# On the importance of discharge observation uncertainty when evaluating and comparing numerical models: a interpreting hydrological examplemodel performance

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Abstract. The comparison of models in geosciences involves refining a single model or comparing various model structures. However, such model comparison studies are invalid without considering the uncertainty estimates of observations in evaluating relative model performance . The accuracy of model skill metrics is also affected by temporal sampling uncertainty, which causes outliers to have a disproportional effect on the skill score. In hydrology, For users of hydrological models, the suitability

- 5 of models can be dependent upon how well their simulated outputs align with observed discharge. This study emphasizes the crucial role of factoring in discharge observation uncertainty when assessing the performance of hydrological models. We introduce an ad-hoc approach, implemented through the eWaterCycle platform, to evaluate the significance of differences in model performance while considering the uncertainty associated with discharge observations. The analysis of the results encompasses 299 catchments from the CAMELS-GB large-sample hydrology datasets that contain collection of catchments
- 10 with hydro-meteorological timeseries, catchment boundaries and catchment attributes provide an excellent test-bed for model evaluation and comparison studies. In this study we use a large-sample dataset to highlight the importance of including these two sources of uncertainty. catchment dataset, addressing 3 distinct use cases that are of practical importance for model users. These use cases involve assessing the impact of additional calibration on model performance using discharge observations, conducting conventional model comparisons, and examining how the variations in discharge simulations resulting from model 15
- structural differences compare with the uncertainties inherent in discharge observations. Two model experiments are set up using 396 catchments of the CAMELS-GB hydrology dataset. The intra-model experiment evaluates the streamflow estimates of the wflow\_sbm hydrological model with and without additional calibrationand the inter-model experiment compares the results of the PCR-GLOBWB and wflow sbm models. The temporal sampling uncertainty , the result of outliers in the squared error probability distribution between simulations and observations, is found to be
- 20 substantial throughout the case studyarea. High sampling uncertainty indicates that the objective function values used to evaluate model performance are heavily influenced by only a few data pointsQur results, based on the 5th to 95th percentile range of observed flow, highlight the substantial influence of discharge observation uncertainty on the interpretation of model performance differences. Specifically, when comparing model performance before and after additional calibration, we find

that in 98 out of 299 instances, the simulation differences fall within the bounds of discharge observation uncertainty. This

- 25 underscores the inadequacy of neglecting discharge observation uncertainty during calibration and subsequent evaluation processes. Furthermore, in the model comparison use case, we identify numerous instances where observation uncertainty masks discernible differences in model performance, underscoring the necessity of accounting for this uncertainty in model selection procedures. While our assessment of model structural uncertainty generally indicates that structural differences often exceed observation uncertainty estimates, few exceptions do exist. The comparison of individual conceptual hydrological
- 30 models indicates that there are no clear trends between model complexity and subsequent model simulations falling within the uncertainty bounds of discharge observations. This is the case for 53 catchment simulations of the inter-model experiment and half of the simulations (210) of the intra-model experiments as indicated by larger sampling uncertaintythan the difference in the KGE-NP objective function. This highlights the importance of reporting and determining the cause of sampling uncertainty before drawing conclusions on large-sample hydrology based model performance. The same conclusion is drawn for the
- 35 streamflow observation uncertainty analysis. One third of the catchments simulations (123)of the intra-model experiment showed smaller streamflow simulation differences than streamflow observation uncertainties, compared to only 4 catchment simulations of the inter-model experiment due to smaller differences between streamflow simulations. The results of this study demonstrate that it is crucial for benchmark efforts based on large-samples of catchments to include streamflow observation uncertainty and objective function sampling uncertainty to obtain more robust results.
- 40 Based on these findings, we advocate for the integration of discharge observation uncertainty into the calibration process and also into the reporting of hydrological model performance as has been done in this study. This integration ensures more accurate, robust, and insightful assessments of model performance, thereby improving the reliability and applicability of hydrological modeling outcomes for model users.

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#### 45 1 Introduction

Many fields in geoscience rely on uncertain data to accurately estimate states and fluxes that support Many fields in geoscience rely on uncertain data to accurately estimate state and fluxes that support decision-making<del>. One</del> . Uncertain data in hydrology encompasses multiple sources that include direct measurements, proxy-based measurements, interpolation techniques, scaling processes, and data management practices [\(McMillan et al.](#page-34-0) [\(2018\)](#page-34-0). A large literature has been devoted on discussing the effect

of data quality limitations on hydrological modelling (e.g. [Yew Gan et al.](#page-36-0) [\(1997\)](#page-36-0); [Kirchner](#page-33-0) [\(2006\)](#page-33-0); [Beven et al.](#page-31-2) [\(2011\)](#page-31-0); [Kauffeldt et al.](#page-33-1) (20 50 ). Data uncertainty can be distinguished into input data uncertainty (e.g. [Kavetski et al.](#page-33-3) [\(2006a,](#page-33-3) [b\)](#page-33-4)) and evaluation data uncertainty (e.g.[McMillan et al.](#page-34-1) [\(2010\)](#page-34-1).

Input data, primarily comprises meteorological variables such as precipitation and temperature. Other input data sources include static data, such as soil and topographic properties that are used to estimate model parameters. The inherent uncertainties

- 55 in input datasets influence the model's simulation of states and fluxes (e.g. [Balin et al.](#page-30-2) [\(2010\)](#page-30-2); [Bárdossy and Das](#page-31-3) [\(2008\)](#page-31-3); [Bárdossy et al.](#page-31-4) (20 ). The uncertainty propagation from input to model output is also closely influenced by the model structure [\(Butts et al., 2004;](#page-31-6) Liu and Gupts The effects of uncertainty propagation have therefore been a focal point in literature, e.g. [Beven](#page-30-4) [\(2006\)](#page-30-4); [Montanari and Toth](#page-35-0) [\(2007\)](#page-35-0); Gupta
	- ✿ .

Evaluation data uncertainty, the focus of this study, plays a pivotal role in determining the potential accuracy and robustness

- 60 of hydrological models. This is the case for model calibration, a processes that involves fine-tuning model parameters to ensure that the model accurately and consistently reflects the observed historical behaviour of the hydrologic system. Typically this <u>is based on discharge. When a model aims to replicate discharge values without including discharge observation uncertainty, the</u> results are constrained to match a precise but potentially not accurate representation of the hydrological response [\(Vrugt et al., 2005\)](#page-36-1) . As a consequence, accurately calibrating the model becomes more challenging due to the demand of incorporating evaluation
- data uncertainty into the calibration process to minimize bias in model parameters [\(McMillan et al., 2010\)](#page-34-1). 65 Multiple studies have demonstrated the importance of accounting for uncertainties in discharge observations. These mainly <u>focus on hydrological model calibration (e.g. [Beven and Binley](#page-30-5) [\(1992\)](#page-30-5); [Beven and Freer](#page-30-6) [\(2001\)](#page-30-6); [Beven and Smith](#page-31-1) [\(2015\)](#page-31-7); [McMillan et al.](#page-34-1)</u> ). In these studies multiple methodologies are used to quantify uncertainty estimates of discharge observations that are subsequently used for model calibration (overview in [McMillan et al.](#page-34-6) [\(2012\)](#page-34-6)).
- 70 Combined, all uncertainty sources (input data, evaluation data, model structure, model parameters, initial conditions) add to a <u>concept in hydrological modelling commonly referred to as the equifinality concept [\(Beven and Freer](#page-30-6) [\(2001\)](#page-30-6); [Beven](#page-30-4) [\(2006\)](#page-30-4); Montanari and</u> ). This concept is characterised by the circumstance of various model configurations yielding similar behavioural or acceptable results. Therefore, the recommendation is to account for all uncertainty sources simultaneously. An example of a method that includes all uncertainty sources during the parameter estimation process is the General Likelihood Uncertainty Estimation
- 75 (GLUE; [Beven and Freer](#page-30-6) [\(2001\)](#page-30-6)) method. In practice, such methodologies are not always applied by model users although the difficulty of implementation can be dispelled [\(Pappenberger and Beven](#page-35-1) [\(2006\)](#page-35-1)).

Hydrological model evaluation by model users is often solely based on discharge observations. The inherent uncertainties in this single source of observational data might obscure the model's ability to simulate actual discharge. Therefore, omitting data uncertainty during model evaluation negatively affects the interpretation of relative model simulation differences as these

might fall within the uncertainty bounds of the observations. 80

Another challenging aspect of hydrological modelling in particular is the large spatial and temporal landscape and hydrological heterogeneity (e.g. Gao et al., 2018). Capturing this variability of the hydrological system. Capturing the large variety in landscape and hydrological heterogeneity, when evaluating or comparing hydrological models, can be achieved through the use of so called large-sample catchment hydrology datasets.

85 These large-sample catchment datasets contain hydro-meteorological <del>timeseries</del>time series, catchment boundaries and catchment attributes for a large number of catchments. They are complemented with streamflow The dataset is complemented with discharge observations at the catchment <del>outlet outlets</del> and meteorological forcing data such as datasets that include precipitation and temperature. The large-sample catchment datasets are collected using a consistent methodology across all catchments.

- 90 Recent large-sample datasets follow the structure introduced by [Addor et al.](#page-30-8)  $(2017)$   $(Addor et al., 2017)$  in the form of the CAMELS(-US) dataset. <u>More recently, [Coxon et al.](#page-31-10) [\(2020\)](#page-31-10)</u> released the CAMELS-GB, that includes estimates of quantified discharge observation uncertainty. This dataset describes 671 catchments in Great Britain of which 503 gauging stations are complemented with quantified discharge observation uncertainty estimates [\(Coxon et al.](#page-31-7) [\(2015\)](#page-31-7)). A recent effort by <del>[Kratzert et al.](#page-34-8) [\(2022\)](#page-34-8)</del> [Kratzert et al.](#page-34-8) [\(2022\)](#page-34-8) combined all available national CAMELS datasets in the overarching CARAVAN dataset for global con-
- 95 sistency and boosting accessibility through data access via Google Earth Engine.

The accessibility of large-sample <u>catchment</u> data triggered a wealth of research as discussed in the overview by <del>[Addor et al.](#page-30-9) [\(2020\)](#page-30-9)</del> <del>, including [Addor et al.](#page-30-9) [\(2020\)](#page-30-9), including use</del> as a test-bed for hydrological model evaluation and model comparison studies (e.g. [Mizukami et al.](#page-34-9) [\(2017\)](#page-34-9); [Rakovec et al.](#page-35-2) [\(2019\)](#page-34-10); [Lane et al.](#page-34-10) (2019); [Feng et al.](#page-32-1) [\(2022\)](#page-32-1)Mizukami et al. (2017); Rakovec et al. (2019); L

). The benefits of <del>using large-sample these</del> datasets are that <del>by including large samples of catchments , the robustness of model</del>

100 results is tested [\(Andréassian et al., 2006;](#page-30-10) [Gupta et al., 2014\)](#page-32-2). In addition, large-sample datasets allow for model evaluation and analyses across catchments to identify correlations between catchment attributes and model performance (e.g. [Donnelly et al.](#page-32-3) [\(2016\)](#page-32-3); Kona ); thereby not only answering if a model is good but also why [\(Kirchner, 2006\)](#page-33-0).

However, the relevance of the results of model evaluation and comparison studies is unclear when (streamflow)observation uncertainty is not included in large sample datasets, as is usually the case. As a result the adequacy of hydrological models

105 might be misconstrued. Therefore, a large literature has been devoted on discussing the effect of data quality limitations on hydrological modelling (e.g. [Yew Gan et al.](#page-36-0) [\(1997\)](#page-36-0); [Kirchner](#page-33-0) [\(2006\)](#page-33-0); [Beven et al.](#page-31-0) [\(2011\)](#page-31-0); [Kauffeldt et al.](#page-33-1) [\(2013\)](#page-33-1); [Huang and Bardossy](#page-33-2) (20  $\overline{) \cdot \overline{}}$ 

Multiple studies pointed out the importance of accounting for uncertainties in streamflow observations while conducting hydrological model calibration or evaluation (e.g. [McMillan et al.](#page-34-1) [\(2010\)](#page-34-1); [Coxon et al.](#page-31-7) [\(2015\)](#page-31-7); [Westerberg et al.](#page-36-2) [\(2020\)](#page-36-2)). These

- 110 studies developed and applied methodologies to determine quantified uncertainty estimates of streamflow observations (overview in [McMillan et al.](#page-34-6) [\(2012\)](#page-34-6)). Recently [Coxon et al.](#page-31-10) [\(2020\)](#page-31-10) released the first large-sample dataset that includes quantified streamflow observation uncertainty estimates: CAMELS-GB which describes 671 catchments in Great Britain of which 503 gauging stations contain quantified observed streamflow uncertainty information [\(Coxon et al., 2015\)](#page-31-7)large-samples of catchments allow for the evaluation of the robustness of model performance [\(Andréassian et al.](#page-30-10) [\(2006\)](#page-30-10); [Gupta et al.](#page-32-2) [\(2014\)](#page-32-2)). Identifying this 115 robustness provides model users with valuable information on the presence or absence of consistency in the model results.
	- In this study<del>we investigate the importance of accounting for streamflow observation uncertainty when conducting model</del> evaluation and comparison studies. This is done by using a workflow that assesses the validity of the differences between model simulations in light of observational uncertainty . The generic layout of the workflow allow for assessments that go beyond streamflow in hydrological modelling and is therefore we assess the effect of omitting discharge observation uncertainty
- 120 while interpreting model performance differences. Specifically, we focus on how this uncertainty influences model selection from the perspective of model users. Thereby, we highlight the importance of incorporating discharge observation uncertainty during model calibration and model evaluation efforts. To achieve this, we developed a generic method that is applicable for any field of geoscience geoscience field where model results are compared against observationswith known uncertainty. We extend the analyses by considering the effect temporal sampling of the simulation and observation time series has on the
- 125 objective functions used to determine model skill. The temporal sampling uncertainty of the time series, hereafter referred to as objective function sampling uncertainty, is the results of outliers in the squared error probability distribution between simulations and observations. [Clark et al.](#page-31-12) [\(2021\)](#page-31-12) identified this as another source of uncertainty that might lead to the wrong conclusions based on objective functions that capture streamflow performance as a few data points can heavily influence the results [\(Clark et al., 2021\)](#page-31-12).
- 130 Two model experiments are performed in this study using the CAMELS-GB dataset as the case study. The *intra-model* evaluation experiment includes the model simulations of distributed hydrological model wflow-sbm [\(van Verseveld et al., 2022\)](#page-36-4) with and without additional calibration. The *inter-model* comparison includesthe distributed hydrological model PCR-GLOBWB [\(Sutanudjaja et al., 2018\)](#page-36-5) and the additionally calibrated wflow\_sbm model. The selection of these two hydrological models is based on the differences in conceptualizations of hydrological processes and calibration routines while being comparable
- 135 to a certain degree as both are distributed hydrological models that are applicable at fine spatial scale  $(1km^2)$ to uncertain observations.

With this study, we outline an analysis procedure that assesses the different sources of uncertainties in the intra-/inter-model benchmarking experiments. Benchmarks are valuable for model evaluation to support interpretation of model performance in otherstudies[\(Seibert, 2001;](#page-35-3) [Schaefli and Gupta, 2007;](#page-35-4) [Pappenberger et al., 2015;](#page-35-5) [Seibert et al., 2018\)](#page-35-6). The inclusion of observation

- 140 and sampling uncertainty in the benchmark procedure not only provides a better indication of the relevance of the differences between benchmark results, but also helps detecting benchmark samples that should be treated with care or may need to be excluded from the benchmark. The analysesis implemented using the eWaterCycle platform [\(Hut et al., 2022\)](#page-33-6) to ensure reproducible model benchmark results. In doing so, the workflow of this study is generally applicable for other studies that want to account for streamflow observation uncertainty and sampling uncertainty. The workflow can be adopted for use in other
- 145 fields in geoscience that aim to use uncertainty estimates when comparing or evaluating models This method determines, based on the 5th to 95th percentile range of flow, if model simulation differences are significant in the context of discharge observation uncertainties. In this study, we highlight 3 use cases based on 8 hydrological models that encompass model refinement efforts, conventional model comparisons, and the influence of model structure uncertainty in light of discharge observation uncertainty. Furthermore, we assess the spatial consistency of model performance results using a large-sample catchment dataset and
- 150 we assess the temporal consistency of model performance metrics by sub-sampling the observation and simulation pairs as demonstrated by [Clark et al.](#page-31-12) [\(2021\)](#page-31-12). By doing so, more informed conclusions can be drawn on model performance based on individual catchments or large-samples of catchments.

#### 2 Methodology

The graphical workflow in Figure [1](#page-5-0)A generic tooling is designed for assessing model simulations while considering the 155 uncertainties inherent in evaluation data. First, the 3 use cases are presented, this is followed by the input data description, evaluation data description, and the discharge observation uncertainty estimates used to conduct the analyses. Next, we

<span id="page-5-0"></span>

Figure 1. Graphical workflow of model experiments and analyses. In with in green the model experiment inputs, in red the models, and in grey the <del>analyses</del> analysis components. Part A describes (a) the model run<del>, part B</del>-runs of two models with inputs and outputs that result in simulation time series. (b) the elassic conventional model comparison that compares objective functions <del>, based</del> on simulation and part E-observation time series. (c) the workflow for of the proposed analysis that compares relative model simulation differences to discharge observation uncertainty assessmentestimates.

describe the employed hydrological models and model runs for calibration and evaluation. The methodology concludes with the explanation of the uncertainty based analyses.

In Figure [1,](#page-5-0) a graphical workflow is presented that provides an overview of the components of the model experiments and 160 analyses described presented in the methodology. Figure [1a](#page-5-0) describes shows a typical model run with inputs and outputs, Figure [1b](#page-5-0) describes a classical shows a conventional comparison of objective functions based on (streamflow) discharge observations and simulations, and Figure [1c](#page-5-0) describes the additional uncertainty analyses uncertainty analysis introduced in this study.

## 2.1 Model Experiment InputsUse cases

#### 2.1.1 CAMELS-GB dataset

- 165 The We devised 3 use cases based on 8 hydrological models that exemplify how users of models, whom themselves are not the model developers, can interpret differences between model simulations in the context of discharge observation data uncertainty. The use cases are:
	- 1. Model refinement in practice: This use case concerns additional model refinement by fine tuning an effective model parameter based on discharge observation post initial calibration. It highlights the value of relative gains in model performance when not considering discharge observation uncertainty in the calibration process.
	- 2. Model comparison for model selection: Here, two distributed hydrological models are compared against the backdrop of uncertainties in discharge observations. This analysis aims to pinpoint scenarios where the disparities between model ✿✿✿✿✿ results are within the margin of error of the discharge observations.
	- 3. Model selection under model structural uncertainty: This use case involves contrasting the uncertainty inherent in the
- 175 model's structure, as seen across various hydrological models, with the uncertainty in discharge observations.

An additional analysis is performed that quantifies uncertainty in the model performance objective functions due to temporal sampling of the discharge simulation and observation pairs. This temporal sampling uncertainty is detailed in Section 2.5.3.

2.2 Data

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## 2.2.1 Case study and catchment selection procedure

- 180 The CAMELS-GB large-sample catchment dataset [\(Coxon et al., 2020;](#page-31-10) [Coxon, 2020\)](#page-31-13) serves as the case study area of the model experiment use cases and contains data (hydro-meteorological timeseriestime series, catchment boundaries and catchment attributes) describing 671 catchments located across Great Britain. The underlying data used to create CAMELS-GB are publicly available and are therefore suitable for evaluating and benchmarking hydrological models as the dataset can be easily extended in the future. A unique feature of the dataset is the availability of quantified streamflow discharge observation
- 185 uncertainty estimates for the flow percentiles of 503 catchments (see [Coxon et al.](#page-31-7) [\(2015\)](#page-31-7)). In this study we evaluated 396 of these 503 catchments

The use cases in this study employ hydrological models with a daily time step. This can cause temporal discretization errors in small catchments due to peak precipitation and peak discharge occurring at the same time step. Therefore, these catchments are excluded through a selection procedure. This procedure calculates the cross-correlation between observed discharge and

- 190 precipitation for a range of lag times. Catchments that predominantly show less than 1 day of lag between observed discharge and precipitation are excluded. Of the 503 catchments with uncertainty estimates, as these contained a complete range of the percentiles of quantified observation uncertainty estimatesrequired for the analyses in Section 2.4.3299 catchments are selected as the case study.
	- 2.2.2 Meteorological <del>Forcing f</del>orcing and Pre-Processingpre-processing
- 195 For consistency we In this study We use the same meteorological forcing that was used to create the CAMELS-GB meteorological timeseries time series and climate indices as input to the hydrological models. This input consists of gridded 1km<sup>2</sup> spatial- and daily temporal resolution <sup>2</sup> daily meteorological datasets. The meteorological variables used in this study are precipitation (CEH-GEAR; [Keller et al.](#page-33-7) [\(2015\)](#page-33-7); [Tanguy](#page-36-6) [\(2021\)](#page-36-6)), reference evaporation (CHESS-PE; [Robinson](#page-35-7) [\(2020a\)](#page-35-7)), and temperature (CHESSmet; [Robinson](#page-35-8) [\(2020b\)](#page-35-8)). Scripting used for pre-processing of the data is The distributed hydrological 200 models use gridded inputs and the conceptual hydrological models aggregated time series of meteorological variables that are
	- <u>readily</u> available in the <del>GitHub repository complementing this study: **paste link + DOI**CAMELS-GB dataset.</del>

## 2.2.3 Streamflow Observations Discharge observations and Quantified Uncertainty Estimates quantified uncertainty <u>estimates</u>

The streamflow discharge observations in the CAMELS-GB dataset were obtained from the UK National River Flow Archive 205 and are daily values in cubic meters per second  $(m<sup>3</sup>*s<sup>-1</sup>)$ . As is common with large-sample catchment datasets several catchments have contain missing flow data in the time series. These missing values are not taken into account in the analyses of this study.

A unique aspect of the CAMELS-GB dataset is the inclusion of quantified streamflow discharge observation uncertainty estimates created by <del>[Coxon et al.](#page-31-7) [\(2015\)](#page-31-7).</del> Coxon et al. (2015). The uncertainty is quantified by utilizing a large dataset of quality

210 assessed rating curves and stage-discharge measurements. In an iterative process, the mean and variance at each stage point is calculated and subsequently fitted using a LOWESS regression method that defines the rating curve and streamflow-discharge uncertainty. By combining the LOWESS curves and variance in a Gaussian Mixture model based on a random draw from the measurement error distribution an estimate of streamflow uncertainty is made, see [Coxon et al.](#page-31-7) [\(2015\)](#page-31-7) Coxon et al. (2015) for more information.

#### 215 2.3 Hydrological Models models

The model selection is in part based on legacy and availability of data [\(Addor and Melsen](#page-30-11) [\(2019\)](#page-30-11)) as well as based on the relevance of the model runs for use in other studies. Below we briefly describe the models . For detailed descriptions the reader is referred to [van Verseveld et al.](#page-36-4) [\(2022\)](#page-36-4) (wflow\_sbm)and [Sutanudjaja et al.](#page-36-5) [\(2018\)](#page-36-5) (A mixture of distributed physically process-based and lumped conceptual hydrological models is selected for the use cases, thereby showcasing the versatility of

220 the analysis. The model refinement and model comparison use cases employ two physically process-based hydrological models: wflow\_sbm [\(van Verseveld et al.](#page-36-4) [\(2022\)](#page-36-4)) and PCR-GLOBWB  $\angle$ Sutanudjaja et al. [\(2018\)](#page-36-5); [Hoch et al.](#page-32-4) [\(2023\)](#page-32-4)). The rationale behind selecting these models lies in their differing approaches to conceptualizing hydrological processes and their respective optimization routines. Despite these differences, both models are suitable for comparison to a certain degree. This comparability stems from their shared classification as distributed hydrological models, similar complexity, parameterization, and applicability

## 225 at a spatial resolution of 1 km.

For the model structure use case, 6 conceptual hydrological models are sourced from the Modular Assessment of Rainfall–Runoff Models Toolbox (MARRMoT: [Knoben et al.](#page-33-8) [\(2019\)](#page-33-8); [Trotter et al.](#page-36-7) [\(2022\)](#page-36-7)). These specific models are selected to encompass a

wide array of model structures. The selection is based on the number of model stores, the quantity of parameters, and differing process representations.

## 230 <mark>2.3.1 <del>wflow\_sbm</del>Distributed hydrological models</mark>

The wflow\_sbm <del>physically based p</del>hysically-based distributed hydrological model <del>[\(van Verseveld et al., 2022\)](#page-36-4) is based on</del> [\(van Verseveld et al.](#page-36-4) [\(2022\)](#page-36-4)) originated from the Topog\_SBM model concept <del>[\(Vertessy and Elsenbeer, 1999\)](#page-36-8)</del> [\(Vertessy and Elsenbeer](#page-36-8) [\(1999\)](#page-36-8) ). This concept was developed for small-scale hydrologic simulations. The wflow\_sbm model deviates from Topog\_SBM by

the addition of capillary rise, evapotranspiration and interception losses ([Gash](#page-32-5) model; Gash [\(1979\)](#page-32-5) Gash (1979)), a root water 235 uptake reduction function <del>[\(Feddes and Zaradny, 1978\)](#page-32-6)</del> [\(Feddes and Zaradny](#page-32-6) [\(1978\)](#page-32-6)), glacier and snow processes, and D8 river routing that uses the kinematic wave approximation <del>. The parameter sets in this study. The parameters (40 in total)</del> are derived from open-source datasets and use pedo-transfer functions to estimate soil properties (see hydroMT software package [\(Eilander and Boisgontier, 2022\)](#page-32-7). We use the [\(Eilander and Boisgontier](#page-32-7) [\(2022\)](#page-32-7)).

The 1 km<sup>2</sup> model version that <sup>2</sup> model version was aggregated from the finest available data scale (90 m). The hydraulic

- 240 parameters related to the river network are upscaled using the method presented in [Eilander et al.](#page-32-8) [\(2021\)](#page-32-8). The parameter upscaling of the wflow\_sbm model is based on the work by [Imhoff et al.](#page-33-9) [\(2020\)](#page-33-9) that uses point-scale (pedo)transfer-function. This method is similar to the multiscale parameter regionalization method [\(Samaniego et al.](#page-35-9) [\(2010\)](#page-35-9)). Parameters are aggregated from the original data resolution with upscaling operators determined by a constant mean and standard deviation across various scales. Fluxes and states are checked for consistency during this process. See van [van Verseveld et al.](#page-36-4) [\(2022\)](#page-36-4) for further
- $245$  information.

#### 2.3.2 PCR-GLOBWB

The PCR-GLOBWB physically based physically-based distributed hydrological model was initially developed for global hy-drology and water resources assessments <del>[\(Sutanudjaja et al., 2018\)](#page-36-5)</del><u>[\(Sutanudjaja et al.](#page-36-5) [\(2018\)](#page-36-5)</u>). The PCR-GLOBWB model calculates the water storage in two soil layers, one groundwater layer, and the exchange between the top layer and the atmosphere.

250 The model accounts for water use and return flow determined by water demand. We use employ the 1 km<sup>2</sup> version that is introduced in  $\left(\frac{2}{\sqrt{10}}\right)$  and  $\left(\frac{2023}{2}\right)$ . The model configuration in this study applies the accumulated travel time approximation for river routing.

#### 2.4 Model Experiments

We study the importance of accounting for streamflow observation uncertainty and objective function sampling uncertainty 255 using two model experiments. The first model experiment is an inter-model comparison of the streamflow estimates of the additionally calibrated wflow\_sbm and the PCR-GLOBWB hydrological and will test if the differnces in model formulations are siginficant in light of observation uncertainty. The second experiment is an intra-model evaluation based on the differences **Table 1.** Overview of the 6 selected conceptual hydrological models showing the model name, number of stores, number of parameters, and key references (adapted from [Knoben et al.](#page-33-10) [\(2020\)](#page-33-10)).



in estimated streamflow of the additional calibration and no-additional calibration of the wflow-sbm model. Hereafter respectively, calibrated and default wflow\_sbm.

## 260 2.3.1 Conceptual hydrological models

<u>MARRMoT is a flexible modelling framework that houses an array of conceptual hydrological models [Knoben et al.](#page-33-8) [\(2019\)](#page-33-8); [Trotter et al.](#page-36-7) (2</u> It is particularly valued in research for assessing model structure uncertainty, as highlighted in [Knoben et al.](#page-33-10) [\(2020\)](#page-33-10). One of the key advantages of MARRMoT is that the conceptual models share a uniform numerical implementation. To achieve this, alterations were made to the original model codes. These alterations ensure a consistent basis for model structure comparisons, 265 allowing for a precise evaluation of differences in hydrological simulations due to varying model structures. In this study, the hydrological models IHACRES, GR4J, VIC, XINANJIANG, HBV-96, and SMAR are selected. Table 1 provides an overview

of the number of stores, number of parameters, and key references.

#### 2.3.2 PCR-GLOBWB Model Run

Both the wflow sbm and PCR-GLOBWB hydrological models are setup such as they are typically used in other studies. 270 Therefore, the

## 2.4 Model runs

The model runs that form the basis of the 3 use cases are performed as intended by the model developers. Meaning, this study employs calibration and or optimization methodologies as recommended by the model developers for model users. The calibrated parameters for the distributed hydrological models were obtained from the model developers. In the case of the

275 . conceptual hydrological models we follow the model run configuration of [Knoben et al.](#page-33-10) [\(2020\)](#page-33-10).

## 2.4.1 PCR-GLOBWB model runs

The PCR-GLOBWB model does not require additional <del>calibration using streamflow observations r</del>egional parameter optimization after deriving the parameter set..., as this is typically not conducted by the model developers. However, this does not imply that the model would not benefit from additional optimization. The model does require an extensive a spin-up period to establish

280 semi steady-state conditions at the start of the model run. The model is spun-up 30 years back to back back-to-back using a single water year climatology that is based on the average values of each calendar-day between 1-10-2000 and 30-09-2007. The following water year 2008 is discarded from analyses to avoid <del>over fitting overfitting</del> at the start of the evaluation period and the model is evaluated for the water years  $2009 - 2015$ .

## 2.4.2 <del>Calibrated and </del>Default <u>and optimized</u> wflow\_sbm <del>Model Runsmodel</del> runs

- 285 The wflow\_sbm model is spun-up using the water year 2000 and additionally calibrated using streamflow discharge observations for the water years 2001-2007. Additional calibration is done perfomered by optimizing a single parameter using the Kling-Gupta Efficiency Non-Parametric (KGE-NP) objective function [\(Pool et al.](#page-35-12) [\(2018\)](#page-35-12)) based on <del>streamflow discharge</del> observations and simulations differences at the catchment outlet<del>resulting .</del> This results in a single *ealibrated parameter set*.  ${\sf Imhoff}$  et al. [\(2020\)](#page-33-9) identified the KsatHorFrac parameter  ${\rm optimized}$  parameter set per catchment. [Imhoff et al.](#page-33-9) (2020) identified
- 290 optimization <u>the horizontal conductivity fraction parameter (KsatHorFrac)</u> as effective for single parameter value <del>per catchment calibration</del>optimization. KsatHorFrac is an amplification factor of the vertical saturated conductivity that controls the lateral flow in the subsurface. The

After calibration, the water year 2008 is discarded from analyses and the model is evaluated for the water years 2009 - 2015. For more information on the effects of calibration, the reader is referred to <del>[Aerts et al.](#page-30-12) [\(2022\)](#page-30-12)</del>Aerts et al. (2022), Section 3.1 295 and Figure 3.

The default wflow sbm model run sets the KsatHorFrac parameter value to the default value of 100. An overview of the model run periods is provided in Table 1. The calibration results of the wflow\_sbm model are presented in Appendix A1. Overview of the model run periods and spin-up years.

## 2.4.3 Conceptual hydrological model runs

- 300 Similar to the other model runs, the conceptual hydrological model runs are spun-up using the water year 2000 and calibrated using the water years 2001-2007. The calibration method uses the Coviariance Matrix Adaptation Evolution Strategy (CMA-ES; [Hansen et al.](#page-32-9) [\(2003\)](#page-32-9); [Hansen](#page-32-10) [\(2006\)](#page-32-10); [Hansen and Ostermeier](#page-32-11) [\(2001\)](#page-32-11)). This method optimizes a single-objective function to find global parameter optimums based on non-separable data problems. A demonstration of the sensitivity of the calibration parameters is shown in [Knoben et al.](#page-33-10) [\(2020\)](#page-33-10). Following calibration based on the KGE-NP objective function, the water year
- 305 2008 is discarded and the models are evaluated based on the water years 2009-2015 using the same KGE-NP objective function.

#### 2.4.4 eWaterCycle

This study is conducted using the eWaterCycle platform [\(Hut et al., 2022\)](#page-33-6). eWaterCycle is a community driven platform for the running of hydrological model experiments. All components that are required to run hydrological models are FAIR by design

310 [\(Wilkinson et al., 2018\)](#page-36-11). This is achieved by versioning models and datasets and creating workflows that are reproducible. Therefore, the platform is suitable for conducting **benchmark** model performance experiments. The model simulations were conducted on the Dutch supercomputer Snellius to ensure faster model run time. We created example notebooks that use the eWatercycle platform on cloud computing infrastructure<del>(paste link + DOI).</del>: https://doi.org/10.5281/zenodo.7956488.

#### 2.5 Analyses

## 315 2.5.1 Model <mark>Evaluation</mark>evaluation

The hydrological model results runs (calibration and evaluation) are evaluated using the Kling-Gupta efficiency non-parametric (KGE-NP, [Pool et al.](#page-35-12) [\(2018\)](#page-35-12)) objective function. This efficiency metric deviates from the more commonly used Kling-Gupta efficiency (KGE, [Gupta et al.](#page-32-12) [\(2009\)](#page-32-12)) by instead of calculating the Pearson correlation and variability bias calculating the calculating the Spearman rank correlation and the normalized-flow-duration curve instead of the Pearson correlation and ability bias. Values range from  $-\infty$  to 1 (perfect score). In addition to the KGE-NP metric, we consider the Nash-Sutcliffe efficiency (NSE, [Nash and Sutcliffe](#page-35-13) [\(1970\)](#page-35-13)) to demonstrate the sensitivity of the results towards the selection of objective function. We include the KGE-NP, KGE, modified KGE [\(Kling et al.](#page-33-12) [\(2012\)](#page-33-12)), and the NSE objective functions in the data repository for completeness and future reference.

## 2.5.2 Objective Function Sampling UncertaintyDischarge observation uncertainty

- 325 The objective function sampling uncertainty is introduced because time series are not infinetly long and might contain outliers. These show up in the tails of the probability distribution of the squared errors between model simulations and observations. The practical implementation is that a few data points in the time series can have a very large influence on the calculated objective function value. To quantify the sampling uncertainty of the KGE-NP and NSE objective functions we applied the methodology of [Clark et al.](#page-31-12) [\(2021\)](#page-31-12). This method combines bootstrap [\(Efron, 1979\)](#page-32-13) and jacknife-after-bootstrap [\(Efron and Tibshirani, 1986\)](#page-32-14)
- 330 methods to calculate the standard error and the tolerance interval of the objective function sampling uncertainty. We extended the GUMBOOT package [\(Clark et al., 2021\)](#page-31-12) by adding the KGE-NP metric. The analysis of the objective function sampling uncertainty is based on the tolerance interval (95th - 5th percentiles) of the jackknife and bootstrap methods. The tolerance intervals of the models corresponding to each model experiment are averaged for each catchment and referred to as sampling uncertainty.

#### 335 2.5.3 Streamflow Observation Uncertainty

The results are analyzed based on three flow categories, ad hoc discharge observation uncertainty based analysis of model performance differences consists of 3 parts. The first part divides the observation and simulation pairs into 3 flow categories similar to [Coxon et al.](#page-31-7) [\(2015\)](#page-31-7), namely low flow, average flow, and high flow conditions. Low flow The low flow category is based on the values observed discharge values at the catchment outlet between the 5th and 25th percentilespercentile range,

- 340 average flow on the 25th and to 75th percentilespercentile range, and high flow on the 75th and to 95th percentiles of observed streamflow at the catchment outlet (Table 2) percentile range. Not all percentiles are included for the low and high flow categories due to limited data availability on quantified <del>streamflow discharge</del> observation uncertainty. <del>Following the creation of</del> flow categories based on the percentiles of observed flow, the simulated streamflow results are divided into flow categories by matching the time steps (dates).
- 345 Overview of flow categories and flow percentile ranges. Flow Category Low Flow O5p O25p Average Flow O25p O75p High Flow Q75p - Q95p

Next, the method In the second part, illustrated in Figure [1C](#page-5-0) is applied to each flow category, catchment, and objective function. First c<sub>2</sub> the absolute difference of the between model simulations is calculated as shown in the example for each flow category and each catchment. This is exemplified in the form of a hydrograph in Figure 2<del>A. The quantified streamflow</del>

- 350 a. The discharge observation uncertainty estimates of the CAMELS-GB dataset contain are processed by averaging the upper and lower bounds <del>per</del> of uncertainty estimates per flow percentile (5, 25, 75, 95). <del>First the percentile boundaries of each flow</del> eategory are averaged (e.g. 5th and 25th percentiles for the low flow category) resulting This results in the orange and red dashed lines in Figure [2B](#page-13-0). Next, the average of upper and lower bounds are taken and multiplied by the observations to create the quantified streamflow observation estimate b. We then take the percentage of discharge observations basd on the average
- 355 uncertainty estimates to convert the uncertainty percentages to discharge observation uncertainty time series in  $m3/s$ ,  $m3/s$ , (green line). These bounds differ in values  $(e.g., +20\%)$  and  $-15\%)$  as the uncertainty distributions are not symmetrical.

<del>A The third part applies a dependent</del> t-test <del>is performed</del> using the time series in Figure [2C](#page-13-0)  $_c$  with a 0.05 significance level to determine if the observation uncertainty time series is greater than the model simulation difference <del>. When this is the case it is</del> not possible to be conclusive on which modelis best performing. time series.

360 This method is subject to certain limitations, particularly regarding the use of the discharge observation uncertainty estimates. Due to absence of data the upper and lower 5th percentiles of flow could not be included while these data points can be most important for users to determine fit-for-purpose of a model. In addition, it is preferred to use the rating curve uncertainty rather than the uncertainty bounds of flow percentiles. We accept these limitations as we promote the use of existing dataset to ensure community participation into implementing the suggested evaluation procedure in other studies.

#### 365 3 Results

Firstly, we present an overview of streamflow simulation based model performance captured by the

## 2.0.1 Temporal sampling uncertainty

<span id="page-13-0"></span>

Figure 2. Example hydrographs of the streamflow discharge observation uncertainty analysis method. (Aa) Calculation calculation of the absolute difference (blue) between model simulations (red and orange). (<del>B</del>b) Calculation calculation of streamflow observation uncertainty in  $m3/$ s  $m3*$ s<sup>-1</sup> (green). Dashed lines indicating upper and lower bounds expressed as percentages of observation uncertainty that are averaged and multiplied with the observations (black). (Vc) Resulting resulting time series, with, in blue, the absolute difference between model simulations and, in green, the averaged discharge observation uncertainty in  $\frac{m3}{\text{sg}}^3$ ;  $\frac{1}{\text{sg}}$ .

Another aspect of model performance evaluations that might misinform model users is the sensitivity of objective functions to the temporal sampling of time series. Temporal sampling uncertainty determines if the error distribution of simulation and 370 observation pairs is heavily skewed. A few data pairs might have a disproportionate effect on the calculated objective functions

that are used to determine model performance. The inclusion or exclusion of these data points due to the selection of the calibration and evaluation period, hence alters the consistency of model performance over time.

To quantify the temporal sampling uncertainty of the KGE-NP and NSE objective functions at the catchment outlets. Secondly, we show the distributions of the objective function difference and the objective function sampling uncertainty.

375 Thirdly, we show for each flow category the percentage of days that the observation uncertainty is greater than the differences

between model simulations. A t-test determines if the model simulation difference time series are significantly greater than the observation uncertainty time series .

The calibration results of the wflow sbm model and the spatially distributed results of the differences in objective function for each model experiment are available in Appendix A1. Appendix A2 contains objective function, we applied the methodology of

380 [Clark et al.](#page-31-12) [\(2021\)](#page-31-12). This method sub-samples the simulation and observation time series through bootstrapping and [\(Efron, 1979\)](#page-32-13) and jacknife-after-bootstrap [\(Efron and Tibshirani, 1986\)](#page-32-14) methods. The change in objective function due to the shuffling of the sub-samples allows for the calculation of the standard error and its tolerance interval. The tolerance intervals corresponding to each model instance are averaged and referred to as temporal sampling uncertainty. We extended the GUMBOOT software package [Clark et al.](#page-31-12) [\(2021\)](#page-31-12) by adding the KGE-NP metric for this study.

#### 385 **3 Results**

In this section we first present an overview of the <u>discharge-based model</u> performance results for each of the 3 use cases. Next, we detail the spatial distributions of the GUMBOOT (sampling uncertainty) resultsfor each objective function. Appendix A3 contains the spatially distributed maximum model performance difference. This is succeeded by the presentation of uncertainty estimates for discharge observations, categorized by flow. Subsequently, the discharge observation uncertainty based analyses

aso of relative model performance is presented. The section ends with the temporal sampling uncertainty analysis results. Appendix A.1 contains the calibration results of the streamflow observation uncertainty analyses. wflow\_sbm model and Appendix A.2 the Nash-Sutcliffe efficiency (NSE) based model performance results of all considered models.

#### 3.1 Streamflow Based Model Performance

The model performance results are based on the streamflow estimates and streamflow observations at 396 catchment outletsand 395 are shown as cumulative distributions functions in Figure [3.](#page-15-0) In general the results show, to a certain degree, comparable skill in capturing observed streamflow by both hydrological models. Note, that the different objective functions in Figures [3a](#page-15-0)b are not directly comparable (Knoben et al., 2019).

The inter-model comparison experiment results of the calibrated wflow sbm & PCR-GLOBWB models show a large difference between the

## 400 3.1 Discharge based model performance

Model performance is assessed using discharge observation and simulations at 299 catchment outlets. The results are shown in Figure 3 as Cumulative Distribution Functions (CDFs) of the KGE-NP <del>distributions of the models above a KGE-NP of 0.25</del> (objective function. These results offer insight into the model's accuracy in simulating observed discharge.

The CDF of the model refinement use case in Figure [3a](#page-15-0) <del>). The KGE-NP median of the calibrated</del> establishes that optimizing 405 a single effective parameter leads to an improvement for approximately 65% of the catchments. The improvements remain modest as indicated by the median value of 0.64 KGE-NP for the default wflow\_sbm is 0.77 compared to a median value of

<span id="page-15-0"></span>

**Figure 3.** Cumulative distribution function (CDF) plots of the Kling-Gupta Efficiency non-parametric (KGE-NP) objective function, derived from discharge estimates and observations at 299 catchment outlets. (a) shows the CDF for the model refinement use case, optimizing the wflow\_sbm\_hydrological\_model\_with\_a\_single\_parameter. (b)\_shows\_the\_CDF\_for\_the\_model\_comparison\_use\_case,\_comparing\_the\_optimized wflow\_sbm and PCR-GLOBWB hydrological models. (c) demonstrates the CDF for the model structure use case, showcasing results from ✿ 6✿✿✿✿✿✿✿✿ conceptual✿✿✿✿✿✿✿✿✿✿ hydrological ✿✿✿✿✿✿ models.

0.43 for PCR-GLOBWB. Larger differences between distributions and, in general, lower values are found based on the NSE metric model and 0.74 KGE-NP for the optimized wflow\_sbm model. Larger model performance differences are found for the model comparison use case in Figure [3b](#page-15-0). <del>The large differences are in part due to the additional calibration of the Here</del>,

- 410 the optimized wflow\_sbm model <del>. Another contributing factor is expected to be the difference in river routing, kinematic</del> wave used by wflow\_sbm and simple accumulation travel time by performs better in 75% of the catchments than the PCR-GLOBWB <del>. The differences between objective functions can be explained by the model. Both models demonstrate poor results</del> for approximately 25% of the evaluated catchments (<0.40 KGE-NP<del>function focusing more on the baseflow component while</del> the NSE objective function focuses more on average and peak flow).
- 415 The inter-model evaluation experiment results capture the effect of additional calibration of the wflow sbm model is shown by the default and calibrated wflow sbm model distributions with median values of 0.65 and 0.77 respectively. The added value of calibration is less pronounced for the NSE results in Figure [3b](#page-15-0) as the model calibration routine only optimizes for the KGE-NP objective function. Here, the median values are lower at 0.25 for the default and 0.50 for the calibrated wflow\_sbm-results of the model structure use case are based on 6 conceptual hydrological models that only deviate in model
- 420 structure (Figure [3c](#page-15-0)). From the spread in model results it is evident that the VIC model lags behind in performance compared to the other models. The IHACRES and SMAR models yield very similar results despite large structural differences. The XINANJIANG and HBV-96 models not only produce comparable outcomes but also share a more similar model structure. The GR4J model consistently outperforms the other models. The <del>differences between distributions of each objective function</del> establishes the importance of reporting multiple performance metrics. Overall, total model structure uncertainty, as expressed
- 425 by the difference between the <del>differences are larger for the inter-model comparison experiment, smaller for the intra-model</del>

<span id="page-16-0"></span>

Fi<mark>gure 4. <del>Cumulative</del> Spatial</mark> distribution <del>function of the absolute Kling-Gupt</del>a Efficiency non-parametric (<del>CDFKGE-NP</del>) <del>plots of </del>objective functions based on streamflow estimate and observation at function difference between the worst and best model's performance per catchment outletand use case. With in blue (a) shows the additionally calibrated model refinement use case based on the default and optimized wflow\_sbm hydrological models. (b) shows the model <del>, in orange</del> comparison results based on the <del>default</del> optimized wflow\_sbm <del>model, a</del>nd in green the PCR-GLOBWB modelhydrological models. (Ac) <del>The Kling-Gupta Efficiency non-parametric (KGE-NP) objective function. (B</del>) The Nash Sutcliffe Efficiency (NSE) objective function. The shows the model structure use case results show closer agreement for objective function values based on the worst and best model performances of the intra-model evaluation than the inter-model comparison6 conceptual hydrological models.

evaluation experiment, and more pronounced for the NSE than the worst and best performing model's CDF is substantial, while the differences between models can be subtle. Median KGE-NP objective function values for the models are as follows: VIC at ✿✿✿✿ 0.65,✿✿✿✿✿✿✿✿✿ IHACRES✿✿ at✿✿✿✿ 0.80,✿✿✿✿✿✿✿ SMAR ✿✿ at ✿✿✿✿ 0.82,✿✿✿✿✿✿✿✿✿✿✿✿✿ XINANJIANG ✿✿ at ✿✿✿✿ 0.84,✿✿✿✿✿✿✿ HBV-96✿✿ at✿✿✿✿✿ 0.85, ✿✿✿ and✿✿✿✿✿ GR4J✿✿ at✿✿✿✿ 0.88✿✿✿✿✿✿✿✿ KGE-NP.

#### 3.2 Objective Function Sampling Uncertainty

430 The distributions of the objective function difference and the sampling uncertainty of each model experiment are shown in Figure ??. The objective function difference distribution shows alarger spread in values for the inter-model comparison (Next, we consider the spatial distribution of the results, presented in Figure [4,](#page-16-0) based on the maximum KGE-NP difference between the models of each use case. Improvements after model refinement are indicated by the positive KGE-NP median of 0.48) than for the intra-model evaluation (KGE-NP median of 0.07). This is to lesser extent the case for the sampling uncertainty

- 435 distributions. Both model experiments show higher values for objective function difference and sampling uncertainty of the NSE than the KGE-NP objective function. This establishes a strong sensitivity of results towards objective function selection. For both objective functions very large values of difference values in Figure [4a](#page-16-0). These values are mainly present in the Northern and Southern parts of Great Britain. No clear spatial patterns are visible for the model comparison use case in Figure [4b](#page-16-0), demonstrating high spatial variability in performance when comparing the wflow\_sbm and PCR-GLOBWB distributed
- 440 hydrological models. More spatially consistent differences are found for the model structure use case in Figure [4c](#page-16-0). Here, the <u>largest</u> differences are present in the <del>negative domain. The relevance of which is debatable as for example Knoben et al. (2018)</del> pointed out that a KGE value of -0.42 and NSE of 0 corresponds to taking the mean of the observationsNorthern and Southern parts of Great Britain.

(A) Box-plot of the objective function difference between the inter-model comparison models (wflow\_sbm calibrated and 445 PCR-GLOBWB) and the intra-model evaluation models (wflow sbm calibrated and default). (B) Box-plot of the sampling uncertainty (average tolerance interval) of both model experiments. The KGE-NP objective function is shown in red and the NSE objective function in blue.

Next, the catchment simulations that contain greater sampling uncertainty than the difference in objective functions are identified (Table ??). Of the 398 catchment simulations under consideration this is the case for 53 catchments based on the

- 450 KGE-NP objective function and 86 catchments based on the NSE objective function of the inter-model comparison. The intra-model evaluation contains more cases as the objective function differences are lower while the sampling uncertainty is similar. This results in 210 catchment simulations that contain greater sampling uncertainty than objective function differences for the KGE-NP objective function and 288 catchments for the NSE objective function. These results demonstrate that in many catchments data points in the tails of the probability distribution of the squared errors between model simulations and
- 455 observations heavily influence the objective function

## 3.2 Discharge observation uncertainty estimates

The discharge observation uncertainty estimates consider the 5th to 95th percentile range of flow. These estimates are categorized into 3 flow conditions and are presented in Figure 5. In the box plot for low flow category, we observe a wide interquartile range, shown by the spread of the box. This indicates a higher variability in discharge observation uncertainty percentages. The

- 460 median value, represented by the line within the box, is at the 20% uncertainty mark. The presence of many outliers above the box indicate occasional large deviations from the median value. For the average flow category, the range of values is narrower than for the low flow category with a median value of 15%. The lowest median value is found for the high flow category at 12%. It is difficult to determine whether the objective function differences are the result of modelling differences or mainly due to sampling. Therefore further research is required that determines the validity of these data points that heavily influence
- the objective function before drawing conclusions on model performance important to mention that the uncertainty is expected to be considerably higher if the underlying data would contain the upper 5th percentiles of flow for this category.

The spatial distribution of the sampling uncertainty results in Figure ?? show clusters of high sampling uncertainty for all model experiments and objective functions in the South of Great-Britain



Figure 5. Number Discharge observation uncertainty estimates of 299 catchment simulations outlets based on the work of [Coxon et al.](#page-31-7) [\(2015\)](#page-31-7) expressed as uncertainty percentages per model experiment and objective function for which sampling flow category. (a) shows the low flow category uncertainty estimates based on the 5th to 25th flow percentiles. (b) presents the 25th to 75th percentile average tolerance intervalflow category. (c) i<del>s larger than s</del>hows the <del>difference in objective function</del>high flow discharge observation uncertainty estimates of the 75th to 95th flow percentiles. 398 catchment simulations are considered.

#### 3.3 Use Cases

- 470 The discharge simulation difference time series of two models is expressed in cubic meters per second and compared to discharge observation uncertainty time series in cubic meters per second. This is <del>most likely due to</del> done by using a t-test to determine if the simulation differences are larger than the discharge observation uncertainty estimates. The instances where this is the <del>presence of chalk geology that is known to cause difficulties for estimating streamflow using hydrological models. The</del> inter-model comparison results in Figures ??ab show that there is agreement on where high sampling uncertainty (>0.4) occurs.
- 475 This is more so the case for the NSE- than the KGE-NP objective function. The intra-model evaluation experiment results in Figures ??CD show more agreement on occurrences than the inter-model comparison. These results show only clusters of objective function differences greater than sampling uncertainty in the West and North of Great-Britain. case are reported in Table 2 for the 3 use cases.

## 3.3.1 <u>Model refinement</u>

480 The model refinement use case results in Table [2](#page-19-0) show that approximately one third of the considered catchments contain instances of simulation differences between the wflow\_sbm default and wflow\_sbm optimized models that are statistically smaller than the discharge observation uncertainty estimates. This demonstrates the importance of incorporating (discharge) observation uncertainty when performing model refinement, especially when based on a large-sample catchment dataset. This consideration should be part of the calibration and subsequent evaluation process. In addition, more catchments contain very

<span id="page-19-0"></span>**Table 2.** Overview of the number of instances per flow category were discharge observation uncertainty exceeds the simulation differences based on 299 catchments. Results are based on dependent t-test's with a significance level of 0.05.



485 high sampling uncertainty  $(>0.4)$  indicating that the averaging of the tolerance interval reduces the sampling uncertainty more for the inter-model comparisonthe results indicate that when discharge observation uncertainty is not considered, it is difficult to draw conclusions on whether the model performs better after refinement. Overall, the results affirm the importance of incorporating discharge observation uncertainty in the optimization routine of wflow\_sbm model.

Spatial distribution of the sampling uncertainty analyses results showing the average tolerance interval of sampling uncertainty 490 per objective function from white to dark red. Red circles indicate sampling uncertainty larger than objective function difference and green circles indicate sampling uncertainty smaller than objective function difference. (A) Inter-model comparison experiment (wflow\_sbm and PCR-GLOBWB) KGE-NP objective function. (B) Inter-model comparison experiment NSE objective function. (C) intra-model evaluation experiment (wflow\_sbm calibrated and default) KGE-NP objective function. (D) intra-model evaluation experiment NSE objective function.

#### 495 3.4 Streamflow Observation Uncertainty

The observation uncertainty percentages per flow category and the percentage of days that the observation uncertainty is greater than the model simulation differences (see Figure [2c](#page-13-0)) are shown in Figure ??. The observation uncertainty percentages in Figure ??A indicate high percentages of uncertainty throughout the case study area with median values of 19.85 (low flow), 15.52 (average flow), and 12.18 (high flow ). All flow categoriescontain outliers of more than 50 %

## 500 3.3.1 <u>Model comparison</u>

For the model comparison use case (Table [2\)](#page-19-0), there is a lower frequency of instances where discharge observation uncertainty surpasses differences in discharge simulations. The comparison between the optimized wflow\_sbm model and the PCR-GLOBWB model reveals that in 5 catchments for low flow, 4 for average flow, and 3 for high flow categories, simulation differences exceed discharge uncertainty estimates. These findings suggest that the interpretation of model performance is not significantly

505 affected by the ad-hoc addition of discharge observation uncertainty. Of interest is that the uncertainty percentages are highest for the However, catchments demonstrating the impact of observation uncertainty warrant carefull examination.

## 3.3.2 <u>Model structure</u>

The analysis of model structure uncertainty in the context of discharge observation uncertainty reveals that only a single instance of the low flow category while the agreement between model simulations is highest for this flow category. This is

- 510 shown by the lower percentages of days that the observation uncertaintyis greater than the simulation differences between models in Figure ??b. In addition, smaller simulation differences (intra-model comparison) result in more percentages of days of observation uncertainty values surpassing simulation difference values. contains discharge observation uncertainty that exceed the simulation difference between all 6 conceptual hydrological models (Table [2\)](#page-19-0). This establishes that based on the selected models the model structure uncertainty, expressed as the difference in discharge simulations, is larger than
- 515 the discharge observation uncertainty estimates for this dataset. However, the investigation into the differences between the individual models yields several insights based on the results in Figure [6.](#page-21-0)

The VIC model results, characterized by its relatively lower performance, contain only a few instances where discharge observation uncertainty exceeds simulation differences, making it identifiable as the lesser performing model. In contrast, the IHACRES and SMAR models exhibit a high level of simulation agreement, demonstrated by a large number of instances in

520 Figure [6c](#page-21-0). This, despite significant differences in their complexity and structural design. Namely, IHACRES is a single store hydrological model and SMAR is a 6 store hydrological model that accounts for soil moisture in a separate store. This alignment of simulation results between models with varying complexities highlights the nuanced influence of structural differences on simulation outcomes. The HBV-96 and XINANJIANG models that most closely resemble each other based on the number of stores, process descriptions, and parameters contain low number of instance, allowing the identification of the better performing model. 525

Next, we applied a t-test to determine in which catchments the observation uncertainty is statistically larger than the differences between simulations for each flow category and experiment (Table ??) . For the inter-model comparison experiment we find that this is the case for 6 catchments of the low flow, 4 catchments of examine the results across the individual flow categories. The low flow category (Figure [6a](#page-21-0)) and the average flow category (Figure [6b](#page-21-0)) show similar trends, though with

530 a lower number of instances for the average flow <del>, and 3 catchments of the category with a lower number of instances for</del> the average flow category. The high flow category (Figure [6c](#page-21-0)) is characterized by a more frequent occurrence of discharge observation uncertainty surpassing simulation differences. This is especially evident between the IHACRES and SMAR

<span id="page-21-0"></span>(A) Distributions of observation uncertainty percentages per flow category of 398 catchments. (B) The percentage of days that the streamflow observation uncertainty is larger than the difference in streamflow simulation per flow category of 398 catchments. With in red the inter-model experiment (calibrated wflow\_sbm and PCR-GLOBWB) and in blue the intra-model evaluation experiment (calibrated and



**Figure 6.** Heat map of the 6 conceptual hydrological models showing for each model combination the number of instances (n=299) that discharge observation uncertainty exceeds simulation differences. (a) number of instances for the low flow category, with in white low values and in red high values. (b) number of instances for the average flow category. (c) number of instances for the high flow category.

models. The variability in structural design and parameterization among different hydrological models leads to notable differences in their outputs, underscoring the importance of selecting the appropriate model by including discharge observation uncertainty

535 in the calibration and evaluation process.

## 3.4 Lemporal sampling uncertainty

✿✿✿ The temporal sampling uncertainty of the KGE-NP objective function is defined as the tolerance interval of the standard error of the objective function due to sub-sampling of the simulation and observation pairs. This analysis provides insights into the temporal reliability and interpretability of hydrological model performances. Analysis of results from the 6 conceptual

540 hydrological models, as shown in Figure [7b](#page-23-0), reveals a pattern consistent with the model performance depicted in Figure [3c](#page-15-0). Specifically, the VIC model displays the highest KGE-NP uncertainty across all catchments, indicating its variability and the challenges in using this model current setup for accurate predictions in different hydrological contexts.

✿✿✿ The IHACRES and SMAR models, along with GR4J, XINANJIANG, and HBV-96, show similar levels of KGE-uncertainty. This consistency across models with varying complexities suggests that KGE-NP uncertainty is influenced not only by the

- 545 model design but also by hydrological conditions and data quality. Uncertainty values range widely, from about 0.1 KGE-NP to over 0.6, indicating significant variability in temporal robustness of results (Figure [7b](#page-23-0)).
	- When comparing the average KGE-NP objective function uncertainty with the KGE-NP differences between individual models, it becomes clear that uncertainty often overshadows the differences between models. These are low values but can potentially influence system scale conclusions. After exclusion of these catchments we can conclude that the model comparison
- 550 is not heavily influenced by the observation uncertainty . The smaller differences between simulation in the intra-model experiment result in many catchment simulations for which additional calibration does not significantly lead to improvements of streamflow estimates in light of observation uncertainty. This is particularly the case in comparisons between GR4J HBV-96, XINANJIANG - HBV-96, and SMAR - IHACRES. These findings imply that the inherent uncertainty in the ease for 116 of the low flow, 114 of the average flow, and 138 catchments of the high flow category. The differences in simulations are 555 more substantial for the inter-model comparison as only a few catchments per flow category are smaller than the observation uncertainty. objective functions may limit the ability to distinguish between model performances, complicating efforts to identify the most fit-for-purpose model based on this metric alone. This underscores the need for a more nuanced approach to model evaluation that considers not only objective function metrics but also other contextual factors and additional performance

measures, ensuring more robust and reliable model selection processes.

#### 560 4 Discussion

This study We introduced an ad hoc method that highlights the importance of taking into account streamflow observation uncertainty and objective function sampling uncertainty when evaluating or comparing including discharge observation uncertainty when evaluating hydrological models. Discharge observation uncertainty is frequently overlooked by model users, leading

<span id="page-23-0"></span>

Figure 7. Result (a) Temporal objective function sampling uncertainty based on 6 conceptual hydrological models expressed as the average tolerance interval of t-test with an statistical significance level of 0.05 determining if the observation standard error due to sub-sampling. With on the horizontal axis the sorted values per catchment and on the vertical axis the KGE-NP objective function uncertainty time series is larger than<sub>t</sub>. (b) Heat map of the simulation time series 6 conceptual hydrological models showing for each f<del>low category and</del> model experiment combination the number of instances (n=299) that the average objective function uncertainty exceeds the objective functions differences of model combinations. 398 catchments are considered With in white low values and in red high values indicating the number of ✿✿✿✿✿✿✿ instances.

to potential misinterpretations of relative model performance. Our findings emphasize the significant impact of discharge observation uncertainty on model performance interpretation. 565

We acknowledge that these are observation uncertainty is not the only sources source of uncertainty as there is uncertainty are uncertainties in model inputs, model structure, parameter sets, and initial or boundary conditions <del>, and more (e.g. Renard</del> et al. (2010); Dobler et al. (2012); Hatterman et al. (2018); Moges et al. (2021)). An uncertainty assessment of the complete modelling chain is necessary to determine the validity of model results. e.g. [Renard et al.](#page-35-14) [\(2010\)](#page-35-14); [Dobler et al.](#page-32-15) [\(2012\)](#page-32-15); [Hattermann et al.](#page-32-16) (20

570 ). Therefore the proposed generic tooling does not replace a full uncertainty analysis of modelling chains that also accounts for the impact of input uncertainties [\(Beven and Freer](#page-30-6) [\(2001\)](#page-30-6); [Pappenberger and Beven](#page-35-1) [\(2006\)](#page-30-4); [Beven](#page-30-4) (2006)). It rather assists model users with interpreting relative model performance and highlights the importance of conducting a full uncertainty analysis. Our study therefore only constitutes just a fraction of a broader challenge, in which input uncertainty plays a substantial role as has been demonstrated in [Bárdossy and Anwar](#page-31-5) [\(2023\)](#page-31-5).

#### 575 4.1 From sampling uncertainty to certainty

The objective function sampling uncertainty assessed in Section 3.2 is the result of outliers in the probability distribution of the squared errors between model simulations and observations. High values of sampling uncertainty indicate that certain data points have an exceptionally large effect on the objective function. It is therefore important to investigate the validity of these data points as measurement error or model error might misconstrue the actual model performance

## 580 4.1 Performance interpretation under discharge observation uncertainty

<u>Our analysis demonstrates that regionally optimizing the wflow\_sbm hydrological model often results in only marginal improvements</u> in model performance (Figure [3a](#page-15-0)). Although any improvement is beneficial, the findings suggest that discerning the superior model variant becomes challenging without factoring in the uncertainty of discharge observations during the calibration process. This is evident in 98 instances for low and average categories of flow and in 118 instances of the high flow category

- 585 (Table [2\)](#page-19-0). The number of instances is expected to further increase when including flows of the lower and upper 5th percentiles of flow are included. The adoption of an ad hoc measure, as introduced in this study, provides a practical though limited method for improving the interpretability of relative model results. For example, the spatial distribution of the results showed agreement on high sampling uncertainty clustered in the South of Great-Britain. This region contains the karst (chalk)geology that is known to be difficult to model correctly (Hartmann et al., 2018). Further inspection of the streamflow observations at the
- 590 catchment outlets did not show unexpected outliers that might indicate measurement error. It is therefore likely that differences between observations and simulations are large and inconsistent and might not only be influenced by how the time series are sampled. Through the detailed inspection of the time series we can deem with a higher degree of certainty that the results are not unjustly influenced by sampling. Therefore, we recommend the integration of discharge observation uncertainty into both the model calibration and evaluation procedures, aligning with the consensus in literature.
- 595 In addition, we compared the distributions of the sampling uncertainty results of each model run and objective function in Appendix A2 to those presented for the VIC model using the large-sample CAMELS-US dataset by [Clark et al.](#page-31-12) [\(2021\)](#page-31-12). The distributions of this study are similar for each model experiment and objective function and of similar magnitude to those of [Clark et al.](#page-31-12) [\(2021\)](#page-31-12). Therefore, When comparing different hydrological models, we find that the same conclusion is valid for both studies in that care should be taken before drawing conclusions at the system scale. This is especially the case for the 600 identified catchments in this study that contain sampling uncertainty values greater than the difference in objective functions
	- between two model simulations.

#### 4.2 Why we should take into account observation uncertainty-

The results of this study demonstrate that (streamflow) observation uncertaintyis important to consider when comparing or evaluating hydrological models. If the difference between model simulations is within the uncertainty bounds of the observation

- 605 uncertainty it is not possible to draw conclusions on best performing model simulations. The intra-model experiment shows that smaller differencesbetween modelssuch as changes made to model structure, inputs, or parameterization and calibration result in more of these occurrences. This is the case for 123 catchments based on the average of all flow categories. This does not mean that the incremental improvements to the model structure are not important, but it does show that they might not be as relevant as expected in light of uncertainty of discharge observations slightly masks the differences in relative model performance as
- 610 shown by the 3 to 5 instances per flow category in Figure [3b](#page-15-0) and Table [2.](#page-19-0) Similarly to the model comparison use case, the model

structure use case indicates that structural uncertainties overshadow the effects of discharge observation uncertainty. However, the comparison of individual models in Figure [6](#page-21-0) shows many instances of discharge observation uncertainty exceeding model performance differences. For instance, the IHACRES and SMAR models, despite their structural differences, demonstrate a <u>high level of simulation agreement (Figure [3c](#page-15-0)) and subsequent difficulty in discerning model performance differences in light</u>

615 of discharge observation uncertainty. In contrast, the VIC and XINANJIANG models, which have similar structures, display for two-thirds of the catchment simulation differences within the uncertainty bounds of the discharge observations. This underlines the complex interplay of model structures and subsequent performance, especially when contrasted with discharge observation uncertainty. The inter-model comparison contained only 3 to 6 catchments (

## 4.2 Eemporal robustness of model performance

620 Model performance can be heavily influenced by a few data points in the time series on which model performance is based [\(Clark et al.](#page-31-12) [\(2021\)](#page-31-12)). This can results in biased model performance interpretations depending on the <del>flow category) of significantly</del> higher observation uncertainty than simulation differences. We recommend that these catchment simulations are removed from benchmarks or model comparisons.

In this study we used the limits of streamflow observation uncertainty at the catchment outlets as described in the CAMELS-GB 625 dataset. Besides the limitations of the quantification of the observation uncertainty itself, this study is limited by the availability of only the uncertainty bounds of uncertainty. If we had ideal data available we would use the standard deviations of the observation uncertainty distributions as these are more conservative estimates. This would result in less catchment simulations showing higher observation uncertainty than the differences between model simulationsselected time period for calibration and evaluation. When models are sensitive to certain data points this can be due to a lack of adequate process descriptions in the

630 considered models. In addition, this might also indicate the presence of disinformative events and model invalidation sites where the runoff coefficient exceeds a value of 1 [\(Beven and Smith](#page-31-1) [\(2015\)](#page-31-1); [Beven](#page-30-13) [\(2023\)](#page-30-13); [Beven and Lane](#page-30-1) [\(2022\)](#page-31-2); [Beven et al.](#page-31-2) (2022) ) or the presence of atypical data (e.g. [Thébault et al.](#page-36-12) [\(2023\)](#page-36-12)).

Models ought to demonstrate adequate performance across the entire time series and this should be accurately represented in the performance outcomes. The assessment of temporal sampling uncertainty does not imply that this is should not be the case,

- 635 it rather points towards in the model simulation and observation pairs that are worth investigating. These instances can serve as indicators that suggest areas where models may require further scrutiny and improvements. Knowing the temporal sampling uncertainty is relevant for model users as it provides information on the consistency of the model performance over time that is necessary to determine the fit-for-purpose of a model. Therefore, it is recommended to include alternative estimators better suited for skewed performance data in the reporting of model performance (e.g. [Lamontagne et al.](#page-34-15) [\(2020\)](#page-34-15); [Shabestanipour et al.](#page-35-15) [\(2023\)](#page-36-13); Toy  $\lambda$ 640
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## 4.3 Moving towards standardized benchmark proceduresPractical implications for model users

We introduced a method that accounts for streamflow observation uncertainty which is kept The method introduced in this study is purposely designed to be as generic and easy to implement as possible. The generality ensures broader applicability

in hydrology and geosciences. The method is applicable for any straightforward as possible to increase the potential for

- 645 adoption in future studies. It can be applied to any hydrological state or flux <del>for which where</del> observation time series including uncertainty estimatesare available. In the absence of uncertainty estimates, one might use this method in combination with multiple evaluation products. A rough estimate of uncertainty can be based on the probability density distribution of multiple observation time series. The ease of implementation is key as it more likely to be adopted by other studies and to be part of standardized benchmarks.
- 650 Benchmark procedures are workflows that are used to compare models. We advocate to include sampling uncertainty and observation uncertainty in our benchmark procedures. This can be achieved by reportingthe uncertainty values and after conducting the analyses excluding catchment simulations from benchmarks. Reporting can be further improved by separating flow conditions. In the case of streamflow the additional information through flow separation can be used to support hypotheses related to connections between streamflow simulations and hydrological process descriptions. This distils into reporting more
- 655 meta-data with model outputs in a standardized mannerinclude uncertainty estimates. In addition, we recommend for the routine reporting of evaluation data uncertainties as well as the temporal sampling uncertainty of objective functions. This would not only yield a clearer understanding of the relevance of differences between model outcomes but also aid in identifying samples that require cautious interpretation. This reporting, however, does not replace model benchmarks that include full uncertainty analyses (e.g. [Lane et al.](#page-34-10) [\(2019\)](#page-34-10)), but enhances the interpretability of model performance in its absence.
- 660 For statistical and model benchmarks to be standardized it is necessary that the community agrees on best practices and provides a template for benchmark experiments and reporting and storage (Hoch and Trigg 2019). Standardized benchmark procedures will increase the longevity of For model benchmark results for future research. Standardization will also reduce redundant work as less model runs are required. This has the benefit of stimulating more time spent on novel research than data intensive studies [\(Jain et al., 2022\)](#page-33-13). Standardized benchmark templates should encompass multiple objective function,
- 665 as is reconfirmed by the sensitivity of results to objective function selection in this study, and workflows for the evaluation of multiple states and fluxes users, this approach offers a pragmatic way to understand the implications of uncertainty in their model selection processes. While our method facilitates a clearer understanding of where and how uncertainties affect relative model performance differences, it should be viewed as a complementary step rather than a replacement for a thorough uncertainty analysis.
- 670 Here, we make an effort to standardize the workflow by firstly using the same meteorological forcing data and streamflow observations that were used to create the

## 4.4 Limitations

The study presented faces several practical limitations. First, the exclusion of the lower and upper 5th percentiles of flow from the analysis introduces a constraint on the uncertainty assessment, overlooking critical flow conditions that are often of

675 significant interest in hydrological studies. This exclusion limits the ability to fully understand model performance under a complete range of hydrological conditions. Second, the reliance on uncertainty bounds rather than direct uncertainty estimates from rating curves, due to their absence in the CAMELS-GB dataset for consistency and secondly through the creation of

reproducible workflows using eWaterCycle [\(Hut et al., 2022\)](#page-33-6). We use eWaterCycle to show how benchmark studies can be done in a reproducible manner using high level readable code. Platforms like eWaterCycle should host standardized benchmark

- 680 procedures to achieve the benefits outlined above. With this study we aim to set first steps by providing documented example notebooks of the scripting (GitHub Repo:add DOI). This can be viewed as a template for a benchmark procedure when studying the difference in hydrological model performance in the light of observation uncertainty and objective function sampling uncertainty dataset, poses another limitation. By using broad uncertainty bounds instead of precise estimates derived from rating curves, the analysis may not capture the true variability and uncertainty inherent in the discharge observations.
- 685 Last, the study's focuses solely on evaluating model performance primarily through discharge simulations, without delying into the reasons behind good or poor model performance as this is outside of the scope of the study. To facilitate comparisons between different studies we encourage the hydrological community when doing benchmark studies to either use, or add to the collection of , community standard benchmark templates. Future work should extent the benchmark procedure to include evaluation of multiple states and fluxes.

690 We set out this study to highlight

#### 5 Conclusions

This study assesses the importance of including <del>streamflow discharge</del> observation uncertainty and <del>objective function uncertainty</del> when conducting hydrological model evaluations or model comparisons based on temporal sampling uncertainty of objective functions in hydrological model performance evaluations based on a large-sample hydrology dataset. By developing a generic 695 and easy to implement method we demonstrate how these uncertainties can be included in benchmark procedures. The scripting accompanying this study is easily adaptable to other case study areas, hydrological models , and forcing inputs due to the implementation in eWaterCycle. catchment dataset. This is done by statistical testing that determines if the difference in discharge simulations between two hydrological models is larger or smaller than the discharge observation uncertainty estimates. To support this analysis flow categories are created between the 5th and 95th percentile range of observed flow and

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700 3 use cases are devised.
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We demonstrated the methodology through two experiments. An inter-model comparison experiment of the In the model refinement use case a substantial 100 out of 299 catchment instances showed discharge simulation differences between the default and optimized wflow\_sbm and PCR-GLOBWB hydrological models and an intra-model evaluation experiment that assesses the benefits of additional calibration based on streamflow observationsof the wflow\_sbm model.

- 705 The main findings of these experiments are that for the sampling uncertainty assessment the intra-model evaluation experiment simulations of 210 (KGE-NP) and 288 (NSE) out of 398 catchments contain higher sampling uncertainty than the difference in objective functions. For the inter-model comparison experiment simulations these are 53 (KGE-NP) and 86 (NSE) catchments out of 398. In these cases models that were within the uncertainty bounds of discharge observations. This emphasizes the need for integrating discharge observation uncertainty in the calibration process for model refinement. As a result it is difficult to
- 710 draw conclusions as to which model is best performing based on streamflow at the catchment outlet before further investigating

the validity of the data points causing the sampling uncertainty. The high number of occurrences establish and highlight the importance of reporting sampling uncertainty.

For the observation uncertainty assessment, discern if the optimization of the model leads to improved simulations of actual discharge. For the intra-model evaluation experiment shows, model comparison use case, we found that depending

- 715 on the flow category, between 114 and 138 catchment simulations with statistically higher streamflow observation uncertainty than differencesbetween model simulations. Hence, no conclusions can be drawn on the better performing model simulation. Lower values of between 3 and model combinations a large fraction of catchments showed discharge observation uncertainty exceeding simulation differences. Thereby suggesting careful consideration of this uncertainty in model performance evaluations. The model structure uncertainty use case that is based on 6 eatchment simulations are found for the inner-model comparison
- 720 experiment. These should be reported and excluded from benchmarking. Given that the number of catchments is low, system scale conclusions are not as strongly affected by the streamflow conceptual hydrological models indicated only a few instances of discharge observation uncertainty exceeding simulation differences. Indicating that model structure uncertainty, expressed as discharge simulation differences, often exceeds discharge observation uncertainty. Comparison of the six individual hydrological models showed no clear relation between model complexity and model performance.
- 725 These experiments demonstrated the importance of not accepting the output of benchmark efforts on face value when no analyses of sampling uncertainty and streamflow observation uncertainty are performed. Implementing the proposed method in standardized benchmark procedures will lead to more robust benchmarking resultsQur study underscores the necessity of integrating discharge observation uncertainty and temporal sampling uncertainty into hydrological model evaluations to ensure accurate, reliable, and meaningful assessments of model performance. Implementing our proposed methodology in reporting 730 practices is expected to improve the robustness of hydrological model result interpretation, aiding in more informed model selection and refinement decisions by model users.

*Code availability.* https://github.com/jeromaerts/CAMELS-GB\_Comparison\_Uncertainty, https://doi.org/10.5281/zenodo.7956488

*Author contributions.* JPMA wrote the publication. JPMA, JMH, and RWH, conceptualized the study. JPMA, JMH, RWH, NCvdG, GC developed the methodology. JPMA, JMH, conducted the analyses. JMH, RWH, NCvdG, GC did internal reviews. RWH, NCvdG are PIs of 735 the eWaterCycle project.

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Figure A1. (A) Spatial distribution of the best performing KsatHorFrac calibration parameter of the wflow\_sbm model based on additional calibration on streamflow observations. (B) Spatial distribution of the KGE-NP objective function based on the calibration period of the wflow\_sbm model.

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- 1 **A.1** wflow\_sbm calibration
- A1 A.2 NSE based model performance results



Figure B1. Cumulative distribution function (CDF) plots of the Nash-Sutcliffe Efficiency (NSE) objective function, derived from discharge estimates and observations at 299 catchment outlets. (a) shows the CDF for the model refinement use case, optimizing the wflow\_sbm hydrological model with a single parameter. (b) shows the CDF for the model comparison use case, comparing the optimized wflow\_sbm and PCR-GLOBWB hydrological models. (c) demonstrates the CDF for the model structure use case, showcasing results from six conceptual hydrological models.