



## Leveraging gauge networks and strategic discharge measurements to aid development of continuous streamflow records

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**Abstract.** Streamflow, or discharge, is an essential measure in the study of rivers and streams. However, quantifying  
25 continuous discharge can be difficult, especially for nascent monitoring efforts, due to the challenges of establishing gauging  
locations, sensor protocols, and installations. Here, we investigate the potential for both simple and complex models to  
accurately estimate continuous discharge (at least daily estimates), using only discrete manual measurements of streamflow.  
We were inspired to do this work because some continuous discharge series generated by the National Ecological Observatory  
Network (NEON) during its pre- and early-operational phases (2015-present) are marked by anomalous data due to sensor  
30 drift, gauge movement, and incomplete rating curves. Using field-measured discharge as truth, we reconstructed continuous  
discharge for all 27 NEON stream gauges over this period via linear regression on nearby donor gauges and/or prediction from  
neural networks trained on a large corpus of established gauge data. Reconstructions achieved median efficiencies of 0.83  
(Nash-Sutcliffe, or NSE) and 0.81 (Kling-Gupta, or KGE) across all sites, and improved KGE at 11 sites versus published  
data. Estimates from this analysis inform ~199 site-months of missing data in the official record, and can be used jointly with  
35 NEON data to enhance the descriptive and predictive value of NEON's stream data products. We provide 5-minute composite  
discharge series for each site that combine the best estimates across modeling approaches and NEON's published data.

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## 1 Introduction

55 Discharge, or streamflow, is a fundamental measure in hydrology, biogeochemistry, and river science more broadly. A measure of water volume over time, discharge is used to infer theoretical watershed runoff (depth of water “blanketing” the land surface, or depth over time), which in turn is integral to understanding watershed processes such as chemical weathering (White & Blum 1995). Accurate, and at least daily, discharge estimates are essential components of nearly any quantitative study of physical or chemical watershed or river processes at the ecosystem scale. Determination of solute fluxes (Bukaveckas et al. 60 1998), gas exchange rates (Hall, 2016), ecosystem metabolism (Odum 1956), and sediment transport (Graf 1984) all require well constrained estimates of discharge.

Despite its centrality to so many fields of study, discharge is a notoriously difficult metric to capture on a regular basis, especially in free-flowing systems, as it may vary greatly with annual cycles and weather events (Turnipseed & Sauer 2010). Established institutions like the USGS (USA), ECCC (Canada), and ANA (Brazil) have honed their instrumentation, methods, 65 and monitoring locations over decades to generate reasonable discharge estimates even under extreme conditions (Benson & Dalrymple 1967; Costa 2004); however, nascent and/or small-budget monitoring efforts face several challenges. Critically, hundreds of these efforts are constantly occurring within academic research groups, municipalities, counties, and other entities building smaller gauge networks, with much less expertise, support, and budget than gauging programs supported by dedicated national programs.

70 Not including purely model-based methods for discharge prediction (Manning 1891; Hsu et al. 1995, Durand et al. 2022), automated discharge estimation requires the careful construction of an empirical “rating curve,” by which discharge can be continuously inferred from water level, or “stage” (but see Shen 1981). To build such a relationship, technicians must sample discharge and stage at points covering the range of observable flow, ideally including flood stage. In dynamic systems, this rating curve must be regularly updated. Point estimates of discharge can be collected using Acoustic Doppler current profiling 75 (Moore et al. 2017), manual flow meter profiling, or light-based methods (Wang 1988) to determine average cross-sectional velocity, or via conservative tracer injections (Tazioli 2011). In many streams, two or more of these methods must be employed, depending on conditions (Turnipseed & Sauer 2010). During 10-year or 100-year floods, no method may be viable or safe. Even under regular storm conditions, a technician may be unable to mount a sampling effort quickly enough to capture peak flow, or may produce an inaccurate measurement. As a result, rating curves may remain in a state of insufficiency for years, 80 during which time high discharge estimates are unreliable, especially where they are made by extrapolating beyond observed maximum flow.

Gauge placement presents another obstacle to the rapid deployment of discharge monitoring stations (Isaacson & Coonrod 2011). Stage measured via pressure transduction is susceptible to bias and nonlinearity under turbulent flow conditions (Horner et al. 2018). Sensors placed in a depositional area may be buried by sediment, and installations in forested watersheds or debris



85 flow regions may be destroyed during floods. Often, equipment must be relocated at least once before a new gauge site can be properly established. Even an established stage-discharge rating curve must be regularly updated and maintained because the bed of the river can change as sediment is deposited or excavated, altering the relationship between stage and flow.

For some studies aiming to quantify stream or watershed processes that require continuous discharge time series, establishment of a high-quality monitoring station may be infeasible. Where co-location with an existing stream gauge is also not possible, 90 record extension (Hirsch 1982; Nalley et al. 2020) and gap-filling (Harvey et al. 2012; Arriagada et al. 2021) techniques cannot be employed, as these rely on prior knowledge of the statistical properties of the discharge time series being augmented. In such scenarios, streamflow reconstruction or prediction techniques are suitable, as these may proceed a priori or from minimal observation. Reconstruction typically involves methods that leverage the correlation between a partially measured target site and nearby “donor” (predictor) gauges. Discharge may also be quantified in the absence of direct measurements at the target 95 location via statistical (Chokmani & Ouarda 2004), mechanistic (Regan et al. 2019), or machine learning (Kratzert et al. 2022) modeling techniques.

Here, we use both linear regression (OLS, L2/Ridge, segmented) and deep learning (LSTM-RNN) approaches to reconstruct discharge from the early operational phase (2015–2022) of the National Ecological Observatory Network (NEON), a time during which site location selection issues and rating curve development rendered potentially unreliable many site-months of 100 discharge estimates (Rhea et al. 2023a). Our goal was to achieve Kling-Gupta Efficiency (KGE) scores greater than those of the official NEON continuous discharge product at as many sites as possible. A secondary goal was to improve temporal coverage of the official record where it contains gaps. For researchers intending to use NEON continuous discharge data between 2015 and 2022, the results of this effort, as well as efforts by Rhea et al. (2023a), can ensure that data gaps and questionable periods in the official record are replaced by high-quality estimates wherever possible. We provide composite 105 discharge series, for all 27 NEON stream gauge locations, built from the best NEON-published estimates and the best estimates generated by this study (<https://doi.org/10.6084/m9.figshare.c.6488065>). Composite series can be visualized at [https://macrosheds.org/data/vlah\\_et\\_al\\_2023\\_composites/](https://macrosheds.org/data/vlah_et_al_2023_composites/).

The success of this effort demonstrates the viability of “virtual gauges.” (*sensu* Philip & McLaughlin 2018; not to be confused with the “virtual staff gauges” of Seibert et al. 2019). In this study, we use the term to describe sites at which discrete discharge 110 is measured at least 35 times across a wide range of flows, and can be used to fit or evaluate models that generate continuous flow. Methods like those presented could be used to reduce the cost and simplify the process of establishing streamflow monitoring sites, especially in river networks that are already partially gauged.

## 2 Methods

### 2.1 Data selection, acquisition, and processing

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We used the “neonUtilities” package (Lunch et al. 2022) in R to retrieve NEON discharge data. Officially released and provisional field measurements (NEON 2023b; accessed 2023-01-23) were used to fit linear regression models and evaluate all models, as these data were collected directly by NEON technicians, using a combination of state-of-the-art methods including acoustic Doppler current profiling (ADCP; Moore et al. 2017), conservative salt tracer releases (Tazioli 2011), and  
120 flow meter measurements (Pantelakis et al. 2022). We used quality-controlled “finalQ” values where available, or “totalQ” values (taken directly from the flowmeter) in their absence. We refer to NEON’s discharge field measurements hereafter as e.g. “the response variable”, or “response discharge time series,” in the context of linear regression, or as the “target” variable in the context of machine learning. In either context, we refer to the 27 NEON sites for which discharge predictions were generated as “target sites” or “target gauges” (Table 1).

125 Continuous discharge data (NEON 2023a; 2023 release accessed 2023-05-01) were also retrieved via neonUtilities. These were used to finetune a subset of site-specific neural network models, and to construct composite discharge series. Evaluation results used to distinguish likely reliable vs. potentially unreliable subsets of NEON’s continuous discharge time series, per site-month, were provided by Rhea et al. (2023a) and accessed through HydroShare (Rhea 2023). Continuous elevation of  
130 surface water data are available, but approximately one third of all site-months are marked by disagreement between reported surface elevation and measured stage, or by likely sensor drift (Rhea et al. 2023a). We therefore chose not to use surface elevation to inform our models, though it no doubt contains predictive value.

Donor gauge data for linear regression analysis were acquired primarily from the US Geological Survey’s National Water  
135 Information System (NWIS), using the “dataRetrieval” package (DeCicco et al. 2022) in R. Additional donor gauge data from Niwot Ridge LTER and Andrews Forest LTER were retrieved from the MacroSheds dataset (Vlah et al. 2023) via package “macrosheds” (Rhea et al. 2023b), and from the EDI data portal (Johnson et al. 2020), respectively.

We used the original CAMELS dataset (Newman et al. 2014; Addor et al. 2017), the USGS National Hydrologic Model with  
140 Precipitation-Runoff Modeling System (NHM-PRMS; hereafter NHM; Regan et al. 2019), and the MacroSheds dataset as training data for neural network simulations of discharge data at each target site. CAMELS watershed attributes were generated for MacroSheds and NHM sites using the code provided at <https://github.com/naddor/camels>, except where otherwise indicated in Table 2, and daily Daymet meteorological forcings (Thornton et al. 2022; *sensu* Newman et al. 2015) were retrieved via Google Earth Engine (Gorelick et al. 2017). All code for this project can be found on GitHub, at  
145 [https://github.com/vlahm/neon\\_q\\_sim](https://github.com/vlahm/neon_q_sim), or in the Zenodo archive at <https://doi.org/10.5281/zenodo.7976251>.

## 2.2 Target sites

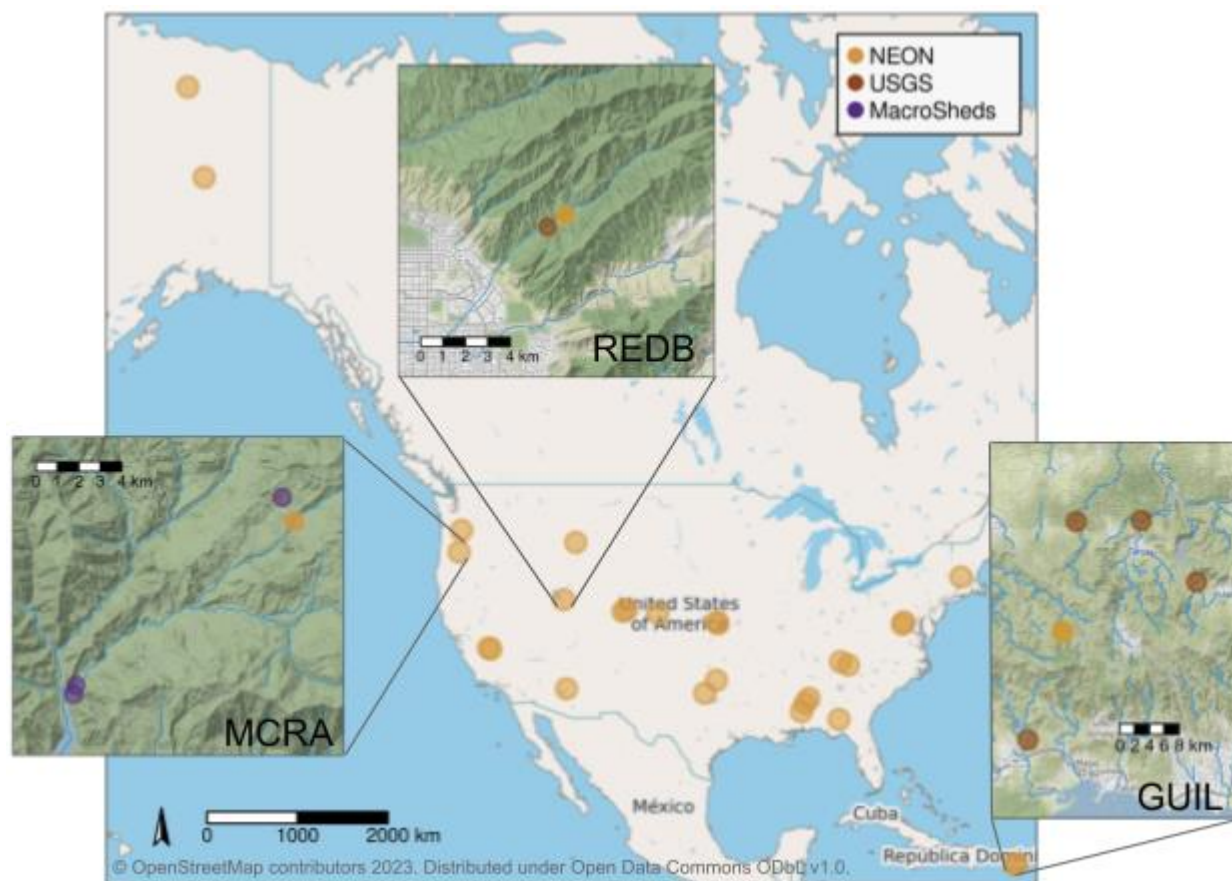


Figure 1. Map of target sites (NEON) and donor gauge candidates for three target sites: MCRA = McRae Creek, state of Oregon; REDB = Red Butte Creek, state of Utah; GUIL = Rio Guilarte, Puerto Rico.

All 27 lotic (flowing) aquatic sites associated with NEON were included as target sites for discharge prediction in this study (Figure 1). Sites TOMB, BLWA, and FLNT are installed on major rivers, downstream of hydropower dams. All other sites have been free of dam influence since 2012 at the latest, and are designated “wadeable streams” by NEON. In addition to the three sites above, hydrology at BLUE, GUIL, KING, MCDI, and ARIK may be influenced by agricultural activity, especially in the relatively arid Midwest (i.e. states KS, CO, OK). Continuous discharge data for TOMB are provided by a nearby gauge of the U.S. Geological Survey’s National Water Information System, and are given at hourly intervals, rather than NEON’s customary 1-minute intervals.

Table 1. Target sites for discharge prediction. See <https://www.neonscience.org/field-sites> for more information.

Site code	Full name	State (USA)	Watershed area (km <sup>2</sup> )	Mean watershed elevation (m)



TOMB	Lower Tombigbee River	AL	47085.3	20
BLWA	Black Warrior River	AL	16159.4	22
FLNT	Flint River	GA	14999.4	30
ARIK	Arikaree River	CO	2631.8	1179
BLUE	Blue River	OK	322.2	289
SYCA	Sycamore Creek	AZ	280.3	645
OKSR	Oksrukuyik Creek	AK	57.8	766
PRIN	Pringle Creek	TX	48.9	253
BLDE	Blacktail Deer Creek	WY	37.8	2053
CARI	Caribou Creek	AK	31.0	225
MCDI	McDiffett Creek	KS	22.6	396
REDB	Red Butte Creek	UT	16.7	1694
MAYF	Mayfield Creek	AL	14.4	77
KING	Kings Creek	KS	13.0	324
HOPB	Lower Hop Brook	MA	11.9	203
LEWI	Lewis Run	VA	11.9	152
BIGC	Upper Big Creek	CA	10.9	1197



GUIL	Rio Guilarte	PR	9.6	551
LECO	LeConte Creek	TN	9.1	579
MART	Martha Creek	WA	6.3	337
WLOU	West St Louis Creek	CO	4.9	2908
CUPE	Rio Cupeyes	PR	4.3	157
MCRA	McRae Creek	OR	3.9	876
COMO	Como Creek	CO	3.6	3021
TECR	Teakettle Creek - Watershed 2	CA	3.0	2011
POSE	Posey Creek	VA	2.0	276
WALK	Walker Branch	TN	1.1	264

### 2.3 Linear regression and model selection

Candidate donor gauges were identified by visually examining an interactive map of NEON gauges, USGS gauges, and  
 165 MacroSheds gauges ([https://macrosheds.org/ms\\_usgs\\_etc\\_reference\\_map/megamap.html](https://macrosheds.org/ms_usgs_etc_reference_map/megamap.html)), generated with package  
 “mapview” (Appelhans et al. 2022) in R. We also used the National Water Dashboard of the USGS  
 (<https://dashboard.waterdata.usgs.gov/app/nwd/en/?aoi=default>) to identify active gauges in Alaska, USA. For each target site,  
 up to four donor gauge candidates were selected on the basis of spatial proximity and geographic similarity to the target site  
 (Figure 1). Generally, no greater than this number of gauges were even remotely reasonable candidates (e.g. within 50 km of  
 170 the target site; not in an urban area; not downstream of a reservoir), but for one target site (MCRA) we had ten nearby candidate  
 gauges to select from—all associated with the Andrews Experimental Forest in western Oregon State, USA. In this case we  
 chose three candidate sites representing a catchment upstream of the target site (GSWS08), downstream of the target site on  
 the MCRA mainstem (GSLOOK), and downstream on a tributary of MCRA (GSWS01). All donor and response discharge  
 time series were neglog transformed (Equation 1; Whittaker et al. 2005) before fitting linear regression models.





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**Equation 1:**  $x_{neglog} = \mathit{sign}(x)\log(|x| + 1)$

Series were scaled by 1000 before transformation, in order to reduce the disproportionate impact of adding one to every value. Response observations were synchronized to the interval of the predictor series by approximate datetime join, allowing forward or backward time-shifts of up to 12 hours if necessary.

One of three forms of linear regression was employed at each site, depending on the number and location of donor gauges, and the donor-target gauge relationships. For sites with a single donor gauge (REDB, HOPB, BLUE, SYCA, LECO), considered predictors were: discharge from the donor gauge, a 4-season categorical variable, and their interaction. Additionally, an intercept parameter could be estimated, or not, for each specification. Thus, up to six models were fit using Ordinary Least Squares (OLS) regression (Galton 1886), ensuring at least 15 observations per model parameter. At LECO, an additional dummy variable was included to address an intercept change due to a wildfire in November of 2016. The best model was selected via 10-fold cross-validation, minimizing mean squared error (MSE). MSE, being a squared-error term, disproportionately penalizes inaccurate prediction of high discharge values, and helps to balance against the relative rarity of high discharge measurements in the field data. At site SYCA, the log-log relationship between discharge at the target gauge and a single donor gauge exhibited a distinct breakpoint, and segmented least-squares regression was used (R package “segmented”; Muggeo 2008). At all other sites (19 in total), predictors included discharge series from 2–4 donor gauges, season, and all interactions. To control overfitting and shrink covarying coefficients toward zero, we used L2 regularization (Ridge regression; Gruber 2017) via R package “glmnet” (Friedman et al. 2010). As with the other regression approaches, 10-fold cross-validation and MSE loss were used for model parameter selection—in this case for the value of the penalty hyperparameter  $\lambda$ , which was set to the mean across folds of  $\lambda$  producing minimum cross-validated error. Unlike OLS and segmented regression, Ridge regression uses biased estimators that complicate calculation of prediction intervals. We generated 95% prediction intervals for glmnet discharge estimates using the 95th percentiles of 1000 bootstrap predictions at each prediction point, generated from 1000 resamples of the fitting data, stratified by season. We emphasize that these prediction intervals should be conservative estimates of the true uncertainty, as they do not fully account for uncertainty due to bias (Goeman et al. 2012).

For each site, we fit two sets of models as described above, one with discharge scaled by watershed area (i.e. “specific discharge” in the surface water hydrology sense) prior to transformation, and one without areal scaling. Only one model from each set was ultimately selected for each target site, on the basis of Kling-Gupta efficiency (KGE; Gupta et al. 2009), a composite model efficiency metric that incorporates measures of correlation, variance, and bias. We also report percent bias and Nash-Sutcliffe efficiency (NSE; Nash & Sutcliffe 1970), a measure of predictive accuracy that implicitly compares predictions to a mean-only reference model.



210 Predictions were generated for all time points during which data were available at the selected donor gauges. At target site  
COMO, a secondary model omitting one donor gauge was able to produce 36% more predictions than the selected model, so  
our predicted discharge at COMO is a composite of both models, preferring the better model's predictions where available.  
We were unable to locate sub-daily donor gauge data near COMO, so regression predictions for this site are at a daily interval.  
Regression predictions for all other sites were generated at sub-daily intervals matching the coarsest interval across predictor  
215 gauges—generally 15 minutes, though note that in most cases these predictions were interpolated to five minutes for our  
composite discharge product.

## 2.4 Neural network setup and operation

220 Supplementing the linear regression methods described above, we simulated discharge data at all 27 target sites using long  
short-term memory recurrent neural networks (LSTM-RNN; hereafter “LSTM”; Hochreiter & Schmidhuber 1997). Four  
LSTM strategies were employed, all of which involved training on a large and diverse corpus of stream discharge data (Table  
3). Two of these strategies included further finetuning to the time-series dynamics of each target site in turn. Due to the relative  
scarcity of field-measured discharge observations (between 39 and 213 per site; mean 122), none were used in LSTM training.  
225 Instead, these measurements were used only to evaluate predictions. LSTMs trained in this study are intended only for  
discharge prediction within the temporal and spatial bounds of NEON's early operational phase, not for forecasting or  
application to other sites. Therefore, all available, daily training data were used as such; no validation set was kept for  
hyperparameter tuning, and no holdout set of daily estimates was kept for evaluation (note that split-sample designs may be  
undesirable more generally: Arsenault et al. 2018; Guo et al 2018; Shen et al. 2022).

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After a hyperparameter search routine, described below, potentially skilled models were identified as those achieving at least  
0.5 KGE and 0.4 NSE. The best performing, potentially skilled LSTM for each site (if applicable) was then re-trained 30 times,  
forming an ensemble. Ensembles were trained for 18 of 27 sites. LSTM predictions included in our composite discharge  
product are means taken across the distributions of ensemble point predictions. Uncertainty bounds were computed as the 2.5  
235 and 97.5% quantiles of these distributions. LSTM skill was evaluated on the basis of mean ensemble efficiency (KGE) with  
respect to field-measured discharge (Table A1).

Daily discharge time series (training data) and field-measured discharge were scaled by watershed area. For each predicted  
day, LSTMs received 5 dynamic Daymet meteorological forcing variables and 11 static watershed attribute summary statistics  
240 (Table 2). Multitask learning (Caruana 1998; Sadler et al. 2022) was found to improve discharge prediction broadly in a  
preliminary analysis, so Daymet minimum air temperature was used as a secondary target variable. Kratzert et al. (2019a)  
found that a maximum of about 150 preceding days were able to influence LSTM output on a similar prediction problem, so



we set the input sequence length to 200 days to ensure full utilization of available information. In other words, for each day of prediction, the model was able to leverage information from the preceding 200 days.

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We employed four different training pipelines described in Table 3. Of the 671 CAMELS watersheds (i.e. basins), we used a subset of 531 with undisputed areas less than 2000 km<sup>2</sup> (Newman et al. 2017). For finetuning data, we used version 1 of the MacroSheds dataset (Vlah et al. 2023). We excluded MacroSheds sites outside North America, or with coastal or urban hydrological influence, for a total of 133 sites out of the 169 that are currently available. We chose MacroSheds sites for finetuning because the MacroSheds and NEON datasets focus primarily on small watersheds, often smaller than 10 km<sup>2</sup> in area, while only eight CAMELS watersheds are smaller than 10 km<sup>2</sup> and most are larger than 100 km<sup>2</sup> (Vlah et al. 2023). Daily mean discharge computed from NEON’s continuous discharge product, only for those site-months deemed Tier 1 or Tier 2 by Rhea et al (2023a), was used alongside MacroSheds data for finetuning.

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For the process-guided strategies, we used NHM estimates for all reaches coinciding with a CAMELS or MacroSheds gauge, for a total of 551 reaches. Only nine target sites on relatively high-order streams were amenable to the process-guided specialist approach, as these sites are on reaches large enough to be modeled by the NHM. The most recent version of the NHM at the time of this writing provides discharge estimates beginning in 1980, and ending in 2016, just before the installation of most NEON target sites.

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Table 2. LSTM input data. \* = Attribute tested as an afterthought, but not included in this study due to negligible improvement in trial parameter search.

<b>Meteorological forcing data (watershed-average time series)</b>	
Maximum air temp	2-meter daily maximum air temperature (°C)
Precipitation	Mean daily precipitation (mm/day)
Solar radiation	Daily surface-incident solar radiation (W/m <sup>2</sup> )
Vapor pressure	Near-surface daily average vapor pressure (Pa)
PET	Potential evapotranspiration (mm); estimated using Priestley-Taylor formulation with gridded alpha product (Aschonitis et al. 2017)
<b>Watershed attributes (statistics computed over full record)</b>	



Precipitation mean	Mean daily precipitation (mm/day)
PET mean	Mean daily potential evapotranspiration (mm/day); estimated using Priestley-Taylor formulation with gridded alpha product (Aschonitis et al. 2017)
Aridity index	Ratio of PET mean to Precipitation mean
Precip seasonality	Seasonality of precipitation; estimated by representing annual precipitation and temperature as sine waves. Positive values indicate summer peaks, while negative values indicate winter peaks. Values near 0 indicate uniform precipitation throughout the year.
Snow fraction	Fraction of precipitation falling on days with temp < 0 °C
High precipitation frequency	Frequency of high precipitation days (days with $\geq 5x$ mean daily precipitation)
High precip duration	Average duration of high precipitation events (number of consecutive days $\geq 5x$ mean daily precipitation)
Low precip frequency	Frequency of dry days (days with precipitation < 1 mm/day)
Low precip duration	Average duration of dry periods (number of consecutive days with precipitation < 1 mm/day)
Elevation	Catchment mean elevation (m)
Slope	Catchment mean slope (m/km)
Area	Catchment area (km <sup>2</sup> )
Source*	Binary indicator for NHM estimates–process-guided LSTMs only.
<b>Target data (time series)</b>	
Discharge	Specific discharge, or discharge normalized by watershed area. The same quantity may be referred to as “runoff” in other studies (mm/day).



Minimum air temp	2-meter daily minimum air temperature (°C)
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265 Table 3. LSTM model training pipelines used in the simulation of discharge at target sites. Here, “NEON” refers to NEON’s continuous discharge product, 2023 release, with quality-flagged estimates and < Tier-2 site-months (according to Rhea et al. 2023a) removed.

Model type	Phase 1	Phase 2	Phase 3
Generalist	Pretrain on CAMELS	Finetune on MacroSheds + NEON	N/A
Specialist	Pretrain on CAMELS	Finetune on MacroSheds + NEON	Finetune on NEON target site
Process-guided generalist	Pretrain on CAMELS + CAMELS-NHM	Finetune on MacroSheds + MacroSheds-NHM + NEON + NEON-NHM	N/A
Process-guided specialist	Pretrain on CAMELS + CAMELS-NHM	Finetune on MacroSheds + MacroSheds-NHM + NEON + NEON-NHM	Finetune on NHM estimates for target site

270 LSTMs were configured in R, and trained, validated, and tested using v1.3.0 of the NeuralHydrology library in Python (Kratzert et al. 2022; Van Rossum & Drake 2009) on the Duke Compute Cluster at Duke University, Durham NC, USA. All trained models used the Adam optimizer (Kingma & Ba 2014) and NeuralHydrology’s “NSE loss” function, after an initial evaluation in which we compared it to MSE and root mean squared error (Table 4). Learning was annealed using series of three fixed rates for pretraining and for round one of finetuning, according to:

$$\text{Equation 2: } r = \begin{cases} a, \epsilon \left\{ 0, \dots, \left\lfloor \frac{E}{3} \right\rfloor \right\} \\ \frac{a}{10}, \epsilon \left\{ \left\lfloor \frac{E}{3} \right\rfloor, \dots, \left\lfloor \frac{2E}{3} \right\rfloor \right\} \\ \frac{a}{100}, \epsilon \left\{ \left\lfloor \frac{2E}{3} \right\rfloor, \dots, E \right\} \end{cases}$$

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Where  $r$  is the learning rate,  $a$  is any power of 10 between 0.1 and  $10^{-7}$ , and  $E$  is the number of training epochs. Learning rate was annealed using series of two fixed rates for round two of finetuning, according to:



**Equation 3:** 
$$r = \begin{cases} \frac{a}{10}, \epsilon \left\{ \mathbf{0}, \dots, \left\lfloor \frac{E}{2} \right\rfloor \right\} \\ \frac{a}{100}, \epsilon \left\{ \left\lfloor \frac{E}{2} \right\rfloor, \dots, E \right\} \end{cases}$$

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Learning rate and other hyperparameters were selected via an inexhaustive (pseudo) grid search (Table 4), i.e. we specified a sequence of possible values for each hyperparameter and randomly selected from them to specify 30 models for each generalist. For each site, one specialist model was then configured to further finetune each of the 30 generalists, again using partial grid search to define any mutable hyperparameters. Otherwise, hyperparameters were inherited from the previous training period (Table 4). Due to our incomplete hyperparameter search procedure, better combinations probably exist. We elected not to exhaustively pursue optimal hyperparameter combinations due to the computational demand of a full grid search, and a lack of access via NeuralHydrology to callback methods necessary for implementation of true random search (Bergstra & Bengio 2012).

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Table 4. LSTM hyperparameter search space for all model types, and selected values (bold, italic) used for pretraining. These were observed to allow for both malleability and high performance of subsequent finetuning iterations over nearly 2000 exploratory LSTM trials. The ditto mark “” indicates that a finetuning parameter is inherited from the preceding training iteration. The relationship of  $a$  to the learning\_rate is defined in Equations 2 and 3. See the NeuralHydrology documentation for parameter definitions: <https://neuralhydrology.readthedocs.io/en/latest/usage/config.html>.

LSTM parameter	Pretrain	Finetune 1	Finetune 2 (specialists only)
hidden_size	20, <b>30</b> , 40, 50	”	”
output_dropout	0.1, 0.2, 0.3, 0.4, <b>0.5</b> , 0.6	0.2, 0.3, 0.4, 0.5	”
learning_rate $a$	$10^{-2}$ , <b><math>10^{-3}</math></b> , $10^{-4}$ , $10^{-5}$	$10^{-2}$ , $10^{-3}$ , $10^{-4}$ , $10^{-5}$	$10^{-2}$ , $10^{-3}$ , $10^{-4}$ , $10^{-5}$
batch_size	32, 64, 128, 256, <b>512</b> , 1024	32, 64, 128, 256, 512	”
epochs	20, <b>30</b> , 40, 50, 60	20, 30, 40	10, 20, 30
finetune_modules	N/A	head, lstm, head & lstm	head, lstm
target_variables	discharge, <b><i>discharge &amp; min air temp</i></b>	”	”
loss	<b><i>NSE</i></b> , MSE, RMSE	”	”



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All LSTM models were outfitted with fully connected, single-layer embedding networks to efficiently encode inputs as fixed-length numerical vectors (Arsov & Mirceva 2019). Separate embedding networks were used for static and dynamic inputs, with 20 neurons for static inputs and 200 neurons for dynamic inputs. All embedding neurons used the hyperbolic tangent activation function. Another advantage of embedding networks in the context of the NeuralHydrology library is that they provide one of few opportunities to introduce dropout, which can improve training efficiency and reduce overfitting (Srivastava et al. 2014).

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## 2.5 Composite discharge data product

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This study generated time-series predictions of discharge for each lotic NEON site using up to three distinct processes: linear regression on absolute discharge, linear regression on specific discharge, and one of four LSTM strategies. We provide regression predictions wherever applicable (24 of 27 sites). LSTM predictions are provided only for sites that had promising model performance after a hyperparameter search, and for which ensemble models were therefore trained (18 of 27). All model outputs and results from this study are archived at <https://dx.doi.org/10.6084/m9.figshare.22344589>.

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In addition to predictions from individual modeling strategies, we provide an analysis-ready discharge dataset for all 27 sites that splices the best available predictions across methods, including published NEON estimates (NEON 2023a; accessed 2023-05-01), into composite series (<https://dx.doi.org/10.6084/m9.figshare.23206592>), which can be visualized interactively at [https://macrosheds.org/data/vlah\\_etal\\_2023\\_composites/](https://macrosheds.org/data/vlah_etal_2023_composites/). Composite series for each NEON site begin at the start of site operation and extend to at most September 30, 2021, the last date included in the 2023 release of NEON's continuous discharge product. We also provide individual model predictions extending through 2022.

315

To construct composite series, we first distinguished as “good” site-months of NEON discharge estimates categorized as Tier 1 or Tier 2 by Rhea et al. (2023a). For a NEON site-month to meet the requirements for at least Tier 2, four requirements must be met. The linear relationship between stage, determined from pressure transducer readings, and field-measured gauge height must score at least 0.9 NSE. The transducer-derived stage series must also pass a drift test, relative to gauge height, but only if sufficient data exist to perform such a test. The rating curve used to relate stage to discharge must score at least 0.75 NSE, and fewer than 30% of predicted discharge values may exceed the range of measured discharge used to build the curve. See Rhea et al. (2023a) for further details.

325

Although only 50% of NEON's 2023-release estimates are classified as Tier 1 or Tier 2, the remainder may still be of high analytical value if NEON's quality control indicators and uncertainty bounds are observed. We also stress that NEON rating curves and protocols have improved over the course of its early operational phase, and continue to do so.



330 We then ranked the available predictions for each site, assigning rank 1 either to predictions from linear regression, or to  
NEON's continuous data product, depending on overall KGE and NSE against field measured discharge. KGE was considered  
first, and used to determine preference except in cases where the difference between NSE scores was greater than that between  
KGE scores, and opposite in sign. Rank 2 predictions were then used to fill gaps of 12 or more hours in the rank 1 series, but  
only "good" NEON site-months were included. Only after this first round of gap-filling were the remaining NEON data  
335 incorporated, with site-years achieving at least 0.5 KGE and 0.4 NSE against field-measured discharge being used to fill still-  
remaining gaps. Finally, daily LSTM predictions (placed at 12:00:00 UTC on the day of prediction) were used to fill any  
recalcitrant gaps, but only if produced by an ensemble model achieving at least 0.5 KGE and 0.5 NSE across all field discharge  
observations. After visual examination of composite series plots, we chose to prefer NEON predictions to linear regression  
predictions at site ARIK, "good" or not, due to frequent sharp disjoints between the two predicted series. See Table A1 for an  
340 account of linear regression and LSTM methods used in the construction of ensemble series.

The prevailing interval varies across data sources used to assemble our composite discharge product, from one minute (NEON)  
to one day (LSTM predictions; regression predictions at site COMO). Regression predictions were primarily generated at 15-  
minute intervals, and their timestamps are always divisible by 15 minutes. Around the prevailing NEON interval there is  
345 considerable variation due to data gaps and sensor reconfigurations, both across sites and across the temporal ranges of each  
site's record. To reduce the complexity associated with irregular time-series analysis, we synchronized the interval across data  
sources to five minutes. Regression estimates were linearly interpolated to five minutes, though gaps larger than 15 minutes  
were not interpolated. NEON estimates were first smoothed with a triangular moving average window of 15 minutes to remove  
unrealistic minute-to-minute noise associated with Bayesian error propagation. They were then interpolated the same way as  
350 the regression estimates, and finally downsampled to five minutes, with some timestamps being shifted by up to two minutes.  
For example, a duration of 30-minute sampling, with a sample taken at 00:03:00, would be shifted by two minutes, by rounding  
each timestamp up to the nearest minute divisible by five.

### 3 Results and discussion

355 This study was designed to produce high-quality estimates of continuous discharge for NEON stream gauges, especially at ten  
gauges for which the KGE of published continuous discharge was lower than 0.8, over the full record, when compared to field-  
measured discharge. A secondary goal was to improve temporal coverage of the official discharge record where possible. Via  
linear regression on discharge from donor gauges, we were able to produce 15-minute discharge estimates at 11 sites with  
360 overall KGE scores higher than those of published series (Figure 2). At four of the same sites, we achieved higher KGE via  
LSTM methods, which generated daily discharge series. Of the ten sites at which published discharge KGE was less than 0.8,  
we improved five to above that mark (mean 0.932,  $n = 5$ ). We caution that evaluation scores for both NEON's published





estimates and ours are computed on a small fraction of each series for which both an estimate and a direct field measurement are available (39-213 per site), and that measurements tend to be collected disproportionately at low flow. Therefore, users of our composite discharge product should observe uncertainties associated with estimates from all methods.

In addition to improvements in accuracy, estimates from this study inform ~5,981 site-days (75%) of missing data in the official discharge record (Figure 3), though note that they also omit ~4,486 site-days otherwise present in NEON’s official record. Omissions occur wherever observations are missing from the records of one or more donor gauges, and LSTM methods did not achieve desired efficiencies. Approximately 1,221 site-days are missing from the official record and from our reconstructions.

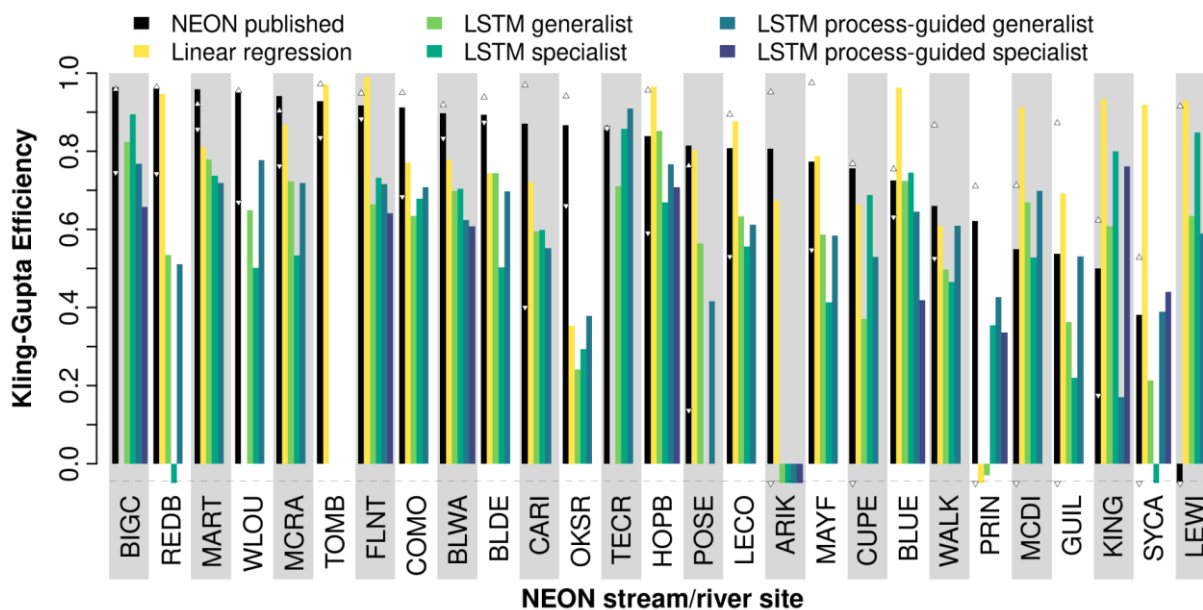


Figure 2. Efficiency of five stream discharge prediction methods and NEON’s published continuous discharge product at 27 NEON gauge locations, versus field-measured discharge. Small, white triangles represent max/min KGE of published discharge by water year (Oct 1 through Sept 30) with at least 5 field measurements (or 2 for site OKSR). NEON estimates with quality flags (dischargeFinalQF or dischargeFinalQFSciRvw of 1) were not included in KGE calculation. For the best performing LSTM method, at all sites except TECR, FLNT, REDB, WALK, POSE, and KING, displayed KGE is averaged over 30 ensemble runs with identical hyperparameters. For the sites just named, performance of a chosen method, after ensembling, dropped below that of at least one other method’s optimal KGE from parameter search. For all other LSTM site-method pairs, which were not ensembled, displayed performance is that of the best model trained during the parameter search phase. Sites are ordered by the KGE of NEON continuous discharge. See Table 3 for LSTM model definitions. KGE of 1 is a

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perfect prediction, while KGE of -0.41 is similar in skill to prediction from the mean. Negative values are truncated at -0.05 in this plot to improve visualization.

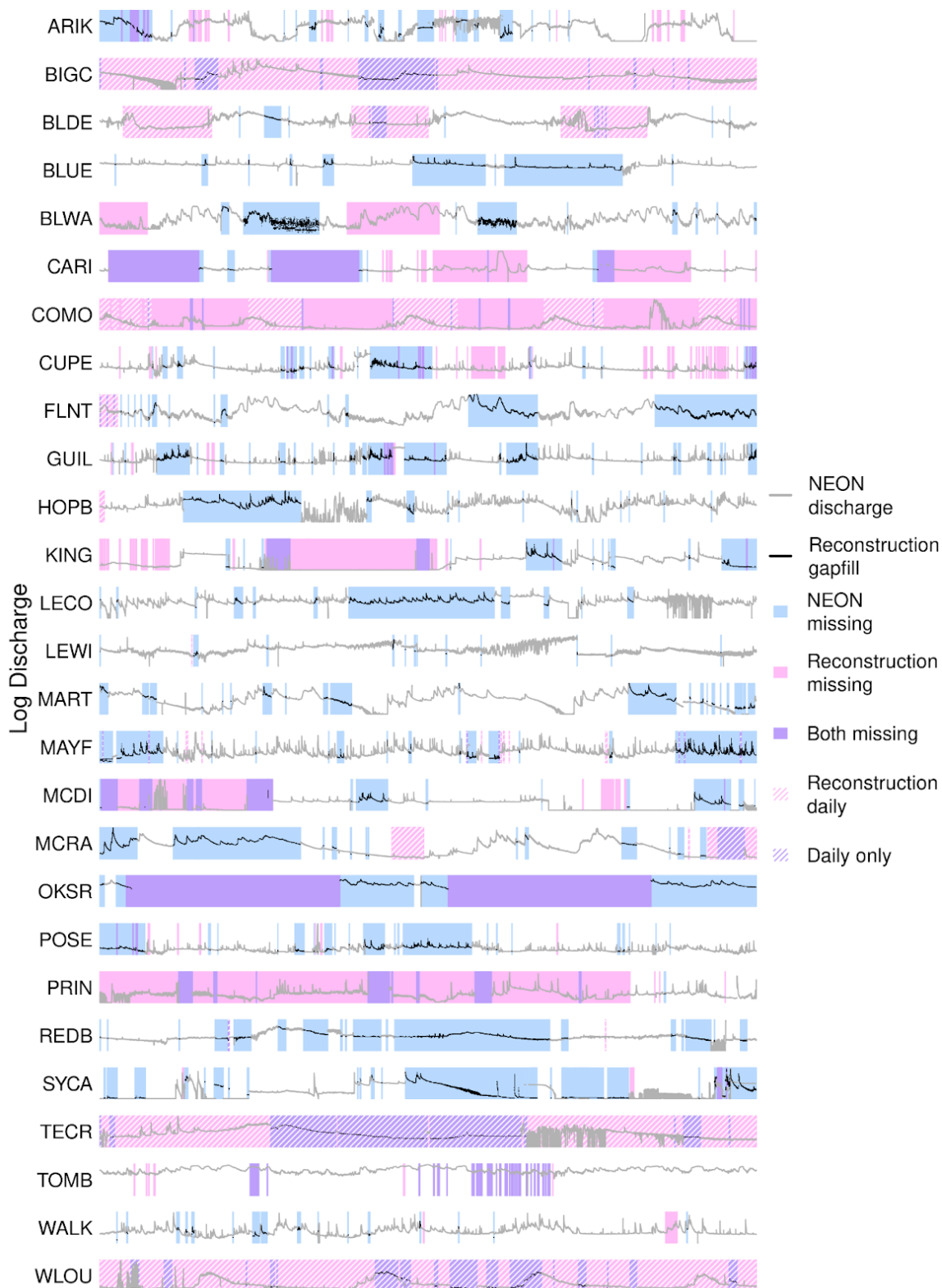




Figure 3. Durations of missing values (gaps) in NEON’s 2023 release of continuous discharge time series, illustrating gaps filled or informed by estimates from this analysis. All officially published values are shown, including those with quality control flags. Gaps smaller than six hours are not indicated.

390 A performance comparison of linear regression and four LSTM strategies is shown in Figure 2 and Figure A1, and detailed in  
Table A1. For 12 of 27 sites, linear regression on specific discharge (i.e. scaled by watershed area) provided the most accurate  
discharge predictions, while linear regression on absolute discharge performed best at the other 12 sites with donor gauges.  
LSTM models (as proper ensembles) outperformed linear regression at only 2 sites. In this study, we treat NEON field-  
measured discharge as truth, which means there are 39-213 observations for each target site. Although these numbers represent  
a tremendous investment of time and technical effort, they do not meet the high data requirements for most machine learning  
395 approaches, so we used field discharge only to evaluate, rather than train, LSTM models. By contrast, in linear regression,  
regardless of the details of any particular method, we ultimately fit a line to the relationship between donor gauge data and  
field measurements at each target site. Because the linear regression models are allowed to “see” all of the target site data (after  
a model is selected via cross-validation), they have a powerful advantage over the LSTM approaches, which in this context  
must essentially treat target watersheds as if they are ungauged. See Figures A2, A3, A4, A5, A7, and A8 for linear regression  
400 diagnostics.

Linear regression was not applicable at sites TECR, BIGC, or WLOU due to the lack of donor gauges contemporary with  
target gauge data. Donor gauges associated with Kings River Experimental Watersheds exist within close proximity to TECR  
and BIGC, but we were unable to access up-to-date discharge records for these gauges.

405 In general, linear regression provided more accurate predictions than all LSTM methods. Linear regression on absolute  
discharge produced estimates with median NSE of 0.848 and median KGE of 0.806, across sites ( $n = 24$ ; Table 5). Linear  
regression on specific discharge (i.e. scaled by watershed area) produced similar median scores (Table 5), but with deviations  
of up to 0.05 NSE and 0.08 KGE at individual sites.

410 The process-guided specialist LSTM strategy yielded predictions on par with those of the other LSTM strategies in terms of  
KGE, (median 0.652;  $n = 9$ ), but performed worst of the four in terms of NSE (median 0.329;  $n = 9$ ), possibly indicating that  
information gleaned from NHM estimates helped this strategy to accurately capture discharge variance and reduce prediction  
bias, without ultimately improving the correlation between predictions and observations. Unlike KGE, NSE only explicitly  
415 captures this latter metric (Nash & Sutcliffe 1970; Gupta et al. 2009). Conversely, the specialist performed better than the  
generalist in terms of NSE, but not KGE, suggesting information contained in NEON’s continuous discharge estimates was of  
disproportionate predictive value relative to each of correlation, variance, and bias, favoring correlation.



The specialist may have also been affected by data filtering choices. After filtering NEON continuous discharge for rating  
 420 curve issues, drift, and quality flags, relatively few daily estimates were available for some sites (47-1642). Annual and  
 seasonal variation in meteorological forcings and discharge in NEON sites' generally small, often mountainous watersheds  
 may be large enough that finetuning a pretrained LSTM on a few hundred days of site-specific data reduces its ability to  
 generalize at that site. Our specialist LSTM strategy in particular might be improved with a broader hyperparameter search,  
 especially one that explores smaller learning rates. Ideally, site-specific finetuning should enable better prediction by allowing  
 425 the network to assimilate information unique to the target site without corrupting previously learned generalities. For validation  
 plots of all ensembled LSTMs, see Figure A6.

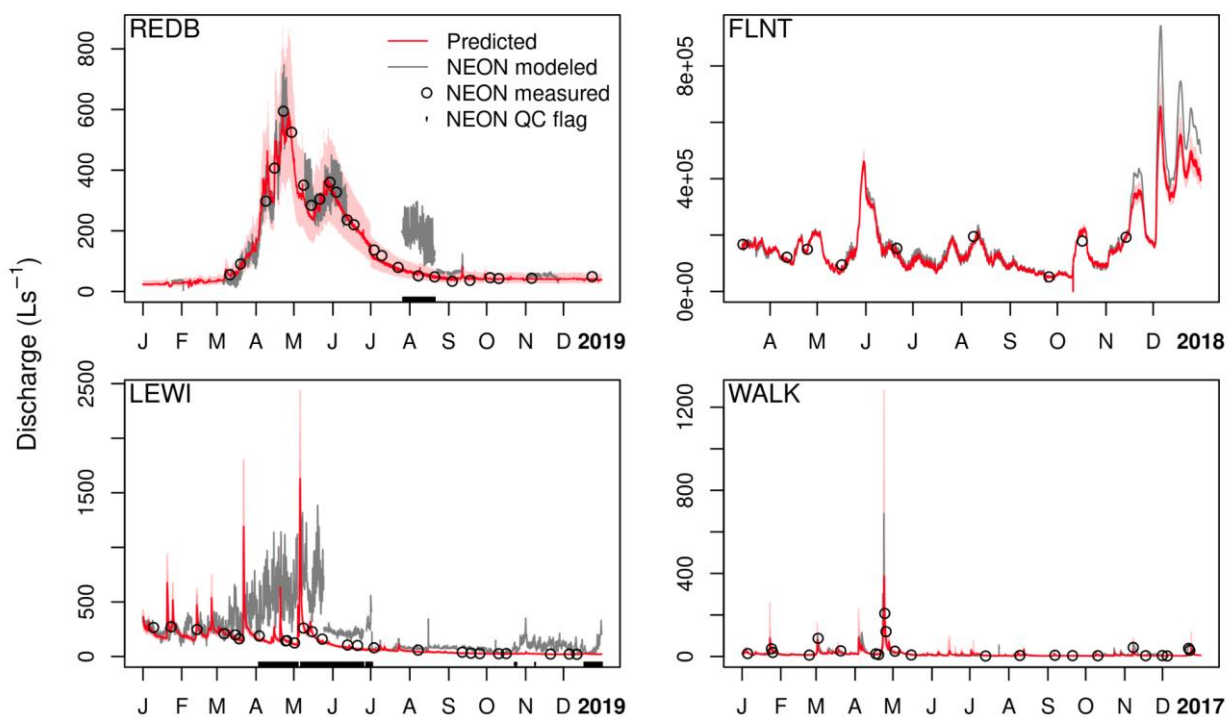
Table 5. Performance of five stream discharge prediction methods, and official continuous discharge time-series data, across  
*n* of 27 NEON gauge locations (final column). For both the Nash-Sutcliffe and Kling-Gupta Efficiency coefficients, a value  
 430 of 1 indicates perfect prediction. A value of 0 NSE indicates that predictive skill is equivalent to prediction from the mean,  
 while negative NSE is worse than mean prediction. This threshold lies at approximately -0.41 for KGE (Knoben et al. 2019).  
 “Linreg” = linear regression on donor gauge discharge series, and “scaled” means predictor and response discharge were scaled  
 by their respective watershed areas.

Model/Data	NSE				KGE				<i>n</i>
	Median	Mean	Min	Max	Median	Mean	Min	Max	
Official record	0.880	0.417	-9.95	0.989	0.839	0.711	-1.50	0.964	27
Linreg	0.848	0.760	-0.038	0.993	0.806	0.746	-0.697	0.988	24
Linreg scaled	0.847	0.757	-0.037	0.993	0.807	0.743	-0.695	0.989	24
Generalist LSTM	0.473	-18.8	-498	0.904	0.634	-0.220	-20.2	0.852	26
Specialist LSTM	0.477	-12.6	-307	0.920	0.556	-0.256	-15.7	0.895	25
Process-guided generalist LSTM	0.434	-31.3	-824	0.848	0.618	-0.453	-26.4	0.869	26
Process-guided specialist LSTM	0.329	-92.0	-831	0.749	0.652	-2.40	-26.5	0.866	9



435 The process-guided specialist LSTM strategy was viable at nine sites for which discharge estimates were available from the National Hydrologic Model. By using a mechanistic (i.e. process-based) model with higher spatial resolution than the NHM, it should be possible to apply this process-guided approach at more of the NEON sites. A potentially stronger process-guided approach would use mechanistic model predictions as features (predictors), rather than training targets, but that would require mechanistic model predictions concurrent with discharge series at target sites, whereas NHM predictions at the time of this  
440 writing are available only through the year 2016. For a summary of process-guided deep learning strategies, see the “Integrating Design” subsection of Appling et al. (2022).

Estimated discharge time series from this study are of practical value for any researcher using NEON continuous discharge data, especially for those sites and site-months at which published data from NEON’s early operational phase may be unreliable  
445 (Rhea et al. 2023a). Figure 4 shows that official records at sites REDB and LEWI are compromised by disagreement (erratic sections of gray lines) between pressure transducer stage readings and manual gauge height recordings, discussed in Rhea et al (2023a). Red lines show improved estimates via linear regression on discharge from donor gauges. Sites FLNT and WALK show generally close agreement between NEON discharge and our regression estimates, but note uncertainty associated with high discharge values.



450



Figure 4. Best linear regression predictions of continuous discharge for four NEON gauge-years, compared with official NEON discharge data. All officially published values are shown, including those with quality control flags, indicated by black marks on lower border. Light red polygons represent 95% prediction intervals. NEON uncertainty is not shown.

455 For practical reasons, field discharge measurements are often collected disproportionately in low flow conditions. As a result, any model attempting to use field measurements to reconstruct continuous discharge will estimate with higher uncertainty at high flow than at low. Mechanistic models that proceed from physical principles, or data-driven approaches that can generalize from prior observations, do not in principle suffer this disadvantage, as they do not depend on observations from a target site. However, these approaches may not reliably generate strong predictions at all sites or under all conditions (Razavi & Coulibaly  
460 2013; Kratzert et al. 2019b), and may produce erratic point estimates where conditions diverge from past observations. Hybrid approaches that successfully leverage field measurements, as well as physical principles or learned relationships, are likely to yield well-constrained predictions where our efforts did not.

This study demonstrates that, in proximity to established streamflow gauges, even simple statistical methods can be used to generate accurate, continuous discharge at “virtual gauges,” where discrete discharge has been measured. The number of field  
465 measurements across sites in this study varies from 39 to 213, but the number required for virtual gauging may be substantially smaller even than the minimum of this range. If the discharge relationships between a target site and all donor gauges were perfectly linear or log-linear, they could in principle be established with only two precise measurements at the target site. More important than the quantity is the distribution of measurements across flow conditions, which should be sufficient to fully characterize all modeled discharge relationships and their linearity or lack thereof (Sauer 2002; Zakwan et al. 2017).  
470 Concretely, we advocate for “storm chasing,” or disproportionately seeking to sample discharge under extreme conditions, and during both rising and falling limbs of storm events, rather than routine sampling. Observed NEON flow conditions relative to predicted discharge can be seen in Figure A9. See Philip & McLaughlin (2018) for further commentary on establishing a virtual gauge network, and Seibert & Beven (2009) and Pool & Seibert (2021) for information on the number and statistical properties of discharge samples required to establish strong stage-discharge or discharge-discharge relationships.

#### 475 **4 Conclusions**

Using linear regression on donor gauge data and LSTM-RNNs, we reconstructed continuous discharge at 5-minute and/or daily frequency for the 27 stream and river monitoring locations of the National Ecological Observatory Network (NEON) over the water years 2015-2022. Relative to field-measured discharge as ground truth, our estimates achieve higher Kling-Gupta efficiency than NEON’s official continuous discharge at 11 sites. We also provide continuous discharge estimates for  
480 ~199 site-months for which no official values have been published. Estimates from this study can be used in conjunction with officially released NEON continuous discharge data to enhance the analytical potential of NEON’s river and stream data





products during its early operational phase. Toward that end, we provide composite discharge series for each site, incorporating the best available estimates across all methods used in this study and NEON’s published estimates. Considering the lag of up to 2.5 years before provisional discharge data become fully quality controlled and officially released by NEON, our methods may also be used to increase the rate at which discharge-associated stream chemistry, dissolved gas, and water quality products become fully usable by the community. All data and results from this study can be downloaded from the Figshare collection at <https://doi.org/10.6084/m9.figshare.c.6488065>. Composite series can be visualized interactively at [https://macrosheds.org/data/vlah\\_etal\\_2023\\_composites/](https://macrosheds.org/data/vlah_etal_2023_composites/). All code necessary to reproduce this analysis is archived at <https://doi.org/10.5281/zenodo.7976251>.

In general, linear regression methods produced more accurate discharge estimates (median KGE: 0.79; median NSE: 0.81;  $n = 24$  sites) than LSTM approaches due to the fact that regression models were able to fully leverage available field measurements as well as highly informative donor gauge data. Nonetheless, LSTM methods achieved median ensemble KGE of 0.71 and NSE of 0.56 across 18 sites, making their estimates a valuable supplement. Although LSTM-generated discharge series are of daily frequency, some users will prefer them to higher resolution regression estimates, as the latter may be subject to error in the event of highly localized precipitation events affecting either donor or target gauges, but not both.

Improvements to our design could be made in several ways. LSTM models could be exposed to additional training data, such as the recently published Caravan compendium of CAMELS offshoots (Kratzert et al. 2023) or future expansions of the MacroSheds dataset (Vlah et al. 2023). Neural networks trained on sub-daily inputs might be better equipped to exploit atmospheric-hydrological dynamics that respond to both daily and annual cycles. Linear regression methods too might be improved with the use of additional predictors, such as continuous water level or precipitation.

The success of simple statistical methods in generating high-quality continuous discharge time series demonstrates the viability of “virtual gauges,” or locations at which a small number of field discharge measurements, in proximity to one or more established gauges, provide a basis for continuous discharge estimation in lieu of a gauging station. Virtual gauges have the potential to greatly expand the spatial coverage of continuous discharge data throughout the USA and any richly gauged region of the world.

## Appendix A

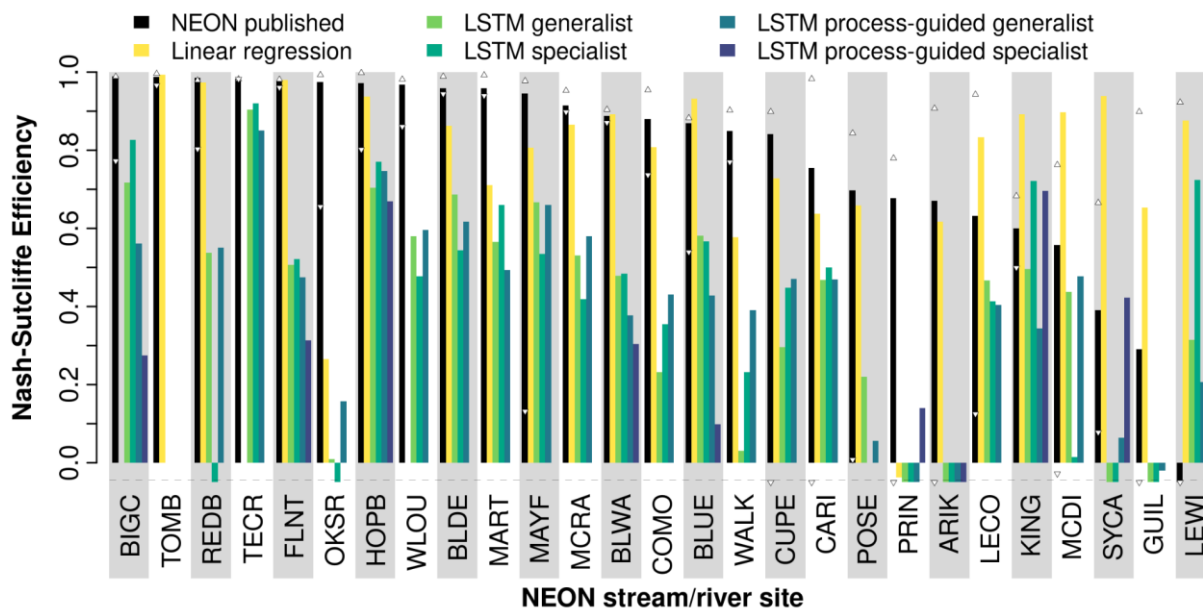
Table A1: Methods from this study used in the construction of composite discharge series. Composite series also incorporate NEON continuous discharge product DP4.00230.001 (NEON 2023a; 2023 release accessed 2023-05-01). “Linreg” = linear regression; “glmnet” = Ridge regression; “lm” = OLS regression; “segmented” = segmented regression; “abs” = absolute discharge; “spec” = specific discharge; “pgdl” = process-guided deep learning.

Site	KGE linreg	NSE linreg	Method linreg	KGE LSTM	NSE LSTM	Method LSTM
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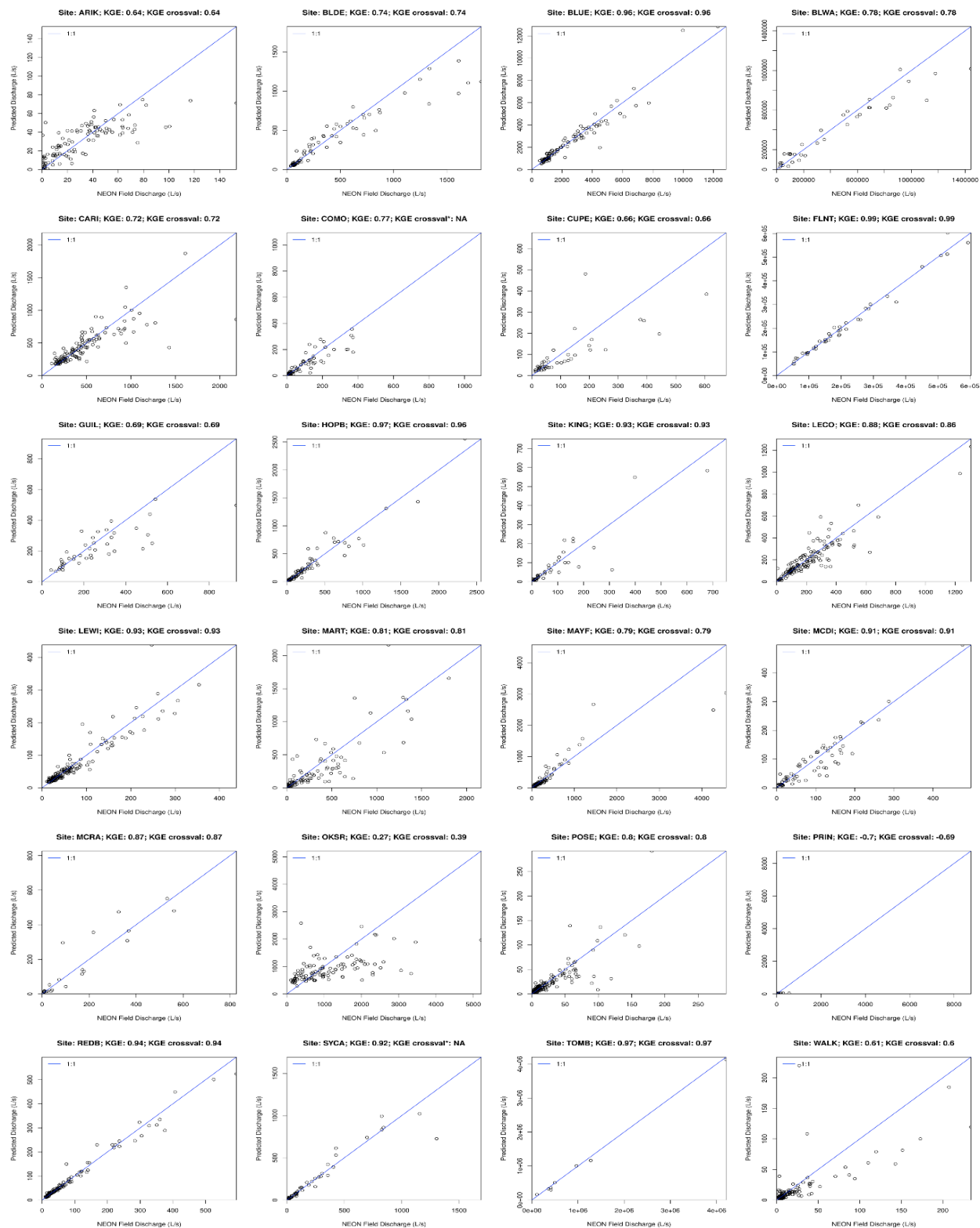




FLNT	0.989	0.980	glmnet_spec	0.664	0.507	generalist
TOMB	0.970	0.993	glmnet_abs			
HOPB	0.966	0.937	lm_abs	0.852	0.704	generalist
BLUE	0.962	0.932	lm_spec	0.746	0.567	specialist
REDB	0.946	0.973	lm_abs	0.511	0.551	generalist_pgdl
KING	0.935	0.888	glmnet_abs			
LEWI	0.929	0.875	glmnet_abs	0.848	0.724	specialist
SYCA	0.919	0.938	segmented_spec			
MCDI	0.912	0.897	glmnet_spec			
LECO	0.877	0.833	lm_spec			
MCRA	0.868	0.866	glmnet_spec	0.723	0.531	generalist
MART	0.811	0.706	glmnet_spec	0.779	0.566	generalist
POSE	0.803	0.648	glmnet_spec			
MAYF	0.787	0.806	glmnet_abs	0.586	0.666	generalist
BLWA	0.779	0.892	glmnet_abs			
COMO	0.771	0.806	glmnet_composite_spec			
BLDE	0.744	0.863	glmnet_abs	0.744	0.687	generalist
CARI	0.721	0.637	glmnet_abs			
GUIL	0.692	0.653	glmnet_abs			
ARIK	0.674	0.596	glmnet_abs			
CUPE	0.663	0.728	glmnet_spec			
WALK	0.607	0.532	glmnet_spec			
BIGC				0.895	0.827	specialist
WLOU				0.778	0.596	generalist_pgdl
TECR				0.711	0.904	generalist
PRIN						
OKSR						



515 Figure A1. Efficiency of five stream discharge prediction methods and NEON’s published continuous discharge product at 27  
 NEON gauge locations, versus field-measured discharge. Small, white triangles represent max/min NSE of published  
 discharge by water year (Oct 1 through Sept 30) with at least 5 field measurements (or 2 for site OKSR). NEON estimates  
 with quality flags (dischargeFinalQF or dischargeFinalQFSciRvw of 1) were not included in NSE calculation. For the best  
 performing LSTM method, at all sites except TECR, FLNT, REDB, WALK, POSE, and KING, displayed NSE is averaged  
 520 over 30 ensemble runs with identical hyperparameters. For the sites just named, performance of a chosen method, after  
 ensembling, dropped below that of at least one other method’s optimal NSE from parameter search. For all other LSTM site-  
 method pairs, which were not ensembled, displayed performance is that of the best model trained during the parameter search  
 phase. Sites are ordered by the NSE of NEON continuous discharge. See Table 3 for LSTM model definitions. NSE of 1 is a  
 perfect prediction, while NSE of 0 is equivalent in skill to prediction from the mean. Negative values are truncated at -0.05 in  
 525 this plot to improve visualization.



<https://doi.org/10.5194/egusphere-2023-1178>

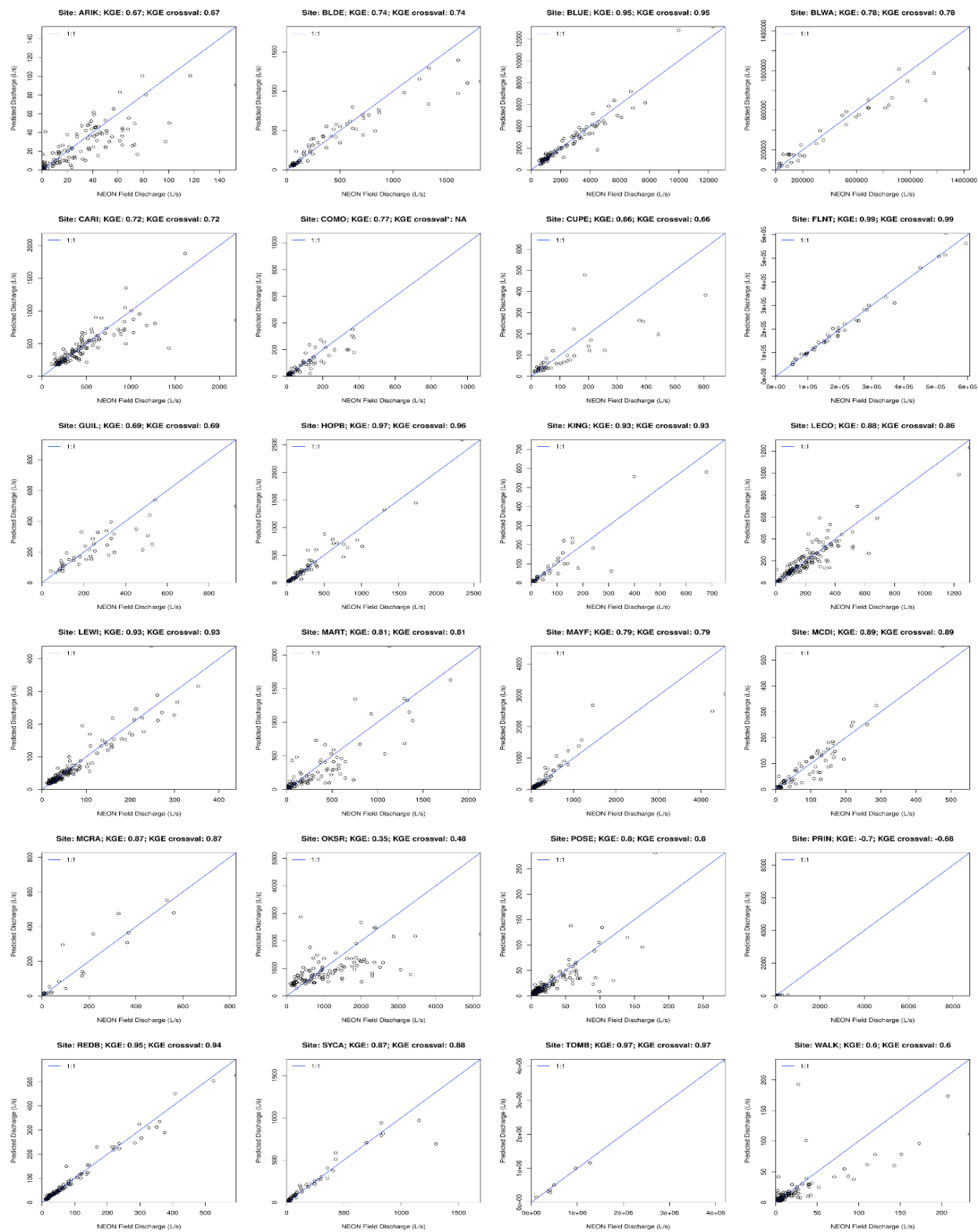
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Figure A2. Observed (field) discharge vs. predictions from linear regression on specific discharge (i.e. scaled by watershed area).

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Figure A3. Observed (field) discharge vs. predictions from linear regression on absolute discharge (i.e. not scaled by watershed area).

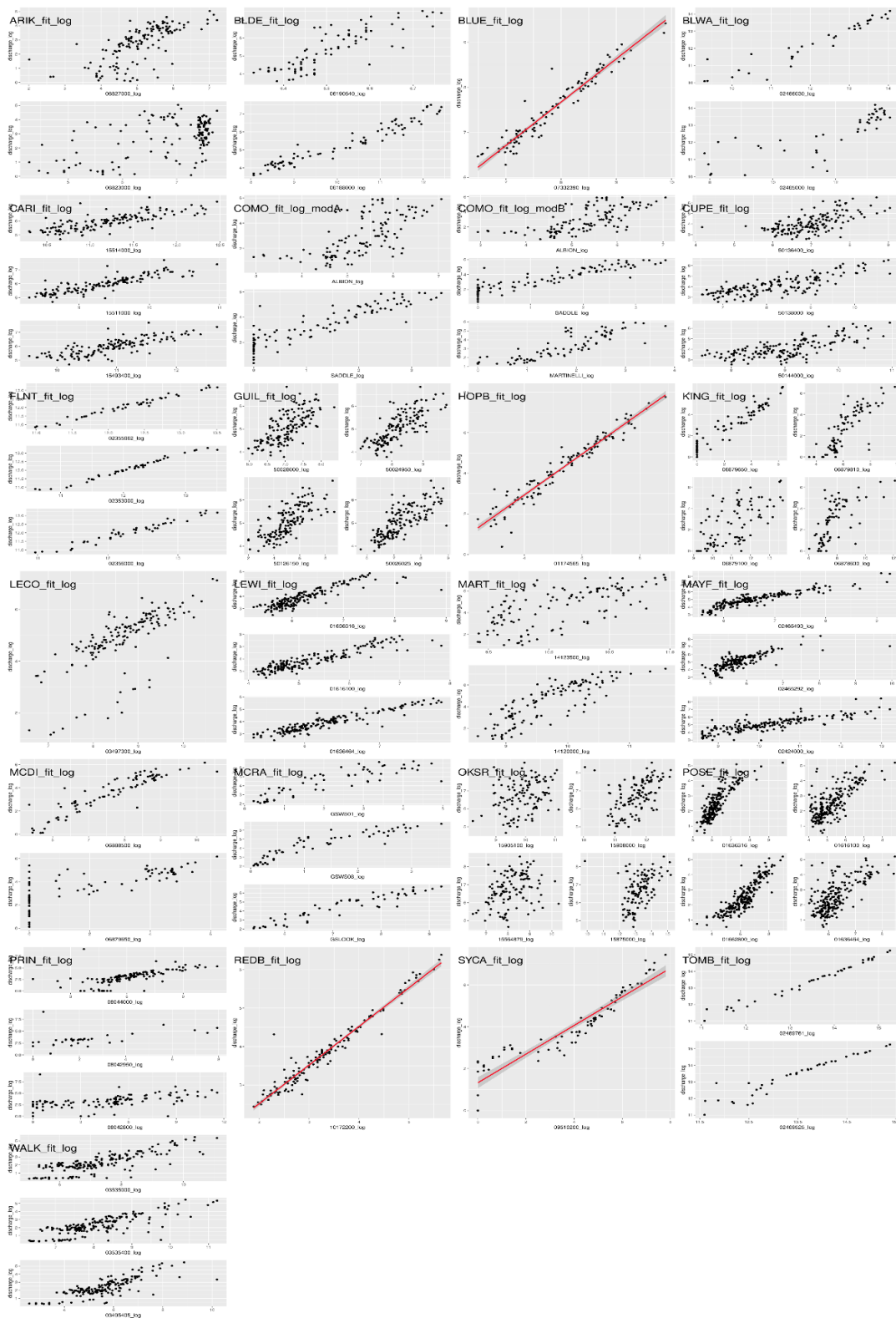




Figure A4: Marginal relationships between donor and target gauges for regression on specific discharge. Regression lines are shown only for single-donor regressions, fitted via OLS. Site SYCA, here exhibiting a breakpoint, was modeled with segmented regression, and thus the regression line shown has no relevance.



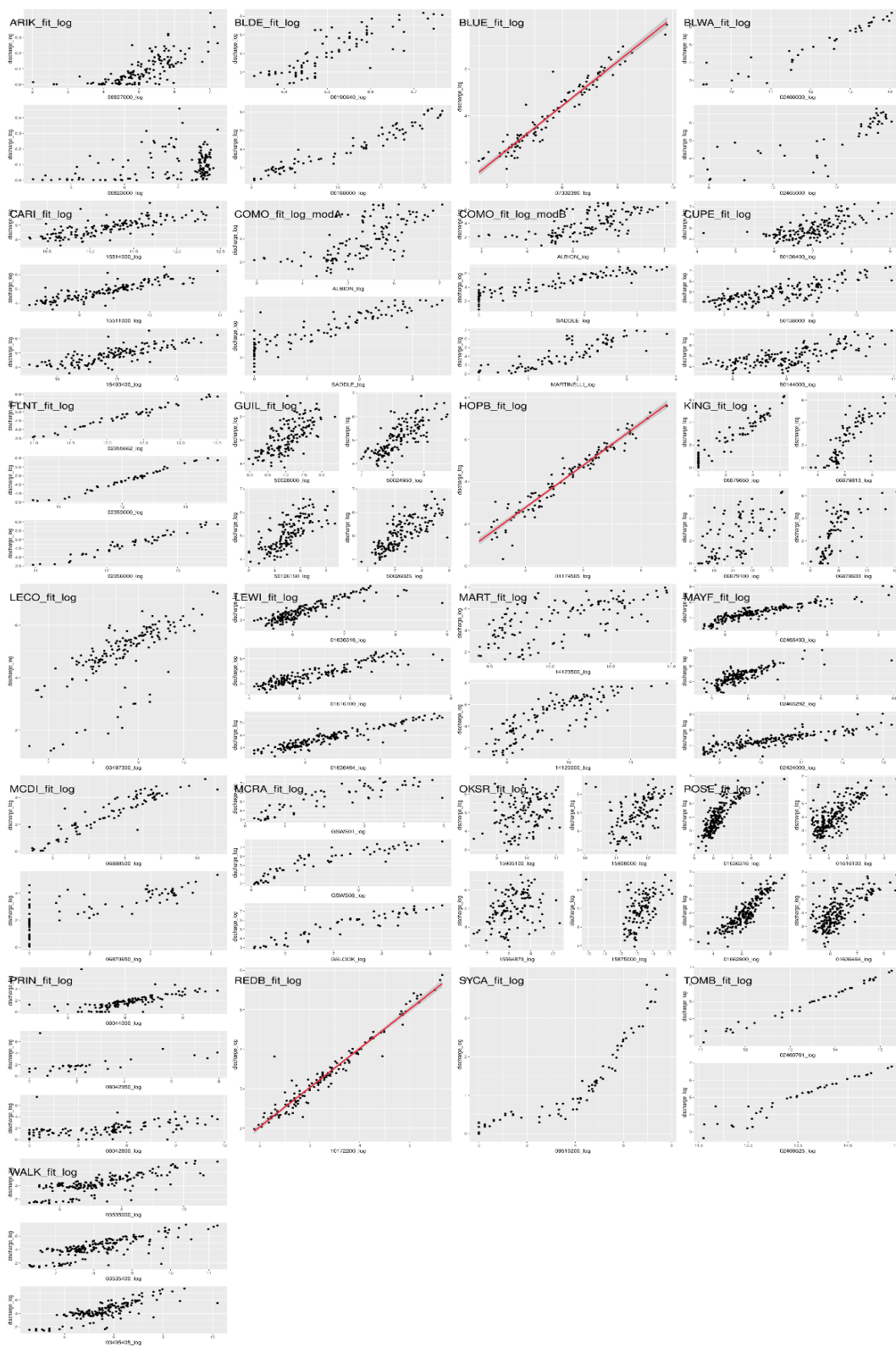




Figure A5: Marginal relationships between donor and target gauges for regression on absolute discharge. Regression lines are shown only for single-donor regressions, fitted via OLS. Site SYCA, here exhibiting a breakpoint, could not be fitted via segmented regression in the context of absolute discharge.

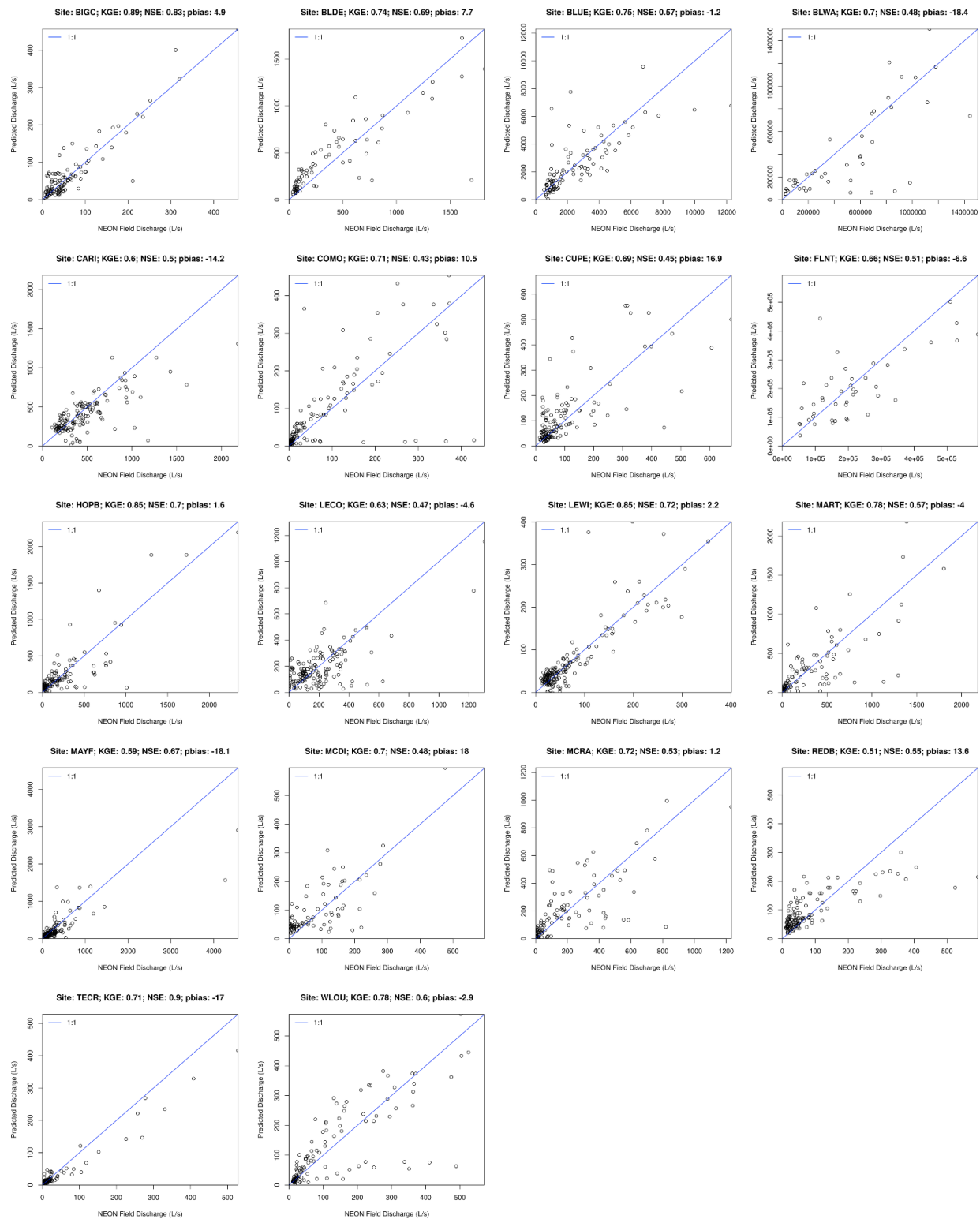




Figure A6. Observed (field) discharge vs. ensembled LSTM predictions.

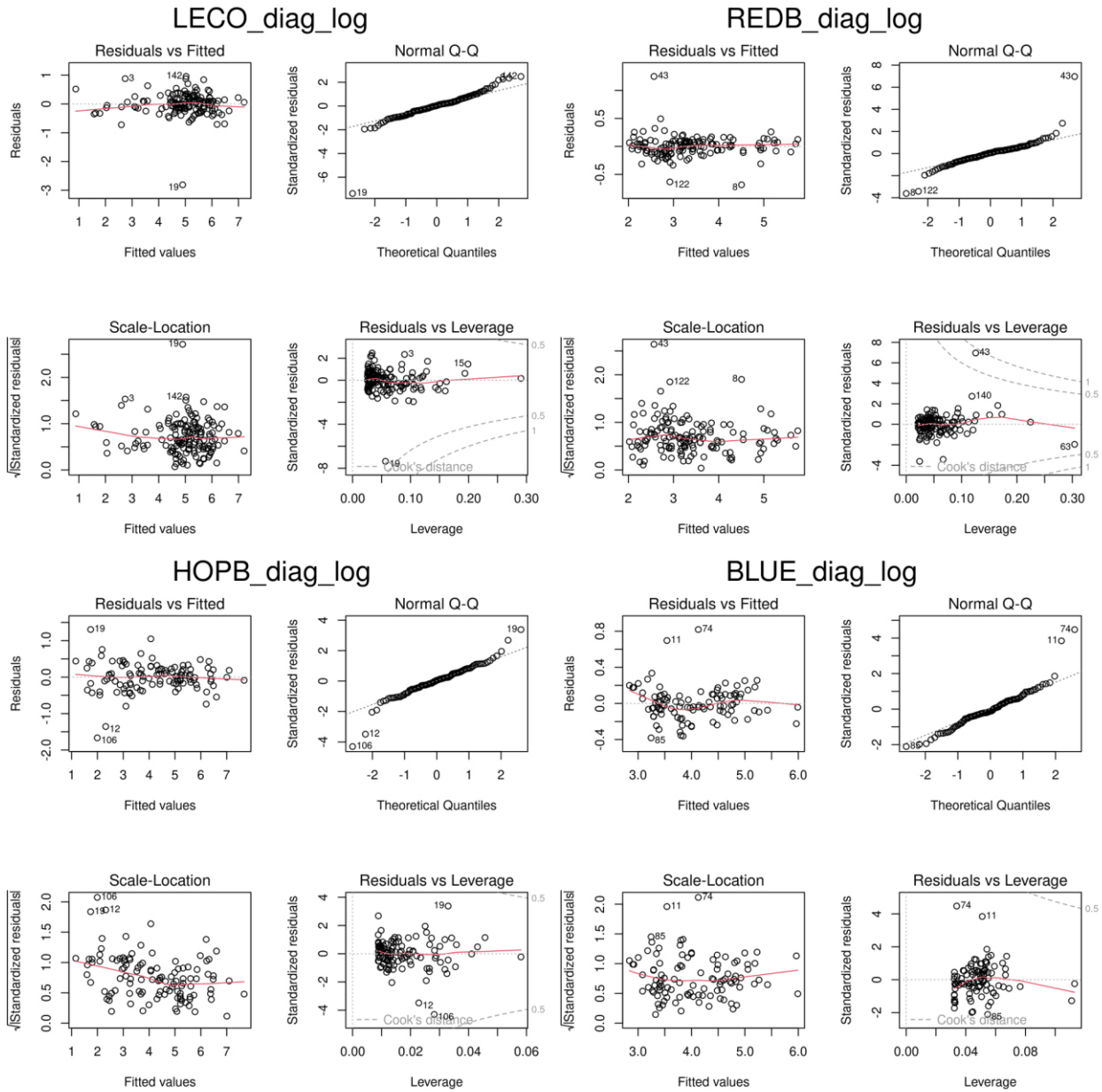


Figure A7. Diagnostic plots for the four sites modeled by OLS regression on specific discharge.

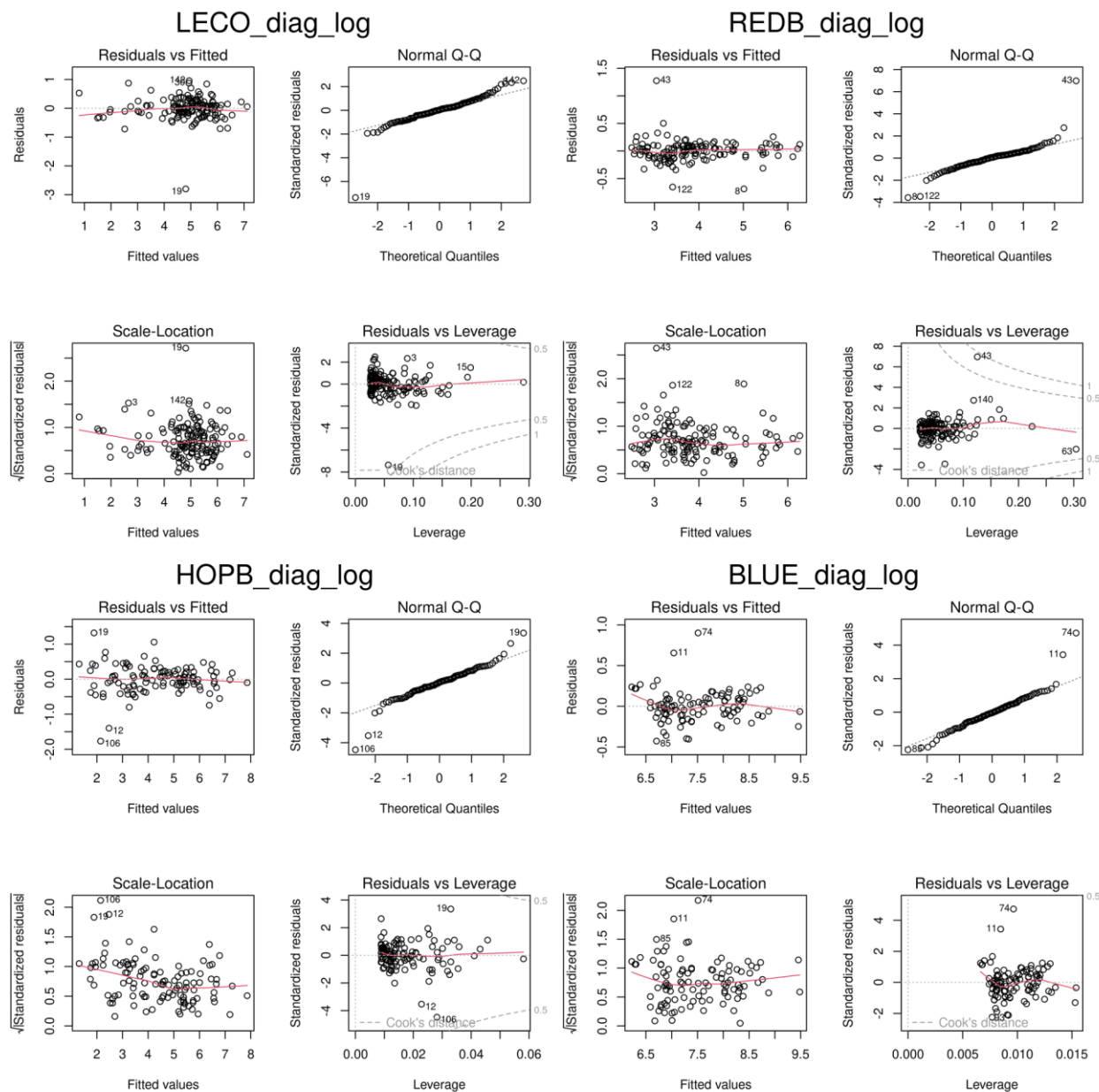


Figure A8. Diagnostic plots for the four sites modeled by OLS regression on absolute discharge.

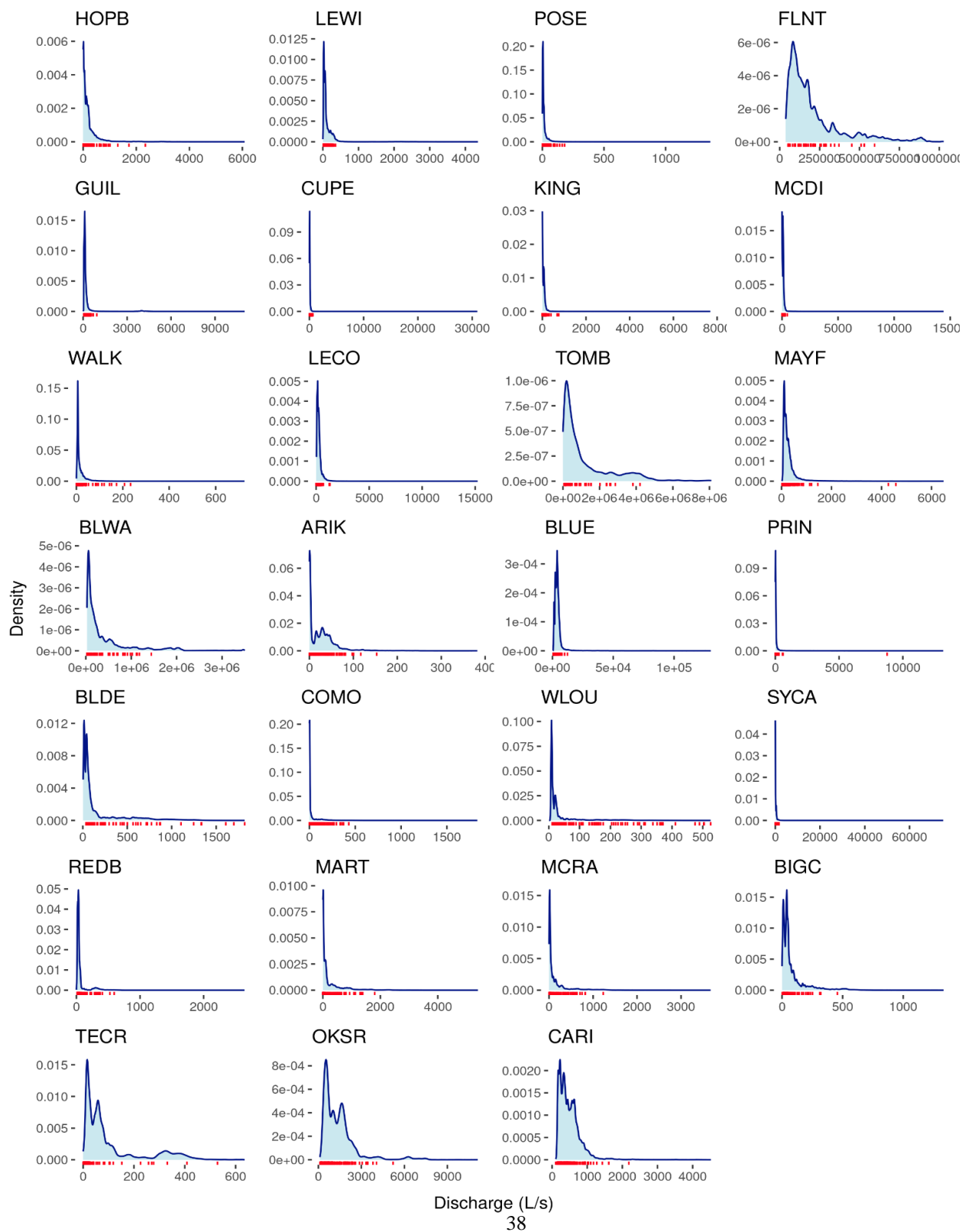




Figure A9. Density of NEON-estimated discharge (blue polygon) relative to field-measured discharge observations (red marks).

### Code availability

560

All code necessary to reproduce this analysis is archived at <https://doi.org/10.5281/zenodo.7976251>.

### Data availability

565 All data and results from this study can be downloaded from the Figshare collection at

<https://doi.org/10.6084/m9.figshare.c.6488065>. Composite series can be visualized interactively at

[https://macrosheds.org/data/vlah\\_et\\_al\\_2023\\_composites/](https://macrosheds.org/data/vlah_et_al_2023_composites/).

### Author contribution

570

MRVR, ESB, and MJV originated the project and identified its goals and methods. MJV carried out all analyses and drafted the manuscript. SR assisted in data collection. All authors took part in steering the project and editing the manuscript.

### Competing interests

575

The authors declare that they have no conflict of interest.

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