution effects and differential
48 preservation (e.g. Tierney et al., 2017), can enable robust estimates of palaeotemperature at local scales.
49 However, recent work has demonstrated that spatial biases in the geochemical proxy record can lead to
50 spurious estimates of regional (e.g. latitudinal temperature gradients) and global temperatures (Judd et al.,
51 2020; Jones and Eichenseer, 2022). Principally, this can be driven by two factors: (1) missing data for some
52 regions (e.g. no high-latitude data); or (2) overrepresentation of other regions (e.g. a high proportion of
53 samples from tropical areas). The latter can be addressed through the down-sampling of data or restricting
54 analyses to specific regions (e.g. Song et al., 2019). However, in order to robustly infer regional or global-
55 scale patterns from an incomplete record, spatial gaps must ultimately be bridged. One common approach,
56 which requires no additional computation, is the spatial visualisation of proxy-derived temperatures against
57 latitude, showing broad latitudinal temperature trends (e.g. Hollis et al., 2019; Vickers et al., 2021).
58 Interpolation is also sometimes used to bridge spatial gaps in palaeoclimatic data (e.g. Taylor et al., 2004),
59 taking advantage of the autoregressive nature of climatic data: much of the information on the climate of
60 any given location is contained in the climate data of nearby locations (Reynolds and Smith, 1994). Adding
61 to this, some proxy-based reconstructions use statistical modelling to infer palaeoclimatic patterns. For

62 example, polynomial regression (Bijl et al., 2009) and cosine functions (Inglis et al., 2020) have been used
63 to reconstruct latitudinal temperature gradients, and 2D-reconstructions of surface temperatures have been
64 created with Gaussian process regression (Inglis et al., 2020). These approaches work well for interpolating
65 relatively densely-sampled data, but the absence of constraints on the modelled parameters means that such
66 models can produce unrealistic temperature estimates when extrapolating from sparse data. Statistical
67 modelling in a Bayesian framework can help overcome this problem by requiring the explicit specification
68 of priors for the model parameters, which can be used to express physical constraints (Chandra et al., 2021).

69 Spatial gaps in the palaeoclimatic record can also be addressed through the integration of additional data.
70 For example, lithological and fossil data can be used to infer past climatic conditions based on analogous
71 modern sediments (Chandra et al., 2021), or based on the premise that the climatic requirements of ancient
72 taxa, biological traits, or ecological communities were similar to those of their nearest modern relatives
73 (Peppe et al., 2011; Royer, 2012; Salonen et al., 2019). Despite this potential, the integration of geochemical
74 proxy data with other sources of information (e.g. ecological data) has rarely been realised in a rigorous,
75 quantitative framework (Burgener et al., 2023).

76 Here, we present a novel Bayesian hierarchical model (e.g. Gelman et al., 2013; McElreath, 2018) that
77 combines quantitative proxies and ecological constraints into a fully quantitative model of the latitudinal
78 gradient of sea surface temperatures, bridging spatial gaps in sparsely sampled palaeoclimatic data. The
79 Bayesian approach offers a powerful framework for integrating various sources of uncertainty and
80 modelling complex hierarchical relationships, and is increasingly used in palaeoclimatic reconstructions
81 (e.g. Weitzel et al., 2019; Yang and Bowen, 2022; Burgener et al., 2023). This model expands upon existing,
82 spatially explicit palaeoclimatic reconstructions by allowing for the integration of (1) prior information
83 based on physical principles and the observed modern sea surface temperature distribution, and of (2)
84 geochemical and ecological palaeoclimatic proxies in a common, quantitative framework. We chose a
85 generalised logistic function to accurately infer the shape of the temperature gradient despite a patchy
86 latitudinal coverage. This choice is motivated by the flexibility and ability of this function to approximate
87 a variety of nonlinear patterns in the underlying temperature gradients that other parametric approaches,
88 such as lower order polynomials (e.g. Bijl et al., 2009; Keating-Bitonti et al., 2011), lack. We test the
89 robustness of this method using down-sampled, simulated latitudinal temperature gradients.

90 We apply this model to the record of the early Eocene climatic optimum (EECO), combining a compilation
91 of geochemical proxies (Hollis et al., 2019), mangrove communities (Popescu et al., 2021), and coral reefs
92 (Zamagni et al., 2012). We use a nearest-living-relative approach (e.g. Greenwood et al., 2017) to establish
93 broad temperature ranges for the ecological data. We choose the EECO to demonstrate the application of
94 the model due to its significance as the interval with the warmest sustained temperatures of the Cenozoic

95 (Pross et al., 2012), rendering it a potential analogue for extreme climate warming scenarios (Burke et al.,
 96 2018). Our integrative approach allows us to shed new light on the long-standing dispute on the steepness
 97 of the early Eocene temperature gradient (Table 1; Sloan and Barron, 1990; Markwick, 1994; Huber and
 98 Caballero, 2011; Tierney et al., 2017; Inglis et al., 2020).

99 Table 1: Inferred latitudinal sea surface temperature (SST) gradients for the early Eocene (EE) or the EECO,
 100 as shown in earlier, proxy-based studies. The gradient values denote the SST difference between the equator
 101 and the polar circle, or other types of gradients. For comparison, a gradient derived from an atmosphere-
 102 ocean general circulation model (GCM) ensemble, and a range of gradients from a model intercomparison
 103 project, are also shown.

Source	Time	Gradient (°C)	Type of gradient	Model	Proxy system
Bijl et al. (2009)	EE	7	equator - polar circle	2 nd order polynomial	<i>TEX</i> ₈₆ , <i>UK</i> ₃₇ ^{K'}
Keating-Bitoni et al. (2011)	EECO	13	equator - polar circle	2 nd order polynomial	<i>TEX</i> ₈₆ , MBT/CBT, Δ_{47} , Mg/Ca, $\delta^{18}O$
Tierney et al. (2017)	EE	12	equator - polar circle	Gaussian function	<i>TEX</i> ₈₆
Cramwinckel et al. (2018)	EECO	21 (± 1)	equator - deep water	-	<i>TEX</i> ₈₆ , Δ_{47} , Mg/Ca, $\delta^{18}O$, deepwater $\delta^{18}O$
Evans et al. (2018)	EE	20 (± 3)	tropics - deep water	-	Δ_{47} , deepwater Mg/Ca
Pross et al. (2012), as shown in Tierney et al. (2017)	EE	26	equator - polar circle	climate model ensemble	none (GCM simulations)
Lunt et al. (2021)	EECO	18–26	tropics - high latitude	DeepMIP climate models	none (GCM simulations)

104 **Materials & Methods**

105 **Geochemical data**

106 Geochemical climatic proxy data were extracted from a latest Paleocene and early Eocene compilation
 107 (Hollis et al., 2019). This compilation provides sea surface temperature data on four different geochemical
 108 proxies for reconstructing seawater temperature: $\delta^{18}O$, Δ_{47} , Mg/Ca and *TEX*₈₆. For our analyses, this dataset
 109 was restricted to the EECO (defined as 53.8–49.1 Ma) and samples originating from near the ocean surface

110 or mixed layer. Consequently, samples labelled as “thermocline”, or “sub-thermocline”, were excluded.
111 Recrystallised $\delta^{18}\text{O}$ samples were also excluded as secondary diagenetic calcite precipitated after deposition
112 can bias isotope measurements and offset temperature values (Schrag, 1999). This filtering resulted in most
113 $\delta^{18}\text{O}$ samples being excluded from the dataset (retaining 8 out of 152). After data filtering, 308 geochemical
114 proxy samples from 23 locations remained (Fig. 1). For a detailed description of each proxy see Hollis et
115 al. (2019).

116 **Ecological data**

117 **Coral reefs.** Today, shallow warm-water coral reefs are limited to tropical and subtropical latitudes
118 ($\sim 34^\circ\text{N}$ – 32°S), with minimum sea surface temperature tolerances ($\sim 18^\circ\text{C}$) being the primary constraint
119 on this distribution (Johannes et al., 1983; Kleypas et al., 1999; Yamano et al., 2001). As coral reefs reside
120 at the upper thermal limit of the oceans today, their maximum sea surface temperature tolerance is less
121 well-constrained, with some studies suggesting up to 35.6°C in the geological past (Jones et al., 2022).
122 Nevertheless, coral reefs have frequently been recognised as tracers of past (sub-)tropical conditions
123 (Ziegler et al., 1984; Kiessling, 2001). During the Eocene, coral communities and reefs expanded across
124 tropical and temperate latitudes, with communities found up to palaeolatitudes of 43°N (Zamagni et al.,
125 2012). Using a compilation of Paleocene–early Eocene coral reefs and community localities (Zamagni et
126 al., 2012), we generated quantitative sea surface temperature estimates for the EECO. To do so, we
127 extracted localities from the compilation that are inferred to be Ilerdian (early Eocene) coral reefs, and that
128 could be confidently assigned to the EECO. We excluded coral knobs and coral-bearing mounds which
129 might have broader climatic limits than warm-water coral reef ecosystems. This filtering resulted in four
130 unique coral reef localities remaining for the EECO, all of which conform to the modern latitudinal range
131 of coral reefs ($<34^\circ\text{N}$). Subsequently, we used statistically derived temperature limits (minimum = 21°C ,
132 average = 27.6°C , maximum = 29.5°C) from the published literature (Kleypas et al., 1999) to define a
133 normal probability distribution of potential temperature values for coral reef localities. This normal
134 probability distribution was defined with a mean of 27.6°C and a standard deviation of 2.125°C , which
135 places the minimum (21°C) at the lower end of the 95% highest density interval of that distribution. As the
136 distribution of modern corals is skewed towards warmer temperatures, this approach results in 16.5% of
137 the probability being placed on temperatures $> 29.5^\circ\text{C}$, allowing for the possibility that Eocene coral reefs
138 were adapted to warmer conditions than present-day coral reefs.

139 **Mangroves.** Mangroves are distributed throughout the tropics and subtropics today. While factors besides
140 sea surface temperatures (SST) influence the distribution of mangroves, empirical lower temperature limits
141 have been established for the genera *Avicennia* (15.6°C) and *Rhizophora* (20.7°C) (Quisthoudt et al., 2012).
142 Both *Avicennia* and members of the Rhizophoraceae family were widespread and co-occurred across

143 tropical and temperate latitudes in the early Eocene. Only *Avicennia*, however, occurred at polar latitudes
 144 (Suan et al., 2017; Popescu et al., 2021). Assuming that Eocene members of these mangrove taxa conform
 145 to similar climatic requirements as their modern relatives, the presence and absence of *Avicennia* and
 146 Rhizophoraceae pollen can be used as a palaeotemperature indicator. For this analysis, published mangrove
 147 occurrence data were taken from Popescu et al. (2021), and converted to quantitative temperature estimates.
 148 From this data, we identify two types of pollen assemblages which we ascribe different temperature
 149 distributions:

- 150 1) *Avicennia*-only assemblages ($n = 2$): the absence of Rhizophoraceae is indicative of temperatures
 151 between 15.6°C (lower temperature limit of *Avicennia*) and 20.7°C (lower temperature limit of
 152 *Rhizophora*). However, a value of 22.5°C is assumed as the upper temperature limit here as
 153 *Rhizophora* is rare below this temperature. We define the *Avicennia*-only temperature distribution
 154 as a normal distribution with a mean of 19.05°C and a standard deviation of 1.725°C, resulting in
 155 95% of the probability density being placed within the temperature limits.
- 156 2) *Avicennia* and Rhizophoraceae assemblages ($n = 5$): the presence of both groups suggests that
 157 the locality should have a minimum temperature of 20.7°C (lower temperature limit of
 158 *Rhizophora*). As the upper thermal limits of *Avicennia* and *Rhizophora* are not well established
 159 in Quisthoudt et al. (2012), we assign the same maximum temperature limits (29.5°C) as coral reef
 160 reef localities, because mangroves are also widely distributed throughout tropical regions.
 161 Consequently, we define the temperature distribution for this locality as a normal distribution
 162 with a mean of 25.1°C and a standard deviation of 2.2°C, with 95% probability density within the
 163 temperature limits.

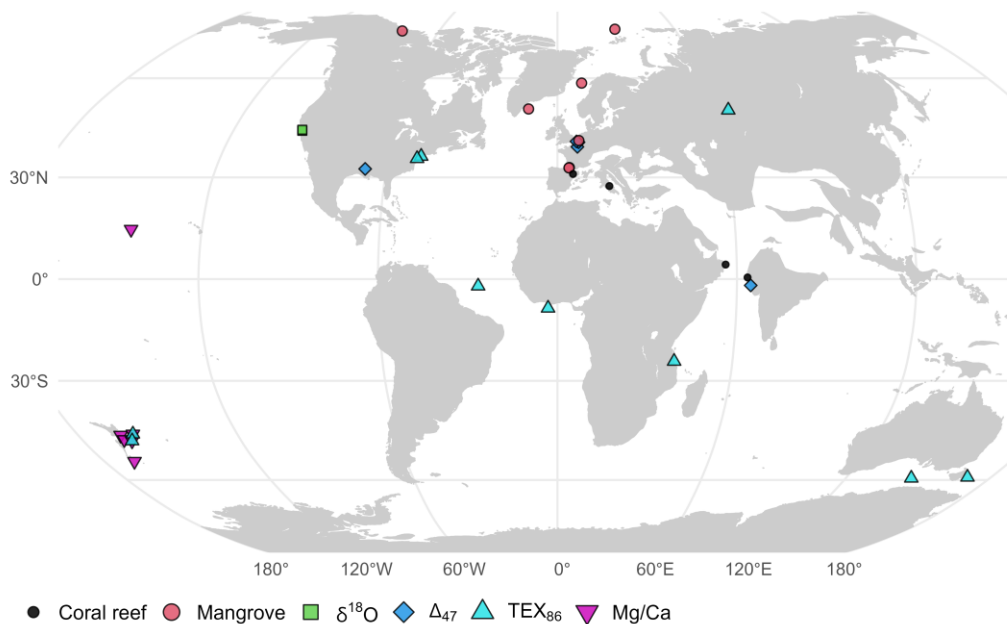


Figure 1: Palaeogeographic distribution of the geochemical and ecological data compilation used in this study. Map is presented in the Robinson projection (ESRI:54030).

164 **Palaeogeographic reconstruction**

165 The palaeogeographic distribution of geochemical and ecological data was reconstructed using the Merdith
166 et al. (2021) Global Plate Model via the palaeoverse R package (version 1.2.0, Jones et al., 2023). The
167 midpoint age of the EECO (51.2 Ma), along with the present-day coordinates of geochemical and ecological
168 data, were used for palaeogeographic reconstruction.

169 **Bayesian framework**

170 **Model structure.** We model the mean temperature (μ) at location j as a function of absolute latitude
171 ($abs(l)$) with a logistic regression (also known as “growth curve” or “Richard’s curve”) of the form:

$$172 \quad \mu_j \sim N(v_j, \sigma), \quad (1)$$

$$173 \quad v_j = A + \frac{K - A}{1 + e^{B(abs(l_j) - M)}}, \quad j = 1, \dots, n, \quad (2)$$

174 where A and K denote the lower and upper asymptote, respectively, M specifies the latitude of maximal
175 growth, i.e. the latitude around which temperature falls most steeply with latitude, B denotes the growth
176 rate, σ denotes the residual standard deviation, and n denotes the number of locations.

177 We use this generalised logistic function because it can follow the equatorial and polar asymptotes observed
178 in the modern, latitudinal SST gradient, but can also accommodate a variety of other shapes, while
179 consisting of only four shape parameters. This flexibility is primarily achieved by shifting the location of
180 the curve along the latitudinal axis by varying M , and by altering the steepness of the curve by varying B .
181 For example, one limb of a second-order polynomial as in Bijl et al. (2009) can be approximated by
182 increasing M towards high latitudes, and decreasing B to reduce the steepness of the curve. The model is
183 designed for modelling the average gradient across both hemispheres, but can also be applied to individual
184 hemispheres, to assess hemispherical differences (see Fig. S4).

185 We infer μ_j from m individual temperature observations $t_{i=1, \dots, m}$, derived from geochemical data, at
186 location j as

$$187 \quad t_{i,j} \sim N(\mu_j, \sigma_j), \quad i = 1, \dots, m, \quad (3)$$

188 where m is the number of observations at each location, and σ_j is the estimated standard deviation of the
189 temperatures at location j .

190 Similarly, μ_j is inferred for locations with ecological proxies from the associated normal temperature
 191 distributions with a given mean and standard deviation, $t_{\mu,j}$ and $t_{\sigma,j}$, as

$$192 \quad t_{\mu,j} \sim N(\mu_j, t_{\sigma,j}). \quad (4)$$

193 This structure implies that μ_j is not fixed at the mean proxy temperature at location j , but is drawn towards
 194 the overall logistic regression curve, i.e. towards v_j . The pull towards v_j tends to be strong when m is low,
 195 when the observations $t_{i=1,\dots,m,j}$ are scattered, i.e. σ_j is high, and/or when the overall standard deviation σ
 196 is low. In practice, this has the desirable consequence that locations with few observations and large
 197 temperature differences between observations have less influence on the overall regression than well-
 198 sampled locations with consistent reconstructed temperatures.

199 We show an expanded model that includes uncertainties on individual temperature observations in the
 200 Supplementary Material (Fig. S5).

201 **Priors.** In a Bayesian framework, priors need to be placed on the unknown parameters of a model. We
 202 placed weakly informative, conjugate inverse-gamma priors on σ and $\sigma_{j=1,\dots,n}$:

$$203 \quad \sigma \sim \sqrt{\text{Inv-Gamma}\left(\alpha + \frac{n}{2}, \beta + 0.5 \times (\mu_j - v_j)\right)}, \quad j = 1, \dots, n, \quad (5)$$

$$204 \quad \sigma_j \sim \sqrt{\text{Inv-Gamma}\left(\alpha + \frac{m}{2}, \beta + 0.5 \times (t_{i,j} - \mu_j)\right)}, \quad i = 1, \dots, m, \quad j = 1, \dots, n. \quad (6)$$

205 We set $\alpha = \beta = 1$, allowing these priors to be quickly overwhelmed by the data as n and m increase, as
 206 we have little *a priori* knowledge of these parameters.

207 In contrast, we put informative priors on the regression coefficients A , K , M and B , based on physical
 208 principles, and loosely based on the modern climate system:

209 **A.** Predicted seawater surface temperatures are not allowed to be $\ll -2^\circ\text{C}$, the freezing point of sea water.
 210 The highest prior density of A is placed around 0°C , and it slowly tapers off towards higher temperatures.
 211 This shape is achieved by placing a skew-normal prior on the lower asymptote, specified as

$$212 \quad A \sim SN(\xi = -3.0, \omega = 12, \alpha_{SN} = 30), \quad (7)$$

213 where ξ , ω , and α_{SN} are the location, scale and shape parameters.

214 **K.** Input of solar energy decreases from the tropics to the poles. Hence, the latitudinal temperature gradient
 215 is broadly negative, i.e. temperature decreases with absolute latitude. This is achieved by setting $K \geq A$.
 216 The prior on the upper asymptote K is a truncated normal distribution with the mean set to K of the modern
 217 SST gradient, with a broad standard deviation:

$$218 \quad K \sim TN(\mu_{TN} = 28, \sigma_{TN} = 15, \alpha_{TN} = A, \beta_{TN} = \infty) \quad (8)$$

219 The distribution is truncated to the left at $\alpha_{TN} = A$, but not truncated to the right (β_{TN}).

220 **M.** A uniform prior is placed on the latitude of greatest steepness of the gradient, allowing it to be steepest
 221 anywhere between latitudes 0° and 90° absolute latitude, as this parameter may vary greatly depending on
 222 the climate state:

$$223 \quad M \sim Uniform(0,90) \quad (9)$$

224 **B.** The steepness or growth rate B of the gradient is constrained to be ≥ 0 and to not be exceedingly high,
 225 as oceanic and atmospheric heat transfer is bound to limit very abrupt SST changes across latitudes on a
 226 global scale. A gamma-distributed prior of the form

$$227 \quad B \sim Gamma(\alpha_G = 4.3, \beta_G = 30) \quad (10)$$

228 was placed on B . The shape and rate parameters α_G and β_G were chosen such that the highest prior density
 229 is at B of the modern SST gradient, 0.11. We informed the prior distribution on B based on a provisional
 230 model run with the modern SST data.

231 **Model validation**

232 To test whether our logistic regression model can adequately describe different latitudinal temperature
 233 gradients at various sample sizes, we used the empirical, modern gradient, representative of an icehouse
 234 climate, and generated three idealised gradients that emulate potential climatic states throughout Earth's
 235 geological history: extreme icehouse, icehouse (modern), greenhouse, and extreme greenhouse (Frakes et
 236 al., 1992). The idealised gradients serve to test whether our model setup is able to infer gradients that are
 237 strongly different from the modern from a varying number of samples.

238 We created test data from these gradients as follows: We randomly sampled (1000 iterations) latitudes at
 239 sample sizes of 5, 10 and 20, with the probability of a latitude being sampled scaling with the decreasing
 240 surface area towards higher latitudes, i.e. lower latitudes are sampled more frequently. For the largest
 241 sample size ($n = 34$), we used the latitudes of the EECO data set of this study in all iterations. For each
 242 latitude, we took the location mean temperature from the gradients, adding random noise from a normal

243 distribution with a standard deviation of 3.8, which corresponds to the average uncertainty associated with
244 the EECO geochemical proxy data (Hollis et al. 2019). With that, we aim to simulate randomly distributed
245 errors in the proxy data, which could arise from miscalibrations, measurement errors, seasonal effects, *ect.*
246 We acknowledge that this approach cannot quantify the potential impact of systematic offsets that may bias
247 all proxy data in the same direction, nor do we know whether a standard deviation of 3.8 is the actual
248 average magnitude of uncertainty that the proxy compilation is afflicted with.

249 To evaluate how well the model performed in reconstructing the idealised gradients from limited sampling,
250 we calculated the coefficient of determination (R^2) for Bayesian regression models (Gelman et al., 2019).
251 For every iteration from the posterior, we intercepted the modelled and the idealised gradient in intervals
252 of 1° latitude and calculated the R^2 based on these values. We report the median, and 95% credible intervals
253 (CI) of the resulting R^2 values. Here and in all other instances, the 95% CI refer to the interval between the
254 2.5% point and the 97.5% point of the samples or sampled posterior distribution.

255 To test whether our model can accurately depict the shape of the modern sea surface temperature gradient,
256 and to facilitate comparison with the Eocene gradient, we applied our model to mean annual sea surface
257 temperatures from Bio-Oracle (Assis et al., 2018), aggregated to a spatial grid resolution of $1^\circ \times 1^\circ$
258 ($n = 46,131$). The R^2 for the modern gradient was calculated as above (Gelman et al., 2019), comparing the
259 modelled gradient and the empirical temperature averages in 1° latitude bins. Only the medians are reported
260 for the modern gradient, as the 95% credible intervals are extremely narrow due to the high precision of the
261 posterior estimates.

262 To reconstruct the idealised gradients and the modern gradient, we used a simplified, non-hierarchical
263 version of our model, as every location is associated with only one temperature value, making the
264 hierarchical structure superfluous. To achieve this, we substituted temperature (t_j) for μ_j in Equation 1 and
265 Equation 5.

266 **Parameter estimation**

267 We estimated the posterior distributions of the model parameters using a Markov chain Monte Carlo
268 (MCMC) algorithm, written in R. Specifically, we sampled the unknown parameters A , K , M and B with
269 Metropolis-Hastings, and used Gibbs sampling to estimate all other unknown parameters (see Gilks et al.,
270 1995; Gelman et al., 2013). Posterior inference on the modern gradient is based on four chains with 60,000
271 iterations each, 10,000 of which were discarded as burn-in. Every 10^{th} iteration was retained, resulting in
272 a total of 20,000 iterations with low autocorrelation. The re-sampled, simulated gradients and the re-
273 sampled, modern gradient were modelled in one chain with 10,000 iterations for each of the 1,000 random

274 samples. 5,000 iterations each were discarded as burn-in, and every 25th iteration was kept, resulting in a
275 total of 200,000 iterations across all 1,000 model runs. For the Eocene model, we ran four chains with
276 600,000 iterations each, discarding 100,000 as burn-in and keeping every 100th iteration, as the
277 hierarchical model structure results in higher autocorrelation of the chains. The Eocene posterior inference
278 is thus based on a total of 20,000 iterations with low autocorrelation (effective multivariate sample size for
279 A , K , M and B is $> 18,000$). Trace plots of the MCMC chains indicate convergence and good mixing of the
280 chains (Fig. S1).

281 **Processing of model results**

282 Modelled sea surface temperature estimates were generated with Equation 2, calculating the sea surface
283 temperatures at any latitude with the parameter estimates of each iteration from the posterior samples. The
284 median and 95% CI of temperatures were then taken from all temperature estimates obtained at the latitudes
285 of interest.

286 The latitudinal gradient was calculated as the difference between the modelled temperature at the equator
287 (0° latitude) and at the poles (90° absolute latitude). To facilitate comparison with earlier estimates, we also
288 calculated the gradient with the temperature at the polar circle (66.6° absolute latitude) being used instead
289 of the temperature at the poles.

290 Differences between Eocene and modern temperatures at a certain latitude were calculated by randomly
291 pairing all iterations of the posterior from the Eocene and modern temperature gradient model, calculating
292 the Eocene and modern temperature using the respective iterations, taking the difference, and then
293 calculating the median (95% CI) from all pairs of iterations.

294 Global average temperatures with 95% credible intervals were calculated by taking the weighted mean of
295 the median (95% CI) of temperature estimates in 1° latitudinal bins. The weights were set to the proportion
296 of global surface area in each latitudinal bin, i.e. decreasing with increasing latitude as:

$$297 \quad \text{weights} = \sin(\alpha_{1,i}) - \sin(\alpha_{2,i}), \quad (11)$$

298 where α_1 is the upper, and α_2 is the lower latitudinal boundary of bin i , i.e. we approximated the shape of
299 the globe as a spheroid.

300 **Results**

301 **Model validation**

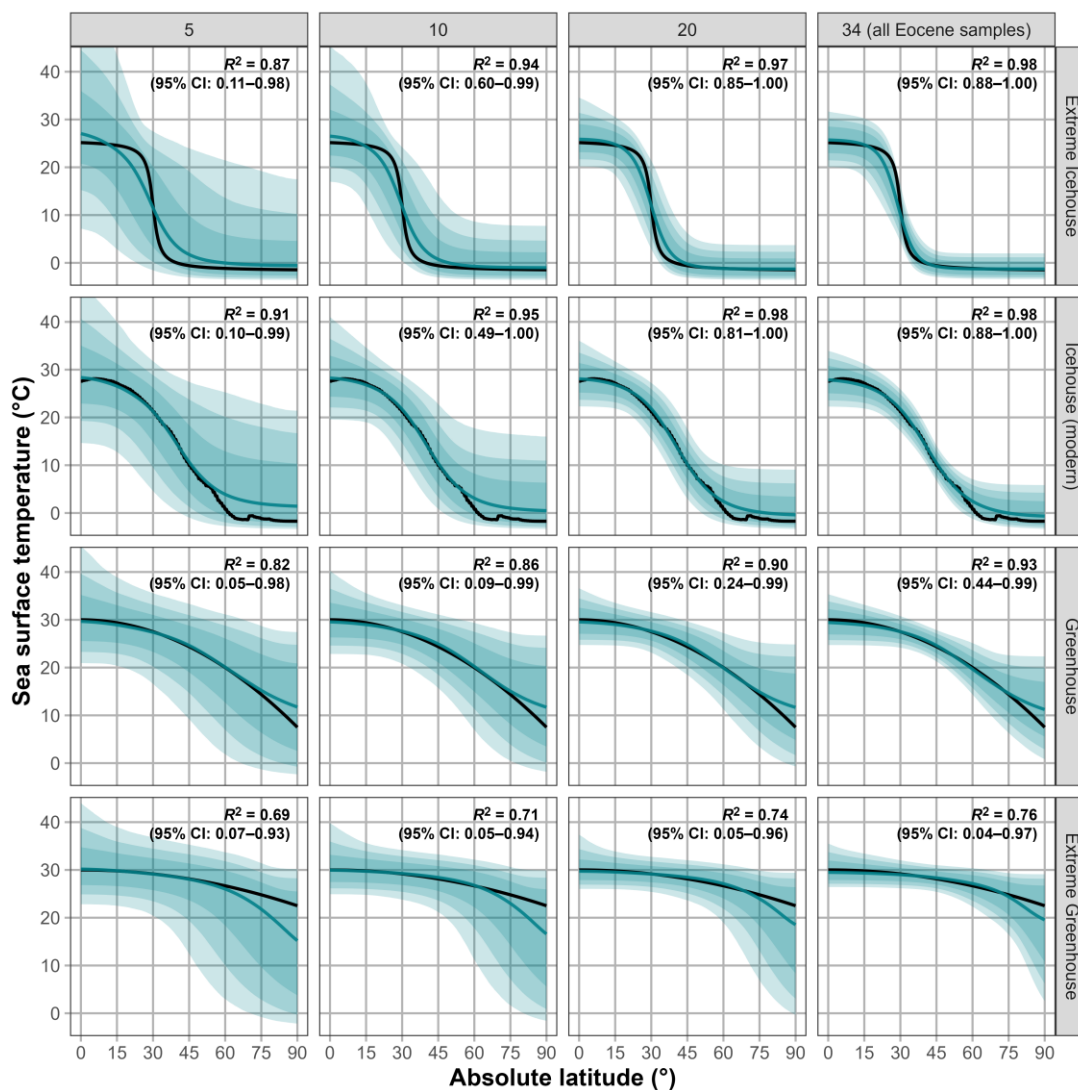


Figure 2: Model reconstructions of simulated latitudinal temperature gradients at various sample sizes. Each column depicts a different reconstruction for given sample sizes: 5, 10, 20 (randomly sampled latitudes), and 34 (latitudes of EECO samples). Each row depicts a different latitudinal temperature gradient that represents idealised or observed climatic states: idealised extreme icehouse, greenhouse, and extreme greenhouse gradients, and the modern gradient, which represents an icehouse state. The black line illustrates the original gradient. The blue line depicts the reconstructed gradient represented by the median sea surface temperature value estimated from 1,000 model runs with different random samples. To generate the random samples, different random noise from a normal distribution with a standard deviation of 3.8°C was added to each temperature. The blue shadings depict the 90%, 95%, and 99% credible intervals. Bold black text within each panel depicts the coefficient of determination (R^2) for estimating goodness of fit between the simulated and modelled gradient. The median (50%)

R^2 value along with the 95% credible intervals from all model runs are shown. Each gradient is depicted in absolute latitude.

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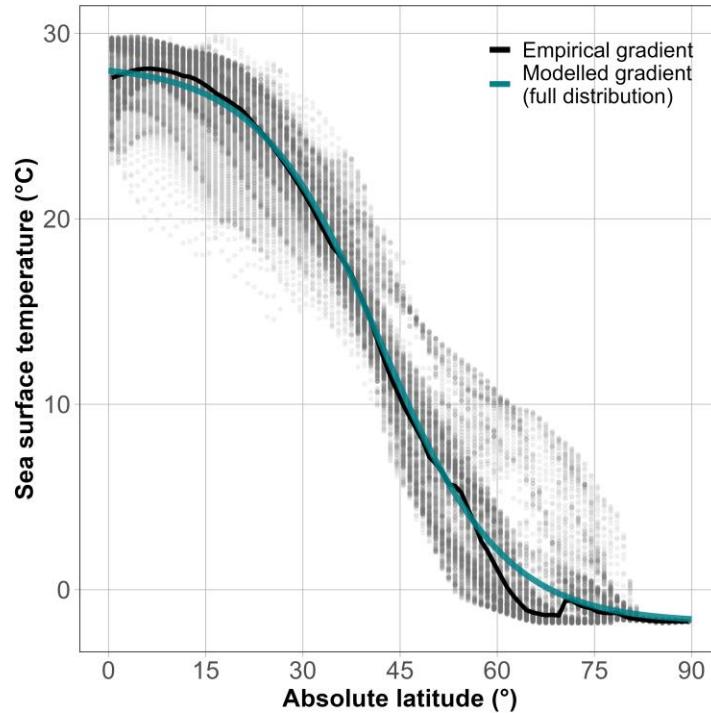


Figure 3: Present-day latitudinal temperature gradient. The present-day empirical latitudinal temperature gradient (median sea surface temperature) is depicted as a black line, and the gradient estimated by the Bayesian model is shown in turquoise ($R^2 = 0.97, N = 42,896$). Grey points depict the individual cell values of the Bio-ORACLE grid of mean sea surface temperatures, which were used to infer the empirical and the modelled gradient. Higher opacity of points indicates higher density of data (multiple overlapping points).

303 Our Bayesian model is able to model a range of idealised temperature gradients, ranging from extreme
304 icehouse to ‘super greenhouse’ scenarios (Fig. 2). Random latitudinal sampling results in accurate
305 reconstructions for most random samples at sample sizes of 10 and 20 for the icehouse scenarios (median
306 of $R^2 > 0.9$). Greenhouse scenarios perform somewhat worse due to the increased uncertainty at high
307 latitudes (median of $R^2 > 0.7$ at sample sizes 10 and 20). A sampling distribution resembling that of the
308 early Eocene dataset used in this study allows for accurate reconstruction of all scenarios, although the R^2
309 is still relatively low in the extreme greenhouse scenario, as a perfectly flat gradient, predicted by the model,
310 would result in an R^2 of 0, despite the original gradient being very flat. This also explains the low lower
311 bounds of the 95% credible intervals in the greenhouse scenarios.

312 The average, modern temperature gradient can be closely approximated with our model when using the full
313 modern SST dataset (Fig. 3); almost all of the variation in the empirical median temperatures in bins of 1°
314 absolute latitude (black line) is explained by the modelled gradient (99.7%). The empirical gradient spans
315 29.3°C from the equator to the poles, the modelled gradient is only slightly higher at 29.6°C. The modern,
316 global mean temperature (GMST) based on our modelled, median gradient is 17.6°C, which is nearly equal
317 to the GMST derived from the empirical median gradient (17.5°C).

318 **EECO reconstruction**

319 The Eocene temperature gradient reconstructed with our Bayesian model is starkly different from the
320 modern (Fig. 4). Modelled, median equatorial temperatures are 2.2°C (95% CI: -0.8–8.5°C) higher for the
321 EECO, and polar temperatures are 18.9°C (5.3–28.9°C) higher. This results in a flattened latitudinal
322 temperature gradient of 13.3°C (3.9–25.2°C) for the EECO, as opposed to 29.6°C for the modern. To
323 facilitate the comparison with latitudinal gradients reported in the literature, which sometimes do not report
324 temperatures at very high latitudes, we report also the EECO gradient between the equator and the modern-
325 day polar circle (66.6° latitude), which is markedly lower at 5.8°C (0.5–12.8°C).

326 The high variability of EECO palaeotemperature proxies, particularly in the mid-latitudes, and the scarcity
327 of high-latitude data, result in substantial uncertainties in the modelled temperature gradient. This is
328 reflected in the residual standard deviation (σ) of the EECO gradient—4.9°C (3.9–6.5°C)—which is more
329 than double the σ for the modern gradient, 2.2°C. This is illustrated by the drastic departure of some of the
330 proxy data from the gradient estimates (Fig. 4).

331 The early Eocene GMST is estimated at 28.3°C (26.3–30.3°C), 10.7°C higher than the modern. A model
332 run excluding the ecological proxies increases the GMST by 1.7°C (-1.8– 5.0°C). The median modelled
333 temperature is higher near the equator and in high latitudes when excluding the ecological proxies, with a
334 flattened median gradient of 10.9°C (Fig. S2). In contrast, including ecological proxies, but widening the
335 uncertainty around the low-latitude ecological proxy data does not significantly change the resulting
336 gradient (Fig. S3).

337 Due to the limited spatial coverage of the early Eocene proxy record, and due to the added model complexity
338 of simultaneously estimating a model across both hemispheres, we pooled the proxy data across both
339 hemispheres. Applying the model separately within each hemisphere results in substantial differences in
340 hemispherical, average temperatures, with the Southern Hemisphere being warmer by 6.1°C (2.9–9.2°C).
341 The inferred latitudinal gradient is somewhat steeper in the Northern Hemisphere (steeper by 1.8°C,
342 although the 95% CI of that difference spans -18.0–14.5°C), but the large uncertainties associated with both

343 gradients, and the lack of polar proxy data in the Southern Hemisphere preclude a more precise statement
344 (see Fig. S4).

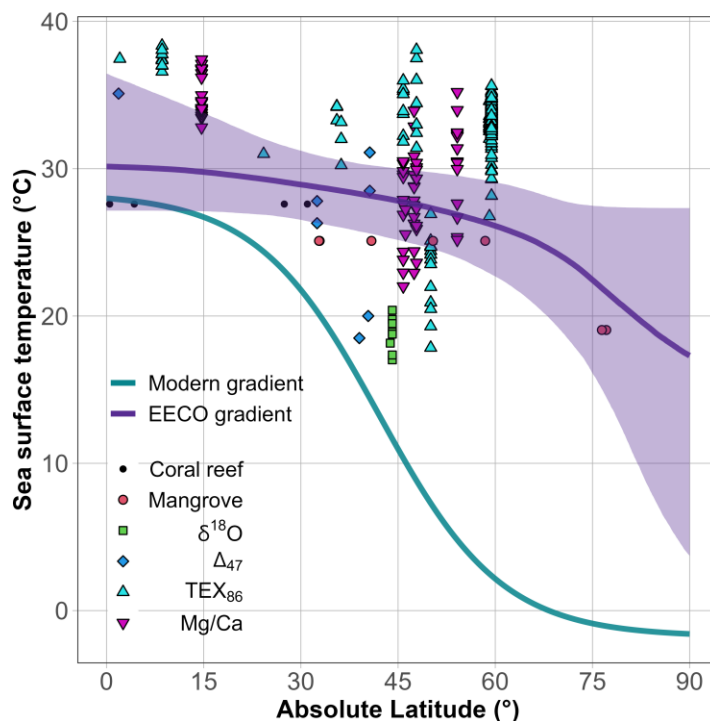


Figure 4: Estimates of the median, latitudinal sea surface temperature gradients of the early Eocene climatic optimum (purple line) and of the present-day (turquoise), both estimated with the Bayesian model. The purple ribbon (shading) depicts the 95% credible interval of the Eocene gradient, the uncertainty of the modern gradient is too low to be visible. Points within the plot depict the geochemical (e.g. TEX_{86}) and the ecological (e.g. mangroves) data. Geochemical data are plotted by their point estimate temperature value. Ecological data are plotted at the mean temperature values of their respective normal distributions.

345 Discussion

346 Improved estimation of latitudinal and global palaeotemperatures

347 Our results show that our Bayesian model can be used to reconstruct different types of latitudinal SST
348 gradients from proxy data with moderate sample sizes ($n = 10\text{--}34$) and patchy sampling distributions
349 (Fig. 2). This is an advancement over previously used linear, quadratic, or Gaussian approximations
350 (e.g. Bijl et al., 2009; Tierney et al., 2017), which can fit only specific types of gradients. As such, our
351 model presents an alternative to non-parametric methods for inferring latitudinal temperature gradients,
352 which are sometimes favoured as they can flexibly follow the shape of an unknown temperature gradient
353 (e.g. Zhang et al., 2019; Jones and Eichenseer, 2022). However, when used for interpolation or prediction

354 outside the proxy range, non-parametric methods such as Gaussian process regression strictly respond to
355 the data (e.g. Inglis et al., 2020). This means that the idiosyncrasies of a patchy proxy record, potentially
356 afflicted with measurement errors, calibration errors, and palaeogeographic and temporal uncertainty (e.g.
357 Buffan et al., 2023), dictate the reconstruction of large-scale climatic patterns, without the option of
358 including additional knowledge (e.g. that latitudinal temperature gradients should be broadly negative).

359 In contrast, our Bayesian parametric model allows for the inclusion of informative priors on the model
360 parameters. The modelled sea surface temperature gradient thus does not strictly follow the proxy data, but
361 instead represents a compromise between the data and prior knowledge. In the EECO example (Fig. 4), the
362 inclusion of informative priors improves the prediction of sea surface temperatures in the unsampled, very
363 high latitudes: Notice that the upper limit of the credible interval does not increase beyond the range of the
364 data, whereas unconstrained approaches such as splines, Gaussian processes or even standard linear
365 regression could lead to unrealistically high upper bounds in this case (see Rasmussen and Williams, 2004).
366 Prior information on the shape of latitudinal temperature gradients on Earth exists for all geological time
367 periods. For example, the greater amount of solar radiation per unit area in low latitudes causes Earth's
368 latitudinal temperature gradient to be broadly negative (Beer et al., 2008). The ease with which such prior
369 information can be integrated is a major advantage of our method, as the shape of the modelled gradient is
370 controlled by four parameters which clearly relate to its magnitude, steepness, and the latitude of its greatest
371 steepness.

372 Palaeoclimate reconstructions are often summarised as global mean surface temperatures (GMST),
373 providing a standardised metric for characterising the state of the Earth's climate (Royer et al., 2004; Inglis
374 et al., 2020). The calculation of global mean surface temperatures directly from sparse proxy data is
375 susceptible to bias (Jones and Eichenseer, 2022). By modelling the temperature variation across latitudes,
376 a complete temperature distribution along a latitudinal axis can be obtained, filling in gaps in the proxy
377 record through inter- or extrapolation. This eliminates the common problem that specific climatic zones
378 dominate the proxy record. Reconstructing the GMST directly from the proxies would lead to an estimate
379 biased towards the well-sampled latitudes. Calculating zonal averages alleviates this problem, but this
380 method relies on comprehensive latitudinal coverage (Inglis et al., 2020). Instead, our method allows for
381 intersecting the modelled temperature gradient at narrow latitudinal intervals, even when significant
382 latitudinal gaps exist. Weighting the temperatures of those latitudinal intervals by area results in GMST
383 estimates without intrinsic spatial biases. We anticipate that this improved method may significantly alter
384 Phanerozoic, proxy-based temperature curves, which have often been directly calculated from the proxy
385 record (Royer et al., 2004; Veizer and Prokoph, 2015). This is particularly relevant for the early Mesozoic

386 and older intervals, for which the spatial coverage is generally poor due to the absence of data from ocean
387 drilling sites (Jones and Eichenseer, 2022).

388 **The role of ecological constraints in palaeoclimatic reconstructions**

389 Our results further exemplify how incorporating quantified ecological temperature constraints can provide
390 more precise temperature reconstructions than geochemical proxies alone, adding to the advances in
391 palaeoclimatic reconstructions achieved by integrating lithological data (Scotese et al., 2021; Burgener et
392 al., 2023). Combining the occurrences of climate-sensitive plant communities (Greenwood and Wing,
393 1995), reptiles (Markwick, 2007), and leaf shapes (Peppe et al., 2011), with geochemical proxies offers
394 substantial potential for improving quantitative palaeoclimatic reconstructions across the Phanerozoic. Our
395 modelling framework offers a straightforward, efficient way of integrating ecological palaeoclimatic data
396 with other proxy data: The hierarchical model structure accounts for variation of temperature estimates
397 from proxies at individual localities, which is treated equivalent to the uncertainty associated with the
398 ecological temperature proxies. A local temperature estimate, based on multiple geochemical proxies, thus
399 has the same weight as a local temperature estimate obtained from the occurrence of a climate-sensitive
400 plant community, whilst preserving the uncertainty associated with each estimate. The model could easily
401 be extended to include uncertainties on individual geochemical proxy data (see Fig. S5), or to variably
402 weight proxy records classified as more or less reliable.

403 Our approach for deriving fully quantitative climate reconstructions from ecological data is borrowed from
404 nearest living relative methods, commonly employed in terrestrial, Cenozoic palaeoclimatic reconstructions
405 (Fauquette et al., 2007; Pross et al., 2012). One major limitation to these methods is that the thermal
406 preferences of taxa may have changed over time. More significantly, in the early Eocene, sea surface
407 temperatures may have reached heights unknown in the modern world, and nearest living relative methods
408 based on the modern are inherently unable to predict such elevated temperatures. This is especially true for
409 taxa that inhabit the warmest part of the ocean today, e.g. coral reefs (Kleypas et al., 1999). Although coral
410 reefs are threatened by warming sea surface temperatures today (Hoegh-Guldberg, 2011), it is conceivable
411 that Eocene reef corals were adapted to a warmer climate. The fossil record indicates that reef development
412 may have been stunted in the early Eocene, with few early Eocene coral reefs occurring in low latitudes
413 (Zamagni et al., 2012). The absence of coral reefs in higher latitudes in the early Eocene could be due to
414 requirements in irradiance, rather than temperature (Muir et al., 2015). Tropical temperatures predicted by
415 the geochemical proxy record indicate hotter-than-modern tropical temperatures for the early Eocene
416 (Fig. S2), suggesting that the modern climatic range of coral reefs may underestimate the early Eocene
417 thermal limits for coral reefs. We have tried to account for that possibility by widening the temperature

418 probability distribution for coral reefs, but the predicted temperatures for the reef and mangrove sites still
419 lie below the temperatures indicated by the geochemical proxy record (Fig. 4, Fig. S2).

420 **Early Eocene climate**

421 The geochemical proxy record and ecological data indicate that the latitudinal SST gradient of the early
422 Eocene climatic optimum was significantly shallower than the modern (Huber and Caballero, 2011), but
423 beyond that, there is little agreement. Earlier, reconstructed early Eocene and EECO SST gradients range
424 from 7–21°C (Table 1); a more recent reconstruction that includes terrestrial air and sea surface
425 temperatures arrives at a gradient of ~13°C (Inglis et al., 2020). Our median poles-to-equator gradient
426 estimate is similar at 13.3°C, but notably shallower when taking the equator-to-polar-circle estimate, 5.8°C,
427 as the geochemical proxy data suggest high temperatures up to latitudes of ~ 60°. Both geochemical and
428 ecological shallow water data indicate that inferred SST gradients based on tropical, shallow water and
429 deep water samples (Cramwinckel et al., 2018; Evans et al., 2018) may overestimate the SST gradient of
430 the early Eocene greenhouse world. Likewise, palaeoclimatic simulations from General Circulation Models
431 tend to estimate steeper gradients than most proxy records (Table 1; Pross et al., 2012; Lunt et al., 2021)

432 The very high variability of the proxy record in mid-latitudes results in large uncertainties on the shape of
433 temperature gradient and on the GMST. Some of this variability may stem from spatial variability in SSTs,
434 as can be observed in the modern (Fig. 3), e.g. due to ocean circulation (Rahmstorf, 2002). Biases and errors
435 in the proxy reconstructions also likely contribute to the observed variability, as geochemical proxies reflect
436 many other factors besides seawater temperature (Hollis et al., 2019). Despite excluding $\delta^{18}\text{O}$ measurements
437 from recrystallised fossils, systematic offsets remain between mostly warm temperatures derived from
438 TEX_{86} , and cooler temperatures derived from $\delta^{18}\text{O}$, Δ_{47} , and the ecological proxies.

439 Temporal changes within the EECO (Westerhold et al., 2018), and seasonality (Keating-Bitonti et al., 2011;
440 Ivany and Judd, 2022) may also contribute to the large variability of the EECO proxy data. Based on the
441 occurrence of heterotrophic carbonates, Davies et al. (2019) suggested that mid- and high-latitude
442 geochemical proxy data from the EECO may be biased towards summer temperatures. Some of the
443 geochemical mid-latitude geochemical proxy data from Hollis et al. (2019) may therefore suggest higher
444 than actual mean annual temperatures, and the variability of temperature estimates from individual localities
445 is higher in mid - high latitudes (Fig. S6). It is difficult to attribute this variability to seasonality alone, as
446 temporal climate variability is also expected to be higher in mid and high latitudes (Schwartz, 2008).
447 Critically, however, the mangrove data strongly supports our inference of a flattened gradient independent
448 of the geochemical proxy record.

449 Recent, marine GMST estimates of the EECO and of the early Eocene range from 23.4–37.1°C, with the
450 lowest GMSTs being derived from $\delta^{18}\text{O}$, and the higher estimates including TEX_{86} (Inglis et al., 2020).
451 Many studies include both marine and terrestrial proxies to derive GMST estimates, but despite great
452 differences in proxy selection and in the calculation of global average temperatures, many recent estimates
453 fall in the range of 27 - 29.5°C (Hansen et al., 2013; Caballero and Huber, 2013; Cramwinckel et al., 2018;
454 Zhu et al., 2019), similar to our median GMST estimate of 28.3°C and well within the 95% credible interval
455 of our GMST estimate (26.3–30.3°C).

456 **Conclusions**

457 The Bayesian hierarchical model presented here is able to reconstruct latitudinal gradients from both
458 geochemical and ecological proxy data, while reflecting the uncertainty associated with the ecological
459 temperature proxies, and accounting for the variation of multiple temperature estimates at individual
460 localities. Using informative prior information allows for accurate temperature reconstructions from records
461 with geographically sparse sampling. By providing temperature estimates across the entire latitudinal range,
462 this method also facilitates the reconstruction of unbiased global average temperatures. Application of our
463 model to the EECO suggests that latitudinal sea surface temperature gradients were shallower than
464 estimated by most previous proxy-based studies. High-latitude pollen records support this interpretation.
465 Our GMST estimate is in good agreement with most existing estimates, indicating that broadly accurate
466 GMST reconstructions are possible even with substantial deviations in the shape of the latitudinal
467 temperature gradient. Our new method opens the door for improving the accuracy of proxy-based
468 palaeoclimatic reconstructions and Phanerozoic temperature curves, particularly in intervals with a patchy
469 and unevenly sampled record. Finally, the flexibility of our approach means that estimates can be efficiently
470 updated when new data, or constraints, are made available.

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478 **Author contributions**

479 Both authors designed the study and carried out data preparation. K.E. programmed the model and
480 conducted the analyses. L.A.J. and K.E. generated the figures. Both authors contributed to the writing of
481 the manuscript.

482 **Competing Interests**

483 The authors declare that they have no conflicts of interest.

484 **Data accessibility**

485 The data and code used to produce the results of this study are available via GitHub
486 (<https://github.com/KEichenseer/PalaeoClimateGradient>) and the linked Zenodo repository
487 (<https://zenodo.org/record/8402530>).

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