An improved near real-time precipitation retrieval for Brazil

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Abstract.

Observations from geostationary satellites offer the unique ability to provide spatially continuous coverage at continental scales with high spatial and temporal resolution. Because of this, they are commonly used to complement ground-based measurements of precipitation, whose coverage is often more limited.

We present a novel, Hydronn, a neural-network-based, near real-time precipitation retrieval for Brazil based on visible and infrared (VIS/IR) observations from the Advanced Baseline Imager (ABI) on the Geostationary Operational Environmental Satellite 16. The retrieval, which employs a convolutional neural network to perform Bayesian retrievals of precipitation, was developed with the aims of (1) leveraging the full potential of latest-generation geostationary observations and (2) providing probabilistic precipitation estimates with well-calibrated uncertainties. The retrieval is trained using more than three years of co-locations with combined radar and radiometer retrievals from the Global Precipitation Measurement (GPM) Core Observatory. Its accuracy is assessed using one month of gauge measurements and compared to the retrievals from passive microwave (PMW) sensors and HYDRO, the VIS/IR retrieval that is currently in operational use at the Brazilian Institute for Space Research.

Hourly, daily and monthly precipitation accumulations are evaluated against gauge measurements for June and December 2020 and compared to HYDRO, the Precipitation Estimation from Remotely Sensed Information using Artificial Neural Networks Cloud Classification System and the Integrated Multi-Satellite Retrievals for GPM (IMERG). Even in its most basic configuration, the accuracy of the proposed retrieval is similar to that of IMERG, which merges retrievals from VIS/IR and microwave observations with gauge measurements. In its most advanced configuration, the retrieval reduces the mean absolute error for hourly accumulations by 22% compared to HYDRO by 44% (41%) for the MSE and increases the correlation by 400% - 138% (312%) for June (December) 2020.

Compared to IMERG, the improvements correspond to 15%, 15% and 39% for June (14%), 12% (12%) and 20% (56%).
respectively. Furthermore, we show that the probabilistic retrieval is well calibrated against gauge measurements when differences in a priori distributions: the distributions of the training data and the gauge measurements are accounted for.

In addition to potential improvements in near-real time precipitation estimation over Brazil, our findings highlight the potential of specialized data-driven retrievals that are made possible through advances in geostationary-sensor technology, the availability of high-quality reference measurements from Hydronn has the potential to significantly improve near-real-time precipitation retrievals over Brazil. Furthermore, our results show that precipitation retrievals based on CNNs that leverage the full range of available observations from latest-generation geostationary satellites can provide instantaneous precipitation estimates with accuracy close to that of state-of-the-art PMW retrievals. The high temporal resolution of the geostationary observation allows Hydronn to provide more accurate precipitation accumulations than any of the tested conventional precipitation retrievals. Hydronn thus clearly shows the GPM mission and modern machine learning techniques. Furthermore, our results show the potential of probabilistic deep-learning-based precipitation retrievals to better characterize the observed precipitation and provide more trustworthy retrieval results. Improve precipitation retrieval from currently available satellite imagery.

1 Introduction

Timely and highly-resolved measurements of precipitation constitute an important source of information for weather forecasting, disaster response and hydrological modeling. These measurements can be provided by dense radar and gauge networks but their coverage is typically limited in less populated regions. However, even where these measurements are available, they are not necessarily without issues. The ability of rain gauge measurements to truthfully represent spatial precipitation statistics at larger scales is limited by their extreme localization (Smith et al., 1996). Ground-based precipitation radars are affected by beam blocking as well as measurement errors caused by the varying altitude of the radar beam along its range (Holleman, 2007).

Since satellite observations provide continuous spatial coverage, they are well suited to complement the measurements from gauges and ground radars. Microwave observations generally provide the most direct space-borne measurements of precipitation because of their sensitivity to emission and scattering from precipitating hydrometeors. Unfortunately, due to their comparably low spatial resolution, these sensors are currently employed only on polar orbiting platforms. Since this limits the width of the satellite swath, a large constellation of sensors on different platforms is required to achieve low revisit times. This approach is the approach pursued by the Global Precipitation Measurement (GPM, Hou et al., 2014). Nonetheless, the revisit times mean revisit time for the passive microwave sensors (PMW) of the GPM constellation still exceed 2 hours in the tropics.

Visible and infrared (VIS/IR) observations from the latest generation of geostationary satellites (Schmit et al., 2005) provide spatial resolutions between 0.5 and 2 km at the sub-satellite point and a temporal resolution of up to 10 minutes for full disk observations. The disadvantage of these observations for measuring precipitation is that they are mostly sensitive to the top of properties of the upper parts of clouds, which are only indirectly related to the precipitation near the surface.
Their unrivaled spatial and temporal resolution nonetheless makes them a valuable source of information for satellite-based precipitation estimates nonetheless.

The operational use of geostationary VIS/IR observations for precipitation retrievals dates back more than 40 years (Scofield and Oliver, 1977) and a large number of different algorithms have been developed over the years (Arkin and Meisner, 1987; Adler and Negri, 1988; Vicente et al., 1998; Sorooshian et al., 2000; Kuligowski, 2002; Scofield and Kuligowski, 2003; Hong et al., 2004; Kuligowski et al., 2016). Due to the aforementioned indirect relationship between observations and precipitation, nearly all of these methods are based on empirical relationships derived from satellite observations co-located with reference data derived from more direct measurement techniques such as ground-based radar. Moreover, operational retrievals often require rely on corrections to improve the accuracy of their estimates. The Self-Calibrating Real-Time GOES Rainfall Algorithm for Short-Term Rainfall Estimates (SCamPR, Kuligowski et al. 2016), for example, is dynamically calibrated using the latest available microwave precipitation estimates. Similarly, the PERSIANN CSS real time dataset is in the process of being Karbalaei et al. (2017) develop a correction for the Precipitation Estimation from Remotely Sensed Information using Artifical Neural Networks (PERSIANN) Cloud Classification System (CCS, Hong et al., 2004) based on retrievals from passive-microwave sensors. PERSIANN CCS is superseded by the PERSIANN PDIR (Nguyen et al., 2020) algorithm, which extends the PERSIANN CCS algorithm with in addition to refining the mathematical formulation of the regression scheme of PERSIANN CCS, adds a regional correction scheme.

Another example is the HYDRO precipitation retrieval that is currently in operational use at the National Institute for Space Research (INPE) in Brazil, which is based on the Hydroestimator algorithm (Scofield and Kuligowski, 2003). It employs an empirical relationship between the 10.7 µm IR channel and precipitation rates with additional corrections. To adapt it for application over South America yet another correction was derived by de Siqueira and Vila (2019), which improved the accuracy of precipitation accumulations but not that of instantaneous precipitation rates.

A common shortcoming of all retrieval algorithms discussed above is that they neglect retrieval uncertainties. The retrieval of precipitation rates from VIS/IR observations constitutes an inverse problem that is strongly underconstrained. This is true even for microwave based retrievals and likely exacerbated by the less direct information content in the VIS/IR observations. The ill-posed character of the retrieval problem leads to significant retrieval uncertainties. Providing probabilistic estimates that quantify these uncertainties would help the characterization of precipitation estimates and thus increase their usefulness.

This study presents Hydronn, a novel real-time precipitation retrieval that uses VIS/IR observations from the GOES 16 Advanced Baseline Imager (ABI, Schmit et al., 2018; Schmit et al., 2005) to retrieve precipitation over Brazil. It was designed with two aims: (1) To leverage the full potential of observations from the latest generation of geostationary sensors and (2) to develop a Bayesian precipitation retrieval algorithm that can provide well-calibrated uncertainty estimates. The algorithm Pfreundschuh et al. (2018) have shown that when a retrieval is cast as a probabilistic regression problem and solved using a neural network, the obtained results are equivalent to those obtained using traditional Bayesian retrieval methods, given that the a priori distribution matches the distribution of the data used to train the neural network. Neural-network-based probabilistic regression techniques thus provide a powerful and flexible way of combining recent advances in deep learning.
with the theoretically sound handling of retrieval uncertainties of Bayesian retrieval methods. Hydronn builds on this approach and uses a convolutional neural network (CNN) to predict a binned approximation of the probability density function (PDF) of the marginal posterior distribution of each output pixel.

The Hydronn retrieval is trained using a large database of co-locations between more than three years of collocated observations from the ABI and the combined radar-radiometer retrievals from the GPM Core Observatory (Grecu et al., 2016)-core observatory (Grecu et al., 2016) over South America. The accuracy of the retrieval—Hydronn’s instantaneous precipitation estimates—is evaluated using a month of gauge measurements. To assess its performance with respect to existing retrievals it is compared to the currently operational HYDRO algorithm as well as separate year of GPM combined retrievals and compared to HYDRO and the Goddard Profiling Algorithm (GPROF, Kummerow et al., 2015) applied to PMW retrievals from the GPM Microwave Imager (GMI). The accuracy of precipitation accumulations is evaluated using gauge measurements from June and December 2020. They are compared HYDRO, and two other commonly used precipitation products: The hourly Precipitation Estimation from Remotely Sensed Information using Artificial Neural Networks Cloud Classification System (PERSIANN CCS, Hong et al., 2004)—which is based on geostationary IR observations only, and the Integrated Multi-Satellite Retrievals for GPM (IMERG, Huffman et al. 2020), which combines observations from microwave, geostationary sensors, and rain gauges.

2 Data

This section presents the rain gauge data, which serve as reference measurements for this study, as well as the baseline algorithms to which Hydronn will be compared. This is followed by a description of the Hydronn retrieval algorithm introduces the various datasets that are used to train and evaluate the Hydronn retrievals.

2.1 GPM CMB

The GPM DPR and GMI Combined Precipitation product (William Olson, 2017) combines observations from the dual-frequency precipitation radar (DPR) and GMI on board the GPM core observatory (Grecu et al., 2016). Although the officially listed shortname for the product is GPM_2BCMB (William Olson, 2017), we will refer to it as GPM CMB since we consider it more readable. Because of the high sensitivity to precipitating hydrometeors of the active and passive microwave observations, the product provides the most accurate space-borne precipitation estimates that are currently available. In this study the product is used as reference data to train the Hydronn retrievals and to assess their accuracy for instantaneous precipitation estimates.

2.2 Rain gauge data

The rain gauge measurements that are used in this study were compiled by the National Institute of Meteorology of Brazil and consists consist of hourly gauge measurement measurements covering the time range May 2000 until May 2020. From this data June and December of 2020 will be used from this data for the evaluation of Hydronn. Data from 2018 and 2019 is used
Figure 1. Overview of the rain gauge data from June and December 2020 used to validate the retrievals. Panel (a) displays their spatial distribution by means of the number of gauges falling into each hexagon. Hexagon-free areas are not covered by any gauges. Panels (b) and (c) show the corresponding mean precipitation measured by all gauges falling into each hexagon.

to derive correction factors for the calibration of the hourly precipitation estimates produced by Hydronn, as will be described in Sec. 3.6 below.

From all available gauge stations only those with a data availability exceeding 90% during June and December 2020 were selected. Their geographical distribution is displayed together with the mean precipitation in Fig. 1. While the gauge density is fairly high on the south-eastern coast of Brazil, it decreases markedly towards the Northwest. Climatologically, the highest precipitation occurs in the Amazonas and surrounding regions in the Northwest.

The precipitation in June 2020 is limited to the south of the country, small parts of the west coast, and the Amazon basin, although the latter is only sparsely covered by the gauge observations. June is typically the beginning of the dry seasons in the central part of the country, however this is not well represented in which is clearly visible the gauge measurements due to their sparsity in this region. More evident are the

December 2020 saw high precipitation amounts on the south-western coast of the country extending towards the Northwest, which manifest northwest, which are associated the South Atlantic Convergence Zone (SACZ, Satyamurty et al., 1998). Very low precipitation rates are observed in the Northeast of the country, which is influenced by large scale subsistence patterns (de Siqueira and Vila, 2019).

2.3 HYDRO

HYDRO is the currently operational near real-time precipitation retrieval at the Center for Weather Forecast and Climate Studies/National Institute for Space Research (CPTEC/INPE). It is based on the Hydroestimator (Scofield and Kuligowski,
2003) and thus uses a combination of empirical power-law relationships between 10.7 µm IR brightness temperatures and surface precipitation with correction factors taking into account model-derived moisture and wind parameters as well as cloud structure. The current version of the retrieval is described in de Siqueira and Vila (2019), which also introduces regional correction factors based on a climatology of surface precipitation rates derived from radar measurements of the Tropical Rainfall Measurement Mission (TRMM, Simpson et al., 1996) and GPM. For this study we use the corrected version of HYDRO proposed in de Siqueira and Vila (2019) with a regional correction for all of Brazil (referred to as HYDROBR in de Siqueira and Vila (2019)).

2.4 PERSIANN-CSS-GPROF GMI

The Goddard Profiling Algorithm (GPROF, Kummerow et al., 2015) is used to retrieve surface precipitation from each of the PMW sensors of the GPM constellation. The algorithm is a Bayesian retrieval scheme that is based on a retrieval database principally built up of collocations of GMI observations and the GPM CMB retrievals. Because GMI is a dedicated precipitation sensor and because its retrieval is based on direct collocations with GPM CMB, the GPROF GMI retrieval is considered the most accurate of the sensors of the GPM constellation. Moreover, since GMI observations can always be collocated with the test data for the Hydronn retrieval, we use GPROF GMI as a baseline to assess the Hydronn retrievals against.

2.5 PERSIANN CCS

PERSIANN CCS (Hong et al., 2004) uses 10.7 µm IR observations from geostationary satellites to retrieve precipitation. Input images are first segmented using increasing temperature thresholds in order to identify pixels that correspond to convective activity. These pixels are consecutively assumed to be precipitating and classified using a neural network based algorithm. Quantitative precipitation estimates at pixel level are derived from this classification by applying a class-specific power law relationship that relates the 10.7 µm brightness temperatures to precipitation.

The dataset that is used for the evaluation against Hydronn are hourly precipitation rates that are distributed in near real time through the PERSIANN data portal (UCI CHRS Data Portal, 2022). Although the global CCS dataset is currently being replaced by the updated PERSIANN Dynamic Infrared-Rain rate (PDIR-Now, Nguyen et al., 2020) we were not able to use it for this study due to the first third parts of the evaluation period missing from the online archive.

2.6 GPM-IMERG

GPM-IMERG (Huffman et al., 2020) combines retrievals from passive microwave and IR observations as well as rain gauge measurements to produce global, half-hourly measurements of precipitation. Due to its reliance on a wealth of measurement sources as well as the sophistication of the retrieval pipeline, the product can be considered one of the most robust satellite-based precipitation products that are currently available (Pradhan et al., 2022).

Three different configurations of IMERG products are available: IMERG-Early and IMERG-Late are based solely on satellite observations and available with latencies of 4 and 14 hours, respectively. IMERG-Final is adjusted using global gauge
measurements but available only after 3.5 months. Although Hydronn has been designed to target near real-time applications and is thus more similar to IMERG-Early, we use IMERG-Final for our comparison as it constitutes the most elaborate precipitation estimates that are currently available and can thus be considered the state of the art of space-borne quantitative precipitation estimation. Global quantitative precipitation estimates.

3 Method

This section describes the implementation of Hydronn, the proposed near real-time precipitation retrieval algorithm for Brazil. It is based on a convolutional neural network (CNN), which is used to predict the a posteriori distribution of instantaneous precipitation. Following this, it is discussed how the probabilistic precipitation estimates can be combined to hourly accumulations and an a priori adjustment is proposed to account for differences between the training data and the gauge measurements that are used to evaluate the retrieval.

3.1 Training data

The training data for the Hydronn retrieval is generated from co-locations of input observations from the GOES-16 ABI (Schmit et al., 2018) and retrieved surface precipitation from the GPM combined product (Grecu et al., 2016). GOES-GPM CMB over South America. Figure 2 shows the domain over which the training data was extracted (marked as 'R1' in Fig. 2). It extends from $-85^\circ$E to $-30^\circ$E in longitude and $-40^\circ$N to $10^\circ$N in latitude. The plot also shows extracted training scenes and corresponding GPM CMB precipitation estimates for September 23, 2019.

The GOES_16 ABI observations were extracted at their native resolutions and combined with the GPM combined surface precipitation by remapping them. The surface precipitation from GPM CMB was mapped to the 2 km resolution of the ABI’s IR channels using a nearest-neighbor criterion. Co-locations interpolation. Collocations were extracted for the time range 2018-01-01 until 2020-01-01 and 2021-01-01 until 2021-09-01. Observations from the first, 11th and 21st day of every month of 1 January 2018 until 1 January 2020 and 1 January 2021 until 1 September 2021.

Collocations from 1 January 2020 are used as test data set to establish the nominal performance of different retrieval configurations until 1 January 2021 were extracted and set aside as test data for assessing the accuracy of the instantaneous precipitation estimates of Hydronn. In addition to this, collocations over an additional region (marked 'R2' in Fig. 2) were extracted on days 1, 6, 11, 16, 21, 26 of each month of the year 2020. This additional test data will be used to investigate the impact of the regional training database on the retrieval accuracy.

The results presented in Pfreundschuh et al. (2018) show the correspondence between the training data of neural network retrievals and the a priori distribution of explicitly Bayesian retrieval schemes. This perspective correspondence between probabilistic neural-network retrievals and Bayesian retrieval methods shown in Pfreundschuh et al. (2018) emphasizes the importance of training data distribution for the retrieval results and their interpretation. Since the retrieval uncertainties depend on the distribution of the training data, the retrieval can provide well-calibrated probabilistic predictions only for test data whose distribution is consistent with that of the training data. The distribution of precipitation
Figure 2. GOES-16 true-color composite from 23 September 2019 (generated using the natural color composite in satpy (Raspaud et al., 2021)). The rectangle R1 marks the domain over South America, which was used for the extraction of training and testing collocations between GOES 16 ANI and GPM CMB. Dashed polygons show the boundaries of the training scenes extracted for this day together with the collocated GPM CMB results. The rectangle R2 marks the secondary domain which is used as an additional test domain to assess the impact of the spatially limited training domain.

rates in the training dataset is displayed in Fig. 3. The detection threshold for precipitation of the GPM radar between 0.2 and 0.4 mm h\(^{-1}\) is clearly visible in the distributions. In addition to this, a weak seasonal cycle is apparent, which mainly impacts the likelihood of moderate precipitation. The gauge measurements exhibit a stronger effect of the seasonal cycle especially for strong rain. It should be noted here, however, that the precipitation estimates in the training data correspond to instantaneous precipitation estimates while the gauge measurements are integrated over the time of an hour. Differences between the seasonal cycles of the datasets may therefore be caused by changes in the temporal evolution of precipitation events. An approach to reconcile the differences between the distributions of training and validation will be proposed in Sec. 3.6 below.

### 3.2 Retrieval configurations

The Hydronn retrieval has been implemented in three different configurations in order to assess how the choice of input observations and output resolution affects its performance. The most basic retrieval configuration is the Hydronn\(_{4\text{IR}}\) retrieval, which only uses brightness temperatures from the GOES-16 10.3 µm channel as input. Due to their sensitivity to cloud top temperatures, longwave IR window channels are also used by HYDRO as well as and the PERSIANN CCS retrieval. The availability of similar channels on a long range historical time series of geostationary sensors makes them suitable for the generation of climate data records. The reliance on a single thermal IR channel has the additional advantage that the information content of the retrieval input is independent of the availability of
Figure 3. Distribution of reference precipitation rates. Panel (a) shows the seasonal PDFs of precipitation rates in the training data. Panel (b) shows the PDFs of precipitation rates measured by the gauges over the time period covered by the training data. Grey lines in the background trace the PDFs of the precipitation rates in the training data shown in Panel (a).

sunlight and thus constant throughout the day. Since this retrieval uses the same input as HYDRO and PERSIANN CCS it allows assessing the benefit afforded by the probabilistic, neural-network-based retrieval technique used by Hydronn.

The second retrieval configuration, denoted as Hydronn\textsubscript{4,All}, uses all available GOES channels at a resolution of 4 km. It uses the same neural network model as the Hydronn\textsubscript{1,IR} configuration adapted to the larger number of input channels, which is the resolution at which both HYDRO and PERSIANN CCS are operating. This model configuration is included to assess the benefit of including all ABI channels in the retrieval.

The third configuration, Hydronn\textsubscript{2,All}, aims to exploit the full potential of GOES observations for precipitation retrievals. The input includes observations from all GOES channels—uses all observations—at their native resolution and precipitation is retrieved at a resolution of the 2 km channels. This means that GOES Ch. 2 is ingested at a resolution of 500 m, Ch. 1, 3, 4 at a resolution of 1 km and the remaining channels at 2 km at nadir. This is in contrast to the other Hydronn configurations and other precipitation retrievals which typically ingest all observations at the same resolution. This configuration aims to explore the extent to which high resolution observations can improve precipitation retrievals even if the reference precipitation measurement only have a resolution of 5 km. Comparison of the Hydronn\textsubscript{4,All} and Hydronn\textsubscript{2,All} configuration aims to address the question whether the increased computational complexity of Hydronn\textsubscript{2,All} can be justified by improvements in retrieval accuracy. The characteristics of the three configurations are summarized in Table 1.
Table 1. Hydronn retrieval configurations

<table>
<thead>
<tr>
<th>Name</th>
<th>Input bands</th>
<th>Input resolution</th>
<th>Output resolution</th>
</tr>
</thead>
<tbody>
<tr>
<td>Hydronn$_{4,IR}$</td>
<td>13</td>
<td>4 km</td>
<td>4 km</td>
</tr>
<tr>
<td>Hydronn$_{4,All}$</td>
<td>1, ..., 16</td>
<td>4 km</td>
<td>4 km</td>
</tr>
<tr>
<td>Hydronn$_{2,All}$</td>
<td>1, ..., 16</td>
<td>0.5, 1 and 2 km</td>
<td>2 km</td>
</tr>
</tbody>
</table>

3.3 Neural network model

All Hydronn retrievals are based on a common similar convolutional neural network (CNN) architecture, which is illustrated in Fig. 4. A preliminary study found CNNs to yield significantly more accurate results than CNNs have been shown to be able to learn semantic features directly from image data (Selvaraju et al., 2017), which sets them apart from conventional regression techniques. Since satellite imagery of clouds exhibits patterns that can be related to different precipitation regimes, we expect this information to help to constrain the precipitation retrieval. In fact, a preliminary study we have conducted found that CNNs yield more accurate precipitation retrievals than a fully-connected neural networks that use only a single pixel as input (Ingemarsson, 2021). The fully-convolutional networks are constructed using what we refer to as Xception blocks, which are based on the Xception architecture network operating on independent pixels. The results have been published as parts of a Master’s thesis and are available online (Ingemarsson, 2021).

CNNs principal building blocks are convolution layers. A convolution layer applies a set of convolution operations to an input image. The parameters of the layer’s convolution kernels are learned during the training of the network. A convolution layers thus corresponds to a set of learnable image transformations. CNNs typically consist of a stack of convolution layers that are interleaved with normalization layers and activation functions. The activation functions are required to allow the CNN to represent non-linear transformations, while normalization has been found to be a crucial ingredient to accelerate the training of CNNs (Ioffe and Szegedy, 2015).

The neural networks used by Hydronn are built up of blocks, each of which comprises two separable convolution layers followed by batch normalization (Ioffe and Szegedy, 2015) and GELU activation functions (Hendrycks and Gimpel, 2016). These blocks were inspired by the Xception model proposed by Chollet (2017). These blocks are combined in an asymmetric A residual connection directly connects the input of each block to its output. These residual connection improve the flow of the gradients through the network and were found to be a crucial ingredient for the training of very deep CNNs (He et al., 2016). The Xception blocks are organized into an encoder-decoder structure with, which was popularized by the UNet model for image segmentation (Ronneberger et al., 2015). The first part of the model, the encoder, combines Xception blocks with down-sampling layers. These downsampling layers reduce the size of the input image by a factor of two and thus double the receptive field of the following layers. This allows the network to efficiently combine information across different regions of the input image.

Following the encoder part of the network, the decoder consists of several stages each containing an upsampling layer and a single Xception block. The upsampling layers allow the network to combine the information extracted at coarser resolution
back down to input resolution. As in the UNet model, skip connections between the corresponding stages of encoder and decoder are included to improve the flow of information through the network.

The head of the network employs 5 stages. Each downsampling stage consists of one downsampling Xception block followed by \( N = 4 \) standard Xception blocks. Layers of \( 1 \times 1 \) convolutions followed by normalization layers and GELU activation function. This network head is computationally equivalent to a fully-connected network that transforms the representation extracted by the encoder and decoder parts of the network to a probability distribution. A final \( 1 \times 1 \) convolution maps the output for each pixel to a vector of length 128. The softmax activation function

\[
\sigma(x) = \frac{\exp(x)}{\sum_i \exp(x_i)}
\]

is applied to each of those vectors to ensure that all elements are positive and sum to 1. This allows the results to be interpreted as probabilities of a categorical distribution.

Since the neural network used by the Hydronn\(_{2,\text{All}}\) retrieval ingests observations at their native resolution, this architecture contains two additional downsampling blocks that allow the network to ingest all ABI channels at their native resolution. These two blocks are omitted for the Hydronn\(_{2,\text{IR}}\) and Hydronn\(_{4,\text{All}}\) retrievals. The encoder and decoder of all Hydronn models comprise 5 stages. The number of internal features for all architectures was set to \( n_f = 128 \), which is probably low compared to other neural network architectures. This was mostly motivated by hardware limitations. Since it was found to be sufficient to achieve good retrieval performance, we did not investigate the impact of this decision further. Set to \( n_f = 256 \) and the number of Xception blocks in each encoder stage to \( N = 3 \).

All available collocations from the training period are used for the training and no distinction is made between day- and nighttime observations. The Adam optimizer (Kingma and Ba, 2014) with an initial learning rate of 0.0005, \( \beta_1 = 0.9, \beta_2 = 0.99 \) and a cosine-annealing learning rate schedule (Loshchilov and Hutter, 2016) is used for training. Warm restarts are performed every 20 epochs and repeated until the retrieval accuracy on a held-out part of the training data converges. Training of a single retrieval model takes about 3 days on an NVIDIA V40 GPU.

### 3.4 Probabilistic precipitation estimates

A defining characteristic of Hydronn is that precipitation is retrieved using a Bayesian framework. This means that, instead of predicting a single precipitation value, it provides an estimate of the full a posteriori distribution of the Bayesian retrieval problem. Hydronn builds on the findings from Pfreundschuh et al. (2018), which showed that probabilistic regression with neural network yields the same results as a traditional Bayesian retrieval using an a priori distribution that is the same as the training data of the neural network. Although Pfreundschuh et al. (2018) proposed to use used quantile regression neural networks (QRNNs) to perform Bayesian remote sensing retrievals with neural networks, a different approach is taken here. Following the work by Sonderby et al. (2020), the range of possible precipitation values is discretized and the probability neural network output is used to predict the probabilities of the observed precipitation falling into each bin is predicted by any of the precipitation bins. By normalizing the predicted probabilities by the width of the corresponding bin, a binned approximation of the probability density function (PDF) of the Bayesian a posteriori distribution can be obtained. We found this approach to
Calculating quantiles, logits the of approach was predicted than can be binned.

**Figure 4.** The neural network architecture used by the Hydronn$_{2, All}$ retrieval. For the Hydronn$_{4,IR}$ and Hydronn$_{4, All}$ retrievals the two additional stages for the processing of the higher-resolution inputs are omitted. Instead, the input comprises all input observations downsampled to four-kilometer resolution. Grey text in parenthesis gives the shape of the tensors at the various stages of the network using channel-first ordering and omitting the batch dimension. Grey, bold text specifies merge operations for data streams. Braces are used to mark the repetition of network components.

295 be equivalent to QRNNs in retrieval accuracy. However, calculating the distribution of the sum of two temporally independent predictions is easier on the binned PDF than on the predicted quantiles, which why the former approach was chosen for the implementation of Hydronn.

This approach we chose this approach, which we refer to for simplicity we refer to as density regression neural network (DRNN), can be easily because we didn’t find an efficient way to calculate the sum of two independent random variables from the quantiles predicted by a QRNN. For two PDFs given over discrete bins the sum can be calculated by weighing all possible sums of bin centers by the product of the corresponding probabilities, and accumulating the resulting probabilities into the bins of the result PDF.

DRNNs can be implemented by treating the retrieval as a classification problem over a discretized range of precipitation values and using a cross-entropy loss to train the network. During inference, the logits. The cross-entropy loss is defined as

\[ L(\hat{y}, y) = -\log(\hat{y}_{\text{bin}(y)}) \]  

(2)
where \( \mathbf{y} \) is the vector of probabilities predicted by the network are transformed into a probability density by applying a softmax activation and normalizing the bin probabilities, and \( \text{bin}(y) \) is the index of the probability bin corresponding to the true precipitation rate \( y \).

Hydronn predicts the a posteriori distribution over 128 logarithmically spaced bins covering the range from \( 10^{-3} \) to \( 10^3 \) mm h\(^{-1}\).

310 This upper limit of the bin range may be unrealistically large but using this range has the advantage that we can compute the sum of two distributions on the same bins as the predictions are made.

The reference precipitation of pixels without rain was set to a log-uniform random value between \( 10^{-3} \) and \( 10^{-2} \) mm h\(^{-1}\). While not strictly necessary for our approach, this Replacing zero values with small random values has the advantage of breaking the degeneracy of low-making the corresponding cumulative distribution function (CDF) continuous, which ensures that all quantiles of the posterior distribution, which makes it easier distribution are always well defined. This allows us to verify the calibration of the probabilistic predictions on the validation data probabilistic predictions from the network using calibration curves.

Since storing the full posterior distribution for all pixels is of little use for operational processing, only a reduced number of relevant statistics are retained in the retrieval output. Those are the posterior mean as well as a sample and 14 quantiles of the posterior distribution. Note that the quantiles are always located around the region of the posterior distribution that contains most of its mass and thus provide a much compacter way of storing the probabilistic retrieval results than the full 128 probabilities. In addition to providing a direct measure of retrieval uncertainty, the quantiles can be used to reconstruct a piece-wise linear approximation of the posterior cumulative distribution function (CDF). The predicted posterior of the retrieved distribution. The CDF can then be used, for example, to detect the exceedance exceedence of certain precipitation thresholds.

325 Compared to training a separate classifier to perform this task, this approach has the advantage that the precipitation threshold can be chosen during inference dependent on the application context after the network has been trained.

3.5 Calculation of hourly accumulations

The precipitation estimates produced by Hydronn correspond to instantaneous precipitation rates. Since GOES 16 imagery is available every 10 minutes, a method is required to accumulate the posterior, aggregate the retrieved, distributions of the instantaneous precipitation rates to hourly accumulations, which can then be compared to in order to compare them to the gauge measurements. While this is not an issue when only the posterior mean is predicted retrieved, it is unclear how the retrieval uncertainties should be aggregated accumulated in time. The problem is illustrated in Fig. 5 using six, consecutive retrievals at a single output pixel. The green lines show the retrieved distributions for each input observation. Because Hydronn has no way of modeling the correlations between consecutive observations it is not clear how the instantaneous distributions can be aggregated to a posterior distribution for the hourly accumulations.

In lack of a formal way to resolve this, we have implemented two heuristics for calculating probabilistic estimates of hourly accumulations from instantaneous measurements.

The first heuristic is to simply average the predicted posterior distributions. For the case of multiple identical observations, this preserves the retrieval uncertainties and thus corresponds to the assumption of strong dependence of the retrieval errors for
consecutive observations. The second approach is to assume temporal independence of the retrieval uncertainty. For identical, consecutive observations this will generally cause the retrieval uncertainty to decay. Given the binned probability densities of two independent random variables, the PDF of their sum can be approximated by calculating weighted histograms of the outer sum of the bin centroids weighted by the product of the bin probabilities.

The blue and red curves in Fig. 5 show the resulting posterior distributions of the hourly accumulations for the assumptions of dependent errors and independent errors, respectively. Despite the differences in the two distributions they both have the same mean value. Under the assumption of temporal independence, the instantaneous retrieval errors have a tendency to compensate for each other, which reduces the retrieval uncertainty. Conversely, strongly dependent errors have a tendency to conserve the uncertainty of the instantaneous retrievals resulting in higher probabilities assigned to stronger precipitation.

![Figure 5](image.png)

**Figure 5.** Retrieved posterior distributions of instantaneous precipitation (green, solid lines) for an hour of ABI observations. The corresponding derived distributions for the hourly accumulations are shown in red and blue for the assumptions of dependent and independent errors, respectively.

For the evaluation of the Hydronn retrieval, we calculate PDFs of hourly accumulations using both approaches. Two types of accumulations are thus produced for each Hydronn configuration: One corresponding to the assumption of dependent retrieval errors, which will be identified with the qualifier '(dep.)', as well as one corresponding to the assumption of independent retrieval errors, which will be identified with the qualifier '(indep.)'. Since the assumptions only affect the predicted retrieval uncertainties and not the predicted mean values, such a distinction is not required when point estimates of precipitation are considered.

### 3.6 Correcting for a priori data assumptions

According to Bayes theorem, the posterior distribution of retrieved precipitation $p(x|y)$ for given input observations $y$ is proportional to the product of the probability of observing $y$ for a given precipitation rate $x$ and the a priori probability of $x$:

$$p(x|y) \propto p(y|x)p(x)$$  \hspace{1cm} (3)
One difficulty with machine learning based retrievals is that the a priori distribution cannot be chosen freely but is dictated by the training data distribution. Fig. 3 indicates that there are inconsistencies between the training data and gauge measurements. For example, the retrieval will learn from the training data that the probability of precipitation values between $10^{-1}$ and $10^{-2}$ mm h$^{-1}$ is effectively zero.

This raises the question whether it is possible to correct for the effect of the a priori assumptions encoded in the training data of the retrieval. To explore this, we propose the following method to correct the probabilistic predictions. Let $p_{\text{Gauges}}(x)$ denote the PDF of precipitation as measured by the available gauges shown in Fig 3 (b). Moreover let

$$r(x) = \frac{p_{\text{Gauges}}(x)}{p(x)}$$

(4)

denote the ratio of the PDFs of the gauge and the a priori distribution of precipitation as defined by the training data. Assuming that $p_{\text{Gauges}}(x) = 0$ wherever $p(x) = 0$ and that the conditional distribution $p(y|x)$ of the observations remains unchanged, a corrected posterior distribution can be obtained by point-wise multiplying the likelihood ratio $r$ with the posterior distribution predicted by Hydronn:

$$p_{\text{Corrected}}(x|y) \propto p(y|x)r(x)p(x),$$

(5)

The difficulty with this approach is that we only know the a priori distribution of retrieved hourly accumulations is not necessarily the distribution of instantaneous rain rates corresponding to the instantaneous precipitation retrievals, i.e., the distribution of the training data, but not for the hourly accumulations retrieved using Hydronn. To infer them, we calculated hourly accumulations for randomly sampled hours over the full year of 2019 for each retrieval configuration. The resulting correction factors for the Hydronn retrievals are displayed in Fig. 3, but depends on how these accumulations are calculated. This leads to a different a priori distributions for each of the two methods used to accumulate the precipitation (see Sec. 3.5). For the assumptions of temporally dependent retrieval uncertainties, the a priori is identical to that.

4 Results

This section evaluates the Hydronn retrievals in three steps. First, the accuracy of the instantaneous rain rates. For the assumption of temporally independent retrieval uncertainties, however, the a priori corresponds to the distribution of the mean of 6 consecutive draws from this distribution.

An issue that we encountered here is precipitation estimates with respect to the GPM CMB reference data is assessed and compared to the GPROF GMI and HYDRO retrievals. Second, the limited numerical resolution of the gauge measurements of 0.2 mm h$^{-1}$, which causes problems when the calibration of probabilistic predictions is evaluated against the gauge measurements. To counteract this, we have added numerical noise to the gauge measurements: Uniform random values from the range $[-0.1,0.1]$ are added to all non-zero measurements, while zero values are replaced by log-randomly distributed values from the range $[10^{-3},5 \times 10^{-3}]$. This slightly increases the mean of the precipitation by about 2%, but this is likely negligible compared to other uncertainties that affect precipitation retrievals-retrieved precipitation accumulations from June and December 2020.
Figure 6. A priori distributions of hourly accumulations and derived correction factors $r$ for the Hydromn$_{4,AB}$ retrieval. Panel (a) displays the a priori distributions of hourly precipitation accumulations derived assuming strong temporal dependence of measurements (blue) and complete independence (red). The gray, dashed line shows the PDF of the gauge measurements. Panel (b) displays the corresponding correction factors for the two assumptions calculated as the ratio between the respective PDFs and the PDF of the gauge measurements.

are evaluated against gauge measurements and compared to accumulations from HYDRO, IMERG, and PERSIANN CCS. Third, a case study of a heavy, flood-producing precipitation event is presented. Definitions of the metrics used to evaluate the retrievals are provided in Appendix A1.

A priori distributions of hourly accumulations and derived correction factors $r$. Panel (a) displays the a priori distributions of hourly precipitation accumulations derived assuming strong temporal dependence of measurements (green) and complete independence (blue). The gray, dashed line shows the PDF of the gauge measurements. Panel (b) displays the corresponding correction factors for the two assumptions calculated as the ratio between the respective PDFs and the PDF of the gauge measurements.

4.1 Instantaneous precipitation estimates

The a priori distributions and corresponding derived correction factors are displayed.

4.1.1 Case study

As first step in the evaluation of the instantaneous precipitation estimates, we consider retrieved precipitation for an overpass of the GPM satellite over a meso-scale convective system (MCS) in the border region between Argentina, Paraguay and Brazil on 16 December 2020, 13:59:00 UTC. The retrieval results are displayed together with a natural color composite in Fig. 6. It is apparent that the assumptions of temporally dependent uncertainties yields better agreement with the gauge data than the assumption of temporally independent uncertainties. The resulting correction factors are thus closer to the $y = 1$ line for the dependence assumption. We found that it was necessary to truncate the correction factors corresponding to the independence
assumption at $r = 10^{-3}$ because larger values would amplify numerical noise leading to the rare occurrence of unrealistically high precipitation values, which would distort the retrieval results. The GPROF GMI and IMERG retrievals exhibit good agreement with the GPM CMB results. This is expected, not only because GPROF and IMERG incorporate PMW observations, but also because GPM CMB is used to derive the retrieval database used by GPROF, and GPROF is in turn used by IMERG.

The HYDRO retrieval, on the other hand, does not agree well with the GPM CMB results. The heavy precipitation retrieved by HYDRO is located in the western part of the MCS, whereas the GPM CMB shows the very heavy precipitation in the north-eastern parts of the system. The Hydronn4_1IR retrieval captures the overall structure of the MCS better than HYDRO but fails to represent its smaller-scale structures. Both, the Hydronn4_All and Hydronn2_All, retrievals improve upon this and yield results that are very similar to those of GPROF GMI and IMERG.

![Figure 7](image.png)

**Figure 7.** A mesoscale convective system over the border region between Argentina, Paraguay, and Brazil on 16 December 2020 observed by GPM and GOES 16. Panel (a) shows a natural color composite (generated using (Raspaud et al., 2021)). Panel (b) shows retrieved surface precipitation from CMB retrieved using combined radar and passive microwave observations. Panel (b) shows precipitation retrieved by GPROF GMI using only passive microwave observations. Panel (c) shows the surface precipitation from the IMERG Final product. Panel (d) shows surface precipitation retrieved by HYDRO from GOES ABI observation. Panels (e), (f), (g) show the corresponding results from the three Hydronn configurations.

Accuracy metrics for the the MCS overpass with respect to the CMB reference data are provided in Table 2. Hydronn4_1IR and Hydronn2_All both exhibit dry biases of the same magnitude as HYDRO and Hydronn4_All even exceeds those. However, all Hydronn retrievals yield significantly more accurate results than HYDRO in terms of the other metrics. The Hydronn2_All retrieval even surpasses IMERG in terms of MSE, MAE, and CSI and achieves results close to those of GPROF GMI.
5 Results

Table 2. Retrieval accuracy metrics for the MCS overpass shown in Fig. 7. Definitions of all metrics can be found in appendix A1.

<table>
<thead>
<tr>
<th>Retrieval</th>
<th>Bias</th>
<th>MAE [mm h(^{-1})]</th>
<th>MSE [(mm h(^{-1}))^2]</th>
<th>Correlation</th>
<th>POD</th>
<th>FAR</th>
<th>CSI</th>
</tr>
</thead>
<tbody>
<tr>
<td>Hydro</td>
<td>-0.598</td>
<td>2.495</td>
<td>46.291</td>
<td>0.228</td>
<td>0.707</td>
<td>0.169</td>
<td>0.618</td>
</tr>
<tr>
<td>GPROF GMI</td>
<td>-0.163</td>
<td>1.699</td>
<td>27.467</td>
<td>0.552</td>
<td>0.998</td>
<td>0.519</td>
<td>0.481</td>
</tr>
<tr>
<td>IMERG</td>
<td>0.28</td>
<td>2.204</td>
<td>40.664</td>
<td>0.429</td>
<td>0.973</td>
<td>0.213</td>
<td>0.77</td>
</tr>
<tr>
<td>Hydronn4,IR</td>
<td>0.612</td>
<td>2.36</td>
<td>30.768</td>
<td>0.506</td>
<td>0.901</td>
<td>0.192</td>
<td>0.74</td>
</tr>
<tr>
<td>Hydronn4,All</td>
<td>0.813</td>
<td>2.362</td>
<td>33.038</td>
<td>0.524</td>
<td>0.916</td>
<td>0.138</td>
<td>0.798</td>
</tr>
<tr>
<td>Hydronn2,All</td>
<td>0.57</td>
<td>2.105</td>
<td>29.918</td>
<td>0.564</td>
<td>0.922</td>
<td>0.14</td>
<td>0.801</td>
</tr>
</tbody>
</table>

This section presents the evaluation of the Hydronn retrievals, which is split into three parts. The first part analyzes the nominal performance of the three Hydronn configurations on the held-out test data. The second part compares the retrieved hourly accumulations to the gauge measurements and the reference precipitation algorithms. Finally, the third part presents a case study of a heavy precipitation event that occurred during the validation period. Evaluation indicates that, while the total amount of precipitation remains less accurate for Hydronn than for the PMW retrievals, the spatial structure of the retrieved precipitation is captured equally well. Moreover, it should be noted that the revisit time for the GPM constellation of PMW sensors at these latitudes is around 1 h (Hou et al., 2014). Hydronn, however, can provide precipitation retrievals every 10 min. While increasing the temporal coverage of the precipitation measurements is also what IMERG aims to achieve by merging PMW retrievals with observations and retrievals from geostationary sensors, this seems to lead to a degradation of the accuracy of the precipitation estimates. To further illustrate the capabilities of the Hydronn retrievals a video of precipitation estimates for the MCS case is provided as a digital supplement to this manuscript (Pfreundschuh, 2022b).

4.1 Evaluation of Hydronn configurations

4.0.1 Accuracy over target region

To obtain an unperturbed assessment of the relative performances of the three Hydronn configurations, we evaluate the performance on the test data, which was derived from the same source (albeit during a different time period) and is therefore guaranteed to have similar statistics as the accuracy of the instantaneous precipitation estimates of Hydronn, we use collocations with GPM CMB from all GPM overpasses of the year 2020 over the target region, i.e., the region to which the training data—Hydronn training data was restricted (R1 in Fig. 2). The results of Hydronn are compared to HYDRO and GPROF GMI. Since GPROF retrievals can be directly collocated with the results from CMB and because GPROF is used by IMERG, we chose GPROF GMI over IMERG for this comparison as it can be expected to provide a stronger baseline. This is corroborated by the case study presented above.
Fig. 8 displays the resulting PDFs of retrieved precipitation conditioned on the value of the reference precipitation. Due to the limited information content of the VIS/IR observations, there are significant uncertainties in all results. These lead to significant wet biases for lightly raining pixels and dry biases for strong precipitation.

Nonetheless, for all assessed algorithms, while all distributions exhibit noticeable spread, GPROF shows the best agreement with the reference data. Conversely, HYDRO hardly shows any sensitivity to the strength of the reference precipitation. For the Hydronn results, slight improvements between the three Hydronn configurations are discernible. While the Hydronn1,IR retrieval exhibits the weakest relationship between reference and retrieved precipitation, the Hydronn1,All configuration yields slightly more accurate results. This can be seen in the sharpening of the conditional PDFs for precipitation rates occurring between 2 and 20 mm h⁻¹ as well as an increase in the slope of the conditional mean retrieved precipitation for rain rates exceeding 2 mm h⁻¹. Clearer improvements in retrieval accuracy are observed for the Hydronn2,All configuration, which yields a slightly sharper distribution and an increased slope in the conditional mean of the retrieved precipitation for precipitation rates larger than 0.5 mm h⁻¹. Comparing the Hydronn2,All results to GPROF shows that the distributions are quite similar for precipitation rates below 10 mm h⁻¹. Above this threshold, GPROF shows better sensitivity to the reference rain rates whereas Hydronn2,All exhibits a stronger tendency to underestimation.

For a more quantitative analysis, Tab. ?? summarizes the retrieval performance using a range of accuracy metrics. The metrics considered here are the bias, mean absolute error (MAE), mean squared error (MSE), the mean of the continuous ranked probability score (MCRPS) and the correlation coefficient. Given a predicted cumulative distribution function $F$ and a reference value $x$, the continuous ranked probability score (CRPS) is defined as

$$\text{CRPS}(F, x) = \int_{-\infty}^{\infty} (F(x') - 1_{x' > x})^2 dx', $$

where $1_{x' > x}$ is the indicator function taking the value 1 where $x' > x$ and 0 otherwise. Fig. 9 displays accuracy metrics for the quantitative precipitation estimates for the full year of test data. The results confirm that Hydronn yields more accurate retrievals than HYDRO. Moreover, the Hydronn versions that use all ABI channels are close to GPROF in terms of their accuracy. All retrievals exhibit weak seasonal variability across all metrics but this does not affect their relative performance significantly.

The 14 quantiles that are produced as retrieval output are used to calculate the CRPS instead of the full predicted PDF, which ensures that the evaluation is representative of the actual retrieval output. In contrast to the other metrics considered in Tab. ??, the CRPS takes into account not only:

### 4.0.2 Accuracy over northern hemisphere

The neural network models used by Hydronn were trained using only observations over Brazil (R1 in Fig. 2). The results from the previous section indicate that Hydronn achieves significantly higher accuracy than HYDRO and even approaches the accuracy of the predicted posterior mean but both sharpness and calibration of the probabilistic precipitation estimates
**Figure 8.** PDFs of retrieved precipitation conditioned on the reference precipitation for GPROF GMI, HYDRO and the three Hydronn configurations. The purple line in each panel shows the mean of the retrieved surface precipitation conditioned on the value of the reference precipitation. (Gneiting and Raftery, 2007) GPROF GMI when all available ABI channels are used. This, of course, raises the question whether Hydronn still works outside the region used for its training.

Overall, To investigates this, we have evaluated the retrievals using collocations from the results from Tab. ?? confirm the tendencies observed in Fig 8. The retrieval accuracy increases as the information content in the input observations is increased. In absolute terms, the largest improvements are achieved when the inputs are extended from a single channel to all channels of the ABI1st, 6th, 11th, 16th, 21st and 26th day of every month of 2020 over the northern hemisphere (marked as R2 in Fig. 2). The results for GPROF and the Hydronn retrievals are displayed in Fig. 10. While the accuracy of GPROF is higher than over Brazil, the accuracy of all Hydronn configurations decreases. However, further improvements can be achieved by ingesting all observations at their native resolutions and retrieving precipitation at 2 km resolution. It should be noted that the test dataset contains observations from all times of the day, so these improvements are not constrained by the availability of daylight; the decrease remains relatively small compared to the improvements over HYDRO that were observed over Brazil. This suggests...
that the neural networks learned robust relationships between the ABI observations and surface precipitation that generalize to observations from outside their training domain.

Algorithm Bias mm h\(^{-1}\) MAE mm h\(^{-1}\) MSE (mm h\(^{-1}\))^2 CRPS Correlation Hydronn\(_{1,IR}\) 0.0009 0.1988 1.3356 0.1807 0.4343 Hydronn\(_{1,All}\) 0.0006 0.1626 1.1848 0.0865 0.5296 Hydronn\(_{2,All}\)

4.1 Validation against rain gauge data

In contrast to Hydronn, From the estimates of instantaneous precipitation we now turn to accumulated precipitation. Since all of the reference algorithms considered here neglect the probabilistic nature of the precipitation retrieval and provide only a single precipitation estimate. The evaluation of Hydronn against the reference algorithms is therefore performed in two steps. Firstly, value as retrieval result, we first assess the accuracy of the deterministic quantitative precipitation estimates is evaluated against the gauge measurements. Secondly Following this, the probabilistic estimates produced by Hydronn and their potential to improve the characterization of the observed precipitation are assessed.

4.1.1 Quantitative precipitation estimates

Accuracy metrics of all retrievals evaluated against the gauge measurements for hourly, daily and monthly precipitation means are provided in Table 3. In terms of correlations for hourly means, HYDRO yields the worst performance with a
correlation of 0.282 for June and 0.134 for December. It is followed by PERSIANN CCS with a correlation of 0.32 and 0.26. IMERG and Hydronn4,IR achieve similar accuracy for hourly estimates with a correlation around 0.4. The Hydronn4,All and Hydronn2,All retrievals further improve the accuracy with correlations, respectively. IMERG yields a correlation of 0.5 and 0.545, respectively. As the integration time increases, the 0.53 for June and 0.4 for December. All Hydronn retrievals yield higher correlations with Hydronn4,IR achieving 0.59 in June and 0.4 in December, Hydronn4,All 0.65 and 0.5, and Hydronn2,All 0.67 and 0.59. Hydronn4,IR has higher MAE for hourly accumulations than both HYDRO and IMERG in June and higher MSE than IMERG in both June and December. Except for this, however, the Hydronn retrievals generally yield more accurate results in terms of MSE and MAE for hourly accumulations than the other retrievals.

The accuracy of all retrievals improves as the accumulation time increases. For daily means, the ranking of the retrieval algorithms remains mostly the same as for hourly means. This is also the case for monthly means with the exception that the accuracy of IMERG increases and rises to the level of the best Hydronn configuration in terms of MSE and outperforms it in terms of MAE in June. A likely explanation for this is the calibration that is applied to the IMERG Final product, which matches it to monthly gauge measurements.

A graphical analysis of the accuracy of the retrieved daily accumulations is provided in Fig 11. In this representation, the large uncertainties that are present in all retrievals are evident. Nonetheless, the results confirm the general findings from the analysis above. The two conventional VIS/IR retrievals, HYDRO and PERSIAN CCS, yield the least accurate results. In par-

Figure 10. Accuracy metrics Retrieval accuracy with respect to GPM CMB for the three Hydronn configurations evaluated overpasses on test data. The value corresponding to the highest accuracy in 1st, 6th, 11th, 16th, 21st and 26th day of each column is marked using bold font. 

Figure 10. Accuracy metrics Retrieval accuracy with respect to GPM CMB for the three Hydronn configurations evaluated overpasses on test data. The value corresponding to the highest accuracy in 1st, 6th, 11th, 16th, 21st and 26th day of each column is marked using bold font. November of 2020 over the domain R2. Each panel shows the average of a metric over the full year as well as its seasonal variability.

The accuracy of all retrievals improves as the accumulation time increases. For daily means, the ranking of the retrieval algorithms remains mostly the same as for hourly means. This is also the case for monthly means with the exception that the accuracy of IMERG increases and rises to the level of the best Hydronn configuration in terms of MSE and outperforms it in terms of MAE in June. A likely explanation for this is the calibration that is applied to the IMERG Final product, which matches it to monthly gauge measurements.

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Table 3. Accuracy metrics for the retrieved mean precipitation compared to gauge measurements at different time scales. The best values in each column are marked using bold font. Definitions of all metrics are provided in appendix A1.

<table>
<thead>
<tr>
<th>Retrieval</th>
<th>Bias [mm h(^{-1})]</th>
<th>MAE [mm h(^{-1})]</th>
<th>MSE [(mm h(^{-1}))^2]</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Hourly</td>
<td>Daily</td>
<td>Monthly</td>
</tr>
<tr>
<td>HYDRO</td>
<td>-0.030</td>
<td>-0.555</td>
<td>0.208</td>
</tr>
<tr>
<td>PERSIANN CCS</td>
<td>0.088</td>
<td>0.035</td>
<td>0.382</td>
</tr>
<tr>
<td>IMERG</td>
<td>0.015</td>
<td>-0.013</td>
<td>0.282</td>
</tr>
<tr>
<td>Hydronn(_{4,IR})</td>
<td><strong>-0.023</strong></td>
<td><strong>-0.002</strong></td>
<td>0.227</td>
</tr>
<tr>
<td>Hydronn(_{4,All})</td>
<td>-0.034</td>
<td>0.084</td>
<td>0.059</td>
</tr>
<tr>
<td>Hydronn(_{2,All})</td>
<td>-0.031</td>
<td>0.084</td>
<td>0.058</td>
</tr>
</tbody>
</table>

June 2020

<table>
<thead>
<tr>
<th>Retrieval</th>
<th>Bias [mm h(^{-1})]</th>
<th>MAE [mm h(^{-1})]</th>
<th>MSE [(mm h(^{-1}))^2]</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Hourly</td>
<td>Daily</td>
<td>Monthly</td>
</tr>
<tr>
<td>HYDRO</td>
<td>-0.037</td>
<td>-0.32</td>
<td>0.215</td>
</tr>
<tr>
<td>PERSIANN CCS</td>
<td>0.096</td>
<td><strong>2.001</strong></td>
<td>0.398</td>
</tr>
<tr>
<td>IMERG</td>
<td>0.014</td>
<td>0.285</td>
<td>0.196</td>
</tr>
<tr>
<td>Hydronn(_{4,IR})</td>
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<td>0.189</td>
</tr>
<tr>
<td>Hydronn(_{4,All})</td>
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<td><strong>-0.006</strong></td>
<td>0.247</td>
</tr>
<tr>
<td>Hydronn(_{2,All})</td>
<td>0.011</td>
<td><strong>0.239</strong></td>
<td><strong>0.226</strong></td>
</tr>
</tbody>
</table>

December 2020

The spatial distribution of the biases of the monthly mean precipitation is displayed in Fig. 12. The For June, the results from all algorithms exhibit dry biases on the west coast of Brazil and in the south of the country. HYDRO and PERSIANN CCS exhibit the strongest biases, while they are weakest in IMERG and Hydronn\(_{4,IR}\).

The results for December are less homogeneous between algorithms. The strongest biases are observed in the PERSIANN CCS results, which strongly overestimate precipitation in central and northern Brazil. HYDRO and Hydronn\(_{4,IR}\), as well as to a lesser extent PERSIANN CCS, Hydronn\(_{4,All}\) and Hydronn\(_{2,All}\), exhibit a systematic dry bias in southern Brazil. Overall, the biases of IMERG are smallest in magnitude and exhibit the least extent of spatial correlation. However, the differences between IMERG and the best Hydronn configuration, Hydronn\(_{2,All}\), are small.
Figure 11. Scatter plots of gauge measurements against retrieved daily accumulations for the reference retrievals HYDRO, PERSIANN CCS, IMERG and the three Hydronn configurations. The first two columns show the results for June 2020. Columns three and four show the results for December 2020. Frequencies have been normalized column-wise to improve the visibility of heavy precipitation events.
Figure 12. **Mean**-Retrieved mean precipitation during June and December 2020. The first two columns show the results for June. Columns three and four show the results for December. Shading in the background of each panel shows the spatial distribution of the mean precipitation of the corresponding retrieval. Colored hexagons show the spatial distributions of the retrieval biases with respect to the gauge measurements.
Finally, we consider the derived retrieval daily cycles of precipitation, which are displayed in Fig. 13. From the reference retrievals, both IMERG and HYDRO IMERG yields the best agreement with the gauge measurements in both June and December. In June, the daily cycle is mostly flat with a weak peak around 14 h. IMERG reproduces this behavior well but exhibits a weak peak that is delayed by about two hours. In addition to exhibiting larger biases, the daily cycles derived from HYDRO and PERSIANN CCS show an increase of precipitation towards the afternoon, which is in disagreement with the gauge measurements. Hydronn4,IR and Hydronn4,All exhibit biases comparable to those of HYDRO and PERSIANN CCS but remain flat throughout the day. The Hydronn4,IR results track the gauge measurements almost exactly although the afternoon peak is delayed by about an hour.

Both Imerg and HYDRO yield relatively good agreement with the gauge measurements for December. IMERG is slightly closer to the gauge measurements during morning and early afternoon but overestimates precipitation in the afternoon and evening. HYDRO slightly underestimates precipitation during the first half of the day but its afternoon peak, despite being close in magnitude to that of the gauge measurements, is delayed by about three hours. PERSIANN CCS shows good agreement with the gauge measurements in the first half of the day but strongly overestimates the afternoon peak. All Hydronn configurations yield good agreement with the gauge measurements. The Hydronn2,IR configurations slightly overestimate precipitation before 10 am, while Hydronn4,IR underestimate the afternoon peak.

### 4.1.2 Probabilistic estimates

We now proceed to evaluate the probabilistic precipitation estimates that are produced by Hydronn. As explained in Sec. 3.5, two probabilistic estimates of the hourly precipitation rates were produced. The first one, (dep.), assumes strong dependence of retrieval errors for consecutive observations, while the second one, (indep.), assumes independent errors. In addition to that, for each of these predictions, a corrected distribution has been calculated for each of these predictions using the correction factors described in Sec. 3.6. This yields four probabilistic predictions for each Hydronn configuration. These predictions will be referred to with the configuration name and the qualifiers (dep.), (dep., corr.) for the predictions derived assuming dependent uncertainties with and without correction, respectively, and (indep.), (indep. corr.) for the corresponding predictions derived using the independence assumption.

We first consider the distribution of precipitation rates as measured by gauges and the retrieval algorithms, which is shown in Fig. 14. All reference retrievals overestimate the frequency of low and moderate rain rates while underestimating the frequency of high rain rates. For each Hydronn configuration, the distributions of the mean as well as a random sample from the retrieval posterior are displayed. The results for the three Hydronn configurations are almost identical to each other. For June, IMERG precipitation accumulations agree very well with the gauge measurements but fail to capture the heavy precipitation exceeding 20 mm h$^{-1}$. HYDRO and PERSIANN CCS underestimate the occurrence of light precipitation $<1$ mm h$^{-1}$. While HYDRO tends to underestimate moderate and heavy precipitation, the tail of the precipitation distribution is well represented by PERSIANN CCS.

The distribution of the posterior mean exhibits similar characteristics as the retrieved values of the reference retrievals. Although slightly closer to the distribution of gauge measurements, the uncorrected distribution of samples of retrieved mean
precipitation for the Hydronn retrievals is close to the gauge measurements up until precipitation of around $8 \text{ mm h}^{-1}$ but underestimates the frequency of heavier precipitation. When instead samples from the posterior distribution obtained assuming temporally independent errors still does not match the gauge distribution very well. This is are considered the representation of heavy precipitation is improved. However, for (indep.) the frequency of heavy precipitation events is still underestimated, which is slightly improved by the a priori correction but correction. Conversely, the correction of the (indep.) results of Hydronn_{4,IR} leads to an overestimation of moderate precipitation remains. Sampling from the posterior distributions corresponding to the assumption of temporally dependent uncertainties yields fairly good agreement with the distribution of gauge measurements. It is improved further by the a priori correction, which mostly improves the agreement at low and moderate rain rates heavy precipitation. The correction slightly improves the representation of very light precipitation for the (dep.) results of Hydronn_{4,All} and Hydronn_{4,All}.

For December, IMERG overestimates the frequency of light precipitation while they are well represented by HYDRO and PERSIANN CCS. All retrievals overestimate the frequency moderate precipitation. HYDRO and IMERG underestimate the
frequency of heavy precipitation, while PERSIANN CCS captures the tail of the distribution well. For the Hydronn retrievals the distribution of the retrieved mean precipitation is again similar to the distribution of IMERG except with a stronger tendency to underestimate the frequency of heavy precipitation. The sampling again recovers the heavy precipitation events. The correction slightly improves the frequencies of low and heavy precipitation but the effect remains small.

The deviations between missing heavy precipitation events in the distribution of retrieved posterior mean values and the reference distribution can the mean retrieved by Hydronn retrievals should thus be understood as an effect of the uncertainties in the retrieval results. These uncertainties lead to a lack of very high precipitation values in the distribution of retrieved means of the retrieval posterior. Because the information content of the VIS/IR observations is insufficient to accurately determine the strength of heavy precipitation events, the retrieved mean will always underestimate the heaviest of those events. When instead of the mean samples from the posterior distribution are considered, and the differences between the a priori and gauge measurement distributions are taken into account, the the extreme values of the distribution are correctly reproduced.

The assumption used to calculate the posterior distribution of hourly accumulations has a clear impact on the distribution of the retrieved precipitation rates. Assuming independent retrieval errors leads to an overestimation of the frequency of light precipitation at the expense of heavy precipitation, while assuming dependent errors has the opposite effect. It is interesting to note that for June the assumption of independent errors yields better agreement with the gauge measurements while for December it is the latter.

In addition to sampling from the posterior distribution, the retrieved quantiles can be used to derive confidence intervals for the predicted precipitation. Their reliability The reliability of the confidence interface for December 2020 is assessed in Fig. 22, which displays the calibration curves of the confidence intervals. While the 15 using calibration curves. The corresponding
Figure 15. Calibration of the confidence intervals derived using the quantiles of the retrieval posterior distribution predicted by each Hydronn configuration –for December 2020. Grey, dashed line in the background shows the expected results for perfectly calibrated results.

results for June can be found in Fig. A1 in the appendix. We discuss only the results from December here because the results from June are practically the same.

For the assumption of dependent retrieval errors leads to an overestimation of the uncertainties, assuming independent errors leads to underestimation. However, for both assumptions this is corrected by, the calibration curve tends to lie above the diagonal, which signifies that the true precipitation values fall into the predicted interval more often than expected. The retrieved confidence intervals thus overestimate the retrieval uncertainty. The opposite effect is observed for the assumption of independent errors. Applying the a priori correction – albeit some underestimation remains for the (indep.) results – improves the calibration for both assumptions.

The results presented in Fig. 15 use the modified gauge measurements described in Sec. 3.6 to which small random noise has been added to non-zero measurements and zeros were replaced with small random values. This was required because quantiles are ill-defined when the CDF of a quantity is discontinuous. So while the results above show that the predicted uncertainties from the Hydronn retrieval are well calibrated, they would not be when compared against the raw gauge measurements. However, since the modifications to the measured precipitation are well within their uncertainty this still demonstrates the meaningfulness of the shows that the predicted confidence intervals are meaningful.

The retrieved quantiles can also be used derive the probabilities of to estimate the probability that an observed pixel exceeding exceeds certain precipitation thresholds. This has been used to derive the probabilities of the hourly precipitation calculate the probabilities of hourly accumulations exceeding and 20 mm h⁻¹, which correspond roughly to the 99 and 99.9% of the CDF of precipitation rate 99.9 percentiles of the distribution of gauge measurements. The ability of the retrievals to detect high-impact precipitation events in December 2020 is assessed using precision-recall (PR) curves (see A1 for definition) in Fig. 16. The corresponding results for June can be found in Fig. A2 in the appendix. For the non-probabilistic retrievals the curves were generated using the predicted precipitation and classifying all pixel pixels above a varying threshold as exceeding the
sought-after precipitation rate. The corresponding curves for the Hydronn retrievals were obtained by varying the probability threshold above which a pixel is classified as an high-impact event.

For the detection of events exceeding 5 mm h\(^{-1}\), HYDRO again exhibits the least skill, followed by PERSIANN CCS. Compared to these two, IMERG performs clearly better. Also here, IMERG yields better results than the two conventional IR retrievals. The detection skill of Hydronn\(_{1,IR}\) is close to noticeably better than that of IMERG, while the two other configurations yield significantly better detection performance than IMERG. Further improve the detection performance. For events exceeding 20 mm h\(^{-1}\), all retrievals yield worse detection accuracy than at 5 mm h\(^{-1}\). Also here HYDRO exhibits the least skill, followed by PERSIANN CCS and IMERG, which yield very similar results. All Hydronn configurations outperform the reference retrievals.

Interestingly, the assumption used to accumulate the uncertainties as well as the a priori correction do not have a significant any noticeable effect on the detection skill. The reason for this is likely that the variation of the probability threshold for the generation of the PR curves has a stimulating effect on the retrieval results. For events exceeding 20 mm h\(^{-1}\), all retrievals yield worse detection accuracy. Also here HYDRO exhibits the least skill, followed by PERSIANN CCS and IMERG, which yield very similar results. All Hydronn configurations outperform the reference retrievals. PR curves are invariant to any transformation that preserves the ranking of the strength of the precipitation events. This means that, although the two assumptions may lead to different assigned probabilities, they both contain the same information on the strength of the observed precipitation event.

Since the Hydronn retrievals can be used to derive a probability of an observation exceeding a given precipitation threshold, a relevant question is how accurate these probabilities are. The calibration of the detection probabilities of events exceeding 5 mm h\(^{-1}\) is displayed in Fig. 22. While the 17 for December 2020 and Fig. A3 for June 2020 in in the appendix. For December, the predictions derived assuming temporally dependent uncertainties are fairly well calibrated. Larger deviations but larger deviations from the diagonal are observed for the probabilities derived assuming independent uncertainties. Moreover, while the correction marginally improves the calibration of the results for the dependent uncertainties, it degrades that of the probabilities derived assuming independent uncertainties. While the results are qualitatively similar across all Hydronn configurations, the detection probabilities increase in magnitude with the information content of the retrieval inputs, indicating that the sharpness of the probabilistic predictions increases. Nonetheless, even for an event with a threshold of only 5 mm h\(^{-1}\) probabilities do not exceed 60 %, which highlights the limitations of the VIS/IR based retrievals for the detection of extreme precipitation. For June, (dep.) yields the best calibrated results for Hydronn\(_{1,IR}\) while for Hydronn\(_{1,AIL}\) and Hydronn\(_{2,AIL}\) (indep.) yields the best calibration. However, the differences are relatively small and both assumptions yield reasonably well calibrated probabilities. The corrections only have a minor effect on the calibration and don’t lead to any consistent improvements.

### 4.2 Case study

As final part of this evaluation, a case of heavy precipitation in the city of Duque de Caxias in the State of Rio de Janeiro is considered, which occurred between the 22nd and 24th of 22 and 24 December 2020 and lead to floodings, flooding (Fohla De S. Paulo, 2020). About 250 mm of accumulated precipitation were measured by the rain gauge in the neighborhood of
Figure 16. Precision-recall curves for the detection of precipitation events with precipitation rates larger than 5 mm h\(^{-1}\) (first row) and 20 mm h\(^{-1}\) (second row) —in December 2020. Columns show the results for the reference retrievals as well as for each of the Hydronn configurations.

Xerém over the period of two days. An overview of the spatial distribution of retrieved accumulated precipitation over the two days is provided.

Gauge measurements and retrieved precipitation accumulations in the area surrounding the gauge in Xerém during the two days are shown in Fig. 18. Fairly good agreement is observed between IMERG and the Hydronn\(_{1,\text{all}}\) and Hydronn\(_{2,\text{all}}\) configurations. Hydronn\(_{1,\text{IR}}\) yields accumulations of slightly lower magnitude and is spatially less well defined than the two other Hydron retrievals. The accumulations from PERSIANN-CCS are lowest in terms of magnitude, whereas those from HYDRO are highest. However, neither of the two agrees well with the spatial distribution retrieved by IMERG or the Hydron retrievals. Both PERSIANN CCS and HYDRO exhibit systematic dry biases in the region around Duque de Caxias compared to the gauge measurements, which is present to a lesser degree also in the results of Hydronn\(_{1,\text{IR}}\). This dry bias is less pronounced in the results of IMERG. The gauge measurements show localized occurrence of heavy precipitation in a number of gauges to the north and east of Xerém and light precipitation along the coast towards the south and east.

The HYDRO retrievals are very high in the north-east of the region but miss the precipitation that fell around Xerém. PERSIANN CCS misses nearly all of the precipitation that fell during the two days. In contrast, IMERG and the Hydronn retrieve more precipitation in the area around Xerém. In particular, Hydronn\(_{4,\text{all}}\) and Hydronn\(_{2,\text{all}}\) both capture the precipitation in the vicinity of Xerém well.
Calibration of the probabilistic precipitation event detection.

In addition to the PR curves, we have calculated commonly used detection metrics for all retrievals in order to simplify the comparison to other studies. These metrics include the probability of detection (POD, the fraction of events that were correctly detected), the false alarm rate (FAR, the fraction of all detections that are wrong) and the critical success index (CSI) for the detection of events with more than 20 mm h\(^{-1}\). The results are displayed in Tab. ?? For the calculation of POD and FAR for the reference retrievals, a retrieved precipitation rate exceeding 20 mm h\(^{-1}\) is counted as a detection. For the Hydronn retrievals the probability threshold has been tuned to yield a FAR close to that of IMERG. As was to be expected from the PR curves in Fig. ??, HYDRO exhibits the least detection skill and does not detect any of the actual occurrences of strong precipitation but still produces false positives. Compared to this, IMERG does significantly better but suffers from a very low POD. PERSIANN performs better than IMERG in terms of POD but also has a higher FAR. The Hydronn retrievals achieve higher POD at lower FAR for all configurations. The POD of extreme precipitation increases markedly as more channels and higher resolution are incorporated. Similar results are observed for the CSI.

![Error metrics for Calibration of the probabilistic precipitation event detection of precipitation events with rain rates exceeding 20 mm h\(^{-1}\).](image)

<table>
<thead>
<tr>
<th>Retrieval</th>
<th>POD</th>
<th>FAR</th>
<th>CSI</th>
</tr>
</thead>
<tbody>
<tr>
<td>PERSIANN</td>
<td>0.006</td>
<td>0.987</td>
<td>0.004</td>
</tr>
<tr>
<td>CCS</td>
<td>0.039</td>
<td>0.926</td>
<td>0.026</td>
</tr>
<tr>
<td>HYDRO</td>
<td>0.000</td>
<td>1.000</td>
<td>0.000</td>
</tr>
<tr>
<td>IMERG</td>
<td>0.18</td>
<td>0.867</td>
<td>0.016</td>
</tr>
<tr>
<td>(dep.)</td>
<td>0.005</td>
<td>0.803</td>
<td>0.063</td>
</tr>
<tr>
<td>(dep., corr.)</td>
<td>0.121</td>
<td>0.811</td>
<td>0.080</td>
</tr>
<tr>
<td>(indep.)</td>
<td>0.079</td>
<td>0.806</td>
<td>0.059</td>
</tr>
<tr>
<td>(indep., corr.)</td>
<td>0.076</td>
<td>0.798</td>
<td>0.058</td>
</tr>
<tr>
<td>PERSIANN</td>
<td>0.109</td>
<td>0.800</td>
<td>0.076</td>
</tr>
<tr>
<td>CCS</td>
<td>0.133</td>
<td>0.808</td>
<td>0.085</td>
</tr>
<tr>
<td>HYDRO</td>
<td>0.167</td>
<td>0.801</td>
<td>0.100</td>
</tr>
<tr>
<td>IMERG</td>
<td>0.145</td>
<td>0.800</td>
<td>0.092</td>
</tr>
<tr>
<td>(dep.)</td>
<td>0.242</td>
<td>0.799</td>
<td>0.123</td>
</tr>
<tr>
<td>(dep., corr.)</td>
<td>0.270</td>
<td>0.804</td>
<td>0.128</td>
</tr>
<tr>
<td>(indep.)</td>
<td>0.267</td>
<td>0.799</td>
<td>0.129</td>
</tr>
<tr>
<td>(indep., corr.)</td>
<td>0.242</td>
<td>0.801</td>
<td>0.123</td>
</tr>
</tbody>
</table>
It is notable that the Hydronn4,All and Hydronn2,All retrievals exhibit considerably finer structures in their results than IMERG or the other retrievals. Moreover, these structures agree well with the gauge measurements. This suggests that the high resolution of the VIS/IR observations allows the retrieval to better resolve small-scale precipitation events.

**Figure 18.** Retrieved precipitation accumulations for an extreme precipitation event in the city of Duque de Caxias in the state of Rio de Janeiro. Shading in background: Panel (a) shows the accumulated gauge-measured precipitation between 2020-12-22 00:00 to 2020-12-24 00:00. Colored markers show the relative bias accumulations using colored hexagons. Locations of the retrieved accumulated precipitation compared to gauges are marked using red points. The green-red star marks the location of Xerém, where the Xerém neighborhood of Duque de Caxias in which the gauge station closest to the reported flooding occurred is located. The remaining panels show the retrieved precipitation accumulations for the tested retrieval algorithms.

The rain rates at the gauge station in Xerém (location marked by green-red star in Fig. 18) are displayed in Fig. 19. The plots show the hourly precipitation rates retrieved by the reference retrievals as well as the mean and posterior distribution for all Hydronn retrievals. Only results obtained with the assumption of dependent retrieval uncertainties and the a priori correction applied are shown. The precipitation measured at the rain gauge far exceeds the precipitation measured by any of the reference retrievals or the retrieved mean of the Hydronn retrievals. The Hydronn retrievals predict elevated uncertainties for the period during which the strongest precipitation is observed. However, the precipitation peaks still exceed the 99th percentile. Two factors may explain that more than the expected 1 % of gauge measurements lie outside the predicted uncertainty range. Firstly, the observations considered here are not randomly sampled but correspond to an event that is known to be extreme. Secondly, as stated in the article in Fohla De S. Paulo (2020), heavy precipitation events are common in this region. This may
indicate that regional factors may act to intensify the precipitation, which is unlikely to be captured in the training data of the retrieval.

Nonetheless, an encouraging result is that the predicted value of the 99th percentile increases with the information content in the retrieval input. This indicates that the neural network can leverage the additional information to produce sharper uncertainty estimates better represent the uncertainty in the retrieval.

![Figure 19](image-url) Retrieved precipitation for an extreme precipitation event that occurred between 2020-12-22 December 22, 2020 and 2020-12-24 December 24, 2020, in the city of Duque de Caxias in the state of Rio de Janeiro. Grey, dashed lines show the precipitation by the gauge station in Xerém. Solid lines show the retrieved mean precipitation for each retrieval algorithm. The shading shows filled contours of the posterior CDF at values [0.01, 0.1, 0.2, . . . , 0.8, 0.9, 0.99].

5 Discussion

The study presented Hydronn, a neural-network-based precipitation retrieval for Brazil, which has been trained using combined radar and radiometer measurements from the GPM Core Observatory satellite. The retrieval compares core observatory. Using all ABI channels at their native resolution, the retrieval yields instantaneous precipitation estimates that are close in accuracy to those of GPROF GMI. The derived accumulations compare favorably against the currently operational precipitation retrieval, HYDRO, as well as the PERSIANN CCS product. In its best configuration the Hydronn retrieval yields retrieval accuracy superior to that of The configurations that use all ABI channels yield more accurate precipitation accumulations than the IMERG Final product across most considered metrics.
5.1 Information content of VIS/IR observations

The three tested retrieval configurations use input observation of increasing information content. The Hydronn\(_{4,\text{IR}}\) configuration only uses a single IR channel at a resolution of 4 km while Hydronn\(_{4,\text{All}}\) uses all available bands of the ABI. The best performing retrieval, Hydronn\(_{2,\text{All}}\), combines the observations from all channels of the GOES ABI at their native resolutions. Clear increases in retrieval performance are observed when all ABI bands are incorporated into the retrieval as well as an additional, albeit smaller, improvement is achieved when all channels are ingested at their native resolutions. This demonstrates the ability of the neural-network-based retrieval to learn complex relationships even from input observations with low information content efficiently combine observations across channels and different spatial scales. The fact that HYDRO and Hydronn\(_{4,\text{IR}}\) use the same observations as retrieval input further highlights the need for advanced statistical retrieval techniques to fully exploit the potential of geostationary VIS/IR observations. Demonstrates the significant improvement that neural-network-based retrievals can achieve compared to conventional methods. This is in good agreement with the findings from Sadeghi et al. (2019), who also report improvements when comparing PERSIANN CCS to a CNN-based retrieval.

The retrieval accuracy of Hydronn in its most advanced configuration is comparable to that of GPROF GMI at the 5 km resolution considered here. Certainly, it must be taken into account that the Hydronn retrievals are evaluated against the data they were trained to reproduce, which will tend to overestimate their accuracy with respect to independent measurements. However, this is also the case for GPROF GMI, whose retrieval database is to large extent built up of collocations with GPM CMB. This result is notable because VIS/IR observations from geostationary satellites are typically understood to merely ‘augment’ (Kidd et al., 2021) the more capable PMW sensors. While the case study from Sec. 4.1.1 indicates that the VIS/IR observation are still inferior in terms of their ability to quantify the total amount of precipitation, the structure of the MCS is truthfully represented. Leveraging the high temporal resolution of the GOES ABI observations, the retrieval easily outperforms all other tested algorithms in terms of hourly and daily accumulations with a considerable margin. This suggests that space-borne precipitation measurements may benefit significantly by making better use of available observations from geostationary satellites.

5.2 Probabilistic precipitation retrievals

A novel aspect of the proposed precipitation retrievals is their ability to provide probabilistic precipitation estimates. In this study we have demonstrated multiple ways in how this may improve the utility of the retrieval results:

1. The results in Fig. 14 show that samples from the retrieval posterior reproduce the gauge-measured distribution of rain rates fairly accurately more accurately than the retrieved mean. The deviations of the distribution of the posterior mean from the gauge measurements can thus be understood as a consequence of the statistical properties of this estimator instead of a retrieval deficiency. The random samples may be useful for applications that are sensitive to heavy precipitation rates, such as runoff modeling or climatological studies. As an example, Fig. 20 shows scatter plots of the 99th percentile of the distribution of gauge-measured and retrieved precipitation during December 2020 for all gauge stations. Also here the Hydronn retrievals yield the best estimates. For this evaluation, monthly
distribution of hourly accumulations at each gauge station and the 99th percentile of the corresponding retrievals for June and December 2020. HYDRO and PERSIANN CCS yield similar accuracy as IMERG, accuracy similar to IMERG in this analysis, despite IMERG having higher accuracy for all other metrics considered in this study. This is likely because both HYDRO and PERSIANN CCS were both developed to correctly represent heavy precipitation, which harms their accuracy in terms of other statistics, developed with a focus on convective precipitation. The regression relations underlying both retrievals were developed from summer precipitation in the US and enforce monotonically decreasing relationship (Hong et al., 2004; Vicente et al., 1998) between brightness temperatures and precipitation rates. This may explain why they succeed in representing heavy, convective precipitation events but fail to represent more general conditions. By explicitly resolving the probabilistic nature of the precipitation retrieval, HYDRONN can provide both climatologically accurate accumulations (see Table 3) and correct representation of heavy precipitation.

It should be noted, however, that these random samples do not take into account spatial correlations. To what extent this may negatively impact applications of the retrieval results remains to be investigated in a follow-up study.

2. The retrieved quantiles allow the derivation of confidence intervals to quantify retrieval uncertainty. By correcting for the difference in a priori distributions as well as the degeneracy of quantiles due to discontinuities in the CDF of gauge measurements, we were able to show that the retrieval uncertainties are well calibrated even against gauge measurements (Fig. 22). Due to the large uncertainties that are inherent to precipitation retrieval from VIS/IR observations (Fig. 8, 11), quantifying these uncertainties has the potential to increases the trustworthiness of the predictions.

3. We have shown that the retrieved quantiles can be used to detect heavy precipitation events (Fig. 22, Table 3). Here all Hydronn retrievals perform better than IMERG although they are based on observations with a significantly lower information content. This clearly shows the benefits of quantifying the retrieval uncertainties. Moreover, we were able to show that the probabilistic detection of these events is fairly well calibrated (Fig. 22, Fig. 17).

These results, however, also show the limitation of VIS/IR retrievals since even for events exceeding 5 mm h\(^{-1}\) the maximum detection confidence is 60%. This certainly puts the suitability of any of the considered retrievals to detect heavy precipitation events into question and calls for new approaches that combine observations from different observational sources.

Finally, we have also investigated how uncertainties from instantaneous precipitation retrievals can be propagated to the full hour. The two approaches that we have tested correspond to assuming temporally independent and temporally dependent retrieval uncertainties. Our results indicate (Fig. 14, Fig. 22) that the assumption of dependent uncertainties overestimates the actual retrieval uncertainty, whereas assuming independent uncertainties underestimates actual uncertainties. It is interesting to note that (Fig A1, Fig. 15). In lack of a better method to infer the distribution of hourly accumulations, our results indicate that assuming dependent uncertainties yields slightly more reliable results (Fig 15, Fig. A1, Fig. 17, Fig. A3). Moreover, it is encouraging that the way the uncertainties are accumulated—accumulations are calculated does not affect the detection of
Figure 20. The Scatter plots of the 99th quantile percentile of the monthly distribution of gauge measurements--hourly precipitation accumulations of each gauge station for June (blue) and December (red) plotted against the 99th quantile percentile of the corresponding retrieved distribution of retrieved precipitation accumulations. The results of the Hydronn retrievals use samples from the posterior distribution of hourly accumulations obtained assuming dependent retrieval errors instead of the posterior mean.

extreme overall detection skill for heavy precipitation events (Fig. 15), which indicates that the probabilities could also be re-calibrated a posteriori (16, Fig. A2).

5.3 Utility of a priori corrections

We have proposed a method to correct for variations in the distribution of precipitation rates in the training data. The corrections have improved the agreement between the distribution of retrieved precipitation rates as well as the calibration of the uncertainty intervals (Fig. 14, Fig. 15). Although for the assumed independent uncertainties the calibration was improved, the distribution of precipitation rates did exhibit slight deviations from the distribution of the gauge measurements. We suspect that the reason for the correction working worse in the latter case is that the a corresponding a priori assumption deviates stronger from the distribution of the gauge measurements (Fig. 6). This led to much higher correction factors, which were truncated to avoid numerical issues.

The clearest relative to comparable ground validation data, the most distinct effect of the a priori correction was observed when the predicted confidence intervals were evaluated against gauge data (Fig. 15, Fig. A1). This allowed us to show that
the Hydronn retrievals can provide well-calibrated uncertainty estimates for their predictions when the differences between the a priori distributions of the training data and the gauge measurements are taken into account. Nonetheless, the correction did not affect the detection of strong precipitation had only minor effects on the observed distribution of precipitation and did not improve the calibration of the detection of heavy precipitation events. We suspect the reason for this to be that the correction mostly affects small precipitation rates due to their high occurrence in the training and validation data as well as the re-calibrating effect of the varying probability threshold in the generation of the PR curves.

The correction relies on the assumptions that the conditional distribution of the observations vector \( p(y|x) \) given the rain rate \( x \) remains constant. It can thus only correct for differences in the measurement characteristics between the rain gauge data, which is used to evaluate the retrieval, and the GPM data, which was the probabilities of light precipitation, which because of their frequency have a strong effect on the calibration of the confidence intervals. However, the statistics used to derive the training data. It can not, however, correct for differences between the training and evaluation data that involves changes in the observed processes, which would change \( p(y|x) \). We argue that this is not an issue for this study since the evaluation and training data are overlapping geographically. Correction may not be precise enough to correct for the differences of the much rarer heavy precipitation events. Whether more specialized corrections that take into account seasonal variability can help with the detection of extreme precipitation remains to be investigated.

6 Conclusions

Hydronn, the presented neural-network-based precipitation retrieval, improves real time precipitation estimates over Brazil. Its performance is superior to both the currently operational algorithm as well as and the much more complex sophisticated, global IMERG Final product, which combines observations from both VIS/IR and passive microwave PMW sensors as well as global gauge measurements.

Our results demonstrate the potential of region-specific retrieval algorithms, which exploit the full potential of locally available satellite observations. This is made possible by the availability of accurate surface precipitation retrievals from the GPM CO-satellite core observatory, which were used to derived the training data for the retrieval. Since this data is available globally between \(-60^\circ \text{N} - 65^\circ \text{N} \) and \(65^\circ \text{N}\), the approach can potentially be applied to most many other regions around the world.

Although our evaluation focused on Brazil, many of the results presented here should be of interest for precipitation retrievals from geostationary satellites in general. In addition to providing further evidence of the potential of deep neural networks to improve quantitative precipitation estimates, we show We have shown that our retrievals work reasonably well even outside their training domain over Brazil. This indicates that, not only the regional training data, but also the ability of deep CNNs to leverage previously discarded, spectral and structural information from the satellite imagery contribute to the good performance of the Hydronn retrievals. Moreover, we have shown how a probabilistic regression approach can be used to perform VIS/IR precipitation retrievals using a Bayesian framework and that the probabilistic predictions improve the representation of the characteristics of the characterization of the observed precipitation.
Finally, the fact that our relatively simple retrieval outperforms state-of-the-art precipitation products despite being solely based on VIS/IR observations, shows the potential of algorithmic innovation—deep learning for quantitative precipitation estimation. The ability of the neural network retrieval to leverage information from all channels of the ABI at their native resolutions shows the strength of the end-to-end approach to retrieval design. This suggests that further improvements for precipitation retrievals should be achievable by expanding the retrieval input to incorporate additional spectral as well as temporal information. There is considerable room to improve space-borne precipitation estimates by making better use of currently available satellite imagery.

**Code availability.** The code to generate the training data, train the machine learning models, run the retrievals and analyze the results is available from a public repository (Pfreundschuh, 2022a).

**Video supplement.** A video of a full day of Hydronn retrieval compared to IMERG is provided as a supplement to this manuscript (Pfreundschuh, 2022b).

### Appendix A: Accuracy metrics

#### A1 Quantitative precipitation estimation

The metrics used in the study to assess quantitative estimates of surface precipitation are the bias, mean-absolute error (MAE), mean-squared error (MSE) and the Pearson correlation coefficient. Their definitions are provided in Table A1.

<table>
<thead>
<tr>
<th>Name</th>
<th>Calculation</th>
<th>Range</th>
<th>Best value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Bias</td>
<td>( \frac{\text{true} - \text{retrieved}}{\text{true}} )</td>
<td>(-\infty) to (\infty)</td>
<td>0</td>
</tr>
<tr>
<td>MAE</td>
<td>( \left</td>
<td>\frac{\text{true} - \text{retrieved}}{\text{true}} \right</td>
<td>)</td>
</tr>
<tr>
<td>MSE</td>
<td>( \left( \frac{\text{true} - \text{retrieved}}{\text{true}} \right)^2 )</td>
<td>0 to (\infty)</td>
<td>0</td>
</tr>
<tr>
<td>Correlation</td>
<td>( \frac{\text{true} - \text{retrieved}}{\text{true} - \text{true}} )</td>
<td>0 to 1</td>
<td>1</td>
</tr>
</tbody>
</table>

**Table A1.** Accuracy metrics used to assess the accuracy of quantitative precipitation estimates \( \text{true} \) against reference measurements \( \text{retrieved} \). Overbars are used here to denote the mean over all pixels in the test data set and \( \sigma_y \) to denote the standard deviation of the quantity \( y \).

The disadvantage of these metrics is that they neglect the probabilistic character of the Hydronn retrievals and do not provide any information on well uncertainties are represented. We use the mean of the continuous ranked probability score (MCRPS)
to assess the accuracy of probabilistic precipitation estimates. For a given, retrieved cumulative probability function \( F \) the continuous ranked probability score (CRPS) with respect to the reference value \( y_{\text{true}} \) is defined as

\[
\text{CRPS}(F; y_{\text{true}}) = \int_{-\infty}^{\infty} (F(x') - 1_{x > y_{\text{true}}})^2 \, dx,
\]

(A1)

For a perfect prediction of \( y_{\text{true}} \) without uncertainty, the predicted CDF \( F \) takes the form of a step function and the CRPS is zero. A CRPS larger than zero measures the deviation from this perfect prediction. The CRPS takes into account both sharpness and calibration of the probabilistic precipitation estimates (Gneiting and Raftery, 2007).

A2 Precipitation detection

To evaluate the skill of the retrievals to detect precipitation or precipitation exceeding a certain intensity we primarily rely on precision-recall (PR) curves. Since Hydron provides a probability that represents how likely an observed pixel contains precipitation, the classification is based on the probability exceeding a certain detection threshold. The detection threshold can be adapted to balance false positive against false negative errors.

Because of this additional degree of freedom, assessing the classification accuracy for a single classification threshold does not fully characterize the skill of the retrieval. PR curves overcome this limitation by displaying the precision, i.e., the fraction of true positives and the total number of predictions, and the recall, i.e., the fraction of all raining pixels that are correctly detected, for all possible detection thresholds.

Retrievals that only predict a single precipitation rate can be used for precipitation detection by counting all pixels with precipitation exceeding a certain threshold as raining. Here the precipitation threshold can be used like a detection threshold to balance false positives and false negatives. In this way a PR curve can be drawn also for those retrievals.

In addition to PR curves we will use the false alarm rate (FAR), probability of detection (POD) and critical success index (CSI) as scalar metrics. They are defined as follows:

\[
\text{FAR} = \frac{FP}{TP + FP},
\]

(A2)

\[
\text{POD} = \frac{TP}{TP + FP},
\]

(A3)

\[
\text{CSI} = \frac{TP}{TP + FP + FN},
\]

(A4)

where TP denotes the number of true positives, FP false positives, and FN false negatives.
Figure A1. Like Fig. A1 but for June 2020.
Figure A2. Like Fig. 16 but for June 2020.
Figure A3. Like Fig. 17 but for June 2020.
Author contributions. II, PE and SP designed the study. SP and II developed the retrieval and analyzed the retrieval results. SP prepared the manuscript. AC and DV provided the gauge measurements, HYDRO retrieval results and valuable feedback.

Competing interests. No competing interests are present.

Acknowledgements. We would like to acknowledge the Brazilian National Institute of Meteorology for the provision of the gauge measurements.

Computations for this study were performed using several freely available programming languages and software packages, most prominently the Python language (Python Language Foundation, 2018), the IPython computing environment (Perez and Granger, 2007), the numpy package for numerical computing (van der Walt et al., 2011). Xarray (Hoyer and Hamman, 2017) and satpy (Raspaud et al., 2021) were used for the processing of satellite data, PyTorch (Paszke et al., 2019) for implementing the machine learning models as well as matplotlib (Hunter, 2007) and cartopy (Met Office, 2010 - 2015) for generating figures.

The training of the machine learning models used in the study were performed on resources at Chalmers Centre for Computational Science and Engineering (C3SE) provided by the Swedish National Infrastructure for Computing (SNIC).


