# Joint probability analysis of storm surge and wave caused by tropical cyclone for the estimation of protection standard: a case study on the eastern coast of the Leizhou Peninsula and Hainan Island of China

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Abstract. The impact of natural hazards such as storm surges and waves on coastal areas during extreme tropical cyclone events can be amplified by the cascading effects of multiple hazards. Quantitative estimation of the marginal distribution and joint probability distribution of storm surges and waves is essential to understanding and managing tropical cyclone disaster
risks. In this study, the dependence between storm surges and waves is quantitatively assessed using the extreme value theory (EVT) and Copula function for the Leizhou Peninsula and Hainan Island of China, based on the numerically simulated surge heights (SHs) and significant wave heights (SWHs) for every 30 minutes from 1949 to 2013. The steps for determining coastal protection standards in scalar values are also demonstrated. It is found that the generalized extreme value (GEV) function and Gumbel Copula function are suitable for fitting the marginal and joint distribution characteristics of the SHs and SWHs, become higher further from the coastline. Lastly, the optimal design values of SHs and SWHs under different joint return periods can be estimated using the non-linear programming method. This study shows the effectiveness of the bivariate Copula function in evaluating the probability for different scenarios, providing a valuable reference for optimizing the design of engineering protection standards.

25 Keywords: Joint probability analysis, Storm surge and wave, Copula function, Tropical cyclone, Leizhou Peninsula and

# Hainan Island

#### **1** Introduction

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Tropical cyclone storm surges and waves could cause severe loss of life and property in offshore and coastal areas (Chen and Yu, 2017; Marcos et al., 2019; Wahl et al., 2015), and it is of great importance to quantify the intensity-frequency relationship

30 of storm surges and waves, in order to understand the joint severity of multi-hazard extreme tropical cyclones (Zhang and Wang, 2021; Galiatsatou and Prinos, 2016).

In the past, many studies have analyzed the single hazard indicators for tropical cyclone storm surges and waves (Lin et al., 2010; Shi et al., 2020; Teena et al., 2012), often with observed time series data or with simulated results by numerical models (Petroliagkis et al., 2016; Bilskie1 et al., 2016; Huang et al., 2013; Papadimitriou et al., 2020). The intensity values of the surge height (SH) or significant wave height (SWH) of a specific return period can be estimated based on the extreme value theory (EVT) (Teena et al., 2012; Muraleedharan et al., 2007; Morellato and Benoit, 2010; Niedoroda et al., 2010). Accordingly, the estimated probabilities of single hazards, such as SH or SWH, have been widely applied in the protection standard in coastal areas (Bomers et al., 2019; Perk et al., 2019; Lee and Jun, 2006).

However, strong storm surges and waves often occur concurrently during tropical cyclone events, which often cause greater

- 40 impact than estimated only with a single variate due to the cascading effects of multi-hazards. For example, when high waves near the coast take place along strong storm surges, the overtopping and overflowing at sea dyke can lead to a large area of inundation and severe damage to coastal facilities (Rao et al., 2012; Hughes and Nadal, 2009; Pan et al., 2019). Similarly, rising sea levels due to storm surges would improve the probability of wave overtopping (Pan et al., 2013; Li et al., 2012). The concurrent interaction between storm surges and waves may cause the modeling of multi-hazards with significant uncertainties.
- 45 Some studies have investigated the physical interaction of storm surges and waves through numerical simulation by coupling storm surge and wave models (Xie et al., 2016; Kimf et al., 2016; Brown, 2010) for specific events. Statistical tools such as joint probability analysis have been used in multidimensional natural hazard assessment (Hsu et al., 2018). Since the Copula function does not restrict the marginal distribution function and can be relatively easily extended to multiple dimensions, it is often used to construct joint probability of multiple variates (Nelsen, 2006; Chen and Guo, 2019).

- 50 There are a variety of applications with Copula function for double hazards, for example, rainfall and storm surge (Jang and Chang, 2022), wind and storm surge (Trepanier et al., 2015), and storm surge and wave (Corbella and Stretch, 2013; Wahl et al., 2012).
- In coastal protection standard design, it is essential to analyze and estimate the joint probability of SH and SWH. Chen et al. (2019) used the Copula functions to analyze the joint probability of extremely significant wave heights (SWHs) and surge heights (SHs) at nine representative stations along China's coasts. Galiatsatou and Prinos (2016) investigated the joint probability of extreme wave heights and storm surges with time by a non-stationary bivariate approach. Marcos et al. (2019) statistically assessed the dependence between extreme storm surges and wind waves along global coastal areas using the outputs of numerical models. Most previous joint probability studies on storm surges and waves mainly focused on location-specific rather than region-wide analysis. In addition, even with the joint probability of bivariate estimation, only an intercepted curve can be obtained since their probability is a three-dimensional surface. In addition, as the intensities of the bivariates and their simultaneous probability are three-dimensional surfaces, the cross-section at a given return period is a curve rather than a specific scale value, so the joint probability of SHs and SWHs alone can not be used directly as a reference value for engineering protection standard. In order to obtain two specific scalars for SH and SWH, other constraints, such as their preferred simultaneous return periods are needed (Xu et al., 2022).
- In this study, we aim to explore the joint probability characteristics of tropical cyclone storm surges and waves for large coastal areas and to investigate the methods and steps for selecting the protection standard of sea dikes. Firstly, the marginal distribution and Copula function of modeling nodes in the study area is fitted based on the long-term numerically simulated tropical cyclone SH and SWH from 1949 to 2013. Next, the optimal Copula functions are selected for every modeling node based on the Kolmogorov-Smirnov (K-S) test, AIC, and BIC. Then, the correlation between SH and SWH is quantified using
- the Copula function to calculate the probabilities under simultaneous, joint, conditional, and different-level combinations. The change in bivariate occurrence probability after increasing the engineering protection standard for the SHs and SWHs is quantitatively assessed. Finally, with the maximum bivariate simultaneous return period as the objective function and the bivariate joint return period as the constraint, the optimum engineering design values of SHs and SWHs are solved by the non-linear programming method.

## 75 2 Study area and data

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#### 2.1 Best tracks of TCs

The best track dataset of historical TCs in the Northwest Pacific (NWP) is obtained from the Tropical Cyclone Data Center of the China Meteorological Administration (CMA). The CMA records in detail the location (longitude and latitude), time (year, month, day, hour), central minimum pressure, and 2-minute average near-center maximum sustained wind speed (MSW) for every 6-hour track point of each TC event since 1949 (Lu et al., 2021). The landfall of TCs in China is concentrated on the southeast coast, especially in the coastal areas of the South China Sea. Figure 1a shows the spatial distribution of the best track and maximum sustained wind speed of 86 historical TCs screened in this study from 1949 to 2013.



Figure 1: Best track and MSW of 86 TCs in this study from 1949 to 2013 (a) and the study area for the joint probability analysis of storm surges and waves of TCs (b).

#### 2.2 Surge heights

The SHs dataset is obtained from the Ocean University of China, mainly through the ADvanced CIRCulation model (ADCIRC) simulations, which includes the SHs of 86 TCs affecting the eastern coast of the Leizhou Peninsula and Hainan Island from 1949 to 2013 (Liu et al., 2018; Li et al., 2016). The previous study provides a water depth map for the study area (Liu et al.,

90 2018). The ADCIRC model integrates the effects of various boundary conditions and external forcing and uses triangular grids with different resolutions, making it more computationally efficient and applicable in numerical simulations. The simulation results are the total water level after the superposition of the water gain caused by a tropical cyclone and astronomical tide, and the time step is 30 minutes.



95 Figure 2: The bathymetry of storm surge modeling area (a) and study area (b).

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To improve the simulation accuracy and computing speed of the hot spot area, the model adopts a triangular grid with nested small- and large-area grids, and the resolutions of different area grids are set in a gradual resolution range from 0.0039° to 0.3°. The calculation region for the large-area is 105.5° E-121.2° E and 3.3° N-26.4° N, and the calculation region for the small- area is 105.5° E-116.5° E and 14.7° N-23.1° N (Figure 2a). And a gradient resolution is used to set the resolution for different regional grids. In the large-area model, the whole large-area contains 9,331 triangular grid nodes and 18,068 triangles; the resolution of the shoreline in the area near Zhanjiang is 0.07°-0.1°, while the resolution in other area is about 1 km-2 km. In the small-area model, the whole small-area contains 41,153 triangular grid nodes and 79,889 triangles; the resolution of the shoreline near Zhanjiang port is 0.0039°-0.01, the resolution of the open boundary is set to 0.1°-0.3°. The full domain is driven

by atmospheric forcing at the surface and surge elevation inversed from the sea surface atmospheric pressure at the open boundary. ADCIRC computes water levels via the solution of the Generalized Wave Continuity Equation (GWCE), which is a combined and differentiated form of the continuity and momentum equations:

$$\frac{\partial^2 \zeta}{\partial t^2} + \tau_0 \frac{\partial \zeta}{\partial t} + Sp \frac{\partial \tilde{J}_{\lambda}}{\partial \lambda} + \frac{\partial \tilde{J}_{\varphi}}{\partial \varphi} - SpUH \frac{\partial \tau_0}{\partial \lambda} - VH \frac{\partial \tau_0}{\partial \varphi} = 0$$
(1)

and the currents are obtained from the vertically-integrated momentum equations:

$$\frac{\partial U}{\partial t} + S_p U \frac{\partial U}{\partial \lambda} + V \frac{\partial U}{\partial \varphi} - fV = -g S_p \frac{\partial}{\partial \lambda} \left[ \zeta + \frac{P_s}{g\rho_0} - \alpha \eta \right] + \frac{\tau_{s\lambda,winds} + \tau_{s\lambda,winds} - \tau_{b\lambda}}{\rho_0 H} + \frac{M_\lambda - D_\lambda}{H}$$
(2)

$$\frac{\partial V}{\partial t} + S_p U \frac{\partial V}{\partial \lambda} + V \frac{\partial V}{\partial \varphi} - f U = -g \frac{\partial}{\partial \varphi} \left[ \zeta + \frac{P_s}{g\rho_0} - \alpha \eta \right] + \frac{\tau_{s\varphi,winds} + \tau_{s\varphi,winds} - \tau_{b\varphi}}{\rho_0 H} + \frac{M_{\varphi} - D_{\varphi}}{H}$$
(3)

where  $H = \zeta + h$  is total water depth;  $\zeta$  is the deviation of the water surface from the mean; h is bathymetric depth;  $Sp = cos\varphi_0/cos\varphi$  is a spherical coordinate conversion factor and  $\varphi_0$  is a reference latitude; U and V are depth-integrated 110 currents in the x – and y – directions, respectively;  $Q_{\lambda} = UH$  and  $Q_{\varphi} = VH$  are fluxes per unit width; f is the Coriolis parameter; g is gravitational acceleration; Ps is atmospheric pressure at the surface;  $\rho_0$  is the reference density of water;  $\eta$  is the Newtonian equilibrium tidal potential, and  $\alpha$  is the effective earth elasticity factor;  $\tau_{s,winds}$  and  $\tau_{s,waves}$  are surface stresses due to winds and waves, respectively;  $\tau_b$  is bottom stress; M are lateral stress gradients; D are momentum dispersion terms; and  $\tau_0$  is a numerical parameter that optimizes the phase propagation properties (Dietrich et al., 2012).

- The boundary condition to force the surge in the subdomain is the time series of the water level on each boundary nodes, which includes both the tide elevation of 8 major constituents (M2, S2, N2, K2, K1, O1, P1, and Q1) in that area from OSU Tidal Prediction Software and the surge elevation extracted from the full domain results (Liu et al., 2018). Comparing the simulation values with the measured surge height at the observation sites, we discover that the absolute standard error is 47 cm, the relative standard error is 22%, and the simulation results are similar to the observed values in most cases. Thus, the dataset could be
- 120 used to assess the hazard of TC storm surges. Figure 3a shows an example of the simulation results of the surge height of TC Nasha (ID:1117) at a specific moment.

#### 2.3 Significant wave heights

The SWHs dataset is also obtained from the Ocean University of China, mainly through the Simulating WAves Nearshore

(SWAN) model, and includes the SWHs of 86 TC events affecting the study area from 1949 to 2013 (Li et al., 2016). The

125 SWAN model has the advantage of high computational accuracy and stability and has been widely used in numerical simulations of offshore waters. The simulation results include indicators such as significant wave height, mean period, and wave direction, and the time step is 1 hour.

The model also uses a triangular grid with nested small- and large-area grids and gradual resolution, but the nodes' scopes and locations differ from those of the storm surge model. The calculation region for the large-area is 15° N-22° N, 110.5° E-118.5°

E, which has a spatial step of 0.083° × 0.083°; the calculation region for the small-area is 21° N-21.2° N, 110° E-110.5° E, which has a spatial step of 0.0033° × 0.0033° (Figure 2b). The SWAN model includes land boundaries and water boundaries, which need to be set up separately. The model assumes that the land boundary does not generate waves and assumes that the land boundary can fully absorb waves that cross or leave the shoreline. As the southern and eastern boundaries of the large-area model are open boundaries and are far from the shoreline, which is the focus of this study, the incoming wave energy at the open boundaries of the large-area model can be ignored, and the open boundary conditions for the small-area are calculated from the large-area model (Li et al., 2016). The governing equations of the SWAN model are as follows:

$$\frac{\partial N}{\partial t} + \frac{\partial}{\partial \lambda} [(c_{\lambda} + U)N] + \cos^{-1}\varphi \frac{\partial}{\partial \varphi} [(c_{\varphi} + V)N\cos\varphi] + \frac{\partial}{\partial \theta} [c_{\theta}N] + \frac{\partial}{\partial \sigma} [c_{\sigma}N] = \frac{S_{tot}}{\sigma}$$
(4)

The wave action density  $N(t, \lambda, \varphi, \sigma, \theta)$  is allowed to evolve in time (t), geographic space  $(\lambda, \varphi)$  and spectral space (with relative frequencies  $\sigma$  and directions  $\theta$ ),  $(c_{\lambda}, c_{\varphi})$  is the group velocity, (U, V) is the ambient current, and  $c_{\theta}$  and  $c_{\sigma}$  are the propagation velocities in the  $\theta$ - and  $\sigma$ - spaces, the source terms  $S_{tot}$  represent wave growth by wind (Dietrich et al., 2012).

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Comparing the observed data of buoy stations with the simulated values reveals that the unstructured grid can well reflect the wave variation conditions in the sea. In addition, the mean absolute and root mean square errors of the simulated results of the locally encrypted unstructured triangular grid are the smallest, indicating that the data can effectively reproduce the wave distribution during tropical cyclones. It shall be noted that the effect of sea level rise due to storm surge was not considered

during the SWH simulation, which will influence the accuracy of SWHs, especially in intermedia and shallow water. In this paper, we choose the SWH as an indicator of tropical cyclone wave hazard. Figure 3b shows an example of the significant

wave height of TC Nasha (ID: 1170) at a specific moment.



Figure 3: Distribution of surge height (a) and significant wave height (b) at a specific moment of TC Nasha (ID: 1117) (UTC: 150 2011.9.29 6:00:00)

#### 2.4 Study area

Based on the location of the nodes of the triangular grid in the storm surge (Section 2.2) and wave datasets (Section 2.3), we select the region with a dense distribution of both as the study area, and the finalized spatial range is 110°E - 113°E, 18°N -22°N (Figure 1b). This area is located east of the Leizhou Peninsula and Hainan Island in the South China Sea, which is one

155 of the most frequently affected areas by tropical cyclones in China. Based on the SHs and SWHs dataset of TCs, we screen 86 historical TC events that simultaneously affected the study area from 1949 to 2013 for joint probability characteristics analysis of storm surge and wave.

# **3 Methods**

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Sklar (Sklar, 1973) elucidates the role that Copula play in the relationship between multivariate distribution and their univariate margins distribution, and states that any multivariate joint distribution can be described by a univariate marginal distribution function and a couple describing the dependence structure between the variables (Nelsen, 2006). Let F(x) and G(y) be the marginal distributions of x and y, C is the Copula, and H(x,y) = C(F(x),G(y)), where H is the bivariate joint distribution function of x and y (Serinaldi, 2015). Therefore, the Copula function is widely utilized in multi-hazard joint probability analysis of natural disasters (Chen et al., 2019; Lee et al., 2013).

## 165 **3.1 Marginal function**

The marginal function means that the probability density function (PDF) and cumulative distribution function (CDF) of the univariate are constructed by intensity-frequency analysis to reflect the probability of occurrence of the univariate at different intensities. The method is widely utilized in natural hazard assessments such as tropical cyclones, floods, droughts, and earthquakes. We select five commonly employed marginal functions for the annual extremes fitting of tropical cyclone storm

- 170 surges and waves, including the Gumbel, Weibull, gamma, exponential, and generalized extreme value (GEV) functions. In this study, the maximum likelihood method is used to estimate the function parameters, based on which the optimal marginal functions for SHs and SWHs are screened by the following steps: Firstly, the p-value of the K-S test is used to determine whether each node rejects the hypothesis that the samples obey a certain functional distribution. Secondly, the optimal function for each node is screened by the three metrics, D-value of the K-S test, AIC, and BIC. The smaller the D-value of the K-S test,
- AIC, and BIC, the better the goodness of fit, thus determining the optimal marginal function for each node. Finally, an optimal function is selected as the univariate marginal function for all nodes, and its PDF and CDF are fitted.

# 3.2 Bivariate Copula function

There are a variety of Copulas families, including Meta-elliptical Copulas (normal and t), Archimedean Copulas (Clayton, Gumbel, Frank, and Ali-Mikhail-Haq), Extreme Value Copulas (Gumbel, Husler-Reiss, Galambos, Tawn, and t-EV), and the
other families (Plackett and Farlie-Gumbel-Morgenstern) (Chen and Guo, 2019). Among these Copulas, the Archimedean Copula is more popular for hydrologic applications. The commonly employed Archimedean Copula functions include Gumbel, Clayton, and Frank (Table 1), which are selected to analyze the joint probabilities of two variables, the SHs, and SWHs of tropical cyclones. Then the maximum likelihood method is used to estimate the parameters of the Copula function. Next, we fit the goodness-of-fit of Copula functions for the tropical cyclone storm surges and waves at each node by the K-S test.
According to the passing rate of the K-S test at the sample nodes, an optimal function is selected as the Copula function for all

nodes of the two-dimensional variables, and the PDF and CDF are calculated.

	Table 1 l	Formulas and	l parameter range	s for three	types of	bivariate A	Archimedean (	Copula function
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Name of Copula	Bivariate Copula	Parameter $\theta$
Clayton	$C_{\theta}(u, v) = [max \{u^{-\theta} + v^{-\theta} - 1; 0\}]^{-1/\theta}$	$\theta \in [-1,\infty) \backslash \{0\}$
Frank	$C_{\theta}(u,v) = -\frac{1}{\theta} \log \left[ 1 + \frac{\left(e^{-\theta u} - 1\right)\left(e^{-\theta v} - 1\right)}{e^{-\theta} - 1} \right]$	$\theta \in R \backslash \{0\}$
Gumbel	$C_{\theta}(u,v) = exp\left[-\left((-\log(u))^{\theta} + (-\log(v))^{\theta}\right)^{\frac{1}{\theta}}\right]$	$\theta \in [1,\infty)$

Note: u and v are uniform (0,1) random variables (Nelsen, 2006).

#### 3.3 Joint probability of storm surges and waves

# 190 3.3.1 Univariate return period

The return period (RP) indicates the period of natural hazard events, and it is a crucial indicator for quantifying the hazard level, which is widely utilized in hazard analysis. The formula for the return period of a single hazard indicator is as follows.

$$RP_{X} = \frac{E_{L}}{1 - F_{X}(x)} = \frac{E_{L}}{1 - P(X \le x)}$$
(5)

where  $RP_X$  is the return period of the univariate X;  $F_X(x) = P(X \le x)$  is the marginal function of the univariate X; and  $E_L$  denotes the time interval of the sample series of the univariate X, the value is taken as 1 in this paper.

## 195 **3.3.2 Bivariate probability and return period**

Based on the Copula function, it can quantitatively estimate the probability of a multivariate being greater than a specified threshold. The bivariate probability refers to the likelihood that various conditions will occur simultaneously, and the bivariate return period refers to the average time interval required for multiple states to be simultaneously greater than a certain threshold. The definitions of three types of joint probabilities and return periods are given according to the univariate return period formula. The first type is when two variables simultaneously reach a given threshold, which will be defined as the simultaneous

formula. The first type is when two variables simultaneously reach a given threshold, which will be defined as the simultaneous probability  $P_{\cap}$  (Eq. 6) and simultaneous return period  $RP_{\cap}$  (Eq. 7). The second type is that at least one variable reaches a given threshold, which is defined as the joint probability  $P_{\cup}$  (Eq. 8) and joint return period  $RP_{\cup}$  (Eq. 9). The third type is the conditional probability  $P_{\parallel}$  (Eq. 10) and conditional return period  $RP_{\parallel}$  (Eq. 11), where when one of the variables reaches a

given threshold, the other variable also reaches a certain threshold. The formula is as follows (Serinaldi, 2015):

$$P_{\cap} = P((X > x) \cap (Y > y)) = 1 - P(X \le x) - P(Y \le y) + P(X \le x, Y \le y)$$
  
= 1 - F<sub>X</sub>(x) - F<sub>Y</sub>(y) + F<sub>X,Y</sub>(x, y) (6)

$$RP_{\cap} = \frac{E_L}{P((X > x) \cap (Y > y))} = \frac{E_L}{1 - F_X(x) - F_Y(y) + F_{X,Y}(x, y)}$$
(7)

$$P_{\cup} = P((X > x) \cup (Y > y)) = 1 - P(X \le x, Y \le y) = 1 - F_{X,Y}(x, y)$$
(8)

$$RP_{\cup} = \frac{E_L}{P((X > x) \cup (Y > y))} = \frac{E_L}{1 - F_{X,Y}(x, y)}$$
(9)

$$P_{|} = P((X > x)|(Y > y)) = \frac{P(X > x, Y > y)}{P(Y > y)} = \frac{1 - P(X \le x) - P(Y \le y) + P(X \le x, Y \le y)}{1 - P(Y \le y)}$$
(10)

$$=\frac{1-F_X(x)-F_Y(y)+F_{X,Y}(x,y)}{1-F_Y(y)}$$
(10)

$$RP_{|} = \frac{E_{L}}{P((X > x)|(Y > y))} = \frac{E_{L} \cdot (1 - F_{Y}(y))}{1 - F_{X}(x) - F_{Y}(y) + F_{X,Y}(x, y)}$$
(11)

where  $F_X(x)$  and  $F_Y(y)$  are the marginal functions of the univariate X and Y, respectively, and  $F_{X,Y}(x,y)$  is the joint distribution function of the two-dimensional variables (X, Y).

# 3.3.3 Combined scenario probability

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To carry out the tropical cyclone storm surge and wave combination scenario simulation, we classify the SH and SWH into five classes (Table 2) by referring to the *Technical directives for risk assessment and zoning of marine disasters—Part 1: Storm Surge* (MNR, 2019) and *Part 2: Waves* (MNR, 2021). We calculate the bivariate probabilities for discretized hazard level

combination scenarios based on the marginal and Copula functions of the storm surge and wave. The formula is as follows:

$$P_{\&} = P(x_{1} < X \le x_{2}, y_{1} < Y \le y_{2})$$

$$= P(X \le x_{2}, Y \le y_{2}) - P(X \le x_{2}, Y \le y_{1}) - P(X \le x_{1}, Y \le y_{2}) + P(X \le x_{1}, Y \le y_{1})$$
(12)
$$= F_{X,Y}(x_{2}, y_{2}) - F_{X,Y}(x_{2}, y_{1}) - F_{X,Y}(x_{1}, y_{2}) + F_{X,Y}(x_{1}, y_{1})$$

Table 2 Hazard level classification thresholds for combined scenarios of tropical cyclone surge height and significant wave height

Hazard level	Surge height (m)	Significant wave height (m)
Ι	[2.5, +∞)	[14.0, +∞)
II	[2.0, 2.5)	[9.0, 14.0)

III	[1.5, 2.0)	[6.0, 9.0)
IV	[1.0, 1.5)	[4.0, 6.0)
V	[0.0, 1.0)	[0.0, 4.0)

#### 3.4 Design of protection standards for storm surge and wave

## 3.4.1 Probability changes under increased storm surge and wave protection standards

215 In actual engineering protection design, if the protection standards of SH and SWH are appropriately increased or decreased, it can change the simultaneous bivariate probability  $P_{0}$ , joint bivariate probability  $P_{0}$ , and conditional bivariate probability  $P_{1}$ . In this paper, we try to estimate the change value of the bivariate probability by raising the return period of storm surge or wave. The formula is as follows:

$$P_{d_{\cap}} = P((X > x_{2}) \cap (Y > y)) - P((X > x_{1}) \cap (Y > y))$$

$$= P(X \le x_{2}, Y \le y) - P(X \le x_{2}) - P(X \le x_{1}, Y \le y) + P(X \le x_{1})$$

$$= F_{X,Y}(x_{2}, y) - F_{X}(x_{2}) - F_{X,Y}(x_{1}, y) + F_{X}(x_{1})$$

$$P_{d_{\cup}} = P((X > x_{2}) \cup (Y > y)) - P((X > x_{1}) \cup (Y > y)) = P(X \le x_{1}, Y \le y) - P(X \le x_{2}, Y \le y)$$

$$= F_{X,Y}(x_{1}, y) - F_{X,Y}(x_{2}, y)$$

$$P_{d_{\parallel}} = P((X > x_{2})|(Y > y)) - P((X > x_{1})|(Y > y))$$

$$= \frac{P(X \le x_{2}, Y \le y) - P(X \le x_{2}) - P(X \le x_{1}, Y \le y) + P(X \le x_{1})}{1 - P(Y \le y)}$$

$$(15)$$

$$= \frac{F_{X,Y}(x_{2}, y) - F_{X}(x_{2}) - F_{X,Y}(x_{1}, y) + F_{X}(x_{1})}{1 - F_{Y}(y)}$$

where  $P_{d_{0}}$ ,  $P_{d_{0}}$ , and  $P_{d_{1}}$  are the changes of the simultaneous probability  $P_{0}$ , the joint probability  $P_{0}$ , and the conditional 220 probability  $P_{1}$  after the univariate return period is raised; and  $x_{1}$  and  $x_{2}$  are the intensity values of variable X for different return periods, respectively, where  $x_{2} > x_{1}$ .

## 3.4.2 Design surge sights and significant wave heights for joint return period scenarios

Based on the binary Copula function, the bivariate joint probability of extreme storm surges and waves under different joint return periods is available. In order to achieve the optimal protection effects, it is natural that we need to set the maximum

bivariate simultaneous probability of SH and SWH as target functions (Eq. 16) and use joint probability as constraints (Eq.

17).

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$$max \{P_{\cap}\} = min \{RP_{\cap}\} = min \left\{ \frac{E_L}{P((X > x) \cap (Y > y))} \right\} = min \left\{ \frac{E_L}{1 - F_X(x) - F_Y(y) + F_{X,Y}(x, y)} \right\}$$
(16)

$$\begin{cases} K = RP_{\cup} = \frac{E_L}{P((X > x) \cup (Y > y))} = \frac{E_L}{1 - P(X \le x, Y \le y)} = \frac{E_L}{1 - F_{X,Y}(x, y)} \\ x \in (0, 40) \\ y \in (0, 40) \end{cases}$$
(17)

According to the non-linear programming method (Bazaraa et al., 2006), for a combined event of extreme SHs and SWHs, a series of (x, y) shall be iterated to minimize  $P((X > x) \cap (Y > y))$  for a given joint return period to obtain the best costbenefit effect. Therefore, the optimal values of SH and SWH can be solved, as illustrated in Figure 4. Since we have the estimation of the joint probability for the study area instead of some specific locations, the optimal design values for SHs and SWHs for all the eastern coasts of the Leizhou Peninsula and Hainan Island can be estimated.



Figure 4: Diagram of determining design surge height and significant wave height based on their joint and simultaneous return periods (red curves are joint return periods ( $RP_{\cup}$ ), black curves are simultaneous return periods ( $RP_{\cap}$ ), and black dots ( $SH_{optimal}$ ,  $SWH_{optimal}$ ) is the optimal design value for SH and SWH).

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## 4 Results and discussion

## 4.1 Optimal marginal function

Since the different densities and locations of the triangular grids in the storm surge and wave models, we use the storm surge triangular grid nodes as the benchmark and the wave node closest to each storm surge node as the wave simulation result based on the nearest neighbor method. Therefore, a dataset of storm surges and waves with the same number and location of nodes is reconstructed, containing 1665 nodes in the study area.

In this paper, based on the reconstructed storm surge and wave simulation results of historical TC events, we calculate each node's annual extremes of SH and SWH. Firstly, the time series of the bivariate annual extremes for all nodes are fitted with five marginal functions, including Gumbel, Weibull, gamma, exponential, and generalized extreme value (GEV). Next, the p-value of the K-S test is used to determine whether the hypothesis that the sample obeys a certain theoretical distribution is rejected. Then, we count the number of nodes passing the K-S test for each function and their percentage of all nodes. Finally, the number of nodes and their percentage of each function being selected as optimal is calculated according to the steps for optimal function selection in Section 3.1 (Table 3).

	Surge height				Significant wave height			
Marginal	Frequency	Percentage	Frequency	Percentage	Frequency	Percentage	Frequency	Percentage
function	of K-S test	of K-S test	of optimal	of optimal	of K-S test	of K-S test	of optimal	of optimal
	passed	passed (%)	function	function (%)	passed	passed (%)	function	function (%)
Gamma	1508	90.57	183	10.99	1464	87.93	159	9.55
Exponential	1567	94.11	216	12.97	1076	64.62	95	5.71
Gumbel (right)	1615	97.00	350	21.02	1629	97.84	149	8.95
Weibull (max)	1469	88.23	416	24.98	300	18.02	494	29.66
GEV	1665	100.00	500	30.04	1657	99.52	768	46.13



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Figure 5: Fitting results of the PDF and CDF of the surge sight and significant wave height based on the GEV function (using node (110.5142° E, 20.2768° N) as an example)

Based on the statistical results, it is found that for fitting the SH, the K-S test of the GEV function had the highest no-rejection rate of 100%, and the corresponding optimal ratio was 30.04%, so GEV is set as the optimal marginal function in this study. For the SWH fitting, the number of nodes with no rejection in the K-S test of the GEV function is 1657, accounting for 99.52%

of the total number of nodes, and the corresponding percentage of preferences is also higher than that of other functions. We apply the GEV function to fit the marginal function of the SH and SWH at all nodes and calculate the PDF, CDF, and RP. Figure 5 shows an example of the PDF and CDF of the SH and SWH for a given node.

# 4.2 Distribution of univariate return periods

Based on the univariate return period formula (Eq. 5), the SH and SWH are estimated for six typical return periods of 5-, 10-, 20-, 50-, 100-, and 200-year at all nodes. To analyze the distribution characteristics of the univariate return period in this study area, we chose the cubic spline interpolation method to interpolate the intensity values at each node with different return periods into a raster with a resolution of 1 km (Figure 6 and Figure 7).

As shown in Figure 6, the SH shows a significant increasing trend as it approaches the coastline. The SHs along the eastern

265 coast of the Leizhou Peninsula are higher than most other regions. Frequent TC events, TC moving direction (Figure 1), and pocket-shaped coastal topography (Figure 2) are all favorable factors to water accumulation in this area. Another area with high SHs is located to the east of Hainan Island. Besides frequent TCs, this area is at the transition zone from the continental shelf to the continental slope, where bathymetry changes rapidly and can bring strong storm surges easily.



270 Figure 6: Spatial distribution of surge heights of tropical cyclones for six typical return periods

As shown in Figure 7, the SWHs near the shore are generally smaller than that in the open sea, and there is a significant decreasing trend in SWH as it gets closer to the coastline. This is mainly attributed to the shallow shore depth, island obstruction, wave breaking, and seabed friction attenuation. Among them, the SWHs in the eastern Leizhou Peninsula are lower than that of other seas, which is mainly influenced by the curved depressed coastline and the topography of the shore section. The SWHs are influenced by the frequency, duration, and intensity of TCs, so the SWH is higher in the east and south of Hainan Island than in the north. The east side of Hainan Island from the continental shelf to the continental slope causes a wave-breaking effect and dissipation caused by the dramatic change in seafloor topography height, which results in a more significant gradient in SWH. In addition, it shall be noted that errors may be introduced during the estimation of SWHs with GEV due to the limited number of TC events.

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Figure 7: Spatial distribution of significant wave heights of tropical cyclones for six typical return periods

# 4.3 Optimal Copula function

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The optimal GEV function is utilized as the marginal function for the TC storm surges and waves, based on which three Copula functions are applied to the bivariate joint fitting of 1665 nodes. The function parameters are fitted by the maximum likelihood method, and the K-S test is used to determine whether the hypothesis that the sample obeys a certain functional distribution is rejected. Next, we count the number of nodes that pass the K-S test for the three types of Copula functions and their percentage of the total number of nodes (Table 4). The statistical results show that the number of nodes passing the K-S test for the Gumbel Copula function is 1603, accounting for 96.28% of all nodes, so it is used as the optimal Copula function. The Gumbel Copula function is applied to the bivariate joint fitting of SH and SWH for all nodes, and the PDF and CDF are calculated.

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290 Table 4 Frequency and percentage of three Copula functions passing the K-S test for all nodes of surge height and significant wave height of tropical cyclones

Copula function	Frequency	Percentage (%)
Clayton	486	29.19
Frank	1398	83.96
Gumbel	1603	96.28

# 4.4 Distribution of bivariate probabilities and return periods

Based on the optimal marginal function and Copula function, we calculate  $RP_{\cap}$ ,  $RP_{\cup}$ , and  $RP_{|}$  of SHs and SWHs. In addition, based on the formula of bivariate probability (Eq. 6 and Eq. 8),  $P_{\cap}$  and  $P_{\cup}$  of SH and SWH are calculated for all nodes with

a combination of 10-, 20-, 50-, and 100-year return period scenarios. To analyze the distribution characteristics,  $P_{\cap}$  and  $P_{\cup}$  for different combinations of return periods at each node are interpolated into a raster with a resolution of 1 km using the cubic spline interpolation method (Figure 8 and Figure 9).

The simultaneous bivariate probability  $P_{\cap}$  gradually decreases as the return period of SH or SWH increases (Figure 8). Overall, the closer to the coastline, the higher  $P_{\cap}$ .  $P_{\cap}$  is greatest when the return period of SH and SWH is 10-year, which is

higher than 0.05.  $P_{\cap}$  is the smallest for SH and SWH of 100-year return period, which is generally lower than 0.009.



Figure 8: Simultaneous probabilities of combined scenarios with four typical return periods for surge height and significant wave heights of tropical cyclones

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The joint bivariate probability  $P_{\cup}$  of SH and SWH is higher than  $P_{\cap}$ , and it gradually decreases with an increasing return period of the two hazard indicators (Figure 9). Overall, the closer to the coastline, the higher  $P_{\cup}$ .  $P_{\cup}$  is highest when the return period of SH and SWH is 10-year, which is greater than 0.13 overall.  $P_{\cup}$  is smallest when the return period for SH and SWH is 100-year, which is less than 0.015. When the return period of SH or SWH is 50- or 100-year, the regional variation in

 $P_{\cup}$  are relatively small.



310 Figure 9: Joint probabilities of combined scenarios with four typical return periods for surge height and significant wave heights of tropical cyclones

Based on the formula of conditional bivariate probability  $P_{\parallel}$  (Eq. 10), we calculate  $P_{\parallel}$  for all nodal univariates with different return periods for the other variable in four return periods, interpolate them into 1 km raster data using cubic spline interpolation. According to the formula, the calculation results are consistent when the positions of the variables are swapped. Therefore,

only  $P_{|}$  for the four return periods of SH in different wave return periods are shown in this paper (Figure 10). When the SWH is a specific return period,  $P_{|}$  gradually decreases as the return period of the SH increases. Under the condition that the return period of SWH is 10-year,  $P_{|}$  for SH with a 10-year return period are concentrated between 0.55 and 0.75, and  $P_{|}$  is generally less than 0.08 if the return period for SH is 100-year. When the return periods of SWHs and SHs are equivalent, the  $P_{|}$  is concentrated between 0.55 and 0.75.



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Figure 10: Conditional probabilities of bivariate for different return periods of tropical cyclone significant wave heights

According to the classification thresholds of the hazard indicators (Table 2), SH and SWH are divided into five classes. We calculate the combined scenario probability  $P_{\&}$  based on Eq. 12 for all nodes with different combinations of SH and SWH for a total of 25 scenarios and interpolate them into 1 km raster data using the cubic spline interpolation method (Figure 11).

Regarding the vertical variation pattern, when the SH hazard level is determined, as the SWH hazard level increases, the high-value area of the combined scenario probability gradually moves away from the coastline, and the scope of the nearshore low-value area gradually expands. This result is consistent with the geographic distribution pattern: the SWH is low nearshore and high offshore. In the horizontal variation pattern, when the hazard level of SWH is determined, as the hazard level of SH increases, the range of low-value areas for the combined scenario probabilities expand, and the low-value area's left boundary gradually approaches the coastline. This result is consistent with the geographic distribution of SHs being high nearshore and low offshore. Overall, the maximum value of the probability for each combined scenario tends to decrease as the hazard level of SH or SWH increases. The larger SH and SWH are concentrated in the eastern Leizhou Peninsula at a certain distance from the coast, with other areas less likely to occur.



335 Figure 11: Probabilities of combined scenarios with different levels of surge height and significant wave height for tropical cyclones

Based on the calculated  $P_{\cap}$ ,  $P_{\cup}$ ,  $P_{\parallel}$ , and  $P_{\&}$  with different return periods, Markov chain Monte Carlo (MCMC) and other methods can be further applied to generate random samples for quantitatively assessing TC storm surges and waves. On the other hand, we can explore the effect of varying the intensity values of SH and SWH on the bivariate joint probabilities and apply it to the engineering protection standard.

#### 340 **4.5 Design of protection standards for storm surge and wave**

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In the design of storm surge and wave protection standards, if one hazard indicator is dominant, upgrading the return period for the other variable can effectively change bivariate  $P_{\cap}$  and  $P_{\cup}$  when the conditions for their return period protection standard are determined. In this paper, we calculate the change in probability based on Eq. 13, Eq. 14, and Eq. 15 to determine the shift in the probability that remains constant when the positions of the two hazard indicators are switched. Therefore, we calculate the change values in  $P_{\cap}$ ,  $P_{\cup}$ , and  $P_{\parallel}$  for all nodes when the return period protection standard for a given variable is increased from 5-, 10-, 20-, and 50-year to 10-, 20-, 50-, and 100-year, respectively. And the data are interpolated into 1 km raster data using the cubic spline interpolation method (Figure 12, Figure 13, and Figure 14).

Figure 12 shows the distribution of the reduction values of bivariate  $P_{\cap}$  for the scenario with elevated univariate return period protection standard of one variable increases, the decline in  $P_{\cap}$  gradually decreases

as the return period protection standard for the other variable increases. Its reduction is concentrated between 0 and 0.035. When the return period protection standard of one variable is fixed, as the design standard of another variable is gradually increased, the decline in  $P_{\cap}$  rises to a certain level and then tends to decrease. When the return period of one variable is 10or 20-year, the decline in  $P_{\cap}$  increases when the protection standard of another variable is raised. If the design standard increase from a 50-year to a 100-year return period, the change value of  $P_{\cap}$  decreases.



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Figure 12: Difference in the simultaneous probability of tropical cyclone surge height and significant wave height for scenarios with elevated return period protection standards

Figure 13 shows the distribution of the reduced values for bivariate  $P_{\cup}$  when the protection standard for the univariate return period is increased. Among them,  $P_{\cup}$  decreases more than  $P_{\cap}$ , and the reduced value of  $P_{\cup}$  varies from 0 to 0.105. As the return period protection standard for one variable gradually increases,  $P_{\cup}$  slowly decreases after the design standard for the other variable increase. When the return period protection standard for one variable is fixed, the decline in  $P_{\cup}$  gradually

## decreases as the design standard for the other variable are increased.



Figure 13: Difference in joint probability of tropical cyclone surge height and significant wave height for scenarios with elevated return period protection standards

Figure 14 shows the distribution of the reduced values of bivariate  $P_{\parallel}$  for the scenario of raising the univariate return period protection standard. As the return period for one variable increases, the decreasing value of  $P_{\parallel}$  tended to decrease after increasing the design standard for the other variable.  $P_{\parallel}$  has a more significant decrease than  $P_{\cap}$  and  $P_{\cup}$ , and the decreasing

value of  $P_1$  varies from 0 to 0.45. When the protection standard of one variable is fixed and low, the reduction in  $P_1$  will tend to decrease after the design standard of another variable are raised to a certain level. When the protection standard for one variable is a 10- or 20-year return period, the decrease in bivariate  $P_1$  tends to increase when the design standard for the other variable's return period is raised, but the decrease in  $P_1$  is slightly reduced when the design standard of the other variable is increased from a 50-year to a 100-year return period. If the protection standard of one variable is high, the decrease in  $P_1$  after the design standard of the other variable is raised always tends to increase.



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Figure 14: Differences in the conditional probability of tropical cyclone surge height and significant wave height for scenarios with elevated return period protection standards

In the engineering protection standard, the appropriate design values of the SHs and SWHs are set according to the bivariate  $RP_{\cup}$  and  $RP_{\cap}$ , and the estimation method is shown in Section 3.4.2. In this paper, the design values of SH and SWH for six  $RP_{\cup}$  for all nodes are calculated based on the above method and interpolated to 1 km raster data by the cubic spline interpolation method (Figure 15 and Figure 16). The design SH and SWH show an apparent increasing trend as the return

period increases, with the high-value area for SH constantly concentrated east of the Leizhou Peninsula and the high-value area for SWH concentrated in the east of Hainan Island.

When  $RP_{\cup}$  is a 5-year return period, the design SHs are between 1.5 m and 2.5 m in the eastern coastal area of the Leizhou Peninsula and fall below 0.5 m in the southeastern coastal region of Hainan Island. As the return period increases, the design SH gradually increases, and when  $RP_{\cup}$  is a 200-year return period, the design SH in the eastern coastal area of the Leizhou Peninsula is generally higher than 3.0 m. The design SH in the northeast coastal area of Hainan Island is mainly between 3.0 m and 15.0 m, while that in the southeast coastal region of Hainan Island is between 0.5 m and 2.0 m, which is lower than that in the northeast.



Figure 15: Design surge heights for six typical joint return period scenarios

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When  $RP_{U}$  is a 5-year return period, the design SWHs in the coastal areas of the Leizhou Peninsula and Hainan Island are less than 2.5 m overall. The further away from the coastline, the design SWH gradually increases. As the return period increases,

the design SWH gradually increases, and the growth is more evident than that of SH. When  $RP_{\cup}$  is a 200-year return period, the design SWH along the coast of the Leizhou Peninsula is generally less than 6.0 m, while the design SWH along the Qiongzhou Strait and southeastern Hainan Island is relatively high.



Figure 16: Design significant wave heights for six typical joint return period scenarios

# **5** Conclusions

400 In this study, we aimed to estimate joint probability analysis of storm surges and waves using Copula functions on a large dataset from a wide area and to determine their respective design standards as scalar values of SWH and SH. Our main conclusions are as follows:

1) The GEV function is the most suitable for fitting the probability distribution characteristics of the annual extremes of tropical cyclone SH and SWH for all nodes in the study area. The Gumbel Copula function is appropriate as a bivariate joint distribution

2) The hazard of a single indicator can be characterized by the univariate intensity values with different return periods, which the optimal marginal function can estimate. Our findings show that the SH exhibits a significant increasing trend closer to the coastline, while SWH is higher farther from the shoreline across different return periods. However, we also observe apparent spatial heterogeneity in the distribution, influenced by factors such as the shoreline shape, coastal and submarine topography,

410 and deflection forces.

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3) Bivariate probabilities are utilized in this study to assess the integrated hazard of multiple indicators, including  $P_{\cap}$ ,  $P_{\cup}$ ,  $P_{|}$ , and  $P_{\&}$ , which effectively compensates for the deficiency of disregarding the correlation among variables in univariate hazard assessment. These four probabilities can visually describe the occurrence probability for different combinations of scenarios; the more significant the probability is, the higher the hazard. Overall,  $P_{|}$  is the largest,  $P_{\cup}$  is the second largest, and  $P_{\cap}$  is the smallest, while  $P_{\&}$  is influenced by the classification of single hazard indicators. When one variable is constant,  $P_{\cap}$ ,  $P_{\cup}$ , and  $P_{|}$  tend to decrease as the return period of the other variable increases.

4) In the actual design for engineering protection standards, the bivariate  $P_{\cap}$ ,  $P_{\cup}$ , and  $P_{|}$  can be reduced by appropriately increasing the design values of the SHs and SWHs. When the return period protection standard of one variable is fixed, as the design standards of another variable gradually increase, the decline in  $P_{\cap}$  and  $P_{|}$  rises to a certain level and then tends to

- 420 decrease, but the decline in  $P_{U}$  gradually decreases. Therefore, developing appropriate design standards for the SHs and SWHs can effectively reduce the impact of tropical cyclone marine hazards on coastal areas. Since the joint probability distribution of the bivariate is a three-dimensional surface, to obtain specific scalar values for these two hazards as design standards, in this study, the optimal design SHs and SWHs under the objective of minimum bivariate simultaneous return period are estimated using a non-linear programming approach with their estimated joint return periods as constraints.
- 425 Although this study provides helpful insights into joint probability analysis of storm surges and waves using Copula functions, several limitations need to be addressed in future research. One limitation is the absence of water level rise caused by storm surges in the numerical modeling of waves, which may introduce errors in the simulation of SWHs in intermediate and shallow water. In addition, exploring the contribution of other indicators, such as long-term sea level rise as environmental hazards, can further improve the accuracy of hazard assessment.

430 *Author contributions.* FWH and ZHX conceived the research framework and developed the methodology. ZHX was responsible for the code compilation, data analysis, graphic visualization, and first draft writing. FWH managed the implementation of research activities and revised the manuscript. CM participated in the data collection of this study. All authors discussed the results and contributed to the final version of the paper.

Competing interests. The authors declare that they have no conflict of interest.

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