

Vortex Preconditioning of the 2021 Sudden Stratospheric Warming: Barotropic/Baroclinic Instability Associated with the Double Westerly Jets

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Abstract. This study explores the abrupt split of the polar vortex in the upper stratosphere prior to a recent sudden stratospheric warming event on 5 January 2021 (SSW21) and the mechanisms of vortex preconditioning by using the Modern-Era Retrospective Analysis for Research and Applications version 2 (MERRA2) global reanalysis data. SSW21 is preceded by the highly distorted polar vortex that was initially displaced off the pole but eventually split at the onset date. Vortex splitting is most significant in the upper stratosphere (1 hPa altitude) accompanied by the anomalous growth of westward-propagating planetary waves (PWs) of zonal wavenumber (ZWN) 2 (WPW2). While previous studies have suggested the East Asian trough as a potential source for the abnormal WPW2 growth, the prominent westward-propagating nature cannot be explained satisfactorily by the upward propagation of the quasi-stationary ZWN2 fluxes in the troposphere. More importantly, WPW2 exhibits an obvious in-situ excitation signature within the barotropically and baroclinically destabilized stratosphere, dominated by the easterlies descending from the stratopause containing the WPW2 critical levels. This suggests that the vortex split is attributed to the WPW2 generated in situ within the stratosphere via instability. Vortex destabilization is achieved as the double-jet structure consisting of a subtropical mesospheric core and a polar stratospheric core develops into SSW21 by encouraging the anomalous dissipation of the upward-propagating tropospheric ZWN1 PWs. This double-jet configuration is likely a favorable precursor for SSW onset, not only for the SSW21 but generally for most SSWs, through promoting the anomalous growth of unstable PWs as well as the enhancement of the tropospheric PW dissipation.

1 Introduction

Sudden stratospheric warming (SSW) is a dramatic stratospheric phenomenon when the cold and strong westerly polar night jet (PNJ) rapidly decelerates or even reverses to easterly with an enormous warming within a week (Matsuno, 1971). During SSW, the polar vortex is largely displaced away from the pole and/or split into two vortices (Charlton and Polvani, 2007, CP07). The impact of SSW is not limited to the polar stratosphere but extends into the mesosphere and above, causing significant changes in the residual circulations (Limpasuvan et al., 2016; Siskind et al., 2010), the distributions of chemical constituents such as ozone (Manney et al., 2009; Pedatella et al., 2018), and the atmospheric tides both in the Northern and Southern hemispheres. The dramatic temperature and wind perturbations during SSWs also descend into the troposphere, thereby altering the storm tracks which are closely tied to the surface weather patterns (Baldwin and Dunkerton, 2001; Hitchcock and Simpson, 2016).

SSW has been recognized as a manifestation of the interaction between the vertically propagating planetary waves (PWs) and stratospheric mean-flow. This is primarily driven by the upward-propagating anomalous tropospheric wave pulses, which can provide sufficient wave forcings to breakdown the polar vortex (Matsuno, 1971), and/or preconditioning of the stratosphere that focuses the tropospheric wave fluxes—not need to be anomalously strong—into the polar stratosphere (Birner and Albers, 2017; Palmer 1981). The preconditioning perspective has also been discussed in terms of the spontaneous wave explosion within the stratosphere (Plumb, 1981) as the polar vortex tunes itself toward the explosive wave-growth point, such as resonance (Albers and Birner, 2014, AB14) or barotropic/baroclinic (BT/BC) instability (Sato and Nomoto, 2015). Recent supports for the vortex preconditioning have been identified from observational (AB14; Iida et al., 2014) and modeling (Rhodes et al., 2021, RLO21) studies on the split-type SSW of January 2009 (SSW09). Such self-tuned SSWs are characterized by nearly instantaneous wave amplification throughout the entire stratosphere at the SSW onset. Within this context, AB14 interpreted the explosive growth of stratospheric wave activities as a manifestation of vortex breakdown, not the cause of SSW.

The major SSW took place on 5 January 2021 (SSW21), exhibiting the highly distorted polar vortex that was initially displaced off the pole but eventually split at the onset date. During the prewarming period, an initial zonal wavenumber

(ZWN) 1 pulse followed by a ZWN2 pulse was identified in the tropopause, suggesting their contributions to the observed vortex collapse (Cho et al., 2022; Lu et al., 2021; Rao et al., 2021). Lu et al. (2021) and Rao et al. (2021) related the intensification of the Aleutian low and the North Atlantic high in late December 2020 to the enhanced tropospheric ZWN1 flux and that of the East Asian trough developed in early January 2021 to the succeeding ZWN2 flux. By performing numerical experiments, Cho et al. (2022) showed that the tropospheric ZWN1 pulse is attributed primarily to the North Pacific bomb cyclones that deepened the Aleutian low with a minor contribution from the Ural blocking.

This study expands upon previous research on SSW21 by examining the prewarming evolution of the vortex throughout the entire stratosphere, rather than solely in the region below 10 hPa conducted by most of previous studies on SSW21. We found that the most significant vortex split occurs in the upper stratosphere (1 hPa). However, the anomalous stratospheric ZWN2 PWs (PW2) amplification responsible for this split cannot be explained by the concomitantly enhanced tropospheric ZWN2 fluxes. Therefore, this study explores vortex preconditioning in the context of the spontaneous PW2 explosion while addressing two questions: i) What is the source of the stratospheric PW2 amplification? ii) How does the stratospheric vortex evolve toward the wave-growth point? To our knowledge, this is the first study to explore the role of vortex preconditioning in SSW21, providing more comprehensive accounts of the dynamics leading to SSW21.

2 Data and Analysis Methods

2.1 The MERRA2 reanalysis data

We use the Modern-Era Retrospective analysis for Research and Applications, version 2 (MERRA2) reanalysis data with a horizontal resolution of $0.625^\circ \times 0.5^\circ$ (longitude \times latitude) and a temporal resolution of 3 hours from the surface to an altitude of 0.1 hPa (Gelaro et al., 2017) covering 42 years (1980–2021). All results in this study are based on the daily average.

2.2 Analysis methods

The Eliassen-Palm flux (EP-flux) and their divergence (EPFD), representing the wave activity flux and wave forcing, respectively, are calculated based on the following formulation (Andrews et al., 1987):

$$\mathbf{F} = (F^\phi, F^z) = \rho_0 a \cos \phi \left(-\overline{u'v'} + \bar{u}_z \frac{\overline{v'\theta'}}{\bar{\theta}_z}, \left[f - \frac{1}{a \cos \phi} (\bar{u} \cos \phi)_\phi \right] \frac{\overline{v'\theta'}}{\bar{\theta}_z} - \overline{u'w'} \right), \quad (1)$$

$$\nabla \cdot \mathbf{F} = \frac{1}{a \cos \phi} \frac{\partial}{\partial \phi} (F^\phi \cos \phi) + \frac{\partial F^z}{\partial z}, \quad (2)$$

where ϕ and z are the latitude and log-pressure height, respectively, ρ_0 is the reference density, a is the mean Earth's radius, and f is the Coriolis parameter. u , v , and w are the zonal, meridional, and vertical wind components, respectively, and θ is the potential temperature. The overbar and prime represent the zonal-mean and the departure from the zonal-mean, respectively. \mathbf{F} is the EP-flux vector, where F^ϕ and F^z are the meridional and vertical components, respectively. EPFD corresponds to $(1/\rho_0 a \cos \phi) \nabla \cdot \mathbf{F}$.

BT/BC instability is evaluated by using the meridional gradient of the quasi-geostrophic potential vorticity (QGPV, Andrews et al., 1987):

$$\bar{q}_y = \beta - \bar{u}_{yy} - \frac{1}{\rho_0} \left(\rho_0 \frac{f^2}{N^2} \bar{u}_z \right)_z, \quad (3)$$

where \bar{q} , β , and N denote the zonal-mean QGPV, the meridional derivative of f , and the Brunt–Väisälä frequency, respectively. The necessary condition for BT/BC instability is that the generally positive \bar{q}_y associated with the wintertime circulation becomes negative (Salby, 1996). In Section 3, we refer to the sum of the first two terms on the right-hand side as the “barotropic term”, while the third term as “baroclinic term”.

A linearized disturbance QGPV equation in log-pressure coordinates is as follows (Andrew et al., 1987):

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$$\left(\frac{\partial}{\partial t} + \bar{u} \frac{\partial}{a \cos \phi \partial \lambda}\right) q' + v' \frac{\partial \bar{q}}{a \partial \phi} = \frac{1}{a \cos \phi} \left[\frac{\partial Y'}{\partial \lambda} - \frac{\partial(X' \cos \phi)}{\partial \phi} \right] + \frac{f_0}{\rho_0} \frac{\partial}{\partial z} \left[\rho_0 \frac{Q'}{e^{\frac{\kappa}{H} z} \left(\frac{\partial T_0}{\partial z} + \frac{\kappa T_0}{H} \right)} \right], \quad (4)$$

$$q' \equiv \frac{1}{a^2 \cos \phi} \left[\frac{1}{\cos \phi} \frac{\partial^2}{\partial \lambda^2} + \frac{\partial}{\partial \phi} \left(\cos \phi \frac{\partial}{\partial \phi} \right) \right] \psi' + \frac{1}{\rho_0} \frac{\partial}{\partial z} \left(\rho_0 \frac{f_0^2}{N^2} \frac{\partial \psi'}{\partial z} \right), \quad (5)$$

$$\frac{\partial \bar{q}}{a \partial \phi} \equiv \frac{2\Omega \cos \phi}{a} - \frac{1}{a^2} \frac{\partial}{\partial \phi} \left[\frac{1}{\cos \phi} \frac{\partial(\bar{u} \cos \phi)}{\partial \phi} \right] - \frac{1}{\rho_0} \frac{\partial}{\partial z} \left(\rho_0 \frac{f_0^2}{N^2} \frac{\partial \bar{u}}{\partial z} \right). \quad (6)$$

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Here, λ is the longitude, and q' is the QGPV perturbation. X' and Y' denote the perturbation of the zonal and meridional components of gravity wave (GW) forcing from their zonal-mean, respectively. Q' is the perturbation diabatic heating rate, and ψ' is the perturbation streamfunction ($\psi' = \phi'/f_0$, where ϕ' is the perturbation geopotential). The first bracketed term on the right-hand side of Equation (4) is the non-conservative forcing term of the QGPV perturbation associated with the GW drag (GWD). In Section 3, we investigate whether the non-conservative GWD forcing defined by Z' below is related to the rapid enhancement of PW2 by using the zonal and meridional components of the parameterized GWD data (McFarlane 1987; Molod et al., 2015).

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$$Z' = \frac{1}{a \cos \phi} \left[\frac{\partial Y'}{\partial \lambda} - \frac{\partial(X' \cos \phi)}{\partial \phi} \right] \quad (7)$$

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3 Results

3.1 Wind and temperature changes during SSW21

Figure 1a shows the time-evolutions of the zonal-mean zonal wind at 60°N and polar-cap temperature over 60–90°N during the development of SSW21. Remarkably, a reversal of the zonal-mean westerlies appears first in the lower mesosphere on 1 January and descends to 10 hPa within 4 days, leading to the onset of major SSW21 (CP07). It is preceded by the enormous deceleration of PNJ by ~ 108 m/s and a rapid 20 K warming in the upper stratosphere (~ 1 hPa) within 8 days (28 December–4 January). Such a decrease (increase) in the zonal wind (temperature) is statistically significant at the 99% confidence level. Anomalous easterlies and warming descend into the troposphere and persist for longer than 20 days, which is much longer than the average persistence (~ 8 days) following SSWs in the reanalysis and CMIP models (Rao and Garfinkel, 2021).

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3.2 Anomalous Enhancement of the Stratospheric PW2

SSW21 is manifested by the polar vortex being severely displaced from the pole and ultimately split into two just before the onset. Associated PW activities are revealed in Figure 1b, which describes the time-evolutions of the geopotential height (GPH) amplitudes of PW1 and 2 at 60°N. As Lag = -1 is approached, the predominant PW1 amplitude drastically

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125 decreases, while the PW2 amplitude appreciably increases having the statistically significant positive anomaly at the
126 95% confidence level at 1–3 hPa. From Lag = -2 to Lag = 1, PW2 dominates in the mid-to-upper stratosphere above 3
127 hPa. Given the prevalent dominance of PW1 in the high-latitude winter stratosphere (Andrews et al., 1987; Matsuno
128 1970), predominant PW2 activity observed in this case and other split-type SSWs is a notable feature. Evidenced in
129 Figure 1c, which compares the polar-stereography series of the horizontal wind speed and the GPH anomaly at 1 and
130 10 hPa, the vortex split is more pronounced in the upper stratosphere than in the lower stratosphere, where PW1 have
131 surpassed PW2 (Figure 1b).

132 Previous studies have suggested that the vortex split is attributed to the enhanced tropospheric ZWN2 fluxes entering
133 the stratosphere, as evidenced by peak pulses of the ZWN2 eddy heat flux averaged over 45–75°N at 100 hPa during 1–
134 5 January. However, this period nearly coincides with that of remarkable PW2 amplification in the upper stratosphere
135 (Figure 1b). This implies that the increased tropospheric fluxes must have instantaneously propagated up to ~28 km
136 within the mid-to-upper stratosphere, which is highly questionable. Therefore, we examine whether the large
137 tropospheric pulses are traceable to the upper stratosphere at the standard group velocity for vertically propagating PW2.
138 Figure 2a illustrates the time-height cross section of the vertical component of EP-flux (EPFz) of PW2 in 45–75°N and
139 the three identical vectors with a slope of 5.5 km/day that correspond to the theoretical group velocity of the vertically
140 propagating Rossby waves of ZWN2 (Esler and Scott, 2005). For comparison purpose with previous studies, the time-
141 series of eddy heat flux ($\overline{v'T'}$) of ZWN1 and 2 in 45–75°N at 100 hPa are also presented below.

142 While $\overline{v'T'}$ of ZWN1 reduces, that of ZWN2 increases from 28 December (Lag = -8), attaining a magnitude 1 STD
143 greater than the climatology (but not significant) during 1–5 January. The theoretical prediction of Rossby waves’
144 vertical propagation well matches the vertical propagation of EPFz below 5 hPa, indicating that the bulk of ZWN2
145 fluxes propagate upward (AB14). However, as evidenced by the third group velocity vector, these waves could approach
146 the upper stratosphere ~2 days after the onset date via upward propagation. This implies that the statistically significant
147 PW2 amplification in the upper stratosphere in Lag = -3–Lag = -1 (Figure 1b) cannot originate from the anomalous
148 injection of the tropospheric wave activity during the same period.

149 More importantly, EPFz is not continuous above 5 hPa and exhibits apparent divergences with the downward EPFz
150 (negative) below the region of upward EPFz (positive) around 3 hPa from Lag = -5 to Lag = -3. Despite the
151 disappearance of downward EPFz after Lag = -2, the divergence continues with the locally maximized upward EPFz
152 above 5 hPa from Lag = -1 to Lag = 1. This feature cannot be explained by linear upward propagation, suggesting a
153 potential for the in situ PW2 generation within the stratosphere. In this view, subsequent statistically significant
154 enhancement in the upward EPFz (exceeding 99% confidence level) above the divergence altitude could be a
155 consequence of the upward propagation of the in situ generated PW2.

156 The evolution of the PW2 GPH in 45–75°N, as a function of zonal phase speed and time at the three altitudes depicted
157 in Figure 2b, supports this perspective. During the strengthening period of ZWN2 $\overline{v'T'}$ (Lag = -8–0), the tropospheric
158 PW2 (100 hPa) has a quasi-stationary nature, whereas the stratospheric PW2 (1–3 hPa) has prominent westward phase
159 speeds of 10–30 m/s (WPW2). The stratospheric WPW2 cannot be explained solely by the upward propagation of the
160 quasi-stationary tropospheric PWs.

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162 3.3 In situ Source of the Stratospheric WPW2: BT/BC Instability

163 To examine the potential source of the stratospheric PW2, we first investigate EP-fluxes and EPFD of PW2 during the
164 WPW2 amplification period (1–5 January, Figure 3a). In this analysis, the overall PW2 behavior is investigated, not
165 exclusively for WPW2.

166 Throughout the period, significantly anomalous divergence of EP-fluxes (positive EPFD) appears, developing with the
167 rapidly intensifying easterlies. This demonstrates the spontaneous PW2 emanation within the stratosphere, which is
168 associated with the background flow: positive EPFD first appears between the easterlies extending from the equatorial
169 stratosphere and the polar jet core (Lag = -4). As the polar stratosphere becomes dominated by the descending
170 stratopause easterlies, the divergence is also enlarged towards 10 hPa and simultaneously intensified, exceeding 50
171 m/s/day at Lag = -2. While the easterlies further strengthen after that, the divergence area narrows below the jet core.
172 Nevertheless, the PW2 fluxes evolving along their propagation have magnitudes comparable to or even greater than the
173 previous ones. The upward propagating tropospheric fluxes, on the other hand, converge before reaching the easterlies,
174 imposing westward forcing. This is consistent with their quasi-stationary nature, which is inhibited by the zero-wind

175 line.

176 As a plausible in situ source for the stratospheric PW2, BT/BC instability is examined. Figures 3b–3d present the
177 latitude-height cross sections of \bar{q}_y and the barotropic and baroclinic terms of Equation (3), respectively. Negative \bar{q}_y
178 satisfying the BT/BC instability condition emerges around the positive EPFD areas during the overall period. Similar to
179 the positive EPFD, this instability is exacerbated by the developing easterlies, attributed to both the barotropic and
180 baroclinic terms. The strengthening easterlies induce the positive \bar{u}_{yy} along their maxima, which dominates the positive
181 β , leading to the vertically oriented negative barotropic term (Figure 3c). Concurrently, the baroclinic term becomes
182 negative from below the easterly core (Figure 3d). To elucidate the dominant factors that make the baroclinic term
183 negative, the third term of the right-hand side of Equation (3) is expanded as follows:

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$$185 \quad -\frac{1}{\rho_0} \left(\rho_0 \frac{f^2}{N^2} \bar{u}_z \right)_z = f^2 \left[\frac{1}{H} \frac{1}{N^2} \bar{u}_z + \frac{1}{N^4} \frac{dN^2}{dz} \bar{u}_z - \frac{1}{N^2} \bar{u}_{zz} \right], \quad (8)$$

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187 where H is the scale height (7 km).

188 Figures 4a–4c present the latitude-height cross sections of the first, second, and third terms of the right-hand side of
189 Equation (8), respectively, divided by f^2 on 3 January as a representative case of the vortex destabilization period (1–5
190 January). It shows that the negative baroclinic term is attributed to both the first and third terms within the developing
191 easterlies in the polar stratosphere, with an insignificant compensation by positive value from the second term.

192 Figures 4d–4g show the latitude-height cross sections of the inverse of the squared Brunt–Väisälä frequency $1/N^2$, the
193 vertical gradient of the zonal-mean zonal wind \bar{u}_z , the vertical gradient of the Brunt–Väisälä frequency dN^2/dz , and
194 the vertical curvature of the zonal-mean zonal wind \bar{u}_{zz} , respectively, those consist of the three terms on Equation (8).
195 The negative first term is induced by the negative \bar{u}_z (Figure 4e) as the subtropical stratospheric easterlies that propagate
196 to the polar stratopause descend into the lower stratosphere on 2–5 January (Figure 3). This negative \bar{u}_z along with the
197 negative dN^2/dz (Figure 4f) makes the second term positive below the easterly jet core. The negative third term, which
198 is maximized above the easterly jet core, is caused by the strong positive \bar{u}_{zz} (Figure 4g) under relatively small
199 contribution by $1/N^2$ (Figure 4d). Therefore, we conclude that the negative baroclinic term is attributed to the negative
200 \bar{u}_z (positive \bar{u}_{zz}) below (centered at) the easterly jet core. Above findings suggest that the developing easterlies cause
201 WPW2 excitation by encouraging strong shear instabilities. These findings align with the numerical study by Dickinson
202 (1973): To serve instability as a source for PWs of a certain zonal phase speed C_x , the region must include a critical
203 layer where the zonal-mean zonal wind matches C_x . The presence of WPW2 critical levels near the in situ PW2
204 generation region is confirmed by the range of easterlies (–40–0 m/s) encompassing that of PW2’s C_x in the mid-to-
205 upper stratosphere (1–3 hPa, Figure 2b). The collocation of negative \bar{q}_y , the emergent PW2, and their critical levels
206 demonstrates that WPW2 grows by extracting energy from the unstable flow.

207 Yamazaki et al. (2021) found similar bursts of quasi-4-day WPW2s originating from the unstable stratosphere beyond
208 their critical level during the major SSWs in 2009, 2013, 2018, and 2019. Regarding the appearance of eastward-
209 propagating PWs of ZWN2 (EPW2) in the mesosphere before the SSW09 onset, Iida et al. (2014) also suspected in situ
210 generation via BT/BC instability in the westerly flow regime. RLO21 confirmed this possibility by identifying the
211 existence of the EPW2 critical level, but they interpreted EPW2 emergence as the over-reflection of the tropospheric
212 PW2 propagating upward. We explore the possibility of over-reflection for the amplified WPW2 by examining the
213 squared refractive index (n^2):

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$$215 \quad n^2 = \left[\frac{\bar{q}_\phi}{a(\bar{u} - C_x)} - \left(\frac{k}{a \cos \phi} \right)^2 - \left(\frac{f}{2NH} \right)^2 \right] a^2. \quad (9)$$

216

217 Here, we set the zonal wavenumber $k = 2$ and the zonal phase speed $C_x = -10$ m/s, which corresponds to the identified
218 WPW2 peak in Figure 2b.

219 Figure 5 presents the latitude-height cross sections of the regions of negative \bar{q}_y and positive n^2 with PW2 EP-fluxes
 220 and EPFD in 2–5 January 2021. On 2 January, the over-reflection signal that bears a resemblance to the illustration in
 221 Figure 1 in RLO21 is identified. Following the waveguide (orange hatched), the upward-propagating WPW2 are allowed
 222 to reach the unstable region (mint shaded) where the critical level of WPW2 ($C_x = -10$ m/s) is located. Leaving behind
 223 a strong EP-flux divergence region, downward PW2 EP-flux vectors point away from the evanescent region of negative
 224 n^2 (without orange hatched), which is formed by the negative \bar{q}_y and positive $\bar{u} - C_x$. These downward vectors can be
 225 interpreted as the over-reflection of upward-propagating WPW2. This is consistent with the local downward EPFz below
 226 the upward EPFz in Figure 2a. The positive n^2 region associated with the transition from positive to negative $\bar{u} - C_x$
 227 under the negative \bar{q}_y from the evanescent region is suggestive of subsequent wave transmission. Transmitted waves
 228 propagating from the critical layer can deposit their momentum, creating a region of EP-flux convergence (westward
 229 acceleration). However, such over-reflection features become obscure from 3 January as the downward EPFz below the
 230 evanescent region disappears. Moreover, the region of positive EPFD shifts to higher latitudes (60–90°N) than the region
 231 where the upward-propagating WPW2 can reach (30–60°N). Therefore, the observed WPW2 amplification are not
 232 satisfactorily explained through the over-reflection perspective.

233 Close inspection of the squared refractive index in Figure 5 also confirms that the wave resonance suggested by AB14
 234 is less likely for the observed WPW2 explosion. Resonant wave events require a three-sided cavity of vertically
 235 propagating PWs capable of trapping their energy. Such a cavity consists of two vertically oriented critical lines—one
 236 in the midlatitudes and another in the polar regions—and a third horizontal one across the upper stratosphere. While
 237 several localized regions of positive n^2 exist within the instability areas, obvious features indicative of wave cavity are
 238 not identified. Furthermore, the characteristic EPFz behavior indicating wave resonance, that is, vertically instantaneous
 239 EPFz (AB14), is not identified in Figure 2a.

240 Alternately, Song et al. (2020) demonstrated that the mesospheric EPW2 was generated by the zonally asymmetric GW
 241 forcing, the non-conservative source term (Z') in the linearized perturbation QGPV equation in Equation (4). We
 242 examine whether the rapid growth of the stratospheric WPW2 before the SSW21 onset is attributable to this mechanism
 243 by investigating Z' in Equation (7).

244 Figure 6a presents the latitude-height cross section of the zonally averaged Z' magnitude ($|Z'|$) and the positive EPFD
 245 of PW2 on 3 January as a representative for the amplification period of WPW2 (1–5 January). The upward propagating
 246 parameterized GWs are dissipated in regions with strong vertical shears of the zonal-mean zonal winds (see Figure S1),
 247 yielding the zonally asymmetric GW forcings. Accordingly, the zonal-mean $|Z'|$ is also identified above the strong shear
 248 region, where the positive EPFD is located. However, due to the small magnitude of the GW forcing, $|Z'|$ above the
 249 positive EPFD region (1–5 hPa) is much smaller than $|Z'|$ in the upper stratosphere and lower mesosphere (above 0.5
 250 hPa), where Z' became significant enough to generate EPW2 in Song et al. (2020). More importantly, as evidenced from
 251 a polar stereography of Z' shown in Figure 6b, we cannot recognize an obvious ZWN2 structure. Therefore, we rule out
 252 the possibility of in situ WPW2 generation driven by zonally asymmetric GW forcing as a non-conservative source of
 253 QGPV perturbation. Thus, at least for the case of SSW21, our results support that BT/BC instability is the most likely
 254 source.

255

256 3.4 Vortex Preconditioning: Double Westerly Jets

257 The above findings lead us to examine the prewarming evolution of PNJ, which adjusts the vortex conducive to
 258 instability. Figures 7a and 7b present the latitude-height cross sections of the zonal-mean zonal wind and the resolved
 259 wave (RW) activities, respectively.

260 On 1–10 December 2020, the wind structure is similar to climatology, with a single maximum in the high-latitude
 261 stratosphere. However, after the westerlies weaken over the following 10 days (11–20 December), the maximum moves
 262 to the subtropical upper mesosphere (21–28 December). On 29 December, the wind structure largely deviates from the
 263 climatology, consisting of two local maxima with comparable strength: one in the subtropical lower-mesosphere and the
 264 other in the polar stratosphere. This so-called a double-jet configuration was also identified before the SSW09 onset
 265 (Iida et al., 2014; RLO21). Along between the two maxima, the subtropical easterly progresses towards the polar
 266 stratopause, which corresponds to a significant negative anomaly above the 95% confidence level. This abnormal
 267 easterly completely separates the double-jets on 1 January, initiating shear instability (Figure 3b).

268 This is achieved through the critical-level interaction between the double westerly jets and RWs (Figure 7b). Around
269 the zero-wind line between the subtropical easterly and the polar westerly, RWs propagating from the mid-latitude
270 troposphere are critical-level filtered, exerting the statistically significant negative EPFD at the 99% confidence level.
271 This negative forcing migrates the subtropical easterly poleward, further separating the jets. Subsequent RWs cannot
272 propagate equatorward any further and are filtered within the poleward-shifted intervening region between the two jets,
273 depositing again the anomalously strong negative forcing. The polar stratopause easterlies attributed to this positive
274 feedback rapidly descend into 10 hPa and intensify dramatically beyond 80 m/s, causing exceptionally strong BT/BC
275 instability. The negative RW forcing is mostly attributed to PW1 (Figure S2), whereas RWs having ZWN greater than
276 1 contributed insignificantly or even counteracted (not shown).

277 In summary, vortex preconditioning for SSW21 is characterized by the double-jet configuration. By facilitating the
278 critical-level interaction with the tropospheric PW1, this wind structure migrates the subtropical stratospheric easterlies
279 into the polar stratopause, thereby initiating catastrophic vortex deceleration and adjusting the vortex toward explosive
280 unstable PW2 growth.

281

282 **3.5 Destabilization of ZWN2 waves**

283 While the westward-propagating nature of the unstable PW2 is explained in connection with the background easterlies,
284 it remains unclear why ZWN2 perturbations are predominantly amplified. One possibility is that the prevailing ZWN2
285 fluxes forced from the troposphere may have been instantaneously destabilized at all altitudes, dominating over other
286 waves. This speculation aligns with Hartmann's (1983) suggestion that predominant disturbances are more likely to be
287 enhanced than those of higher ZWNs, despite their larger growth rates. However, it is not the case because the localized
288 EPFz divergences in the stratosphere are decoupled from the troposphere (Figure 2a). Furthermore, the quasi-stationary
289 tropospheric PW2 are not allowed to enter the stratosphere across their critical layer, as evidenced by their convergence
290 near the zero-wind line (Figure 3a).

291 The more probable explanation is that WPW2 arise in situ within the destabilized stratosphere that nonlinearly interacts
292 with PW1. Hartmann (1983) found that with the presence of PW1, the barotropic instability of PNJ could enhance the
293 growth rates of shorter waves with similar phase speeds. Manney et al. (1991) identified similar destabilization of both
294 waves 2 and 3, but wave 2 in particular. Relevant features are identified in Figure 8, which presents Ertel's PV (EPV)
295 on the 1500 K isentropic surface (near 2 hPa). From 1 January, irreversible mixing associated with substantial PW1
296 dissipation (Figure 7b) causes vortex filamentation along the vortex edge, yielding two additional high EPV cores.
297 Concurrently, the initially localized negative EPV meridional gradient develops into a zonal-mean field, with the higher
298 (lower) EPV advected toward the lower latitudes (pole). With growing instability, the two localized high EPV cores
299 merge into one, exhibiting a ZWN2 pattern. Numerical experiments exploring the most unstable mode with respect to
300 the given zonal flow can provide further convincing evidence, but that is beyond the scope of this study.

301

302 **4 Summary and Conclusion**

303 During the SSW21 onset, an anomalous WPW2 growth appears, which eventually splits the polar vortex. Previous
304 studies have suggested that the enhanced ZWN2 fluxes originating from the tropospheric precursor events are
305 responsible for this stimulating PW2 activities. However, simultaneous enhancements in PW2 activities in the
306 tropopause and the upper stratosphere are not explained solely by the vertical propagation of the tropospheric PW2. The
307 prominent westward-propagating PW2 in the upper stratosphere that differs from the quasi-stationary tropospheric PW2
308 complements this view.

309 This study demonstrates that the explosive WPW2 amplification occurs in situ within the polar stratosphere driven
310 toward BT/BC instability, where the easterlies rapidly descend from the stratopause including the critical layer of WPW2.
311 Vortex destabilization is induced as the abnormal double-jet structure having subtropical mesospheric and polar
312 stratospheric cores evolves toward SSW21 within just 7 days. Therefore, we suggest vortex preconditioning for SSW21
313 as the double-jet structure, which initiates vortex deceleration as well as tunes the vortex toward instability by facilitating
314 the critical-level interaction with the tropospheric PWs.

315 Our findings provide some key insights into preconditioning of SSWs. First, vortex destabilization is an inevitable

316 consequence of the zonal wind reversal to easterlies connected to the major SSWs. We found that all 26 major SSWs
317 for 42 years (selected following the CP07 definition) exhibit BT/BC instability associated with the prevalent easterlies
318 in the stratosphere at their onset (Figure S3). Given that an unstable flow supports the in situ PW explosion, which can
319 even shape the vortex geometry shortly before the SSW onset, we suggest to look in more detail into the influences of
320 BT/BC instability on the characteristics of SSW, including its onset, intensity, and duration. Second, the double-jets
321 structure is likely a stratospheric precursor that favors triggering SSW. Approximately 70% (19) of 26 major SSWs
322 exhibit this wind configuration within two weeks prior to their onset, despite variance in their occurrence timing (not
323 shown). The present case SSW21 that occurred under unfavorable tropical conditions (the westerly quasi-biennial
324 oscillation and weak convections) for SSW, reinforces this perspective. RLO21 also reported that this wind structure
325 and associated unstable PW generation are commonly identified in other SSW events. Therefore, the preceding double-
326 jets structure are worth examining in SSW studies to improve our understanding and predictability of SSWs. While this
327 study focuses on the evolution of the double-jet structure toward SSW, it would also be fruitful to investigate the
328 formation of such wind structure considering the interplay among PWs, GWs, and mean-flow (Iida et al., 2014; RLO21;
329 Sato and Nomoto, 2015).

330 **Data availability**

331 The MERRA2 data are available from the Global Modeling and Assimilation Office at NASA Goddard Space Flight
332 Center through the NASA GES DISC online archive (available online at <https://doi.org/10.5067/WWQSQ8IVFW8>,
333 GMAO, 2015). All results made in this study can be provided by the corresponding authors upon request.

334 **Author contributions**

335 JHY, HYC, and MJK conceived the study. JHY conducted formal analysis and visualized the results. JHY wrote the
336 draft with a contribution from HYC and MJK.

337 **Competing interests**

338 The authors declare that they have no conflict of interest.

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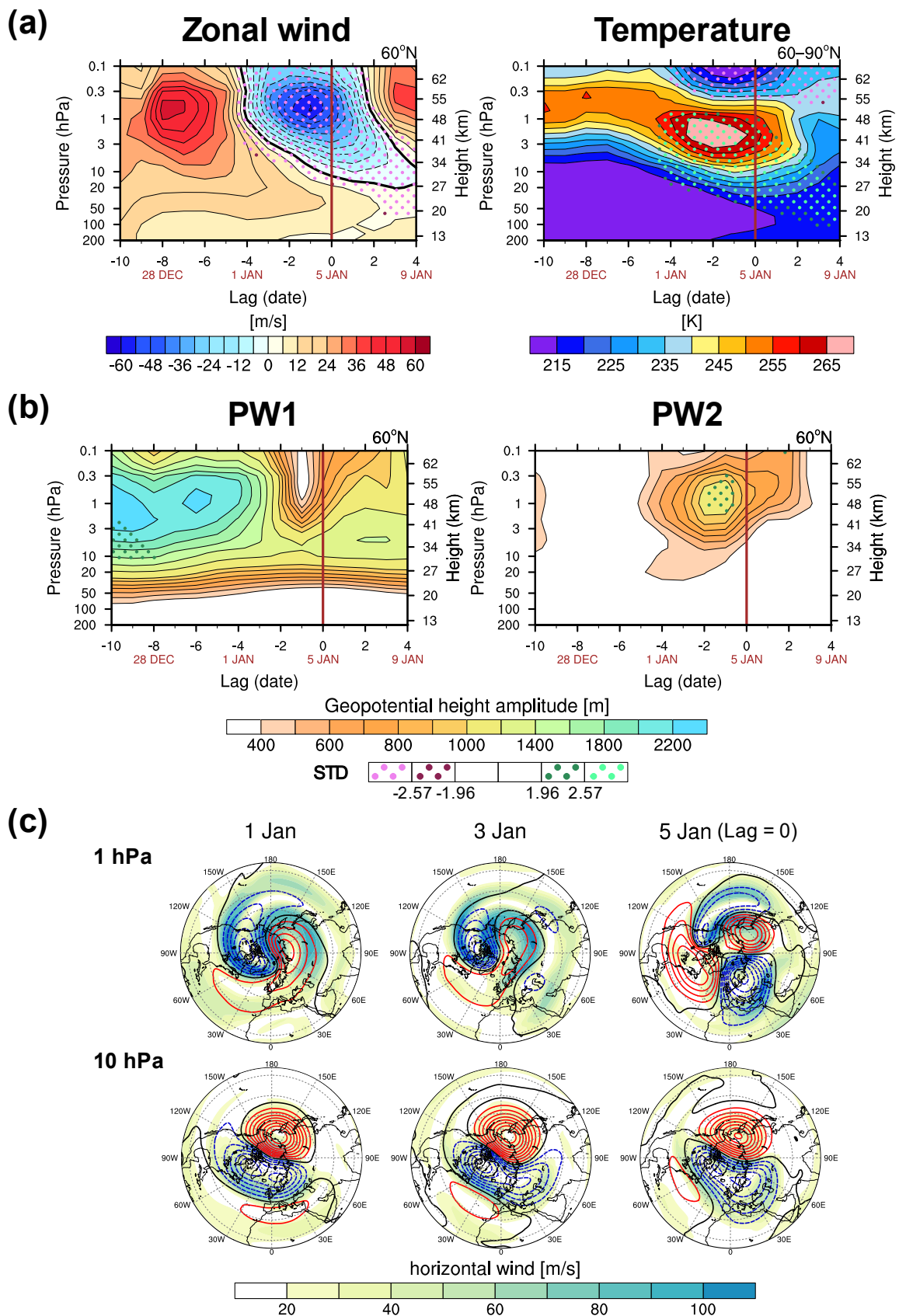
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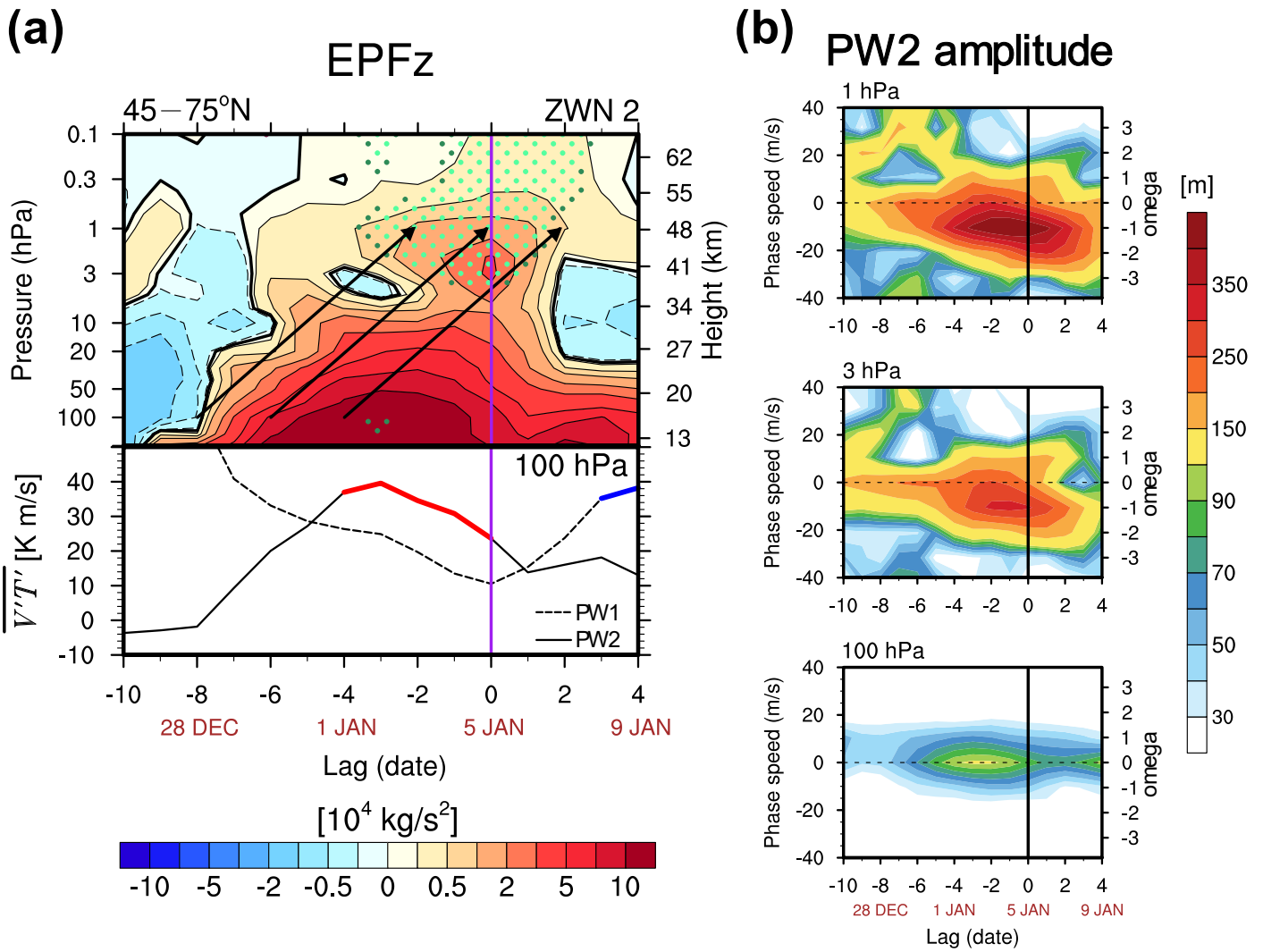
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420

421 **Figure 1:** Time-height cross sections of (a) the zonal-mean zonal wind at 60°N (left) and polar cap temperature averaged
 422 over 60–90°N (right) and (b) the geopotential height (GPH) amplitude of the planetary waves (PWs) with zonal
 423 wavenumbers (ZWN) 1 (PW1, left) and 2 (PW2, right) at 60°N. The dark and bright pink (green) dots denote regions
 424 where the analyzed variable is algebraically smaller (larger) than its 42-year climatology by more than 1.96 and 2.57
 425 standard deviations (STD), indicating that the variable is significantly anomalous at the 95 and 99% confidence levels,
 426 respectively. (c) Polar stereography series of the horizontal wind speed (shading) and GPH anomalies from their zonal-
 427 mean (contours) at 1 hPa (upper) and 10 hPa (lower) on 1, 3, and 5 January. The red (blue) contour represents the
 428 positive (negative) value.



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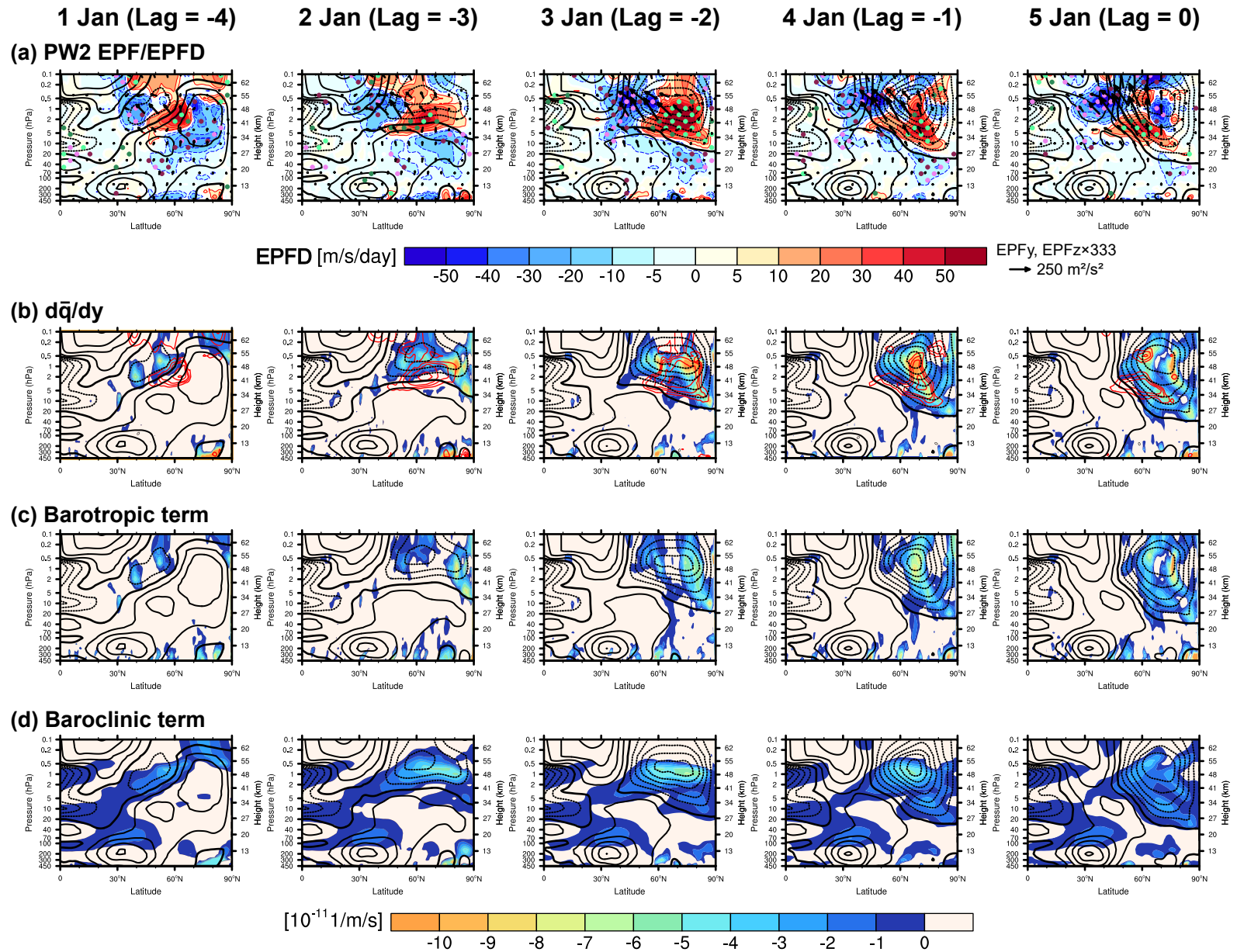
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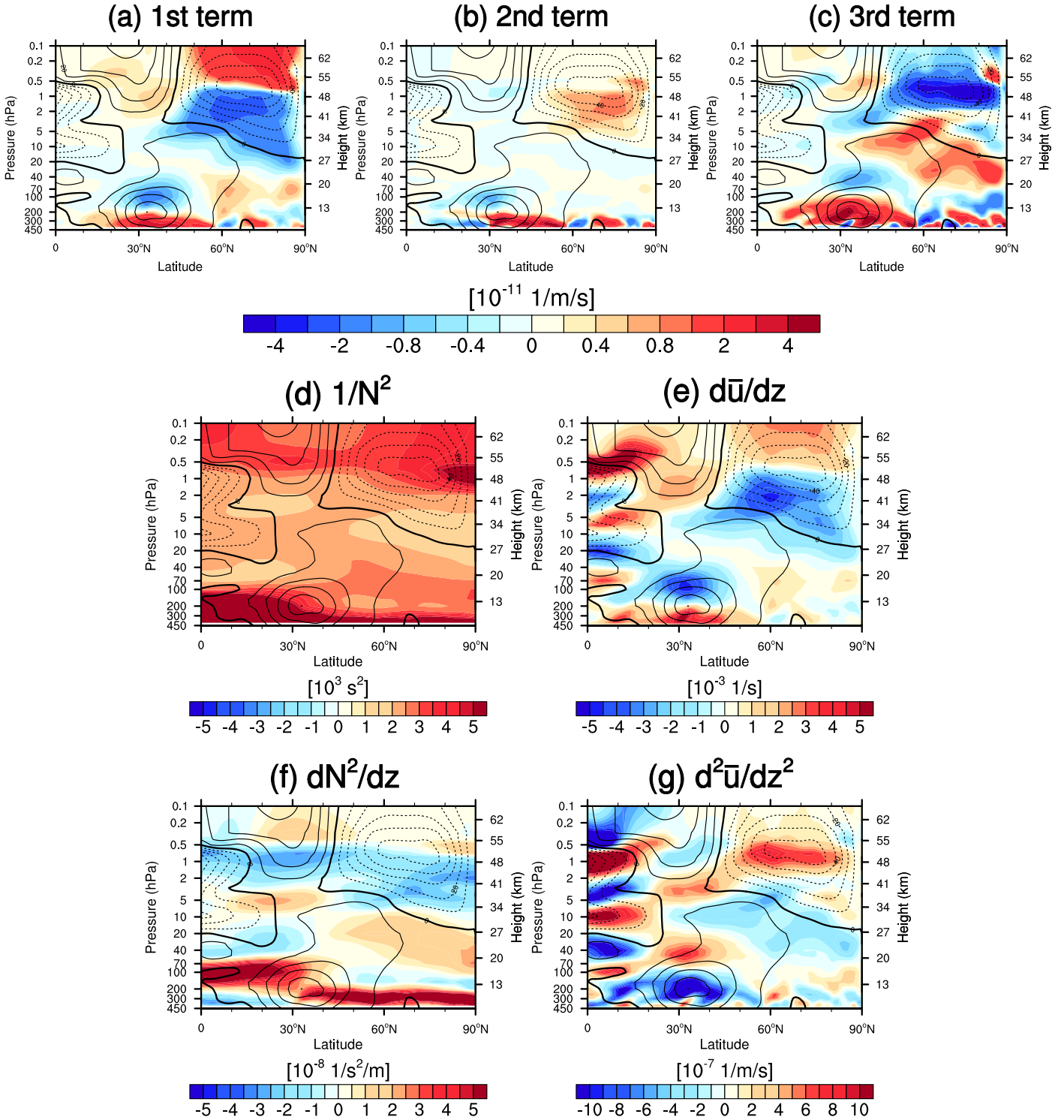
Figure 2: (a) Time-height cross sections of the vertical component of Eliassen-Palm fluxes (EPFz) of PW2 (upper) and time-series of eddy heat flux ($\overline{v'T'}$) of PW1 (dashed) and PW2 (solid) at 100 hPa (lower) averaged over 45–75°N. The overlaid blue (red) thick line denotes $\overline{v'T'}$ of PW1 (PW2) having a magnitude 1 STD greater than its climatology. The three identical arrows indicate the group velocity vectors of the vertically propagating Rossby waves of ZWN2 with a slope of 5.5km/day. (b) Time-zonal phase speed cross sections of the PW2 GHP amplitude at 1, 3, and 100 hPa averaged over 45–75°N. The purple and black vertical lines in (a) and (b), respectively, represent the onset date.



436

437 **Figure 3:** Latitude-height cross sections of (a) Eliassen-Palm fluxes (EP-fluxes, vectors) overlaid on their divergences (EPFD, colors) of PW2, (b) the meridional gradient of
 438 the quasi-geostrophic potential vorticity (\bar{q}_y , colors) overlaid by the positive EPFD of PW2 (red contour), (c) barotropic, and (d) baroclinic terms of Equation (3) in 1–5 January.
 439 The black contours present the zonal-mean zonal winds. The solid, dashed, and thick solid lines indicate positive, negative, and zero wind, respectively.

3 January (Lag = -2)



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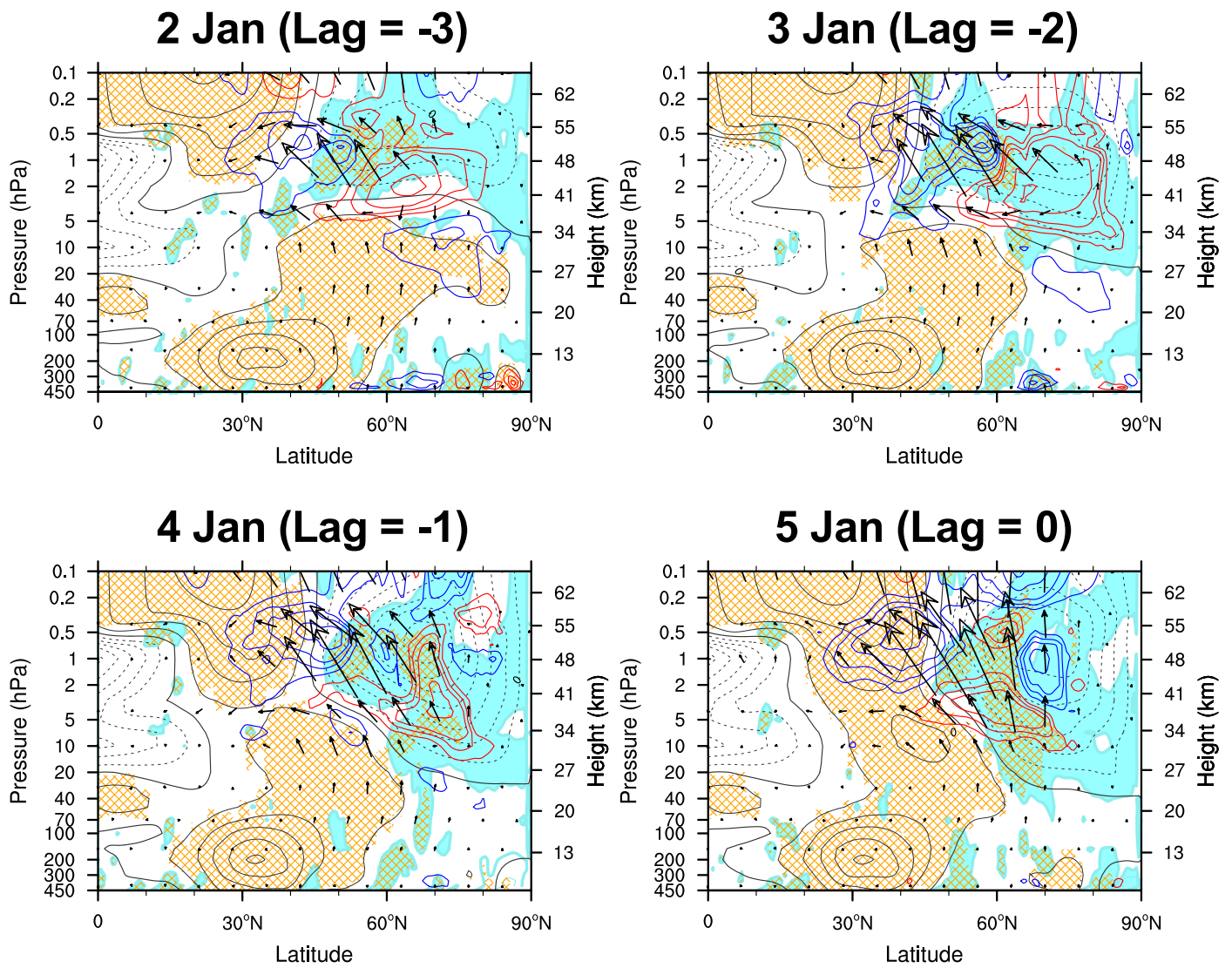
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Figure 4: Latitude-height cross sections of (a–c) the three terms on the right-hand side of Equation (8) divided by f^2 , (d) the inverse of the squared Brunt–Väisälä frequency $\frac{1}{N^2}$, (e) the vertical gradient of the zonal-mean zonal wind \bar{u}_z , (f) the vertical gradient of the squared Brunt–Väisälä frequency N^2_z , and (g) the vertical curvature of the zonal-mean zonal wind \bar{u}_{zz} on 3 January 2021. The black contours present the zonal-mean zonal winds. The solid, dashed, and thick solid lines denote positive, negative, and zero wind, respectively.

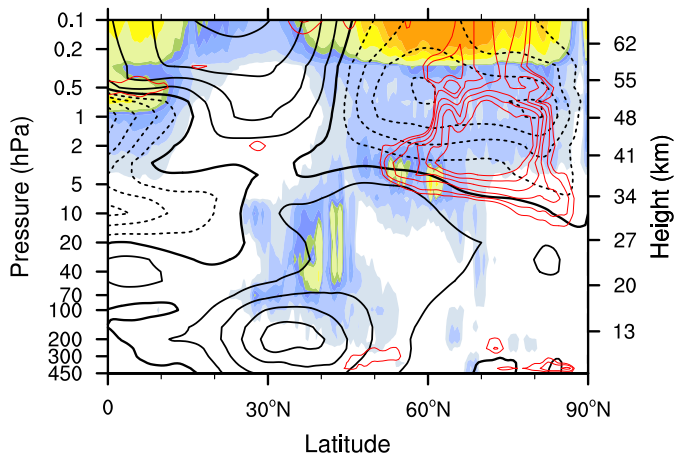


446

447 **Figure 5:** Latitude-height cross sections of the negative \bar{q}_y (mint shading) and positive refractive index squared (n^2 ,
 448 orange hatching) overlaid by PW2 EP-fluxes (vectors) and EPFD (contours, where the red and blue contours denote the
 449 positive and negative values, respectively) in 2–5 January 2021. The black contours present the zonal-mean zonal winds.
 450 The solid, dashed, and thick solid lines denote positive, negative, and zero wind, respectively.

3 January (Lag = -2)

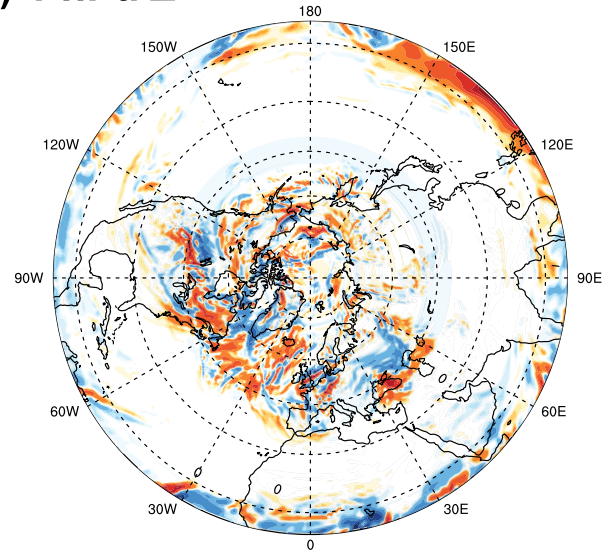
(a) Zonal-mean $|Z'|$



$[10^{-6} \text{ 1/s/day}]$



(b) 1 hPa Z'



$[10^{-6} \text{ 1/s/day}]$

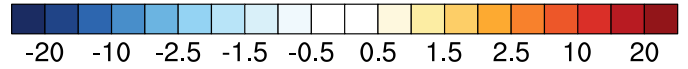
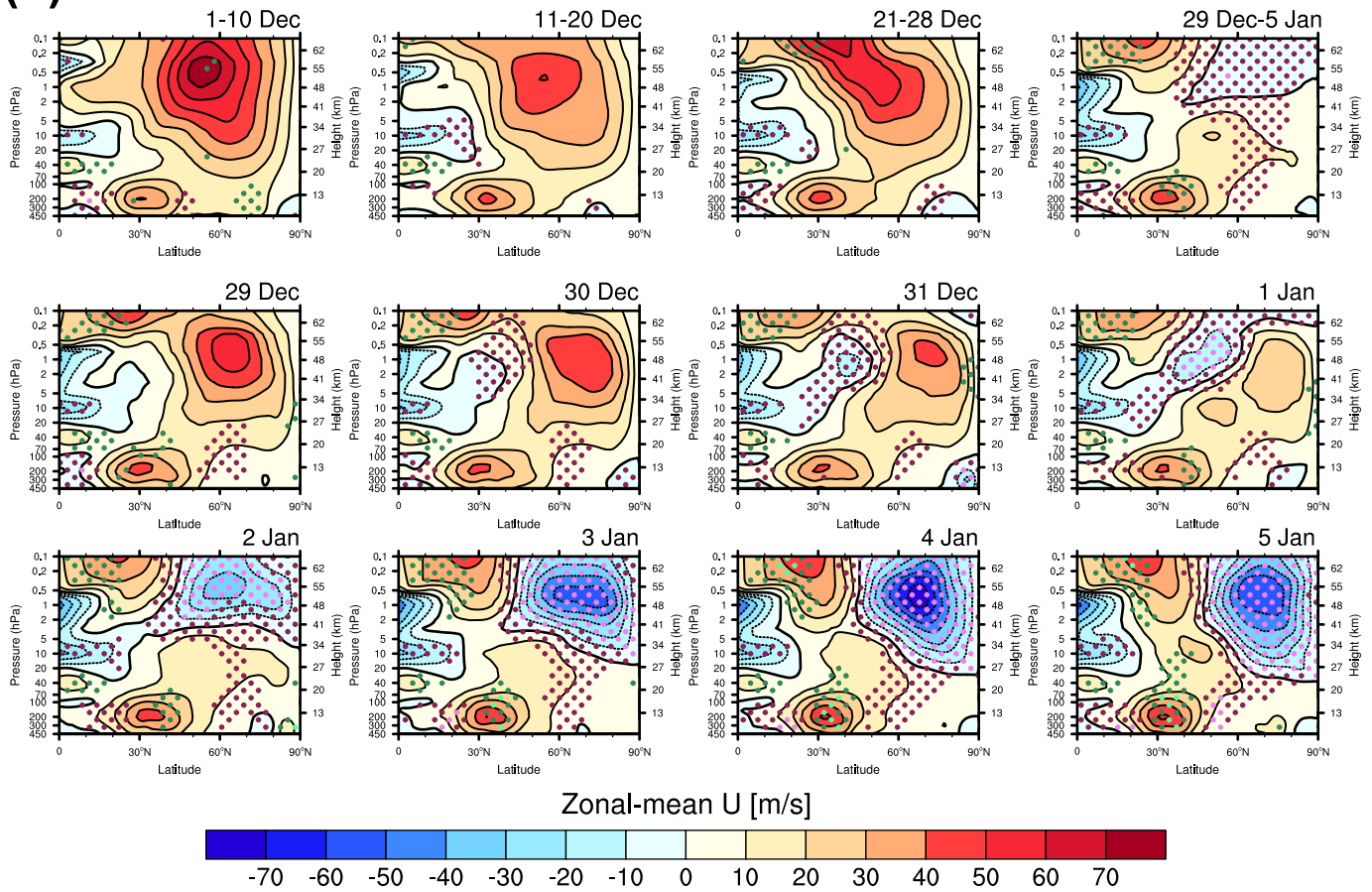
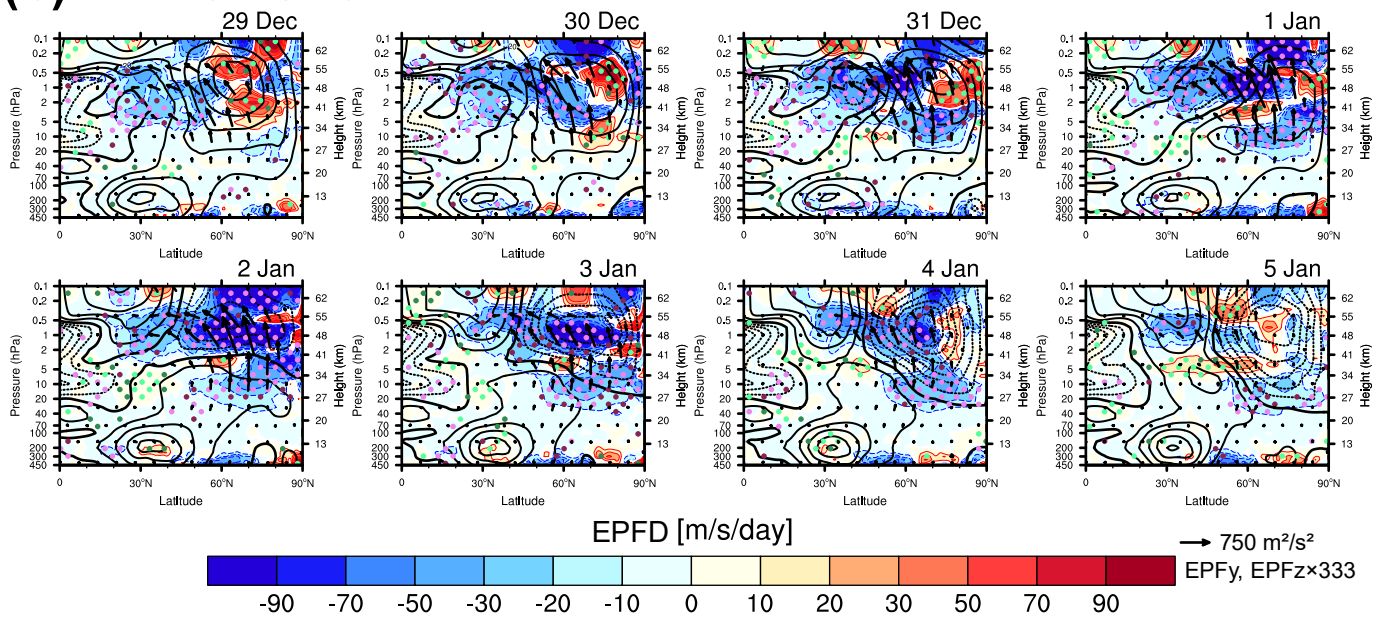


Figure 6: (a) Latitude-height cross section of the zonal-mean magnitude of the non-conservative forcing (Z' , shading) overlaid by the positive EPFD of PW2 (red contour) on 3 January 2021. The black contours present the zonal-mean zonal winds where the solid, dashed, and thick solid lines denote positive, negative, and zero wind, respectively. (b) Polar stereography of Z' at 1 hPa altitude on 3 January 2021.

(a) Zonal-mean U



(b) EP-flux and EPFD



456

457 **Figure 7:** Latitude-height cross sections of (a) the zonal-mean zonal winds averaged over 1–10, 11–20, 21–28 December
 458 2020, and 29 December 2020–5 January 2021 (first row), daily from 29 December 2020 to 5 January 2021 (second to
 459 third row), and (b) EP-fluxes (vectors) overlaid on EPFD (colors) of the resolved waves. The black contours in (b) are
 460 the zonal-mean zonal winds. The contour specifications are the same as in Figure 3.

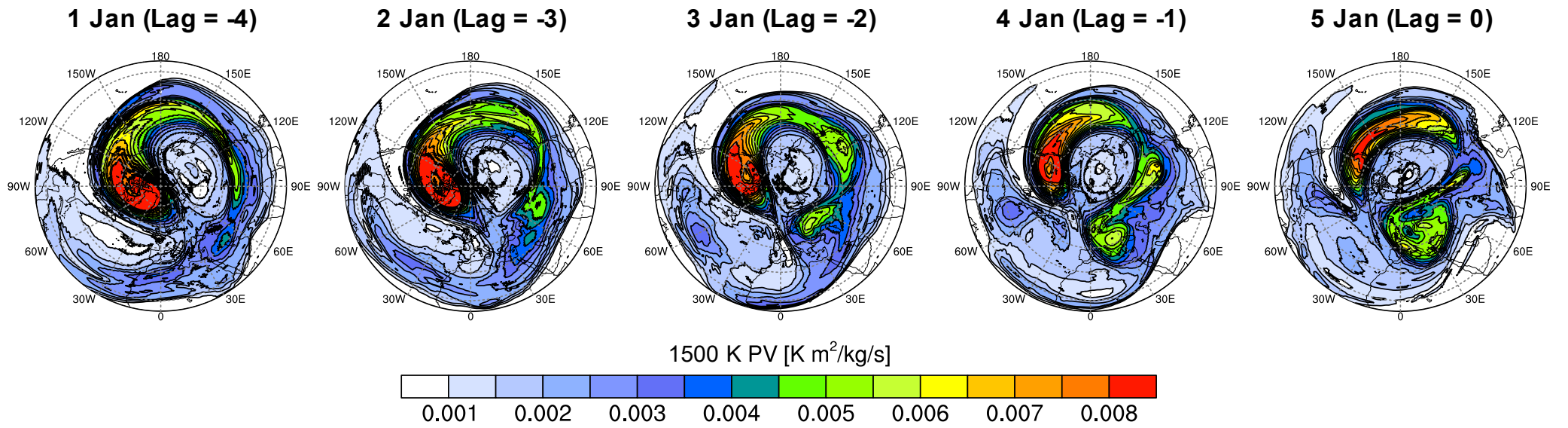


Figure 8: Time series of Ertel's potential vorticity at the 1500 K isentropic surface (~2 hPa).