



1 **Understanding hydrologic controls of slope response to**  
2 **precipitations through Machine Learning analysis**  
3 **applied to synthetic data**

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10 **Abstract:**

11 The assessment of the response of slopes to precipitation is important for various  
12 applications, from water supply management to hazard assessment due to  
13 extreme rainfall events. It is well known that the underground conditions prior to  
14 the initiation of rainfall events control the hydrological processes that occur in  
15 slopes, affecting the water exchange through their boundaries. The present study  
16 aims at identifying suitable variables to be monitored and modelled to predict the  
17 response of the slope to precipitations. A case study consisting of a loose  
18 pyroclastic coarse grained soil cover overlaying a karstic bedrock located in the  
19 southern Apennines (Italy) is described, where field monitoring has been carried  
20 out, comprising stream level recordings, meteorological recordings, and soil  
21 water content among others. Nevertheless, to enhance the field dataset, the slope  
22 hydraulic behaviour of the case study has been simulated with a physically based  
23 model linked to a synthetic rainfall time series, getting a consistent hourly  
24 timeseries dataset of 1000 years, containing information on rainfall, aquifer water  
25 level and soil volumetric water content at different depths. Machine Learning  
26 techniques have been used to unwrap the relationships amongst the studied  
27 variables, which relations are commonly non-linear. The Random Forest



28 technique has been used to assess the way the slope response could be addressed  
29 and the importance of each variable on the slope response and the k-means  
30 clustering technique has been used to explore the geometrical disposition of data,  
31 and so the identification of seasonally recurrent different scenarios linked to the  
32 slope response. It has been shown that the slope response in terms of the rainwater  
33 being stored in the soil cover is naturally highly dependent on the rainfall amount,  
34 but water drainage and storage processes can be identified by normalizing the  
35 change in water storage with the rainfall depth. Indeed, with the methodology  
36 presented here, different hydrometeorological scenarios controlling major  
37 hydrological processes have been identified not only from the meteorological and  
38 seasonal behaviour but also from the underground conditions prior to the rainfall  
39 initiation, weighting the role, on one hand, of the field capacity value on the ease  
40 of the water to flow in and out of the soil cover and, on the other hand, of the  
41 ground water level, the increase of which gives evidence of the activation of slope  
42 drainage even during relatively intense rainfall events.

43 **Keywords:** Water storage, slope response, underground antecedent conditions,  
44 hydrological controls

## 45 **1. Introduction**

46 Slope response to precipitations is highly non-linear, in terms of runoff  
47 generation, rainwater infiltration and subsurface drainage processes, which are  
48 mostly depending on the initial soil moisture state at the onset of the rainfall event  
49 (Tromp-Van Meerveld and McDonnell, 2006; Nieber and Sidle, 2010; Damiano  
50 et al., 2017). The initial or antecedent conditions are related to hydrological  
51 processes that occur in the slope, which control water exchanges between the  
52 slope and surrounding systems (i.e., atmosphere, surface water, deep  
53 groundwater). These processes occur through the boundaries of the slope, and  
54 often evolve over long timescales.



55 While the importance of antecedent conditions on overland runoff and drainage  
56 has been early identified, and their role as predisposing conditions has already  
57 been recognized (Ponce & Hawkins, 1996; Tromp-Van Meerveld & McDonnell,  
58 2006), only recently the scientific community started providing new perspectives  
59 to better understand slope predisposing conditions to landslides (Bogaard and  
60 Greco, 2018), and so to develop physically-based models capable of integrating  
61 this hydrological knowledge for predicting their occurrence (Greco et al., 2018;  
62 Bordoni et al., 2015).

63 The storage of infiltrating water within the soil also requires drainage  
64 mechanisms developing in the slopes in response to precipitations to be not so  
65 effective to drain out much rainwater (Marino et al., 2020b; Greco et al., 2021).  
66 Consequently, especially for nowcasting and early warning purposes, the  
67 identification of hydrological variables suitable to identify slope predisposing  
68 conditions is extremely useful. Thus, to better understand how the complex  
69 hydrological predisposing conditions may control the processes involving the  
70 slope response in terms of water storage, a field monitoring campaign allowing  
71 the assessment of the slope water balance is highly recommended (Marino et al.,  
72 2020a).

73 The identification of suitable variables to be monitored in the field is indeed  
74 useful to achieve an insight of the behaviour of the interconnected hydrological  
75 systems (i.e., groundwater, surface water, soil water). The proper evaluation of  
76 the hydrological scenarios in a region of interest could impact from flood hazard  
77 assessment and the study of rainfall-induced landslides (Bogaard and Greco  
78 2016), to the prediction of possible crop water stress conditions in relation to  
79 defoliation (Capretti and Battisti, 2007), pathogen expansions in chestnut grove  
80 (Gao and Shain, 1995), and plant mortality in a climate change context as well  
81 (McDowell et al., 2008).



82 This research focuses on a case study in an area sensitive to problems associated  
83 to both dry and wet seasons, but where particularly destructive rainfall triggered  
84 landslides occurred. The triggering of rainfall-induced shallow landslides is  
85 controlled by the increase of water storage within the soil cover after intense and  
86 persistent precipitations, leading to pore pressure build up (Bogaard and Greco  
87 2016). Such geo-hazards are recurrent along the slopes covered with unsaturated  
88 pyroclastic deposits typical of wide areas of Campania, southern Italy (Fiorillo et  
89 al., 2001; Revellino et al., 2013). Slope equilibrium is guaranteed by the  
90 additional shear strength promoted by soil suction (Lu and Likos 2006; Greco  
91 and Gargano 2015), which reduction often leads to slope failure due to shear  
92 strength loss by soil wetting during rainwater infiltration (Olivares and Picarelli,  
93 2003; Damiano and Olivares, 2010; Pagano et al., 2010; Pirone et al., 2015).

94 Not only the rainfall characteristics and the soil saturation play a role in the  
95 hydrological slope response to precipitations. Recent studies show that the  
96 response of soil covers to precipitations is affected by the wetness of the soil-  
97 bedrock interface, which controls the leakage of water into the underlying  
98 fractured limestone (Marino et al., 2020a, b). At the contact between soil cover  
99 and bedrock, intense weathering modifies the physical properties of the soil as  
100 well as of the fractured bedrock, which seem to be hydraulically interconnected.  
101 The changing hydraulic behaviour of the soil-bedrock interface can be related to  
102 the storage of water in the uppermost part of the fractured bedrock (Greco et al.,  
103 2018, 2014). Therefore, the aquifer water level arises as another possible  
104 monitoring variable to be considered within slope controls.

105 The aim of this study is to identify the major hydrological processes controlling  
106 the slope response to precipitations, and the most suitable variables to quantify  
107 them. Therefore, a methodological approach gathering wide knowledge on field  
108 process simulations and data analysis is presented. In that way, a 1-D physically  
109 based mathematical model, that couples the interaction between the unsaturated



110 pyroclastic soil cover and the underlying perched aquifer (Greco et al., 2018),  
111 was applied to describe the behaviour of a slope located in Campania (southern  
112 Italy), under a 1000-years long hourly rainfall synthetic time series. The model  
113 had been previously calibrated and validated on data from field monitoring  
114 carried out since 2001 (Greco et al., 2013; Comegna et al., 2016; Damiano et al.,  
115 2012). The results of the simulations provide the time series of soil suction, water  
116 content and aquifer water level, assumed as representative of real field  
117 conditions. Once identified the rainfall events within the 1000-years hourly  
118 timeseries, a specific dataset is built with the antecedent conditions one hour  
119 before the beginning of any rainfall event, comprising the previously named  
120 variables plus the total rainfall amount and the change in water stored in the soil  
121 cover at the end of the rainfall events. The dataset was analysed with Machine  
122 Learning techniques, i.e., clustering, and random forest, to disentangle the  
123 nonlinear processes controlling the slope hydraulic behaviour due to rainfall  
124 events, and thus to identify the role played by the variables, suitable to be  
125 monitored in the field, on the slope response to precipitations.

126



127        **2. Materials and methods**

128        The studied slope belongs to the Partenio Massif, and it has the typical  
129        characteristics of many pyroclastic slopes of Campania (southern Italy) (Greco  
130        et al., 2018). Indeed, three major zones characterized by unsaturated pyroclastic  
131        deposits can be identified in Campania (Cascini et al., 2008): Campanian  
132        Apennine chain, composed by carbonate rock covered by a variable layer of  
133        pyroclastic soil (from 0.1 to 5 m); Phlegraean district, formed by underlying  
134        densely fractured volcanic tuff bedrock, placed under several meters of  
135        pyroclastic soils; and Sarno and Picentini Mountains, where a thin layer of  
136        pyroclastic material is over a terrigenous bedrock. In these three areas, the  
137        thickness of the soil covers results quite variable, according to the slope  
138        inclination and to the distance from the eruptive centre (De Vita et al., 2006;  
139        Tufano et al., 2021).

140        A synthetic dataset of slope hydrologic response to precipitations, based on soil  
141        cover interaction with rainfall (in the uppermost boundary) and underlying  
142        shallow aquifer (in the lowermost boundary), has been built. The synthetic  
143        dataset has been considered reliable to reproduce slope response to climate  
144        forcing in terms of soil volumetric water content, perched aquifer water level,  
145        and rainfall.

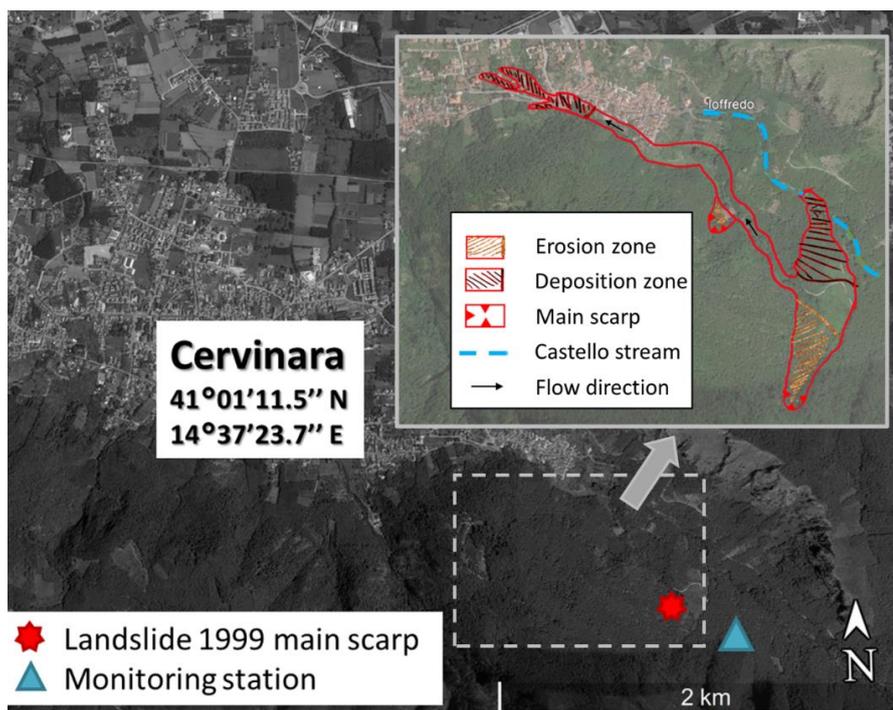
146        Moreover, the obtained data set has been analysed with Machine Learning  
147        techniques, as they result quite powerful to identify non-linear relationships  
148        between variables. Besides, the results which come from these data analyses have  
149        been compared a priori to the limited dataset from field monitoring, showing a  
150        reasonable agreement.

151        **2.1. Case study**

152        The study area refers to the north-east slope of Monte Cornito, part of the Partenio  
153        Massif (Campania, southern Italy), 2 km from the town of Cervinara, about 40



154 km northeast of the city of Naples. The slope was involved in a series of rapid  
155 shallow landslides after a rainfall event of 325 mm in 48 hours during the night  
156 between 15–16 December 1999, causing casualties and heavy damages (Fiorillo  
157 et al., 2001). A field monitoring station was installed nearby the big landslide  
158 scarp since 2001. Further details of the investigated zone, with indications of the  
159 area affected by the largest of the landslides triggered in 1999, are shown in  
160 Figure 1.



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161

162 **Figure 1. Location of the study area and indication of the zone affected by a large**  
163 **landslide in 1999<sup>1</sup>**

164 Partenio Massif is part of the southern Apennines area. The bedrock mainly  
165 consists of Mesozoic-Cenozoic fractured limestones, mantled by loose

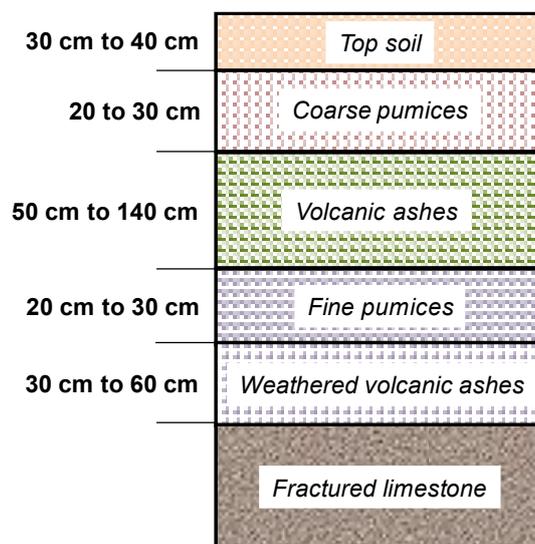
<sup>1</sup> Google (2022) *Cervinara, Italy*. Available at:  
<https://www.google.com/maps/@41.0114559,14.6411297,2097m/data=!3m1!1e3> (Accessed: 7  
March 2022)



166 pyroclastic deposits, resulting from the explosive volcanic activity of Somma-  
167 Vesuvius and Phlegrean Fields, which occurred over the last 40.000 years  
168 (Rolandi et al., 2003).

169 The fractured limestone formations of the southern Apennines often host large  
170 karst aquifers, through which a basal groundwater circulation occurs, for which  
171 regional groundwater recharge between 100 and 500 mm/year has been  
172 estimated, with 200 mm/year regarding the area of Cervinara (Allocca et al.,  
173 2014). Moreover, recent studies showed that, in the upper part of the karst system,  
174 denoted as epikarst (Hartmann et al., 2014), more permeable and porous than the  
175 underlying rock, a perched aquifer often develops (Williams, 2008; Celico et al.,  
176 2010). It temporally stores water and favors the recharge of the deep aquifer  
177 through the larger fracture system. The water, which is accumulated temporally  
178 in the epikarst, also reappears at the surface in small ephemeral streams.

179 Specifically, the slope of Cervinara has an inclination between 35° and 50°, at an  
180 elevation between 500 m and 1200 m above sea level. The soil cover, usually in  
181 unsaturated conditions, is the result of the air-fall deposition of the materials from  
182 several eruptions, so it is generally layered. It mainly consists of layers of  
183 volcanic ashes (with particle size in the range of sands to loamy sands) alternating  
184 with pumices (sandy gravels), laying upon the densely fractured limestone  
185 bedrock. Near the soil-bedrock interface, a layer of weathered ashes,  
186 characterized by finer texture (silty sand), with lower hydraulic conductivity,  
187 moderate plasticity and low cohesion, is often observed (Damiano et al., 2012).



188

189 **Figure 2. Characteristic soil profile for the slope near the scarp of the landslide**  
190 **occurred in 1999 in Cervinara**

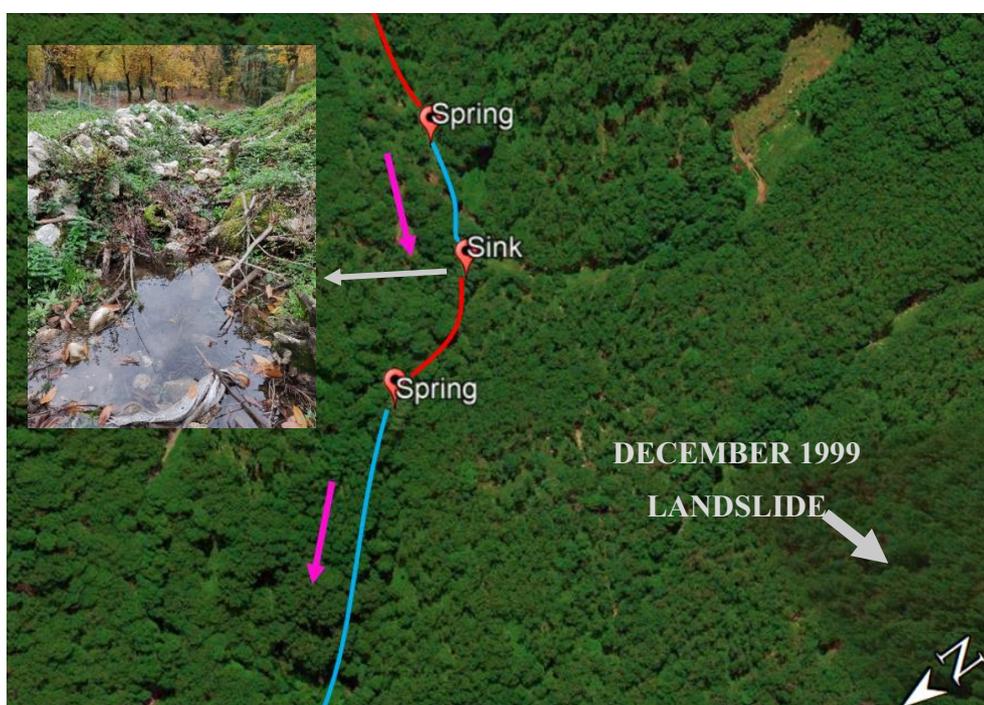
191 The soil cover thickness varies spatially from a minimum of 1.0 m, in the steepest  
192 part of the slope, to larger values at its foot (up to 4-5 meters). Figure 2 shows  
193 the soil layers constituting the cover, as found throughout the slope near the main  
194 scarp of 1999 landslide.

195 The pyroclastic ashes usually exhibit high porosity (up to 75%) and quite high  
196 values of saturated hydraulic conductivity (ranging up to  $1 \times 10^{-5}$  m/s). Thus, this  
197 kind of soil lets rainwater infiltrate during the most intense rainfall events, with  
198 little runoff generation, and it can store a large amount of water.

199 The climate is Mediterranean, which is characterized by dry and warm summer  
200 and rainy autumn and winter, with mean annual precipitation of about 1600 mm,  
201 mostly occurring between October and April. The total potential  
202 evapotranspiration  $ET_0$ , estimated with the Thornthwaite formula (Shuttleworth,  
203 1993), is between 700 mm and 800 mm in the altitude range between 750 m and  
204 400 m (Greco et al., 2018). The vegetation mainly consists of widespread  
205 deciduous chestnuts, with a dense understory of brushes and ferns, growing



206 during the flourishing period (between May and September). In fact, visual  
207 inspections of the soil profile showed a large amount of organic matter and roots.  
208 In most cases, roots are denser in the uppermost part of the soil cover and become  
209 sparse between the depth of 1.50 m and 2.00 m below the ground surface,  
210 reaching the basal limestones and penetrating the fractures.



\*Maps Data: Google, ©2022 CNES/Airbus, Maxar Technologies

— Interval with water    — Interval without water    → Water flow direction

211

212 **Figure 3. Identification of surface water flow in the Castello stream at the beginning**  
213 **of the rainy season in November 2021 by visual recognition of springs and sinks in**  
214 **the watercourse<sup>2</sup>**

215 Moreover, in the surrounding area, several ephemeral and perennial springs are  
216 present, mostly located at the foot of the slopes, which supply a network of small  
217 creeks and streams, allowing to show the activity of the aquifer discharge to the

<sup>2</sup> Google (2022) *Cervinara, Italy*. Available at:  
<https://www.google.com/maps/@41.0088511,14.65137,786m/data=!3m1!1e3> (Accessed: 7  
March 2022)



218 surface water. An indication regarding the Castello stream (the main stream for  
219 this side of the basin), with springs, is shown in Figure 3, where, during a field  
220 recognition in November the 11<sup>th</sup> 2021, the surface water flow appeared (springs)  
221 and disappeared (sinks) in some points along the stream course. Normally the  
222 stream exhibits its lowest water depth values up to the beginning of the late  
223 autumn (Marino et al., 2020a, p.3.3), but it is interesting to note that the surface  
224 water in the stream emerging from the epikarstic springs is feasible to be  
225 monitored as an indicator of the slope drainage status.

#### 226 **2.1.1. Field monitoring data**

227 Several hydrological monitoring activities have been carried out at the slope of  
228 Cervinara since 2001, initially consisting of measurements of precipitations and  
229 manual readings (every two weeks) of soil suction by “Jet-fill” tensiometers,  
230 equipped with a Bourdon manometer (Damiano et al., 2012). Afterwards, since  
231 November 2009, an automatic monitoring station has been set at an elevation of  
232 585 m a.s.l., near a narrow track close to the landslide scarp of December 1999.  
233 The installed instrumentation consisted of tensiometers, time domain  
234 reflectometry (TDR) probes for water content measurements, and a rain gauge  
235 (Greco et al., 2013; Comegna et al., 2016).

236 Since 2017, the hydro-meteorological monitoring was enriched (Marino et al.,  
237 2020a), aiming at understanding the seasonal behaviour of the slope and the  
238 interactions between the hydrological systems, i.e., the unsaturated soil cover, the  
239 epikarst, and the underlying fractured bedrock.

240 Specifically, the data collected by tensiometers and TDR probes were  
241 supplemented with those from a meteorological station (composed by a thermo-  
242 hygrometer, a pyranometer, an anemometer, a thermocouple for soil temperature  
243 measurement, and a rain gauge), and with the water level in two streams at slope



244 foot, so to gain useful information for the assessment of the water balance of the  
245 studied slope.

246 The data collected during these field monitoring activities have been useful to  
247 highlight seasonally recurrent soil moisture distributions. More details about the  
248 recurrent seasonal behaviour related to the moisture conditions of the soil profile  
249 of the area of Cervinara can be found in Marino et al. 2020a.

## 250 **2.2. Synthetic dataset**

251 Aiming at identifying suitable variables to be monitored in the field for the  
252 identification of the conditions controlling different slope responses to the  
253 precipitations, a rich dataset of rainfall and underground monitored variables,  
254 such as soil moisture and groundwater level, is needed. However, a complete  
255 field monitored dataset is not always possible to be analyzed and, when it exists,  
256 it is commonly available for short periods, granting a relatively low measurement  
257 density. Hence, a synthetic dataset, aiming at improving the information obtained  
258 from field monitoring, has been generated. This dataset has been obtained by  
259 means of the physically based mathematical model described hereinafter (section  
260 2.2.2). The model has been run with a 1000-years synthetic hourly rainfall series,  
261 obtained with a stochastic rainfall generator, for which further details are given  
262 in section 2.2.1.

### 263 **2.2.1. Definition of synthetic rainfall events**

264 The Neyman-Scott rectangular pulse model (NSRP) has been used to obtain a  
265 1000-years long synthetic hourly series of precipitations. The NSRP model  
266 reproduces the precipitation process as a set of rain clusters, composed by  
267 possibly overlapping rain cells embodied by rectangular pulses, each one with  
268 random origin. The storm duration is represented by the cell width and its height  
269 represents the associated rainfall intensity, so that when multiple cells overlap,

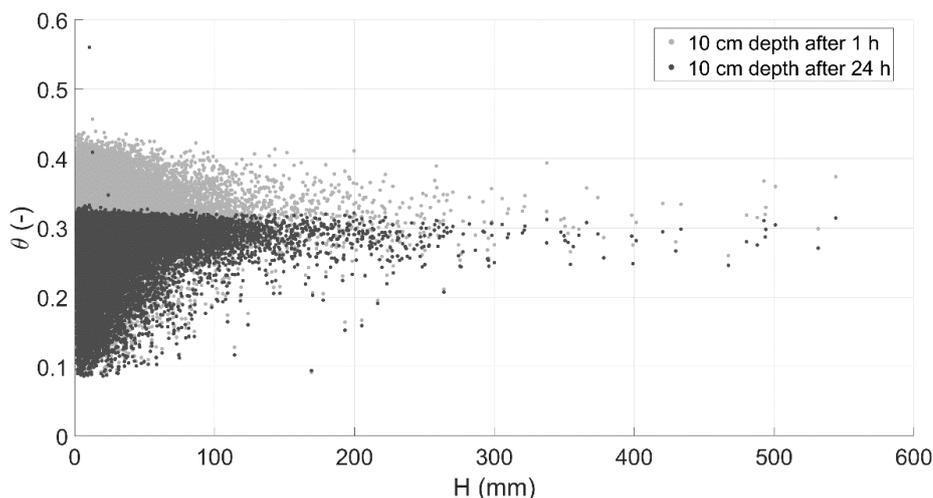


270 the total intensity is the sum of the intensities of the overlapping cells (Rodriguez-  
271 Iturbe et al. 1987; Cowpertwait et al. 1996).

272 NSRP model calibration requires the identification of five parameters, using the  
273 method of moments (Peres and Cancelliere, 2014), based on available rainfall  
274 data for the investigated site. Specifically, the data from the rain gauge station of  
275 Cervinara, situated near the Loffredo village, belonging to the Civil Protection  
276 Agency of Campania Region available from January 2001 to December 2017  
277 with a time resolution of 10 min, were used.

278 The aim of this study is the identification of variables expressing the slope  
279 conditions responsible of different responses to precipitations. In that sense, it is  
280 important to define the events within the rainfall time series to clearly distinguish  
281 antecedent conditions from the effects of the current rainfall event.

282 In other words, within the 1000-years long time series, a criterion should be  
283 identified to separate rainfall events, so that a new event begins only when the  
284 effects of the previous one disappeared. For this study, the events were defined  
285 as periods with at least 2mm of rainfall, preceded and followed by at least 24h  
286 with less than 2mm (i.e., smaller than the mean daily potential evapotranspiration  
287 estimated for the case study).



288

289 **Figure 4. Scatter plot of event rainfall depth and mean volumetric water content of**  
290 **the top 10 cm soil depth 1 hour (grey dots) and 24 hours (black dots) after the end**  
291 **of each rainfall event**

292 In fact, the mean volumetric water content ( $\theta$ ) at 10 cm depth drops below soil  
293 field capacity ( $\theta \cong 0.35$ ) 24 hours after the end of each event (Figure 4) in all  
294 the cases in which such value was overcome at the end of the event. This shows  
295 that a dry interval of 24 hours after a rainfall event is long enough for drainage  
296 processes to remove from the topsoil most of the water infiltrated from the  
297 previous event. As topsoil moisture controls the infiltration capacity at ground  
298 surface, after such interval the infiltration of new rainfall is only little affected by  
299 the remnants of the previous rainfall event.

300 With the assumed separation criterion, a total of 53061 rainfall events within  
301 1000 years are obtained, with durations ranging between 1 and 570 hours, and  
302 total rainfall depth between 2 and 710 mm.

### 303 2.2.2. Slope hydrological model

304 A simplified 1-D model has been built, previously validated according to the data  
305 collected during the hydrological monitoring activities (Greco et al., 2013), to  
306 investigate the hydrological response of the slope to synthetic hourly  
307 precipitation data. The unsaturated flow through the soil cover is modelled with



308 1-D head-based Richards' equation (Richards, 1931), assuming for simplicity a  
309 single homogeneous soil layer, and it is coupled with a model of the saturated  
310 water accumulated in the perched aquifer. The adoption of a 1-D model is  
311 allowed thanks to the geometry of the considered soil cover, as well as to the  
312 prevailing water potential gradients orthogonal to the ground surface in  
313 unsaturated conditions.

314 The root water uptake has been accounted in the source term of the model,  
315 according to the expressions by Feddes et al. (1976), based on estimated potential  
316 evapotranspiration, with maximum root penetration depth equal to the soil cover  
317 thickness and triangular root density shape.

318 Two boundary conditions are considered for the unsaturated soil cover. At  
319 ground surface (i.e., the upper boundary condition), if the rainfall intensity is  
320 greater than the current infiltration capacity, the excess rainfall forms overland  
321 runoff. Otherwise, all rainfall intensity is set as infiltration. The bottom boundary  
322 condition links the soil cover to a perched aquifer developing in the fractures and  
323 hydraulically connected to the unsaturated cover through the weathered soil layer  
324 (less conductive and capable of retaining much water), located at the contact  
325 between the cover and the bedrock. This soil layer penetrates the vertical conduits  
326 and fractures (Greco et al., 2013). In this context, the perched aquifer is modelled  
327 as a linear reservoir model, that receives water from the gravitational leakage of  
328 the overlying unsaturated soil cover and releases it as deep groundwater recharge  
329 and spring discharge (Greco et al., 2018). The pressure head at the soil–bedrock  
330 interface is assumed to follow the fluctuations of the water table of the underlying  
331 aquifer.

332 The hydraulic parameters of the soil cover have been obtained from previous  
333 laboratory tests (Damiano and Olivares, 2010) and field monitoring data analysis  
334 (Greco et al., 2013), considering the van Genuchten-Mualem model for the



335 hydraulic characteristic curves (van Genuchten, 1980). The parameters  
336 describing the hydraulic behaviour of the perched aquifer hosted in the upper part  
337 of the limestone bedrock have been derived from previous studies, which showed  
338 that the model satisfactorily reproduced the fluctuations of water potential and  
339 moisture, observed at various depths in the unsaturated soil cover, both during  
340 rainy and dry seasons (Greco et al., 2013; 2018). Model parameters are  
341 summarized in Table 1.

342 **Table 1. Hydraulic parameters of the coupled model of the unsaturated soil cover**  
343 **and of the aquifer hosted in the Epikarst (Greco et al. 2021).**

Soil cover	Soil cover thickness (m)	2
	Saturated water content (-)	0.75
	Residual water content (-)	0.01
	Air entry value ( $m^{-1}$ )	6
	Shape parameter (-)	1.3
	Saturated hydraulic conductivity (m/s)	$3 \times 10^{-5}$
Epikarst	Epikarst thickness (m)	14
	Effective porosity (-)	0.005
	Time constant of linear reservoir (days)	871 days

344

345 The equations have been numerically integrated with the finite difference  
346 technique, with a time step of 1 hour over a spatial grid with vertical spacing of  
347 0.02 m.

348 It is important to note that, even if the model simplifies the reality assuming a  
349 homogeneous soil profile, a more complex approach considering a layered profile  
350 would lead to difficult application of the model at less detailed scales such as  
351 regional and catchment scales. Consequently, the hydraulic properties of the  
352 homogeneous soil layer should be considered as effective properties, useful to  
353 reliably reproduce the observed phenomena.



354        **2.2.3. Synthetic hydrometeorological data**

355        As it has been stated from previous sections, the dataset comes from the  
356        simulation of the hydrologic response of a slope to 1000-years long hourly  
357        rainfall time series, carried out with a physically based model, calibrated for the  
358        case study. The output contains the time series of soil water content and suction  
359        at all depths throughout the soil cover, of the water exchanged between the soil  
360        and the atmosphere, of the leakage through the soil-bedrock interface, and of the  
361        predicted water level of the underlying aquifer.

362        One hour before the onset of each rainfall event, the following variables have  
363        been extracted, as they would be measurable in the field and are representative  
364        of antecedent conditions: the aquifer water level ( $h_a$ ), the mean volumetric water  
365        content in the uppermost 6 cm of soil cover ( $\theta_6$ ) and the mean volumetric water  
366        content in the uppermost 100 cm of soil cover ( $\theta_{100}$ ). To quantify the effects of  
367        rainfall on the slope response, the change of the water stored in the soil cover at  
368        the end of each rainfall event ( $\Delta S$ ) has been computed and compared with the  
369        total rainfall depth of the event ( $H$ ).

370        Specifically, the inclusion of soil water content information has been chosen, as  
371        it can be obtained from available satellite-derived remote sensing products (Pan  
372        et al., 2020; Paulik et al., 2014) or from field sensor networks (Wicki et al., 2020).  
373        Besides, as the model introduces a linear relationship to estimate the outflow  
374        from the groundwater system, the monitored stream water level has been  
375        considered comparable to the simulated groundwater level, as the two variables  
376        are assumed directly proportional in the model.

377        **2.3. Data analysis techniques**

378        The resulting dataset has been analyzed with Machine Learning techniques,  
379        aiming at capturing the complex interactions between the hydrological  
380        subsystems (i.e., soil cover, fractured bedrock, surface water). Indeed, the



381 analysis of the data is not only constrained to classical statistical analyses, such  
382 as data frequency distributions, but also to data classification based on their  
383 geometrical distribution, and on quantifying the importance of the considered  
384 antecedent variables on the simulated response as well.

### 385 **2.3.1. Variable importance assessment by Random Forest**

386 The Random Forest is a Machine Learning method that sets its basis on the theory  
387 of regression/classification trees, bagging data and capturing even the complex  
388 or non-linear interactions in-between the data of a set with relatively low bias  
389 (Breiman, 2001). This method is often used to forecast a desired variable based  
390 on predictor variables in terms of regression or classification set of randomly  
391 constructed trees. In this case, a regression based Random Forest technique is  
392 applied to predict the slope response ( $\Delta S$ ) at the end of each rainfall event, using  
393 as predictors all possible triplets of variables described in the section 2.2.3 (total  
394 rainfall depth, aquifer water level, mean volumetric water content in the  
395 uppermost 6 cm and mean volumetric water content in the uppermost 100 cm):  
396 A total of 100 trees with a maximum leaf split of 20 nodes have been built for all  
397 variable combinations and trained with the 80% of the dataset randomly selected  
398 to obtain different regressor models. Then, the best triplet of predictor variables  
399 is selected according to the lowest value of the Root Mean Squared Error (RMSE)  
400 calculated using the test data set consisting of the 20% of the remaining data.

401 Furthermore, to understand how a single variable affects the regression model,  
402 the predictor importance is measured by the sensitivity of Random Forest model  
403 to the predicted variable (i.e., soil cover response), which is proportional to the  
404 RMSE, by permuting on purpose the variables between the levels of the model  
405 and estimating the change in the RMSE. Hence the most important variable is the  
406 one that exhibits the greatest change in RMSE after the permutations. Hence, the  
407 importance of predictor variables follows the magnitude of the change in RMSE.



408 This feature is usually referred to in relative terms to the most important variable,  
409 called variable relative importance (Hastie et al., 2008).

### 410 **2.3.2. Data classification by clustering analysis**

411 The exploratory analysis of spatial large datasets is often performed by means of  
412 clustering techniques, aiming at identifying different classes in the data,  
413 accounting on the distribution of the variables under study. There are two types  
414 of clustering algorithms used for class identification purposes: algorithms based  
415 on the density of points and algorithms based on the distance between points. The  
416 algorithm used here is named k-means, and it is a distance-based procedure to  
417 cluster data, based on the number of desired clusters and their centroids. The  
418 algorithm proceeds to iteratively minimize the variance of the Euclidean distance  
419 of cluster elements from their centroids, by accordingly moving these latter.  
420 Consequently, the data labelling is done based on their geometrical disposition in  
421 the studied plane or space, depending on the target number of clusters to be  
422 identified (Lloyd, 1982; Arthur and Vassilvitskii, 2007). When variables with  
423 very different magnitudes are being related for clustering purposes, it is  
424 convenient to normalize the data keeping the relative distances between  
425 observations. Therefore, the clustering here is applied to the standardized data to  
426 exploit the variance of each variable and keeping the geometrical disposition  
427 between observations stable.

428 As the k-means algorithm does not automatically estimate the optimal number of  
429 clusters to be identified within the dataset, the Silhouette metric has been used  
430 here to evaluate the preferred number of clusters (Rousseeuw, 1987; de Amorim  
431 and Hennig, 2015). In fact, this metric quantifies the quality of cluster  
432 identification by scoring the difference between the overall average intra-cluster  
433 distances and the average inter-cluster distances related to the maximum between  
434 the latter two. In that way the metric would always be a value ranging from -1  
435 and 1, where typically 1 means that clearly distinguished clusters have been



436 identified, 0 means that the identified clusters are indifferent, and -1 means that  
 437 data are mixed in the identified clusters.

### 438 3. Results and discussion

439 The analysis is developed on both field monitored and synthetic datasets, to  
 440 quantify the information provided by the defined antecedent variables useful to  
 441 predict the seasonal changes of the slope response to precipitations.

#### 442 3.1. Role of measurable variables on the slope response

443 To select the most appropriate triplets of predictor variables, four Random Forest  
 444 models for predicting the change in water storage ( $\Delta S$ ) in the soil cover,  
 445 associated to rainfall events, are trained on the dataset consisting of all possible  
 446 combinations of the synthetic variables:  $\langle H, \theta_6, h_a \rangle$ ,  $\langle H, \theta_{100}, h_a \rangle$ ,  $\langle H, \theta_6, \theta_{100} \rangle$   
 447 and  $\langle \theta_6, \theta_{100}, h_a \rangle$ . For each Random Forest model, the values of the Root Mean  
 448 Square Error (RMSE) are calculated, and the importance of each predictor  
 449 variable is evaluated according to the procedure described in Section 2.3.1. The  
 450 obtained results are reported in Table 2.

451 **Table 2. RMSE and variable importance for  $H$ ,  $\theta_6$ ,  $\theta_{100}$  and  $h_a$  in the prediction**  
 452 **of soil response described as  $\Delta S$**

Dataset	RMSE	Importance			
		H	$\theta_6$	$\theta_{100}$	$h_a$
$\langle H, \theta_6, h_a \rangle$	5.353	0.963	0.024	-	0.012
$\langle H, \theta_{100}, h_a \rangle$	4.336	0.964	-	0.024	0.010
$\langle H, \theta_6, \theta_{100} \rangle$	4.706	0.962	0.014	0.022	-
$\langle \theta_6, \theta_{100}, h_a \rangle$	24.665	-	0.313	0.340	0.345

453

454 As it could be seen from Table 2, an expected behavior on the slope response,  
 455 quantified as  $\Delta S$ , answers back highly depending on the rainfall amount as the  
 456 most important variable in the triplet, while the antecedent conditions show an



457 almost negligible importance with less than 3%. Additionally, the absence of total  
 458 rainfall among the predictors leads to a substantial increase in the RMSE  
 459 (24.665). This result is physically expected; the more it rains the more the water  
 460 storage in the slope increases. Nevertheless, such strong relationship between  $H$   
 461 and  $\Delta S$  could conceal important hydrological processes going on the slope. For  
 462 this reason, normalization schemes could be introduced to account different  
 463 processes in the slope response. In this case the ratio  $\Delta S/H$  is used as a measure  
 464 of the association between the amount of rain and how much it was stored in the  
 465 soil cover, pursuing to detach the water drainage processes from the water  
 466 accumulation processes. To this end, additional Random Forest models are  
 467 trained on the same four datasets for predicting the normalized water storage in  
 468 slope  $\Delta S/H$ .

469

470 **Table 3. RMSE and variable importance for  $H$ ,  $\theta_6$ ,  $\theta_{100}$  and  $h_a$  in the prediction**  
 471 **of soil response described as  $\Delta S/H$**

Dataset	RMSE	Importance			
		$H$	$\theta_6$	$\theta_{100}$	$h_a$
$\langle H, \theta_6, h_a \rangle$	0.213	0.352	0.329	-	0.319
$\langle H, \theta_{100}, h_a \rangle$	0.197	0.293	-	0.405	0.302
$\langle H, \theta_6, \theta_{100} \rangle$	0.203	0.340	0.261	0.399	-
$\langle \theta_6, \theta_{100}, h_a \rangle$	0.210	-	0.292	0.414	0.293

472

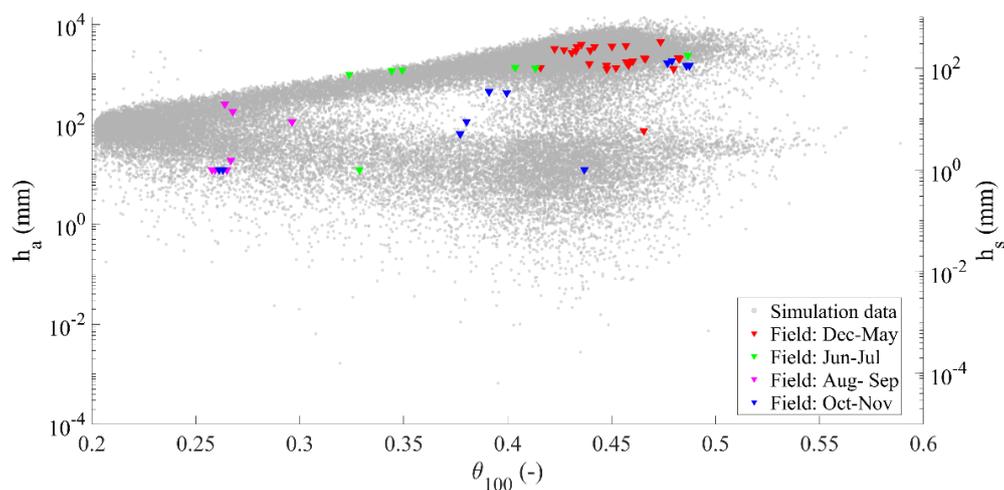
473 Normalizing the slope response as  $\Delta S/H$  (Table 3) highlights the important role  
 474 played by the other variables. It is worth to note the importance of the ground  
 475 water level, which can be compared with the importance of the two water  
 476 contents and the total rainfall depth. The importance of  $h_a$  on the slope response  
 477 suggests the presence of conditions of change in soil storage less connected to



478 rainfall values and more linked to the capability of water exchange between the  
479 aquifer and the soil cover, as it will be discussed in the following sections.  
480 Moreover, in Table 3 the variables with the lowest RMSE values are total rainfall  
481 depth, aquifer water level and mean volumetric water content in the uppermost  
482 100 cm. According to the Random Forest model, they are the most informative  
483 for predicting the slope response. Therefore, the triplet  $\langle H, \theta_{100}, h_a \rangle$  is used for  
484 further analysis.

### 485 **3.2. Underground antecedent conditions**

486 The field monitoring activities allow to get a complete dataset that traces the  
487 rainfall values coupled with the soil mean volumetric water content in the  
488 uppermost meter of the soil profile ( $\theta_{100}$ ) and the water depth of the Castello  
489 stream ( $h_s$ ), both measured hourly for three years. The field monitored data,  
490 composed by 57 rainfall events, include the water level of the Castello stream  
491 rather than the direct measurement of the aquifer water level ( $h_a$ ). Nevertheless,  
492 a direct relationship links the water level in the aquifer and the water level in the  
493 stream, as assumed for the mathematical modelling. This dataset has been  
494 enriched synthetically, as it has been described in section 2.2.

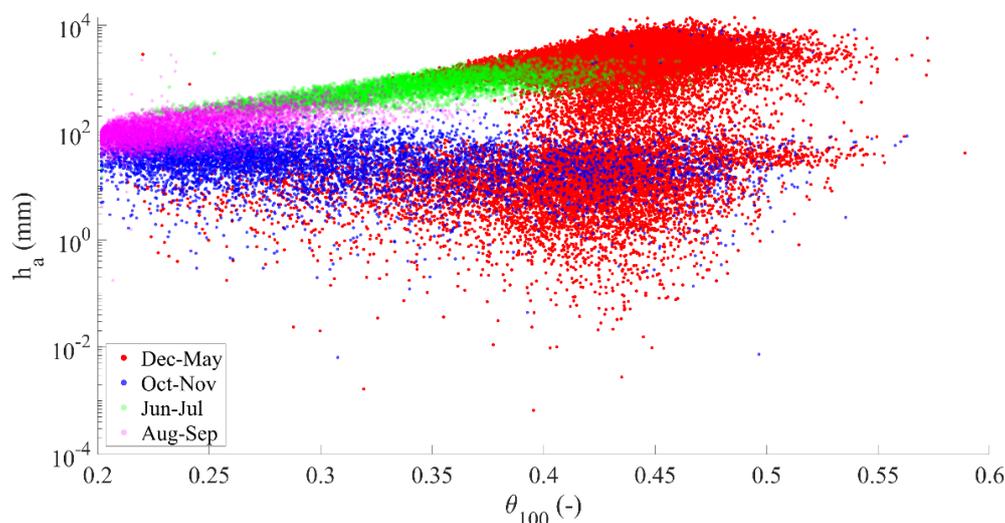


495

496 **Figure 5. Field monitored mean volumetric water content in the upper meter of the**  
 497 **soil profile ( $\theta_{100}$ ) and water depth in the Castello stream ( $h_s$ ) compared with**  
 498 **simulated data (the vertical axis is plotted in logarithmic scale to help visualizing of**  
 499 **small water levels).**

500 Therefore, to analyze the effects of the underground conditions on the slope  
 501 response, Figure 5 shows the simulated data (circular dots in the background) and  
 502 the field monitored data (triangular colored dots). Logarithmic axes are used to  
 503 distinguish the very low aquifer water level from the high values.

504 Four major seasonally recurrent conditions could be identified for the water in  
 505 the subsurface system from field monitored data: first, a condition usually  
 506 occurring between December and May is characterized by the highest water  
 507 content in the soil and the highest measured water level in the stream. Second,  
 508 the period from June to July is characterized by intermediate water content  
 509 values, with still high level in the stream. Third, the period from August to  
 510 September is characterized by the lowest values of water content in the soil, but  
 511 also the lowest water depth  $h_s$  measured in the stream (few centimeters, in some  
 512 cases nearly zero). Finally, the period from October to November is characterized  
 513 by a wide range of values in soil water content and a relatively low range of  
 514 stream water depth.



515

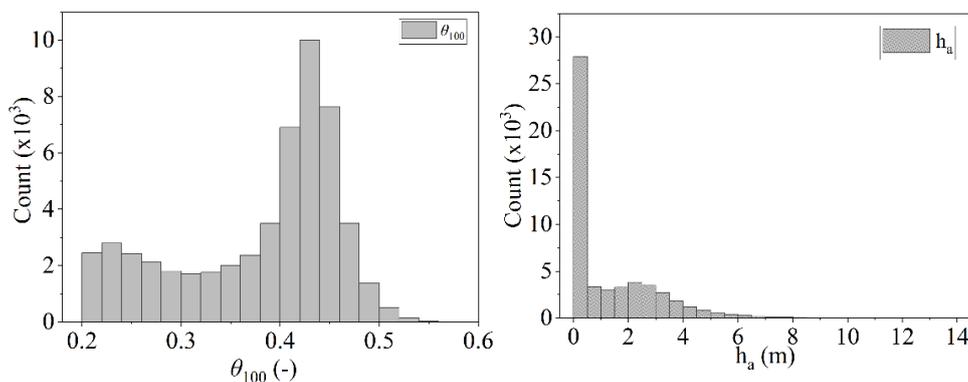
516 **Figure 6. Seasonal behavior of the aquifer water level ( $h_a$ ) and the mean**  
517 **volumetric water content of the upper meter of the soil profile ( $\theta_{100}$ ) for the**  
518 **synthetic dataset (the vertical axis is plotted in logarithmic scale to help**  
519 **visualizing small water levels).**

520 The underground antecedent conditions are naturally linked to a seasonal  
521 behavior dominated by the hydrological conditions which can be traced in time  
522 as it can be seen from the synthetic data (Figure 6). The months from December  
523 to April follow a winter and spring behavior, characterized by wet soil conditions  
524 and aquifer water levels ranging from low to high. From June to July, a late spring  
525 behavior is visible, characterized by relatively dry soil (i.e., most of the data  
526 falling below soil field capacity), in combination with relatively high  
527 groundwater levels (indicating a still active slope drainage). In August and  
528 September, a summer like behavior is shown, with the driest soil water content  
529 and generally low aquifer water level. Finally, in October and November, the end  
530 of the dry season is shown: a wide range of soil wetness coupled with a still low  
531 aquifer water level.

532 For both the field monitored and synthetically obtained datasets, the observed  
533 conditions are the result of the time lag between the beginning of the rainy season  
534 and the slope response. The recurrent seasonal behavior observed for the



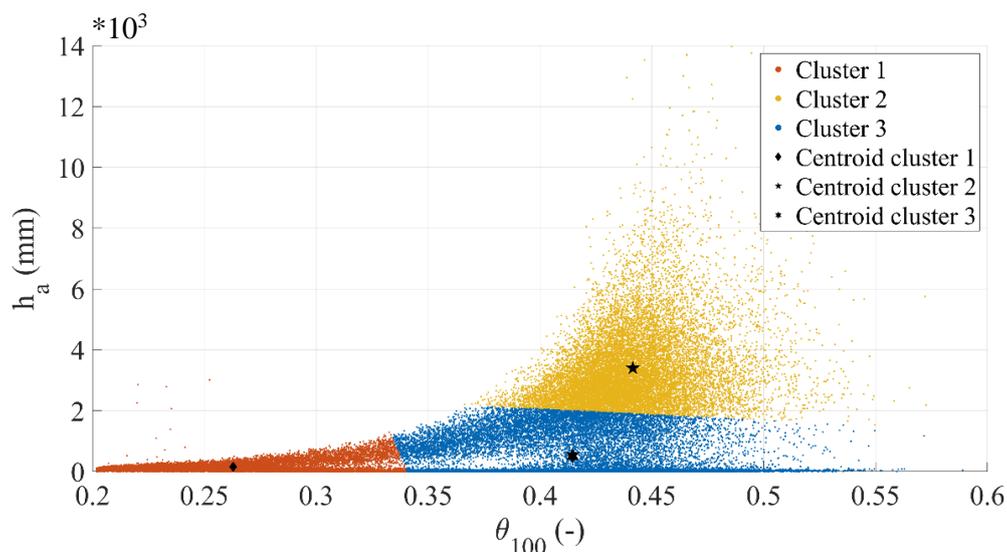
535 synthetic dataset, although delayed or anticipated owing to the year-by-year  
536 variability of rainfall, is close to that observed in the field.



537

538 **Figure 7. Histograms for data distributions of  $\theta_{100}$  (left) and  $h_a$  (right) for the**  
539 **synthetic dataset**

540 The overall situation for the synthetic dataset of antecedent conditions (i.e.,  
541 duplets  $\langle \theta_{100}, h_a \rangle$ ) can be described by the distribution of each individual  
542 variable, which can be seen in the histograms shown in Figure 7. It is interesting  
543 to note that, for both  $\theta$  and  $h_a$ , a bimodal behaviour is observed, corresponding  
544 to dry and wet field conditions.

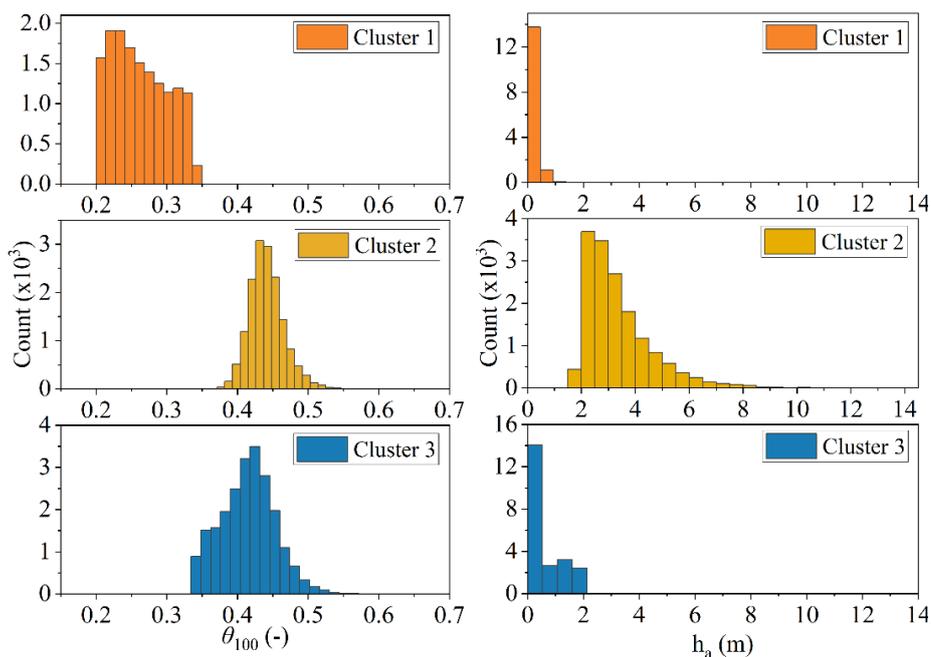


545

546 **Figure 8. Identified clusters for the duplets  $\langle \theta_{100}, h_a \rangle$  representing underground**  
547 **antecedent conditions of the synthetic dataset. For each cluster, the centroids are**  
548 **shown.**

549 The k-means clustering technique has been used to investigate the geometrical  
550 distribution of the duplets  $\langle \theta_{100}, h_a \rangle$ , with number of clusters ranging from 2 to  
551 7. According to the Silhouette metric, the optimal number of clusters is 3, with a  
552 metric value of 0.7, allocating the 28%, 30% and 42% of the data in clusters 1, 2  
553 and 3 respectively. Figure 8 shows the 3 clusters obtained within the synthetic  
554 dataset. Centroid positions are also displayed, showing the zones of the clouds  
555 where most of the dots are gathered. This representation of the data use both  
556 vertical and horizontal axes in linear scale to let visualize distance magnitudes  
557 between the different clusters, but it corresponds to the same dataset shown in  
558 Figure 6.

559 The distribution of the data after clustering is also analyzed for each cluster and  
560 the histograms are shown in Figure 9. It looks clear that the clusters capture  
561 different couplings of dry and wet underground antecedent conditions.



562

563 **Figure 9. Histograms for data distributions of  $\theta_{100}$  (left) and  $h_a$  (right) according**  
 564 **to each identified cluster in the duplets  $\langle \theta_{100}, h_a \rangle$**

565 In fact, cluster 1 captures dry conditions, with a volumetric water content below  
 566 the field capacity  $\theta_{fc}$  (it was estimated as 0.35 with the empirical relationship  
 567 proposed by Twarakavi et al. (2009) according to the van Genuchten model  
 568 parameters) and low values of  $h_a$ . Differently, clusters 2 and 3 capture scenarios  
 569 related to relatively wet soil cover conditions (i.e.,  $\theta_{100} > \theta_{fc}$ ), coupled to low  $h_a$   
 570 in cluster 3, gathering scenarios normally observed in late autumn, and to the  
 571 highest  $h_a$  conditions for cluster 2, comprising conditions normally occurring in  
 572 late winter and spring.

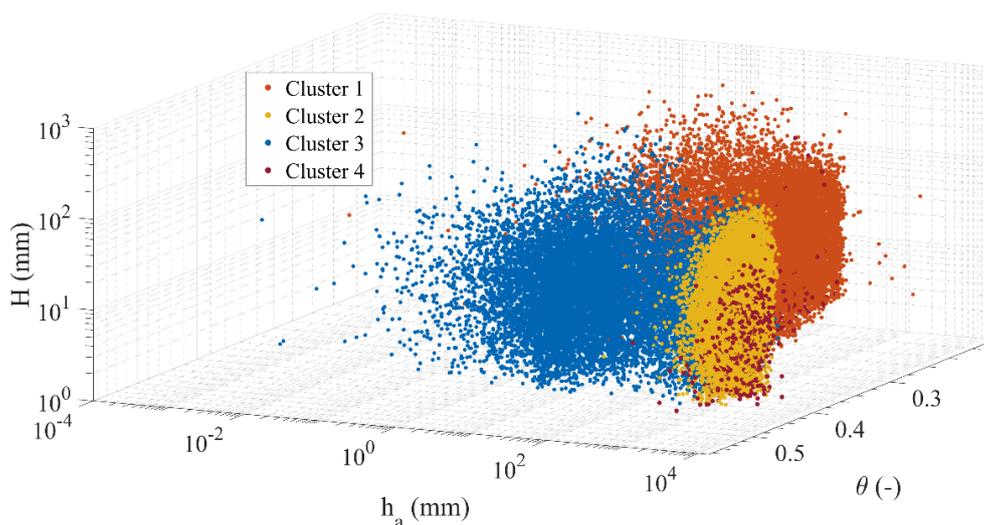
573 The two chosen variables,  $\theta_{100}$  and  $h_a$ , allow identifying three different  
 574 antecedent slope conditions one hour before the onset of any rainfall event.  
 575 Hence, it is worthy to investigate how these different antecedent conditions may  
 576 be related to different slope responses to precipitations.



577 **3.3. Effects of underground antecedent conditions on the slope**  
578 **response to rainfall**

579 The analysis of the data has been focused on identifying clusters within the  
580 triplets  $(\theta_{100}, h_a, \Delta S/H)$ , aiming to evaluate the slope response as the amount of  
581 rainwater being stored/drained in the soil cover. The results are being plotted in  
582 the space composed by the variables that can be monitored in the field:  
583  $(\theta_{100}, h_a, H)$ .

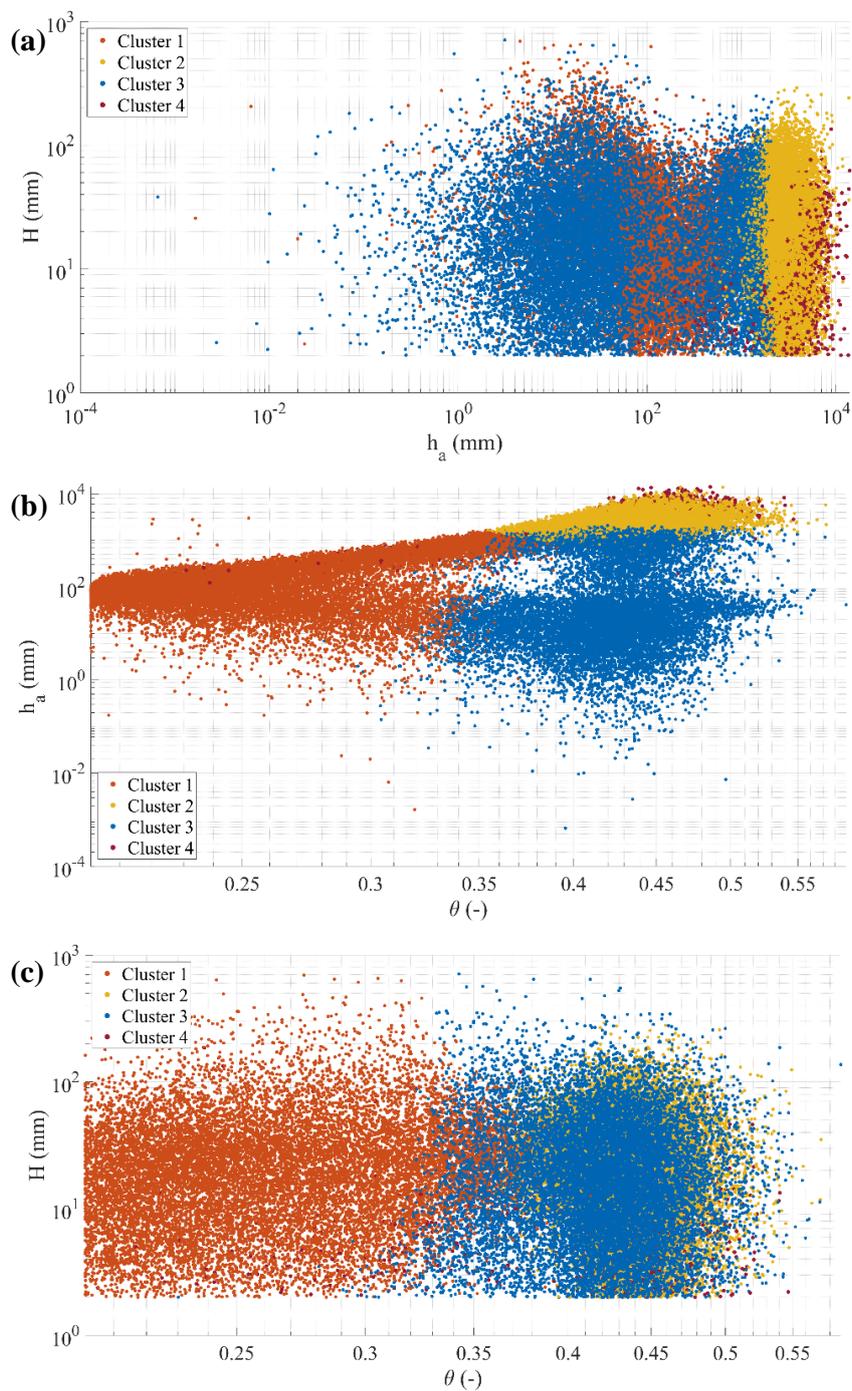
584 As it is not always expected to experience increased soil storage during rainfall  
585 events, the identification of draining slope conditions is an important aspect.



586

587 **Figure 10. Clustering results of the synthetic data triplets  $\langle \theta_{100}, h_a, \Delta S/H \rangle$**   
588 **represented in the space  $(\theta_{100}, h_a, H)$**

589



590

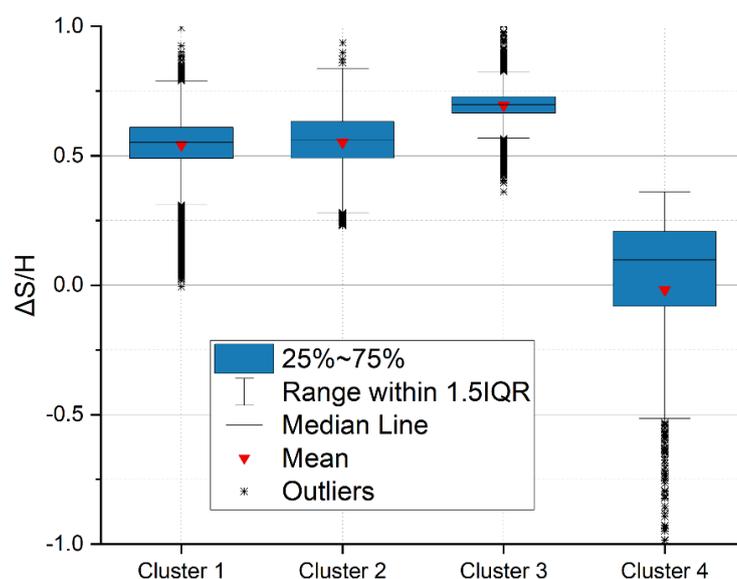
591

592

**Figure 11. Clustering results of the triplets  $(\theta_{100}, h_a, \Delta S/H)$  in (a)  $(\theta_{100}, h_a)$  plane; (b)  $(\theta_{100}, H)$  plane; (c)  $(H, h_a)$  plane**



593 Figure 10 and Figure 11 show the data clusters for the triplets  $(\theta_{100}, h_a, \Delta S/H)$ ,  
 594 for any identified rainfall event, represented in the  $(\theta_{100}, h_a, H)$  space in a  
 595 logarithmic axis representation. The Silhouette metric in this case suggests 4 as  
 596 an optimal number of clusters with a metric value of 0.61. It is remarkable that  
 597 three of the clusters are close to those already identified from the antecedent  
 598 (seasonally recurrent) underground conditions (section 3.2).



599

600 **Figure 12. Distribution of the slope response  $\Delta S/H$  for the data in each cluster**

601 Specifically, cluster 1, 2 and 3 correspond to different slope processes according  
 602 to  $\Delta S/H$  (Figure 12). Even if cluster 1 and cluster 2 show similar responses, with  
 603 slightly smaller  $\Delta S/H$  for cluster 1, the controlling processes are indeed different;  
 604 the conditions of cluster 1 are typically occurring in dry seasons with long dry  
 605 periods between short rainfall events, leading to dry antecedent conditions, so  
 606 that accumulation of water in the soil cover (increase in water storage) is expected  
 607 at each event. The data in cluster 2 are typically related to wet seasons, especially  
 608 in late winter and spring, where rainfall events are more frequent, leading to  
 609 antecedent wet soil ( $\theta_{100} \geq \theta_{fc}$ ) and antecedent high ground water level.



610 However, these conditions do not seem to correspond to effective slope drainage,  
611 so that the slope response in cluster 2 results comparable to that observed in  
612 cluster 1 in terms of  $\Delta S/H$ . Instead, the conditions gathered in cluster 3 differ  
613 from those in cluster 2 for the lower aquifer water level  $h_a$ , and the highest  $\Delta S/H$   
614 indicates the lowest slope drainage.

615 The additional cluster 4 identified here highlights a particular slope response, as  
616 it catches all the conditions where nearly zero and negative  $\Delta S$  take place,  
617 meaning an effective slope drainage during rainfall events. It is interesting to note  
618 that, even for relatively high rainfall events (above 100 mm), this slope response  
619 occurs when soil moisture is above the field capacity and when this condition is  
620 coupled with very high groundwater level, probably due to the high permeability  
621 all along the soil cover and to the hydraulic connection with the underlying  
622 aquifer.

#### 623 **4. Conclusions**

624 This study aims at identifying and analysing the major hydrological controls of  
625 the slope response to precipitations and, in that way, defining suitable variables  
626 to be monitored in the field to predict such response. The studied case refers to  
627 the hydrological processes in a slope system consisting of a pyroclastic soil cover  
628 overlaying a fractured karstic bedrock, where a perched aquifer develops during  
629 the rainy season. A synthetic time series of slope response to precipitations has  
630 been built, thanks to a physically based model, previously calibrated with field  
631 monitoring data, coupled with a stochastic rainfall generator. The seasonal  
632 behaviour of the slope shows substantial agreement between synthetic and  
633 experimental data. The synthetic dataset has been explored with Random Forest  
634 and k-means clustering, to evaluate the slope response characterized as the  
635 change in water stored in the soil cover ( $\Delta S$ ) during precipitation events with  
636 rainfall depth  $H$ , starting from different underground antecedent conditions.  
637 These were quantified through the mean volumetric water content in the



638 uppermost meter of soil cover ( $\theta_{100}$ ) and the aquifer water level ( $h_a$ ), one hour  
639 before the onset of rainfall.

640 The ratio  $\Delta S/H$ , which allows identifying slope response regardless the amount  
641 of event precipitation, is sensitive to both  $h_a$  and  $\theta_{100}$ , with the groundwater level  
642 being the most influential antecedent variable. The underground antecedent  
643 conditions, characterized by  $\theta_{100}$  and  $h_a$  and linked to the seasonal  
644 meteorological forcing, allow identifying different slope responses, related to the  
645 seasonally active hydrological processes.

646 High perched groundwater level, typical of winter and spring, indicates active  
647 slope drainage, which compensates rainwater infiltration, so that the soil storage  
648 remains stable, or even reduces, even after large rainfall events.

649 Differently, low perched groundwater level corresponds to impeded slope  
650 drainage. When it occurs with initially dry soil cover (typically in summer and  
651 early autumn), it tends to retain all the infiltrated rainwater as increased soil  
652 storage. When the soil cover is already wet (i.e., above the field capacity) at the  
653 onset of rainfall events, as it usually happens in late autumn and early winter, the  
654 increase of soil storage is smaller, as the soil approaches saturation.

655 The presented results suggest that monitoring antecedent conditions, by  
656 measuring suitable variables to identify the major hydrological processes  
657 occurring in the slope in response to precipitations, can be useful to understand  
658 such processes and to develop effective predictive models of slope response.  
659 Therefore, the proposed methodology can be replicated also in other contexts and  
660 be useful for several hydrologic applications: from the water supply towards  
661 natural streams due to infiltrated water, to the hydric stress estimation in crops  
662 (e.g., the centenary chestnut forests in the area of the case study) especially in  
663 very dry seasons, but also for the design of effective monitoring networks



664 exploiting geohydrological information for geohazard prevention (and early  
665 waring).

666



667 **Author contributions**

668 RG and DR formulated the research aim; PM provided the field measurements;  
669 PM and GS supplied the model simulations; DR and GS curated and analyzed  
670 the data; RG oversighted the research activities; DR worked on the preparation  
671 and the data visualization.

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676 Campania “L. Vanvitelli”.

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