Vortex streets to the lee of Madeira in a km-resolution regional climate model

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Abstract. Atmospheric vortex streets are a widely studied dynamical effect of isolated mountainous islands. Observational evidence comes from case studies and satellite imagery, but the climatology and annual cycle of vortex shedding are often poorly understood. Using the non-hydrostatic limited-area COSMO model driven by the ERA-Interim reanalysis, we conducted a ten-year-long simulation over a mesoscale domain covering Madeira and Canary Archipelagos at high spatial (grid spacing 1 km) and temporal resolutions. Basic properties of vortex streets were ~~analyzed~~ analysed and validated through a 6-day-long case study in the lee of Madeira Island. The simulation compares well with satellite and aerial observations and with existing literature on ~~idealized~~ idealised simulations. Our results show a strong dependency of vortex shedding on local and synoptic flow conditions, which are to a large extent governed by the location, shape, and strength of the Azores high. As part of the case study, we developed a vortex identification algorithm. The algorithm is based on a set of ~~objective~~ criteria and enabled us to develop a climatology of vortex shedding from Madeira Island for the 10-year simulation period. The analysis shows a pronounced annual cycle with an increasing vortex shedding rate from April to August and a sudden decrease in September. This cycle is consistent with mesoscale wind conditions and local inversion height patterns.

1 Introduction

Flow around isolated mountainous islands can lead to the formation of atmospheric vortex streets. ~~Favorable~~ Favourable conditions for the formation of vortex streets are quasi-steady upstream winds and a well-mixed planetary boundary layer capped by a thermal inversion below the island top (Etling, 1989).

Despite a striking similarity with the classic Kármán vortex street (Kármán, 2013), atmospheric vortex streets have different vorticity generation and decaying mechanisms. While Kármán vortex streets result from the instability of the wake behind cylinders in uniform laboratory flows, atmospheric vortex streets form in a stably-stratified (a stratification below and above the inversion layer) turbulent flow passing asymmetric flat obstacles. The wake vorticity of Kármán vortex streets is generated by a viscous boundary layer, whereas vortex shedding can also be observed with free-slip boundary conditions in 3D numerical

simulations. Atmospheric vortex shedding is speculated to be a result of potential vorticity creation (Etling, 1989) and tilting of baroclinically generated horizontal vorticity under the deformation of isentropes that can be predicted by linear gravity wave theory (Smolarkiewicz and Rotunno, 1989). Wake patterns and vertical variations of Kármán vortex streets in unstratified

25 fluids and a ~~nonrotating~~ non-rotating reference frame depend solely on the Reynolds number Re. In contrast, atmospheric vortex streets are also ~~characterized~~ characterised by the Froude number Fr, Rossby number Ro, and Strouhal number St (Horváth et al., 2020), whose definitions are given in Section 2.3.

Many studies focused on one or several specific aspects of vortex streets, which can be roughly divided into three categories: geometry, kinematics, and dynamics.

30 Geometry describes the shape of individual vortices and vortex streets. The total length of vortex streets can reach 400 km or more (Etling, 1989), which indicates a lifetime of individual vortices of over 10 hours considering a mean flow advection velocity of $10 \mathrm{~m~s}^{-1}$. Based on satellite images from the Aqua and Terra Moderate Resolution Imaging Spectroradiometer (MODIS) satellites, Young and Zawislak (2006) investigated aspect ratios of vortex streets, i.e. the ratio of the distance between two vortex tracks to the distance between ~~neighboring~~ neighbouring like-rotating vortices. They reported higher ratios (0.36 -

35 0.47) compared to the value 0.28 derived by Kármán (2013) for Kármán vortex streets.

Kinematics of vortex streets include the shedding frequency and advection velocity of vortices. Using the Weather Research and Forecasting (WRF) model, Nunalee and Basu (2014) performed a detailed analysis of the Strouhal number. The Strouhal number represents a direct relation between vortex shedding frequency, wind velocity, and the crosswind island diameter at the inversion base. Tsuchiya (1969), using satellite images in the wake of Cheju Island, South Korea, reported that the advection

40 velocity of vortices approximates 76% of the undisturbed flow when the aspect ratio is 0.332.

Dynamics of vortex streets refer to vortex generation, shedding, and decaying mechanisms. Heinze et al. (2012) employed an ~~idealized~~ idealised large eddy simulation to study the azimuthally averaged structure of vortices. They found a warm core with convergence at the surface and divergence at the vortex top, and suggested that a ~~sinking~~ lower inversion at the vortex ~~center~~ centre might explain cloud-free eyes in observations. From a mathematical perspective, the vertical vorticity

45 can be derived from turbulent stresses and the tilting of horizontal vorticity ~~and turbulent stresses (Epifanio, 2015), whereas Rotunno et al. (1999) argued that the latter is inessential~~(Epifanio, 2015; Rotunno et al., 1999). Schär and Smith (1993a) performed numerical simulations of a single layer of symmetric shallow-water flow past a circular mountain in a ~~nonrotating environment with~~ non-rotating environment with a frictionless surface. They proposed two mechanisms for the production of potential vorticity. First, internal dissipation, which is derived from a theory indicating that the steady-state Bernoulli function

50 is the stream function of the total vorticity flux. Second, flow separation leads to the joining of two flow streams with different values of the Bernoulli function. Subsequently, Schär and Smith (1993b) relaxed the symmetric flow conditions and ~~analyzed~~ analysed observed vortex streets with instability theory. With continuously stratified flow models, Schär and Durran (1997) used the dimensionless mountain height to identify different flow conditions that are conducive for vortex shedding and gravity wave breaking, respectively. They suggested the ~~generalized~~ generalised Bernoulli theorem (Schär, 1993) for the explanation

55 of potential vorticity generation. The dynamics of shedding in geophysical wakes are very similar to those of homogenous wakes, which have been well documented (Epifanio, 2015).

However, the study of vortex shedding in the lee of isolated islands is still limited by the availability of wind fields with high spatial and temporal resolutions. Satellite images of stratocumulus clouds, which are capped by an inversion base and can act as tracers of vortex streets, have been widely used for the study of vortex shedding (Young and Zawislak, 2006; Etling, 2019).

60 They can provide information about geometric characteristics of vortex streets through daily snapshots in the case of polar-orbiting satellites such as MODIS Terra and Aqua, but they are restricted to cloudy conditions (Young and Zawislak, 2006). With cloud motion winds and ocean surface winds from the Advanced Scatterometer (ASCAT), Horváth et al. (2020) reported an asymmetric vortex decay with larger peak vorticity in cyclonic eddies than in anticyclonic eddies at Guadalupe island. They argued that it is ascribed to Guadalupe's ~~nonaxisymmetric~~ non-axisymmetric shape and the Earth's rotation, where the

65 latter factor is also supported by experiments of Ruppert-Felsot et al. (2005). Ito and Niino (2015) adopted a non-hydrostatic mesoscale model for numerical simulations of vortex streets in the lee of Cheju Island. They speculated that vortices are more likely generated through gravity wave breaking and the baroclinicity of flows over mountains than through viscous boundary layers. The importance of air-sea interactions on the wake patterns of Madeira Island was studied using the WRF numerical model by Caldeira and Tomé (2013). They proposed that the enhanced vertical mixing by increased sea surface temperature

70 (SST) could lead to the erosion of the inversion base and a transition from vortex-shedding to a long straight wake. Aerial observations were employed for the study of atmospheric wakes in the lee of Hawaii (Smith and Grubišić, 1993) and Madeira Island (Grubišić et al., 2015). Grubišić et al. (2015) recommended potential vorticity, which can be generated by gravity wave breaking and is ~~conservative~~ conserved in an adiabatic and inviscid flow, for the study of vorticity sources rather than the ~~nonconservative~~ non-conserved vertical vorticity.

75 The impacts of vortex streets on the atmosphere and ocean have received relatively little attention. Using the Regional Oceanic Modeling System ocean circulation model, Couvelard et al. (2012) investigated the influence of wakes induced by Madeira Island on the ocean-eddy generation with an eddy tracking algorithm developed by Nencioli et al. (2010). They proposed that the island-induced wind-wake contributes to oceanic surface kinetic energy and vorticity, as well as the generation and containment of ocean eddies. Nunalee et al. (2015) used a coupled mesoscale model and ray-tracing framework to explore

80 km-scale optical refractive perturbations caused by wake vortices of three islands. These perturbations are crucial for long-range optical communication systems that depend on precise laser guidance. Their study highlights the necessity of considering heterogeneous atmospheres (especially in the presence of vortex streets) for optical wave propagation studies. With a focus on atmosphere-ocean interactions, Azevedo et al. (2020) studied the detailed responses of upper oceanic profiles of temperature, salinity, and turbulence to the Madeira warm wakes, which mainly result from intense solar radiation in cloud-free conditions.

85 In this study, we ~~focused~~ focus on vortex streets in the lee of Madeira Island. It involves not only a case study as in most previous studies but also a climatology over one decade. The Madeira Archipelago is located near the northwestern African coast and forms part of Macaronesia. The weather and climate patterns in Macaronesia are mainly influenced by the subtropical semi-permanent Azores high-pressure system (Davis et al., 1997), prevailing north-easterly trade winds (Cropper and Hanna, 2014), local orographic characteristics (Carrillo et al., 2016), surrounding ocean currents, and Sahara dust advection (Cropper,

90 2013). Madeira Island is the largest (740 km^2) and highest (1862 m) island in this archipelago and the major source of atmospheric flow disturbances, while Porto Santo and Desertas play a minor role due to low altitudes. Madeira Island experiences
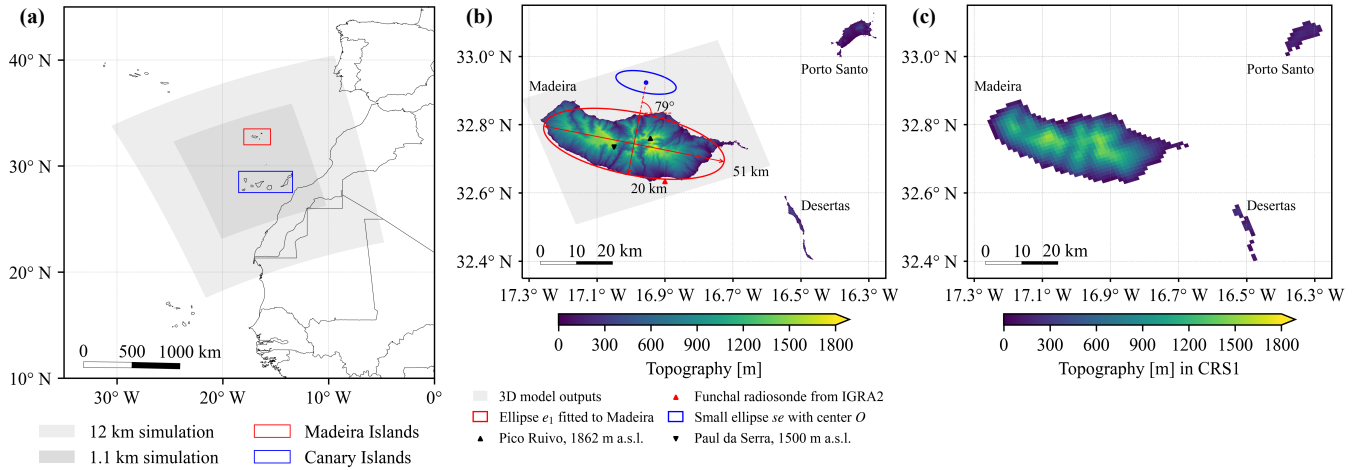
Figure 1. (a) 12 km (CPS12) and 1.1 km (CRS1) COSMO model simulation domains, and the location of Madeira and Canary Archipelagos. (b) Topography of Madeira Archipelago with 30 m horizontal resolution from European Environmental Agency under the GMES RDA project; The ~~gray~~ grey shading shows the region with decadal model outputs in all 60 (61) vertical model layers (levels). The Funchal radiosonde data from IGRA2 were used to calculate the inversion height. A red ellipse e_1 was fitted to the topography of Madeira using a Gaussian mixture model. The blue ellipse se was obtained by scaling e_1 to its 1/9 in area and then shifting along its minor axis for the length of its minor axis. se was employed to extract decadal 3D upstream conditions, which are only available within the ~~gray shaded~~ grey-shaded area in (b). It is important to mention that these upstream conditions cannot be assumed to be undisturbed due to the proximity of se to the island. The altitude of two mountain peaks indicated by black triangles is used to compare with the inversion height. (c) The topography with a horizontal ~~resolution~~ grid spacing of 1.1 km used in CRS1. The geographic map is from the Natural Earth.

less precipitation in summer than in winter. This can be mostly attributed to the more northern position of the Intertropical Convergence Zone (ITCZ) in summer and its associated dry region from the Hadley circulation. More precipitation is observed in the north or northeast windward regions than in the lee sides due to prevailing north-easterlies and orographic lifting (Cropper,

95   2013). The choice of Madeira Island for enhancing our understanding of land-atmospheric interactions is justified by its good isolation from continents, clear dynamical effects created by its topography, and the vulnerability to extreme weather events induced by its geographical conditions (Ramos et al., 2018).

Plenty of theoretical studies have been devoted to the dynamics of vortex streets and many observational studies concentrated on the geometry and kinematics. Nevertheless, they usually relied on limited case studies and ~~idealized~~ idealised numerical

100   simulations. This study ~~makes a significant contribution~~ contributes to this research field with realistic simulations of the real atmosphere and a vortex identification algorithm. This algorithm allowed us to investigate the climatology of vortex shedding to the lee of Madeira.
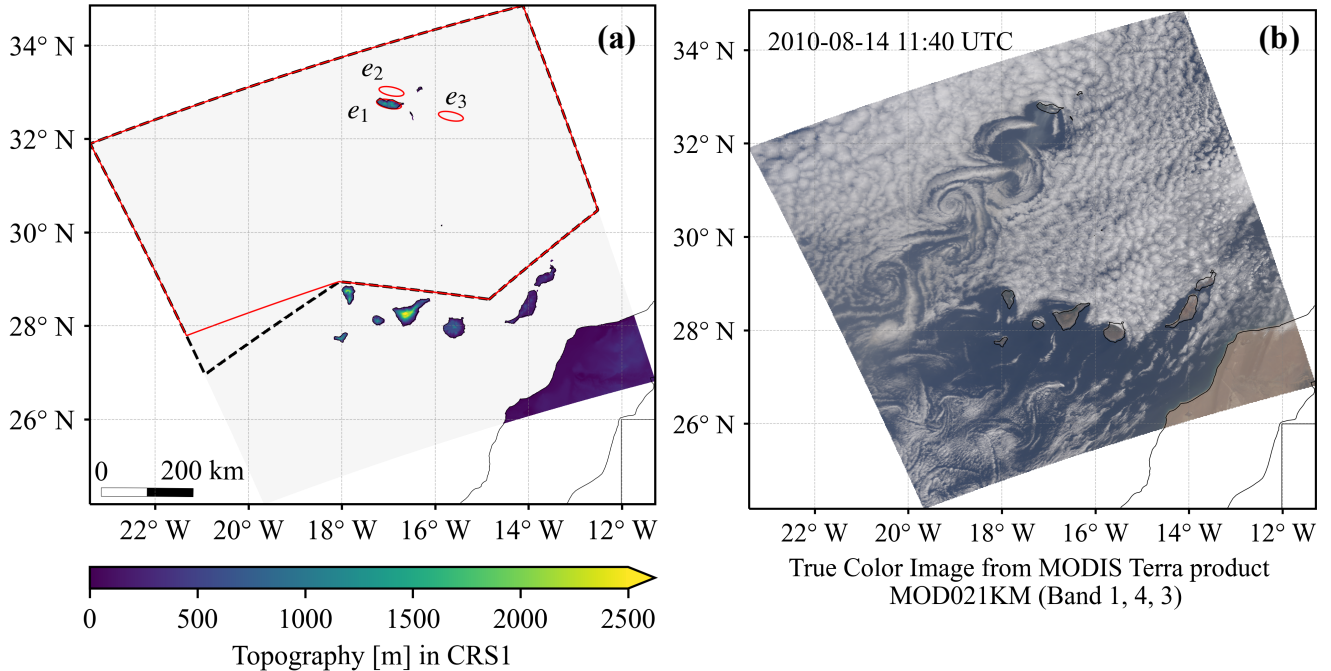
Figure 2. (a) The ~~gray~~ grey shading shows the region used for subsequent analysis. The red ellipses e_2 and e_3 were obtained by shifting e_1 as defined in Fig. 1b along its minor and major axes to extract upstream and undistorted flow conditions, respectively. The black dashed and red polygons were used for vortex identification in Section 2.4. (b) An example of vortex streets to the lee of Madeira is visible through stratocumulus clouds using the data product MOD021KM from MODIS Terra satellite (Savtchenko et al., 2004). Such pictures can be viewed directly on the website of NASA Worldview (https://worldview.earthdata.nasa.gov). The geographic map is from the Natural Earth.

2 Data and methods

2.1 Model simulations

105 We used the non-hydrostatic Consortium for Small-Scale Modeling model in climate mode COSMO-CLM (Baldauf et al., 2011; Rockel et al., 2008). Specifically, we employed a refactored version of COSMO-CLM 5.09, which has been ported to run on hybrid GPU-CPU architectures in a joint effort between MeteoSwiss, the ETH-based Center for Climate Systems Modeling (C2SM), and the Swiss National Supercomputing Center (CSCS) (Fuhrer et al., 2014, 2018). In COSMO, a third-order Runge–Kutta split-explicit scheme is used for integrating compressible Euler equations (Wicker and Skamarock, 2002).

110 A fifth-order upwind scheme is used for horizontal advection and an implicit Crank-Nicholson scheme is adopted for vertical advection. The model is equipped with a full set of ~~parameterization~~ parameterisation schemes (see Ban et al., 2014). We used a horizontal ~~resolution~~ grid spacing of 1.1 km for a ~~convection-resolving~~ convection-allowing simulation (CRS1) over east Macaronesia (1100 km $\times$ 1100 km) as shown in Fig. 1a. This simulation was run ~~with the deep and shallow convection scheme off~~ without employing the shallow and deep convection schemes. Lateral boundary conditions were provided by a

115   convection-parameterizing simulation with a horizontal ~~resolution~~ grid spacing of 12 km (CPS12) driven by the ERA-Interim reanalysis with 6-hourly frequency (Dee et al., 2011).

     The simulation domain was defined relative to a rotated north pole at 43° N and 170° W, and contains 60 vertical layers up to 23.5 km altitude. The thickness of each layer widens from 20 m at the surface to around 1200 m near the model top. At the top of the model domain, we used implicit Rayleigh damping for the vertical velocity following Klemp et al. (2008) to prevent the

120   reflection of upward-propagating gravity-wave energy. CPS12 spanned from 2000-01 to 2015-12 including a spin-up period of 5 years, while CRS1 run from 2005-11 to 2015-12 and was initialized for 2 months before the analysis period to ensure a proper adjustment of the soil moisture (Ban et al., 2015). Both simulations provide hourly outputs on selected vertical levels over the entire respective simulation domains, and CRS1 also provides hourly data on all model levels over a smaller region indicated by ~~gray~~ grey shadings in Fig. 1b. While the wind data are available at altitudes of 10 m and 100 m for the whole

125   domain in CRS1, 100-meter winds at 1.1 km horizontal ~~resolution~~ grid spacing were used for our vortex shedding analysis. For the case study in Section 3.2, we restarted the model simulation from 2010-08-01 00:00 UTC to generate 3D hourly data at a vertical interval of 100 m up to 5 km above the surface over the entire simulation domain of CRS1. Unless explicitly specified, the data used for analysis come from the original decadal CRS1.

     Figure 1b shows the digital elevation model of Madeira Archipelago with a horizontal resolution of around 30 m based on

130   data from the European Environment Agency (https://sdi.eea.europa.eu). We fit an ellipse ~~centered~~ centred at 32.74° N and 16.99° W with an area of about 800 km^2 to Madeira Island using a Gaussian mixture model (Reynolds, 2015). The length of the major and minor axes of the ellipse are about 51 and 20 km, respectively. The minor axis is oriented at 79° and is approximately parallel to the prevailing trade winds. Figure 2a shows the model domain of CRS1 used for analysis, where we excluded 80 grid points at the lateral boundaries to eliminate any effect of the relaxation zone. In addition to the original ellipse

135   e_1 fitted to Madeira Island, we shifted it along its major and minor axes to extract upstream conditions at e_2 ~~centered~~ centred at 33.01° N and 16.94° W, and undisturbed flow conditions at e_3 ~~centered~~ centred at 32.48° N and 15.66° W. An example of vortex streets in the leeward of Madeira Island is shown in Fig. 2b.

2.2   Observational data sources

     In addition to model simulations, we explored multiple observational data sources for validation or comparison. The ERA-

140   Interim reanalysis (Dee et al., 2011), with a horizontal ~~resolution~~ grid spacing of about 79 km and a frequency of 6 hours, was used to provide initial and boundary conditions for CPS12. For data analysis, we employed the ERA5 reanalysis (Hersbach et al., 2020), which is also produced by the European Centre for Medium-Range Weather Forecasts (ECMWF) and embodies hourly climate records at a higher horizontal ~~resolution~~ grid spacing of around 31 km.

     ASCAT is a C-band (5.255 GHz) fan-beam scatterometer system on ~~polar orbiting~~ polar-orbiting meteorological operational

145   (MetOp) platforms from the European Organisation for the Exploitation of Meteorological Satellites (EUMETSAT) (Figa-Saldaña et al., 2002). The primary mission of ASCAT is to provide 10-meter global ocean wind vectors that are mainly used for assimilation in numerical weather prediction models. On ASCAT, six antennas cover two 550 km swaths with an interval of 360 km at a minimum orbit height of 822 km. A wind product, at a resolution of 25 km on a 12.5 km nodal grid,

is generated from ASCAT level 1b data using an empirical geophysical model function by the Ocean and Sea Ice Satellite Application Facility (OSI SAF). However, we used ASCAT Wind Data Processor (AWDP) software to derive wind data from measurements of ASCAT onboard the Metop-A satellite at a higher resolution of around 17 km on a 6.25 km grid to provide more details about vortex streets (Vogelzang et al., 2017). When discussing vortex streets, we refer to modelled vortices by default; otherwise, we stress that the vortices are based on observations. Note that although the terms horizontal resolution and grid spacing are often used interchangeably (also in our study), they are different for ASCAT wind products and the products introduced below, as their values at each grid are derived by aggregating observations from surrounding grids.

For the comparison of vortex streets in simulations and the real atmosphere, we employed the high rate SEVIRI level 1.5 image data of the geostationary satellite Meteosat-9 in the Meteosat Second Generation (MSG) from EUMETSAT (Schmetz et al., 2002). These data provide ~~high rate~~ high-rate transmissions in 12 spectral channels covering 81° S to 81° N and 79° W to 79° E every 15 minutes. They have a sampling distance of 3 km and a horizontal ~~resolution~~ grid spacing of 4.8 km at the sub-satellite point, and a sampling distance of 4 to 5 km in our analysis region. An introduction to create and interpret standard RGB images from METEOSAT/SEVIRI can be found on the website of an international training project EUMeTrain founded by EUMETSAT (https://www.eumetrain.org). We used the Natural Colors RGB for daytime (08:00 - 19:00 UTC) and the Night Microphysics RGB for nighttime.

Vertical temperature profiles from radiosonde observations at Funchal and Tenerife on a daily (normally at 12:00 UTC) and twice-daily (normally at 00:00 and 12:00 UTC) basis, respectively from the Integrated Global Radiosonde Archive (IGRA) version 2 (Durre et al., 2006) were explored for a decadal climatology of inversion height. The location of Funchal radiosonde station is shown in Fig. 1b. As the geopotential height is often not available at reported pressure levels, it was computed using the hydrostatic relation (Durre and Yin, 2008). Albeit IGRA V2 provides the inversion height defined as the height of the warmest temperature in the sounding, we estimated it based on the definition from Kahl (1990), i.e. the lowest layer where temperature increases with height.

To validate simulated precipitation patterns, we used a data set of conventional meteorological surface stations. The network contains 17 stations in the height range 25-1799 m. Most stations cover at least 5 years of the simulation period 2006-2015. The validation of precipitation against this data set is conducted following the method described in Ban et al. (2020). That is, CPS12 model outputs are interpolated to station sites with ~~nearest-neighbor~~ nearest-neighbour interpolation and for CRS1 the grid cell with the smallest altitudinal difference within a 4 km radius is selected for comparison.

2.3 Basic flow parameters

Following Snyder et al. (1985) and Heinze et al. (2012), the Froude number Fr was defined here as the ratio of inertial to buoyancy forces. In the case of a uniformly stratified airstream, it is given by $Fr = U/(Nh_m)$ where N denotes the Brunt-Väisälä frequency, U the upstream wind speed, and h_m the mountain height. In ~~a number of~~ some studies, the inverse of Fr was alternatively used and referred to as the dimensionless mountain height, i.e. $h_{dim} = Fr^{-1} = Nh_m/U$.

The concept of the dividing streamline h_{ds} is commonly used in the analysis of flow past 3D topography. Here the height of this streamline h_{ds} is the upstream height that separates the streamlines passing over a three-dimensional hill in a stably

stratified flow from those passing around the hill. h_{ds} can be calculated based on Sheppard's energy theory (Sheppard, 1956): upstream air parcels at an altitude above h_{ds} would have sufficient kinetic energy to surmount the island, whereas below h_{ds}

185 the flow is quasi horizontal around the island. Sheppard's energy theory assumes that all kinetic energy is converted to potential energy, and thus h_{ds} provides the lowest possible dividing streamline height. In the case of general upstream profiles $U(z)$ and $N(z)$, h_{ds} can be estimated from (Heinze et al., 2012)

$$\frac{1}{2}U^2(h_{ds}) = \int_{h_{ds}}^{h_m} N^2(z)(h_m - z)dz \,, \tag{1}$$

where $N(z)$ is the Brunt-Väisälä frequency defined as

190 $$N(z) = \left(\frac{g}{\theta(z)} \frac{\partial\theta(z)}{\partial z} \right)^{1/2} . \tag{2}$$

Here $g = 9.81 \text{ m s}^{-2}$ is the gravitational acceleration and $\theta(z)$ the upstream potential temperature.

For upstream profiles of uniform N and U, h_{ds} can be obtained analytically as (Sheppard, 1956)

$$h_{ds} = h_m(1 - Fr) \,. \tag{3}$$

In atmospheric flows past 3D obstacles, vortex shedding occurs at $Fr < 0.4$ (Etling, 1989), which appears to be roughly

195 consistent with the laboratory experiments of Hunt and Snyder (1980). These results are also consistent with ~~idealized~~ idealised numerical experiments using free-slip lower boundary conditions (Schär and Durran, 1997). For instance, Schär and Durran (1997) found vortex shedding for $Fr = 1/3$, while for $Fr = 2/3$ there was nonlinear flow over the topography with gravity wave breaking and no vortex shedding.

However, the validity of Sheppard's energy theory was questioned by ~~?~~ Smith and Gronas (1993) from a theoretical perspec-

200 tive. They argued that the deceleration of air parcels approaching the mountain is due to the pressure gradient associated with ~~the~~ a hydrostatic gravity wave aloft, rather than due to vertical displacements ~~. However, we believe that in situations with a pronounced inversion, as considered here,~~ of air parcels. Therefore, relationships between the dividing streamline ~~concept is valid~~ height and vortex shedding should be investigated and interpreted with caution.

In our realistic simulation, N and U vary vertically, so we approximated Eq. (2) as

205 $$N^2 = \frac{g}{\theta} \frac{\theta(h_m) - \theta(h_{surf})}{h_m} \,, \tag{4}$$

for the estimation of h_{dim}, where h_{surf} denotes the surface height. Likewise, U and θ are expressed as the vertical average of wind velocity and potential temperature below h_m, respectively.

The Rossby number is a dimensionless parameter for rotating reference frames. It is defined by the ratio between inertial force and Coriolis force as

210 $$Ro = \frac{U}{fL} \,, \tag{5}$$

where L is the relevant spatial scale, and $f = 2\Omega\sin\phi$ is the Coriolis parameter with $\Omega = 7.29 \times 10^{-5}$ s^{-1} being the rate of Earth's rotation and ϕ being the latitude.

Another important parameter, defining the dimensionless shedding frequency of vortices, is the Strouhal number, defined as

$$St = \frac{D}{TU},\tag{6}$$

where D is the ~~crosswind island diameter~~ width of the island perpendicular to the wind direction at the inversion base, and T is the shedding period between two successive vortices on the same side of obstacles.

2.4 Rule-based vortex identification

In this section, we introduced a rule-based vortex identification algorithm consisting of wavelet analysis and a series of criteria. The central idea of our algorithm is inherited from McWilliams (1990). He suggested judging the reliability of an algorithm in terms of both the prior plausibility of criteria and the posterior performance.

Several concerns in designing criteria are illustrated below. To extract individual vortices, we firstly denoised the spatial field of relative vorticity using wavelet analysis (Doglioli et al., 2007), of which theoretical and technical aspects are presented in Appendix A. Although in the case of ocean eddies, it is more objective to determine vortex boundaries based on closed streamlines (Nencioli et al., 2010), this method does not apply to atmospheric vortices due to strong background winds. As older ~~shedded~~ shed vortices have a smaller area with relative vorticity above a given threshold, the main challenge is to separate small vortices from noise. Accordingly, we intentionally put stricter constraints on smaller vortices. The selected criteria are presented and explained below, and the order is designed to ~~maximize~~ maximise computational efficiency.

1. Minimum magnitude of absolute values of relative vorticity for a vortex at a height of 100 m: 3×10^{-4} s^{-1}.

   This step identifies grid cells that could belong to a vortex and clusters adjacent grid points above a threshold. The cell identification is based on a cloud identification algorithm from Mosimann (2016). Mosimann (2016) used a list-based union-find data structure (e.g., Cormen et al., 2001) to successively build up the clusters.

2. Minimum peak magnitude of absolute values of relative vorticity in a vortex: 4×10^{-4} s^{-1}.

   This criterion poses a weak constraint on peak absolute values of relative vorticity in extracted clusters from the first step.

3. Minimum size of a vortex: 100 km^2.

   Albeit this criterion will eliminate smaller vortices, it is an essential step to distinguish vortices from noise.

4. A vortex should not be in contact with the model topography.

   If a vortex contacts with the model topography, we regard it as not ~~shedded~~ shed, although it might be in its generation phase.

5. The ~~center~~ centre of a vortex should be located within the black dashed polygon in Fig. 2a for our case study in Section 3.2 and within the red polygon in Fig. 2a for our climatological study in Section 3.3.

   The black dashed polygon denotes the region where vortices ~~shedded~~ shed from Madeira Island can appear and was used for the case study to identify as many vortices as possible. However, if it was employed for decadal vortex identification, a significant number of vortices ~~shedded~~ shed from La Palma island in the Canary Archipelago would be wrongly incorporated. So for decadal analysis, we adopted the red polygon to avoid the interference of La Palma island.

6. If the vortex size is less than $450 \ \mathrm{km}^2$, there must be a local potential temperature maximum at $2 \ \mathrm{m}$ altitude within the vortex area or within the circle defined by the nominal radius around its ~~center~~ centre.

   This criterion is well justified by the properties of ~~shedded~~ shed vortices. As reported by Heinze et al. (2012), both positive and negative shed vortices have a warm core and do not exhibit a significant vertical tilt within the boundary layer. This structure is also supported in Fig. 11 and Fig. 12. This feature was used to track vortex shedding in ~~idealized~~ idealised simulations (Heinze et al., 2012). The nominal radius of a vortex is defined as the radius of a circle that has the same area as the vortex.

7. If the vortex size is in the range of ~~less than~~ <450~~(450 to 900, or larger than~~, 450-900, or >900 ~~)~~ km^2, the angle between the mean wind vector within a vortex and the vector connecting the Madeira ~~center and vortex center~~ centre and vortex centre should be less than $30°$~~(,~~ $40°$, or $50°$~~)~~, respectively.

   This requirement restricts the advection direction of a vortex. The thresholds were selected conservatively based on our observations to exclude vortices that are unlikely to be ~~shedded~~ shed from Madeira Island. Although ~~shedded~~ shed vortices can be deviated from their original tracks by synoptic flows (Etling, 2019), we consider this condition as an exception and focused on normal cases.

8. Maximum ratio of the largest distance between two grid cells within a vortex to its nominal radius: 5.

   The criterion limits the deviation of vortex shape from a circle (McWilliams, 1990). It is mainly used for the elimination of elongated vorticity signals, which may be due to noise or vorticity banners attached to the terrain (Schär et al., 2003).

9. There must be at least one vortex satisfying all the above conditions either at the previous hour or the next hour.

   It aims at excluding isolated vortices that have no precursor and successor.

The quantification and climatology of vortex shedding behind Madeira rely on vortex counting. We used two kinds of counting methods serving different purposes. After vortices shed from Madeira are identified at each hour, the hourly number of vortices over the study domain can be obtained directly by counting different vortices (e.g. Fig. 7). Thereafter, the daily and monthly number of vortices are aggregated from the hourly numbers (Fig. 15 and Fig. 16). The second approach is applied to investigate the spatial distribution of vortex shedding (i.e. Fig. 14). For each grid cell at each hour, we counted the vortex number as one if any identified vortex covers this grid cell. Then the hourly vortex count at each grid cell is obtained by summing the vortex number through the whole study period (2006-2015). Consequently, both counting methods will result in

the same vortex being counted multiple times, as the lifetime of a vortex typically is longer than one hour. To count unique vortices, Lagrangian tracking would have to be used already during the model simulation. However, this study is based on hourly model output. Therefore, an approach where we accept multiple counting is likely more robust than an approach with additional criteria for the uniqueness of vortices and will not qualitatively change the results of this study.

3   Results

3.1   General meteorological conditions

Fig. C1a presents annual mean precipitation over our analysis region in the ERA5 reanalysis from 2006 to 2015. It ranges from 43 to 564 with increasing amounts from the southeast to the northwest. Wetter conditions can be observed near the islands as an effect of orographic lifting. Although Fig. C1a-c indicate negative biases of simulated precipitation in comprison to the ERA5 reanalysis over the ocean, especially in CRS1, the above-mentioned spatial patterns are well simulated in both CPS12 and CRS1. Fig. C1d-f display precipitation over Madeira Archipelago in a zoomed-in version. The horizontal resolutions of the ERA5 reanalysis (0.25°)and CPS12 (12)are insufficient to resolve the topography. Indeed, maximum elevation over Madeira amounts to around 1862 in reality, 1546 in CRS1, 600 in CPS12, and 330 in ERA5. As a result, To quantitatively evaluate the lifting and splitting of the ambient flow cannot properly be represented in ERA5 and CPS12, yielding too small precipitation amounts and unrealistic patterns. In contrast, CRS1 produces much larger precipitation amounts approximately centered over Madeira.

The high values over Madeira Island in CRS1 are qualitatively consistent with the fact that occasionally even flash floods can occur (Fragoso et al., 2012; Luna et al., 2011). To quantitatively validate the simulations, we compared simulated annual mean precipitation against observations at conventional surface stations (Fig. 3). The CPS12 simulation reaveals reveals a large underestimation with typical biases amounting to 40-80%, in particular at mountain stations. In CRS1 we found more realistic results as the convection is partially resolved and the topography is more realistic. In particular, some of the mountain stations now exhibit precipitation amounts around 1000 mm close to observations, and the biases are reduced considerably. However, precipitation is still underestimated, and the asymmetry of the Madeira precipitation (with higher amounts upstream) is not fully captured. It is likely that these These systematic errors are likely due to the representation of microphysical processes, as a considerable fraction of precipitation in Madeira falls as drizzle.

Figure 4 demonstrates annual variations in precipitation over Madeira Island in the ERA5 reanalysis, CPS12, and CRS1, while the comparison of spatial patterns is shown in Fig. C1. Although the grid cells used in each dataset do not cover the same region (see the caption), the comparison reveals that the three datasets qualitatively agree. Interestingly, a drying trend can be observed in both observations and simulations from April to August, and is interrupted by a sudden change to wetter conditions in September. Although there is no study reporting a direct relationship between precipitation and vortex shedding, we can see a synchronous change in vortex shedding patterns in Section 3.3.

The 100-meter wind climatology in CRS1 during 2006-2015 over the analysis region defined in Fig. 2a is shown in Fig. 5. Equivalent plots with data from the ERA5 reanalysis (not shown) have quite similar monthly patterns and indicate good
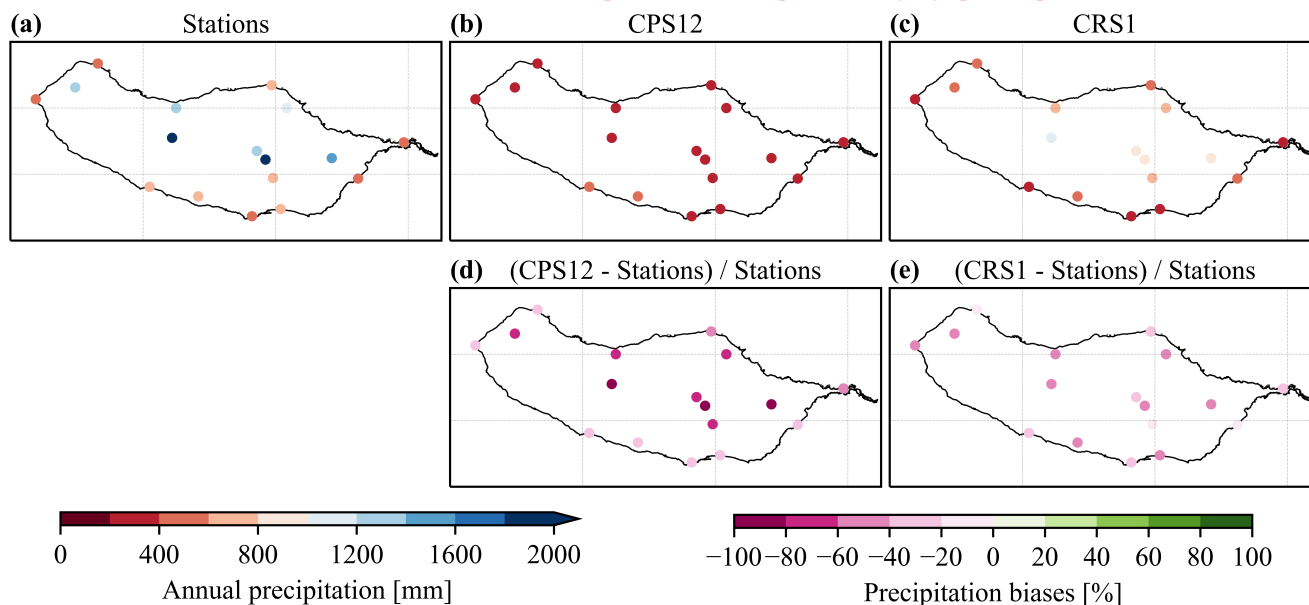
Figure 3. ~~Validation~~ Evaluation of precipitation [mm] against conventional surface stations. Annual-mean precipitation amounts (2006-2015) from (a) the observational dataset, (b) CPS12, and (c) CRS1. Relative biases [%] of (d) CPS12 and (e) CRS1 with respect to observations at stations. The geographic map is from the GADM.

305   performance of our simulation in terms of wind climatology. Our analysis region is dominated by north-easterlies throughout the year, consistent with trade winds. A significant concentration in wind direction and an increase in mean wind speed from April to August generate ~~favorable~~ favourable conditions for vortex shedding as shown in Section 3.3.

    In Fig. 6a, the monthly inversion height observed at the Funchal radiosonde station from 2006 to 2015 also shows very interesting patterns. Firstly, the observed monthly mean inversion height decreases from about 1.5 km in April to around 1

310   km in July and August, which is conducive ~~for~~ to flow splitting and thus vortex shedding. It then increases to above 1.6 km in September and results in ~~unfavorable~~ unfavourable conditions for vortex shedding, like the winds in Fig. 5, both of which are influenced by the Azores high-pressure system. The observed monthly mean inversion height is about 1.5 km from September to April. By comparing the monthly inversion height in observations and simulations in CRS1, we can detect that their standard deviations are rather close and the monthly patterns are very well simulated despite consistent negative biases of around 150

315   m. As atmospheric conditions at Funchal are disturbed by Madeira Island, we also ~~showed~~ show the monthly inversion height in CRS1 over the ellipse *se* from Fig. 1b with upstream conditions under prevailing north-easterlies. Unfortunately, the flow in *se* is still strongly affected by the orography and therefore does not represent undisturbed upstream conditions (which we lack due to the limited domain with 3D data). However, using it still gives us some indications about the variability of the inversion height. The simulated values over *se* are close to those near Funchal except in July and August, where the monthly mean
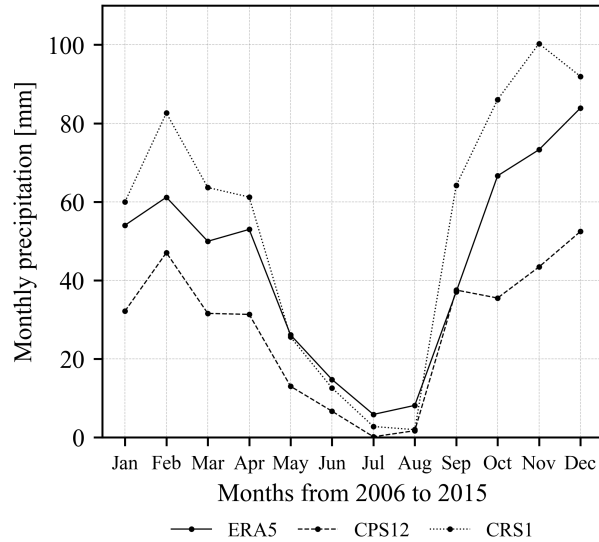
Figure 4. Monthly precipitation [mm] over Madeira Island in the ERA5 reanalysis, CPS12, and CRS1 from 2006 to 2015. For each dataset, the grid cells whose ~~center~~ centres are located within the ellipse e_1 in Fig. 2a were used to calculate the spatially-averaged monthly precipitation. That is, one grid cell ($\sim$961 km^2) in the ERA5 reanalysis, six grid cells ($\sim$864 km^2) in the CPS12, and 666 grid cells ($\sim$800 km^2) in the CRS1 were adopted.

320   inversion height is lower at Funchal, possibly due to downslope winds (Durran, 1990) resulting from strong north-easterlies as shown in Fig. 5. Typical vertical temperature profiles from the radiosonde observations and the simulation are given in Fig. C2. The simulated and observed inversion height in this example agrees relatively well but shows the same bias as in Fig. 6a.

The simulation data for Fig. 6a were extracted using the same timestamps as the Funchal radiosonde observations with 98.4% of the observations being conducted at 12:00 UTC. Consequently, we present the diurnal cycle of inversion height in
325   Fig. 6b to examine the representativeness of the data at 12:00 UTC. The model outputs near Funchal show a clear diurnal cycle. The hourly mean inversion height exceeds 1250 m from 12:00 to 17:00 UTC and lies below 1150 m from 21:00 to 08:00 UTC. Such a diurnal cycle can also be observed for each calendar month (not shown). Hence, the observations and simulations near Funchal primarily at 12:00 UTC in Fig. 6a are representative even though the 12:00 UTC data exhibit around 80 m higher inversion height than the daily mean. As the simulated values over ellipse se in Fig. 6b display nearly no diurnal cycle,
330   the simulated values over ellipse se in Fig. 6a are also quite representative. The inversion height estimated with the Tenerife radiosonde observations at 28.32° N and 16.38° W reveals similar monthly patterns and negative biases in simulations as in Fig. 6a, and is generally lower than that at Funchal (not shown).
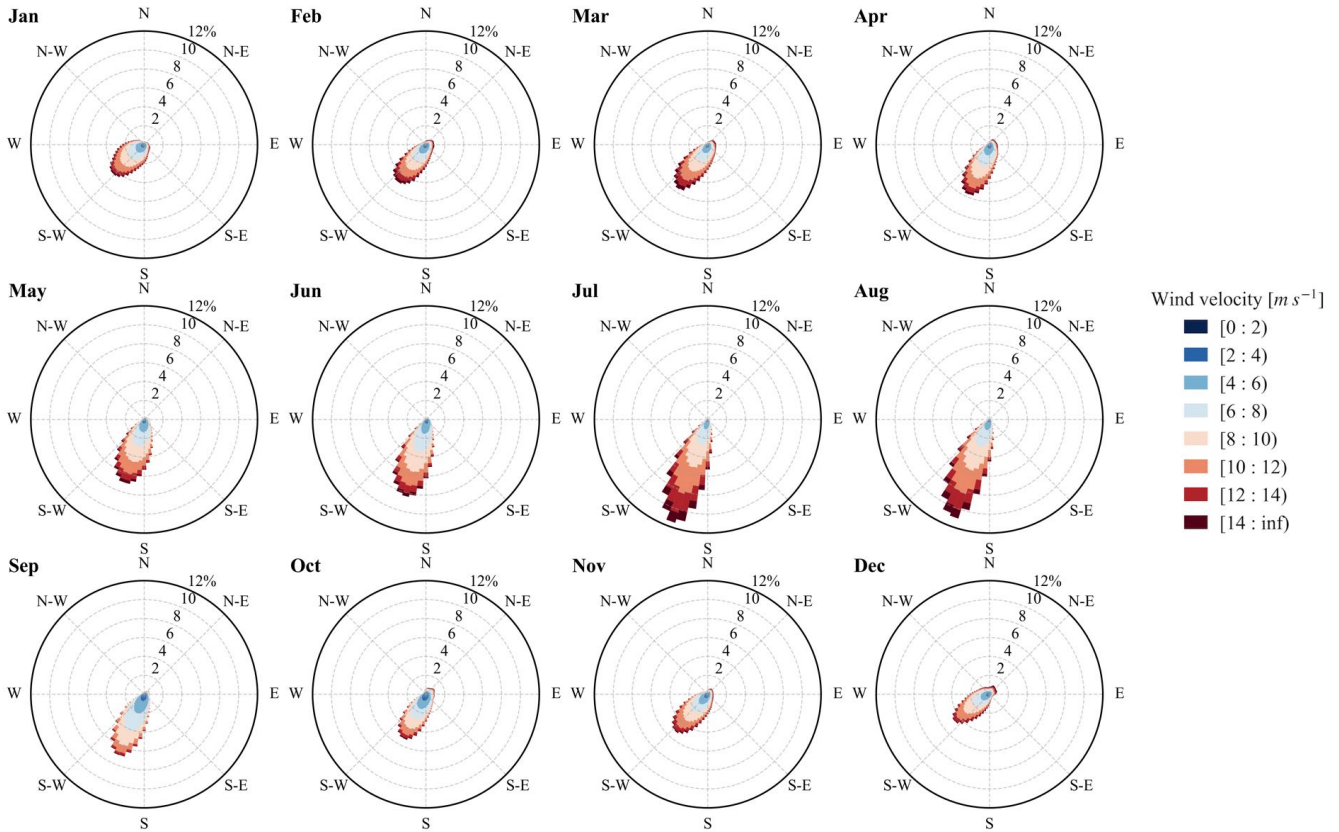
Figure 5. Simulated monthly 100-meter wind climatologies for 2006-2015 in CRS1 over the analysis region defined in Fig. 2a based on hourly data in CRS1. The wind roses can be understood as histograms of wind direction that simultaneously take into account wind velocity varying from 0 to more than 14 m s^{-1}. Each sector with a width of 5° points in the direction of the wind and its radius represents the frequency.

3.2 Case study of 03-09 August 2010

To investigate the characteristics of vortex streets, we selected a vortex shedding event that lasted for about one week from
335 2010-08-03 20:00 UTC to 2010-08-09 07:00 UTC. The animation of simulated 100-meter wind velocity and direction during this period can be found in Supporting Information V1 (Gao et al., 2021). The average upstream wind velocity is around 12 m s^{-1}. We can see that winds are accelerated at the island flanks and decelerated before and behind Madeira Island, which indicates horizontal flow splitting. The corresponding animation of derived 100-meter relative vorticity is shown in Supporting Information V2 (Gao et al., 2021), which acts as a good tracer for vortex streets and shows some variations during this event.
340 Snapshots of this vortex shedding event can be found in Fig. 9 and Fig. 11. In animation V2, lime contours encompass 347 identified vortices using our vortex identification algorithm described in Section 2.4. For this case study, the vortex detection methodology was checked manually. Of all identified vortices, 344 were identified correctly, and three were wrongly identified
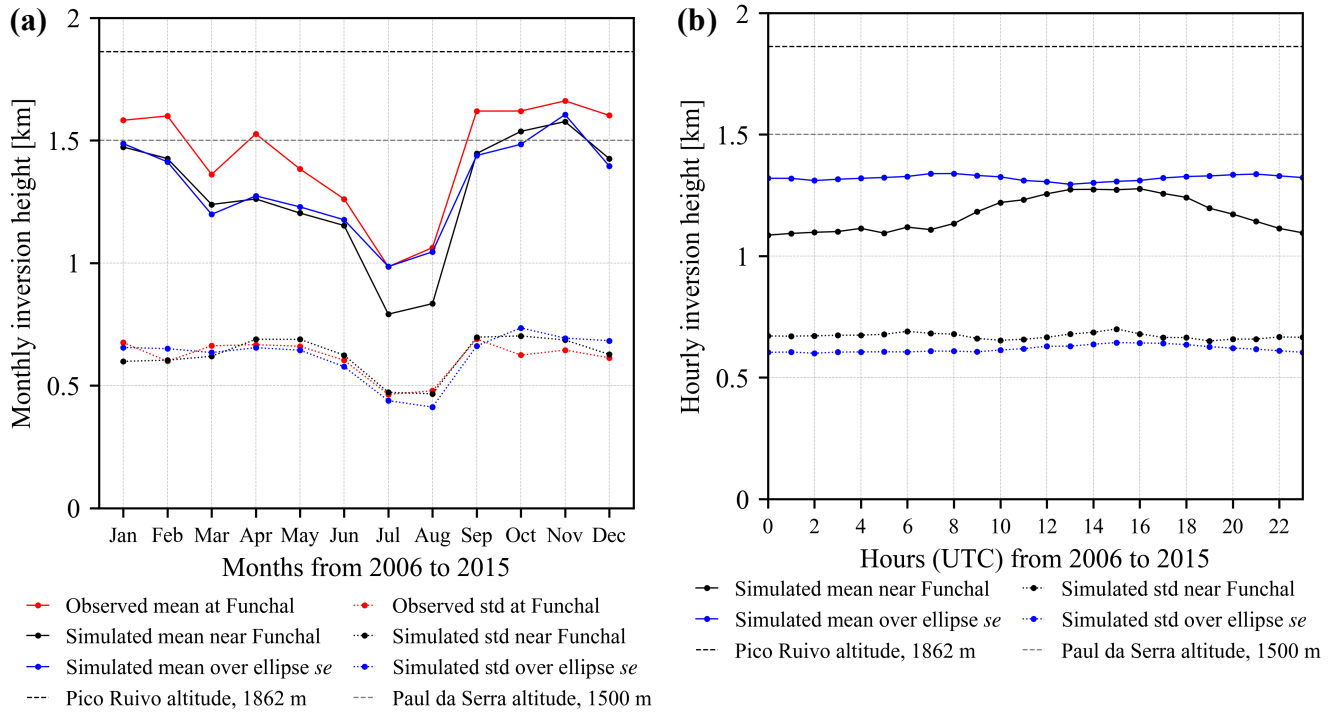
Figure 6. (a) Monthly climatology of inversion height and (b) diurnal cycle of inversion height. Both panels show monthly/hourly means and standard deviations (std). The observed values were calculated from the Funchal radiosonde data from IGRA2, and the simulated values near Funchal were calculated based on the model simulation CRS1 at the grid point closest to the Funchal radiosonde station. The simulated values over *se* were used to represent upstream conditions where decadal 3D model outputs are available. The altitude of two mountain peaks, Pico Ruivo (1862 m) and Paul da Serra (1500 m) at Madeira Island, are indicated for reference.

and highlighted in cyan in animation V2. This corresponds to a false-positivity rate (FPR) (Yang et al., 2020) of 0.9% and one falsely identified vortex every 44 hours. Occasionally, stratocumulus clouds can also serve as tracers for vortex streets, so we ~~visualized~~ visualised cloud patterns during this period in Supporting Information V3 (Gao et al., 2021) using the ~~high rate~~ high-rate SEVIRI rectified image data of the Meteosat-9 in MSG from EUMETSAT (Schmetz et al., 2002). Although cloud patterns are not as indicative as relative vorticity for the detection of vortex streets, we can still observe a ~~well-organized~~ well-organised vortex shedding event in animation V3 that agrees well with the simulations.

Figure 7 demonstrates time series of local flow conditions around Madeira Island during this period. The uppermost array of arrows represents the mean 100-meter wind direction and velocity ~~within~~ averaged over ellipse e_3 in Fig. 2a, which can be assumed as undisturbed flow conditions. Wind velocity in e_3 generally exceeds $10 \, \mathrm{m \, s^{-1}}$ with only slightly varying wind direction. Winds over e_2 are much weaker and significantly dispersed, so we used undisturbed flow conditions from e_3 for subsequent analysis. The green line in Fig. 7 shows the number of correctly identified vortices ~~shedded~~ shed from Madeira Island, which shows large variations during this period. The dimensionless mountain height h_{dim} ~~within~~ averaged over e_3
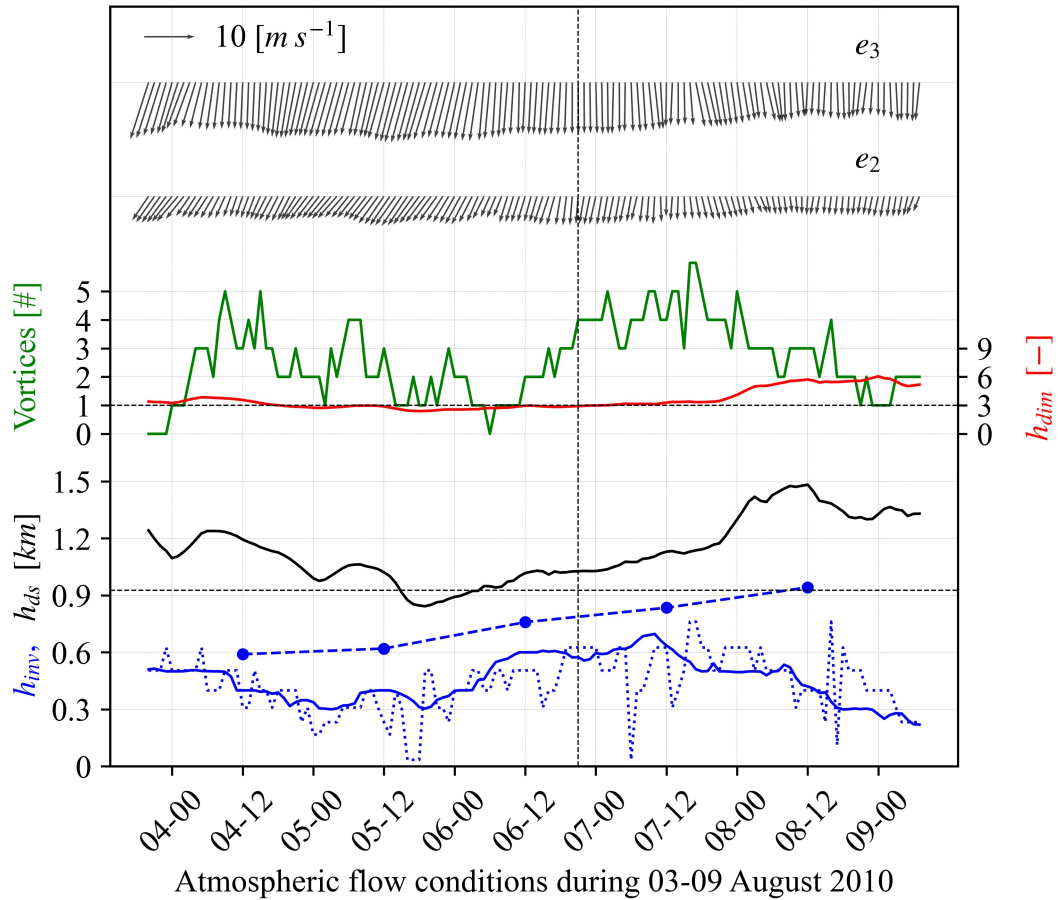
Figure 7. Local flow conditions during the case study period (from 2010-08-03 20:00 UTC to 2010-08-09 07:00 UTC). The top two rows of arrows represent average wind arrows over ellipses e_3 and e_2, and a wind velocity of 10 m s^{-1} is shown for reference. The third row shows the number of identified vortices ~~shedded from Madeira~~ (green line), and the average dimensionless mountain height h_{dim} over e_3 (red line). The dividing streamline height h_{ds} over e_3 are shown in the black line. The solid blue line represents the inversion height h_{inv} over e_3, and dashed and dotted blue lines show h_{inv} in Funchal radiosonde observations and CRS1 in a grid cell closest to the Funchal radiosonde station, respectively. A selected timestamp 2010-08-06 21:00 UTC for subsequent analysis is indicated by a vertical dashed black line.

355 shown in the red line is generally above 3, a value that Schär and Durran (1997) used to specify flow conditions ~~favorable~~ favourable for vortex shedding. The dividing streamline height h_{ds} mostly exceeds 60% of the peak mountain height in CRS1 ($\sim$0.93 km denoted with a dotted black line), which is a widely used threshold to distinguish flow conditions conducive for vortex shedding. The weak vortex shedding signals at the middle of this period seems to coincide with stages where h_{ds} and h_{dim} fall below the corresponding thresholds. ~~In addition, a sudden increase of the inversion base over e_3 in the solid blue~~

360 ~~line at 2010-08-06 05:00 UTC also precedes the increasing vortex shedding signal.~~ The comparison of inversion height from Funchal radiosonde observations at 12:00 UTC and a grid cell in CRS1 closest to Funchal radiosonde station in the dashed and
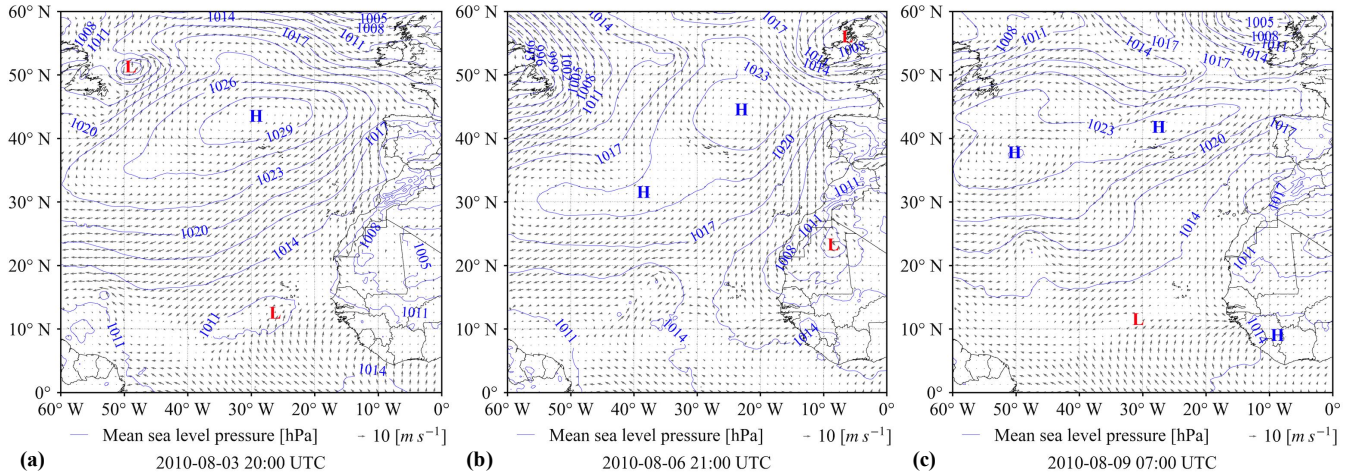
Figure 8. Synoptic flow conditions including mean sea level pressure and 10-meter winds from the ERA5 reanalysis at the (a) starting, (b) middle, and (c) ending time of the case study period. A wind velocity of 10 m s^{-1} is shown for reference. H (L) represents high (low) pressure systems. The geographic map is from the Natural Earth.

dotted blue lines shows expected patterns as described in Section 3.1: negative bias and vulnerability to perturbations in lower levels in the simulations.

Synoptic flow conditions including mean sea-level pressure and 10-meter winds from the ERA5 reanalysis during this period are shown in Fig. 8. At the beginning of this period, a high-pressure system ~~centered~~ centred north of the Azores resulted in a strong north-easterly flow, especially over the northwest of our study domain. Subsequently, the high-pressure system moved northeast and deformed towards a circle, which ~~led to a stronger north-easterly flow that stimulated well-organized~~ was associated with well-organised vortex streets in the lee of Madeira Island, whose major axis is approximately perpendicular to the mesoscale wind direction. At the end of this event, the vortex shedding phenomenon weakened with the ~~vanishment~~ weakening of the high-pressure system. Consequently, we can identify a clear correlation between vortex shedding in the lee of Madeira Island and the high-pressure system, which is well known as the semipermanent Azores high (Davis et al., 1997) and forms one pole of the North Atlantic Oscillation (NAO) (Visbeck et al., 2001).

We manually tracked four positive vortices ~~labeled~~ labelled as P1 to P4 and four negative vortices (N1-N4) starting from the selected timestamp. Tracks of P1 and N1 are shown in Fig. 9 and the animation of their propagation can be found in Supporting Information V4 (Gao et al., 2021). Based on the eight vortices, we calculated several key numbers to compare with existing literature and satellite images. The ratio of advection velocity of vortices to undisturbed wind velocity over e_3 has a mean of 0.82 and a standard deviation of 0.02, while existing literature reported a large range of values like 0.76 in Tsuchiya (1969) or 0.90 ± 0.37 in Heinze et al. (2012). The average shedding interval of like-rotating vortices is about 6.7 hours, and a rough estimation based on satellite images in this period gives a value of around 7 hours. The corresponding Strouhal number has a mean of 0.154 and varies from 0.142 to 0.166, which also lies in or close to the reported range from Nunalee and Basu (2014)
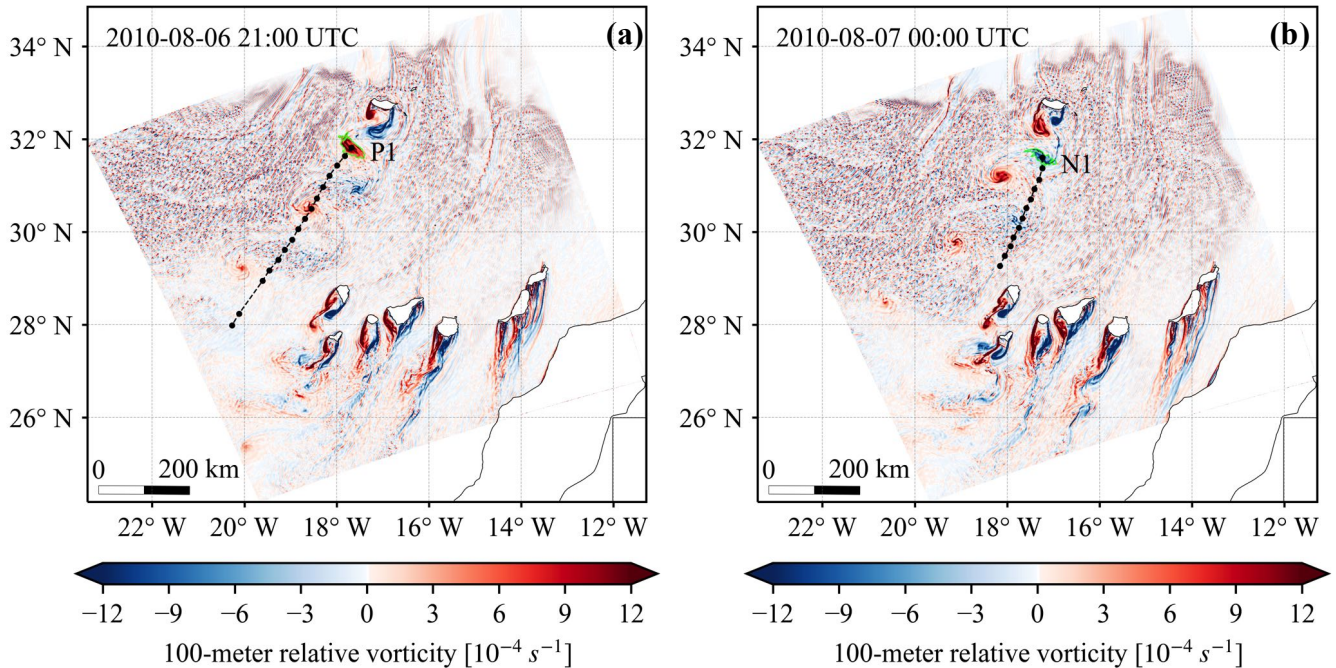
Figure 9. Relative vorticity at 100 m and tracks of (a) a positive vortex P1 ~~shedded~~ shed at 2010-08-06 21:00 UTC and (b) a negative vortex N1 ~~shedded~~ shed at 2010-08-07 00:00 UTC. The relevant vortices are encompassed by lime contours, and the tracks in the next hours are shown with black lines and dots on an hourly basis. A gap in the lower half of the track of P1 results from a false rejection of that vortex by our algorithm. The geographic map is from the Natural Earth.

between 0.15 and 0.22. Figure 10 presents the size of eight tracked vortices from 100 km^2 to 1600 km^2 against their distance to Madeira ~~center~~ centre up to 600 km. We can see a faster decay of negative vortices, which might be attributed to the Coriolis force, as the Rossby number defined in Eq. (5) has a value of around 4 considering a relevant length scale of $L = 35 \text{ km}$, a flow velocity of $u = 10 \text{ m s}^{-1}$, and a latitude of $\phi = 32 \deg$.

385   For the decade-long simulations, only a reduced set of output fields was stored. To investigate the simulated vortex streets in detail, we restarted the model simulation on 2010-08-01 00:00 UTC for the case study period to generate variables every 100 m in the lowest 5 km above the surface. Figure 11 shows the 100-meter relative vorticity, 10-meter potential temperature, and 100-meter specific humidity at the selected timestamp in the new model simulation. Small differences can be found between Fig. 11a and Fig. 9a due to stochastic properties of simulations. We can identify positive potential temperature anomalies at

390   10 m altitude as mentioned in Section 2.4 and positive specific humidity anomalies around both positive and negative vortices. Both kinds of anomalies were observed in the wake of Hawaii (Smith and Grubišić, 1993). The potential temperature anomalies result mainly from temperature anomalies and could be used as a tracer for vortex streets in ~~idealized~~ idealised simulations (Heinze et al., 2012).
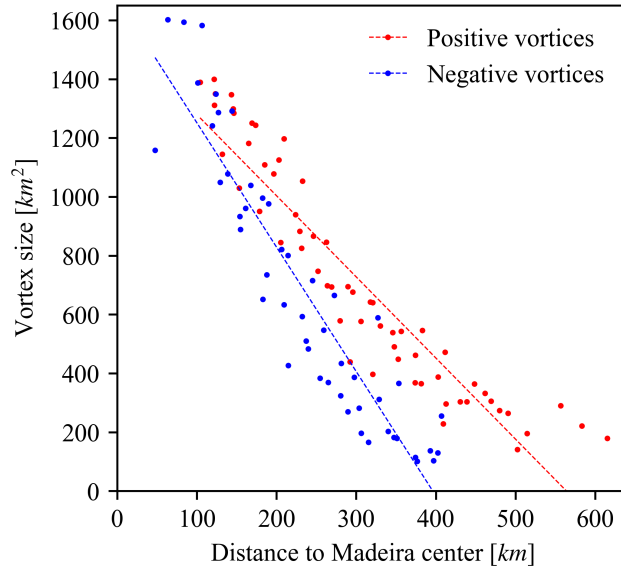
Figure 10. The size of four positive and four negative tracked vortices (see Supporting Information V4, Gao et al., 2021) against their distance to Madeira ~~center~~centre. Two dashed lines are fitted to the scatter plots to show different decaying rates of positive and negative vortices.
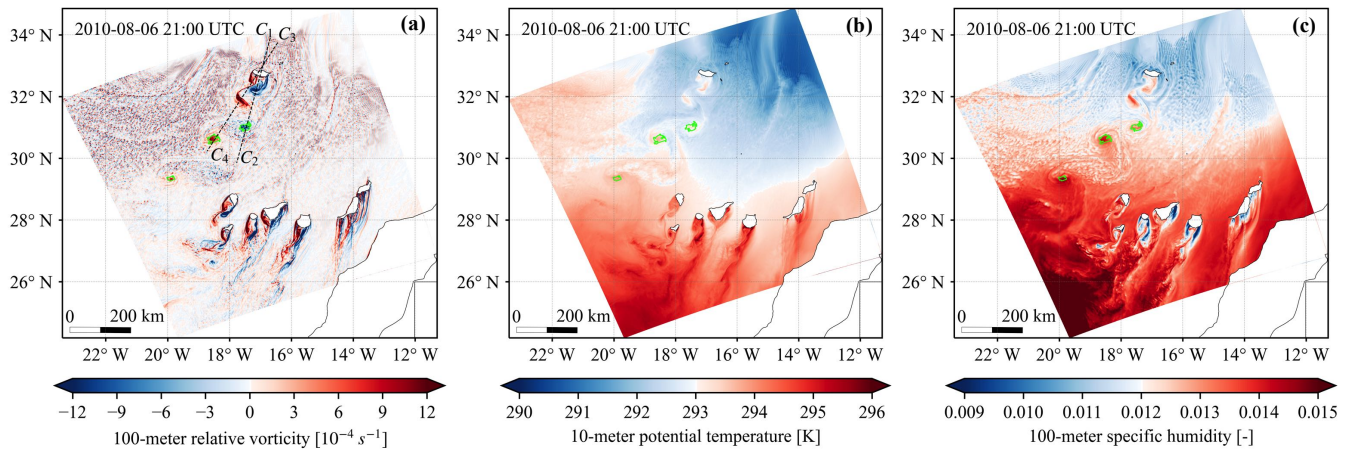
Figure 11. (a) 100-meter relative vorticity, (b) 10-meter potential temperature, and (c) 100-meter specific humidity at 2010-08-06 21:00 UTC. The vertical structures of the vortices were investigated along two cross-sections (C_1-C_2 and C_3-C_4) shown in (a). The identified vortices are encompassed by lime contours. The geographic map is from the Natural Earth.

The vertical structures of vortex streets along two cross-sections C_1-C_2 and C_3-C_4 depicted in Fig. 11a are shown in Fig. 12. The two cross-sections show similar signals. From Fig. 12a we can observe a well-mixed upstream boundary layer, gravity waves above the island, distorted downstream isentropes, a lowering of the downstream capping inversion, and six downstream
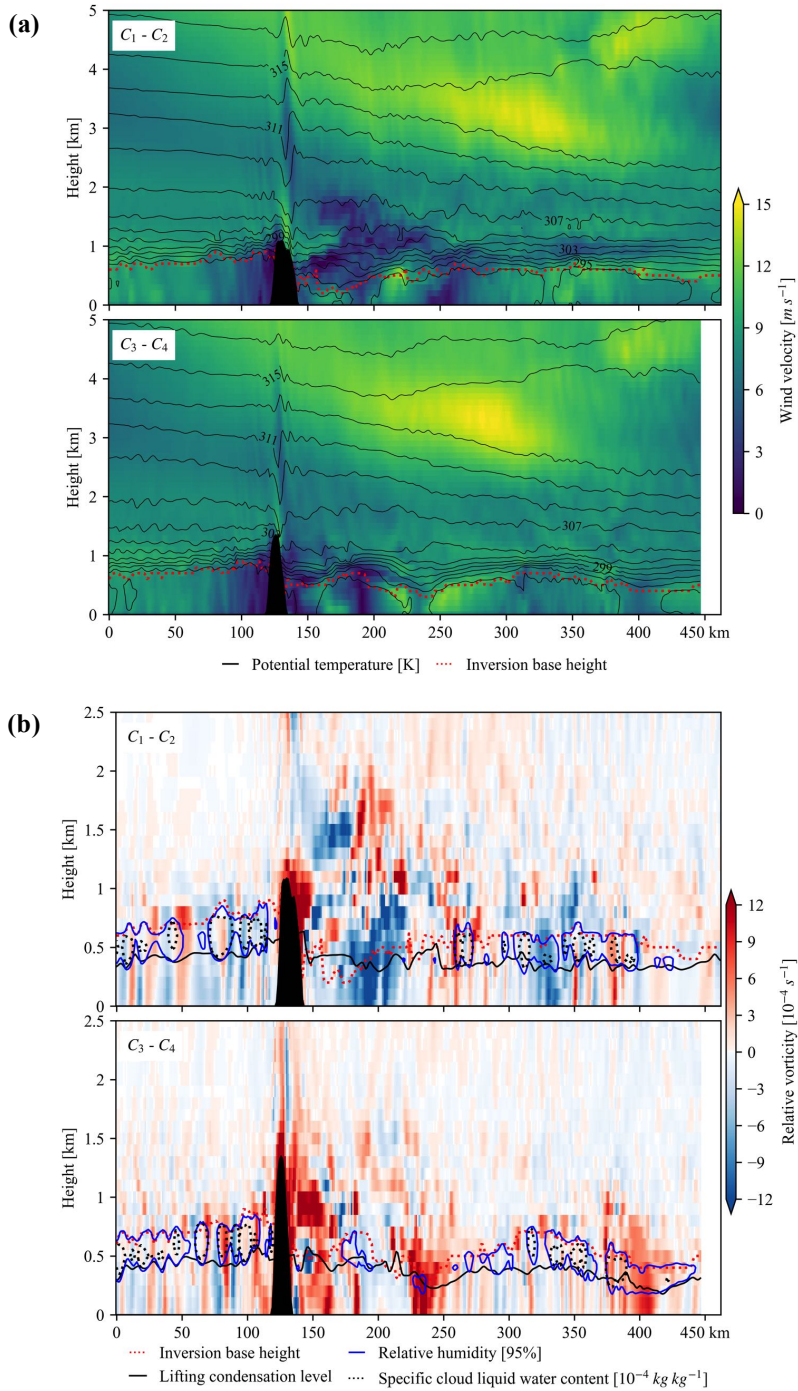
Figure 12. Vertical structure of (a) wind velocity, potential temperature, inversion base height, and (b) relative vorticity, relative humidity, lifting condensation level, and specific cloud liquid water content along two cross-sections C_1-C_2 and C_3-C_4 shown in Fig. 11a at 2010-08-06 21:00 UTC.
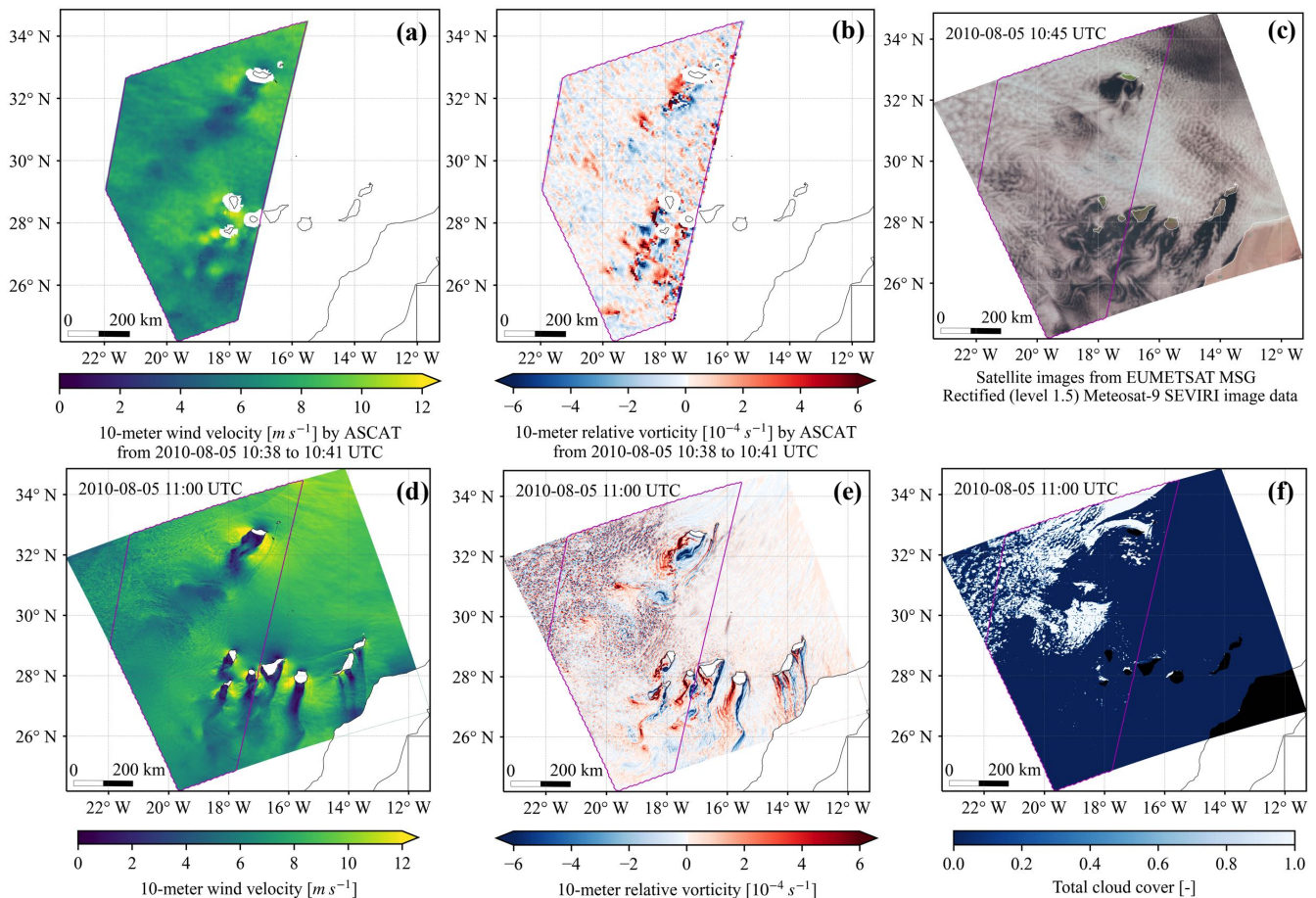
Figure 13. Comparison of satellite data (top row) versus simulation data (bottom row): (a) 10-meter winds and (b) the derived relative vorticity at a horizontal resolution of 6.25 km measured by ASCAT onboard Metop-A from EUMETSAT. The magenta polygons indicate the area with available ASCAT data over the analysis region. (c) Satellite image constructed with data observed by MSG Meteosat-9 from EUMETSAT. The NIR1.6, VIS0.8, and VIS0.6 channel data were used to represent red, green, and blue. The second row shows (d) 10-meter winds, (e) the derived relative vorticity, and (f) total cloud cover in CRS1 at a time point (2010-08-05 11:00 UTC) close to that of observations. The geographic map is from the Natural Earth.

positive potential temperature anomalies extending from the surface to the inversion height. The last potential temperature anomaly from C_1 to C_2 has no corresponding vortex, which indicates that vortex streets can still impact the atmosphere further downstream even though the vortices already dissipated. The lifting condensation level (LCL) is the height where an air parcel would saturate when lifted adiabatically. Although the LCL is estimated based on surface data (Romps, 2017), it well captures the lower bounds of contours of 95% relative humidity. The cloud-free region in the lee of Madeira Island in the animation V3 in Supporting Information (Gao et al., 2021) can be explained by the lowering of the inversion base below the LCL and can result in intense solar radiation and thus a warm oceanic wake (Azevedo et al., 2020). In satellite images, we could sometimes observe cloud-free conditions (eyes) in the ~~center of shedded~~ centre of shed vortices. The lower inversion base than LCL was assumed to be responsible for cloud-free eyes of vortices (Heinze et al., 2012), but this is not supported by our simulation as the inversion base is higher than LCL at downstream vortices.

It is still difficult to validate the track and timing of individual vortices in realistic simulations because of limited observations. During our case study period, vortex streets in the lee of Madeira Island were captured in only three snapshots by ASCAT onboard the MetOp-A satellite, of which the clearest one at around 2010-08-05 10:40 UTC ~~are~~ is shown in Fig. 13a-b. The 10-meter relative vorticity derived from the observed wind vectors shows distinct vortex shedding signals which coincide with cloud patterns observed by Meteosat-9 in Fig. 13c. The corresponding model outputs at 2010-08-05 11:00 UTC in Fig. 13d-e also show obvious vortex streets in the lee of Madeira Island, which agrees well with the observations. Note also that we cannot expect a perfect spatial fit as vortex shedding is a chaotic phenomenon and the timing in a long simulation such as ours. The simulated cloud patterns in Fig. 13f do not agree with the observations and it looks like the model has difficulties in the simulation of clouds for this specific situation. This is not uncommon, as the simulation of clouds is still a big challenge even in high-resolution weather and climate models (Bretherton, 2015), and the dynamics of stratocumulus clouds are particularly hard to resolve (Schneider et al., 2019).

For further justification of our vortex identification algorithm, relevant vortex statistics are presented in Appendix B.

3.3 Climatology of Madeira vortex streets

In this section, we present the decadal analysis of vortex streets in the lee of Madeira Island. For the case study in Section 3.2, we required the ~~center of vortices shedded~~ centre of vortices shed from Madeira Island to be within the black dashed polygon in Fig. 14, to incorporate as many vortices as possible. For the decadal analysis, we chose a smaller domain, shown by the red polygon in Fig. 14, ~~in order to reduce the number of vortices shedded~~ to exclude vortices shed from the La Palma island in the Canary Archipelago. The vortex count shown in Fig. 14 shows a strongly increased frequency to the southwest of Madeira island, which corresponds to the lee during trade wind conditions.

Figure 15a shows the daily vortex count during 2010 and the 10-day moving average. As the parameters of our algorithm were tuned based on data from February and August 2010, we validated it using data from November 2010 against a manual analysis of the simulated vorticity field. During this month, there are 199 identified vortices and 171 correctly identified vortices, which correspond to a false positive rate (FPR) of 14% and one falsely identified vortex every 26 hours. Although this FPR does not ~~reveal as good~~ suggest as good a performance as 0.9% in the case study in Section 3.2, the second index
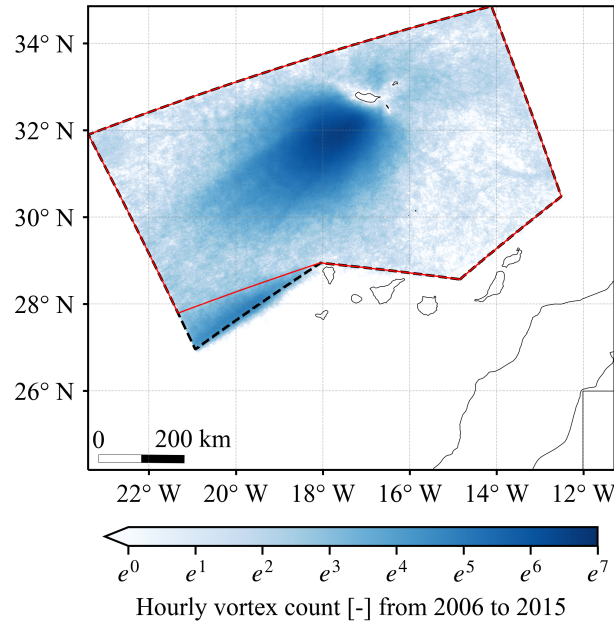
Figure 14. Hourly vortex count at each grid cell in CRS1 from 2006 to 2015 (totally 87,648 hours, $e^7 \approx 1097$). It shows the results when we used the dashed black polygon to restrict the region where the ~~center~~ centre of vortices ~~shedded~~ shed from Madeira Island can appear as described in Section 2.4. For each grid cell at each hour, we counted the vortex number as one if an identified vortex covers this grid cell. The exponential scale was used to account for the unevenly distributed frequency in vortices. The geographic map is from the Natural Earth.

1/(26 h) still provides confidence in our algorithm. Figure 15b shows the monthly vortex count from 2006 to 2015, and the corresponding boxplots are shown in Fig. 16, where several interesting phenomena can be observed. While Fig. 16a shows distinct ~~interannual~~ inter-annual variations, Fig. 16b indicates a large monthly discrepancy. An increasing vortex shedding rate can be observed from April to August in Fig. 16b, as the wind direction is increasingly concentrated and the mean wind speed is increased Fig. 5 and the inversion height decreases from around 1.5 to 1 km in Fig. 6a. There are large variations and occasionally strong vortex shedding signals in March, which might result from abnormally lower inversion base in Fig. 6a and less precipitation in Fig. 4. Furthermore, we can see a sharp transition from August to September resulting from a sudden deceleration of winds in Fig. 5 and the increase of inversion height in Fig. 6a. This transition is also found in the study of Grubišić et al. (2015) by manually checking satellite images of eight years.

4 Conclusions

This study investigated vortex streets in the lee of Madeira Island during 2006-2015. We used the regional climate model COSMO with a horizontal ~~resolution~~ grid spacing of 1.1 km, driven by the ERA-Interim reanalysis. Firstly, we explored meteorological conditions over our study area using the ERA5 reanalysis, model simulations, and radiosonde observations.
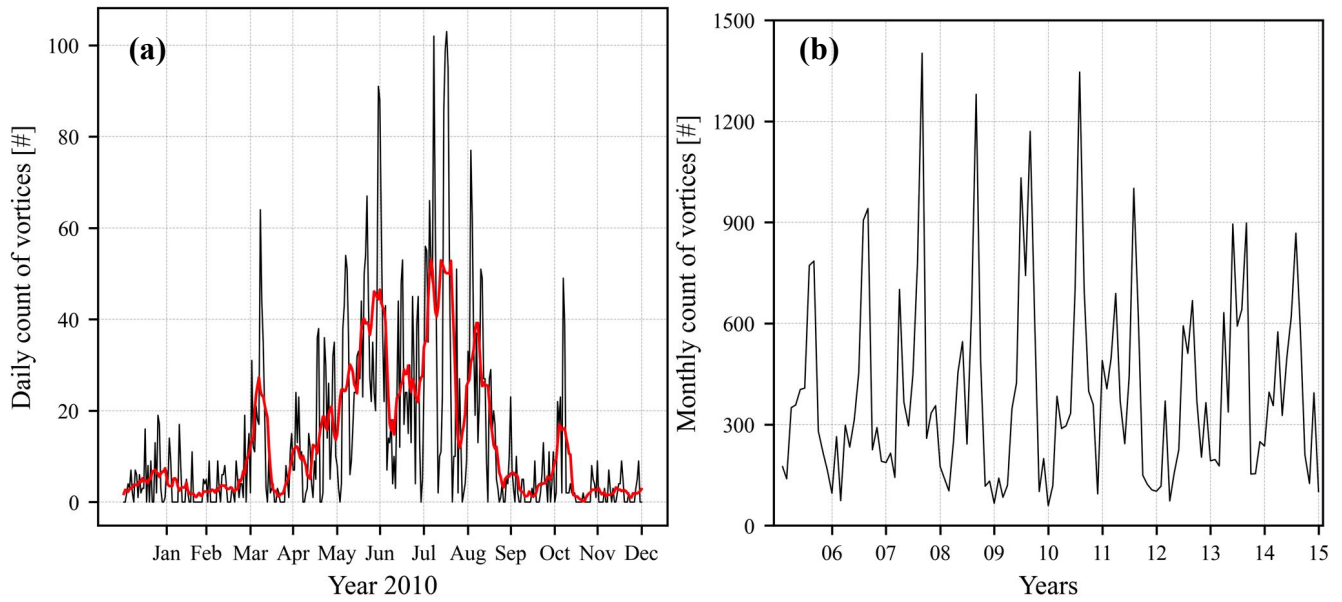
Figure 15. (a) Daily count of identified vortices in CRS1 in 2010 in black and its 10-day moving average in red. (b) Monthly count of identified vortices in CRS1 from 2006 to 2015.
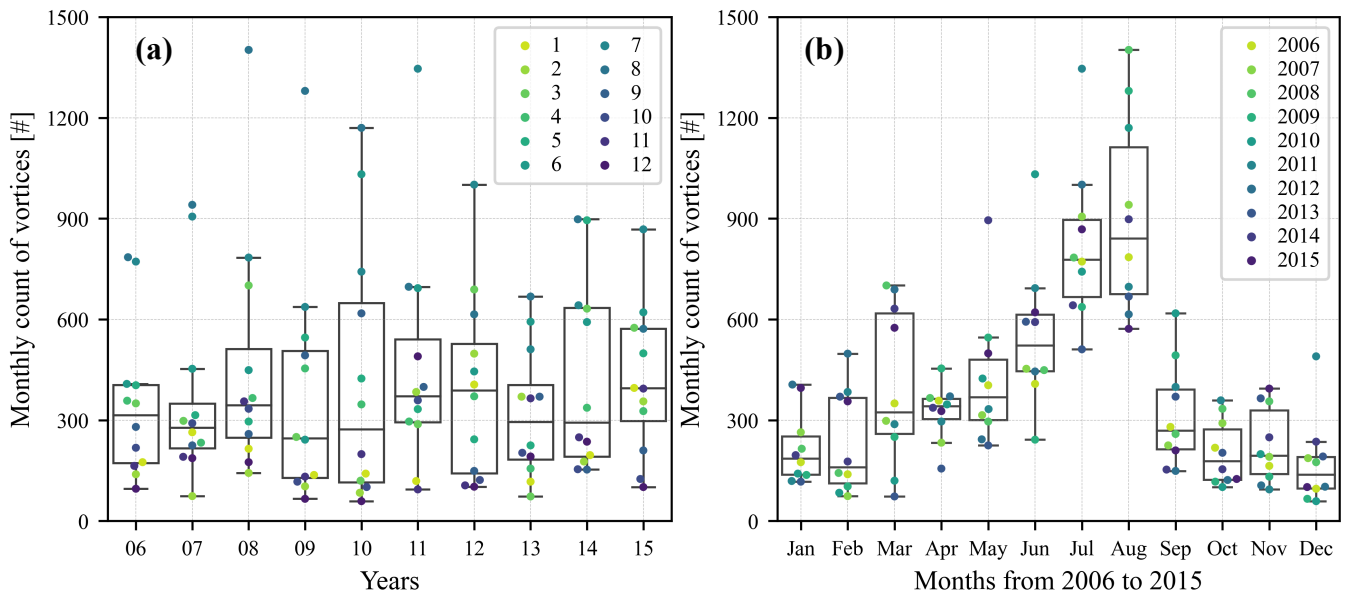
Figure 16. Boxplot of the monthly count of identified vortices in CRS1 from 2006 to 2015 in (a) each year and (b) each month. The boxes show quartiles of the data, and the whiskers extend to values within 1.5 times of the inter-quartile range from the low or high quartiles.

Then we studied the basic properties of vortex streets based on a case study during 03-09 August 2010 and developed a vortex
identification algorithm. This algorithm was subsequently used for the climatological analysis of vortex streets over a 10-year
period.

Although there are some discrepancies between simulated and observed precipitation, the added value of high-resolution
simulations that partly resolves the complex topography and convective processes is rather prominent. In particular, the CRS1
simulation shows more realistic spatial patterns and less negative biases over Madeira Island than the CPS12 simulation with
12 km horizontal ~~resolution~~ grid spacing. The monthly wind conditions over our analysis region can be well simulated and
reveal some interesting phenomena. From April to August, the trade wind speed increases and the direction becomes better
defined. Between August and September, the trades become much weaker again. In addition, the monthly patterns of inversion
height obtained from radiosonde observations at Funchal are also well captured in CRS1. From April to August the inversion
height decreases from 1.5 to 1 km, whereas it increases abruptly to above 1.6 km in September. Such monthly patterns of
winds and inversion height can be explained by the migration of the Hadley cell (Carrillo et al., 2016) and associated shifts of
the Azores high.

A vortex shedding event behind Madeira Island during 03-09 August 2010 observed by Meteosat-9 of EUMETSAT is well
captured by CRS1. This event was chosen as a case study to investigate and validate the basic properties of vortex streets
in realistic simulations. During this period, both synoptic and local atmospheric conditions were found to be conducive ~~for~~
to vortex shedding. The synoptic flow conditions from the ERA5 reanalysis reveal a direct dependence of vortex shedding
in the lee of Madeira Island on the location, shape, and magnitude of the Azores high. The upstream undisturbed 100-meter
winds have a velocity over $10 \mathrm{~m~s^{-1}}$ and show small spatial and temporal variations. In addition, both the dimensionless
mountain height and the dividing streamline height satisfy widely studied requirements for flow splitting and vortex shedding.
Overall, the numerical model indicates good performance in realistically simulating vortex shedding in this region and reveals
interesting properties of vortex streets. Firstly, the ratio of advection velocity of vortices to undisturbed wind velocity over
e_3 was estimated to be around 0.82 and the Strouhal number varies between 0.142 and 0.166, both values lying well within
reported ranges in literature. It is found that the negative vortices show faster decay rates than positive vortices. A potentially
attractive explanation is related to the role of the Coriolis force, which sharpens positive (cyclonic) vortices and ~~widens~~ weakens
negative (anticyclonic) ones. The investigation of structures of vortex streets in realistic atmospheric simulations brought us
several new insights. Although positive potential temperature and specific humidity anomalies around vortices are well known
for many vortex streets, the fact that they can propagate further downstream than the dynamical (vorticity) contribution of
the vortices has not yet been widely noticed. Finally, the lowering of the capping inversion below the LCL is responsible for
cloud-free regions in the lee of Madeira Island.

Based on the case study, we developed a rule-based vortex identification algorithm. The algorithm was manually validated
and shows a good performance with few wrong identifications. This algorithm enabled us to draw a 10-year climatology of
vortex shedding to the lee of Madeira. Monthly patterns of the number of identified vortices ~~shedded~~ shed from Madeira
Island are consistent with that of winds over our analysis region and the inversion height observed at Funchal. These patterns
are mainly governed by the annual cycle of the trades, Hadley circulation, and the Azores high. From April to August, the

vortex shedding rate is increasing. This is driven by a strengthening of the trade winds and a lowering of the inversion height. Thereafter, the sudden weakening of the trade winds and an increase in inversion height in September lead to a pronounced and sharp drop in vortex shedding frequency, confirming the results of Grubišić et al. (2015) obtained from satellite images for eight years.

Lastly, we point out some limitations in our work and make several suggestions for future studies. Although the islands in the Canary Archipelago, especially La Palma and El Hierro, also show very nice vortex shedding signals, we do not consider multiple islands in one paper for simplicity and feasibility. While we used the six-hourly ERA-Interim reanalysis as initial and boundary conditions for CPS12, the employment of the ERA5 reanalysis with higher spatial and temporal resolution might improve the simulation of vortex streets. Although our work involved only 2D vortex identification, our algorithms can be extended for 3D vortex identification. The 3D vortex ~~visualization~~visualisation, automatic vortex tracking, and vortex identification using deep learning could also be considered in further works. The kinematic vorticity number could also be considered for vortex identification in future work (Schielicke et al., 2016). Finally, we noted some considerable challenges such as limitations in the simulation of the cloud cover in particular in areas of stratocumulus. Nevertheless, we believe that our model-based generation of a vortex-shedding climatology is overall ~~succeful and of considerable interest~~successful.

Code and data availability. The ERA5 reanalysis can be obtained from the Climate Data Store (https://cds.climate.copernicus.eu). The ASCAT and MSG data are provided by EUMETSAT (https://navigator.eumetsat.int), and the ASCAT Wind Data Processor (AWDP) is available from the OSI SAF (https://nwp-saf.eumetsat.int). The radiosonde observations are from IGRA 2 (https://www.ncei.noaa.gov). The observational station data are provided by Portuguese Institute of the Sea and the Atmosphere and by Portuguese Environment Agency and it is available upon request. The MODIS satellite data are from the NASA website (https://ladsweb.modaps.eosdis.nasa.gov). The digital elevation model of Madeira Archipelago can be obtained from the European Environment Agency (https://sdi.eea.europa.eu). The maps in the figures are from the Natural Earth (https://www.naturalearthdata.com/) and the GADM (https://gadm.org/). The model simulations are available from the authors upon request. The code for analysis can be found in this GitHub repository: https://github.com/l975421700/DEoAI_analysis. The source code for generic cell identification that has been used for the first step of the rule-based vortex identification is available under https://doi.org/10.5281/zenodo.7506042.

Video supplement. The Supporting Information (four videos) can be found at *Supporting Information: Vortex streets to the lee of Madeira in a km-resolution regional climate model* (https://doi.org/10.5281/zenodo.4462118).

Appendix A: The wavelet analysis for denoising

Abramovich et al. (2000) focused on statistical applications of the wavelet analysis and could serve as a good start point for statisticians. All wavelets in the basis are derived from two mutually orthonormal parent wavelets through translations of the scaling function ϕ and dilations and translations of the mother wavelet ψ as

$$\phi_{j_0k}(t) = 2^{j_0/2}\phi(2^{j_0}t - k),\tag{A1}$$

$$\psi_{jk}(t) = 2^{j/2}\psi(2^{j}t - k),\tag{A2}$$

where $j_0 \in Z$ is fixed, Z is the set of integers, $k \in Z$, and $j = j_0, j_0 + 1, j_0 + 2, ...$

Intuitively we can regard ϕ as a kernel function and ψ as a ~~localized~~ localised oscillation, where a unit increase of j in Eq. (A2) doubles the frequency or resolution of $\psi_{jk}(t)$. A unit increase of k shifts the location of $\phi_{j_0k}(t)$ by 2^{-j_0} and $\psi_{jk}(t)$ by 2^{-j}.

Given a wavelet basis and assuming a signal to be infinite, *g(t)* can be represented through a wavelet series as

$$\boldsymbol{g}(t) = \sum_{k\in Z} c_{j_0k}\phi_{j_0k}(t) + \sum_{j=j_0}^{\infty}\sum_{k\in Z} w_{jk}\psi_{jk}(t),\tag{A3}$$

where $c_{j_0k} = \int_R \boldsymbol{g}(t)\phi_{j_0k}(t)dt$ and $w_{jk} = \int_R \boldsymbol{g}(t)\psi_{jk}(t)dt$.

Considering ~~discretly~~ discretely sampled signals $\boldsymbol{g} = (g(t_1), g(t_2), ..., g(t_n))^T$ (assume $n = 2^J$ where J is a positive integer) at a constant interval, the DWT needs to be considered as

$$\boldsymbol{d} = \mathbf{W}\boldsymbol{g},\tag{A4}$$

where $\mathbf{W}$ is an $n \times n$ orthogonal matrix associated with selected wavelets, and $\boldsymbol{d}$ is an $n \times 1$ vector comprising discrete scaling coefficients u_{j_0k} ($\approx c_{j_0k} \times \sqrt{n}$, $k = 0, 1, ..., 2^{j_0} - 1$) and discrete wavelet coefficients d_{jk} ($\approx w_{jk} \times \sqrt{n}$, $j = j_0, j_0 + 1, ..., J - 1$, $k = 0, 1, ..., 2^j - 1$).

The inverse DWT can be obtained based on the orthogonality of $\mathbf{W}$ as $\boldsymbol{g} = \mathbf{W}^T\boldsymbol{d}$ and used to denoise through reserving only a part of the largest values in $\boldsymbol{d}$ (Wickerhauser, 1996; Ruppert-Felsot et al., 2005), where coefficients above (below) a threshold are assumed to correspond to signals (~~noises~~noise). The choice of the threshold depends on a measure of the number of significant coefficients N_0 defined as

$$N_0(\boldsymbol{g}) = e^{H(\boldsymbol{g})},\tag{A5}$$

where $H(\boldsymbol{g})$ is the entropy of $\boldsymbol{g}$ and defined as

$$H(\boldsymbol{g}) = -\sum_{i=1}^{n}\boldsymbol{p}_i\ln\boldsymbol{p}_i,\tag{A6}$$

where $\boldsymbol{p}_i = |\boldsymbol{g}_i|^2 / ||\boldsymbol{g}||^2$ and $||\boldsymbol{g}||^2 = \sum_i |\boldsymbol{g}_i|^2$.

As for the selection of parent wavelets, the function support (compact or infinite), orthogonality, smoothness (i.e. regularity or the number of continuous derivatives), and the number of vanishing moments should be considered. Wang et al. (2018) gives a good ~~visualized~~ visualised introduction to wavelet families, while some recommendations and requirements about their selection can be found in Domingues et al. (2005) and Jawerth and Sweldens (1994). The Haar basis is the oldest and simplest wavelet basis for $\boldsymbol{g(t)}$. Albeit the Haar basis does not have a good time-frequency ~~localization~~ localisation, and the resulting wavelets are discontinuous and thus unsuitable for smooth functions, its performance was equivalent to other wavelets in our preliminary analysis, as also reported by Siegel and Weiss (1997). Therefore, it is selected for our further analysis for simplicity. In real cases, signals are normally zero outside a finite interval. As simply setting the signals to be zero outside the finite interval results in discontinuities at boundaries, periodic boundary handling is adopted as a solution.

Appendix B: Identified vortex statistics

In Fig. B1, we ~~displayed~~ display several properties of extracted vortices using the first two steps of our vortex identification algorithm, identified vortices through subsequent criteria, and three falsely identified vortices during the case study period. Figure B1a shows that the mean relative vorticity of identified vortices distributes well above the threshold 3×10^{-4} s^{-1} selected to identify candidate grids. Some extracted vortices have mean relative vorticity below the selected threshold. Two reasons can explain this phenomenon: These vortices have a mean size of 4 km^2 and thus are vulnerable to ~~noises~~ noise; The wavelet transform could increase the relative vorticity above the threshold, whereas we extract the vortex characteristics based on the original data. We can see a sharp edge of the size of identified vortices at the threshold of 100 km^2, which indicates some falsely rejected small vortices. However, we expect those small vortices to have less relevance and accept the threshold to eliminate a large number of noisy structures. Figure B1c-e reveals significant discrepancies between statistics of identified vortices and the thresholds in our algorithm. This is a great signal that indicates our algorithm consists of loose criteria and does not implicitly determine these vortex characteristics.

Appendix C: Extra figures

Fig. C1a presents annual mean precipitation over our analysis region in the ERA5 reanalysis from 2006 to 2015. It ranges from 43 to 564 mm with increasing amounts from the southeast to the northwest. Wetter conditions can be observed near the islands as an effect of orographic lifting. Although Fig. C1a-c indicate negative biases of simulated precipitation in comparison to the ERA5 reanalysis over the ocean, especially in CRS1, the above-mentioned spatial patterns are well simulated in both CPS12 and CRS1. Fig. C1d-f display precipitation over Madeira Archipelago in a zoomed-in version. The horizontal grid spacing of the ERA5 reanalysis (0.25°) and CPS12 (12 km) are insufficient to resolve the topography. Indeed, maximum elevation over Madeira amounts to around 1862 m in reality, 1546 m in CRS1, 600 m in CPS12, and 330 m in ERA5. As a result, the lifting and splitting of the ambient flow cannot properly be represented in ERA5 and CPS12, yielding too small precipitation amounts
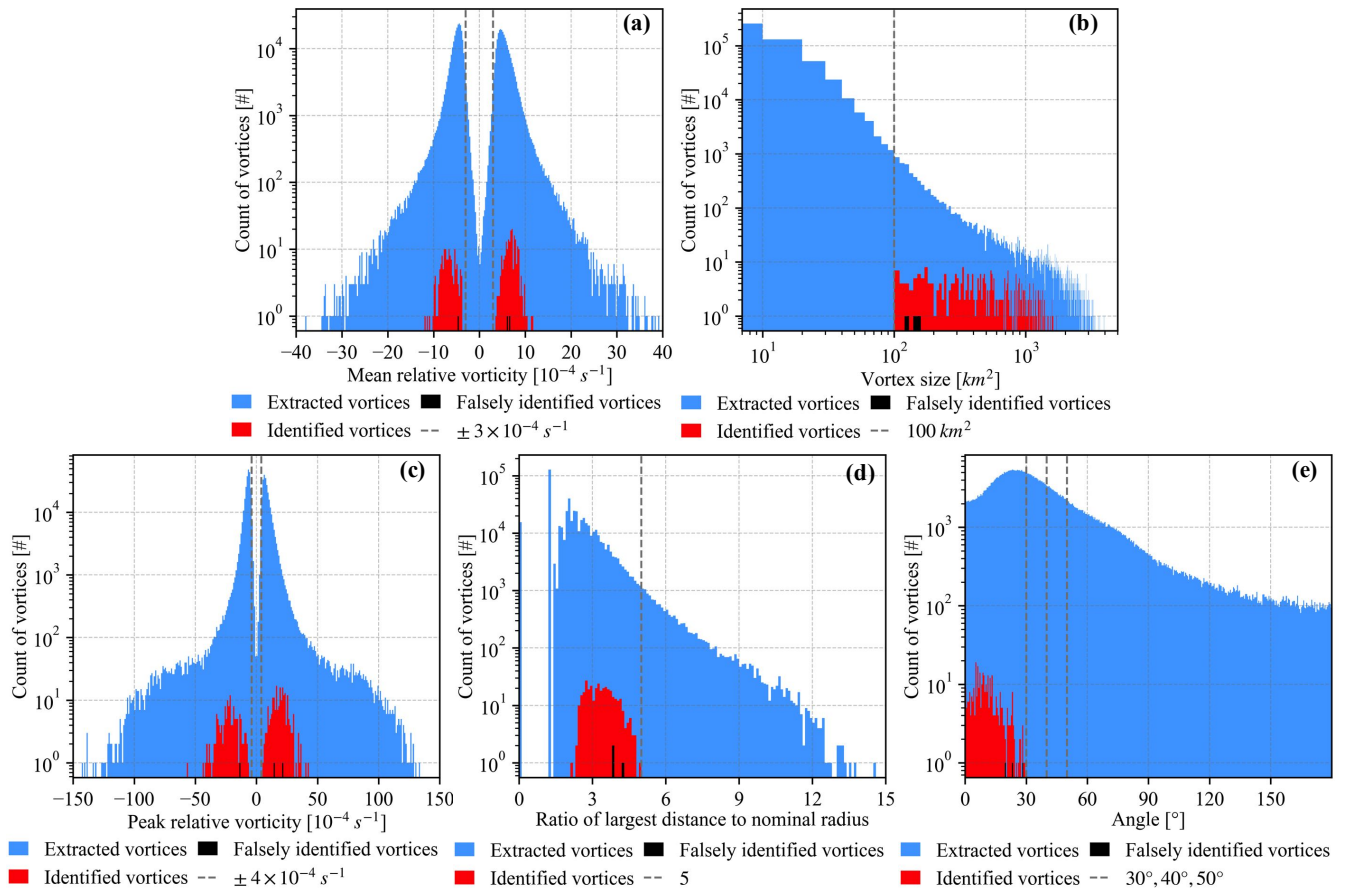
Figure B1. Histograms of vortex statistics including (a) mean relative vorticity, (b) vortex size, (c) peak ~~or maximum~~ relative vorticity, (d) the ratio of the largest distance within a vortex to its nominal radius, and (e) deviation angles described in Section 2.4. The blue shadings represent extracted vortices using the first two steps of our algorithm, and the red (black) shadings represent the correctly (falsely) identified vortices using our algorithm during the case study period.

and unrealistic patterns. In contrast, CRS1 produces much larger precipitation amounts approximately centred over Madeira. The high values over Madeira Island in CRS1 are qualitatively consistent with the fact that occasionally even flash floods can occur (Fragoso et al., 2012; Luna et al., 2011).

565 *Author contributions.* CS and JVT initiated and led the study. JVT conducted the decadal model simulation. QG and CZ contributed ideas in the early stage of the study. QG and CZ developed the code for the automatic vortex identification. QG performed the data analysis and created all figures and tables with contributions from CZ and DL. QG wrote the manuscript with contributions from all authors.
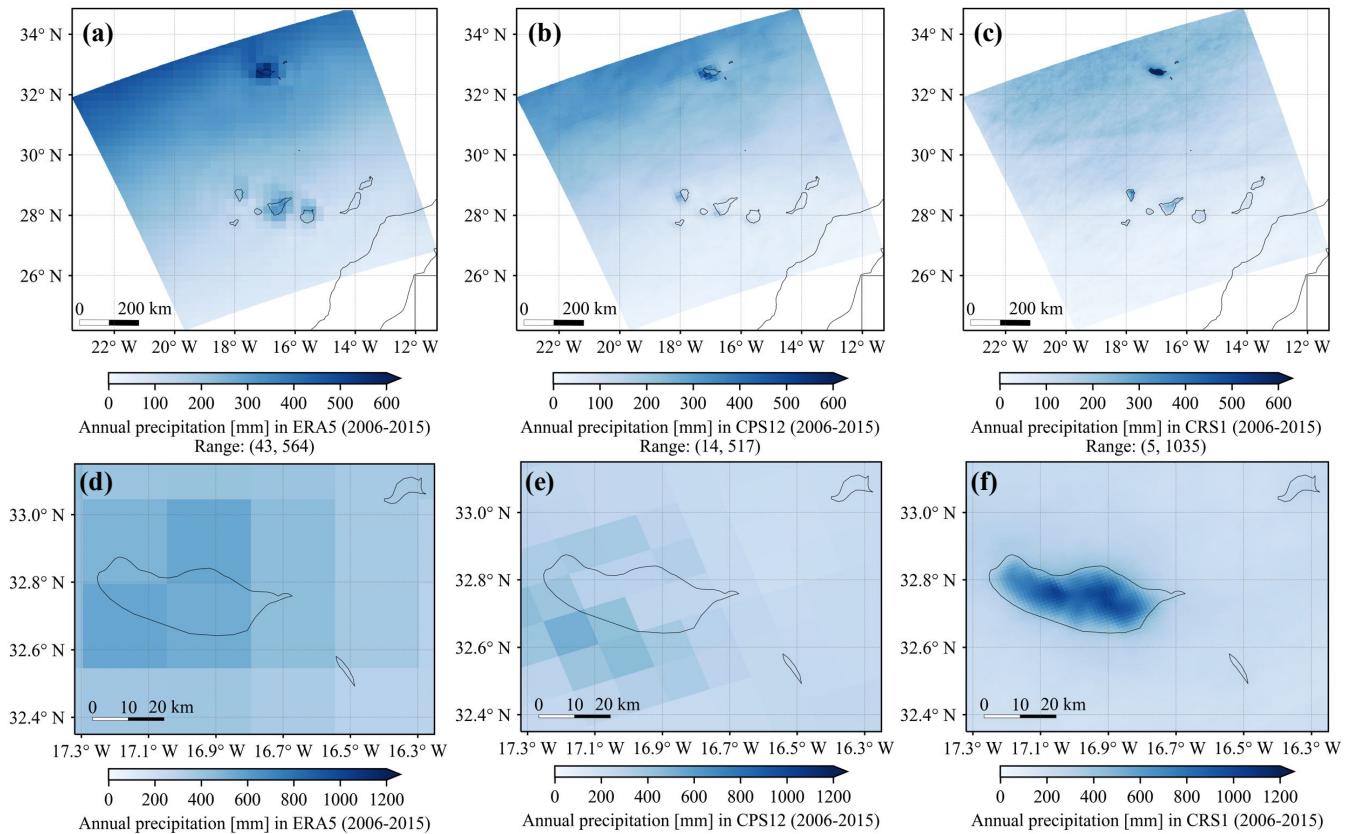
Figure C1. Annual precipitation [mm] over (a-c) the analysis region and (d-f) Madeira Archipelago in (a, d) the ERA5 reanalysis, (b, e) CPS12, and (c, f) CRS1 from 2006 to 2015. Note the different scales for the top and bottom row panels. The geographic map is from the Natural Earth.

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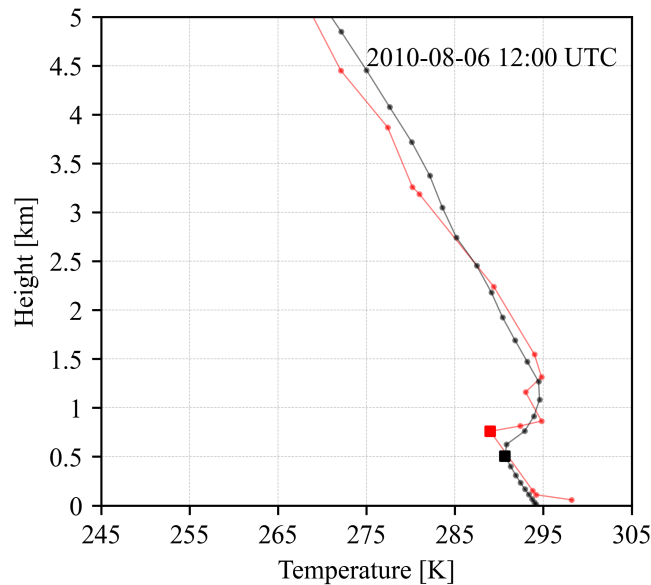
Figure C2. Typical vertical temperature profiles at Funchal from the radiosonde observations (red line) and the model simulation (black line) at 2010-08-06 12:00 UTC. Nearest neighbour interpolation is used to extract data from the model simulation at Funchal. The red and black squares represent the inversion height calculated from the vertical temperature profiles.

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