

# 1 WRF-Comfort: Simulating micro-scale variability of outdoor heat 2 stress at the city scale with a mesoscale model

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10 **Abstract.** Urban overheating, and its ongoing exacerbation due to global warming and urban development, leads to increased  
11 exposure to urban heat and increased thermal discomfort and heat stress. To quantify thermal stress, specific indices have been  
12 proposed that depend on air temperature, mean radiant temperature (MRT), wind speed, and relative humidity. While  
13 temperature and humidity vary on scales of hundreds of meters, MRT and wind speed are strongly affected by individual  
14 buildings and trees, and vary at the meter scale. Therefore, most numerical thermal comfort studies apply micro-scale models  
15 to limited spatial domains (commonly representing urban neighborhoods with building blocks) with resolutions on the order  
16 of 1 m and a few hours of simulation. This prevents the analysis of the impact of city-scale adaptation/mitigation strategies on  
17 thermal stress and comfort. To solve this problem, we develop a methodology to estimate thermal stress indicators and their  
18 subgrid variability in mesoscale models - here applied to the multilayer urban canopy parametrization BEP-BEM within the  
19 WRF model. The new scheme (consisting of three main steps) can readily assess intra-neighborhood scale heat stress  
20 distributions across whole cities and for time scales of minutes to years. The first key component of the approach is the  
21 estimation of MRT in several locations within streets for different street orientations. Second, mean wind speed, and its subgrid  
22 variability, are parameterized as a function of the local urban morphology based on relations derived from a set of microscale  
23 LES and RANS simulations across a wide range of realistic and idealized urban morphologies. Lastly, we compute the  
24 distributions of two thermal stress indices for each grid square combining all the subgrid values of MRT, wind speed, air  
25 temperature, and absolute humidity. From these distributions, we quantify the high and low tails of the heat stress distribution  
26 in each grid square across the city, representing the thermal diversity experienced in street canyons. In this contribution, we  
27 present the core methodology as well as simulation results for Madrid (Spain), which illustrate strong differences between heat  
28 stress indices and common heat metrics like air or surface temperature, both across the city and over the diurnal cycle.

## 1 Introduction

The combination of urban development and climate change has increased heat exposure in cities in recent decades (Tuholske et al., 2021) and a continuation of these trends in the 21st century would be difficult to offset locally from an air temperature perspective (Broadbent et al., 2020; Krayenhoff et al., 2018; Zhao et al., 2021). Adaptation options that target contributions to heat exposure other than the air temperature, such as radiation (e.g., via shade) and wind (e.g. via improved street ventilation), should therefore be considered. Quantification of these contributions relative to air temperature requires the application of comprehensive thermo-physiological heat stress metrics such as the Universal Thermal Climate Index, UTCI (Jendritzky et al., 2012), the Physiological Equivalent Temperature, PET (Höppe, 1999), or the Standard Effective Temperature, SET (Gagge et al., 1986). Moreover, exposure to heat hazards is moderated by infrastructure-based and social/mobility-based adaptations to heat, and by buildings and associated cooling mechanisms. Here, the focus is the development of a tool to quantify the outdoor component of heat exposure in cities, accounting for all relevant meteorological variables.

Heat exposure in urban areas is affected by several meteorological variables that vary on different spatial and temporal scales (Nazarian et al., 2022). While temperature and humidity vary on spatial scales on the order of hundreds of meters, shortwave and longwave radiation and wind speed are strongly affected by individual buildings and vary at the scale of a few meters. For this reason, most numerical thermal comfort studies in urban areas apply micro-scale models with resolutions on the order of ~~one~~ m and spatial domains that are limited to an urban block or neighborhood (Nazarian et al., 2017; Zhang et al., 2022; Geletič et al., 2018). While these studies include substantial detail at the micro-scale, they are very expensive computationally and therefore can be applied only to a few neighborhoods and they neglect the interactions with larger scale meteorological phenomena (e.g., land/sea breezes, mountain/valley winds, urban breezes) that often play a relevant role in outdoor thermal comfort and its variation across cities. On the other hand, contemporary meso-scale numerical models can be applied to the whole urban area and surrounding regions, and therefore capture these larger-scale phenomena, but have spatial resolutions of several hundred meters at best. These models use a grid mesh that does not resolve buildings and is therefore too coarse to capture the fine-scale variation of radiation and wind flow of relevance to outdoor heat exposure and ultimately thermal comfort.

The objective of this work is to fill the aforementioned gap by developing a model that includes the most crucial capabilities of micro-scale assessments of thermal exposure within meso-scale models. This new model will quantify the spatial variability (i.e., statistical representation of the microscale distribution) for longwave and shortwave radiation as well as wind speed within each meso-scale grid square. Subsequently, it will capture the range of thermal exposure, as quantified by the UTCI and SET thermal stress metrics, within each urban grid square across a city at each time of day. The focus here is on the *range* of thermal exposure, such that we identify the cool and hot spots within the grid cell without having to resolve the entire spatial distribution. We argue that this represents the most crucial information for heat management and urban design interventions, as it identifies whether people can move and search for optimal thermal conditions. For example, if hot spots are experiencing extreme heat stress but the cool spots are at slight heat stress, pedestrians have the opportunity, and autonomy, to seek shade

63 and thermal respite (i.e., [temporal and](#) spatial autonomy as described in Nazarian et al. (2019)). Conversely, if the conditions  
64 in the cool spot are already in extreme heat stress, this can be used to inform urban design interventions or heat advisories to  
65 vulnerable populations to avoid being outside at that place and time. Overall, representing the range of heat exposure at the  
66 neighborhood scale while covering regional-scale phenomena is key to human-centric assessments of urban overheating  
67 (Nazarian et al., 2022).

68 The new model is embedded in the multi-layer urban canopy parameterization BEP-BEM (Martilli et al., 2002; Salamanca et  
69 al., 2010) which simulates the local-scale meteorological effects of the `grid_`-average urban morphology within the Weather  
70 Research and Forecasting (WRF) mesoscale model (Skamarock et al., 2019 version 4.3 has been used in this study). Here,  
71 BEP-BEM is extended to quantify the spatial variation of the mean radiant temperature and wind speed within the grid square  
72 at the pedestrian level. To our knowledge, three schemes in the published literature have attempted to capture thermal exposure  
73 in an urban canopy model. Pigliautile (2020) implemented a scheme to estimate human thermal exposure in the Princeton  
74 Single-Layer Urban Canopy Model. However, the scheme has not been run within a mesoscale model. Jin et al. (2022) calculate  
75 urban mean radiant temperature (MRT) in a mesoscale model, while Lemonsu (2015) and Leroyer et al. (2018) assess UTCI  
76 in mesoscale modeling applications within Paris and Toronto, respectively. Moreover, Giannaros et al (2018, 2023), made an  
77 offline coupling of WRF-BEP\_BEM with RayMan (Matzarakis et al. 2007). However, none of these approaches account for  
78 the within-grid spatial variation of wind speed, and their assessment of sub-grid spatial variation of radiation exposure (i.e.,  
79 mean radiant temperature) is limited. Here, we further extend the BEP-BEM model embedded in the WRF meso-scale model  
80 to overcome these limitations and more fully assess spatial variation of thermal exposure within each urban grid square.

81 In section 2, the methodology is described in detail, with a focus on model development and implementation in WRF. In  
82 Section 3, we present an example of the type of outputs that can be produced. Conclusions are in section 4.

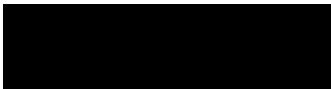
## 83 **2 Methodology**

84 The most complete thermal stress indices invariably depend on four meteorological variables: air temperature, mean radiant  
85 temperature (MRT), relative humidity, and wind speed. Among these, MRT and wind speed have the largest spatial variability  
86 in the urban canopy, and this variability is often captured with 3D micro-scale models of urban airflow and radiative heat  
87 transfer. At the meso-scale, however, it is not feasible to incorporate such models, motivating the simplified urban canopy  
88 parameterizations developed here. Below we detail how the BEP-BEM urban canopy model is modified to a) introduce a  
89 simplified model for MRT variation within a meso-scale grid cell (Sec. 2.1) and b) parameterize airflow variability (Sec. 2.2)  
90 in the urban canopy within a grid cell, and make a simple estimate of air temperature variability. These meteorological  
91 parameters are then used to estimate the sub-grid scale variation of thermal stress indices (Sec. 2.3), namely SET and UTCI,  
92 as two of the most commonly used indices for outdoor environments (Potchter et al 2018). Lastly, we discuss how multi-scale

93 temporal and spatial variabilities in thermal exposure can be effectively communicated using the outcomes of the updated  
94 WRF-BEP-BEM model.

### 95 2.1 A simplified model for MRT variability in the urban canopy

96 The mean radiant temperature is a measure of the total radiation flux absorbed by the human body, including both shortwave  
97 (from the sun, either directly or after reflection on the walls or road) and longwave (emitted from solid bodies like walls or  
98 road, or from the sky) radiation. Whether pedestrians are shaded or in the sunshine, as well as their distance from warm surfaces  
99 emitting radiation, is therefore very important. BEP-BEM applies a simple urban morphology: two street canyons of different  
100 orientations, each with the same street width and building height distribution on each side of the canyon (Martilli et al. 2002).  
101 To capture the within-grid spatial extremes of mean radiant temperature, we assess pedestrian locations at the center of the  
102 street for two canyon orientations considered in BEP-BEM and at positions located at a distance of 1.5 m from the building  
103 wall on each side of the street, representing the sidewalks. Thus, there are 6 positions (three for each street direction) in each  
104 urban grid square where we compute the mean radiant temperature (shown for the example of North-South and East-West  
105 streets in Fig. 1). For shortwave reflection and longwave emission and reflection radiation exchange, the standard BEP view  
106 factor and shading routines (Martilli et al. 2002) are used to estimate the amount of shortwave (direct and diffuse) and longwave  
107 radiation reaching a vertical segment 1.80 m tall and located in each of the six positions previously mentioned (Fig. 1, Appendix  
108 A). Reflection of shortwave radiation and emission and reflection of longwave radiation from both building walls and the  
109 street surface are accounted for via these view factors. The pedestrian is “transparent” from the perspective of the urban facets,  
110 meaning that its presence does not alter the shortwave and longwave radiation reaching the building walls and road. The mean  
111 radiant temperature is computed by weighting the radiation reaching each side of the vertical segment by 0.44, and the radiation  
112 reaching the downward- and upward-facing (at 1.80 m height) surfaces of the pedestrian by 0.06 each. This approach follows  
113 the six-directional weighting method (Thorsson et al. 2007) and aggregates the four lateral weightings of 0.22 into two lateral  
114 weightings of 0.44 since BEP-BEM is a two-dimensional model (e. g. the streets are considered infinitely long). Namely,



(1)

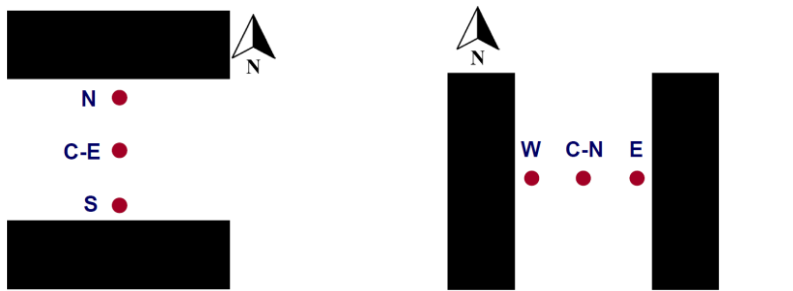
115  
116 where, for an N-S oriented street,  $i=1,2$  are for the vertical sides of the pedestrian looking East, and West respectively, and  
117  $i=3,4$  are for the top and bottom. Therefore,  $W_{1,2}=0.44$ , while  $W_{3,4}=0.06$ , while the absorptivity of the pedestrian in the  
118 shortwave and longwave, two constants  $a_K$  and  $a_L$ , respectively, are  $a_K=0.$ , and  $a_L=0.97$  the absorption coefficient for long-  
119 wave radiation, or emissivity, of the human body),  $K_{1,2}$  and  $L_{1,2}$  are the short and longwave radiation reaching the vertical  
120 segment, and  $K_{3,4}$  and  $L_{3,4}$  are short and longwave radiation reaching the top and bottom respectively, and  $\sigma$  is the Stefan-  
121 Boltzmann constant (see Appendix A for details about how the radiation components are computed).

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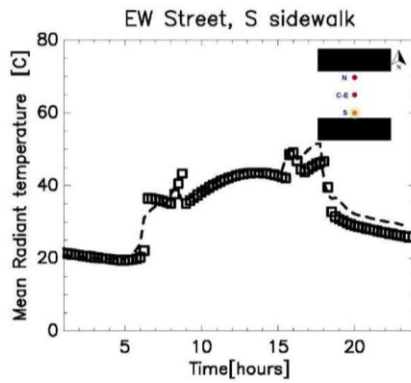
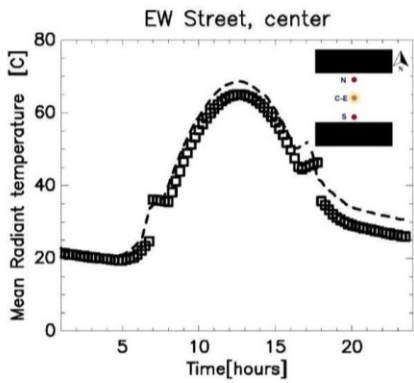
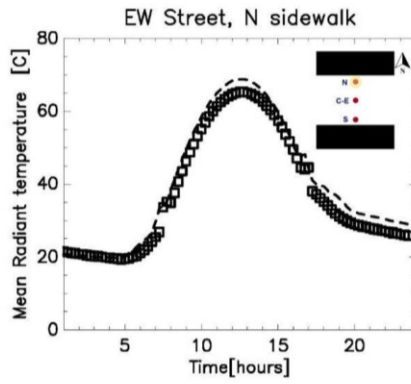
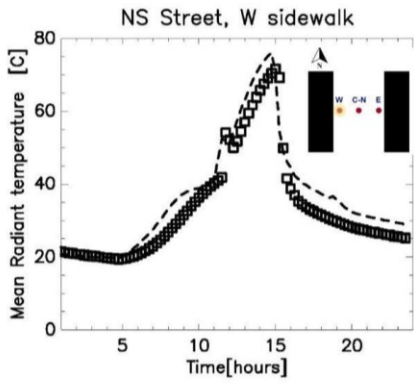
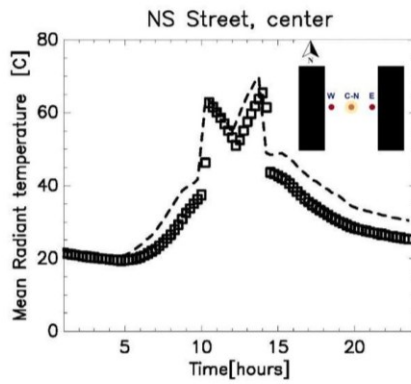
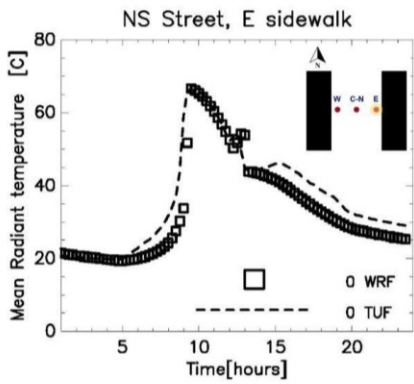
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**Figure 1:** Two street directions (left: E-W canyon, right: N-S canyon) and pedestrian locations considered for Mean Radiant Temperature calculations.

122 The diurnal progression of the mean radiant temperature computed by this new model in BEP-BEM is subsequently compared  
 123 with that obtained from TUF-Pedestrian, a more detailed three-dimensional model that has been evaluated against  
 124 measurements (Lachapelle et al. 2022; Jiang et al. 2023). TUF-Pedestrian is configured with identical input parameters and  
 125 meteorological forcing, and with long canyons that approximate the two-dimensional BEP-BEM canyon geometry. The new  
 126 model clearly captures the relevant details of the diurnal progression of MRT at all six locations (Fig. 2), with a mean absolute  
 127 difference of 3.4 K, and a root mean square difference of 4.3 K across all locations. A comparison of the shortwave radiation  
 128 loading on the pedestrian between the two models reveals very good excellent agreement (Appendix B-A Fig. B-A1, B-A2),  
 129 considering the highly simplified urban morphology used by BEP-BEM, with biggest errors limited to short periods of time;  
 130 thus, most of the model disagreement arises from differences between longwave loading on the pedestrian as a result of  
 131 different methods for computation of surface temperature between the models. Overall, the new model of mean radiation  
 132 temperature in BEP-BEM provides satisfactory results.



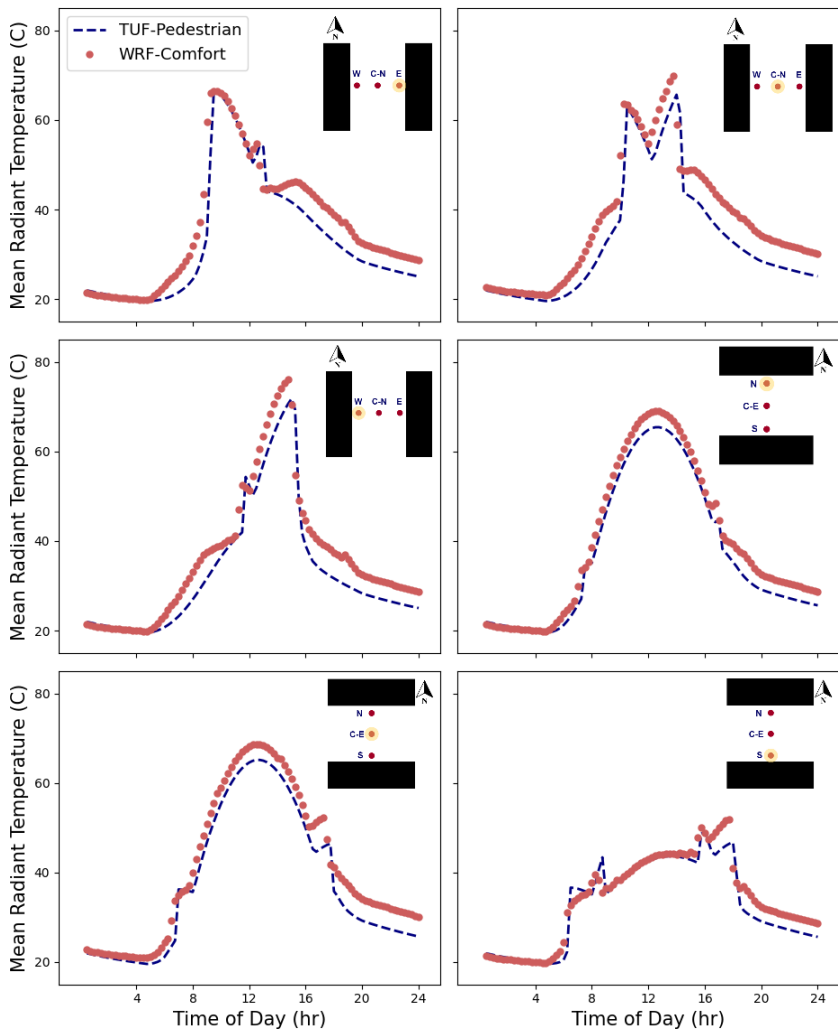


Figure 2: Comparison of diurnal variation of Mean Radiant Temperature (MRT) between the new model in BEP-BEM and TUF-Pedestrian for each of the six locations in Fig. 1.

## 2.2 Parameterize airflow variability in the urban canopy

Mesoscale models solve conservation equations for the three components of momentum. From these, it is possible to derive the spatially averaged wind velocity in each grid cell, at the grid resolution of the mesoscale model, commonly of the order of 300m-1km. The spatially averaged wind velocity in the urban canopy ( $\langle V \rangle$ ), close to the pedestrian height (~2.5m), is the square root of the sum of the spatial average of the two horizontal components  $u$ , and  $v$ , (neglecting the vertical component, which is usually at least one or two orders of magnitude smaller than the horizontal),

$$\langle V \rangle = \frac{1}{V_{air}} \sqrt{\left( \int_{V_{air}} u dV \right)^2 + \left( \int_{V_{air}} v dV \right)^2} \quad (2)$$

where here  $V_{air}$  is the volume of the grid cell occupied by air (e. g. without the buildings)

However, the wind velocity calculated in mesoscale models is different from the average wind speed that would be experienced by a person in the grid cell. This is better represented by the spatial average of the wind speed ( $\langle U \rangle$ ) (e. g. the modulus of the vector), written as

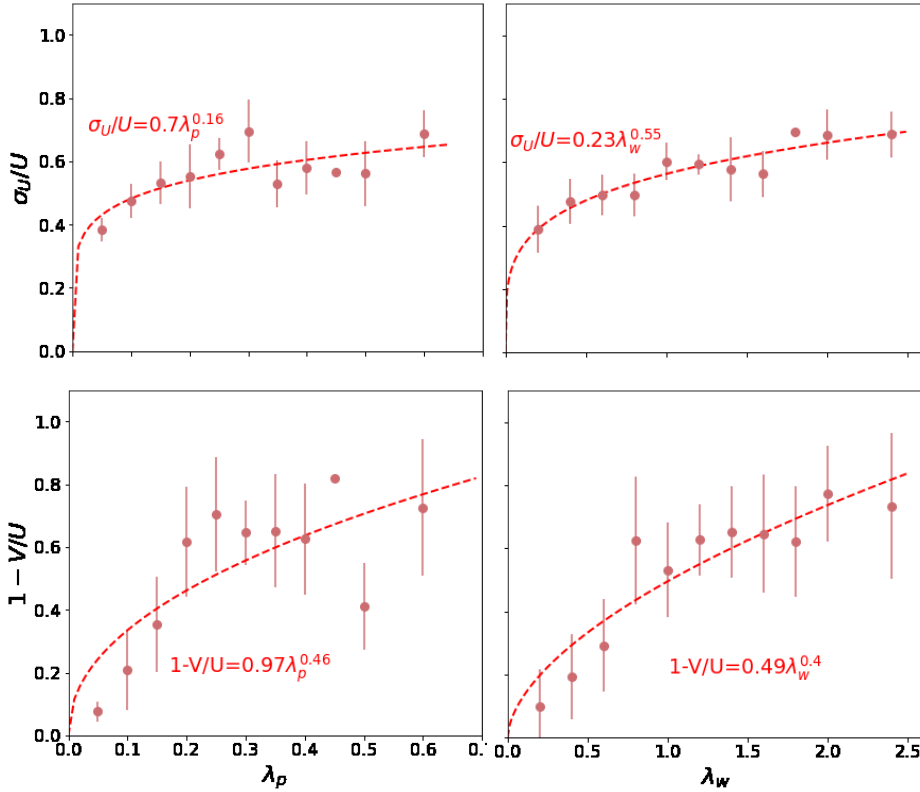
$$\langle U \rangle = \frac{1}{V_{air}} \int_{V_{air}} \sqrt{u^2 + v^2} dV \quad (3)$$

To assess the impact of airflow on human thermal comfort, the wind speed should be estimated from the wind velocity computed in the mesoscale models. Additionally, it is critical to parameterize and estimate the spatial variability of mean wind speed in the urban canopy. Accounting for these factors, the range of wind speed variability at the pedestrian level is estimated, which is critical for the quantification of spatial variability of outdoor thermal stress and comfort.

Here, we describe the parameterization of a) wind speed-to-velocity ratio and b) wind speed distribution, based on urban density parameters. Data are considered from over 173 microscales CFD simulations of urban airflow ~~are considered~~ over realistic and idealized urban configurations, spanning a wide range of building plan area ( $\lambda_p$ ), frontal area ( $\lambda_f$ ), and wall area ( $\lambda_w$ ) densities representative of realistic urban neighborhoods in different types of cities. CFD simulations are conducted using 162 large-eddy simulations (LES) and 11 Reynolds-averaged Navier–Stokes (RANS) schemes detailed in Appendix [CB](#).

Mean wind velocity ( $\langle V \rangle$ ), speed ( $\langle U \rangle$ ) and its spatial standard deviation ( $\sigma_U$ ) are computed at a horizontal cross-section at pedestrian height for each CFD simulation and used for deriving parameterizations (Fig 3). An additional data point is added at  $\lambda_p = \lambda_w = 0$ , ensuring that wind speed is equal to wind velocity, and its standard deviation is set to zero, for the non-urban case.





162 **Figure 3:** Relationship between  $1 - \langle V \rangle / \langle U \rangle$  (bottom row), and  $\sigma_U / \langle U \rangle$  (top row), and two morphological parameters,  $\lambda_p$  (left column), and  
 163  $\lambda_w$  (right column) based on the CFD simulations. Dots represent the average of the value among all the simulations that share the same  
 164 morphological parameter, and the vertical bar indicates the standard deviation. The dashed line and the formula indicate the best fit.

165

166 Parameterizations are derived (shown in Fig. 3) for two density parameters ( $\lambda_p = A_p / A_{tot}$ , and  $\lambda_w = A_w / A_{tot}$ , where  $A_p$  is the  
 167 area of the horizontal surface occupied by buildings, or the roof area,  $A_w$  is the area of vertical (wall) surfaces, and  $A_{tot}$  is the  
 168 total horizontal area). We find that  $\lambda_w$  better predicts mean wind speed and its spatial variability at the pedestrian height,  
 169 because it represents both horizontal and vertical heterogeneities in the urban canopy. Note that  $\lambda_F$  has not been included in  
 170 the study, given the difficulty to estimate it for real urban areas, and to translate it to the simplified 2D urban morphology used

171 by BEP-BEM. In any case,  $\lambda_F$  is closely related to  $\lambda_w$ . Therefore, the following parameterizations are implemented at the  
 172 pedestrian height (1.8m) as a function of the wall area density  $\lambda_w$

173

$$174 \quad \langle U \rangle = \frac{\langle V \rangle}{1 - 0.49\lambda_w^{0.4}} \quad (4)$$

$$175 \quad \sigma_U = \langle U \rangle (0.25\lambda_w^{0.55}) \quad (5)$$

176 We, therefore, assign three values of wind speed in each grid cell,

$$177 \quad \langle speed \rangle_1 = \max(0.01, \langle U \rangle (1 - 0.25\lambda_w^{0.55}))$$

$$178 \quad \langle speed \rangle_2 = \langle U \rangle \quad (6)$$

$$179 \quad \langle speed \rangle_3 = \langle U \rangle (1 + 0.25\lambda_w^{0.55})$$

180 Note that here we consider the three values equally likely, in order to realistically span the range of possible values that the  
 181 wind speed can take in each grid cell. Since UTCI has been designed for 10m wind speeds, a simple log law is used to  
 182 rescale wind speed at 10m, before passing it to the UTCI routine.

### 183 2.3 Calculation of the thermal comfort index

184 To represent the subgrid spatial variability of air temperature, detailed CFD simulations are not available, so we simply used  
 185 a variability of 1 degree Celsius, which we consider to be a conservative estimate of the spatial variability of air temperature  
 186 over a spatial scale of the order of one km squared. Therefore, for each grid cell, we have three values for air temperature:

187

$$188 \quad Temp_1 = Temp_{WRF} - 1$$

$$189 \quad Temp_2 = Temp_{WRF} \quad \text{-----} \quad (7)$$

$$190 \quad Temp_3 = Temp_{WRF} + 1$$

191 ~~w~~Where  $Temp_{WRF}$  is the air temperature provided by WRF.

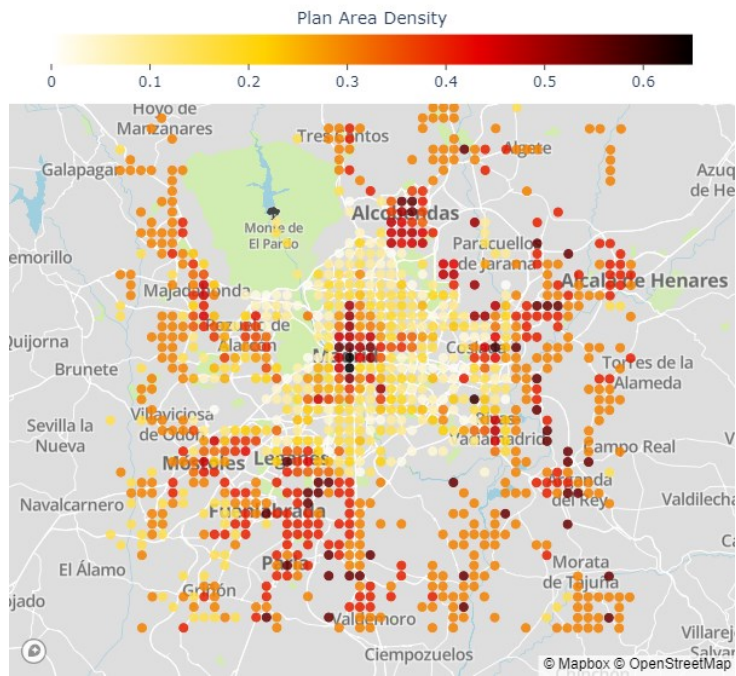
192 We therefore have, for each urban grid cell, *three* values of wind speed, *three* values of temperature, and *six* values of mean  
 193 radiant temperature. No variability of the absolute humidity is considered, but the relative humidity is computed using the  
 194 three values of air temperature.

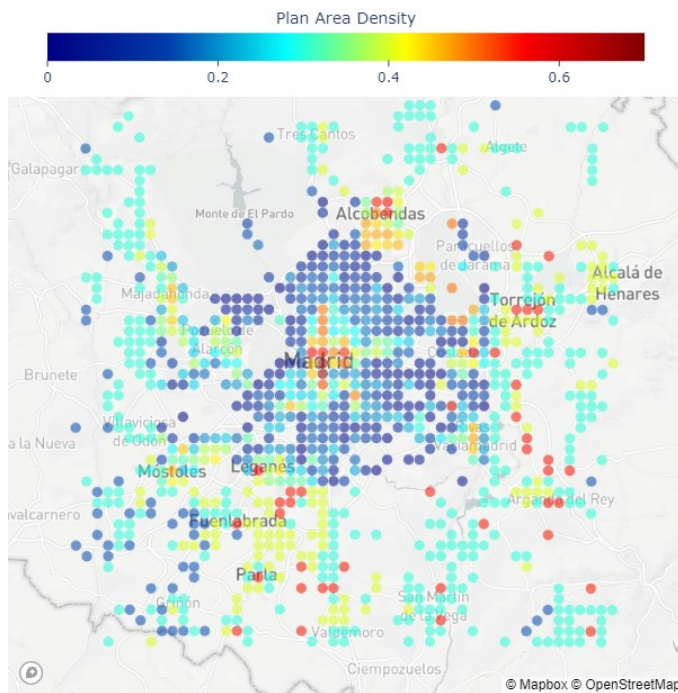
195 Based on the variation of these climate variables, assumed uncorrelated, 54 possible combinations of the air temperature, mean  
 196 radiant temperature, and wind speed values can be formed. For each one of these combinations, we calculate the corresponding

197 SET or UTCI value. Based on the resulting distribution, we estimate the value of the 10th, 50th, and 90th percentile SET or  
198 UTCI for each grid square (at each output time).

### 199 3. Characterization of thermal comfort in regional-scale models: Madrid case

200 To illustrate the capabilities of the new scheme, a typical heat wave day in the city of Madrid (Spain) is simulated with WRF.  
201 Madrid is located on a plateau at 500-700m above sea level, in the middle of the Iberian Peninsula. It experiences hot summers,  
202 with frequent heat waves that are increasingly causing severe heat stress in the population, and it is therefore considered a  
203 relevant case study. Four nested domains have been used, with resolutions of 27, 9, 3, and 1km respectively. The city  
204 morphology (Fig. 4) is derived from high-resolution LIDAR data that covers most of the metropolitan area of Madrid (Martilli  
205 et al., 2022), while the morphology of the surrounding towns is determined based on Local Climate Zone maps (Brousse et  
206 al., 2016). It is also important to mention that the city is located on a hilly terrain, with higher elevations in the N-W part of  
207 the urban area (around 700m a.s.l.) dropping to 500m a.s.l. or less in the S-E. Moreover, there are two topographical  
208 depressions on the two sides of the city center, caused by the rivers Jarama and Manzanares (for a detailed description of the  
209 topography see also Martilli et al. 2022, where the same set-up was used). Other model configurations are the NOAH  
210 vegetation model for the non-urban grid points and the Bougeault and Lacarrere (1989) PBL scheme for turbulence  
211 parameterization. WRF coupled with BEP-BEM has previously been successfully used to simulate a heat wave period in  
212 Madrid (Salamanca et al., 2012). The period used in this paper is three days (14-16 July 2015). In particular, the analysis will  
213 focus on the 15th, when the maximum simulated temperature was above 40 Celsius. More information about the validation  
214 and a sensitivity study to select the optimal set-up can be found in Rodriguez-Sanchez (2020).





216

217

**Figure 4.** Map of the plan area building density over the Madrid region. The underlying map was created with Mapbox OpenStreetMap

218

### 3.1 Sub-grid scale variability of MRT and thermal comfort.

219

In order to understand how urban morphology affects the simulated heat stress, we focus on two grid points with very different urban morphology. One is located in the dense core of the city, with a building plan area density of  $\lambda_p = 0.69$ , and a height-to-width ratio (H/W) value of 1.6. The second is located in the southern part of the urban area, in a residential ~~neighborhood~~neighbourhood with a much lower building density ( $\lambda_p = 0.2$ ) and a H/W=0.1.

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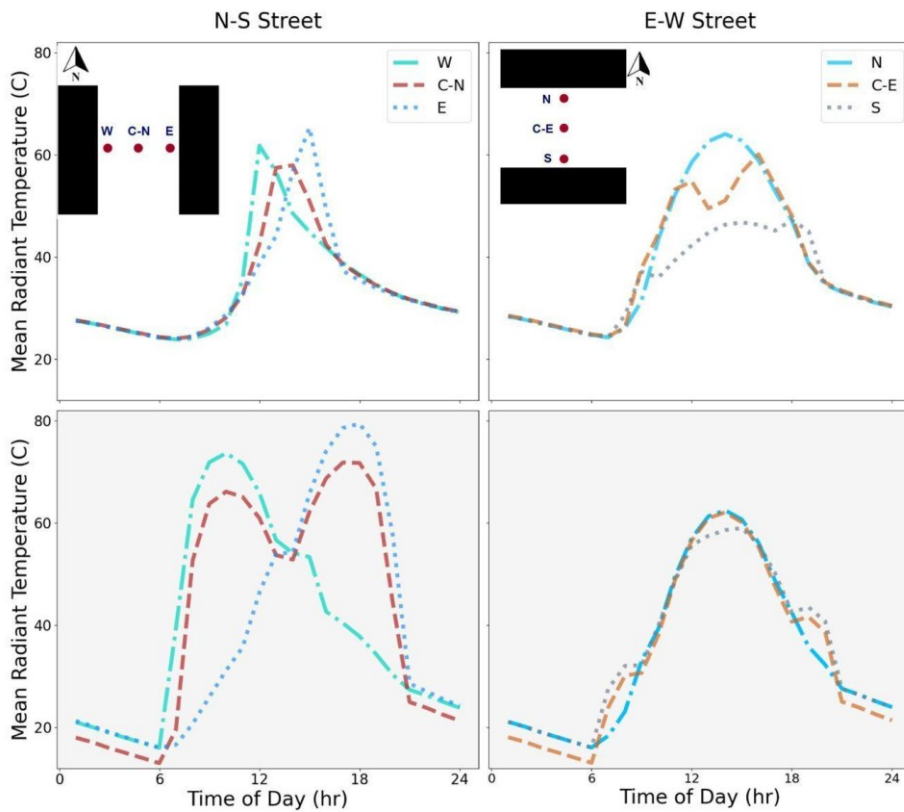
In Figure 5, the diurnal evolution of the mean radiant temperature in the six points (three per street direction) is presented for the high urban density point and the low urban density point. During the daytime, the impact of the shadowing is clear, with reduced mean radiant temperature in the high-density point compared to the more exposed low-density. On the other hand, during nighttime, the reduced sky-view factor in the high-density point slows down the cooling compared to the more open low-density location.

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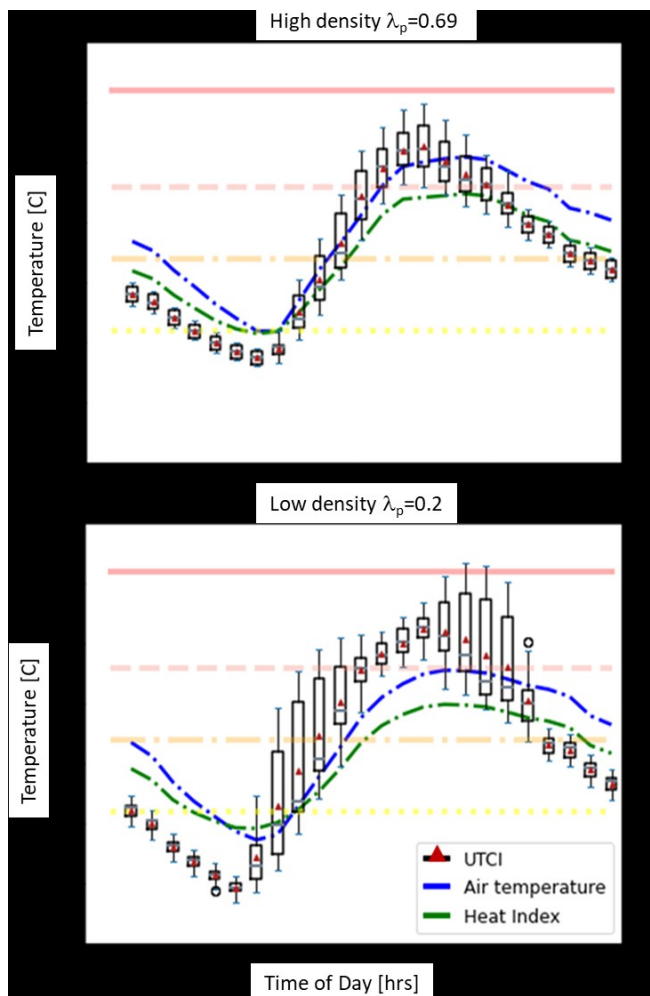


228

229 **Figure 5.** Diurnal evolution of MRT for 6 points in the urban canopy. The top row (white background) corresponds to a grid [point](#) with the  
 230 highest building density in the center of Madrid ( $\lambda_p = 0.69$ ) while the bottom row (with grey background) shows MRT in a low-density  
 231 neighborhood ( $\lambda_p = 0.19$ ). The left column is for an N-S street, while the right column shows an E-W street.

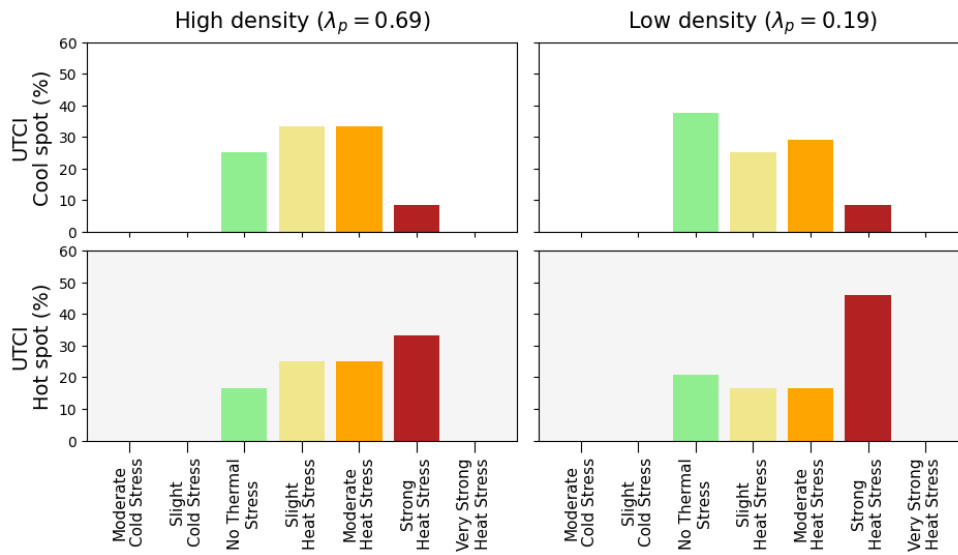
232 This behavior helps to explain the heat stress index (Figure 6), [which is here introduced here as an example of an index that](#)  
 233 [could be computed with standard outputs from a meteorological model, i.e., e.g. without having information related to](#)

234 [the radiation environment](#) (e.g., [MRT](#)) and urban morphology. The air temperature indicates hotter values both during the  
235 day and the night in the high urban density point compared to the low-density location. The Heat Index, which considers air  
236 temperature and humidity only, and does not include mean radiant temperature or wind, shows the same tendency. On the  
237 other hand, the UTCI behavior communicates a different and more complete result. In the low-density neighborhood, more  
238 exposed to the sun, the UTCI shows a stronger sub-grid spatial variability, in particular during the morning and afternoon,  
239 with the potential for stronger heat stress than in the high-density neighborhood. During nighttime, the spatial variability is  
240 reduced, due to reduced MRT variation as the shadowing effect disappears, and higher UTCI values are found at the high  
241 urban density location. This difference in behavior between the two locations can be seen also in Fig. 7, where the fractions of  
242 the 10th percentile of UTCI values (i.e. representative of one of the coolest spots in the grid cell) and the 90th percentile (i.e.,  
243 one of the hottest) in the different heat stress regimes are shown for the two points. Here we can see that in the low-density  
244 urban point, the cool location is in a comfortable UTCI range most of the time, while the hot (90th percentile UTCI) subgrid  
245 location is under stress most of the time. On the other hand, less variability is present in the high-density neighborhood, with  
246 fewer extreme values, and most of the time in the strong or moderate heat stress regime for both the cool and hot locations  
247 within the grid square. This kind of detail is not available from the Heat Index distribution which does not account for the  
248 mean radiant temperature, wind, or their variabilities (Fig. 8).

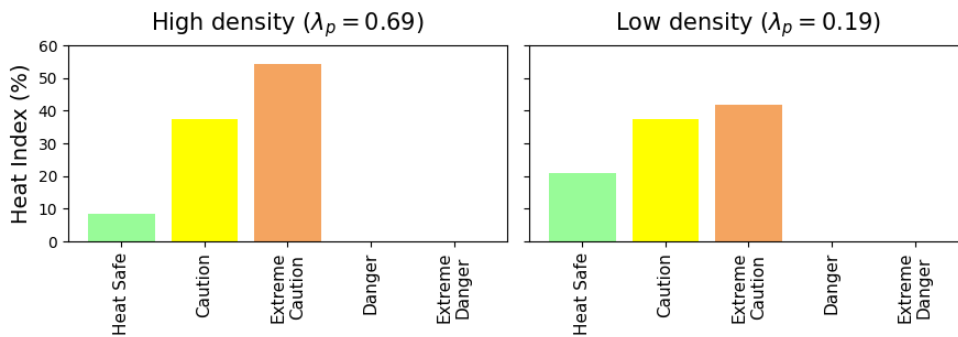


249 **Figure 6.** Diurnal evolution of UTCI compared with 2-m air temperature and Heat Index calculated from air temperature and relative  
 250 humidity at each grid point). The UTCI boxplot at each hour represents the subgrid-scale distribution calculated based on 6 MRT, 3 wind  
 251 speeds, and 3 air temperature values (54 combinations in total). The horizontal lines represent the thermal comfort zones for UTCI (i.e.  
 252 above +46C: extreme heat stress; +38 to +46: very strong heat stress; +32 to +38: strong heat stress; +26 to +32: moderate heat stress; and  
 253 +9 to +26: no thermal stress).





255  
256  
257 **Figure 7.** From top to bottom, the frequency of UTCI class over a 24-hour period, for a subgrid location that is cooler (i.e. 10th percentile  
258 of UTCI in the urban canopy, top), and for a subgrid location that is hotter (i.e. 90th percentile of UTCI in the urban canopy, bottom), for  
259 the high-density (left) and low-density (right) points.



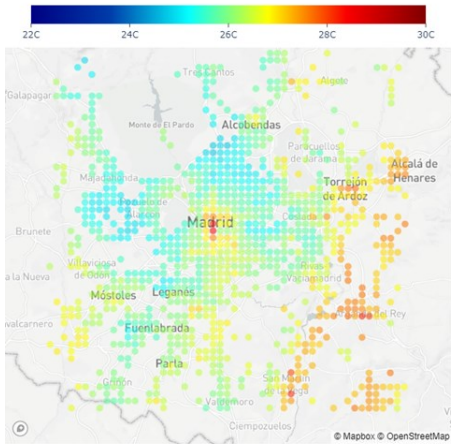
260  
261 **Figure 8.** same as Figure 7, but for the Heat Index  
262

### 3.2 City-scale maps of outdoor thermal comfort and heat stress indicators.

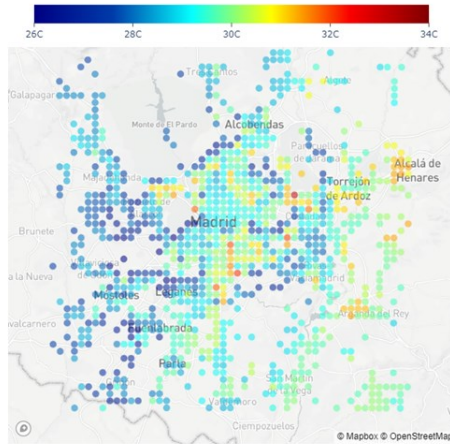
The previous analysis helps to understand the spatial distribution of the different variables presented in Fig. 9 at 10 and 16 UTC (note that Madrid is at Longitude 3W, so UTC is essentially equal to solar time). In the dense city center, the distribution of 2m air temperature at 0900 UTC shows a hot region in the dense city center, with cooler areas in the less dense regions around it. This effect is due to the fact that in the dense region, the reduced sky-view factor of the streets (high H/W), as well as the larger thermal storage capacity in the buildings, reduce the nocturnal cooling, and increase the vertical mixing in that part of the city compared to the surroundings. Such a difference is still visible in the morning. The higher temperatures in the S-E part of the urban area, and cool temperatures in the N-W are the result of the topographical differences. The spatial distribution of air temperature is qualitatively similar to the spatial distribution of the 10-percentile of UTCI (e. g. the cool spot in the grid cell), even if the differences between the center and the surrounding urban areas are not as intense as for 2m air temperature. On the other hand, the 90-percentile map (hot spot), shows a completely different pattern; due to the fact that in on the city center, at that time of the day, the whole street is still in the shadow, while in the surrounding, less dense urban areas there are points completely exposed to the sun. As a comparison, the map of surface temperature (a variable often used to represent the spatial distribution of heat in cities) as seen from a satellite, i.e. based only on a weighted average of roof, street, and vegetation temperatures (see full equations in Martilli et al. 2021), does not show a clear pattern, and it is uncorrelated with the other maps. This is a clear indication that this variable should not be used for the assessment of the heat hazard or heat stress in urban areas.

At 1600 UTC the air temperature shows again higher values in the city center, lower in the urban surroundings, and a gradient from hotter S-E at lower elevations to cooler N-W at higher elevations (Fig. 10). Such a tendency is present also for the 10th percentile (cool spot), but with less variability. The 90th percentile map (hot spot) indicates that the area with elevated heat stress extends well beyond the city center, including lower-density regions that, even if they have lower air temperatures, are fully exposed to the sun. Finally, as it was the case for 0900 UTC, the surface temperatures have a map uncorrelated with neither the air temperatures nor the UTCI maps.

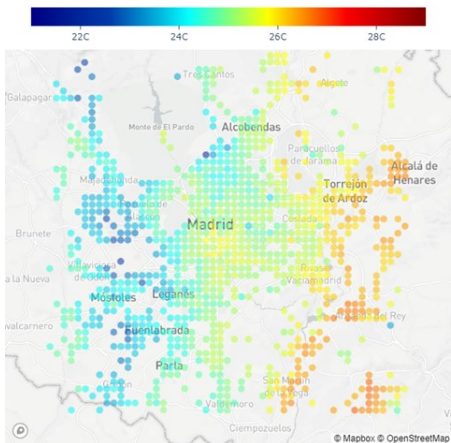
Air temperature



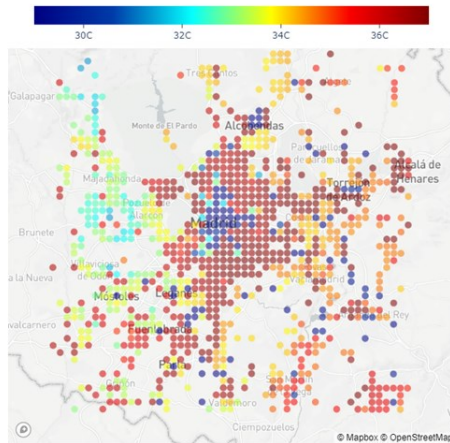
Surface temperature



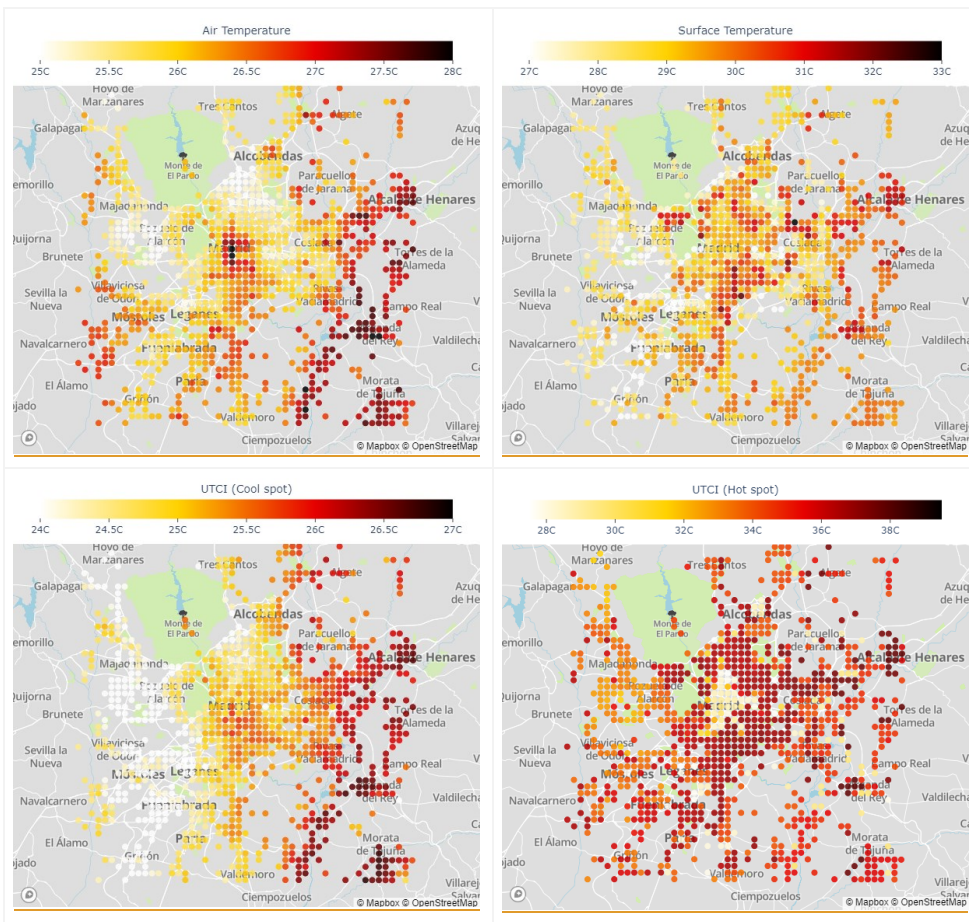
UTCI (Cool spot)



UTCI (Hot spot)

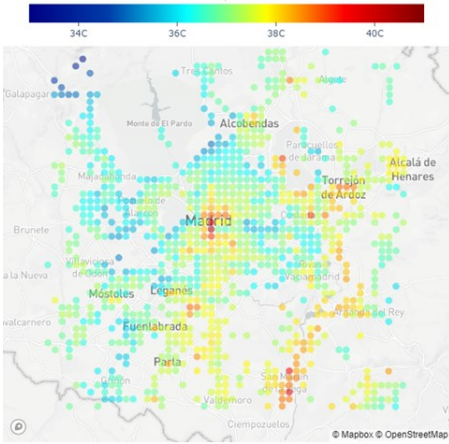


286  
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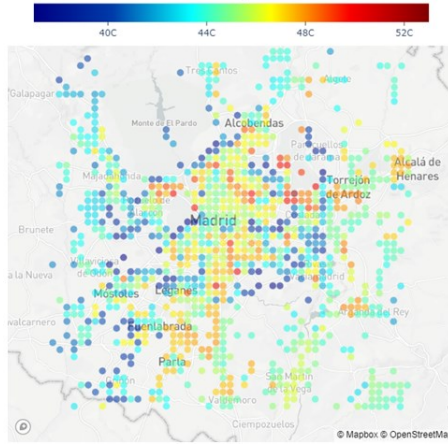


288 **Figure 9.** Spatial maps at 0900 UTC for 2-m air temperature (top left), surface temperature (top right), UTCI cool spot e. g. the 10  
 289 percentile of UTCI captured in the urban canopy model (bottom left), and UTCI hot spot e. g. 90 percentile of UTCI in the urban canopy  
 290 (bottom right). Surface temperature is equivalent to that seen by a nadir-view satellite sensor (i.e., an area-weighted average of canopy  
 291 ground temperature, roof temperature, and vegetation temperature in non-urban fractions is considered). The underlying maps were created  
 292 with Mapbox OpenStreetMap  
 293

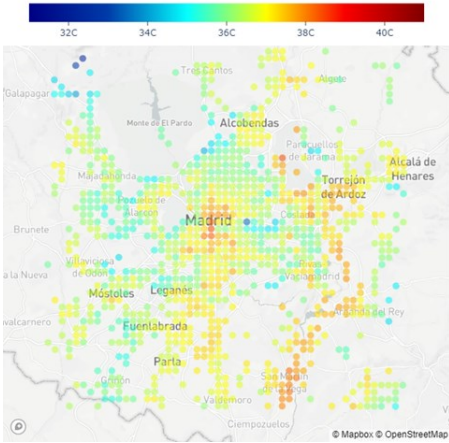
Air temperature



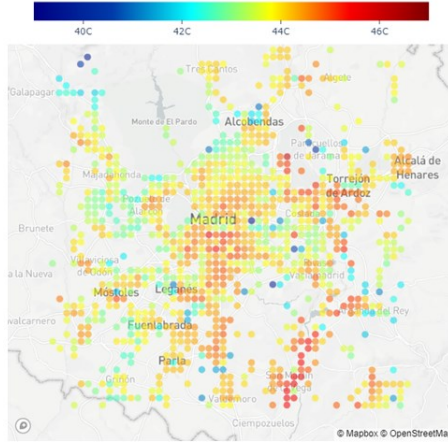
Surface temperature



UTCI (Cool spot)



UTCI (Hot spot)





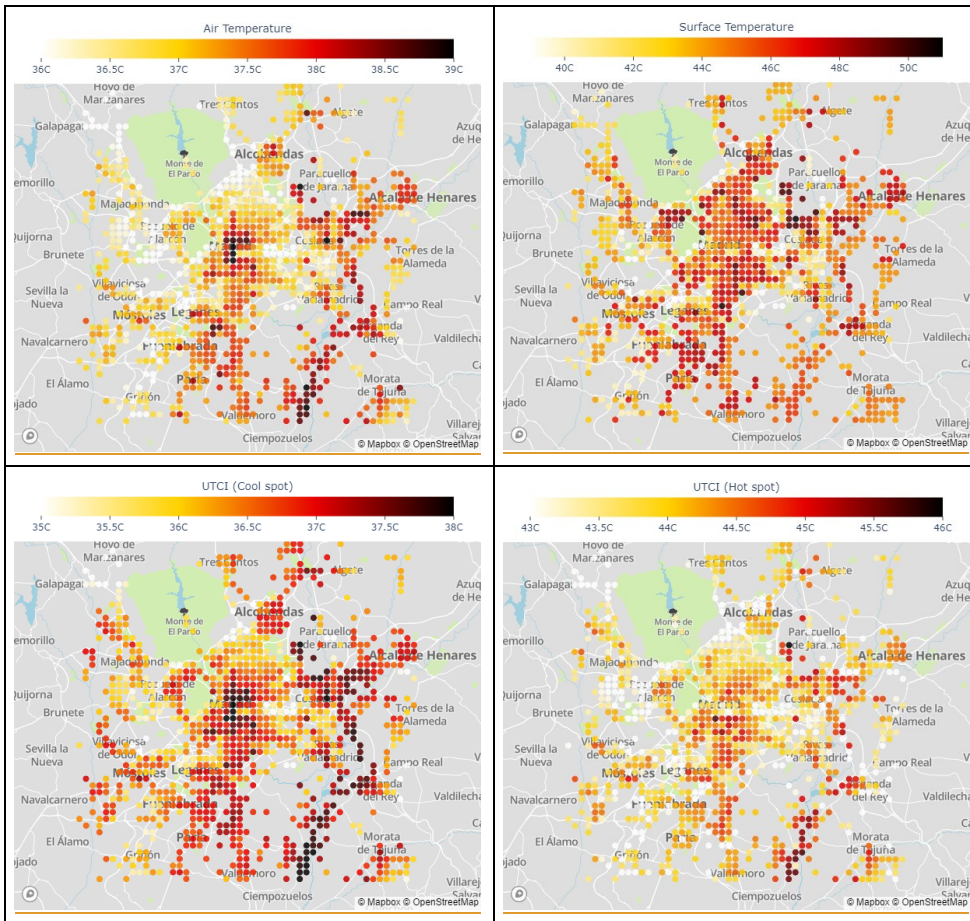


Figure 10. Same as Figure 9, but at 1600 UTC.

#### 4. Limitations

The main limitation of the approach we proposed here to account for the sub-grid variability of mean radiant temperature, is the idealization of the urban morphology adopted by the urban canopy parameterization BEP-BEM. This consists of

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302 representing the urban morphology as a series of infinite urban canyons, all with the same width, separated by buildings of  
303 constant width, and variable building height. Two street orientations are considered for each grid cell: North-South, and East-  
304 West. The dimensions of the buildings and street canyons are determined such that the building plan area density, the density  
305 of urban vertical surfaces per horizontal area, and the mean building height are equal to those of the real morphology of the  
306 grid cell. ~~As a result~~Thanks to this, the total surface areas of walls, roads and roofs ~~are the same~~ in the idealized morphology  
307 used by BEP-BEM ~~closely approximate the corresponding surface areas in the real neighbourhood and in the real one~~, and –  
308 to a certain extent – the street and buildings of the idealized morphology can be considered representatives of an ~~average~~the  
309 “mean” street and ~~set of buildings~~ present in the grid cell. The advantage of ~~this~~such approach, common ~~among~~to the most  
310 widely-used urban canopy parameterizations (Masson, 2000, Kusaka et al. 2001), is that it allows ~~to~~accurately estimatione of  
311 shadowing and radiation trapping effects in the urban canopy ~~with~~at low computational cost, without considering the real urban  
312 morphology. Keeping the computational cost low was an essential requirement considering the computational resources  
313 available when these urban canopy parametrizations were developed (about 20 years ago). With today’s ~~computational~~  
314 resources, ~~there may be potential~~this requirement can probably be relaxed to account for more complexity in the urban  
315 morphology. However, this would require deep changes in the structure of the urban canopy parametrization BEP-BEM that  
316 are beyond the scope of the present article. ~~For this~~This is the reason ~~why~~we decided to keep the idealized morphology of  
317 BEP-BEM and estimate the mean radiant temperature in six locations representatives of the middle of the street and the  
318 sidewalks. So, the mean radiant temperatures computed are representatives of those six points of an “average~~mean~~” street in  
319 the grid cell. Indeed, in a grid cell of a mesoscale model (that typically has a size of the order of one km<sup>2</sup>) there is a variety of  
320 street and building dimensions and orientations, so the present approach ~~cannot capture the full spatial~~underestimates the real  
321 ~~sub-grid~~ variability of mean radiant temperature, ~~a variability that increases and such underestimation increases~~  
322 the heterogeneity of the real urban morphology. Nevertheless, it represents a step forward, since it accounts for the ~~range (and to~~  
323 ~~some extent, the~~ variability) of mean radiant temperature within the “average~~mean~~” idealized street canyon, that can be  
324 reasonably considered the most likely street typology within the grid cell, something that previous approaches does not.  
325 Overall, the current approach is likely to accurately quantify the mean radiant temperature of at least one “average” shaded  
326 pedestrian and one “average” sunlit pedestrian (during periods with direct shortwave irradiance), and thus capture the largest  
327 source of spatial variation of both MRT and UTCI (Middel and Krayenhoff, 2019). Another limitation of the approach  
328 presented here is the lack of street trees. Currently work ~~is~~ in progress to introduce trees in the version of BEP-BEM  
329 implemented in WRF ~~via implementation of the BEP-Tree model~~ (Krayenhoff et al. 2020), and in this way ~~be able to~~account  
330 for their impacts on mean radiant temperature ~~as well as on air temperature, humidity, and wind~~.

331 The approach used to estimate the mean wind speed and its sub-grid variability is grounded on a large number of CFD  
332 simulations over a variety of urban morphologies. Indeed, as shown in Fig. 3, the sub-grid variability of wind speed can be  
333 quite large, and certainly strongly influenced by the relative arrangements of buildings and streets. So, the approach presented  
334 here will likely underestimate the sub-grid variability of wind speed – and this is why we decided to give the same likelihood

Con formato: Superindice

335 to the three values of wind speed estimated in (6), instead of assuming a Gaussian distribution of the probabilities of wind  
336 speed in the grid cell. To fully capture this variability a complete coupling between the mesoscale and a detailed CFD  
337 model would be needed - something that we may be able to do in the near future, but is still unavailable we still cannot do with  
338 current computational resources. Another limitation of the present approach is that the CFD simulations used to build the  
339 database from which the parametrization has been derived; are all for a neutral atmosphere, so thermal effects on wind speed  
340 and its sub-grid variability are neglected.

#### 341 5.4. Conclusions

342 A new parameterization to quantify intra-neighborhood/neighborhood heat stress variability in urban areas using a mesoscale  
343 model is presented. This approach is based on two primary developments: 1) calculation of mean radiant temperature at several  
344 locations within the idealized urban morphology used by the urban canopy model BEP-BEM; and 2) parameterization of mean  
345 wind speed and its sub-grid spatial variability as a function of the local urban morphology and the mean wind velocity  
346 computed by the WRF mesoscale model, using relations developed from a large suite of CFD simulations over a range of  
347 realistic and idealized urban neighborhoods. The components of the new parameterization have been validated against  
348 microscale model results. From this approach the sub-grid variability of a heat stress index (i.e. UTCI or SET) can be computed  
349 for every grid point, permitting quantification of the heat exposure at both cool and hot locations within each grid square at  
350 each time.

351 The new parameterization has been implemented in the multilayer scheme BEP-BEM in WRF and used to simulate a heatwave  
352 day over Madrid (Spain) as proof of concept. The results of this initial application demonstrate the following:

- 353 I. The new parameterization gives information that is more suitable for the evaluation of heat stress than the air  
354 temperature, being based on an index (UTCI or SET) that also combines air humidity, wind speed, and mean radiant  
355 temperature.
- 356 II. The new parameterization provides substantively more information than air temperature alone (or any other index  
357 that does not account for the mean radiant temperature). It provides information about the sub-grid variability (such  
358 that heat stress in both cool and hot locations in each grid square is quantified). To our knowledge, this has ~~not~~  
359 been done before with a mesoscale model.
- 360 III. The results for the investigated case, indicate a strong intraurban variability, both in air temperature and UTCI values,  
361 that can be linked to the differences in urban morphology and elevation above sea level. The ability to assess the  
362 differential impacts of urban morphology on heat stress is key to the provision of guidance for urban planning  
363 strategies that mitigate urban overheating.
- 364 IV. Nadir-view surface temperature (i.e., as seen from a satellite-mounted remote sensor) is poorly correlated with both  
365 air temperature and UTCI maps, indicating that, despite its ubiquitous use at present, it is unlikely to be an adequate  
366 metric for heat impact assessment studies.



367 Finally, we consider that this new development introduces a new methodology for deploying mesoscale models to assess urban  
368 overheating mitigation strategies.  
369

370

371 ***Code Availability***

372 The code of WRF-comfort can be obtained here:

373 <https://doi.org/10.5281/zenodo.7951433>

374 The results of the simulation over Madrid shown in the manuscript are stored here:

375 <https://zenodo.org/record/8199017>

376

377 ***Competing interests***

378 The authors declare that they have no conflict of interest

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515 Appendix A. Computation of Radiation for Mean Radiant Temperature

516 As explained in the text, the mean radiant temperature at pedestrian level is represented using formula (1). The full expression  
517 of the longwave radiation components for the vertical faces of the pedestrian ( $L_1, L_2$ ), for the case of an urban morphology  
518 with buildings of constant height and walls with no windows, is as follows:

519 
$$L_1 = \sum_{i=1,n} \psi_{1i,p} \varepsilon_W (Rl_{1W_i} + \sigma T_{1i}^4) + \psi_{1G,p} \varepsilon_G (Rl_G + \sigma T_G^4) + \psi_{1S,p} Rl_S$$

520 
$$L_2 = \sum_{i=1,n} \psi_{2i,p} \varepsilon_W (Rl_{2W_i} + \sigma T_{2i}^4) + \psi_{2G,p} \varepsilon_G (Rl_G + \sigma T_G^4) + \psi_{2S,p} Rl_S$$

521 Where (see Fig A1):

522  $\psi_{1i,p}$  is the view factor from wall section  $i$  of building 1 to the side 1 of the pedestrian

523  $\varepsilon_W$  is the emissivity of the wall

524  $Rl_{1W_i}$  is the long wave radiation reaching the section  $i$  of the wall of building 1

525  $T_{1i}$  is the surface temperature of the section  $i$  of the wall of building 1

526  $\psi_{1G,p}$  is the view factor from the ground (or street) to the side 1 of the pedestrian

527  $\varepsilon_G$  is the emissivity of the ground

528  $Rl_G$  is the longwave radiation reaching the ground (street)

529  $T_G$  is the surface temperature of the ground (street)

530  $\psi_{1S,p}$  is the view factor from the sky to side 1 of the pedestrian

531  $Rl_S$  is longwave radiation from the sky

532  $\sigma$  is the Stefan-Boltzmann constant.

Con formato: Fuente: Cursiva



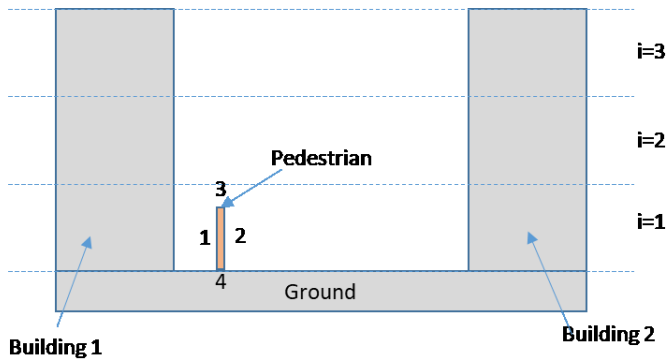


Figure A1. Schematic of the Street canyon.

Similar meaning applies for side and building 2.

The values of the surface temperatures and the longwave radiations are computed with BEP BEM. The view factors are estimated based on formulas A13-A19 of Martilli et al. 2002, using a height for the pedestrian of 1.8 m.

For the longwave radiation reaching the top of the pedestrian, we made the simple assumption that it is equal to the radiation coming from the sky,  $L_3 = Rl_s$ , while for the longwave radiation reaching the bottom of the pedestrian, the assumption is that it is equal to the radiation emitted and reflected by the ground, or  $L_4 = \epsilon_g Rl_g + \epsilon_g \sigma T_g^4$ . We consider that these assumptions are reasonable, giving that the contribution of the radiation reaching the top and bottom of the pedestrian is only 6% each to the final value of the mean radiant temperature.

A similar approach is followed for the short wave radiation, leading to:

$$K_1 = \sum_{i=1,n} \psi_{1i,p} \alpha_i R_{s_{1W_i}} + \psi_{1G,p} \alpha_G R_{s_G} + R_{s_{1S}}$$

$$K_2 = \sum_{i=1,n} \psi_{2i,p} \alpha_i R_{s_{2W_i}} + \psi_{2G,p} \alpha_G R_{s_G} + R_{s_{2S}}$$

Where

$R_{s_{1W_i}}$ =short wave radiation reaching the section  $i$  of the wall of building 1

$\alpha_i$ =albedo of the section  $i$  of the wall of the building

Con formato: Fuente: Cursiva

550  $RS_G$  is the short wave radiation reaching the ground

551  $\alpha_G$  is the albedo of the ground

552  $RS_{1S}$  is the short wave radiation from the sun reaching directly side 1 of the pedestrian, computed using formula A10 of

553 Martilli et al. 2002, using a height of the pedestrian of 1.8m.

554 Similar meaning for side and wall 2.

555 Regarding the radiation reaching the top of the pedestrian,  $K_3$ , for simplicity only the radiation coming directly from the sun

556 is considered, without accounting for the reflection from the walls. So the value is zero if the pedestrian is in full shadow, and

557 to estimate it, the formula used is from A11 of Martilli et al. 2002. The value of the radiation reaching the bottom of the

558 pedestrian is the value reflected by the ground, or  $K_3 = \alpha_G RS_G$ .

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Appendix **BA**. *Comparison of Short wave calculation in BEP-BEM and TUF-pedestrian.*

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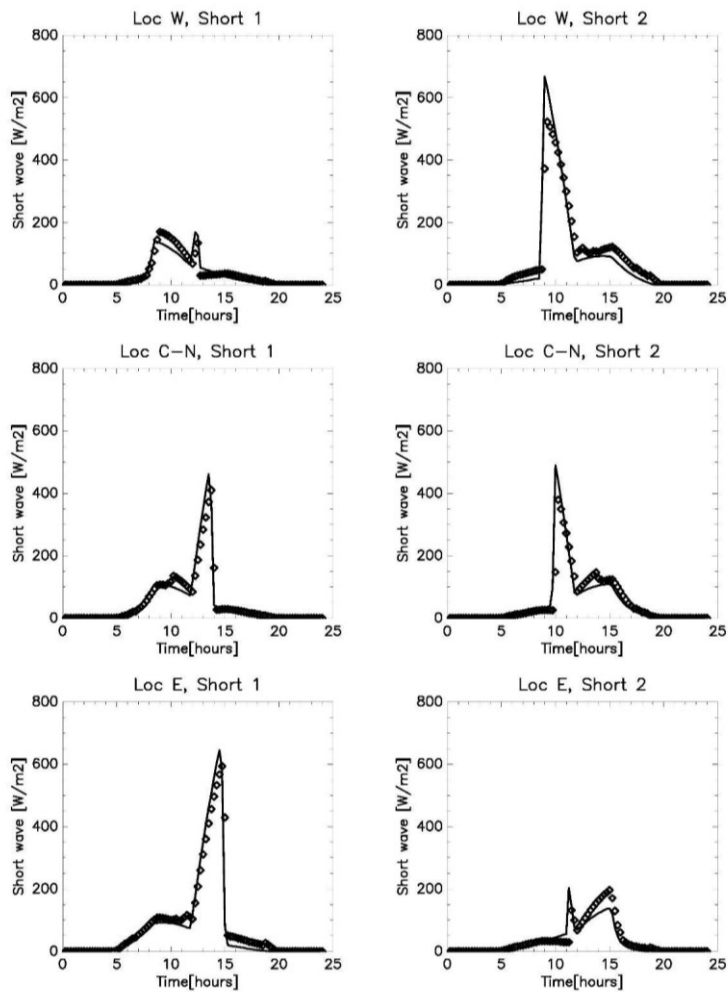
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Short wave radiation is an essential component of the MRT. Below we compare the short wave radiation reaching the vertical sides of the segment representing the human body computed by BEP-BEM vs those estimated with the more detailed model TUF-pedestrian.

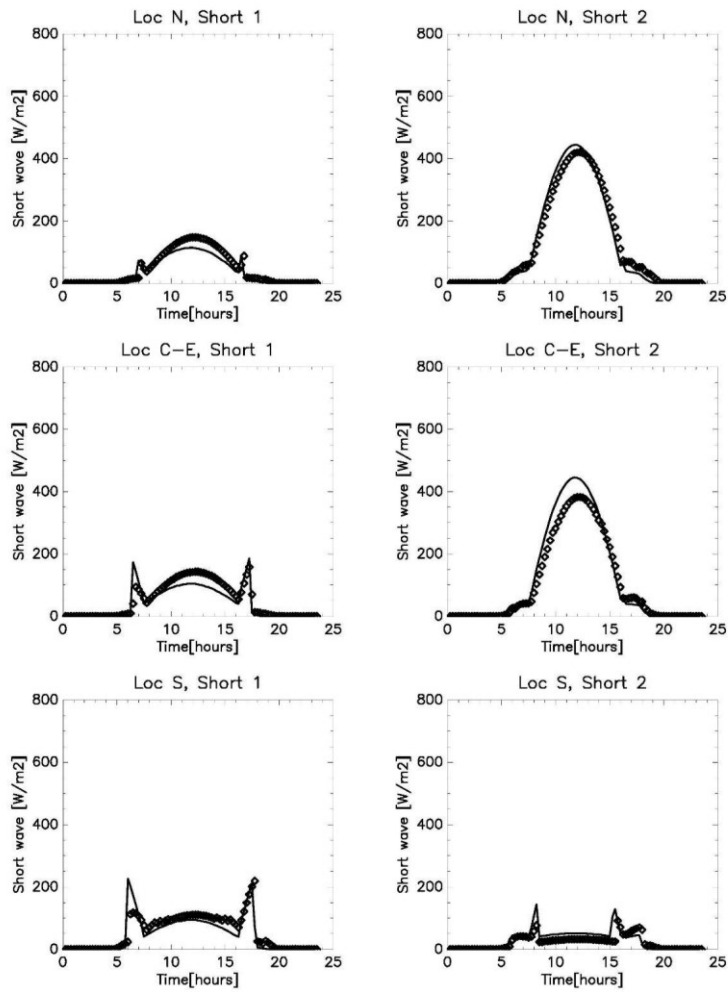
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566  
 567 Figure BA.1. Comparison of short wave radiation at the two sides of the vertical segment representing the pedestrian for the  
 568 N-S oriented street. Solid line is the WRF, while diamonds are TUF. Short 1 means the side 1 of the pedestrian, while Short 2  
 569 the side 2.



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572 Figure BA.2. Same as BS1, but for an E-W oriented street

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### Appendix C.B. CFD simulations for wind speed variability

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Data from over 173 microscales CFD simulations of urban airflow are considered over realistic and idealized urban configurations, spanning a wide range of building plan area ( $\lambda_p$ ), frontal area ( $\lambda_f$ ), and wall area ( $\lambda_w$ ) densities representative of realistic urban neighborhoods in different types of cities. CFD simulations are conducted using 162 large-eddy simulations (LES) and 11 Reynolds-averaged Navier–Stokes (RANS) schemes detailed in Table B.1.

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Table B.1 Details of CFD microscale simulation cases considered in this study. Simulations are classified based on the configuration (urban form) used. These classifications include **UA** (Uniform height with **A**ligned configuration), **US** (Uniform height with **S**taggered configuration), **VA** (Variable height with **A**ligned configuration), **VS** (Variable height with **S**taggered configuration), **UR** (Uniform height with **R**ealistic configuration), and **VR-WD** (Variable height with **R**ealistic configuration and multiple **W**ind **D**irections considered).

Model	Classification	$H_m$ [m]	$H_{max}$ [m]	$\lambda_p$ range	Count	Source	Example
LES	UA	16	16	[0.0625 - 0.64]	7	Nazarian et al. 2020 Lu et al. 2022	
LES	US	16	16	[0.0625 - 0.64]	7	Nazarian et al. 2020 Lu et al. 2022	
LES	VA	16	20, 24	[0.0625 - 0.64]	42	Lu et al. 2022 Lu et al. 2023	
LES	VS	16	20, 24	[0.0625 - 0.64]	42	Lu et al. 2022 Lu et al. 2023	
LES	UR	16	16	[0.057 - 0.536]	64	Lu et al. 2022	
RANS	VR-WD	14.5-34	variable	[0.190 - 0.680]	11	Sanchez et al. (2017) Santiago et al. (2017) Kracht et al. (2017) Borge et al. (2018) Kracht et al. (2019) Santiago et al. (2020) Sanchez et al. (2021)	

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In the LES simulations, airflow over idealized and realistic urban arrays to determine the model parameters (Nazarian et al., 2020; Lu et al., 2022, 2023). Realistic urban layouts are prepared by rasterizing building footprints from an open-source dataset OpenStreetMap using OSM2LES (Lu et al., 2022). 64 realistic urban neighborhoods were obtained assuming uniform building height (Table B.1) from several major cities such as Sydney and Melbourne (Australia), Barcelona (Spain), Detroit,

585 Los Angeles, and Chicago (United States). Idealized urban arrays are considered in aligned and staggered arrangement that  
586 follows (Coceal et al., 2007) with varying urban density ( $\lambda_p$  in [0.0625,0.64]) and height variability ( $H_{std}=[0m,2.8m,5.6m]$ ).  
587 Simulations are conducted in the Parallelized Large-eddy Simulation Model (PALM, version r4554) (Maronga et al., 2020)  
588 following the same setup in (Nazarian et al., 2020), which has validated results against Direct Numerical Simulation (Coceal  
589 et al., 2007) and wind tunnel experiments (Brown et al., 2001). The computational domain is discretized using the second-  
590 order central differences (Piacsek and Williams, 1970) where the horizontal grid spacing is uniform and the vertical spacing  
591 follows the staggered Arakawa C-grid. The minimal storage scheme is employed in the time integration to solve the filtered  
592 prognostic incompressible Boussinesq equations where the pressure perturbation was calculated in Poisson's equation and was  
593 solved by the FFTW scheme (Frigo and Johnson, 1998).

594 The RANS dataset is derived from steady-state CFD-RANS simulations performed with the Realizable k- $\epsilon$  turbulence model  
595 (STAR-CCM+, Siemens) over realistic urban areas. The size of the computational domains is determined following the best  
596 practice guideline of COST Action 732 (Franke et al., 2010). The horizontal area covers around 1-1.5 km<sup>2</sup> and the domain top  
597 is at around 8H, being H the mean height of buildings. The resolution of the irregular polyhedral mesh used in all CFD-RANS  
598 simulations goes from 0.5 m close to buildings to 6 m out of the built-up area, which results in between 3 and 8 million grid  
599 points depending on the complexity of the geometry. Inlet vertical profiles for wind speed, turbulent kinetic energy (k), and  
600 its dissipation ( $\epsilon$ ), are established in neutral atmospheric conditions. The evaluation of the CFD-RANS simulations was  
601 addressed in previous studies summarized in Table B2 and more information is provided in previous publications.

602