

1    **Boundary of nighttime ozone chemical equilibrium in the mesopause region: long-**  
2    **term evolution ~~from~~determined using 20-year satellite observations**

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8

9 **Abstract.** The assumption of nighttime ozone chemical equilibrium (NOCE) is widely ~~usedemployed~~ for  
10 ~~retrieval of retrieving~~ the  $O_x$ - $HO_x$  components in the mesopause from rocket and satellite measurements.  
11 In this work, ~~the~~ recently developed analytical criterion of determining the NOCE boundary is ~~applied~~  
12 ~~(4) used (i) to study of the~~ connection of this boundary with O and H spatiotemporal variability ~~basing based~~  
13 on ~~the~~ 3D ~~modeling of~~ chemical transport ~~modeling~~, and (2ii) to retrieve and analyze the spatiotemporal  
14 evolution of the NOCE boundary in 2002-2021 from ~~the~~ SABER/TIMED data set. It was revealed, first,  
15 that the NOCE boundary ~~well~~ reproduces ~~well~~ the transition zone dividing deep and weak ~~diurnal~~  
16 ~~photochemical~~ oscillations of O and H ~~at the low and middle latitudes caused by the diurnal variations of~~  
17 ~~solar radiation~~. Second, the NOCE boundary is sensitive to sporadic abrupt changes in the middle  
18 atmosphere dynamics, in particular, due to powerful sudden stratospheric warmings leading to ~~the~~ events  
19 of ~~an~~ elevated (up to  $\sim$ 80 km) stratopause, which took place in January-~~February~~~~March~~ 2004, 2006, 2009,  
20 2010, 2012, 2013, 2018, and 2019. Third, the space-time evolution of this ~~characteristics~~characteristic  
21 expressed via pressure-~~height~~ altitude contains a clear signal of 11-year solar cycle in the ~~range of~~ 55°S-  
22 55°N range. In particular, ~~averagethe mean~~ annual ~~the~~ NOCE boundary averaged in this range of latitudes  
23 anticorrelates well with  $F_{10.7}$  index with the coefficient ~~of~~ -0.9695. Moreover, it shows a weak linear trend  
24 of ~~49~~the  $56.2 \pm 3642.2$  m/decade.

## 26 1 Introduction

27 The mesopause (80-100 km) is an interesting region of ~~Earth~~the Earth's atmosphere possessing  
28 quite a number of unique phenomena and processes which can be considered as sensitive  
29 indicators/predictors of global climate change and anthropogenic influences on atmospheric composition  
30 (e.g., (Thomas et al., 1989)). Here, the summer temperature at middle and high latitudes ~~in the summer~~  
31 reaches its lowest values (down to 100K (Schmidlin, 1992)). The temperatures below 150K lead to water  
32 vapour condensation and formation of the highest altitude clouds ~~on Earth~~in the Earth's atmosphere, the  
33 so-called Polar Mesospheric Clouds or Noctilucent Clouds, consisting primarily of water ice (Thomas,  
34 1991). In ~~opposite~~turn, the temperature of the winter mesopause is essentially higher, so there is a strong  
35 negative temperature gradient between the summer and winter hemispheres. At these altitudes,  
36 atmospheric waves ~~with of~~ various spatiotemporal scales are observed, in particular, internal gravity  
37 waves coming from the lower atmosphere. Destruction of gravity waves leads to strong turbulence that  
38 affects the atmospheric circulation and ultimately manifests itself in the mentioned temperature structure  
39 of this region.

40 Many layer phenomena in the mesopause are ~~connected with~~related to the photochemistry of the  
41  $O_x$ - $HO_x$  components (O,  $O_3$ , H, OH, and  $HO_2$ ). ~~Here, there~~There is a narrow (in height) transition region

42 where photochemistry ~~behavior~~behaviour transforms rapidly from “deep” diurnal oscillations, when the  
43 difference between daytime and nighttime values of the  $O_x$ - $HO_x$  components can ~~re~~reach several orders  
44 of magnitude, to weak photochemical oscillations. As ~~the~~a result, above this region, ~~there takes place~~O  
45 and H ~~accumulation and their~~accumulate to form the corresponding layers. This layer formation  
46 ~~manifesting~~manifests ~~itself~~itself in the appearance of a secondary ozone maximum and airglow layers of OH  
47 and O excited states. Thus,  $O_x$ - $HO_x$  photochemistry in the mesopause is responsible for the presence of  
48 important (first of all, from a practical point of view) indicators observed in the visible and infrared  
49 ranges, which are widely used for ground-based and satellite monitoring of climate changes and  
50 ~~waves~~wave activity. Moreover,  $O_x$ - $HO_x$  photochemistry provides the total chemical heating rate of this  
51 region, influences the radiative cooling and other useful airglows (for example, by  $O_2$  excited states),  
52 ~~involves~~is involved in the plasma-chemical reactions and formation of layers of the ionosphere ~~layers~~.  
53 The mentioned transformation of  $O_x$ - $HO_x$  ~~behavior~~behaviour with height may ~~happens~~occur via the  
54 nonlinear response of  $O_x$ - $HO_x$  photochemistry to the diurnal variations of solar radiation in the form of  
55 subharmonic (with periods of 2, 3, 4, and more days) or ~~the~~ chaotic oscillations (e.g., Sonnemann and  
56 Fichtelmann, 1997; Feigin et al., 1998). This unique phenomenon was predicted many years ago (e.g.,  
57 Sonnemann and Fichtelmann, 1987) and investigated theoretically by models ~~with~~ taking into account ~~of~~  
58 different transport processes (e.g., Sonnemann and Feigin, 1999; Sonnemann et al., 1999; Sonnemann and  
59 Grygalashvily, 2005; Kulikov and Feigin, 2005; Kulikov, 2007; Kulikov et al., 2020). It was revealed, in  
60 particular, ~~that~~ the ~~appearance of~~ nonlinear response is controlled by ~~the~~ vertical eddy diffusion  
61 (Sonnemann and Feigin, 1999; Sonnemann et al., 1999), so that 2-day oscillations can only survive at ~~the~~  
62 real diffusion coefficients, but the eddy diffusion in zonal direction leads to the appearance of the so-  
63 called reaction-diffusion waves in the form of propagating phase fronts of 2-day oscillations (Kulikov and  
64 Feigin, 2005; Kulikov et al., 2020). Recently, the satellite data processing ~~found~~revealed the first  
65 evidence ~~that of the existence of~~ 2-day photochemical oscillations ~~exist~~ in the real mesopause (Kulikov et  
66 al., 2021).

67 While regular remote sensing measurements of most  $O_x$ - $HO_x$  components are still limited, the  
68 indirect methods based on the physicochemical assumptions are useful tools ~~to monitor~~for monitoring  
69 these trace gases. In many papers, ~~the~~ O and H distributions were retrieved from the daytime and  
70 nighttime rocket and satellite measurements of the ozone and the volume emission rates of OH(v),  $O(^1S)$ ,  
71 and  $O_2(a^1\Delta_g)$  (e.g., Good, 1976; Pendleton et al., 1983; McDade et al., 1985; McDade and Llewellyn,  
72 1988; Evans et al., 1988; Thomas, 1990; Llewellyn et al., 1993; Llewellyn and McDade, 1996; Mlynczak  
73 et al., 2007, 2013a, 2013b, 2014, 2018; Smith et al., 2010; Xu et al., 2012; Siskind et al., 2008, 2015).  
74 The retrieval technique is based on the assumption of ~~the~~-ozone photochemical/chemical equilibrium and

75 physicochemical model of the corresponding airglow, which describe the ~~relations~~relationship between  
76 local O and H values and ~~the~~ measurement data.

77 The daytime photochemical ozone equilibrium is a good approximation everywhere in the  
78 mesosphere ~~—~~ lower thermosphere (MLT) region (Kulikov et al., 2017) due to ozone photodissociation,  
79 whereas the applicability of the assumption of nighttime ozone chemical equilibrium (NOCE) is limited:  
80 there is an altitude boundary ~~upper~~above which NOCE is satisfied ~~with~~to ~~an~~ accuracy better than 10%.  
81 Below this boundary, the ozone equilibrium is disturbed essentially and cannot be used. Good (1976)  
82 supposed that NOCE is fulfilled above 60 km, whereas other papers apply the NOCE starting from 80  
83 km, independent of latitude and season. However, studies of NOCE within the framework of the 3D  
84 chemical-transport models (Belikovich et al., 2018; Kulikov et al., 2018a) revealed that the NOCE  
85 boundary ~~of NOCE~~ varies within the range of 81–87 km, depending on latitude and season. ~~Due to In~~  
86 view of the practical ~~necessity~~need to determine the local altitude position of this boundary, Kulikov et al.  
87 (2018a) presented a simple criterion ~~localizing of determining~~ the equilibrium boundary using only the  
88 data provided by the SABER (Sounding of the Atmosphere using Broadband Emission Radiometry)  
89 instrument onboard the TIMED (Thermosphere Ionosphere Mesosphere Energetics and Dynamics).  
90 Using~~Making use of~~ this criterion, Kulikov et al. (2019) retrieved the annual evolution of the NOCE  
91 boundary from the SABER data. It was revealed that ~~the~~a two-month averaged NOCE boundary  
92 essentially depends on season and latitude and can rise up to  $\sim$  86 km. Moreover, the analysis of the  
93 NOCE boundary in 2003–2005 showed that this characteristic was sensitive to unusual dynamics of  
94 stratospheric polar vortex during the 2004 Arctic winter ~~2004~~, which was named ~~as~~a remarkable winter in  
95 the 50-year record of meteorological analyses (Manney et al., 2005). Moreover, Belikovich et al. (2018)  
96 found by 3D simulation that the excited OH layer ~~well~~ repeats well spatiotemporal variability of the  
97 NOCE boundary. These results ~~let~~allowed us to speculate that the NOCE boundary can be considered as  
98 an important indicator of ~~mesopause~~mesopause processes.

99 The main goals of this paper are (1) to investigate the ~~connection of~~relationship between the NOCE  
100 boundary according to the mentioned criterion ~~with~~and O and H variability with the use of the 3D  
101 chemical transport model, and (2) to retrieve and analyze the spatiotemporal evolution of the NOCE  
102 boundary in 2002–2021 from the SABER/TIMED data set. In the next section, we present the used model.  
103 In Section 3, we briefly describe ~~shortly~~ the criterion ~~to determine of~~determining the NOCE boundary  
104 local height and study how this height ~~relates with~~is related to the features of O and H distributions from  
105 the 3D model. Section 4 explains the methodology of determining the NOCE boundary from satellite  
106 data. Section 5 presents the main results obtained from SABER/TIMED data, ~~which are~~ discussed in  
107 Section 6.

109 **2 3D model**

110 We use the 3D chemical transport model of the middle atmosphere developed by the Leibniz  
 111 Institute of Atmospheric Physics (e.g., Sonnemann et al., 1998; Körner and Sonnemann, 2001;  
 112 Grygalashvily et al., 2009; Hartogh et al., 2004, 2011). The three-dimensional fields of temperature and  
 113 winds were adopted by Kulikov et al. (2018b) from the Canadian Middle Atmosphere Model (Scinocca et  
 114 al., 2008) for the year 2000 with an updated frequency of 6 hours. To exclude unrealistic jumps in the  
 115 evolution of calculated chemical characteristics, a-linear smoothing between two subsequent updates of  
 116 these parameters is applied. The model takes into account 3D advective transport and vertical diffusive  
 117 transport (both, turbulent and molecular). The Walcek-scheme (Walcek, 2000) and the implicit Thomas  
 118 algorithm (Morton and Mayers, 1994) are used for advective and diffusive transport, respectively. The  
 119 model grid includes 118 pressure-height levels (from the ground to  $\sim$ 135 km), 32 and 64 levels in latitude  
 120 and longitude, respectively. The chemical part considers 22 constituents ( $O$ ,  $O(^1D)$ ,  $O_3$ ,  $H$ ,  $OH$ ,  $HO_2$ ,  
 121  $H_2O_2$ ,  $H_2O$ ,  $N$ ,  $NO$ ,  $NO_2$ ,  $NO_3$ ,  $N_2O$ ,  $CH_4$ ,  $CH_2$ ,  $CH_3$ ,  $CH_3O_2$ ,  $CH_3O$ ,  $CH_2O$ ,  $CHO$ ,  $CO$ ,  $CO_2$ ), 54 two-  
 122 and three-body reactions, and 15 photo-dissociation reactions. The model uses pre-calculated  
 123 dependences of dissociation rates on the altitude and solar zenith angle (Kremp et al., 1999).  
 124 For the The chemistry calculation, we apply is calculated by the Shimazaki scheme (Shimazaki, 1985)  
 125 at for the integration time of 9 sec.

127 **3 The NOCE criterion**

128 The nighttime ozone chemistry at the mesopause heights is determined mainly by two reactions R1-  
 129 R2 (e.g., Allen et al., 1984), see Table 1. Thus, The secondary ozone loss via the  $O + O_3 \rightarrow 2O_2$  reaction  
 130 becomes important above  $\sim$  95 km (Smith et al., 2009). Kulikov et al. (2023) verified with simulated and  
 131 measured data that this reaction does not influence the NOCE boundary determination and may be  
 132 skipped. Thus, the ozone equilibrium concentration ( $O_3^{eq}$ ) corresponding to the instantaneous balance  
 133 between the production and loss terms is as follows:

$$134 O_3^{eq} = \frac{k_1 \cdot O \cdot O_2 \cdot M}{k_2 \cdot H}, \quad (1)$$

135 where  $M$  is air concentration, and  $k_{1-2}$  are the corresponding rate constants of the reactions (see Table 1).

136 As mentioned above, the NOCE criterion was developed in Kulikov et al. (2018a). The main idea is  
 137 that the local values of  $O_3$  and  $O_3^{eq}$  are close to each other ( $O_3(t) \approx O_3^{eq}(t)$ ), when  $\tau_{O_3} \ll \tau_{O_3^{eq}}$ , where  
 138  $\tau_{O_3}$  is the ozone lifetime and  $\tau_{O_3^{eq}}$  is the local time scale of  $O_3^{eq}$ .

139  $\tau_{O_3} = \frac{1}{k_2 \cdot H}$ , (2)

140  $\tau_{O_3}^{eq} \equiv \frac{O_3^{eq}}{|dO_3^{eq}/dt|} = \frac{O}{H \cdot \left| \frac{d(O)}{dt(H)} \right|}$  (3)

141 As shown in Kulikov et al. (2018a),  $\tau_{O_3}^{eq}$  can be determined from a simplified photochemical model  
 142 describing the  $O_x$ - $HO_x$  evolution in the mesopause region (Feigin et al., 1998), so the criterion ~~for validity~~  
 143 of the NOCE validity can be written in the form:

144  $Cr = \frac{\tau_{O_3}}{\tau_{O_3}^{eq}} = 2 \frac{k_1 \cdot k_4 \cdot O_2^2 \cdot M^2}{k_2} \left( 1 - \frac{k_5 + k_6}{k_3} \right) \cdot \frac{1}{k_2 \cdot H \cdot O_3} \ll 1$  (4)

145 where  $k_i$  are the corresponding reaction constants from Table 1. Calculations with the global 3D  
 146 chemistry-transport model of the middle atmosphere showed (Kulikov et al. 2018a) that the criterion  
 147  $\tau_{O_3}/\tau_{O_3}^{eq} \leq 0.1$  ~~well~~ defines well the boundary of the area where  $|O_3/O_3^{eq} - 1| \leq 0.1$ .

148 Kulikov et al. (2023) presented the theory of chemical equilibrium of a certain trace gas  $n$ . Strictly  
 149 mathematically, the cascade of ~~the~~ sufficient conditions for  $n_i(t) \cong n_i^{eq}(t)$  was derived considering its  
 150 lifetime, equilibrium concentration, and time dependences of these characteristics. In case of the  
 151 nighttime ozone, it was proved that ~~the~~  $\tau_{O_3}/\tau_{O_3}^{eq} \ll 1$  is the main condition for NOCE validity and the  
 152 criterion  $\tau_{O_3}/\tau_{O_3}^{eq} \leq 0.1$  limits ~~the~~ possible difference between  $O_3$  and  $O_3^{eq}$  to ~~be not~~ more than  
 153 ~10%. Moreover, Kulikov et al. (2023) slightly corrected the expression for the criterion (4):

154  $Cr = 2 \frac{k_1 \cdot O_2 \cdot M}{k_2} (k_4 \cdot M \cdot O_2 \cdot \left( 1 - \frac{k_5 + k_6}{k_3} \right) + k_2 \cdot O_3) \cdot \frac{1}{k_2 \cdot H \cdot O_3} \leq 0.1$  (5)

155 Other~~One more~~ important condition for  $O_3 \approx O_3^{eq}$  at the time moment  $t$  is:

156  $e^{\int_{t_{bn}}^t \tau_{O_3}^{-1} dt} \gg 1$ , (6)

157 where  $t_{bn}$  is the time of the beginning of the night. ~~It means the nighttime data measured near the The~~  
 158 ~~ozone equilibrium concentration jumps at sunset should be excluded from consideration due to the~~  
 159 ~~shutdown of photodissociation. Thus, the condition (6) shows that it takes time for the ozone~~  
 160 ~~concentration to reach a new equilibrium.~~ Kulikov et al. (2023) revealed that, at the solar zenith angle  $\chi >$   
 161 ~~95°, the condition (6) is fulfilled in almost in all cases. and the condition (5) becomes the main criterion~~  
 162 ~~for NOCE validity. In addition, Kulikov et al. (2023) demonstrated with the use of a 3-D model that the~~  
 163 ~~criterion (5) almost ideally reproduces the NOCE boundary found by direct comparison of  $O_3$  and  $O_3^{eq}$~~   
 164 ~~concentrations, see Figure 1 in Kulikov et al. (2023).~~

165 Figures 1-3 demonstrate model examples of O and H time-height variations above different points  
 166 ~~in over~~ three months. In order to focus ~~our~~ attention on diurnal oscillations, the concentrations are  
 167 normalized by mean daily values, ~~correspondingly which were calculated as a function of altitude. These~~

168 daily average O and H values were different for each altitude. One can see in all panels of these Figures,  
 169 first, below 81-87 km, figures "deep" diurnal oscillations that occur below 81-87 km. Due to the shutdown  
 170 of sources at night and high rates of the main HO<sub>x</sub> and O sinks nonlinearly dependent on air concentration  
 171 (Konovalov and Feigin, 2000), the variables change during each night within at the range of several orders  
 172 of magnitude with low values of time evolution. Above 83-88 km, the situation differs essentially  
 173 from the previous case. One can see the relatively weak diurnal oscillations. These regimes of O and H  
 174 behaviorbehaviour are in-consistenteach other, i.e. deep H diurnal oscillations correspond to the same  
 175 dynamics in O<sub>2</sub> and so on. There exists a few-km thick layer (transition zone) dividing deep and weak  
 176 oscillations whichwhose height position isdependeddepends on latitude and season. In particular, in  
 177 summer the middle latitude transition is higher than in winter. Figures 1-3 show also the magenta lines  
 178 pointing the NOCE boundary in accordance towith the criterion (5) (Cr = 0.1). One can see that the  
 179 NOCE criterion almost perfectly reproduces the features of the transition zone. Thus, our criterion is not  
 180 only the useful technical characteristic to retrieve O from satellite data, but it also points to an  
 181 important dynamical process in the O<sub>x</sub>-HO<sub>x</sub> photochemistry.

#### 183 4 Boundary of the NOCE boundary from satellite data

184 We use the version 2.0 of the SABER data product (Level2A) for the simultaneously measured  
 185 height profiles of pressure (p), altitude (z), temperature (T), O<sub>3</sub> (at 9.6  $\mu$ m), and total volume emission  
 186 rates of OH\* transitions at 2.0 (VER) within the 0.0001–0.02 mbar pressure interval (altitudes  
 187 approximately 75–105 km) in 2002-2021. We consider only nighttime data when the solar zenith angle  $\chi$   
 188 > 95°.

189 Kulikov et al. (2018a) noted that the term  $k_2 \cdot H \cdot O_3$  in the expression for the NOCE criterion can  
 190 be rewritten in the form dependeddepending on measurable characteristics only with the use of the  
 191 corresponding OH( $\nu$ ) model by Mlynczak et al. (2013a):

$$192 k_2 \cdot H \cdot O_3 = VER/A(T, M, O), \quad (7)$$

193 where  $A(T, M, O)$  is at the function in square brackets ofequationin Eq. (3) in the paper by Mlynczak et al.  
 194 (2013a) with the parameters corrected by Mlynczak et al. (2018):

$$195 A(T, M, O) = \frac{0.47 \cdot 118.35 / (215.05 + 2.5 \cdot 10^{-11} \cdot O_2 + 3.36 \cdot 10^{-13} \cdot e^{220/T} \cdot N_2 + 3 \cdot 10^{-10} \cdot O)}{O} + 0.34 \cdot 117.21 / (178.06 + 4.8 \cdot 10^{-13} \cdot O_2 + 7 \cdot 10^{-13} \cdot N_2 + 1.5 \cdot 10^{-10} \cdot O) + 0.47 \cdot \frac{117.21 / (215.05 + 2.5 \cdot 10^{-11} \cdot O_2 + 3.36 \cdot 10^{-13} \cdot e^{220/T} \cdot N_2 + 3 \cdot 10^{-10} \cdot O) - (20.05 + 4.2 \cdot 10^{-12} \cdot O_2 + 4 \cdot 10^{-13} \cdot N_2) / (178.06 + 4.8 \cdot 10^{-13} \cdot O_2 + 7 \cdot 10^{-13} \cdot N_2 + 1.5 \cdot 10^{-10} \cdot O)}{(178.06 + 4.8 \cdot 10^{-13} \cdot O_2 + 7 \cdot 10^{-13} \cdot N_2 + 1.5 \cdot 10^{-10} \cdot O)}$$

$$199 \quad \theta = \frac{\frac{0.47 \cdot 118.35}{215.05 + 2.5 \cdot 10^{-11} \cdot O_2 + 3.36 \cdot 10^{-13} \cdot e^{\frac{220}{T}} \cdot N_2 + 3 \cdot 10^{-10} \cdot O} + \frac{0.34 \cdot 117.21}{178.06 + 4.8 \cdot 10^{-13} \cdot O_2 + 7 \cdot 10^{-13} \cdot N_2 + 1.5 \cdot 10^{-10} \cdot O} +}{\frac{0.47 \cdot 117.21 \cdot (20.05 + 4.2 \cdot 10^{-12} \cdot O_2 + 4 \cdot 10^{-13} \cdot N_2)}{(215.05 + 2.5 \cdot 10^{-11} \cdot O_2 + 3.36 \cdot 10^{-13} \cdot e^{\frac{220}{T}} \cdot N_2 + 3 \cdot 10^{-10} \cdot O) \cdot (178.06 + 4.8 \cdot 10^{-13} \cdot O_2 + 7 \cdot 10^{-13} \cdot N_2 + 1.5 \cdot 10^{-10} \cdot O)}}. \quad (8)$$

200 This function is the result of the combination of the equations of physicochemical OH\* balance in the  $v = 8$  and  $v = 9$  states. It depends on the constants of the processes describing sources and sinks ~~on~~at the corresponding levels, in particular, the OH( $v$ ) removal ~~in~~on collisions with O<sub>2</sub>, N<sub>2</sub>, and O. Below 86-87 km,  $A(T, M, O) \cong A(T, M, O = 0) \equiv A(T, M)$  ~~because of due to~~ relativity small O concentrations. Thus, by combining Eqs. (5) and (7), the NOCE criterion for SABER data can be recast in the following form:

$$206 \quad VER \geq VER_{min}(T, M) = 20 \cdot \frac{k_1 \cdot O_2 \cdot M}{k_2} (k_4 \cdot O_2 \cdot M \cdot \left(1 - \frac{k_5 + k_6}{k_3}\right) + k_2 \cdot O_3) \cdot A(T, M) \quad (8). \quad (9)$$

207 Due to the strong air-concentration-dependence,  $VER_{min}$  decreases rapidly with height. In particular, at 105 km,  $VER \gg VER_{min}$ . At 75 km, the relationship is ~~the~~-inverse. We determine the local position of the NOCE boundary (pressure level  $p_{eq} p_{eq}^l$  and altitude level  $z_{eq} z_{eq}^l$ ) according to the criterion (89), where  $VER = VER_{min}(T, M)$ . We ~~carried out special verification~~verified that the approximation  $A(T, M, O) \cong A(T, M)$  is valid near the NOCE boundary. With the use of annual SABER data, we calculated simultaneous datasets of  $A(T, M)$  and  $A(T, M, O)$ . In the second case, we used O retrieved ~~O~~ from the same SABER data. The maximum and mean differences between  $A(T, M)$  and  $A(T, M, O)$  were found to be  $\sim 2\%$  and  $\sim 0.1\%$ , respectively.

215 The total range of latitudes according to the satellite trajectory over a month ~~is was~~  $\sim(83.5^{\circ}\text{S} - 216 83.5^{\circ}\text{N})$ . This range was divided into 20 bins and all single local values of  $p_{eq} p_{eq}^l$  and  $z_{eq} z_{eq}^l$  falling into 217 one bin during a month or a year were averaged, respectively. For convenience, In particular, several 218 thousand values of  $p_{eq}^l$  and  $z_{eq}^l$  fall into one bin during a month. Following Mlynczak et al. (2013a), 219 averages were determined by binning the data of a certain day by local hour and then averaging over the 220 hour bins that contain data to obtain the daily average value. Then we calculated monthly mean values of 221  $p_{eq} p_{eq}^m$  and  $z_{eq} z_{eq}^m$  and annually mean values of  $p_{eq}^y$  and  $z_{eq}^y$  (hereafter, the indexes «m» and «y» 222 indicate the monthly and annually average, respectively). Then, for convenience, the values of  $p_{eq} p_{eq}^m$  and 223  $p_{eq}^y$  were recalculated into the pressure-heights (pseudoheights)  $z_{eq} z_{eq}^m$  altitudes  $h_{eq} h_{eq}^m$  and  $h_{eq} h_{eq}^y$ . The 224 dependence of  $z_{eq} z_{eq}^m$  on the pressure  $p_{eq} p_{eq}^m$  was taken adopted from Mlynczak et al. (2013a, 225 2014):

$$226 \quad h_{eq} h_{eq}^{m,y} = -H_a \cdot \log(p_{eq} p_{eq}^{m,y} / p_0), H_a = 5.753474, p_0 = 11430.49428 \text{ hPa.} \quad (10)$$

227 Note that the use of both, geometrical and pressure coordinates is a rather common approach when 228 analyzing long-term evolution of the obtained data, especially, when the data is the result of averaging

229 over time and space. In particular, Lübken et al. (2013) demonstrated the importance of distinguishing  
230 between trends on pressure and geometrical altitudes in the mesosphere, since the second includes the  
231 atmospheric shrinking effect and is more pronounced. Grygalashvily et al. (2014) analyzed the linear  
232 trends in OH\* peak height and revealed a remarkable decrease at geometrical altitudes, which is almost  
233 absent at pressure altitudes.

234 Kulikov et al. (2023) studied the systematic uncertainty of the retrieved NOCE boundary height.  
235 Following the typical analysis presented, for example, in Mlynczak et al. (2013a, 2014), the uncertainty  
236 was obtained by calculating the root-sum-square of the individual sensitivity of the retrieved  
237 ~~characteristics~~characteristic to the perturbation of O<sub>3</sub>, T, rates of reactions, and parameters of the A  
238 function. The systematic error of ~~z<sub>eq</sub> p<sup>a</sup>~~ NOCE pressure altitude  $h_{eq}^m$  and ~~z<sub>eq</sub> varies~~ geometrical altitude  
239  $z_{eq}^m$  varied in the range of 0.1-0.3 km, whereas the random error ~~is~~was negligible due to averaging  
240 in over time and space.

## 242 5 NOCE boundary in 2002-2021 from SABER/TIMED data: main results

243 ~~Figures~~Figure 4-7 demonstrate ~~demonstrates~~ the ~~contour map of~~ space time evolution of  
244 ~~pseudoheight~~ ~~z<sub>eq</sub> p<sup>a</sup>~~ ~~the pressure altitude~~  $h_{eq}^m$  in 2002-2021 and examples of ~~z<sub>eq</sub> p<sup>a</sup>~~ time evolution, in all  
245 latitude bins. Figures 5 (left column) show the mean (for 2002-2021) annual cycle and of  $h_{eq}^m$  at four  
246 specific latitudes and Figures 6 (left column) present the Fourier spectra at ~~different~~these latitudes. It can  
247 be seen obtained from the data in Figure 4. Note, first, that above ~55°S-58°S, N, there are data gaps due  
248 to specified by the satellite sensing geometry. For example, in 2002-2014, at 66.8-75.15°S, N in 2002-  
249 2014, measurements ~~ever~~covered 6 months per year only. In 2015, because of slight ~~change~~changes in  
250 the satellite geometry, ~~there appeared~~ additional months ~~appeared~~. This is especially noticeable above  
251 ~66°S, N and manifests itself by extension of the variation range of ~~z<sub>eq</sub> p<sup>a</sup>~~  $h_{eq}^m$  at these latitudes in 2015-  
252 2021. Second, the variation range of ~~z<sub>eq</sub> p<sup>a</sup>~~  $h_{eq}^m$ , annual cycle and spectrum of harmonic oscillations  
253 depend~~depends~~ essentially on the latitude. Near the equator, ~~z<sub>eq</sub> p<sup>a</sup>~~  $h_{eq}^m$  varies in the 81-83 km range  
254 mainly and there are two main harmonics with periods of 1/2 and 1 year in the spectrum. At low latitudes,  
255 the variation range of ~~z<sub>eq</sub> p<sup>a</sup>~~  $h_{eq}^m$  narrows down to a minimum (~82.2-83.2 km at 16.7-20.05°S, N) ~~that~~,  
256 which is accompanied by with the appearance of a wide spectrum of harmonics with periods of 1/5, 1/4,  
257 1/3, 1/2, and 1 year. At middle latitudes, the range of ~~z<sub>eq</sub> p<sup>a</sup>~~  $h_{eq}^m$  variation monotonically increases up to  
258 ~81.5-85.5 km with latitude and the harmonic with a period of 1 year becomes the main mode in the  
259 spectrum of oscillations. At both, low and middle latitudes, there is no signal from quasi-biennial  
260 oscillations but one can see a remarkable amplitude of a harmonic with a period of ~10 years, which can

be associated with a manifestation of 11-year solar cycle. Note It is interesting that the mentioned features are typical for both hemispheres. At high latitudes,  $\langle z_{eq}^{pa} h_{eq}^m \rangle$  varies in the range of 79-86.5 km. At these latitudes, itone can ~~see~~ the main difference between ~~the northern~~ and ~~southern~~ hemispheres: the sharp falls and rises of the ~~northern~~ boundary of NOCE by several km (up to 3-4 km) appearing in January-FebruaryMarch 2004, 2006, 2009, 2010, 2012, 2013, 2018 and 2019 and ~~absent~~ that are ~~absent~~ at ~~southern~~ latitudes.

Analyzing the Figure 6, one can note The analysis of Figures 5-6 demonstrates the following redistribution in the annual cycle with increasing latitude from equator to polar latitudes. Near the equator, the annual cycle has two maxima in June – July and in December – January. The first one is more pronounced. That is why there are two main harmonics with periods of 1/2 and 1 year in the spectrum. At low latitudes, one maximum (summer) ~~remains in place, and does not change, while~~ the other ~~begins to approach~~ approaches the first one. As ~~the~~ a result, the ~~wide~~ spectrum of harmonics ~~takes place~~ is wide. At middle latitudes, the maxima gradually merge so that the 1 year-harmonic becomes the main one.

Figures 8-9 demonstrate the Figure 7 (left) demonstrates a contour map of the space-time evolution of the average annual  $\langle z_{eq}^{pa} \rangle$  ( $\langle z_{eq}^{pa} \rangle$ , hereafter, the angle brackets are used to denote the values averaged in time and space) pressure altitude  $h_{eq}^y$  in 2002-2021 and examples of . Figure 8 presents the time evolution of this characteristic at different latitudes. BasingBased on Fourier's the Fourier spectra presented in Figure 7, Figures 6 (left column), we can suppose that, at low and middle latitudes, the interannual variation of  $\langle z_{eq}^{pa} \rangle h_{eq}^y$  is caused by the 11-year solar cycle mainly. Figure 409 (left) presents the correlation coefficient of  $\langle z_{eq}^{pa} \rangle h_{eq}^y$  with  $F_{10.7}$  index (solar radio flux at 10.7 cm, see the red curve in Figure 810) as a function of latitude. One can see good anticorrelation (with a coefficient from -0.7472 to -0.992) between  $\sim 55^{\circ}$ S and  $\sim 55^{\circ}$ N. At high latitudes, the absolute value of the correlation coefficient decreases sharply updown to  $\sim 0.5658$  in the south and to  $\sim 0.1$  in the north. BlueThe blue curve in Figure 410 shows latitude-averaged  $\langle z_{eq}^{pa} \rangle h_{eq}^y$  in the range of  $55^{\circ}$ S- $55^{\circ}$ N. In this case, the anticorrelation with  $F_{10.7}$  index is close to ideal (coefficient  $\sim -0.9695$ ).

With the use of multiple linear regression in the  $55^{\circ}$ S- $55^{\circ}$ N range:

$$\langle z_{eq}^{pa} \rangle (h_{eq}^y \text{ (year)}) = \text{const} + \alpha \cdot \text{year} + \beta \cdot F_{10.7} \text{ (year)}, \quad (911)$$

we determined a slow (up to 10 m/year) linear trend in  $\langle z_{eq}^{pa} \rangle$  of  $h_{eq}^y$  as a function of latitude in the range of  $55^{\circ}$ S- $55^{\circ}$ N (see Figure 12). One can see a tendency to increase  $\langle z_{eq}^{pa} \rangle$  at most latitudes with trend up to 10 m/year, but with high uncertainty the uncertainties essentially larger than the trend values.

292 Applying the regression analysis to latitude-averaged  $\langle z_{eq}^{pa} \rangle h_{eq}^y$  (blue curve in Figure 11) gives 10)  
293 gave us a more statistically significant value of the trend:  $4.92 \pm 35.62 \pm 4.22$  m/year.

294 ~~Figures 13-16 demonstrate~~ Figure 11 demonstrates the ~~contour map of space~~ time evolution of  
295 ~~real the geometrical~~ altitude ~~of NOCE boundary~~  $z_{eq}^m$  in 2002-2021, ~~examples of~~  $z_{eq}$  time evolution, ~~in all~~  
296 ~~latitude bins. Figures 5 (right column) show the mean (for 2002-2021) annual cycle and of~~  $z_{eq}^m$  ~~at four~~  
297 ~~specific latitudes and Figures 6 (right column) present the Fourier spectra at~~ different ~~these~~ latitudes.  
298 Comparing obtained from the data in Figure 11. Comparison with Figures 4-7, it can be seen, first,  $z_{eq}$   
299 and 5-6 (left columns) shows that  $z_{eq}^m$  repeats many qualitative features of ~~the~~ space-time evolution of  
300  ~~$z_{eq}^{pa}$  pressure altitude  $h_{eq}^m$~~ . In particular, in the direction from the equator to the poles, the variation  
301 range of  ~~$z_{eq}^m$~~  first decreases ~~up~~ ~~down~~ to 1 km at  $16^\circ$ - $25^\circ$ S, N, ~~and~~ then ~~expanding~~ ~~expands~~ to several  
302 km at middle and high latitudes. In Figure 15, one ~~One~~ can see the same redistribution of the annual cycle  
303 with latitude, ~~as it was mentioned in Figure 6~~ ~~similarly to the pressure altitude case~~. Near the equator, the  
304 annual cycle possesses two maxima occurring in June – July and in December – January. At low  
305 latitudes, one maximum continues ~~to be~~ in summer, whereas the other shifts ~~into the~~ to spring. At middle  
306 latitudes, the maxima gradually coalesce forming a single summer maximum. At ~~north~~ high ~~northern~~  
307 latitudes, there are the same local sharp variations of the NOCE boundary in January-February 2004,  
308 2006, 2009, 2010, 2012, 2013, 2018 and 2019, which ~~are~~ absent at ~~south~~ ~~southern~~ latitudes. ~~Second~~ ~~One~~  
309 can see from Figure 5 that, on ~~the~~ average,  ~~$z_{eq}^m$~~  is lower than  ~~$z_{eq}^{pa}$~~ . The difference  ~~$z_{eq}^{pa} - z_{eq}$~~   
310 varies in the range of 0 – 1.5 km at equator, 0 – 2.5 km at  $50^\circ$ - $58^\circ$ S, N and 1-4 km at  $75^\circ$ - $83^\circ$ S, N. The  
311 maxima and minima of  ~~$z_{eq}^{pa} - z_{eq}$~~  are reached in winter and summer, respectively. In general, the  
312 variation range of  $z_{eq}$  during the year is wider  $h_{eq}^m$  by about 10.5-41 km, depending on latitude. ~~Third~~,  
313 ~~the~~ ~~One~~ can see from Figure 6 that the  $z_{eq}^m$  spectra of harmonic oscillations are similar to  ~~$z_{eq}^{pa}$~~  ~~the~~  $h_{eq}^m$   
314 spectra except for ~~no~~ the absence of a signal of the 11-year solar cycle.

315 ~~Figures 17-18 demonstrate the~~ Figure 7(right) demonstrates a contour map of space-time evolution  
316 of ~~the annually~~ average ~~annual~~  $\langle z_{eq} \rangle$  ~~geometrical altitude~~  $z_{eq}^y$  in 2002-2021 ~~and examples~~  
317 ~~of~~. Figure 12 presents the time evolution of this ~~characteristics~~ characteristic at different latitudes. One  
318 can see, ~~at all latitudes, that~~ there is no clear evidence of 11-year solar cycle manifestation ~~at all latitudes~~.  
319 This is confirmed by the calculation of the correlation coefficient of  $\langle z_{eq} \rangle z_{eq}^y$  with  $F_{10.7}$  index as a  
320 function of latitude (see Figure 19.9 (right)). Moreover, the latitude-averaged (in the range of  $55^\circ$ S-  
321  $55^\circ$ N)  $\langle z_{eq} \rangle z_{eq}^y$  has a correlation coefficient equal to  $\sim 0.5455$ .

322 ~~With~~ As in the case of  $h_{eq}^y$ , we found with the use of multiple linear regression ~~as in the case of~~  
323  ~~$z_{eq}^{pa}$~~ , we determined the slow (up to  $\sim 10$  m/year) and statistically insignificant linear trend in

324  ~~$\langle z_{eq} \rangle$  of  $z_{eq}^y$  as a function of latitude in the range of 55°S–55°N (see Figure 20). One can see a~~  
325 ~~tendency to decrease  $\langle z_{eq} \rangle$  at most latitudes with trend up to 10 m/year, but with high uncertainty.~~  
326 ~~Applying. Moreover, the regression analysis toof latitude-averaged  $\langle z_{eq} \rangle$  gives us the trend equal to~~  
327 ~~4.48±6.73 m/year.  $z_{eq}^y$  also revealed a statistically insignificant trend.~~

## 329 6 Discussion

330 The NOCE boundary is an important technical ~~characteristics~~characteristic for ~~the~~ correct  
331 application of the NOCE approximation to retrieve the nighttime distributions of minor chemical species  
332 of MLT. ~~Remind also, that BelikovichKulikov et al. (2019) repeated the O and H retrieval by Mlynczak~~  
333 et al. (2018) ~~found by 3D simulation from the SABER data for the year 2004. It was revealed that the~~  
334 ~~application of the NOCE condition below the boundary obtained according to the criterion could lead to a~~  
335 ~~great (up to 5–8 times) systematic underestimation of O concentration below 86 km, whereas it was~~  
336 ~~insignificant for H retrieval. The results presented in Figures 4, 5 and 11 demonstrate that the, except for~~  
337 ~~high northern latitudes, there is a stable annual cycle of the NOCE boundary. The monthly mean~~  
338 ~~boundary can rise up to geometrical altitudes of 82–83 km ( $\sim(5.2\text{--}6.2)\cdot10^3$  hPa) at low latitudes and up to~~  
339 ~~84–85 km ( $\sim(3.7\text{--}4.4)\cdot10^3$  hPa) at middle and high latitudes. Thus, the SABER O data below these~~  
340 ~~altitudes/pressures may be essentially incorrect and the retrieval approaches without using the NOCE~~  
341 ~~condition (e.g., Panka et al., 2018) should be more appropriate.~~

342 Note that the NOCE condition was used not only for O and H derivation from satellite data. This  
343 assumption is a useful approach helping (i) to study hydroxyl emission in the MLT region with simulated  
344 and measured data, in particular, OH\* mechanisms, morphology and variability caused, for example, by  
345 atmospheric tides and gravity wave activity (e.g., Marsh et al., 2006; Nikoukar et al., 2007; Xu et al.,  
346 2010, 2012; Kowalewski et al., 2014; Sonnemann et al., 2015); (ii) to analyze the MLT response to  
347 sudden stratospheric warmings (SSWs) (e.g., Smith et al., 2009); (iii) to derive exothermic heating rates  
348 of MLT (e.g., Mlynczak et al., 2013b); (iv) to analytically simulate the mesospheric OH\* layer response  
349 to gravity waves (e.g., Swenson and Gardner, 1998); and (v) to derive the analytical dependence of  
350 excited hydroxyl layer ~~well repeats spatiotemporal variability of the NOCE boundary. Let~~ discuss the  
351 ~~obtained results from the point of view~~ number density and peak altitude on atomic oxygen and  
352 temperature (e.g., Grygalashvily et al., 2014; Grygalashvily, 2015). Perhaps some results require  
353 revision or reanalysis taking the NOCE boundary into account. For example, Smith et al. (2009) used the  
354 NOCE condition to analyze the ozone perturbation in the MLT, in particular, during the SSW at the  
355 beginning of 2009 (the central day was January 24). Our preliminary results of processing the SABER

356 and simulated data in January 2009 show that the NOCE boundary above 70°N may jump from ~80 km to  
357 ~90-95 km due to a short-time abrupt temperature fall above 80 km during this SSW. Thus, one can  
358 assume that the NOCE condition is not a good approximation for the description of ozone variations  
359 directly in the process of SSWs. This case will be studied in a separate work. Note also that after the SSW  
360 of January 2009 there began a long-time (several tens of days) event of elevated (up to ~80-85 km)  
361 stratopause (see, e.g., Figure 1 in Smith et al. (2009)), which led to the corresponding increase of  
362 temperature above 80 km. The occurrence of this event and its duration are in a good correlation with  
363 sharp lowering of the NOCE boundary at high northern latitudes (see Figures 4 and 11). Moreover, all  
364 abrupt changes of the NOCE boundary at these latitudes in January-March of other possible applications  
365 of this feature years (2004, 2006, 2010, 2012, 2013, 2018, and 2019) can be also associated with the  
366 elevated stratopause events in these years (see García-Comas et al. (2020) and references there).

367 The carried out analysis revealed unusual behavior of According to the used chemical-transport  
368 model, the NOCE boundary at the north pole latitudes in January February 2004, 2006, 2009, 2010, 2012,  
369 2013, 2018 reproduces well the transition zone dividing deep and 2019. All these time periods are known  
370 for strong local changes of the middle atmosphere dynamics due to extremely powerful sudden  
371 stratospheric warming which leaded to appearance of elevated (from typical 50-60 km to ~80 km)  
372 stratopause events weak diurnal oscillations of O and H (see García-Comas et al. (2020) and references  
373 there). Thus, we can speculate that Figures 1-3). We verified this feature with the annual run of SD-  
374 WACCM-X model for the year 2017 provided by the NCAR High Altitude Observatory  
375 (<https://doi.org/10.26024/5b58-nc53>). Despite the low time resolution of the downloaded data (3-hour  
376 averaging), we obtained the results (see Figure 13) similar to Figures 1-3. Note also that both models give  
377 the same consistence between the altitudes of the NOCE boundary of NOCE is sensitive to sporadic  
378 abrupt changes in the dynamics of the middle atmosphere and the mentioned transition zone at high  
379 latitudes in spring and autumn.

380 The space-time evolution of the NOCE boundary expressed in terms of ~~pseudoheights pressure~~  
381 ~~altitudes~~ contains a clear signal of the 11-year solar cycle in the ~~range of~~ 55°S-55°N ~~range~~, which is  
382 suppressed mainly at high latitudes. The weak correlation of  $z_{eq}^{pa} h_{eq}^y$  with  $F_{10.7}$  index at ~~south~~ high  
383 ~~southern~~ latitudes may be caused by the mentioned data gaps ~~due to specified by the~~ satellite sensing  
384 geometry. The same reason and distortions by ~~sudden stratospheric warming, SSWs~~ evidently, determine  
385 no correlation at ~~north~~ high ~~northern~~ latitudes. Thus,  $z_{eq}^{pa}$  at low and middle latitudes  $h_{eq}^y$  can be  
386 considered as a sensitive indicator of solar activity. ~~The~~ Below, we present a simple and short explanation  
387 for this. Let us consider the NOCE criterion (9) at the pressure level  $p_{eq}$ :

$$VER(p_{eq}) = VER_{min} (T, M(p_{eq})).$$

388 In a zero approximation

$$389 \quad VER_{min} = 20 \cdot \frac{k_1 \cdot o_2(p_{eq}) \cdot M(p_{eq}) \cdot \left( k_4 \cdot o_2(p_{eq}) \cdot M(p_{eq}) \cdot \left( 1 - \frac{k_5 + k_6}{k_3} \right) + k_2 \cdot o_3(p_{eq}) \right) \cdot A(T, M(p_{eq}))}{k_2} \approx$$

$$390 \quad 20 \cdot \frac{k_1 \cdot k_4 \cdot (o_2(p_{eq}) \cdot M(p_{eq}))^2 \cdot A(T, M(p_{eq}))}{k_2} \sim \frac{k_1 \cdot k_4 \cdot (p_{eq}/T)^4 \cdot A(T, p_{eq})}{k_2} \sim \frac{\exp(470/T) \cdot p_{eq}^4 \cdot A(T, p_{eq})}{T^{8.2}},$$

391 where  $A(T, p_{eq}) =$

$$392 \quad \frac{0.47 \cdot 118.35}{215.05 + 2.5 \cdot 10^{-11} \cdot O_2 / M \cdot \frac{p_{eq}}{k_B T} + 3.36 \cdot 10^{-13} \cdot e^{\frac{220}{T}} \cdot N_2 / M \cdot \frac{p_{eq}}{k_B T}} + \frac{0.34 \cdot 117.21}{178.06 + 4.8 \cdot 10^{-13} \cdot O_2 / M \cdot \frac{p_{eq}}{k_B T} + 7 \cdot 10^{-13} \cdot N_2 / M \cdot \frac{p_{eq}}{k_B T}} +$$

$$393 \quad \frac{0.47 \cdot 117.21 \cdot (20.05 + 4.2 \cdot 10^{-12} \cdot O_2 / M \cdot \frac{p_{eq}}{k_B T} + 4 \cdot 10^{-13} \cdot N_2 / M \cdot \frac{p_{eq}}{k_B T})}{(215.05 + 2.5 \cdot 10^{-11} \cdot O_2 / M \cdot \frac{p_{eq}}{k_B T} + 3.36 \cdot 10^{-13} \cdot e^{\frac{220}{T}} \cdot N_2 / M \cdot \frac{p_{eq}}{k_B T}) \cdot (178.06 + 4.8 \cdot 10^{-13} \cdot O_2 / M \cdot \frac{p_{eq}}{k_B T} + 7 \cdot 10^{-13} \cdot N_2 / M \cdot \frac{p_{eq}}{k_B T})}.$$

394 Our analysis of  $A(T, p_{eq})$  shows that this function can be approximately rewritten as  $A(T, p_{eq}) \approx$   
 395  $const + \frac{const}{const + \frac{p_{eq}}{T}}$ . So, one can see that  $VER_{min}$  is strongly dependent on  $T$ . Moreover, it anticorrelates  
 396 with  $T$ . Gan et al. (2017) and Zhao et al. (2020) analyzed the simulated and measured data and revealed a  
 397 clear correlation between the MLT temperature above 80 km and the 10.7-cm solar radio flux. Moreover,  
 398 the dependence of the correlation coefficient of  $T$  with  $F_{10.7}$  index on latitude in the 55°S-55°N range  
 399 given in Figure 9 in the paper by of Zhao et al. (2020) is consistent with our Figure 9 (left panel), taking  
 400 into account the sign of the correlation. Thus, we can conclude that the found anticorrelation of the NOCE  
 401 boundary  $h_{eq}^y$  with solar activity is caused by the strong connection with temperature, which, in turn, is  
 402 in a good correlation with the  $F_{10.7}$  index. A detailed analysis of the reasons why the solar cycle does not  
 403 manifestweakly manifests itself in the spatio-temporal variability of  $z_{eq}$  requires a separate study.  $z_{eq}^y$  is  
 404 not so simple and is beyond the scope of this work.

405 Figures 6 and 15 present Figure 5 illustrates an interesting peculiarity. At middle latitudes, the  
 406 summer  $z_{eq}^y h_{eq}^m$  and  $z_{eq}^y z_{eq}^m$  are remarkably (forby several kilometers) higher than the winter ones,  
 407 while the opposite relationship could be expected. Due to more effective daytime HO<sub>x</sub> photoproduction at  
 408 these altitudes, the summer H values at the beginning of nightthe night are higher than the ones in  
 409 winter. So, the summer ozone lifetimes should be lessshorter and the NOCE condition of NOCE is more  
 410 favorablefavourable than in winter. Nevertheless, the same ratio between the summer and winter the  
 411 NOCE boundaries at middle latitudes was revealed in Belikovich et al. (2018) and Kulikov et al. (2018a),  
 412 where the boundary of this equilibrium was determined by direct comparison of  $O_3$  and  $O_3^{eq}$

413 concentrations from results of 3-D3D chemical-transport models. Based on the results ~~in~~ of Section 3,  
 414 ~~one~~ we can assume that the discussed effect is connected with the height position of the transition zone,  
 415 which demonstrates the same variation (see Figures 1-3). Kulikov et al. (2023) derived the equations  
 416 describing pure chemical O and H nighttime evolution:

$$417 \quad \begin{cases} \frac{dO}{dt} = -2 \cdot k_4 \cdot M \cdot O_2 \cdot H - 2 \cdot k_2 \cdot H \cdot O_3 \\ \frac{dH}{dt} = -2 \cdot k_4 \cdot M \cdot O_2 \cdot \frac{k_5+k_6}{k_3} \cdot \frac{H^2}{O} \end{cases} \quad (4012)$$

418 )

420 Neglecting the second term in the first equation as ~~a~~ secondary one, this system can be solved analytically  
 421 ~~solved~~, so that the nighttime evolution times of O and H are ~~as follows~~:

$$422 \quad \tau_O \equiv \frac{O}{|dO/dt|} = \frac{1}{2 \cdot k_4 \cdot M \cdot O_2} \cdot \left( \frac{O}{H} \right)_{t=t_{bn}} - \left( 1 - \frac{k_5+k_6}{k_3} \right) \cdot (t - t_{bn}), \quad (4113)$$

423 )

$$425 \quad \tau_H \equiv \frac{H}{|dH/dt|} = \frac{1}{2 \cdot k_4 \cdot M \cdot O_2} \cdot \frac{k_3}{k_5+k_6} \cdot \left( \frac{O}{H} \right)_{t=t_{bn}} - \left( \frac{k_3}{k_5+k_6} - 1 \right) \cdot (t - t_{bn}), \quad (4214)$$

426 )

428 where  $t_{bn}$  is the time of the beginning of the night,  $\left( \frac{O}{H} \right)_{t=t_{bn}}$  is the O/H ratio ~~O/H~~ at the beginning of the  
 429 night. Note that  $k_3$  is ~~essentially much~~ larger than  $k_5 + k_6$  (see Table 1). ~~Basing~~ Based on the daytime O  
 430 and H distributions in the mesopause region obtained in Kulikov et al. (2022), we calculated ~~O/H in the~~  
 431 ~~ratio of the summer and O/H to the winter O/H (see Figure 14)~~. During the summer, ~~this ratio O/H at~~  
 432 middle latitudes is remarkably less than in winter ~~in both, northern and southern hemispheres~~, whereas  
 433 ~~the~~ air concentration ~~increases and the rate of reaction R4 (see Table 1) increase~~ due to a decrease in  
 434 temperature. As ~~the~~ a result, the summer  $\tau_O$  and  $\tau_H$  are essentially ~~less shorter than~~ their winter values ~~that~~  
 435 ~~explain, which explains~~ the summer rise of the transition zone and the NOCE boundary.

436 Finally, let us briefly discuss other qualitative indicators of the NOCE boundary, which could be  
 437 found in the SABER database. As mentioned above, Kulikov et al. (2019) showed that the nighttime O  
 438 SABER profiles are correct above the NOCE boundary, whereas the H profiles hold within the whole  
 439 pressure interval. Kulikov et al. (2021) demonstrated that, in the altitude range of 80-85 km, many H  
 440 profiles have a sharp jump in concentration when it increases from  $\sim 10^7 \text{ cm}^{-3}$  to  $\sim 10^8 \text{ cm}^{-3}$ . Our analysis

441 with the criterion (9) shows that the altitude of these jumps can be used as a rough indicator of the NOCE  
442 boundary.

443

444 **7 Conclusions**

445 The NOCE criterion is not only ~~the~~<sup>useful</sup> technical ~~characteristics to retrieve O~~<sup>O</sup> characteristic for  
446 the retrieval of O from satellite data, but it also reproduces the transition zone position, which  
447 ~~divides~~<sup>separates</sup> deep and weak diurnal oscillations of O and H at low and middle latitudes.

448 ~~The~~<sup>At</sup> ~~middle~~<sup>latitudes, the summer</sup> boundary of NOCE ~~is~~<sup>is</sup> remarkably (by several kilometers)  
449 higher than the winter one, which is accompanied with the same variation of the transition zone. This  
450 effect is explained by the markedly lower values of the O and H nighttime evolution times in summer  
451 than in winter by virtue of the lower values of the O/H ratio at the beginning of the night and air  
452 concentration increase.

453 ~~The~~<sup>The</sup> NOCE boundary according ~~to~~<sup>to</sup> the criterion is sensitive to sporadic abrupt changes in the  
454 dynamics of the middle atmosphere.

455 The NOCE boundary at low and middle latitudes expressed in ~~pseudoheight~~<sup>pressure</sup> altitudes  
456 contains a clear signal of 11-year solar cycle and can be considered as ~~a~~<sup>a</sup> sensitive indicator of solar  
457 activity.

458 ~~At middle latitudes, summer boundary of NOCE is remarkably (for several kilometers) higher than  
459 winter one that is accompanied by the same variation of the transition zone. This effect is explained by  
460 the markedly lower values of the O and H nighttime evolution times in summer than in winter due to  
461 lower values of the ratio O/H at the beginning of the night and air concentration increase.~~

462

463 **Data availability.** The SABER data are obtained from the website (<https://saber.gats-inc.com>). The data  
464 of solar radio flux at 10.7 cm in 2002-2021 were downloaded from  
465 [http://www.wdcb.ru/stp/solar/solar\\_flux.ru.html](http://www.wdcb.ru/stp/solar/solar_flux.ru.html) and <https://www.spaceweather.gc.ca/forecast->  
466 [prevision/solar-solaire/solarflux/sx-5-en.php](https://www.spaceweather.gc.ca/forecast-).

467

468 **Code availability.** Code is available upon request.

469

470 **Author contributions.** MK and MB ~~carried out the performed~~ data processing and analysis and wrote the  
471 manuscript. AC, SD, and AM contributed to reviewing the article.

472

473 **Competing interests.** The authors declare that they have no conflict of interest.

474

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476

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482

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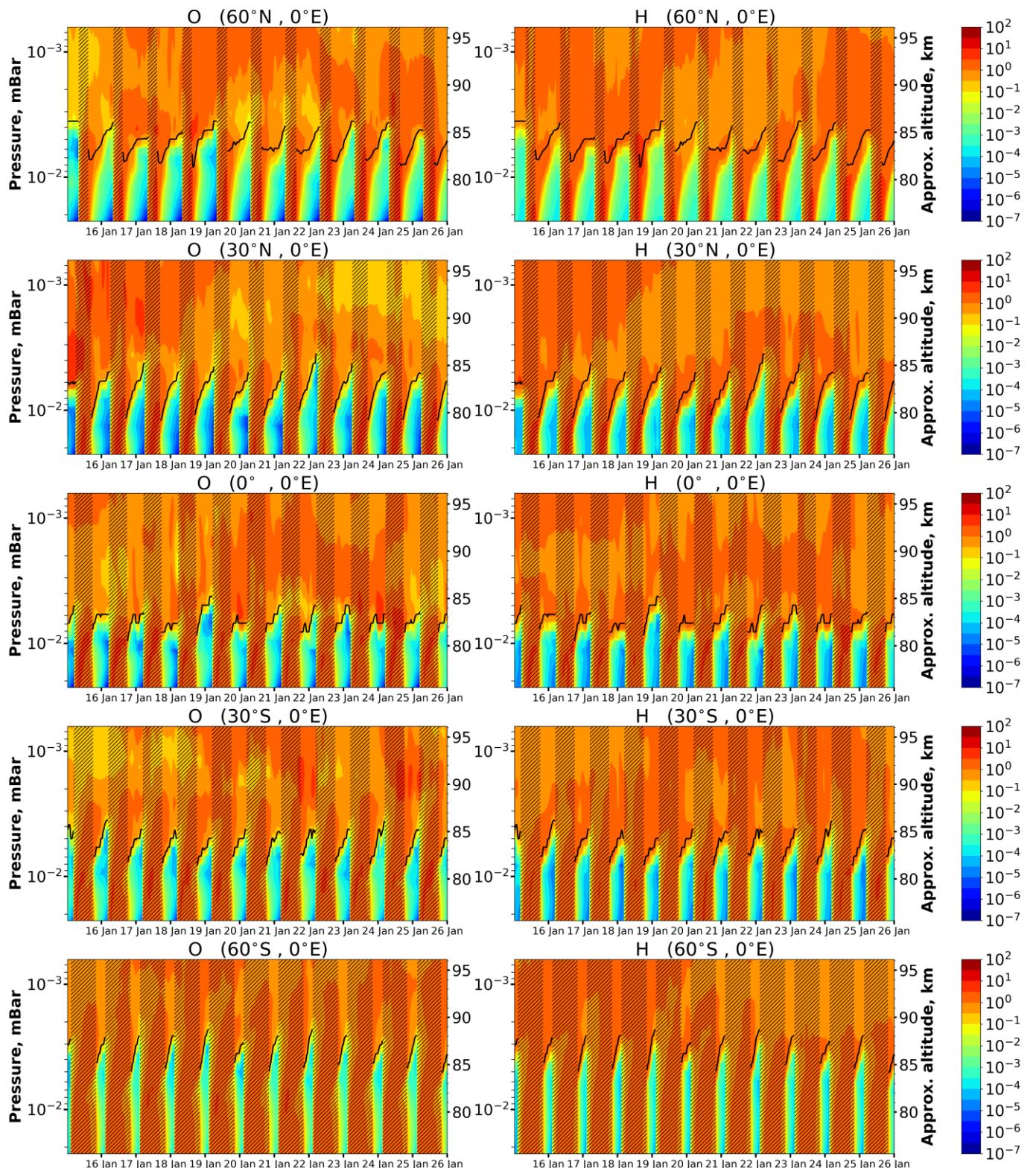
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679 **Table 1.** List of reactions with corresponding reaction rates (for three-body reactions [cm<sup>6</sup> molecule<sup>-2</sup>  
680 s<sup>-1</sup>], for two-body reactions [cm<sup>3</sup> molecule<sup>-1</sup> s<sup>-1</sup>]) taken from Burkholder et al. (2020).

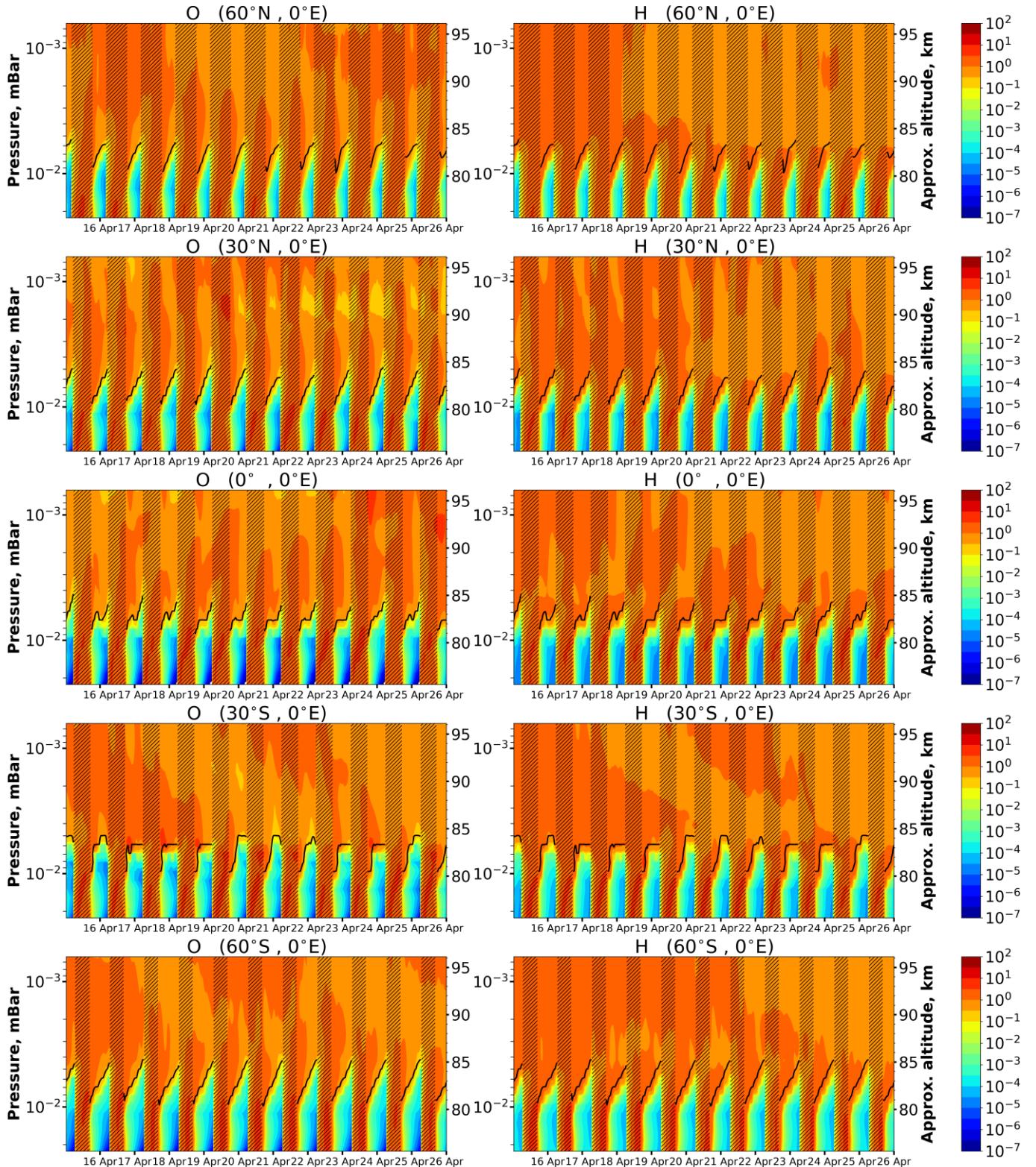
	<b>Reaction</b>	<b>Rate constant</b>
<b>R1</b>	O+O <sub>2</sub> +M → O <sub>3</sub> +M	$k_1 = 6.1 \cdot 10^{-34} (298/T)^{2.4}$
<b>R2</b>	H+O <sub>3</sub> → O <sub>2</sub> +OH	$k_2 = 1.4 \cdot 10^{-10} \exp(-470/T)$
<b>R3</b>	O+HO <sub>2</sub> → O <sub>2</sub> +OH	$k_3 = 3 \cdot 10^{-11} \exp(200/T)$
<b>R4</b>	H+O <sub>2</sub> + M → HO <sub>2</sub> +M	$k_4 = 5.3 \cdot 10^{-32} (298/T)^{1.8}$
<b>R5</b>	H+HO <sub>2</sub> → O <sub>2</sub> +H <sub>2</sub>	$k_5 = 6.9 \cdot 10^{-12}$
<b>R6</b>	H+HO <sub>2</sub> → O+H <sub>2</sub> O	$k_6 = 1.6 \cdot 10^{-12}$

681

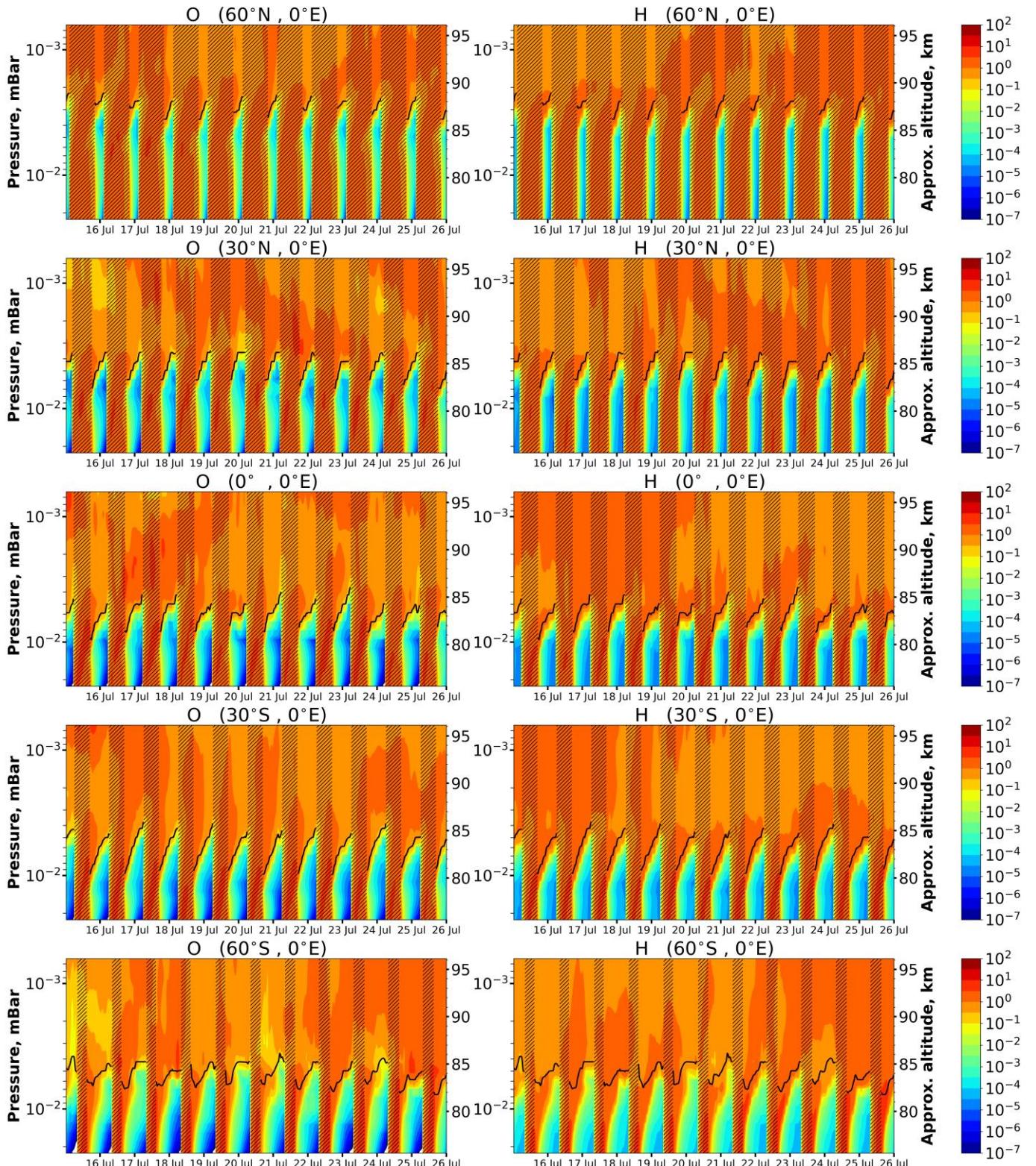
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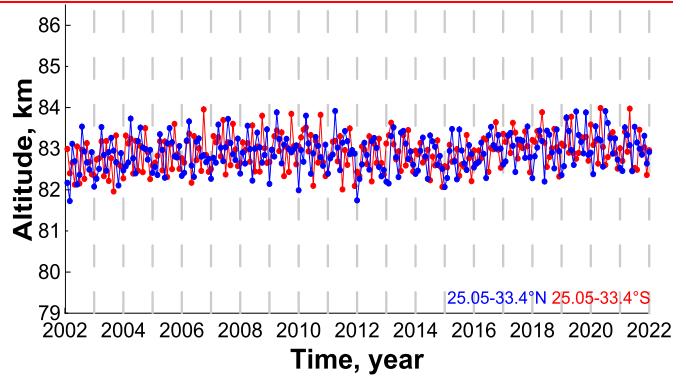
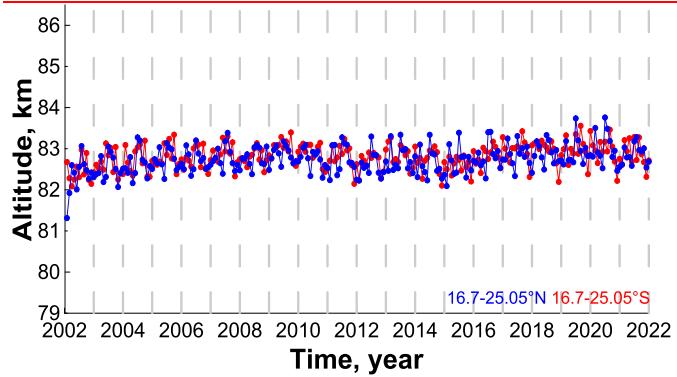
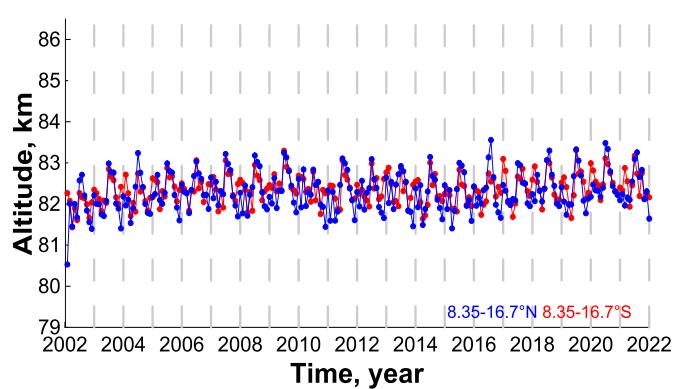
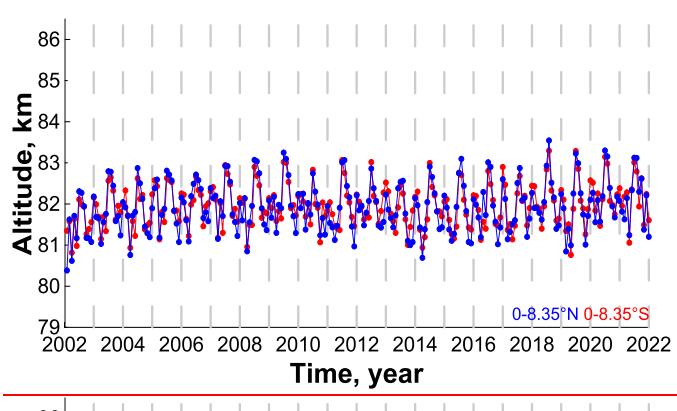
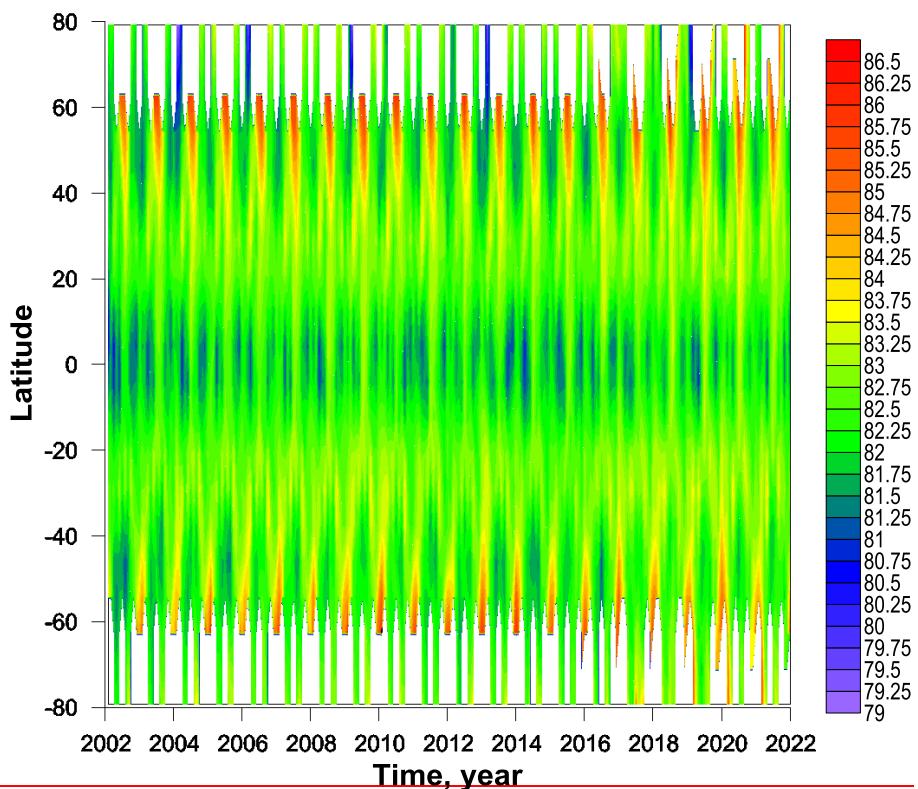
683  
 684 Figure 1. O and H time-height variations above different points in January 2000 calculated by the 3D  
 685 chemical transport model of the middle atmosphere. The concentrations are normalized by  
 686 mean daily values, correspondingly The dark, calculated as a function of altitude. Dark bars mark  
 687 daytime, light bars mark nighttime. The magenta lines point the NOCE boundary altitude in  
 688 accordance to criterion (5) ( $Cr = 0.1$ ).  
 689



691 Figure 2. The same as in Fig. 1, but in April 2000. Black lines point NOCE boundary according  
 692 to criterion (5) ( $Cr = 0.1$ ).  
 693



694  
 695 Figure 3. The same as in Fig. 1, but in July 2000. Black lines point the NOCE boundary altitude  
 696 according to criterion (5) (Cr = 0.1).  
 697



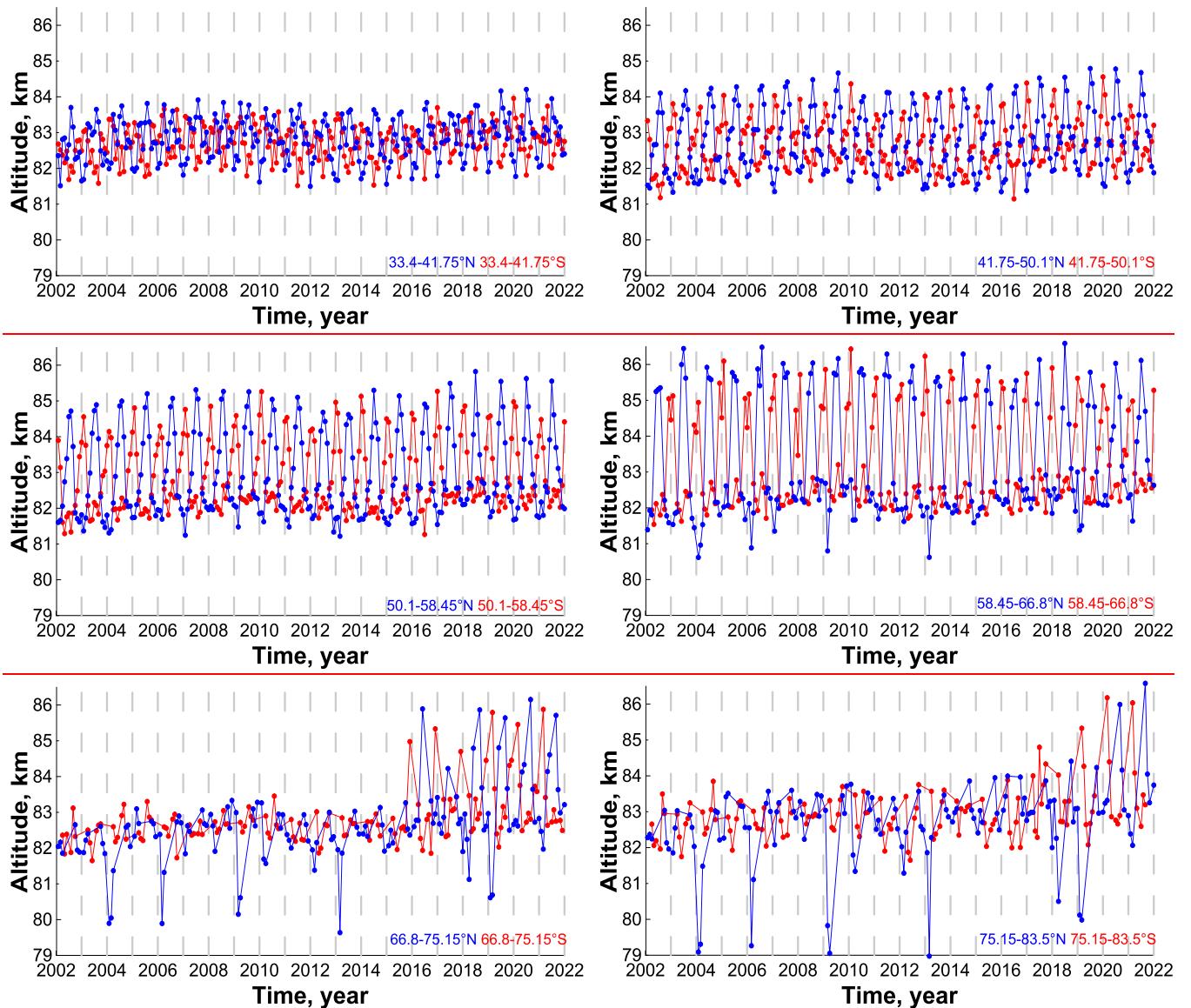


Figure 4. The space time evolution of  $z_{eq}^{pa}$ . White color indicates data gaps due to the satellite sensing geometry.

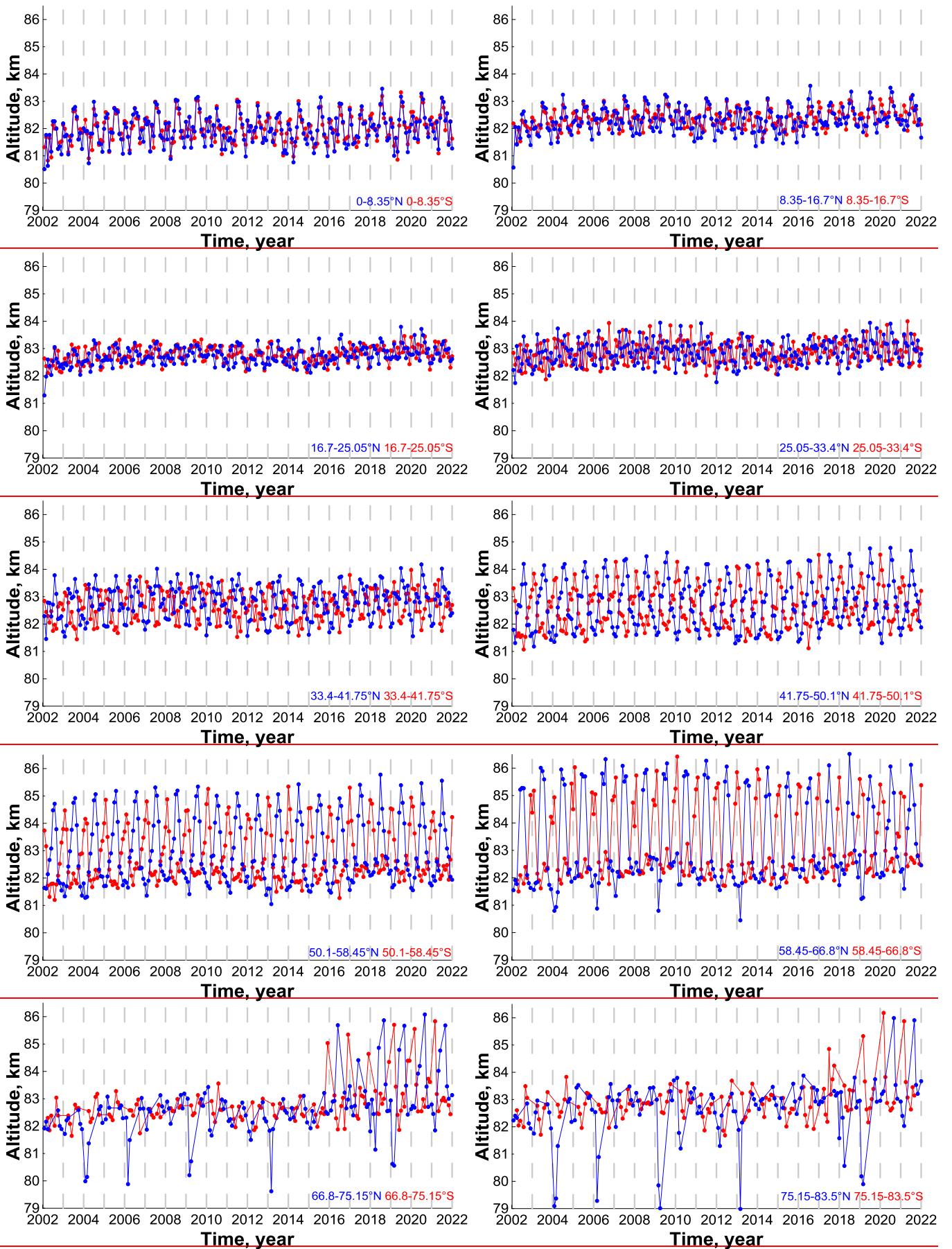
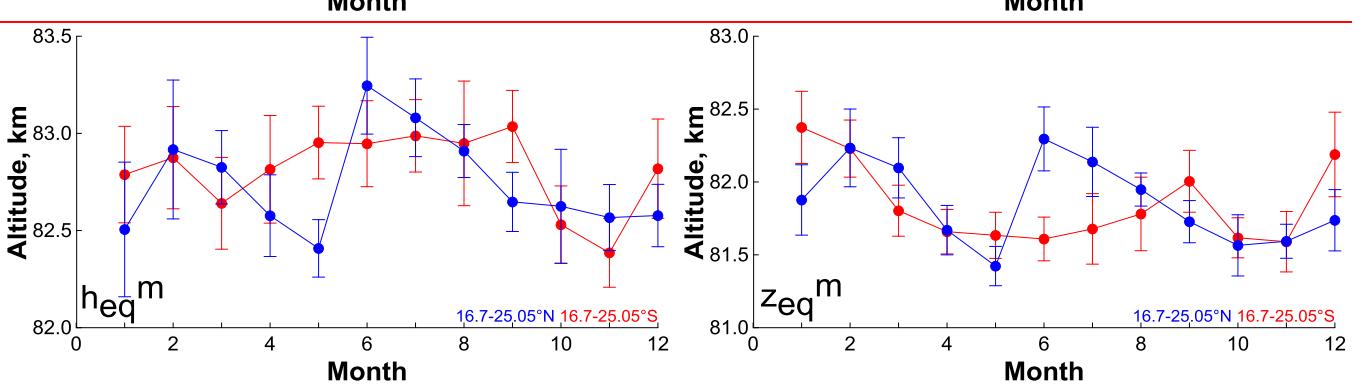
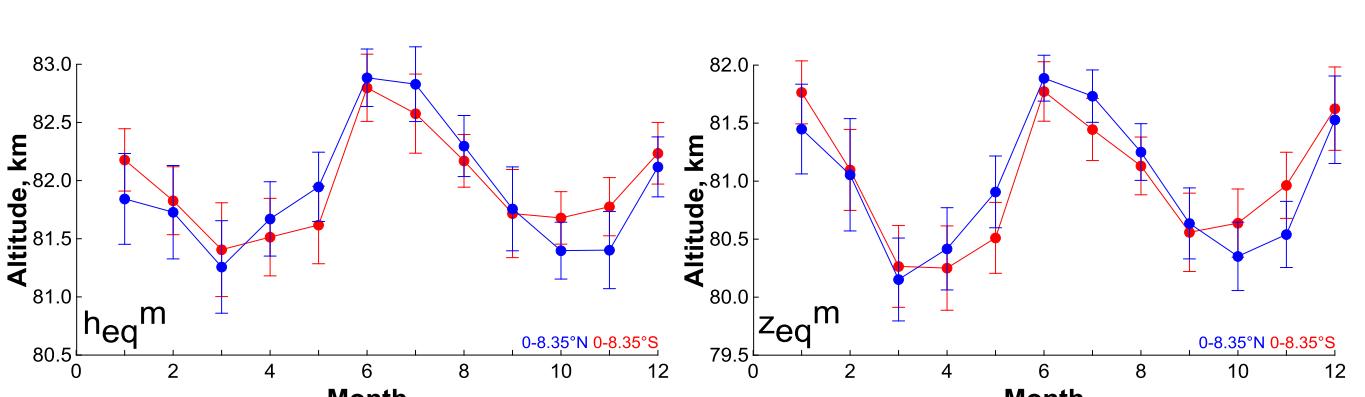
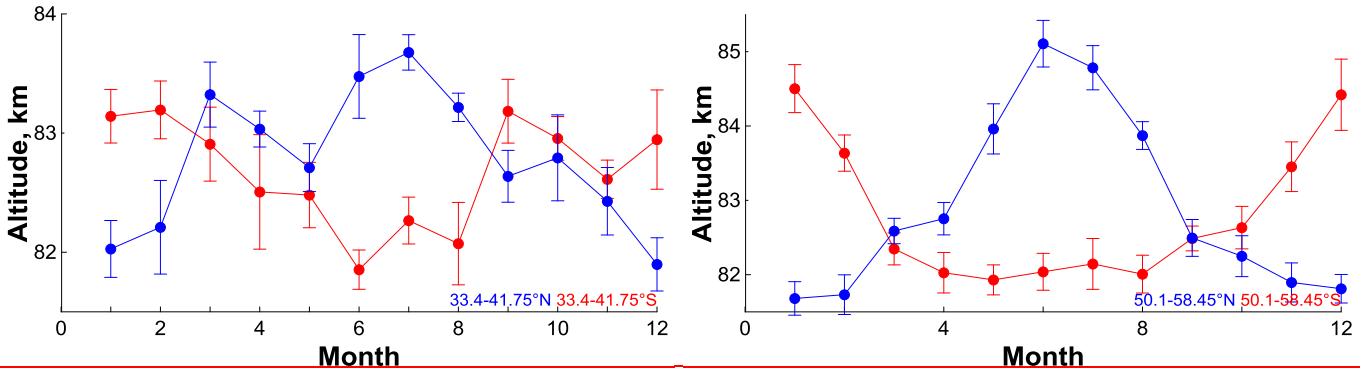
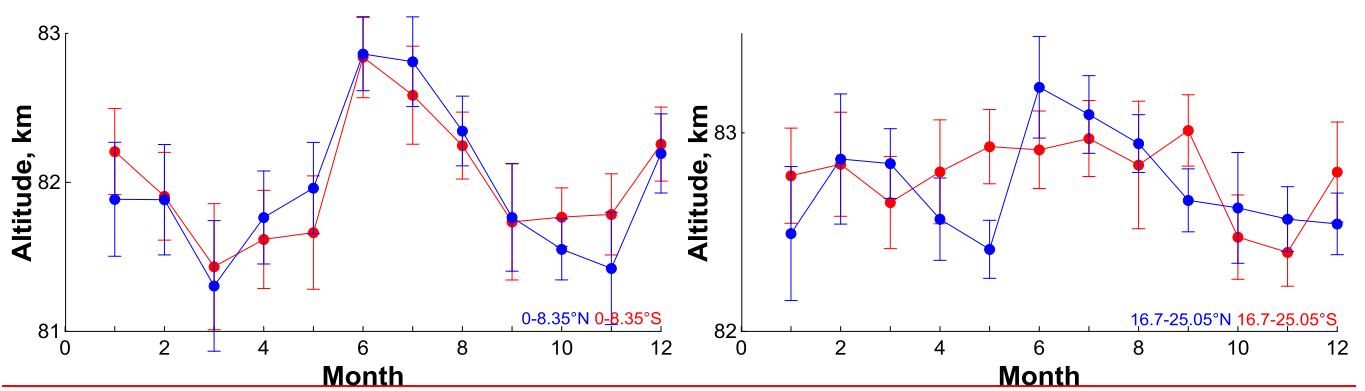
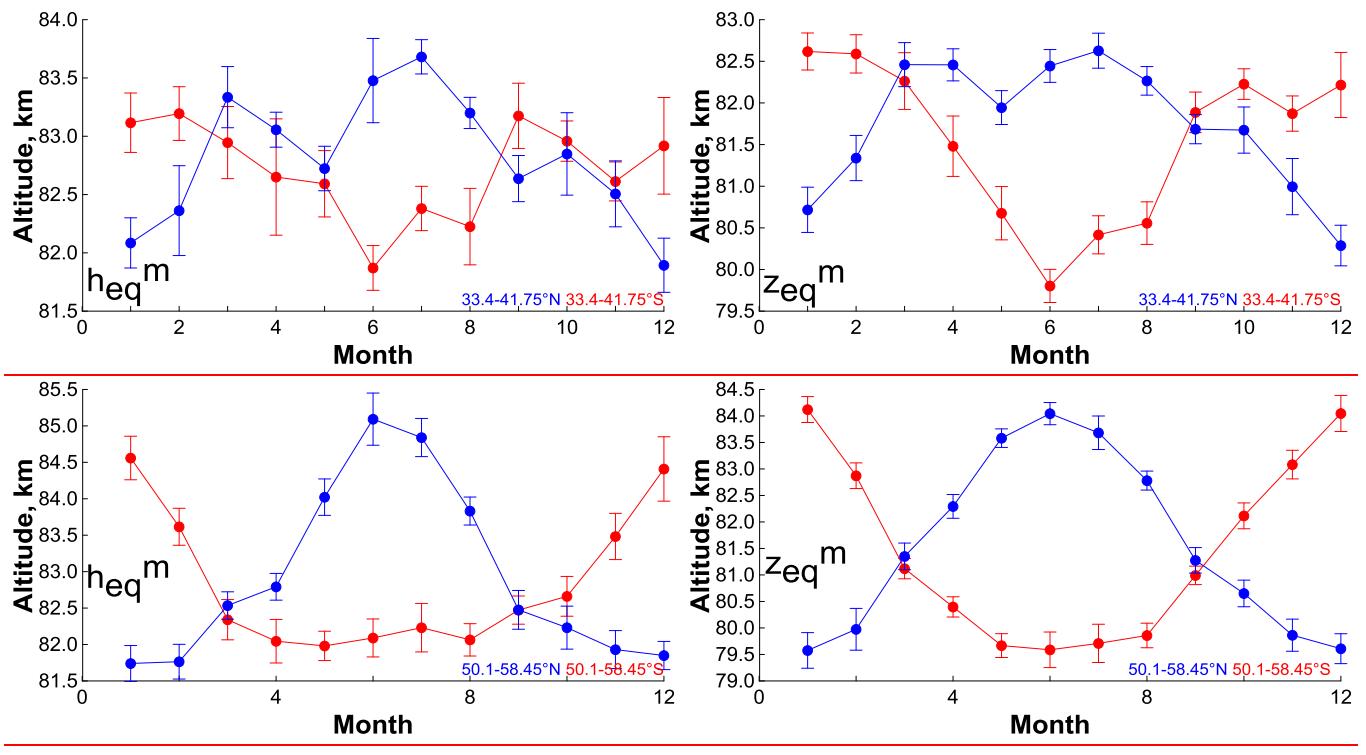
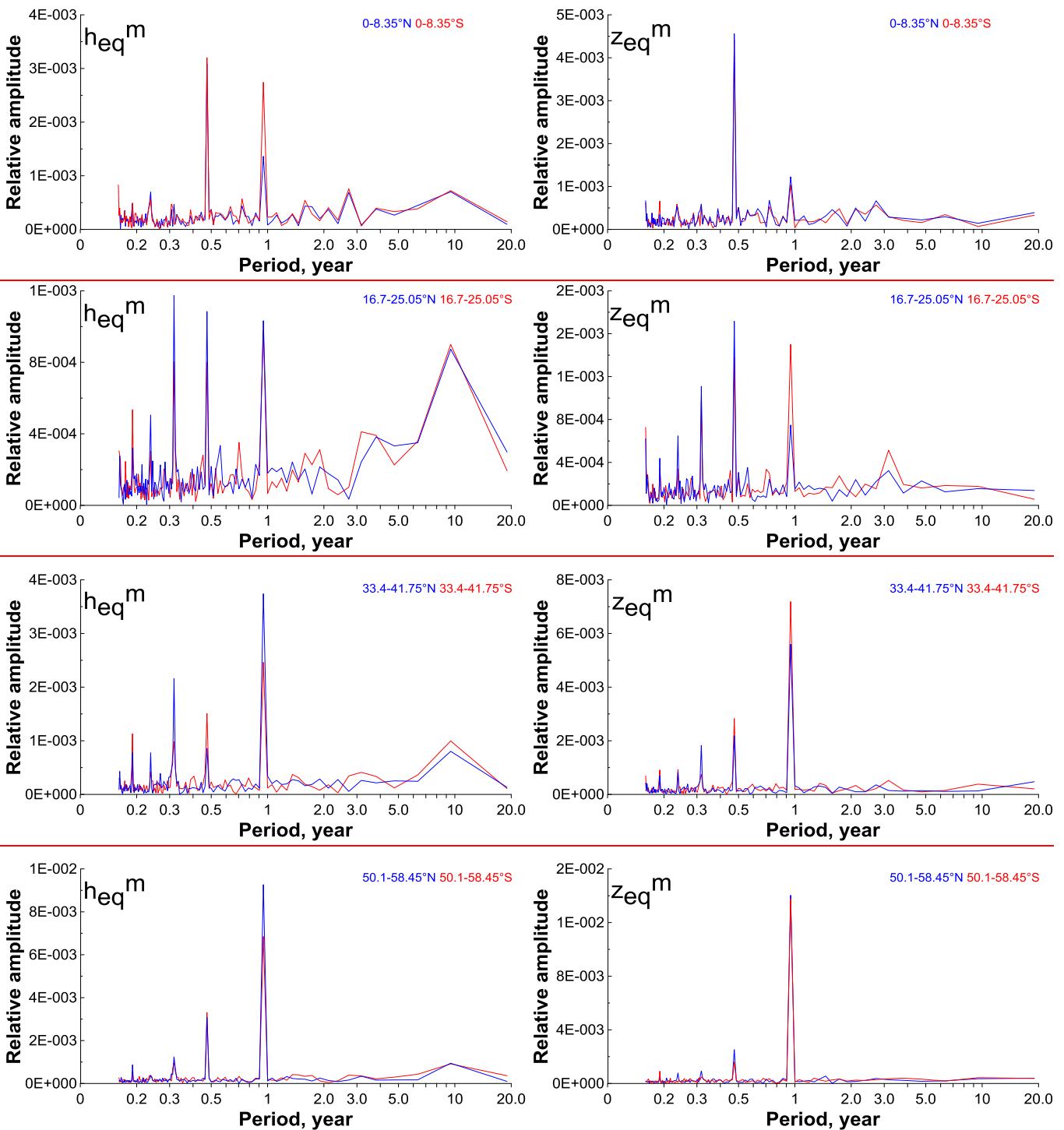


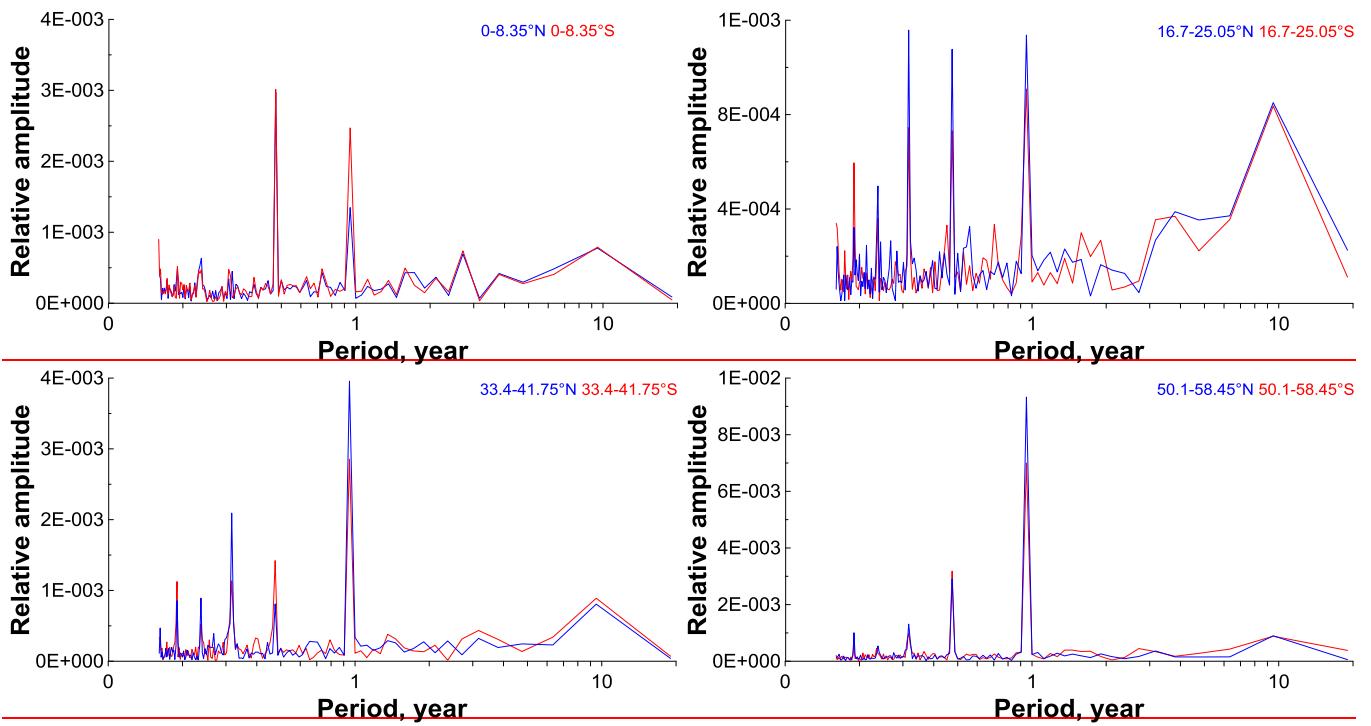
Figure 5. The time evolution of  $z_{eq}^{pa}$  Time evolution of monthly mean pressure altitude  $h_{eq}^m$  at different latitudes.





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 719 **Figure 5. Figure 6.** Average (for 2002-2021) annual cycle of  $z_{eq}^{pa}$  monthly mean pressure altitude  $h_{eq}^m$   
 720 and geometrical altitude  $z_{eq}^m$  at somefourspecific latitudes.  
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734 Figure 7. Fourier spectra of  $z_{eq}^{pa}$  time evolution monthly mean pressure altitude  $h_{eq}^m$  and  
735 geometrical altitude  $z_{eq}^m$  at the same four specific latitudes as in Figure 6. In each spectrum, the  
736 amplitudes of harmonics were normalized to the corresponding zero harmonic.

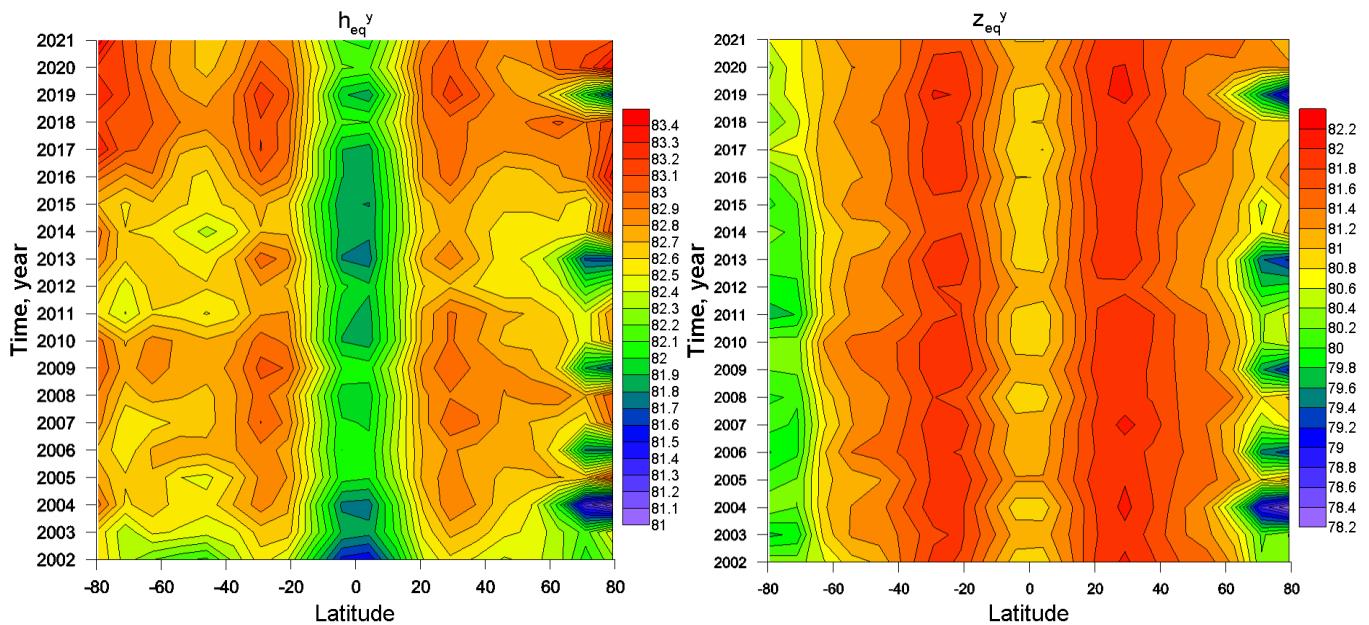
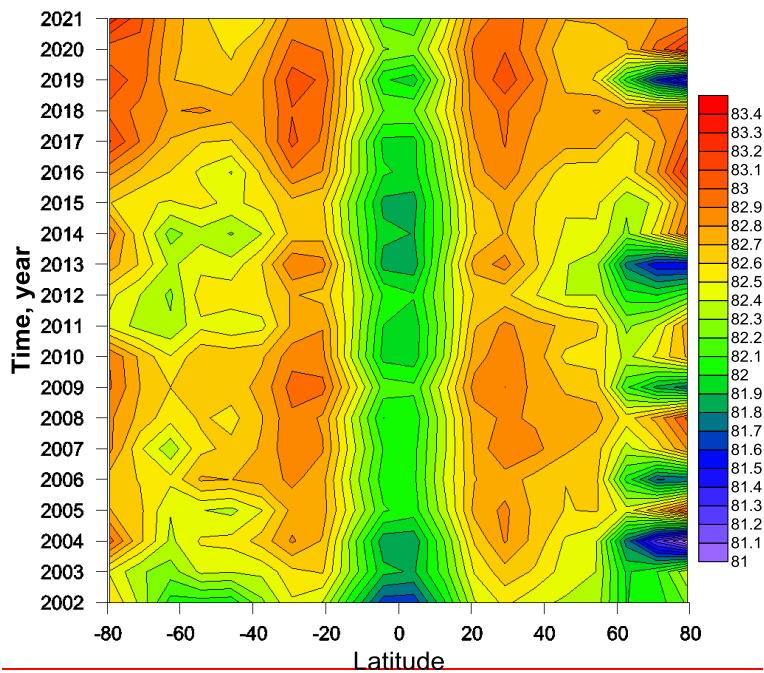
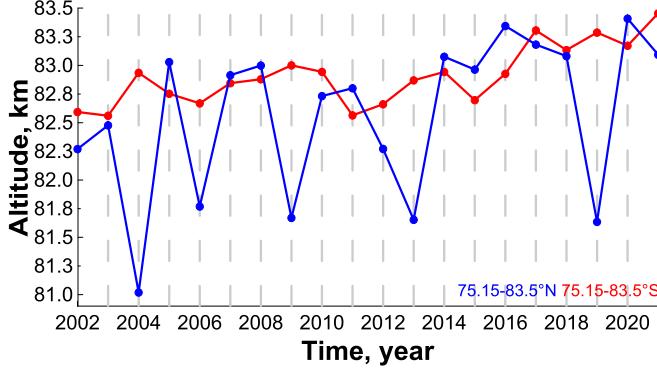
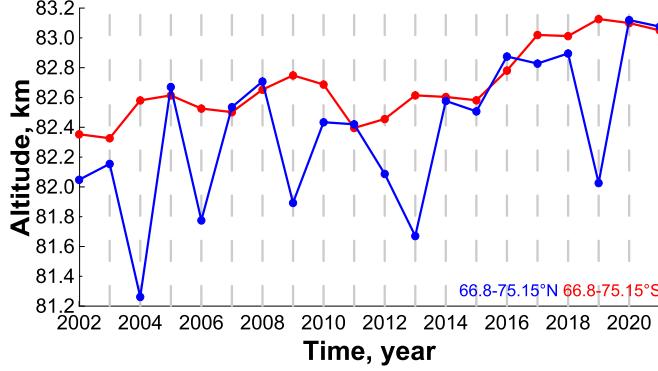
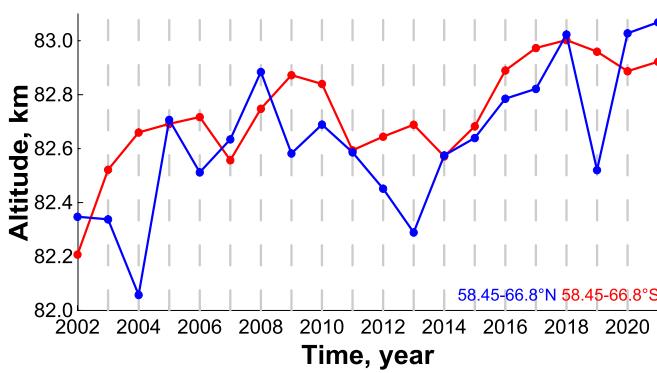
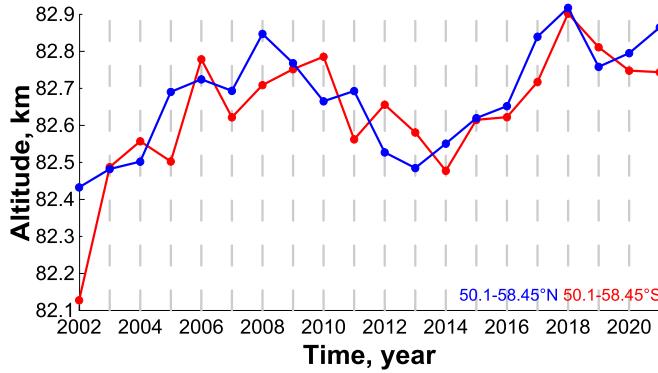
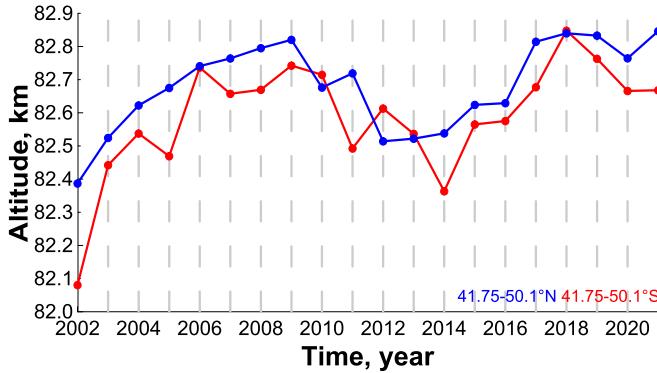
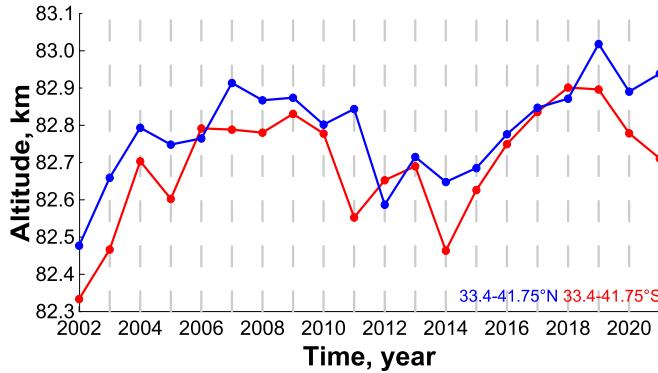
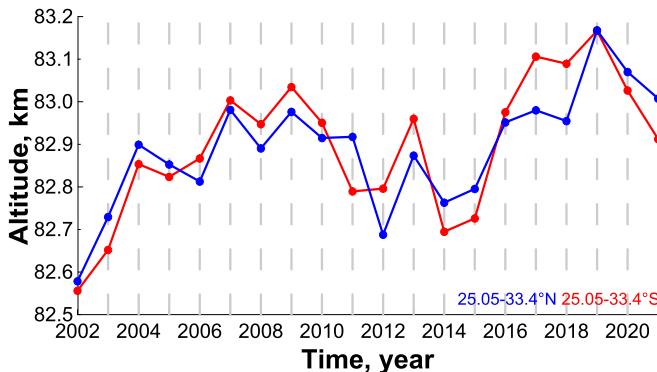
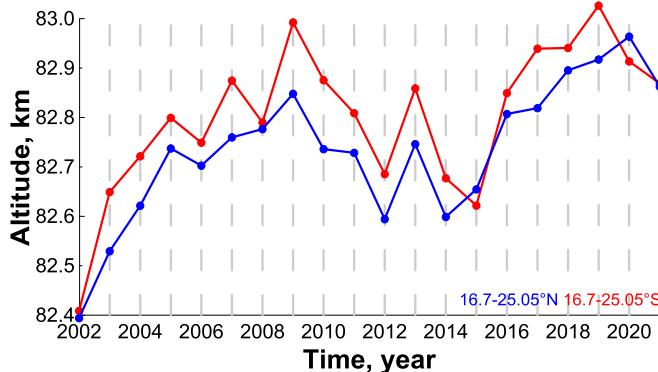
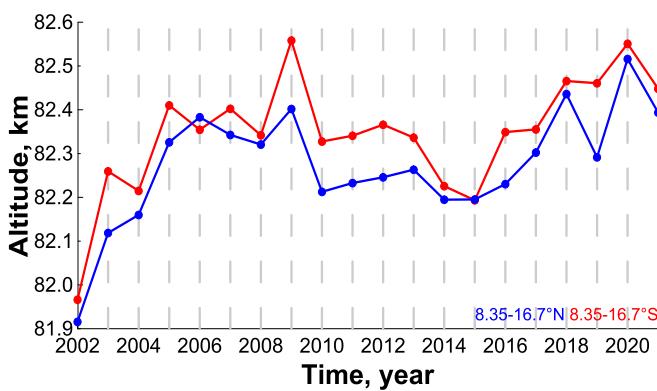
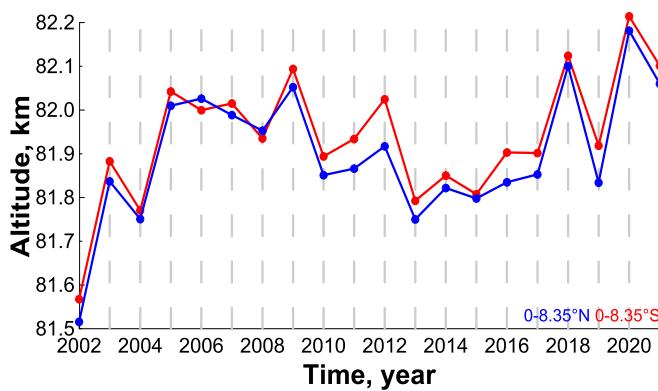


Figure 7.

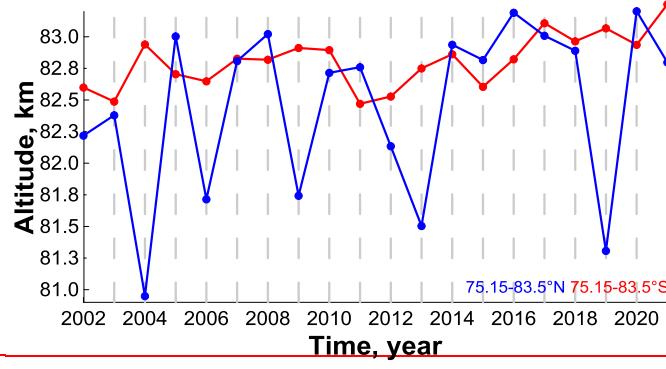
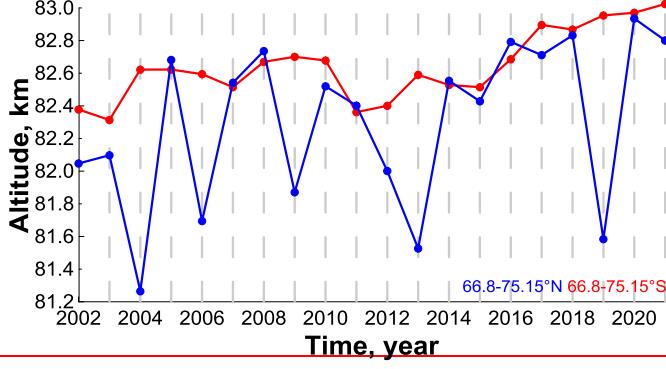
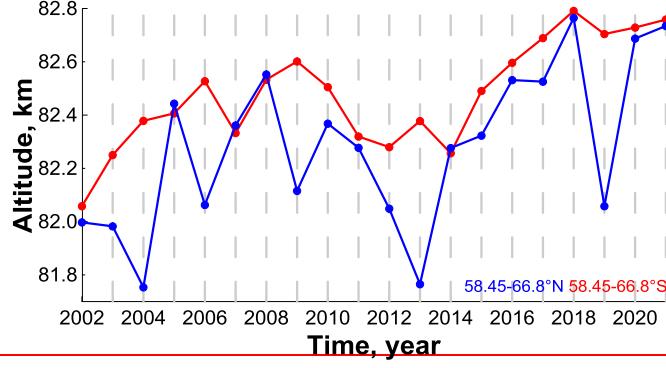
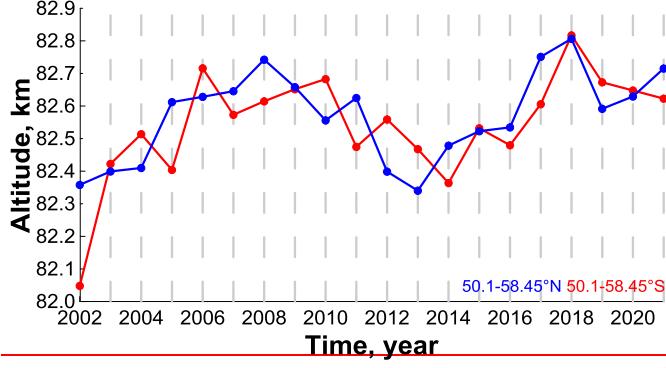
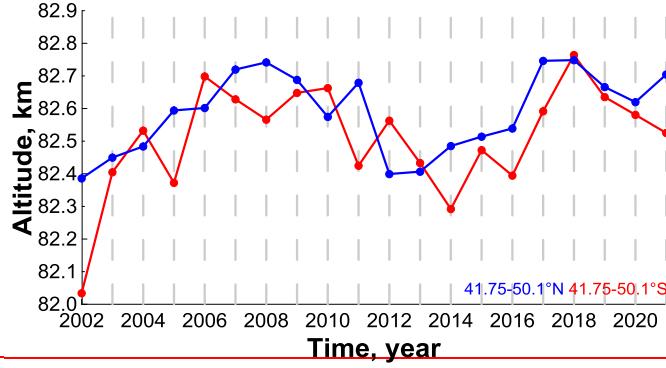
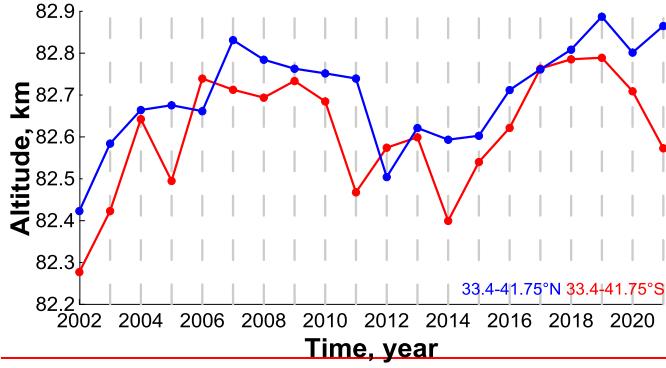
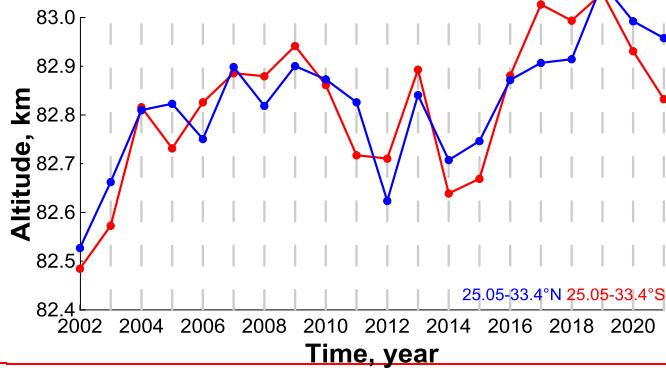
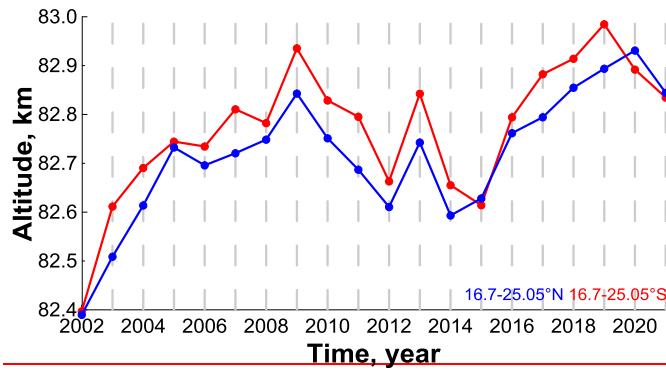
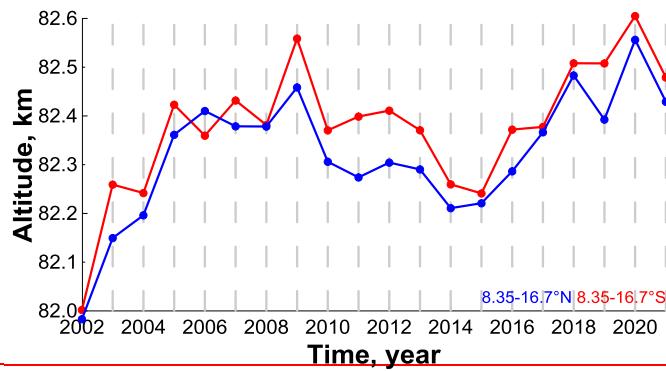
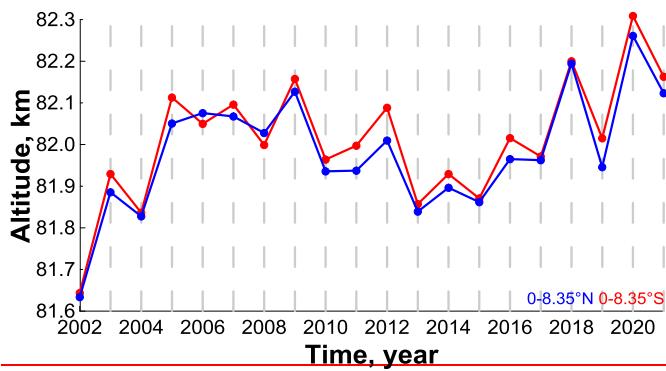


Latitude-time evolution of annually mean pressure altitude  $h_{eq}^y$  (left) and geometrical altitude  $z_{eq}^y$  (right).



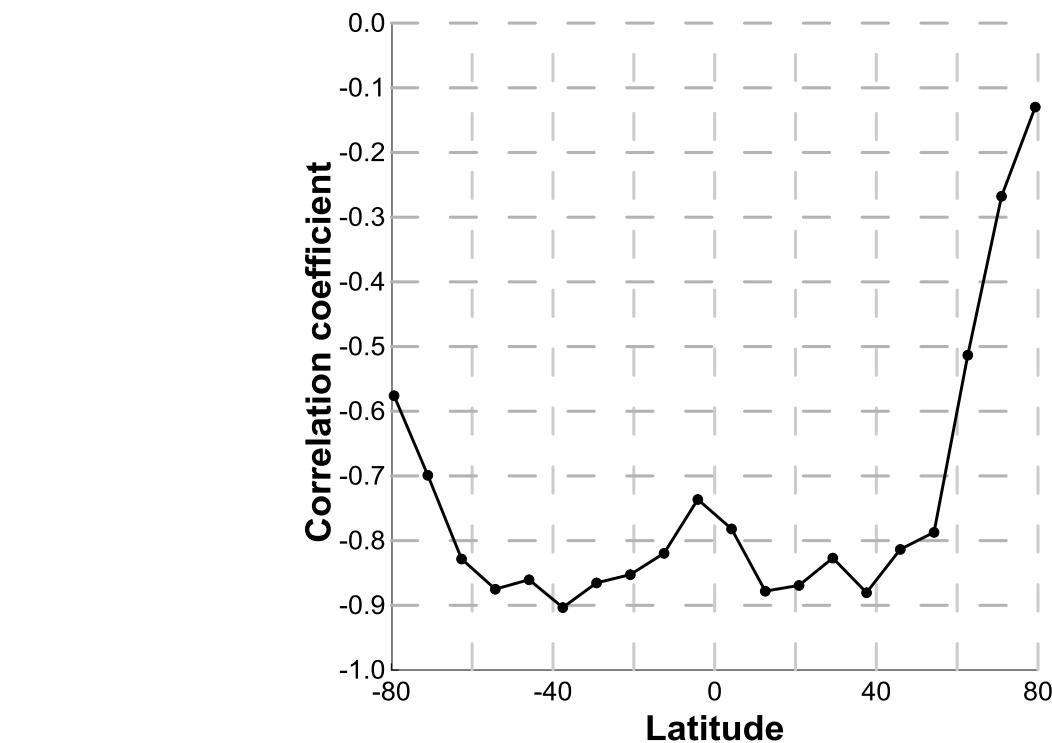
750 | Figure 8. ~~The latitude-time Time~~ evolution of ~~average annual~~  $z_{eq}^{pa}$ .

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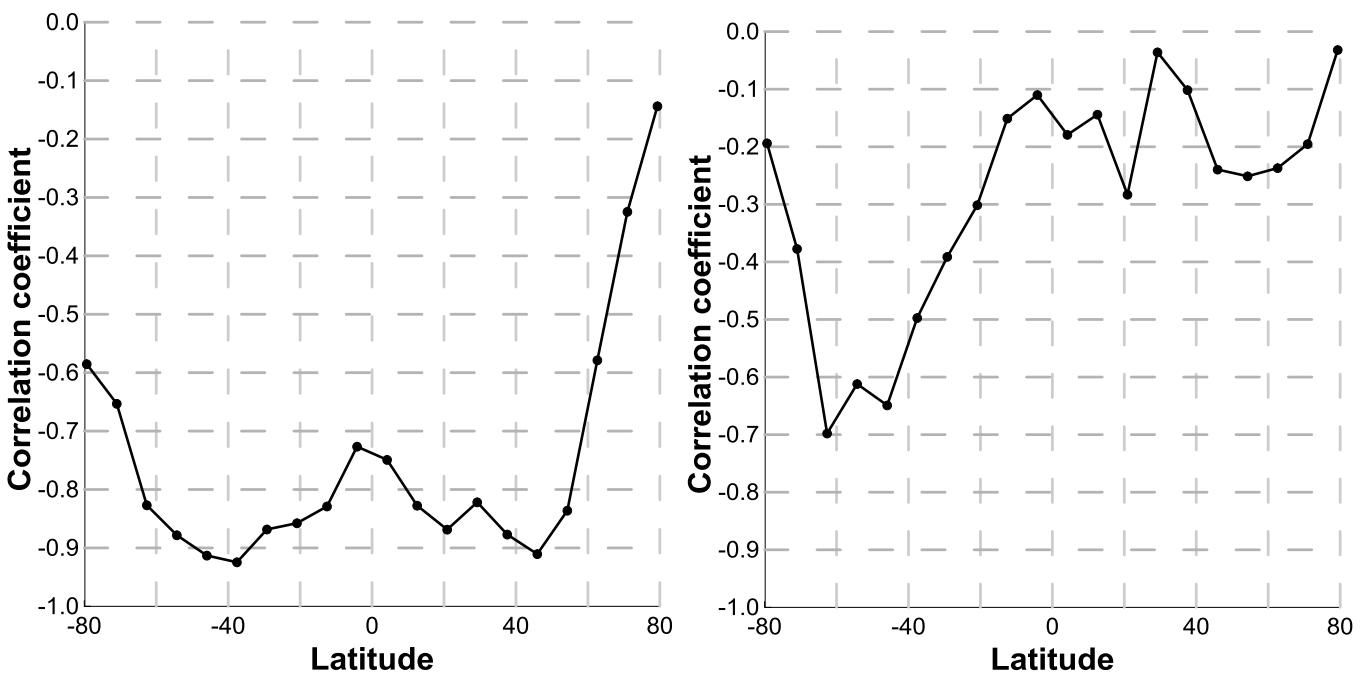


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Figure 9. The time evolution of average annual  $\langle z_{eq}^{pa} \rangle$  (annually mean pressure altitude  $h_{eq}^y$ ) at different latitudes.



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Figure 10. The correlation coefficient of  $\langle z_{eq}^{pa} \rangle$  with  $F_{10.7}$  index at different latitudes with pressure altitude  $h_{eq}^y$  (left) and geometrical altitude  $z_{eq}^y$  (right) as a function of latitude.

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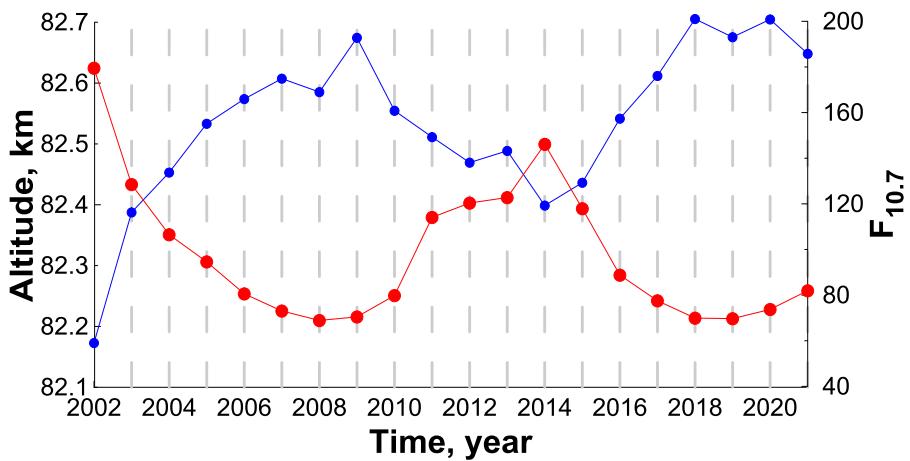
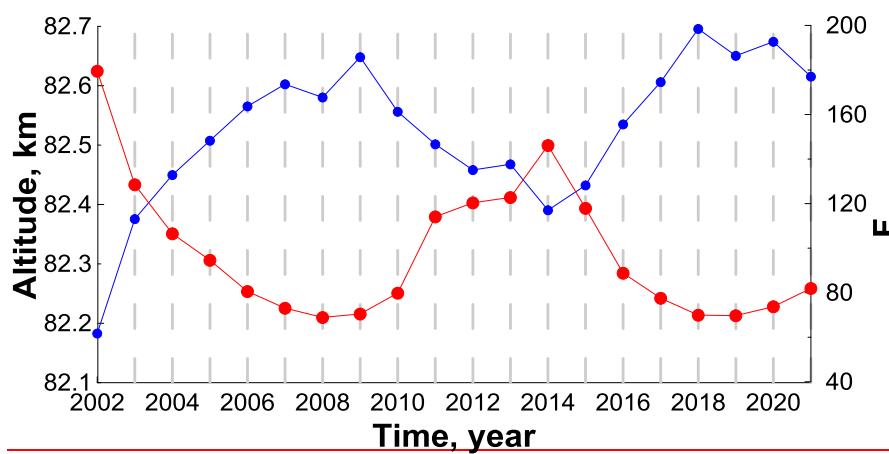


Figure 10. Red curve:  $F_{10.7}$  index (solar radio flux at 10.7 cm). Blue curve: latitude-averaged pressure altitude *hegy* in ~~this~~ the range between  $\sim 55^\circ\text{S}$  and  $\sim 55^\circ\text{N}$ .

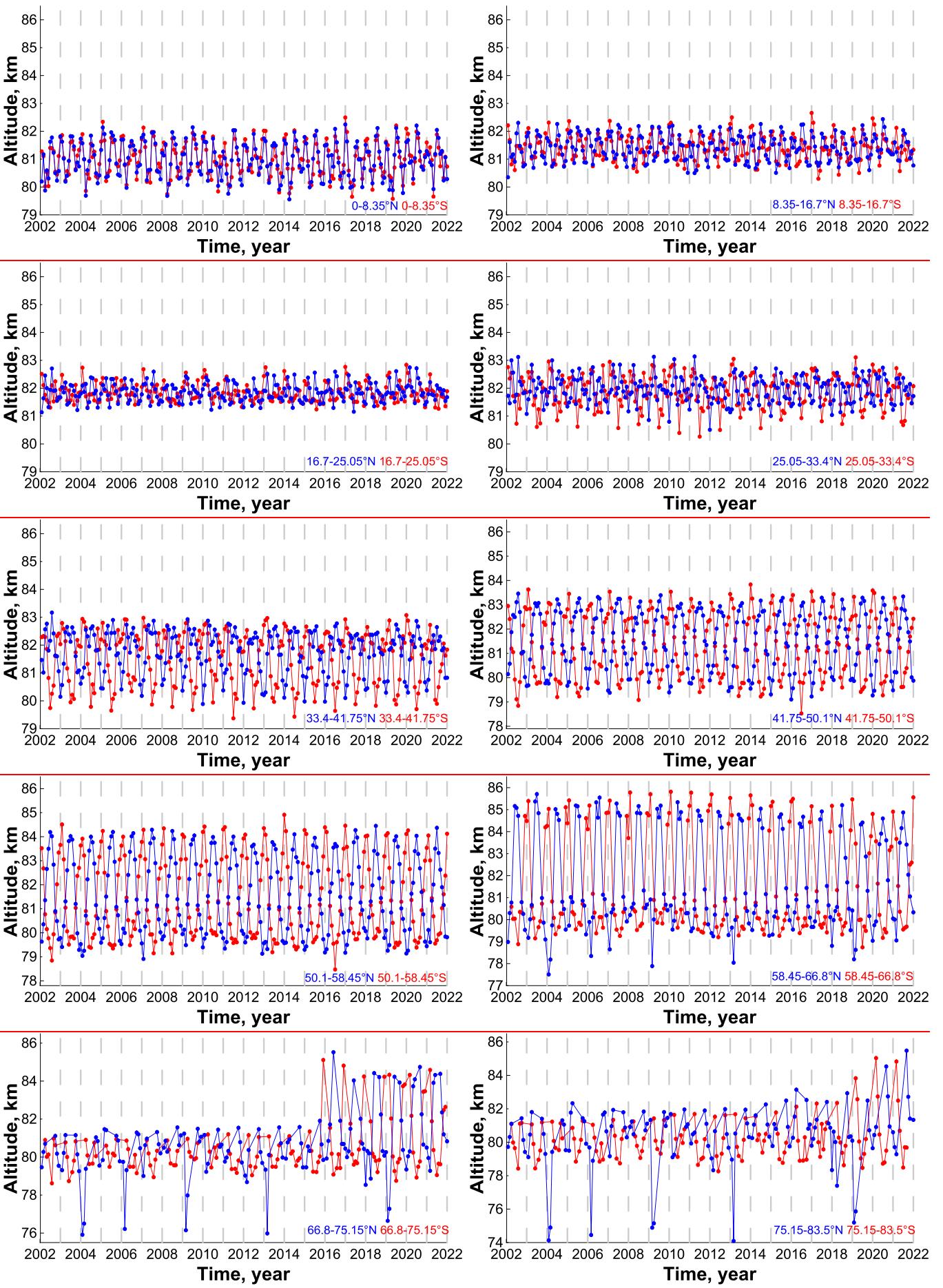
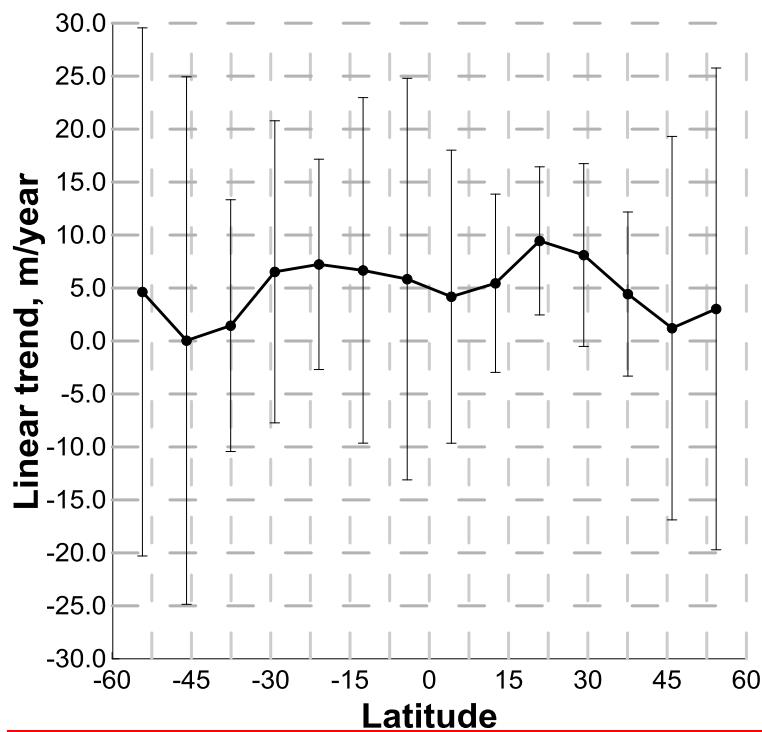
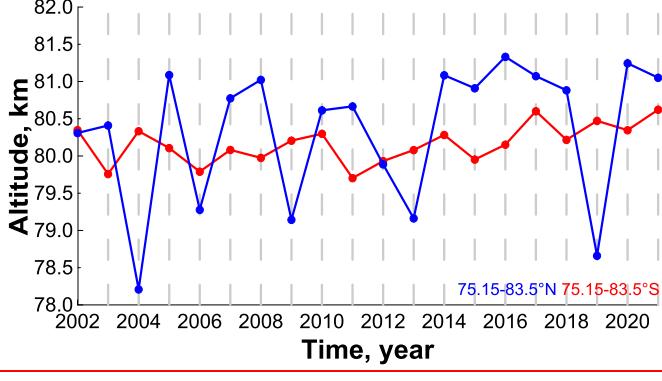
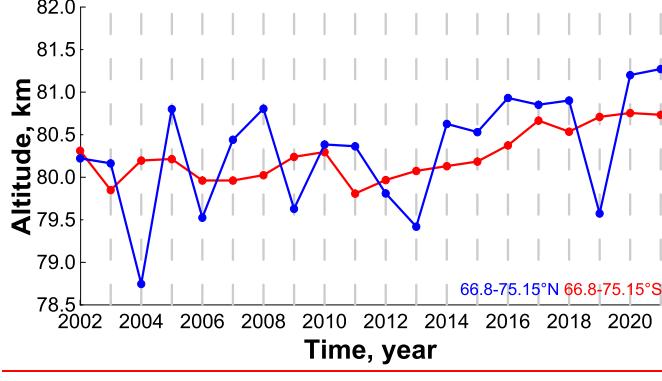
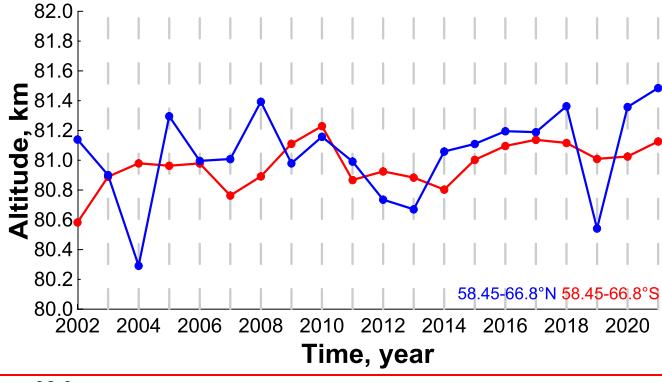
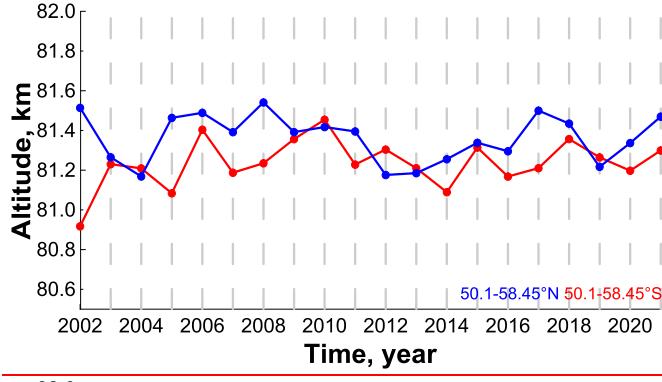
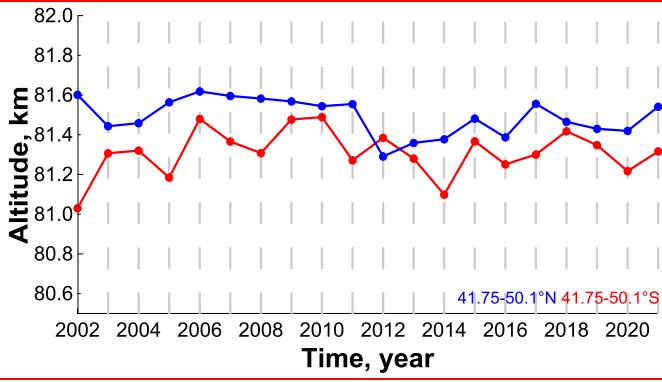
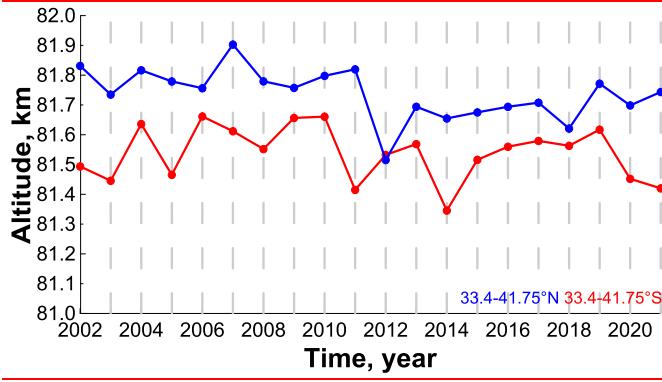
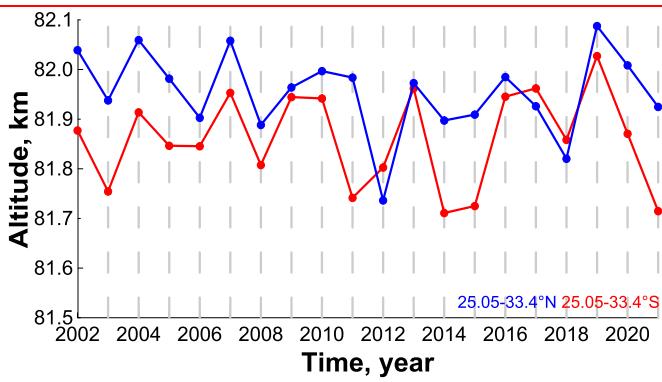
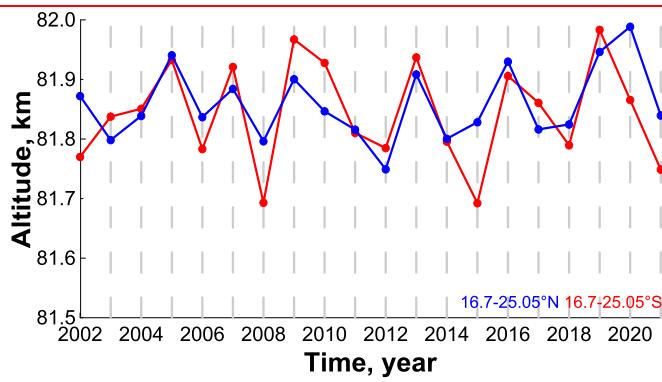
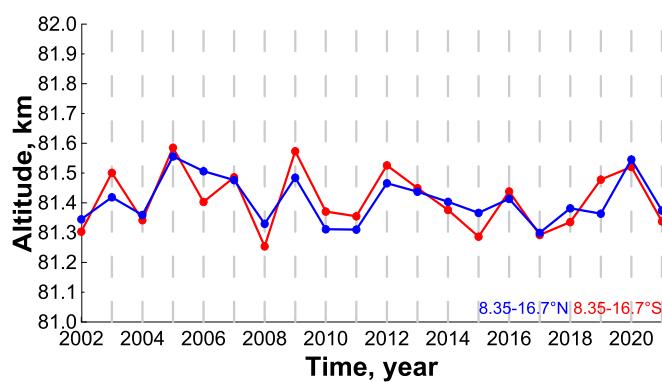
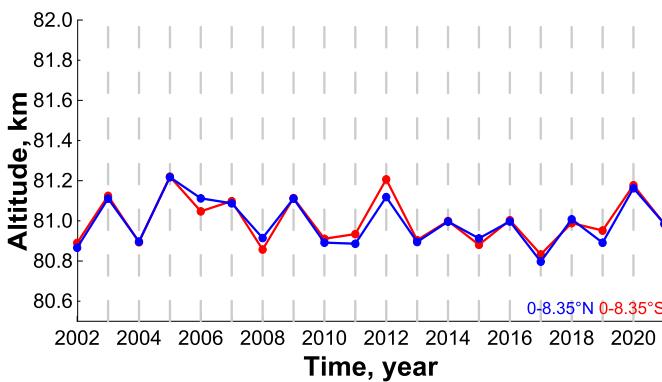


Figure 11.



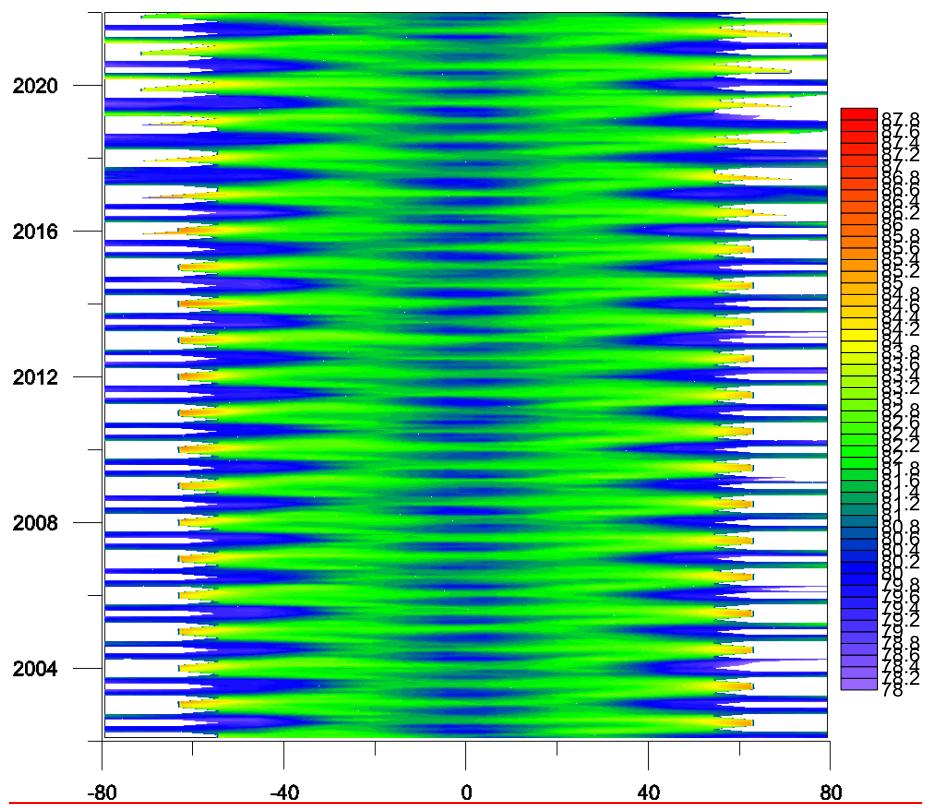
778  
779 Time evolution of monthly mean geometrical altitude  $z_{eq}$   $m$  at different latitudes.  
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786 | Figure 12. ~~Linear trend in  $\langle z_{eq} \rangle^{pa}$  Time evolution of annually mean geometrical altitude  $z_{eq}^y$  at~~

787 | different latitudes derived from multiregression analysis.





789 ~~Figure 13. The space time evolution of  $z_{eq}$ . White color indicates data gaps due to the satellite sensing~~  
790 ~~geometry.~~  
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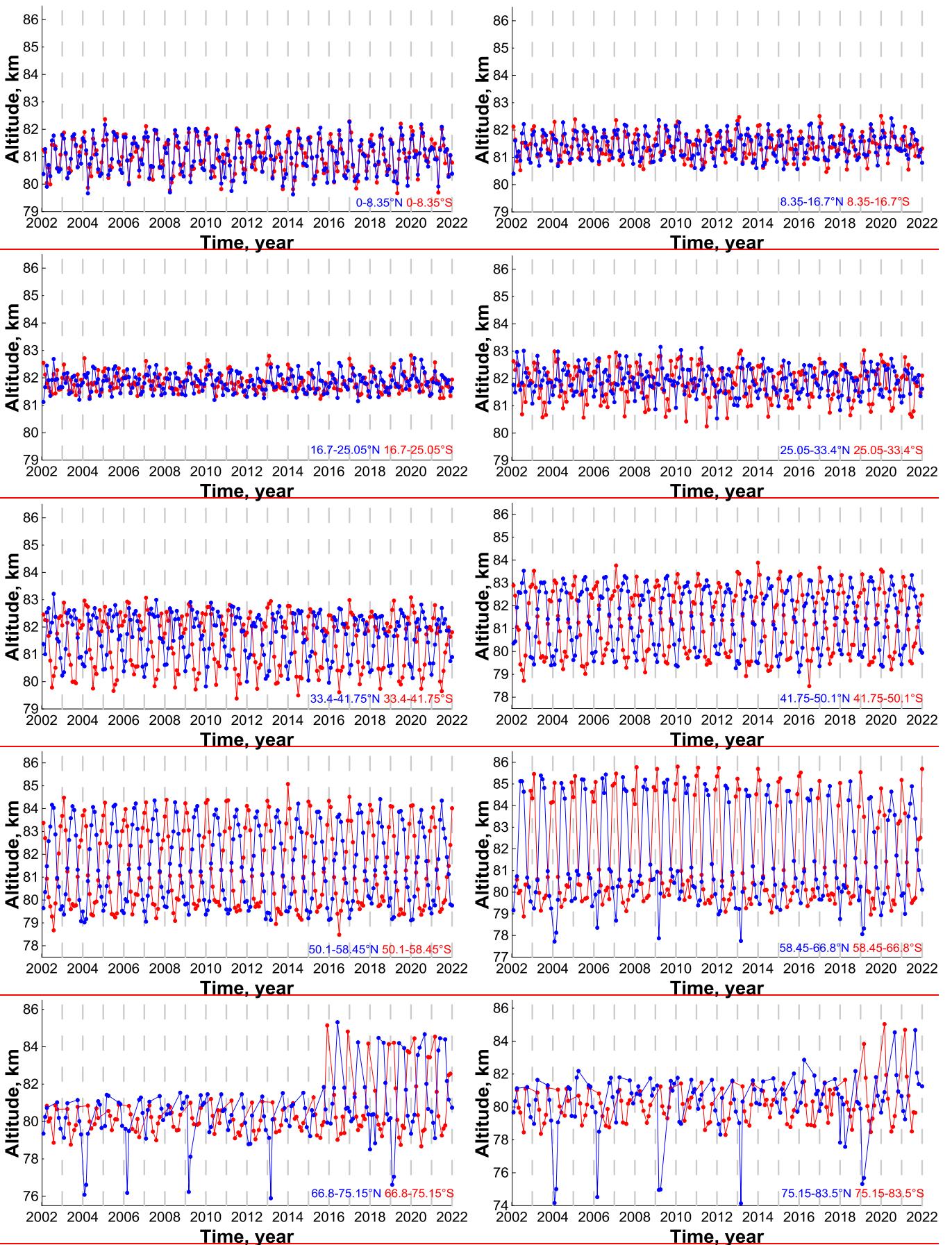


Figure 14. The time evolution of  $z_{eq}$  at different latitudes.

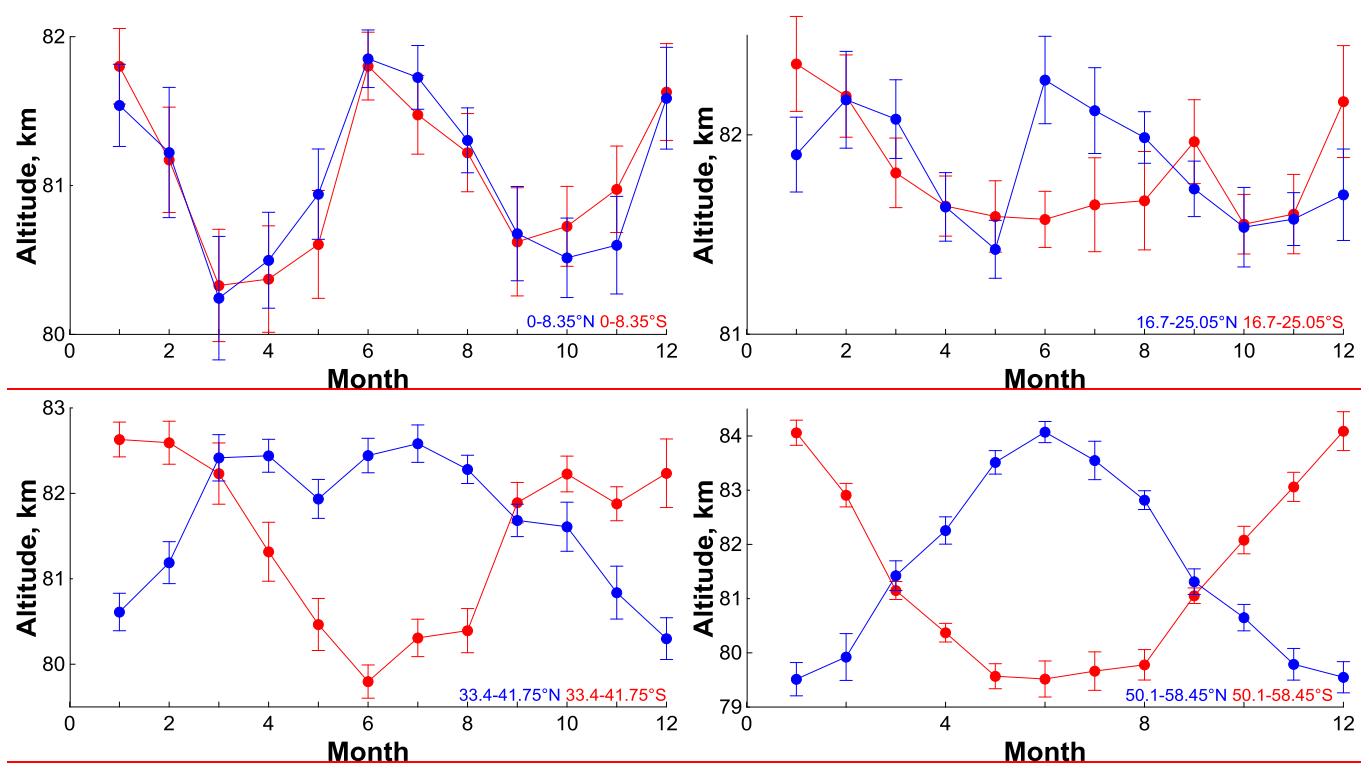
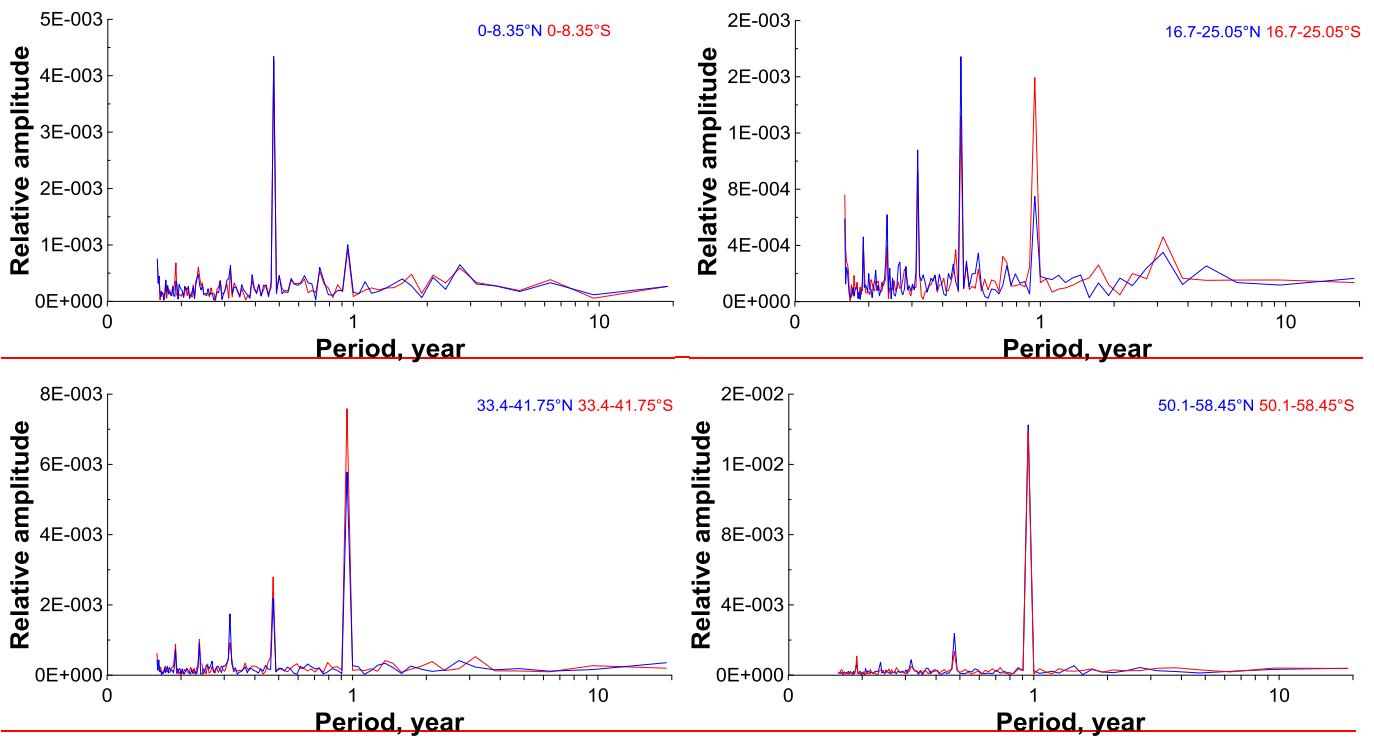


Figure 15. Average (for 2002-2021) annual cycle of  $z_{eq}$  at some latitudes.



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806 **Figure 16.** Fourier' spectra of  $z_{eq}$  time evolution at different latitudes. In each spectrum, the amplitudes of  
807 harmonics were normalized to corresponding zero harmonic.  
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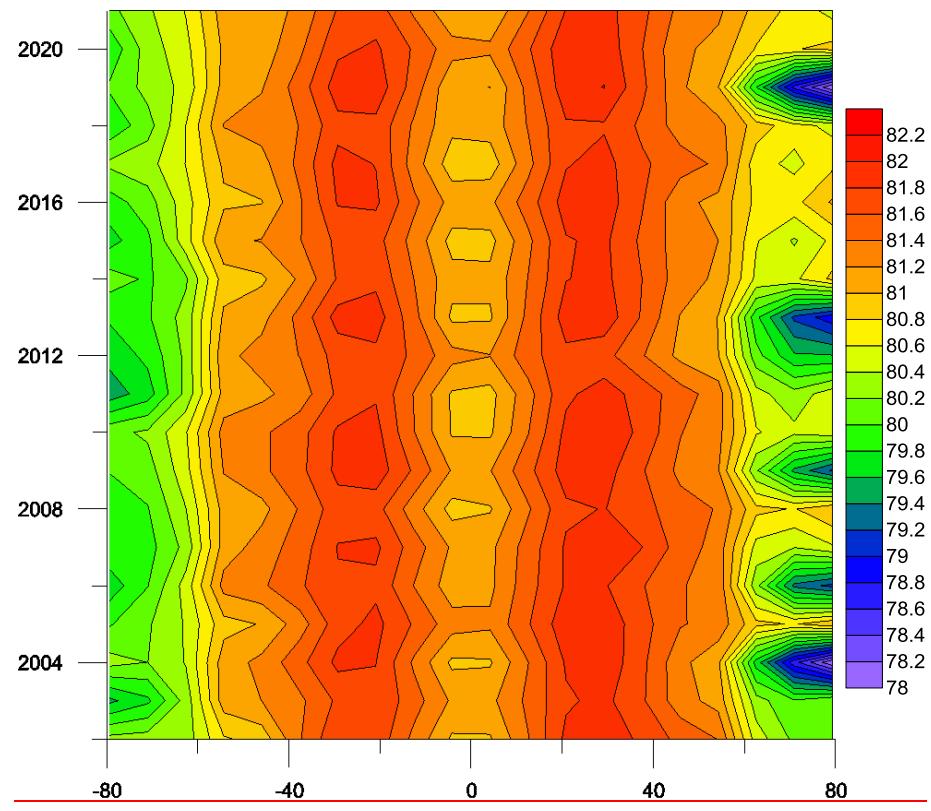


Figure 17. The latitude-time evolution of average annual  $z_{eq}$ .

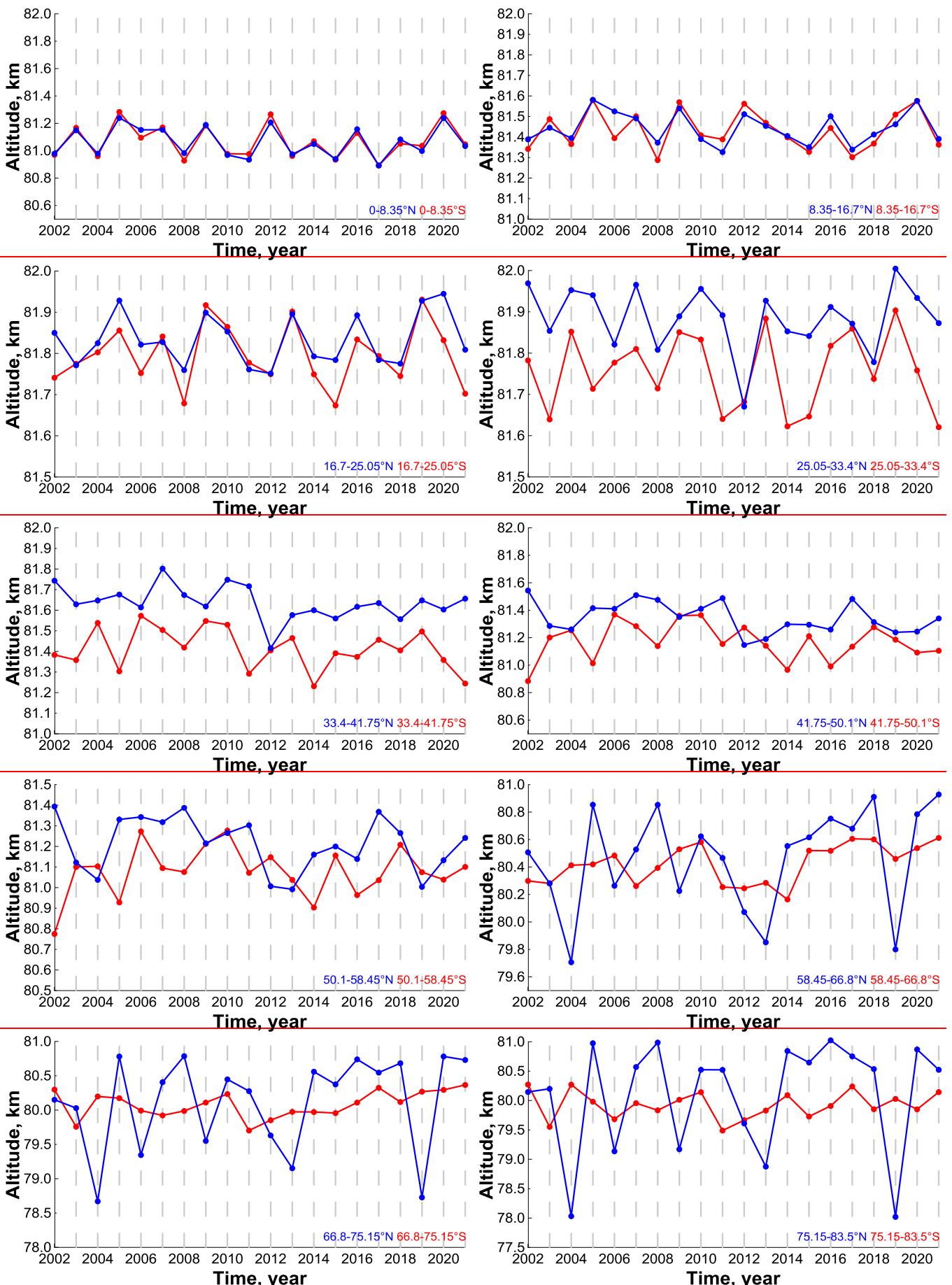


Figure 18. The time evolution of average annual  $z_{eq}$  ( $\langle z_{eq} \rangle$ ) at different latitudes.

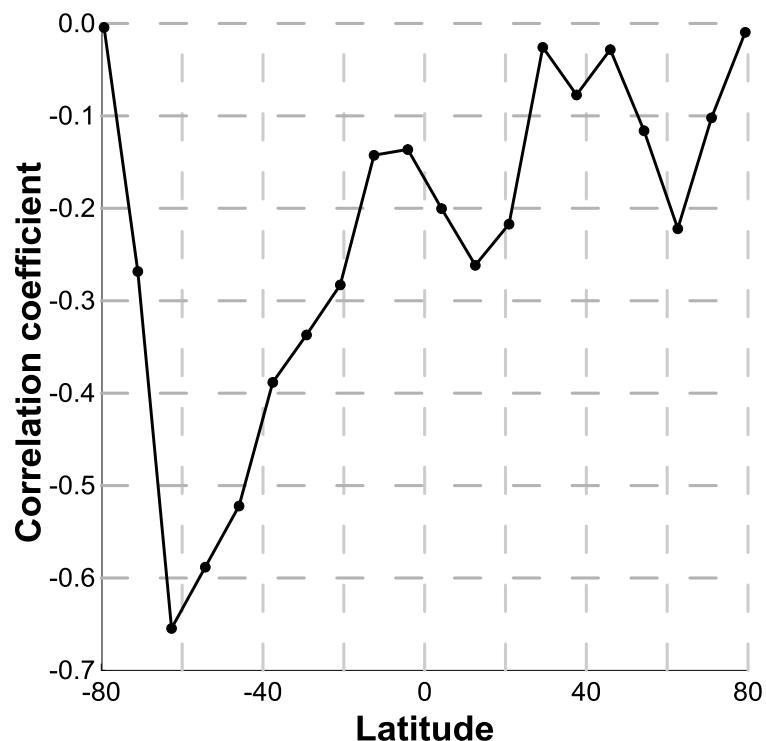
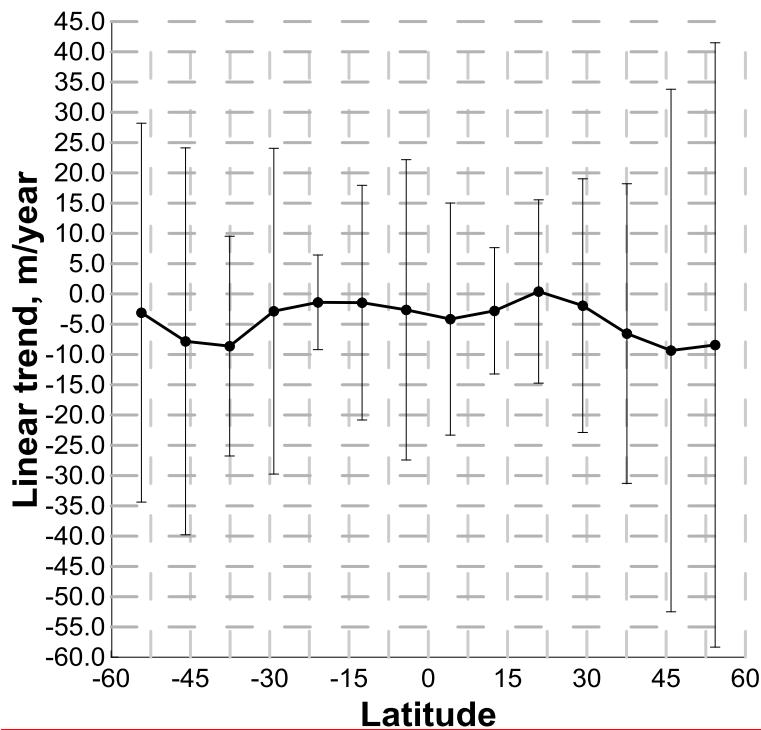
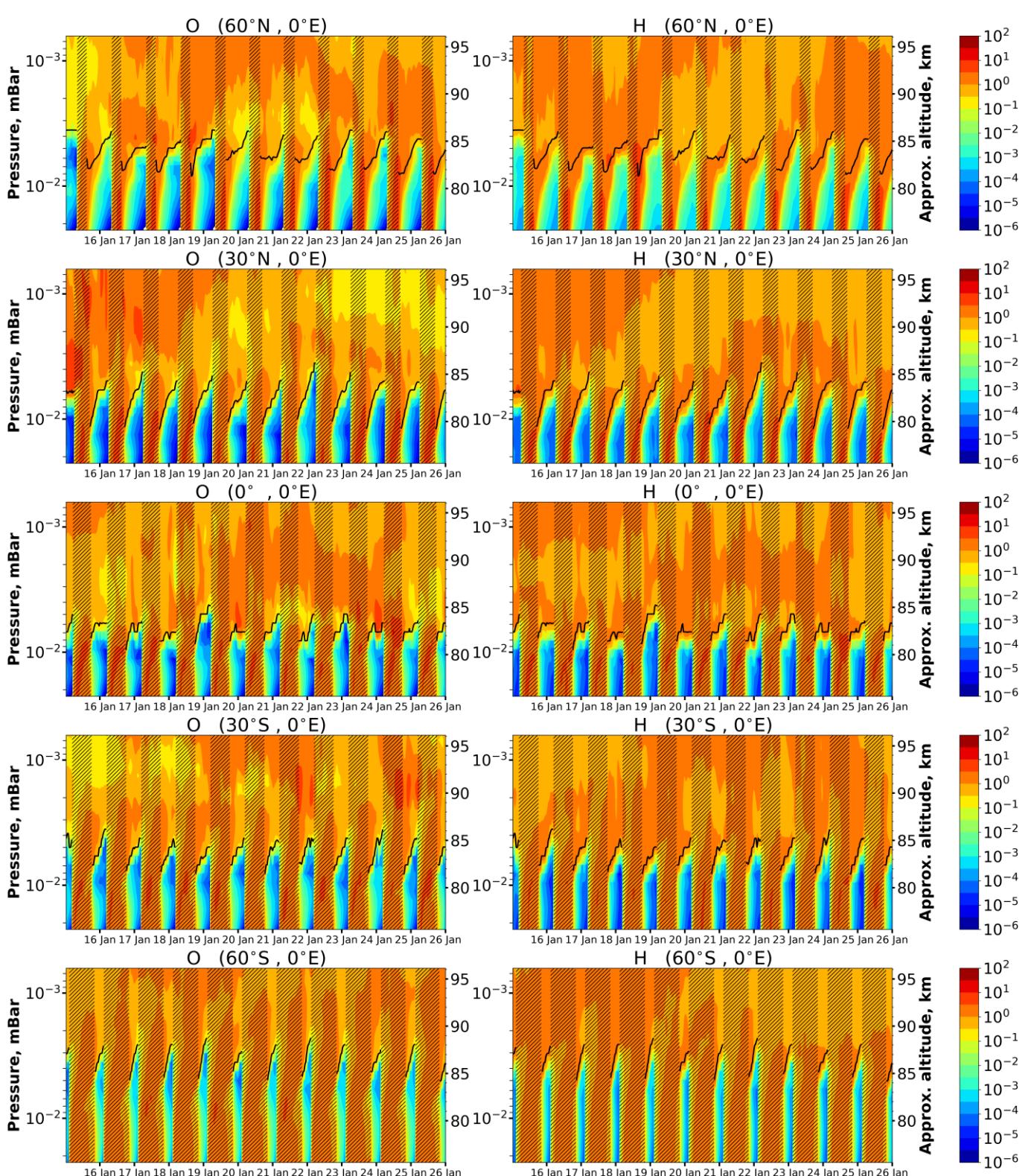
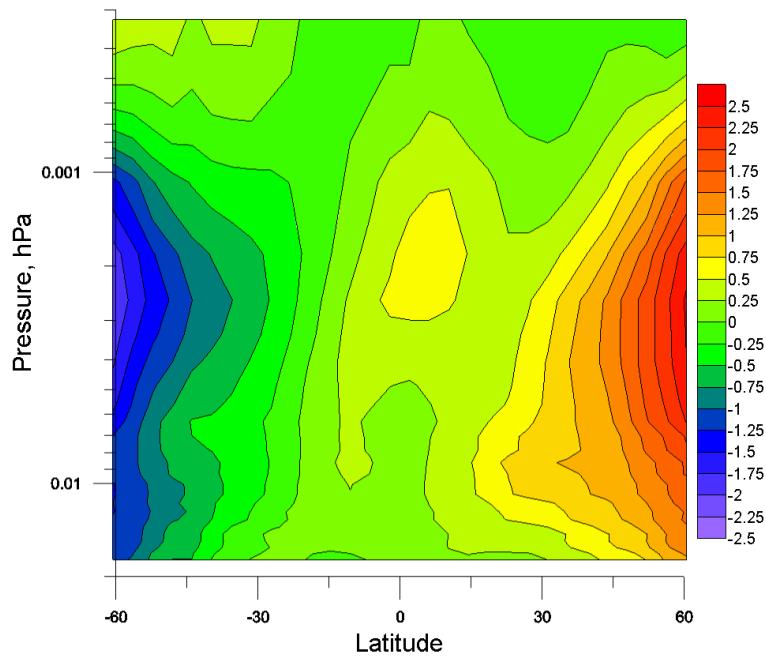


Figure 19. The correlation coefficient of  $\langle z_{eq} \rangle$  with  $F_{10.7}$  index at different latitudes.





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Figure 13. O and H time-height variations above different points in January 2017 calculated by 3D chemical  
transport model CMAM. Concentrations are normalized by mean daily values, correspondingly. Dark bars mark  
daytime, light bars mark nighttime. Black lines point the NOCE boundary altitude according to criterion (5)  
( $Cr = 0.1$ ).



831  
 832 Figure 14. Logarithm of the ratio of  $(O/H)_w$  and  $(O/H)_s$  distributions obtained with the use of daytime  
 833 seasonally mean distributions of O and H averaged in 2003-2015.  $(O/H)_w$  was determined from the  
 834 SABER data measured in December, January, and February.  $(O/H)_s$  was determined from the SABER  
 835 data measured in June, July, and August.