



Bayesian age models and stacks: Combining age inferences from radiocarbon and benthic $\delta^{18}\text{O}$ stratigraphic alignment

Taehee Lee¹, Devin Rand², Lorraine E. Lisiecki², Geoffrey Gebbie³, Charles Lawrence⁴

¹Department of Statistics, Harvard University, Cambridge, USA

5 ²Department of Earth Science, University of California, Santa Barbara, 93106, USA

³Physical Oceanography Department, Woods Hole Oceanographic Institution, Woods Hole, 02543, USA

⁴Division of Applied Mathematics, Brown University, Providence, 02906, USA

Correspondence to: Devin Rand (drand@ucsb.edu), Taehee Lee (taehee_lee@fas.harvard.edu)

Abstract. Previously developed software packages that generate probabilistic age models for ocean sediment cores are
10 designed to use either age proxies (e.g., radiocarbon or tephra layers) or stratigraphic alignment (e.g., of benthic $\delta^{18}\text{O}$) and
cannot combine age inferences from both techniques. Furthermore, many radiocarbon dating packages are not specifically
designed for marine sediment cores and default settings may not accurately reflect the probability of sedimentation rate
variability in the deep ocean, requiring subjective tuning of parameter settings. Here we present a new technique for generating
Bayesian age models and stacks using ocean sediment core radiocarbon and benthic $\delta^{18}\text{O}$ data, implemented in a software
15 package named BIGMACS (Bayesian Inference Gaussian Process regression and Multiproxy Alignment of Continuous
Signals). BIGMACS constructs multiproxy age models by combining age inferences from both radiocarbon ages and benthic
 $\delta^{18}\text{O}$ stratigraphic alignment and constrains sedimentation rates using an empirically derived prior model based on 37 ^{14}C -
dated ocean sediment cores (Lin et al., 2014). BIGMACS also constructs continuous benthic $\delta^{18}\text{O}$ stacks via a Gaussian process
regression, which requires a smaller number of cores than previous stacking methods. This feature allows users to construct
20 stacks for a region that shares a homogeneous deep water $\delta^{18}\text{O}$ signal, while leveraging radiocarbon dates across multiple
cores. Thus, BIGMACS efficiently generates local or regional stacks with smaller uncertainties in both age and $\delta^{18}\text{O}$ than
previously available techniques. We present two example regional benthic $\delta^{18}\text{O}$ stacks and demonstrate that the multiproxy
age models produced by BIGMACS are more precise than their single proxy counterparts.

1 Introduction

25 The accuracy with which ocean sediment core data can reconstruct past climate events depends on the quality of the
core's age model (i.e., estimates of age as a function of core depth), yet age models are often constrained by only a single
dating proxy type. A common technique is radiocarbon dating, which directly dates individual sediment layers. However, this
method is restricted to the last 50 ka BP, suffers from variable surface reservoir ages (Waelbroeck et al., 2001; Sikes et al.,
2016; Stern & Lisiecki, 2013; Skinner et al., 2019), and is often low resolution causing the age model to be highly dependent
30 on assumptions regarding sediment accumulation rate variability. An alternative technique is the stratigraphic alignment of



benthic $\delta^{18}\text{O}$ to a target stack (e.g., Imbrie et al., 1984; Lisiecki & Raymo, 2005), which represents the mean benthic $\delta^{18}\text{O}$ signal across multiple cores. Benthic $\delta^{18}\text{O}$ is often measured at higher resolution than radiocarbon data but provides only relative age information between cores and temporal offsets between benthic $\delta^{18}\text{O}$ signals can introduce age errors during stratigraphic alignment (Skinner & Shackleton, 2005; Labeyrie et al., 2005; Waelbroeck et al., 2011; Stern & Lisiecki, 2014; 35 Lund et al., 2015).

Software packages exist to produce probabilistic age models using radiocarbon ages (Blaauw & Christen 2011; Loughheed & Obrachta, 2019) or benthic $\delta^{18}\text{O}$ alignments (Lin et al., 2014; Ahn et al., 2017), but none of these probabilistically combine age inferences from both dating techniques. Furthermore, many of these packages were not specifically designed for marine sediment cores (Ramsey, 1995; Haslett & Parnell, 2008; Blaauw, 2010; Blaauw & Christen 2011) and default settings 40 may not accurately reflect the probability of sediment accumulation rate variability in marine settings. Users must often subjectively choose parameter settings which may ultimately affect the interpretation of a study.

Here we present a new technique for generating Bayesian age models and stacks of ocean sediment core data, implemented in a software package named BIGMACS (Bayesian Inference Gaussian Process regression and Multiproxy Alignment of Continuous Signals). BIGMACS constructs multiproxy age models by combining age inferences from both 45 radiocarbon ages and $\delta^{18}\text{O}$ stratigraphic alignment. Radiocarbon ages directly date sediment layers while benthic $\delta^{18}\text{O}$ provides relative age constraints between radiocarbon ages and beyond 50 ka BP. BIGMACS can also probabilistically incorporate any additional age information at specified depths, such as inferences from tephra layers, magnetic reversals, or user-identified tie points. Sedimentation rates are realistically constrained with an empirically derived prior model rather than subjective parameter settings. BIGMACS constructs continuous benthic $\delta^{18}\text{O}$ stacks via a Gaussian process regression (Rasmussen and 50 Williams, 2006) that requires a smaller number of cores than previous methods (e.g., Ahn et al., 2017; Lisiecki & Stern, 2016). This feature encourages users to construct target stacks from neighboring cores that share homogeneous $\delta^{18}\text{O}$ signals, thus leveraging radiocarbon observations across multiple cores.

Section 2 provides a summary of some common techniques used for radiocarbon dating, $\delta^{18}\text{O}$ alignment and $\delta^{18}\text{O}$ stack construction. Section 3 describes the statistical methods used in BIGMACS, including an overview of the Bayesian 55 framework, the prior model that constrains sedimentation rates, and the likelihood models for different proxy types. We also describe the methods used to draw Markov Chain Monte Carlo (MCMC) age model samples and the regression technique employed to construct continuous stacks from a small number of cores. In section 4, we present two example regional Atlantic stacks: a Deep Northeast Atlantic (DNEA) stack, and an Intermediate Tropical West Atlantic (ITWA) stack. The two stacks are composed of 6 and 4 cores respectively, that are chosen based on an evaluation of their water mass histories. In section 60 5, we compare a multiproxy age model, a $\delta^{18}\text{O}$ -only age model, and a radiocarbon-only age model for one additional core. We demonstrate that age model precision is increased when using both radiocarbon ages and $\delta^{18}\text{O}$ alignment. Finally, we discuss potential future applications of BIGMACS and the factors affecting its runtime.



2 Background

2.1 Radiocarbon Age Models

65 Radiocarbon ages must be calibrated from ^{14}C years to calendar years with a calibration curve that accounts for
changes in past atmospheric ^{14}C production rates (Reimer et al., 2020; Heaton et al., 2020). The uncertainty of the calibrated
age is a combination of the calibration curve uncertainty, the radiocarbon measurement uncertainty, and the marine reservoir
age uncertainty. Techniques to calibrate radiocarbon ages have evolved from interpolation techniques such as Calib (Stuiver
& Reimer, 1993) to Bayesian calibration methods (e.g., Oxcal by Ramsey, 1995; Bcal by Buck and Christen, 1999; Matcal by
70 Lougheed & Obracht, 2016) which typically generate asymmetric, nonparametric calendar age distributions due to slope
changes in the calibration curve.

Planktonic foraminiferal radiocarbon dates must also be corrected for the reservoir age of the surface ocean. Previous
studies have used different methods to estimate past reservoir ages, including using modern measurements from the Global
Ocean Data Analysis Project (GLODAP, Key et al., 2004, Waelbroeck et al., 2019) and the Calib database (Reimer & Reimer,
75 2001), comparing stratigraphically aligned age models with radiocarbon age models (Stern & Lisiecki, 2013; Skinner et al.,
2021), and modelled reservoir ages from a Large Scale Geostrophic Ocean General Circulation Model (LGS-OGCM, Butzin
et al., 2020; Butzin et al., 2017, Langner & Mulitza 2019).

Constructing a sediment core age model, which estimates sediment ages for all core depths, from a sequence of
radiocarbon ages requires simulating the core's sedimentation rate. The median age model and age model uncertainty depend
80 on the radiocarbon calibration method, the applied sedimentation rate constraints, and the outlier identification procedure
(Christen, 1994; Ramsey, 2009b, Christen & Pérez, 2009). Multiple software packages have been published to construct
probabilistic radiocarbon age models that apply a variety of statistical techniques (e.g., Ramsey, 1995, 2001, 2008, 2013;
Blaauw & Christen, 2005; Haslett & Parnell 2008; Blaauw, 2010; Blaauw & Christen, 2011; Lougheed & Obracht, 2019).

Oxcal (Ramsey, 1995) provides modelling routines for multiple depositional environments; the routine known as the
85 P_Sequence is commonly used for modelling marine and lacustrine cores. P_Sequence uses a Poisson process in which the
number of depositional events per unit depth is determined by a user-specified parameter which affects the uncertainty of the
age model. Oxcal also includes multiple options to identify outliers, including an agreement index which measures the overlap
between the posterior distribution of the age model and the radiocarbon likelihood at depths where radiocarbon ages exist.

Bchron (Haslett & Parnell, 2008) constructs age-depth models using a monotone Markov process and piecewise linear
90 interpolation paths with random durations. While Bchron requires few user-specified parameter settings, the minimal
sedimentation rate constraints applied by the software package can result in age model samples that exhibit extreme
sedimentation rate variability. Age models constructed with Bchron often have confidence interval widths that are larger than
other software packages, particularly with radiocarbon records of low resolution (Blaauw & Christen, 2011). Bchron identifies
two types of outliers based on the shift required to satisfy the monotonicity constraint. Standard outliers have a prior probability



95 of 5% and require a shift defined *a priori* by a normal distribution with variance equal to double the radiocarbon analytical measurement error. Larger outliers have a prior probability of 0.1% and are excluded from the age model construction process.

Bacon (Blaauw & Christen, 2011) separates cores into fixed segments and uses an auto-regressive gamma process to simulate sedimentation rates. The user specifies priors for a beta distribution that controls age model autocorrelation and a gamma distribution that governs sedimentation rate variability. Radiocarbon ages are modelled with a generalized student's t-distribution (Christen & Pérez, 2009) that scales the error associated with radiocarbon measurements. The amount of scaling depends on two parameters which are set by default to assign a 70% chance that the reported error was underestimated by a factor between 1 and 2. Christen & Pérez (2009) explain that the choice of these parameter values is a “practical guideline” which they estimated to reflect the state of radiocarbon data at the time.

Undatable (Lougheed & Obrachta, 2019) uses a Monte Carlo sampling algorithm designed to emulate statistical models of sedimentation rate variability. Its quick runtime encourages parameter tuning through trial and error. Users set a scaling parameter that controls uncertainties at midpoints between radiocarbon ages as well as a bootstrapping percentage designed to handle outlying radiocarbon ages. These parameters have large effects on the resulting age model requiring the user to decide which age model is most appropriate based on trial and error rather than calculating an age model based on a prior model of sedimentation rate variability.

110 2.2 Benthic $\delta^{18}\text{O}$ Age Models

In the calcite tests of foraminifera, the ratio of ^{18}O to ^{16}O measured relative to a standard, denoted $\delta^{18}\text{O}$, is a proxy for global ice volume, local water temperature and the local $\delta^{18}\text{O}$ of seawater, which often correlates with salinity. Due to the relatively homogeneous temperature and salinity changes of the deep ocean, previous studies have assumed benthic $\delta^{18}\text{O}$ changes synchronously (Shackleton, 1967) and have used the proxy as a global stratigraphic signal to construct ocean sediment core age models (e.g., Pisias et al., 1984; Lisiecki and Raymo, 2005). The most conservative technique for aligning records to a target is to assume that large, easily identifiable features in the signals, such as glacial terminations, occurred simultaneously, create tie points between these features, and linearly interpolate between the tie points (e.g., Huybers & Wunsch, 2004). However, this linear interpolation method may misalign smaller scale features due to changes in sedimentation rates between tie points.

120 Software packages have been published that automate the alignment process and optimize the fit of the entire signal. Lisiecki & Lisiecki (2002) developed the deterministic software package Match, which utilizes dynamic programming to minimize a cost function based on sedimentation rate changes and the sum-of-square error misfit between signals. Match was used to align 57 benthic $\delta^{18}\text{O}$ records and construct the global “LR04” Plio-Pleistocene stack (Lisiecki & Raymo, 2005) and a 1.5-Myr multiproxy geomagnetic paleointensity and $\delta^{18}\text{O}$ stack (Channell et al., 2009).

125 The Bayesian package HMM-Match (Lin et al., 2014) performs a point-based alignment using a hidden Markov model and returns estimates of alignment uncertainty based on the distribution of Markov Chain Monte Carlo (MCMC) age model samples. HMM-Match considers the probability of every possible alignment given the fit to the alignment target and



the modelled sedimentation accumulation rate changes. The probability of a given benthic $\delta^{18}\text{O}$ residual to the target is modelled with a fixed Gaussian distribution based on the record's $\delta^{18}\text{O}$ residuals and a mean shift from the target.

130 Sedimentation rates are realistically constrained using a log-normal mixture distribution fit to observed normalized sedimentation rates derived by linearly interpolating between calibrated radiocarbon ages in 37 cores.

Diachronous benthic $\delta^{18}\text{O}$ signals are an additional source of uncertainty in benthic $\delta^{18}\text{O}$ aligned age models. Previous studies have identified temporal offsets up to 4 kyr between $\delta^{18}\text{O}$ records during terminations (Skinner & Shackleton, 2005; Lisiecki & Raymo, 2009; Stern & Lisiecki, 2014). Because stratigraphic alignment relies on the assumption that benthic $\delta^{18}\text{O}$ between the input and the target core varies synchronously, these offsets can cause age errors in $\delta^{18}\text{O}$ -aligned age models. Thus, without a direct dating proxy (e.g., radiocarbon, tephra, etc.), $\delta^{18}\text{O}$ stratigraphic alignment is an inadequate tool to study the sequence of climate responses at different locations during glacial terminations (e.g., Khider et al., 2017) or millennial-scale events. To mitigate the impacts of diachronous $\delta^{18}\text{O}$ change, benthic $\delta^{18}\text{O}$ alignment should ideally be restricted to cores which have experienced a similar history of deep water mass change.

140 **2.3 Benthic $\delta^{18}\text{O}$ Stacks**

Benthic $\delta^{18}\text{O}$ stacks are used as a common framework by which new paleoceanographic measurements are compared and are often used as targets during stratigraphic alignment (e.g., Imbrie et al., 1984; Lisiecki & Raymo, 2005; Channell et al., 2009). Stacks require that the individual $\delta^{18}\text{O}$ records are first aligned to have comparable relative or absolute ages so that each point in the stack represents a snapshot of $\delta^{18}\text{O}$ values from multiple locations at the same time. Inaccuracy in relative age estimates between cores will typically decrease the signal-to-noise ratio of the stacked signal, but over-alignment of noise in the signals could artificially enhance variability that was not globally synchronous. The risk of over-alignment can be reduced by placing constraints on sedimentation rate variability (e.g., Lisiecki & Lisiecki, 2002; Lin et al., 2014).

To create a stack using software that performs pairwise alignments of cores, all $\delta^{18}\text{O}$ records to be included in the stack are aligned to a single target core, which is typically a $\delta^{18}\text{O}$ record that spans the entire length of the stack with high resolution, low noise, and no apparent hiatuses. Any problems in the signal of the target core could propagate to create errors in core alignments and the average $\delta^{18}\text{O}$ value of the stack. In the LR04 global stack, the authors checked for such errors by performing pairwise alignments to multiple target cores and comparing the stacks (Lisiecki and Raymo, 2005); however, this is a laborious process and requires subjective evaluation. Because $\delta^{18}\text{O}$ variability is not globally synchronous (Skinner & Shackleton, 2005; Labeyrie et al., 2005; Waelbroeck et al., 2011; Stern & Lisiecki, 2014; Lund et al., 2015), Lisiecki and Stern (2016) created regional stacks and used a different alignment target for Atlantic versus Pacific cores.

The sensitivity of stacks to the choice of a single alignment target can be mitigated by aligning to a target that incorporates information from all cores in the stack. HMM-Stack (Ahn et al., 2017), which models the stack using a profile Hidden Markov model (HMM), begins with an initial alignment to a user specified target and then aligns all cores to an iteratively updated stack, which is optimized to fit all cores in the stack. Here we present a new stack construction algorithm



160 which offers several improvements to HMM-Stack, including the opportunity to simultaneously incorporate age constraints
from all cores during the stacking process.

3 Methods

3.1 Bayesian Framework

BIGMACS probabilistically constructs realistic age models and stacks by combining information from age proxies
165 and stratigraphic alignment with a prior model of sedimentation rate variability. In Bayesian statistics, the age information
from proxy data are termed the likelihoods. Specifically, the likelihood returns the probability of observing the age proxies
given the proposed age model and the set of model parameters. Here we refer to the likelihood as the emission model.
Simply stated, the emission model returns the probabilities of residuals (or misfit) between observed data and estimated
values from a particular age model. The emission model for each proxy (radiocarbon, $\delta^{18}\text{O}$, and additional age information)
170 is discussed in section 3.3 and detailed formulations are given in the supplement.

The sedimentation rate model is called a prior distribution. The prior calculates the probability of both the
normalized sedimentation rate for a particular depth in the core as well as any sedimentation rate change, given the model
parameters which are derived from the same sedimentation rate data as Lin et al., (2014). We refer to the prior distribution as
the transition model. The transition model calculates the probability of a simulated sequence of sedimentation rates,
175 independent of the proxy data, as described in section 3.2.

The posterior distribution is calculated using Bayes' rule and is proportional to the product of transition and
emission models. Because there is no closed form for this posterior distribution (i.e., it is not known), we employ a sampling
approximation. To improve computational efficiency, we sample the posterior using a combination of the particle smoothing
(Doucet et al. 2001; Klaas et al. 2006) and Metropolis Hastings algorithms (Metropolis et al. (1953); Hastings (1970);
180 Martino et al. (2015); section 3.4). The median age model and 95% confidence bands are calculated from the distribution of
age model samples.

The stacking algorithm is completed in two steps: an age model construction step in which a set of $\delta^{18}\text{O}$ records are
aligned in parallel to a target stack (as described above), and a stack construction step in which a nonparametric regression is
performed across the $\delta^{18}\text{O}$ data on the set of aligned cores. These two steps are performed iteratively until convergence. The
185 alignment target during age model construction is the stack from the previous iteration; for the first iteration, an initial target
stack is provided by the user. The stack construction process is described in more detail in section 3.5 and S5.

3.2 Transition Model

For a given age, the transition model calculates the probability of the normalized sedimentation rate and the change
in sedimentation rate from the previous depth (for a more detailed description, see S1 and S4.1). Probabilities for normalized
190 sedimentation rates are calculated with a prior distribution fit to observed sedimentation rates from 37 radiocarbon dated cores



(Lin et al., 2014). However, where the previous study interpolated sedimentation rates every 1 kyr, we interpolate by 1 cm depth increments and fit a new log-normal mixture distribution (Figure S1). Interpolating sedimentation rates by depth correctly represents the frequency at which higher sedimentation rates are observed in the sediment archive, whereas interpolating by time over represents frequency of lower sedimentation rates (which deposit less sediment per unit time).
195 Sedimentation rates are normalized relative to a time-dependent average sedimentation rate calculated using the Nadaraya-Watson Kernel (Langrene and Warin, 2019). This accounts for longer scale changes in the depositional environment, which can be associated with transitions between glacial and interglacial oceanographic conditions.

Changes in sedimentation rates depend on both the current and previous sedimentation rate, and thus the previous two depths. However, because storing all sampled combinations of three consecutive depths is intractable for computation
200 ($O(N^3)$, where N is the number of age model samples), normalized sedimentation rates are classified into three states: expansion, contraction, and steady. Expansion specifies a below average sedimentation rate and refers to a stretching of the local portion of the record. Contraction specifies a higher sedimentation rate than the average, which requires “squeezing” the record during alignment to the target. If the local sedimentation rate is within 8% of the core’s average, the state is classified as steady. The probabilities of transitioning from one state to the other states can either remain fixed using the sedimentation
205 rate data from Lin et al., (2014), or can be optimized via the Baum-Welch Expectation Maximization algorithm (Rabiner, 1989; Durbin et al., 1998).

BIGMACS allows a sedimentation rate change at every depth where there is proxy data ($\delta^{18}\text{O}$, ^{14}C , or additional age information). However, in the case of low-resolution records, BIGMACS imposes a minimum age model resolution, which forces a sedimentation rate calculation every 15 cm. This depth interval was selected based on the depth spacing between the
210 radiocarbon data used for the prior (Lin et al., 2014).

3.3 Emission Model

BIGMACS uses different emission models for radiocarbon, $\delta^{18}\text{O}$ and additional age information (see S2 and S4.1 for more information). For radiocarbon and $\delta^{18}\text{O}$ data, the emission model is specified via generalized student’s t-distributions (Christen & Pérez, 2009).

215 For radiocarbon data, the emission model returns the likelihood of observing age offsets from measured radiocarbon ages and depends on the radiocarbon measurement, calibration curve, and the reservoir age. The emission model also depends on two fixed parameters that control the scaling of the standard deviation. While Christen & Pérez (2009) and Blaauw & Christen (2011) set the fixed parameters of α and β to three and four, we choose values of ten and eleven which results in a distribution that is more similar to a Gaussian distribution. This effectively assigns smaller probabilities to large radiocarbon
220 residuals and improves agreement between the core age models and the radiocarbon observations.

The $\delta^{18}\text{O}$ emission model returns the likelihood of observing different magnitudes of $\delta^{18}\text{O}$ offsets from the alignment target and depends on the target stack’s time-dependent mean and variance. During alignment, Gaussian stacks are translated into a generalized student’s-t distribution with the fixed parameters of α and β set to three and four, respectively, based on



observed $\delta^{18}\text{O}$ residuals for the ITWA and DNEA stacks (Figure S2), to deal with potential $\delta^{18}\text{O}$ outliers. The $\delta^{18}\text{O}$ emission
225 model also includes core-specific scale and shift parameters which are learned across alignment iterations with the Baum-
Welch Expectation Maximization algorithm (Rabiner, 1989; Durbin et al., 1998). These parameters account for vital effects
among different benthic foraminifera species (e.g., Marchitto et al., 2014) and different local water mass properties at different
locations (e.g., temperature and $\delta^{18}\text{O}$ of seawater). The resolution-weighted average of the shift and scale parameters learned
for each core will have final values close to zero and one, respectively. In other words, the final mean and amplitude of the
230 stack will reflect a resolution-weighted average of the stack's component cores. Optionally, the user can choose not to shift or
scale individual cores during stack construction; with this setting, the variance in the stack would reflect the total $\delta^{18}\text{O}$ variance
between cores.

The emission model for the additional age information (e.g., stratigraphic tie points or dated tephra layers) can either
be specified as a uniform or Gaussian distribution with a mean and uncertainty specified by the user. Specifying the model as
235 a uniform distribution will force the age model to pass through the given uncertainty range and should be used when the user
is confident about the age information. Specifying a Gaussian distribution will allow the age model to pass farther from the
additional age constraint.

3.4 Record Alignment

This section describes the sampling strategy employed during age model construction and section 3.5 describes the
240 Gaussian process regression used to construct a stack. Formulations for both the sampling algorithms and stack construction
are provided in the supplement (S4.2 and S5).

Because the posterior is not given as a distribution in a closed form, age model samples are drawn using a Markov-
Chain Monte Carlo (MCMC) algorithm (Peters, 2008; Martino et al., 2015). To increase computational efficiency, BIGMACS
first initializes each sample using particle smoothing (Doucet et al. 2001; Klaas et al. 2006) and then refines the initialized
245 samples with the MCMC algorithm. Particle smoothing can be understood as a continuous version of a Hidden Markov model
(HMM, Durbin et al. (1998)). Whereas the HMM considers all possible hidden states because they are finite, the particle
smoothing considers only a finite number of proposals because there are infinitely many possible states. In BIGMACS, the
hidden states, or “particles”, represent possible ages for each depth in the core. Particle smoothing consists of a forward
algorithm and a backward algorithm. The forward algorithm iteratively samples and reweights particles, while the backward
250 algorithm samples from the particles one-by-one in reverse based on their assigned weights. BIGMACS first runs particle
smoothing with the state-space model defined by the transition and emission models.

BIGMACS then runs the Metropolis-Hastings algorithm (Metropolis et al. (1953); Hastings (1970); Martino et al.
(2015)) to sample the proposed ages from the particle smoothing algorithm as the starting points. The Metropolis-Hastings
algorithm updates the samples block-wise, meaning that hidden states in the same sedimentation state category (expansion,



255 contraction, and steady) are simultaneously treated in each iteration. Initialized age samples from particle smoothing allows
the use of shorter chains to reach the burn-in phase.

Once the set of sampled ages are obtained, BIGMACS updates parameters of the transition and emission models via
the Expectation Maximization (EM) algorithm (Dempster et al., 1977) and then iterates the process with the updated
transition and emission models until convergence. If a stack is to be constructed, the final age samples are inputs to the stack
260 construction algorithm.

3.5 Stack Construction Algorithm

During stack construction BIGMACS first aligns records to an initial $\delta^{18}\text{O}$ stack by drawing age model samples from
the posterior, and then updates the stack based on the new alignments. The updated stack serves as the target for the next
alignment iteration and the whole process is repeated until convergence.

265 A benthic $\delta^{18}\text{O}$ stack serves as a target for aligning multiple records simultaneously. Because age models are
continuous, we design the stack construction algorithm to also be continuous, such that a mean and standard deviation can be
defined explicitly for any age. Previous stack construction methods (Lisiecki & Stern 2016; Ahn et al., 2017) involved binning
 $\delta^{18}\text{O}$ data and were thus limited by the amount of data in each bin. In contrast, the continuous approach of BIGMACS allows
the creation of a stack using a smaller number of records and/or with uneven data resolution over time.

270 BIGMACS constructs a stack via a Gaussian process regression (Rasmussen and Williams, 2006), which is a
continuous and nonparametric kernel-based method. In contrast to the well-known polynomial regression, a distinctive feature
of a Gaussian process regression is that its variance function is permitted to change along the inputs (i.e. the x-axis). BIGMACS
uses the Ornstein-Uhlenbeck (OU, Rasmussen and Williams, 2006) kernel, which we find allows enough variance to resolve
millennial scale events (e.g., see sections 4.3 and 6.1.2). BIGMACS trains the OU kernel's hyperparameters, which adjust its
275 amplitude and width, across iterations based on the data used to make the stack.

To allow the stack to reflect changes in the variance of $\delta^{18}\text{O}$ as a function of time, BIGMACS follows a heteroscedastic
Gaussian process regression (Lee & Lawrence 2019). A homoscedastic Gaussian process assumes that the residuals of the data
from the regression is constant but nevertheless adjusts its variance function to the proximity of data points. Thus, its variance
function is narrow when data points are dense and wide where the data are less dense. A heteroscedastic Gaussian process
280 model has a variance function that changes in response to the spread of the data points along inputs which allows the variance
of the regression to be sensitive to the spread of responses in addition to changes in variance associated with data density from
the homoscedastic Gaussian process model.

Gaussian process regressions have two major drawbacks: time complexity and outlier sensitivity. A matrix inversion,
which has a time complexity equal to size of the data set cubed, is required to estimate hyperparameters for the kernel and to
285 compute the posterior predictions. Thus the model becomes intractable as the size of dataset increases. To address this,
BIGMACS adopts the variational free energy approximation (Titsias, 2009) to make the time complexity linear to the size of
dataset.



290 Outlier sensitivity results from the Gaussian modelling of residuals. During stack construction BIGMACS disregards outliers before performing the regression. The following two steps are iterated: 1) kernel hyperparameters are estimated after disregarding outliers, 2) outliers are classified by the stack which is constructed from the estimated kernel hyperparameters.

After BIGMACS obtains a Gaussian process regression using the $\delta^{18}\text{O}$ data from every core on each sample age model, the software averages the set of regressions using moment-matching (Murphy, 2012) to produce a single Gaussian model in a closed form. Detailed formulations for the stack construction algorithm can be found in the supplementary note (section S5).

295 4 Results

To demonstrate the performance of BIGMACS with differing amounts and quality of data, we present two example stacks: a Deep Northeast Atlantic (DNEA) stack and an Intermediate Tropical West Atlantic (ITWA) stack. The DNEA stack is constructed using high-resolution data with relatively little noise; it consists of 2,112 $\delta^{18}\text{O}$ data points and 150 radiocarbon ages from six cores that range in depth between 2273 and 3166 m (two from the western Iberian Margin and three off the west coast of Africa). The ITWA stack is constructed from 1,066 $\delta^{18}\text{O}$ data points and 51 radiocarbon ages across four cores from the Caribbean to the northern coast of Brazil that range in depth from 1100 and 1299 m; these cores contain a relatively large number of $\delta^{18}\text{O}$ outliers (Figure 1). The DNEA stack spans a full glacial cycle while the ITWA stack extends to ~55 ka. We used the Deep North Atlantic (DNA) and Intermediate North Atlantic (INA) stacks from Lisiecki & Stern (2016) as initial targets for the DNEA and ITWA stacks respectively. Default settings were used to construct both stacks. Additionally, we
305 construct radiocarbon-only and $\delta^{18}\text{O}$ -only age models for each input core to compare with the stack's multiproxy age models.

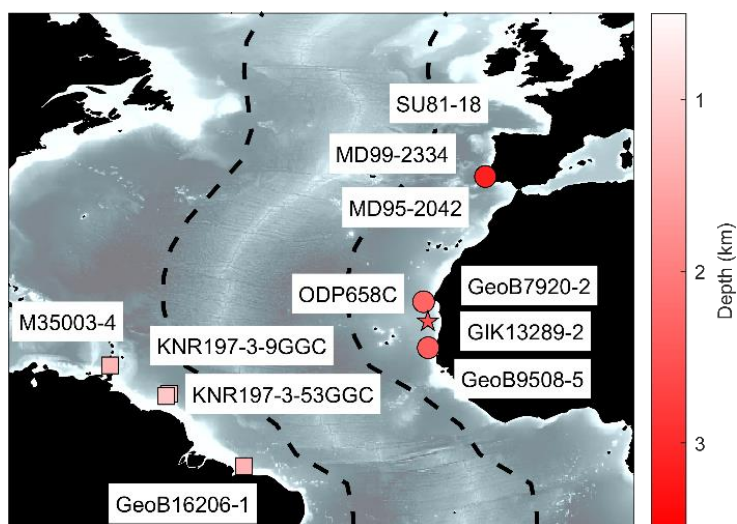


Figure 1: Cores used to construct the DNEA stack (circles) and the ITWA stack (squares). A star indicates the core for which we use the DNEA stack as the alignment target. Dotted lines indicate east and west transects plotted in Figure 2.



310

Core	Lat	Lon	Depth	¹⁴ C Citation	$\delta^{18}\text{O}$ Citation
DNEA					
MD95-2042	37.8	350	3146	Shackleton et al., 2004; Bard et al., 2017	Shackleton et al., 2000
MD99-2334	37.8	350	3166	Skinner & Elderfield, 2003; Skinner & Shackleton., 2004; Waelbroeck et al., 2019	Skinner & Shackleton, 2005
SU81-18	37.8	350	3135	Vogelsang et al., 2001;	Waelbroeck et al., 2001
GeoB7920-2	20.8	341	2278	Collins et al., 2011	Tjallingii et al., 2008
ODP658C	20.8	341	2273	deMenocal et al., 2000	Knaack & Sarnthein, 2005
GeoB9508-5	14.5	342	2384	Mulitza et al., (2008)	Mulitza et al., (2008)
ITWA					
M35003-4	12.1	299	1299	Hüls & Zahn, 2010	Hüls & Zahn, 2000
KNR197-3-53GGC	8.23	307	1272	Oppo et al., 2018	Oppo et al., 2018
KNR197-3-9GGC	7.93	306	1100	Oppo et al., 2018	Oppo et al., 2018
GeoB16206-1	-1.58	317	1367	Porthilo-Ramos et al., 2017	Voigt et al., 2017
Example					
GIK13289-2	18.1	342	2485	Sarnthein et al., 1994	Sarnthein et al., 1994

Table 1: Core locations and data citations.

4.1 Core Selection and Assessing Homogeneity

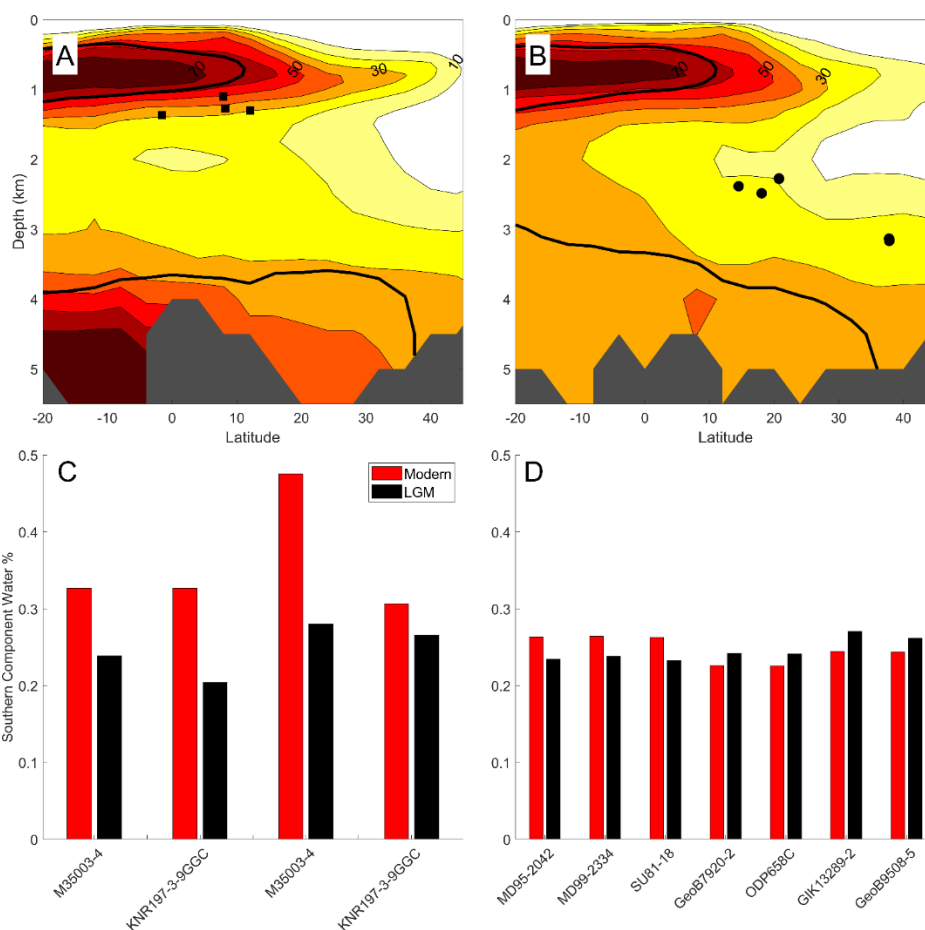
315 When choosing alignment targets or a population of cores to construct a stack, we suggest that researchers evaluate core locations with respect to water mass reconstructions and directly compare the features of the $\delta^{18}\text{O}$ time series to evaluate whether the algorithm's assumption of homogeneous $\delta^{18}\text{O}$ variability is reasonable. Before constructing a regional stack, the user should identify neighboring cores evaluated to have homogeneous $\delta^{18}\text{O}$ signals, or similar water mass histories. Figure 2 shows model estimates of the fraction of Southern Component Water (SCW) in two Atlantic transects, during the present day (coloured contours, Gebbie & Huybers, 2010) and at the LGM (solid black line, Oppo et al., 2018). Here SCW refers to water that formed in the Antarctic and sub-Antarctic regions defined by Gebbie & Huybers (2010).

325 Core sites in the DNEA stack are just below the core of modern Northern Component Water (NCW, Figure 2) and are bathed today by 23-26% SCW and 74-77% NCW (Table S1). Glacial water mass reconstructions suggest that water mass composition at these sites was very similar during the LGM (Gebbie & Huybers, 2010; Oppo et al., 2018). A relatively constant water mass composition during the deglaciation at these sites is also suggested by neodymium isotope compilations (Howe et al., 2016; Pöppelmeier et al., 2020). Collectively, these studies support our assumption that the benthic $\delta^{18}\text{O}$ signals of these cores changed homogeneously (i.e., nearly synchronously) during Termination 1.



The cores compiled for the ITWA stack are located near the boundary between AAIW and NADW, yielding more variability in their modelled water mass percentages. SCW percentages for cores in the ITWA stack range from 31-48% and 20-28% for the modern and LGM, respectively. During the deglaciation, AAIW experienced expansion in this region as demonstrated by a decrease in nutrients in the phosphate maximum zone (Oppo et al., 2018). Thus, the cores in the ITWA stack may have experienced moderately heterogeneous water mass changes during Termination 1. Despite moderate differences between these sites, BIGMACS is able to align these records and generate a stack that is representative of their $\delta^{18}\text{O}$ variability.

335



340

Figure 2: (A) Western and (B) Eastern Atlantic transects of water mass composition. Transect paths are shown as dotted lines in Figure 1. Colored contours show modern Southern Component Water percentages (Gebbie & Huybers 2010) along each transect and solid black line shows the 50% contour during the LGM (Oppo et al., 2018). Solid circles represent cores in the DNEA stack, squares are cores in the ITWA stack. Histograms of modern (red) and LGM (black) southern component water percentages for cores in the (C) ITWA and (D) DNEA stacks.



4.2 Age Proxies

To calibrate radiocarbon ages to calendar years, we use the Marine20 calibration curve (Heaton et al., 2020), a constant
345 reservoir age offset (ΔR) equal to zero, and a reservoir age standard deviation of 200 years. We make no corrections for the
different planktonic species used to measure radiocarbon in each core (see Table 1 for data citations).

For the longest core in each stack, we provide additional age information (crosses in Figures 4A and 5A) beyond the
last radiocarbon date. MD95-2042 in the DNEA stack is constrained with ages from Lisiecki & Stern (2016) identified based
on an alignment of the alkenone-based SST record (Pailler & Bard, 2002) to a synthetic Greenland $\delta^{18}\text{O}$ record on a speleothem
350 age model (Barker et al., 2011; Barker & Diz., 2014). M35003-4 in the ITWA stack is constrained by an age estimate of 55.4
ka BP at 9.5 m depth based on the alignment by Hüls & Zahn, (2000) of variations in *N. dutertrei* and CaCO_3 to
Dansgaard/Oeschger events in the GISP2 $\delta^{18}\text{O}$ record (Grootes & Stuiver, 1997). This additional age information is modelled
using Gaussian distributions with the standard deviations reported in Lisiecki & Stern (2016) for MD95-2042 and a standard
deviation of 1 kyr for M35003-4.

355 4.3 Stack Results

Figure 6 compares the DNEA and ITWA stacks. The ITWA stack is, on average, 0.56 ‰ lighter than the DNEA stack
due to the differences in deep water properties at the core sites. The ITWA core sites which span 1100-1299 m are bathed by
warmer and less saline waters than the DNEA cores from 2273-3166 m. The time-dependent standard deviation in each stack
(defined by the distribution of Gaussian Process regressions) reflects the variance in the aligned $\delta^{18}\text{O}$ records. Between 0 and
360 60 ka BP, the average standard deviation of the stacks is 0.13 ‰ in the DNEA and 0.2 ‰ in the ITWA. In particular, the ITWA
stack has larger standard deviation during the termination, which reflects anomalously high $\delta^{18}\text{O}$ values during the deglaciation
in some of the ITWA cores. For example, many of the records in the ITWA stack include several anomalously high $\delta^{18}\text{O}$ values
during the deglaciation; Oppo et al., (2018) attributes these outliers to slope instabilities at the Demerara Rise. Because
BIGMACS models a Gaussian distribution for $\delta^{18}\text{O}$ residuals, the outliers produce large, symmetric confidence intervals about
365 the mean.

The standard deviations of the two BIGMACS stacks are both smaller than the DNA and INA regional stacks from
Lisiecki & Stern (2016), which average 0.24 ‰ and 0.36 ‰, respectively. This likely stems from greater benthic $\delta^{18}\text{O}$ spatial
variability within the larger regions defined in Lisiecki & Stern (2016) and the application of (small) record-specific shift and
scale adjustments to the DNEA and ITWA cores during stacking with BIGMACS.

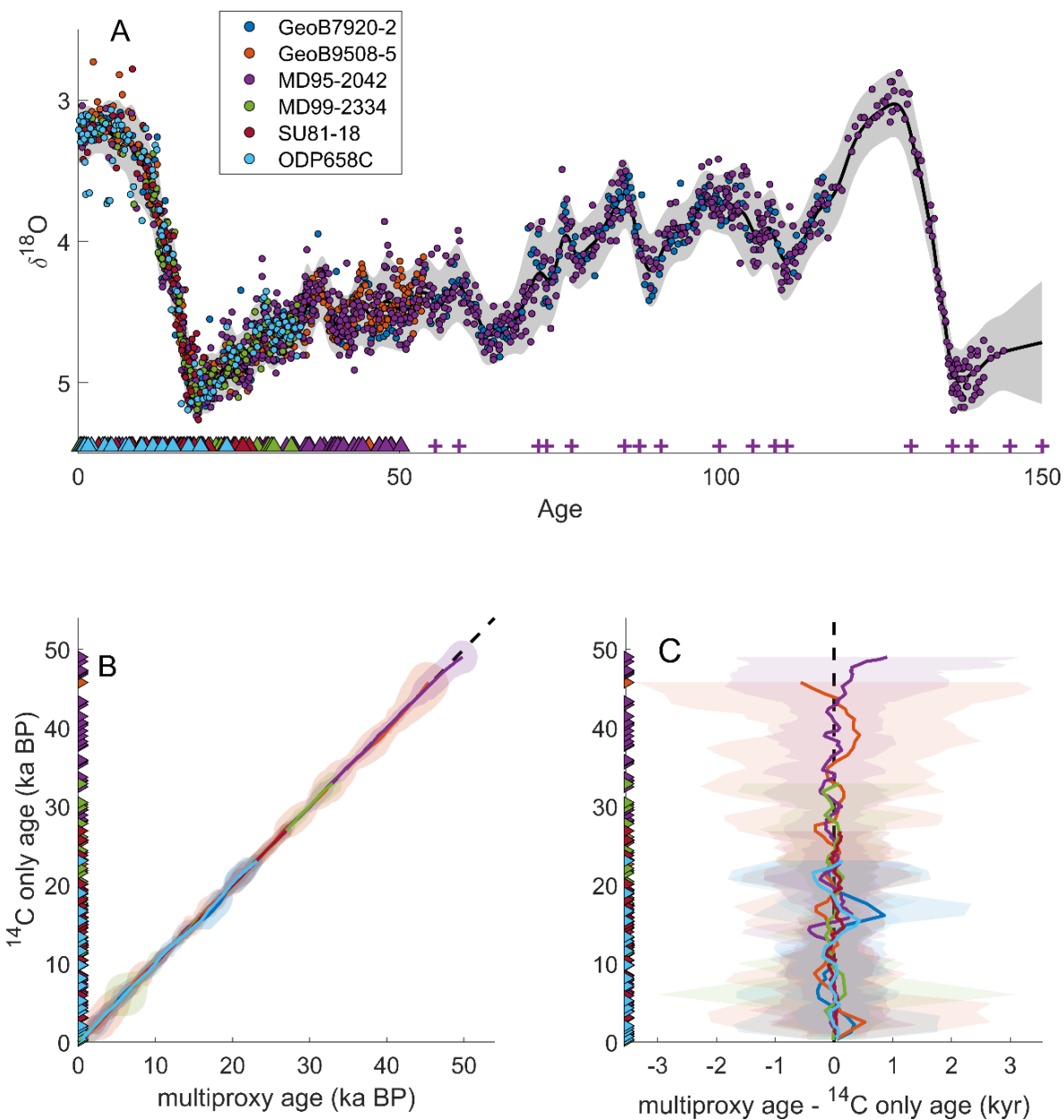
370 The Gaussian process regression also creates smoother stacks than previous binning methods. The Gaussian process
regression creates estimates of $\delta^{18}\text{O}$ for each point in time by incorporating information from neighboring data points, which
increases the stack's autocorrelation, compared to the binning procedure used in Lisiecki & Stern (2016). Given the large
volume of the deep ocean, we expect changes in benthic $\delta^{18}\text{O}$ to respond gradually; hence smoothing may increase the signal-
to-noise ratio of “local” stacks with less densely sampled $\delta^{18}\text{O}$ measurements and relatively few cores. Although there is a risk



375 that the Gaussian process regression may over-smooth the data, our DNEA stack still resolves millennial scale events. For example, figure 4(a) shows peaks at 24, 29 and 38 kyr corresponding to approximate ages of Heinrich Events H2 to H4 (Hemming, 2004) and similar in the DNA stack (Figure S4).

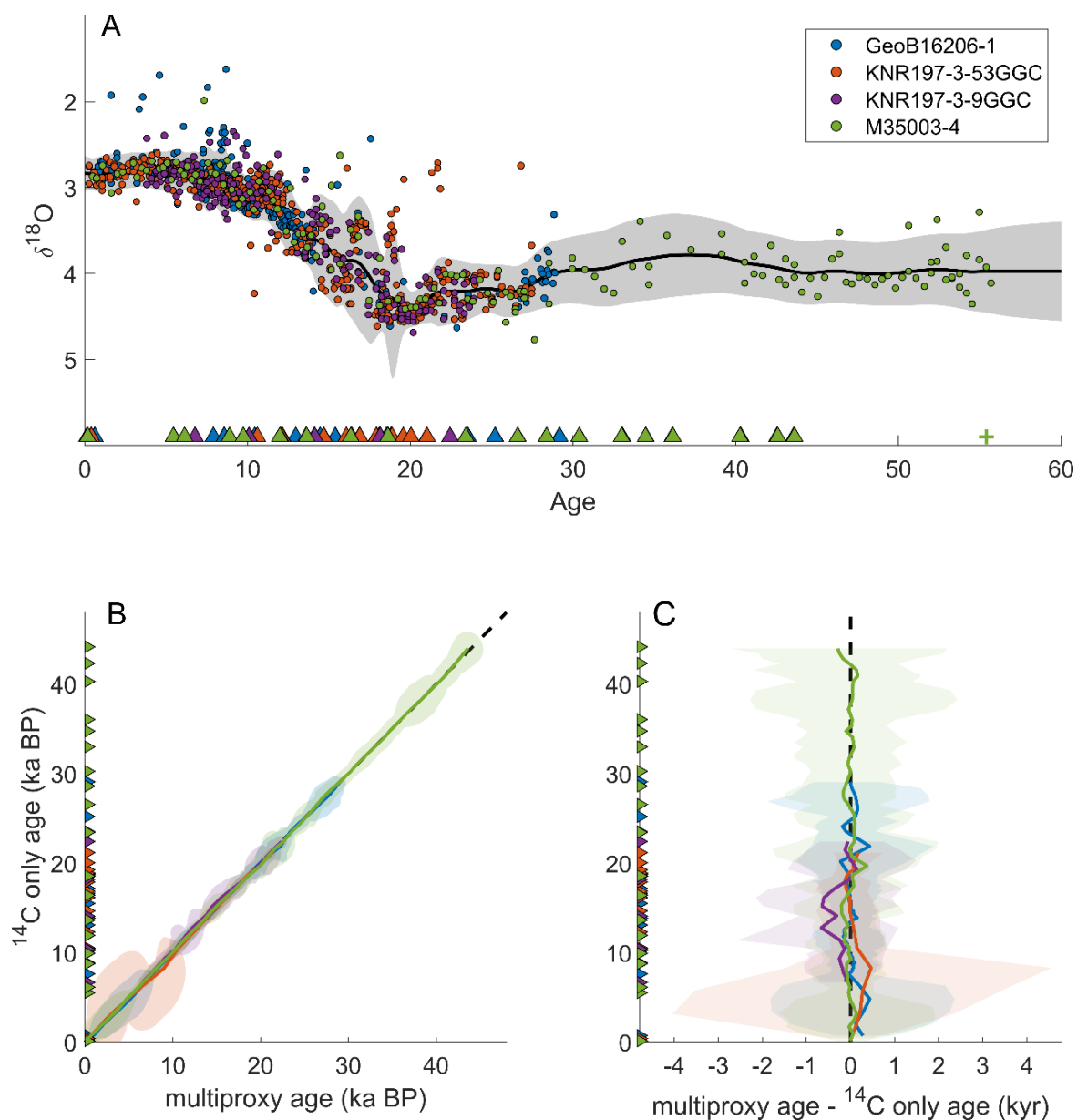
To evaluate the multiproxy age models of the ITWA and DNEA stacks, we compare them with radiocarbon-only and $\delta^{18}\text{O}$ -only age models for each core (with inclusion of the same additional ages in cores MD95-2042 and M35003-4). We find
380 good agreement between median radiocarbon and multiproxy age models for each core (panels B and C in Figures 3 and 4), indicating that the $\delta^{18}\text{O}$ alignments did not cause the multiproxy age models to stray from the radiocarbon data. Furthermore, the multiproxy age models have 95% confidence interval widths that are on average 262 years smaller than the radiocarbon age models and 1.92 kyr smaller than $\delta^{18}\text{O}$ -only age models (Figure S3).

The good agreement between the radiocarbon and multiproxy median age models also supports our assertion that the
385 input cores for each stack share homogeneous $\delta^{18}\text{O}$ signals. If the $\delta^{18}\text{O}$ records changed asynchronously, the alignments (which rely on the assumption of synchronous $\delta^{18}\text{O}$ change) would likely cause differences between the median age estimates of the radiocarbon-only and multiproxy age models. This assertion of synchronous $\delta^{18}\text{O}$ change is also supported by the relatively small shift and scale parameters learned for each core during the stacking procedure, indicating similar $\delta^{18}\text{O}$ values across all core sites (Table S1).



390 **Figure 3: The Deep Northeast Atlantic (DNEA) stack. (A)** The solid black line and shaded region represents the median stack value and 2-sigma upper and lower bounds. Filled circles are the shifted and scaled $\delta^{18}\text{O}$ data points from each core on the multiproxy age models. Filled triangles mark the radiocarbon ages from the respective cores. Purple crosses are the tie points for MD95-2042 taken from Lisiecki & Stern (2016). (B) ^{14}C -only age models vs. the multiproxy age models for each core in the DNEA stack. Each core plots along the black dashed 1:1 line. (C) The difference between the multiproxy age models and the ^{14}C age models for each core in the DNEA stack. Coloured shading shows the joint uncertainty distribution for ^{14}C and multiproxy age estimates for each core.

395



400 **Figure 4: The Intermediate Tropical West Atlantic (ITWA) stack. (A) The solid black line and shaded region represents the median**
stack value and 2-sigma upper and lower bounds. Filled circles are the shifted and scaled $\delta^{18}\text{O}$ data points from each core on the
multiproxy age models. Filled triangles mark radiocarbon ages from the respective cores. The green cross is the tie point for M35003-
4 from Hulz et al., (2000). (B) ^{14}C -only age models vs. the multiproxy age models for each core in the ITWA stack. Each core plots
along the black dashed 1:1 line. (C) The difference between the multiproxy age models and the ^{14}C age models for each core. Coloured
405 **shading shows the joint uncertainty distribution for ^{14}C and multiproxy age estimates for each core.**

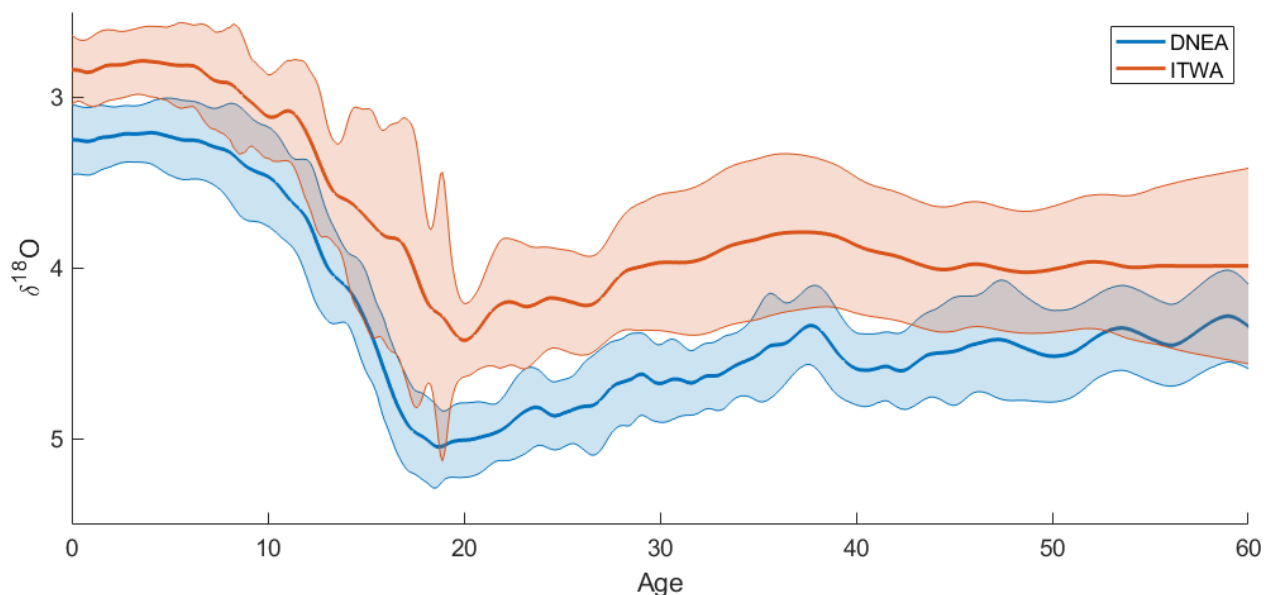


Figure 5: Comparison of the DNEA and ITWA stacks. Median values are displayed as the thick solid line, and shading marks plus and minus two standard deviations.

5 GIK13289-2 Age Model Comparison

410 To further evaluate the differences between single proxy and multiproxy age models, we compare three age models for GIK13289-2 constructed by BIGMACS: a radiocarbon age model, a $\delta^{18}\text{O}$ -only age model, and a multiproxy age model constrained by both $\delta^{18}\text{O}$ and radiocarbon data (Figure 6). The alignment target for the multiproxy and $\delta^{18}\text{O}$ -only age models is the DNEA stack.

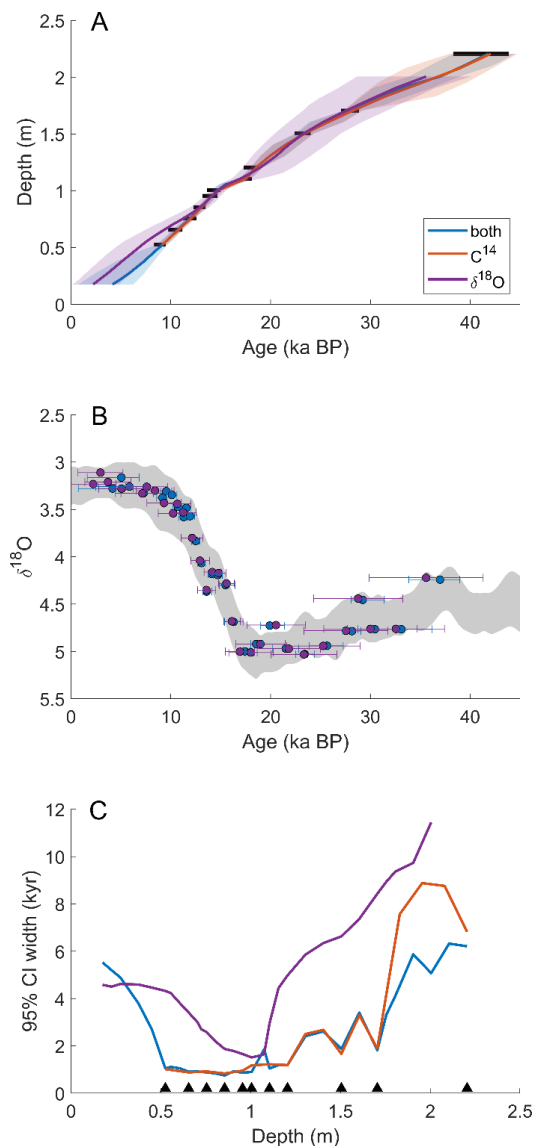
415 The multiproxy and radiocarbon age models show similar median ages. However, the radiocarbon age model has larger confidence intervals between core depths of 1.7 and 2.2 m where there is a ~10-kyr gap between radiocarbon measurements. The multiproxy age model is constrained by five $\delta^{18}\text{O}$ data points between these depths which serve to decrease age uncertainty. At a depth of 2 m, the 95% confidence interval width for the multiproxy age model (5.0 kyr) is 3.8 kyr smaller than the 95% confidence interval width for the radiocarbon age model (8.8 kyr).

420 The $\delta^{18}\text{O}$ -only age model for GIK13289-2 is based only on $\delta^{18}\text{O}$ alignment and has considerably larger uncertainty than the multiproxy age model, with a 95% confidence interval width as much as 6.6 kyr larger. Furthermore, there is disagreement between the median age models during the Holocene, with a maximum age difference of 2.2 kyr. The apparent error in median age estimates from $\delta^{18}\text{O}$ -only alignments likely results from near-constant $\delta^{18}\text{O}$ values during the Holocene, which allows for more possible alignments that fit the target and a less precise age model. The confidence interval for the $\delta^{18}\text{O}$ age model spans both the multiproxy and radiocarbon median ages, suggesting realistic uncertainty estimates for the alignment.

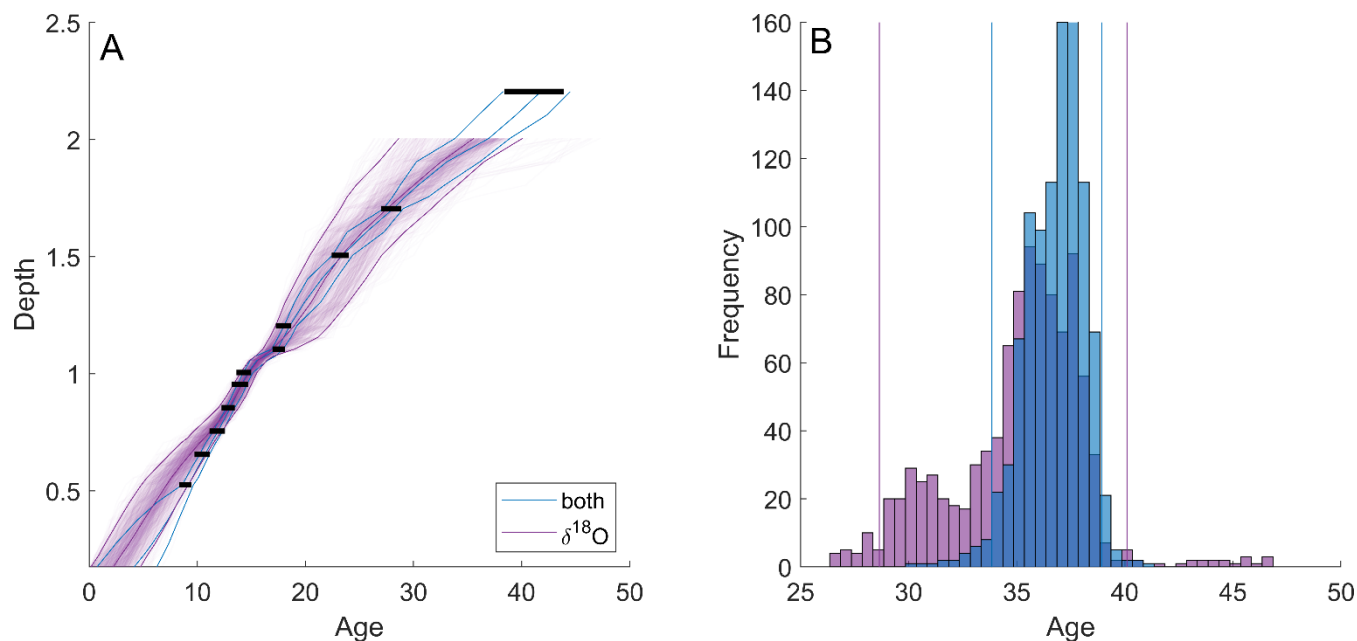
425 In Figure 7, the shading of the $\delta^{18}\text{O}$ -based age model represents age model sample density. The non-Gaussian nature of the $\delta^{18}\text{O}$ -based age estimates is evident at the end of the age model, where the median age and darker shading are located



near the upper end of the 95% confidence interval. The multiproxy age model samples at this depth (which are constrained by the final radiocarbon age) agree with the dense cluster of $\delta^{18}\text{O}$ -only age model samples. Frameworks have been developed to use the distribution of age model samples, such as those provided by BIGMACS, to estimate the probability of timing differences between climate responses recorded in multiple cores (Parnell et al., 2008; Khider et al., 2017).



435 **Figure 6: Comparison of a $\delta^{18}\text{O}$ -only age model, radiocarbon-only age model, and multiproxy age model for GIK13289-2. (A) Age vs. depth plot, solid black lines represent calibrated radiocarbon ages. (B) The shifted and scaled $\delta^{18}\text{O}$ for the $\delta^{18}\text{O}$ -only age model and multiproxy age model aligned to the DNEA stack. (C) 95% confidence interval widths for each age model. Black triangles indicate the depths of the radiocarbon ages. Note that the radiocarbon-only age model does not extend beyond the top ^{14}C date of ~10 ka BP, and we do not display the ^{14}C age model in panel (B).**



440 **Figure 7: (A) Sample density of the $\delta^{18}\text{O}$ -only age model for GIK13289-2. The median age model and 95% confidence bands are plotted as solid purple lines. The multiproxy median age model and 95% confidence bands are also plotted (solid blue lines) along with the calibrated radiocarbon ages (horizontal black lines). (B) Histogram of $\delta^{18}\text{O}$ -only age samples (purple) and multiproxy age model samples (blue) for the last depth in the $\delta^{18}\text{O}$ -only age model (approximately 2 m). Confidence interval widths for both age models are indicated with vertical lines.**

445 **6 Discussion**

6.1 Applications

In this section we discuss the advantages and limitations of the BIGMACS software compared to other available age modelling and stacking techniques and provide practical advice on the types of applications most suitable for BIGMACS.

6.1.1 Radiocarbon and multiproxy age models

450 Sediment core age models spanning the last 40-50 kyr are most commonly generated using only radiocarbon dates, occasionally supplemented by one or two tie points or other age constraints. Software packages commonly used to generate probabilistic radiocarbon age models (i.e., Bacon, Oxcal, Undatable) use models of sedimentation rate variability with tuneable parameters, which adjust the amount of age uncertainty between measured ^{14}C dates. In most cases, users have no specific information on which parameter values are most appropriate for the specific core analysed. Thus, parameter tuning usually
455 increases the subjectivity and labour involved to create an age model. BIGMACS can be used in ^{14}C -only mode to produce radiocarbon age models for ocean sediment cores without parameter tuning. Because BIGMACS applies a prior model based on observed sedimentation rate variability (Lin et al., 2014), the age uncertainty between ^{14}C observations returned by BIGMACS is physically realistic and less subjective than using tuned parameters in other software packages. BIGMACS can also estimate a time-varying baseline sedimentation rate that facilitates analysis of cores with large sedimentation rate changes



460 between glacial and interglacial climates. BIGMACS allows users to choose the calibration curve and reservoir ages applied to each core, including the addition of new calibration curve files.

Multiproxy age models generated by BIGMACS provide additional advantages compared to traditional probabilistic ^{14}C age models. In ^{14}C -only age models, each core's age model is constrained only by the ^{14}C dates from an individual core; however, multiproxy age models can use age constraints from multiple nearby cores, which are often available for locations of particular paleoceanographic interest (e.g., cores SU81-18, MD95-2042, and MD99-2334 on the Iberian Margin). For cores sharing a similar water mass history (which is likely for neighboring cores from similar water depths), multiproxy age models use both benthic $\delta^{18}\text{O}$ alignment and ^{14}C dates to generate age models for each core that are constrained by all ^{14}C dates in the group of cores. This is particularly useful for cores with lower resolution ^{14}C dating or with ambiguous ^{14}C outliers. Our example of GIK13289-2 (Figure 6) demonstrates that multiproxy alignment is helpful for extending age estimates beyond the range of ^{14}C dates (e.g., the Holocene portion of GIK13289-2) and decreasing age uncertainty between widely spaced ^{14}C dates, even in cases where benthic $\delta^{18}\text{O}$ data are also relatively low resolution. In most cases, these age model benefits are enhanced when BIGMACS is used to generate a multiproxy stack (e.g., Figures 3 and 4) instead of alignment to a fixed target.

Users should be aware that the age uncertainties returned by BIGMACS for age models generated by multiproxy alignment or stacking do not include the age uncertainty of the alignment target. Thus, age uncertainties between the ^{14}C dates (or other direct age proxies) in a core should be interpreted as relative age uncertainties that reflect alignment uncertainty, rather than absolute age uncertainty. For multiproxy stacks constrained by densely sampled ^{14}C dates with small calibration uncertainty, such as the DNEA stack from 0-25 ka (Figure 3), the absolute age uncertainty of the stack will be small. However, where the absolute age uncertainty of the alignment target or stack is larger, an assessment of a core's absolute age uncertainty should incorporate both the absolute age uncertainty of the target/stack and alignment uncertainty. For example, absolute age uncertainty for the DNEA stack beyond 45 ka can be estimated by constructing an age model for MD95-2042 using only the ^{14}C dates and additional age information (i.e., tie points marked as crosses in Figure 3A). Because GeoB7920-2 contains no direct age proxies beyond 45 ka, its absolute age uncertainty could be estimated as the sum of variance in the alignment uncertainty (the age model uncertainty resulting from alignment to the DNEA stack) and the variance of the age model constructed for MD95-2042 using only radiocarbon data and the additional tie points.

485 **6.1.2 Stacking**

Creating a multiproxy stack in BIGMACS offers advantages compared to traditional stacking techniques. First, these multiproxy stacks can be created with as few as two cores. All cores in the multiproxy stack must have benthic $\delta^{18}\text{O}$ for alignment, but the stack can include cores that lack ^{14}C or other age constraints. Second, whereas most previous stacks have been constructed by pairwise alignments of each core to a single target (e.g., Lisiecki and Stern, 2016), BIGMACS aligns all cores simultaneously while updating the alignment target until convergence is achieved. This process reduces the time required to create a stack as well as sensitivity to the choice of the initial alignment target. Third, the multiproxy stack's age model and alignments evolve simultaneously based on the direct age proxies in all the aligned cores, whereas most recent stacks aligned



all cores before estimating the stack's age model (e.g., Huybers and Wunsch, 2004; Lisiecki & Raymo, 2005; Lisiecki & Stern, 2016). Although BIGMACS and HMM-Stack both iteratively update the alignment target using the aligned $\delta^{18}\text{O}$ signals, stacks
495 produced by HMM-Stack implicitly inherit the age model of the original alignment target because HMM-Stack contains no procedure to adjust the alignment target's age model.

Another innovation in BIGMACS is the use of the Gaussian process regression to create time-continuous estimates of the $\delta^{18}\text{O}$ stack's mean and variance. Most previous stacks relied on either interpolation of each core's $\delta^{18}\text{O}$ measurements to an even time spacing (e.g., Huybers & Wunsch, 2004) or binning and averaging all cores' $\delta^{18}\text{O}$ measurements within a
500 certain time window (e.g., Lisiecki and Raymo, 2005). The Gaussian process regression requires fewer cores, samples at any resolution without interpolation, smooths the stack to increase its signal-to-noise ratio, and realistically increases stack variance across $\delta^{18}\text{O}$ gaps. The hyperparameters of the OU kernel determine the overall smoothness of each stack, but for the stacks presented here, smoothing from the Gaussian process regression inhibits precise estimates of the amplitude and rate of change of events occurring on timescales of ~ 2 kyr or less. For example, the DNA stack of Lisiecki and Stern (2016), which averaged
505 $\delta^{18}\text{O}$ values using 0.5 kyr bins, decreased by 0.47 ‰ in 1.5 kyr (from 87 to 85.5 ka) during Heinrich event 8; however, in the DNEA stack produced by BIGMACS, the $\delta^{18}\text{O}$ change is spread over an interval at least twice as long (89 to 85 ka BP, Figure S4). Additionally, although a $\delta^{18}\text{O}$ response during Greenland interstadial 19 is recorded in both the DNA and DNEA stack at 72 ka, smoothing by the Gaussian process regression and alignment uncertainty appears to have reduced its amplitude in the BIGMACS DNEA stack.

510 An important caveat that applies to all $\delta^{18}\text{O}$ alignments, including BIGMACS multiproxy alignments and stacks, is that the $\delta^{18}\text{O}$ records aligned should all be homogeneous, meaning that they share the same underlying $\delta^{18}\text{O}$ signal. Because previous studies have observed temporal offsets between benthic $\delta^{18}\text{O}$ signals from core sites bathed by different water masses (Skinner & Shackleton, 2005; Labeyrie et al., 2005; Waelbroeck et al., 2011; Stern & Lisiecki, 2014), users should only align or stack cores which share the same deep water mass history over the length of the records analysed. Whether $\delta^{18}\text{O}$ is
515 homogeneous across core sites can, in part, be evaluated by comparing the amplitude of change and mean offset (after species-corrections) between cores. For example, BIGMACS estimates only small shift and scale differences between the cores included in the DNEA and ITWA stacks (Table S1), although large shifts are observed between the stacks. Another test is to compare the core sites' present-day deep water mass composition and reconstructions or models of deep water mass extents at the LGM. Although glacial water mass estimates are inherently uncertain due to differences between various models and reconstructions, BIGMACS offers the flexibility to easily build different stacks to evaluate the sensitivity of results to different
520 models of benthic $\delta^{18}\text{O}$ homogeneity.

BIGMACS may be able to align and stack proxies other than benthic $\delta^{18}\text{O}$; however, the software can currently only align and stack one proxy at a time. For BIGMACS to accurately construct a probabilistic stack of an alternate proxy, the proxy must be homogeneous across the records in the stack with residuals that can reasonably be described with the generalized
525 student's t-distribution that BIGMACS uses for the $\delta^{18}\text{O}$ emission model. Because the emission model is based on the variance that best describes the observations, it does not require a specific assumption about the level of noise in the measurements.



However, low ratios of signal-to-noise in the proxy aligned could yield unreliable results. Preliminary analysis of planktonic $\delta^{18}\text{O}$ alignments and stacks have yielded encouraging results, but the more heterogeneous nature of surface variability requires caution in the selection of cores which can reasonably be considered heterogeneous.

530 The computational complexity of BIGMACS also places constraints on its applications. For the records in this study, multiproxy alignment of a single core to a target takes only 1-2 minutes while the multiproxy stacks take 1-2 hours to build on a typical desktop machine. In testing, we have successfully created $\delta^{18}\text{O}$ -only and multiproxy stacks of Late Pleistocene $\delta^{18}\text{O}$ spanning the past 800 kyr, which take approximately 12 hours to run. However, we have not yet evaluated the performance of BIGMACS for records longer than 800 kyr. For a more detailed discussion of the time complexity for BIGMACS, see
535 supplemental text S6.

7 Conclusion

The new software package, BIGMACS, constructs multiproxy sediment core age models and benthic $\delta^{18}\text{O}$ stacks constrained by radiocarbon ages, $\delta^{18}\text{O}$ alignment, and other additional age constraints. BIGMACS requires no parameter tuning and uses an empirically derived prior model of sedimentation rate variability specific to the marine depositional environment.
540 Radiocarbon ages are modelled using a student's t-distribution, following the methods of Christen and Pérez (2009). BIGMACS also constructs time-continuous stacks using Gaussian process regression and requires fewer cores than traditional binning methods. This facilitates building stacks for more localized regions using as few as two cores from within a homogeneous water mass as assessed by deep water mass reconstructions and/or evaluation of the estimated shift and scale parameters for the aligned cores. Example multiproxy regional stacks are presented for the Deep Northeast Atlantic (DNEA)
545 and Intermediate Tropical West Atlantic (ITWA). The stacks' median $\delta^{18}\text{O}$ values provide well-dated regional climate signals, while the stacks' standard deviations include the effects of spatial variability, age uncertainty, measurement noise, and, in the ITWA stack, the effects of $\delta^{18}\text{O}$ outliers likely caused by sediment disturbances. Finally, a comparison of radiocarbon-only, $\delta^{18}\text{O}$ -only, and multiproxy age models for one core demonstrates that the multiproxy age model yields smaller age uncertainties, particularly between radiocarbon measurements and during the Holocene $\delta^{18}\text{O}$ plateau.

550 Code Availability

The software package BIGMACS (developed and tested in MATLAB R2021b) and the user guide can be downloaded from <https://github.com/eilion/BIGMACS>.



Author Contributions

Taehee Lee (first author with Devin Rand) conceptualized the evolution of overarching research goals, performed a formal
555 analysis, developed the methodology and the software, and performed writing – review and editing. Devin Rand (first author
with Taehee Lee) curated data, validated results, visualized the data, and performed writing – original draft preparation.
Lorraine Lisiecki conceptualized the project, acquired funding, served as a project administrator, supervised, and performed
writing – review and editing. Geoffrey Gebbie acquired funding, provided resources, supervised, and performed writing –
review and editing. Charles Lawrence conceptualized the project, performed a formal analysis, acquired funding, served as a
560 project administrator, supervised, and performed writing – review & editing.

Competing Interests

The authors declare that they have no conflict of interest.

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References

- Ahn, S., Khider, D., Lisiecki, L. E., and Lawrence, C. E.: A probabilistic Pliocene–Pleistocene stack of benthic $\delta^{18}\text{O}$ using a
profile hidden Markov model, 2, <https://doi.org/10.1093/climsys/dzx002>, 2017.
- Andrés Christen, J. and Pérez E, S.: A New Robust Statistical Model for Radiocarbon Data, *Radiocarbon*, 51, 1047–1059,
570 <https://doi.org/10.1017/S003382220003410X>, 2009.
doi:10.1016/j.quascirev.2004.03.006 | Elsevier Enhanced Reader:
- Bard, E., Fairbanks, R., Arnold, M., Maurice, P., Duprat, J., Moyes, J., and Duplessy, J.-C.: Sea-level estimates during the last
deglaciation based on $\delta^{18}\text{O}$ and accelerator mass spectrometry ^{14}C ages measured in *Globigerina bulloides*, *Quaternary
Research*, 31, 381–391, [https://doi.org/10.1016/0033-5894\(89\)90045-8](https://doi.org/10.1016/0033-5894(89)90045-8), 1989.
- 575 Bard, E., Rostek, F., and Ménot-Combes, G.: Radiocarbon calibration beyond 20,000 ^{14}C yr B.P. by means of planktonic
foraminifera of the Iberian Margin, 61, 204–214, <https://doi.org/10.1016/j.yqres.2003.11.006>, 2004.
- Barker, S. and Diz, P.: Timing of the descent into the last Ice Age determined by the bipolar seesaw, *Paleoceanography*, 29,
489–507, <https://doi.org/10.1002/2014PA002623>, 2014.
- Barker, Stephen, Gregor Knorr, R. Lawrence Edwards, Frédéric Parrenin, Aaron E. Putnam, Luke C. Skinner, Eric Wolff, and
580 Martin Ziegler. "800,000 years of abrupt climate variability." *science* 334, no. 6054 (2011): 347-351.



- Blaauw, M.: Methods and code for ‘classical’ age-modelling of radiocarbon sequences, *Quaternary Geochronology*, 5, 512–518, <https://doi.org/10.1016/j.quageo.2010.01.002>, 2010a.
- Blaauw, M.: Methods and code for ‘classical’ age-modelling of radiocarbon sequences, *Quaternary Geochronology*, 5, 512–518, <https://doi.org/10.1016/j.quageo.2010.01.002>, 2010b.
- 585 Blaauw, M. and Christen, J. A.: Radiocarbon peat chronologies and environmental change, 54, 805–816, <https://doi.org/10.1111/j.1467-9876.2005.00516.x>, 2005.
- Blaauw, M. and Christen, J. A.: Flexible paleoclimate age-depth models using an autoregressive gamma process, *Bayesian Anal.*, 6, <https://doi.org/10.1214/11-BA618>, 2011.
- Brázdil, R., Dobrovolný, P., Trnka, M., Řezníčková, L., Dolák, L., and Kotyza, O.: Extreme droughts and human responses to
590 them: the Czech Lands in the pre-instrumental period, *Clim. Past*, 15, 1–24, <https://doi.org/10.5194/cp-15-1-2019>, 2019.
- Bronk Ramsey, C.: Radiocarbon Calibration and Analysis of Stratigraphy: The OxCal Program, *Radiocarbon*, 37, 425–430, <https://doi.org/10.1017/S0033822200030903>, 1995.
- Bronk Ramsey, C.: Development of the Radiocarbon Calibration Program, *Radiocarbon*, 43, 355–363, <https://doi.org/10.1017/S0033822200038212>, 2001.
- 595 Bronk Ramsey, C.: Dealing with Outliers and Offsets in Radiocarbon Dating, *Radiocarbon*, 51, 1023–1045, <https://doi.org/10.1017/S0033822200034093>, 2009.
- Buck, C. E. and Christen, J. A.: Making Complex Radiocarbon Calibration Software More Accessible: a New Approach?, 3, n.d.
- Butzin, M., Köhler, P., and Lohmann, G.: Marine radiocarbon reservoir age simulations for the past 50,000 years: Marine
600 Radiocarbon Simulations, *Geophys. Res. Lett.*, 44, 8473–8480, <https://doi.org/10.1002/2017GL074688>, 2017.
- Butzin, M., Heaton, T. J., Köhler, P., and Lohmann, G.: A Short Note on Marine Reservoir Age Simulations Used in IntCal20, *Radiocarbon*, 62, 865–871, <https://doi.org/10.1017/RDC.2020.9>, 2020.
- Channell, J. E. T., Xuan, C., and Hodell, D. A.: Stacking paleointensity and oxygen isotope data for the last 1.5 Myr (PISO-1500), *Earth and Planetary Science Letters*, 283, 14–23, <https://doi.org/10.1016/j.epsl.2009.03.012>, 2009.
- 605 Christen, J. A.: Summarizing a Set of Radiocarbon Determinations: A Robust Approach, 43, 489–503, <https://doi.org/10.2307/2986273>, 1994.
- Christen, J. A. and E, S. P.: A New Robust Statistical Model for Radiocarbon Data, *Radiocarbon*, 51, 1047–1059, <https://doi.org/10.1017/S003382220003410X>, 2009.
- Collins, J. A., Schefuß, E., Heslop, D., Mulitza, S., Prange, M., Zabel, M., Tjallingii, R., Dokken, T. M., Huang, E., Mackensen, A., Schulz, M., Tian, J., Zarriess, M., and Wefer, G.: Interhemispheric symmetry of the tropical African rainbelt over the past
610 23,000 years, *Nature Geosci.*, 4, 42–45, <https://doi.org/10.1038/ngeo1039>, 2011.
- deMenocal, P., Ortiz, J., Guilderson, T., Adkins, J., Sarnthein, M., Baker, L., and Yarusinsky, M.: Abrupt onset and termination of the African Humid Period: rapid climate responses to gradual insolation forcing, *Quaternary Science Reviews*, 19, 347–361, [https://doi.org/10.1016/S0277-3791\(99\)00081-5](https://doi.org/10.1016/S0277-3791(99)00081-5), 2000.



- 615 Dempster, A. P., Laird, N. M., and Rubin, D. B.: Maximum Likelihood from Incomplete Data Via the EM Algorithm, 39, 1–22, <https://doi.org/10.1111/j.2517-6161.1977.tb01600.x>, 1977.
- DeVries, T. and Primeau, F.: Dynamically and Observationally Constrained Estimates of Water-Mass Distributions and Ages in the Global Ocean, 41, 2381–2401, <https://doi.org/10.1175/JPO-D-10-05011.1>, 2011.
- Doucet, A., de Freitas, N., and Gordon, N.: Sequential Monte Carlo Methods in Practice, 12, n.d.
- 620 Gebbie, G. and Huybers, P.: Total Matrix Intercomparison: A Method for Determining the Geometry of Water-Mass Pathways, 40, 1710–1728, <https://doi.org/10.1175/2010JPO4272.1>, 2010.
- Gebbie, G. and Huybers, P.: The Mean Age of Ocean Waters Inferred from Radiocarbon Observations: Sensitivity to Surface Sources and Accounting for Mixing Histories, 42, 291–305, <https://doi.org/10.1175/JPO-D-11-043.1>, 2012.
- Grootes, P. M. and Stuiver, M.: Oxygen 18/16 variability in Greenland snow and ice with 10–3- to 105-year time resolution, 625 *Journal of Geophysical Research: Oceans*, 102, 26455–26470, <https://doi.org/10.1029/97JC00880>, 1997.
- Haslett, J. and Parnell, A.: A simple monotone process with application to radiocarbon-dated depth chronologies, 57, 399–418, <https://doi.org/10.1111/j.1467-9876.2008.00623.x>, 2008.
- Hastings, W. K.: Monte Carlo sampling methods using Markov chains and their applications, 13, n.d.
- Heaton, T. J., Köhler, P., Butzin, M., Bard, E., Reimer, R. W., Austin, W. E. N., Bronk Ramsey, C., Grootes, P. M., Hughen, 630 K. A., Kromer, B., Reimer, P. J., Adkins, J., Burke, A., Cook, M. S., Olsen, J., and Skinner, L. C.: Marine20—The Marine Radiocarbon Age Calibration Curve (0–55,000 cal BP), *Radiocarbon*, 62, 779–820, <https://doi.org/10.1017/RDC.2020.68>, 2020.
- Hemming, S. R.: Heinrich events: Massive late Pleistocene detritus layers of the North Atlantic and their global climate imprint, *Reviews of Geophysics*, 42, <https://doi.org/10.1029/2003RG000128>, 2004.
- 635 Howe, J. N. W., Piotrowski, A. M., and Rennie, V. C. F.: Abyssal origin for the early Holocene pulse of unradiogenic neodymium isotopes in Atlantic seawater, *Geology*, 44, 831–834, <https://doi.org/10.1130/G38155.1>, 2016.
- Hüls, M. and Zahn, R.: Millennial-scale sea surface temperature variability in the western tropical North Atlantic from planktonic foraminiferal census counts, 15, 659–678, <https://doi.org/10.1029/1999PA000462>, 2000.
- Huybers, P. and Wunsch, C.: A depth-derived Pleistocene age model: Uncertainty estimates, sedimentation variability, and 640 nonlinear climate change, 19, <https://doi.org/10.1029/2002PA000857>, 2004.
- Imbrie, John, James D. Hays, Douglas G. Martinson, Andrew McIntyre, Alan C. Mix, Joseph J. Morley, Nicklas G. Pisias, Warren L. Prell, and Nicholas J. Shackleton. The orbital theory of Pleistocene climate: support from a revised chronology of the marine $\delta^{18}\text{O}$ record. (1984).
- Key, R. M., Kozyr, A., Sabine, C. L., Lee, K., Wanninkhof, R., Bullister, J. L., Feely, R. A., Millero, F. J., Mordy, C., and 645 Peng, T.-H.: A global ocean carbon climatology: Results from Global Data Analysis Project (GLODAP): GLOBAL OCEAN CARBON CLIMATOLOGY, *Global Biogeochem. Cycles*, 18, n/a-n/a, <https://doi.org/10.1029/2004GB002247>, 2004.



- Pailler, D. and Bard, E.: High frequency palaeoceanographic changes during the past 140 000 yr recorded by the organic matter in sediments of the Iberian Margin, *Palaeogeography, Palaeoclimatology, Palaeoecology*, 181, 431–452, [https://doi.org/10.1016/S0031-0182\(01\)00444-8](https://doi.org/10.1016/S0031-0182(01)00444-8), 2002.
- 650 Peters, G.: *Markov Chain Monte Carlo: stochastic simulation for Bayesian inference* (2nd edn). Dani Gamerman and Hedibert F. Lopes, Chapman & Hall/CRC, Boca Raton, FL, 2006. No. of pages: xvii +323. Price: \$69.95. ISBN10: 1-58488-587-4, ISBN13: 978-1-58488-587-0, *Statistics in Medicine*, 27, 3213–3214, <https://doi.org/10.1002/sim.3240>, 2008.
- Pöppelmeier, F., Blaser, P., Gutjahr, M., Jaccard, S. L., Frank, M., Max, L., and Lippold, J.: Northern-sourced water dominated the Atlantic Ocean during the Last Glacial Maximum, *Geology*, 48, 826–829, <https://doi.org/10.1130/G47628.1>,
655 2020.
- Klaas, M., Briers, M., de Freitas, N., Doucet, A., Maskell, S., and Lang, D.: Fast particle smoothing: if I had a million particles, in: *Proceedings of the 23rd international conference on Machine learning - ICML '06, the 23rd international conference*, Pittsburgh, Pennsylvania, 481–488, <https://doi.org/10.1145/1143844.1143905>, 2006.
- Knaack, J.-J. and Sarthein, M.: Stable isotopes of foraminifera of ODP Hole 108-658C, <https://doi.org/10.1594/PANGAEA.227736>, 2005.
660
- Khider, D., Ahn, S., Lisiecki, L. E., Lawrence, C. E., and Kienast, M.: The Role of Uncertainty in Estimating Lead/Lag Relationships in Marine Sedimentary Archives: A Case Study From the Tropical Pacific, *Paleoceanography*, 32, 1275–1290, <https://doi.org/10.1002/2016PA003057>, 2017.
- Labeyrie, L., Waelbroeck, C., Cortijo, E., Michel, E., and Duplessy, J.-C.: Changes in deep water hydrology during the Last
665 Deglaciation, *Comptes Rendus Geoscience*, 337, 919–927, <https://doi.org/10.1016/j.crte.2005.05.010>, 2005.
- Langrené, N. and Warin, X.: Fast and Stable Multivariate Kernel Density Estimation by Fast Sum Updating, *Journal of Computational and Graphical Statistics*, 28, 596–608, <https://doi.org/10.1080/10618600.2018.1549052>, 2019.
- Lee, T. and Lawrence, C. E.: Heteroscedastic Gaussian Process Regression on the Alkenone over Sea Surface Temperatures, <https://doi.org/10.5065/y82j-f154>, 2019.
- 670 Lin, L., Khider, D., Lisiecki, L. E., and Lawrence, C. E.: Probabilistic sequence alignment of stratigraphic records, *Paleoceanography*, 29, 976–989, <https://doi.org/10.1002/2014PA002713>, 2014.
- Lisiecki, L. E. and Lisiecki, P. A.: Application of dynamic programming to the correlation of paleoclimate records: DYNAMIC PROGRAMMING SIGNAL CORRELATION, *Paleoceanography*, 17, 1-1-1–12, <https://doi.org/10.1029/2001PA000733>, 2002.
- 675 Lisiecki, L. E. and Raymo, M. E.: A Pliocene-Pleistocene stack of 57 globally distributed benthic $\delta^{18}\text{O}$ records, 20, <https://doi.org/10.1029/2004PA001071>, 2005.
- Lisiecki, L. E. and Raymo, M. E.: Diachronous benthic $\delta^{18}\text{O}$ responses during late Pleistocene terminations, 24, <https://doi.org/10.1029/2009PA001732>, 2009.
- Lisiecki, L. E. and Stern, J. V.: Regional and global benthic $\delta^{18}\text{O}$ stacks for the last glacial cycle: Last Glacial Cycle Benthic
680 $\delta^{18}\text{O}$, *Paleoceanography*, 31, 1368–1394, <https://doi.org/10.1002/2016PA003002>, 2016.



- Lougheed, B. C. and Obrochta, S. P.: MatCal: Open Source Bayesian ^{14}C Age Calibration in Matlab, *JORS*, 4, 42, <https://doi.org/10.5334/jors.130>, 2016.
- Lougheed, B. C. and Obrochta, S. P.: A Rapid, Deterministic Age-Depth Modeling Routine for Geological Sequences With Inherent Depth Uncertainty, 34, 122–133, <https://doi.org/10.1029/2018PA003457>, 2019.
- 685 Lund, D. C., Tessin, A. C., Hoffman, J. L., and Schmittner, A.: Southwest Atlantic water mass evolution during the last deglaciation, *Paleoceanography*, 30, 477–494, <https://doi.org/10.1002/2014PA002657>, 2015.
- Marchitto, T. M., Curry, W. B., Lynch-Stieglitz, J., Bryan, S. P., Cobb, K. M., and Lund, D. C.: Improved oxygen isotope temperature calibrations for cosmopolitan benthic foraminifera, *Geochimica et Cosmochimica Acta*, 130, 1–11, <https://doi.org/10.1016/j.gca.2013.12.034>, 2014.
- 690 Martino, L., Read, J., and Luengo, D.: Independent Doubly Adaptive Rejection Metropolis Sampling Within Gibbs Sampling, 63, 3123–3138, <https://doi.org/10.1109/TSP.2015.2420537>, 2015.
- Metropolis, N., Rosenbluth, A. W., and Rosenbluth, M. N.: Equation of State Calculations by Fast Computing Machines, 7, n.d.
- Murphy, K. P.: Machine learning: a probabilistic perspective, MIT Press, Cambridge, MA, 1067 pp., 2012.
- 695 Oppo, D. W., Gebbie, G., Huang, K.-F., Curry, W. B., Marchitto, T. M., and Pietro, K. R.: Data Constraints on Glacial Atlantic Water Mass Geometry and Properties, 33, 1013–1034, <https://doi.org/10.1029/2018PA003408>, 2018.
- Parnell, A. C., Haslett, J., Allen, J. R. M., Buck, C. E., and Huntley, B.: A flexible approach to assessing synchronicity of past events using Bayesian reconstructions of sedimentation history, *Quaternary Science Reviews*, 27, 1872–1885, <https://doi.org/10.1016/j.quascirev.2008.07.009>, 2008.
- 700 Piasias, N. G. and Shackleton, N. J.: Modelling the global climate response to orbital forcing and atmospheric carbon dioxide changes, *Nature*, 310, 757–759, <https://doi.org/10.1038/310757a0>, 1984.
- Portilho-Ramos, R. C., Chiessi, C. M., Zhang, Y., Mulitza, S., Kucera, M., Siccha, M., Prange, M., and Paul, A.: Coupling of equatorial Atlantic surface stratification to glacial shifts in the tropical rainbelt, *Sci Rep*, 7, 1561, <https://doi.org/10.1038/s41598-017-01629-z>, 2017.
- 705 Quinonero-Candela, J., Ramussen, C. E., and Williams, C. K. I.: Approximation Methods for Gaussian Process Regression, 24, n.d.
- Rabiner, L. R.: A tutorial on hidden Markov models and selected applications in speech recognition, *Proceedings of the IEEE*, 77, 257–286, <https://doi.org/10.1109/5.18626>, 1989.
- Ramsey, C. B.: Deposition models for chronological records, *Quaternary Science Reviews*, 27, 42–60, <https://doi.org/10.1016/j.quascirev.2007.01.019>, 2008.
- 710 Ramsey, C. B. and Lee, S.: Recent and Planned Developments of the Program OxCal, *Radiocarbon*, 55, 720–730, <https://doi.org/10.1017/S0033822200057878>, 2013.
- Rasmussen, C. E. and Williams, C.K.I.: Gaussian Processes for Machine Learning (Adaptive Computation and Machine Learning), The MIT Press, 2005.



- 715 Reimer, P. J. and Reimer, R. W.: A Marine Reservoir Correction Database and On-Line Interface, *Radiocarbon*, 43, 461–463,
<https://doi.org/10.1017/S0033822200038339>, 2001.
- Reimer, P. J., Austin, W. E. N., Bard, E., Bayliss, A., Blackwell, P. G., Bronk Ramsey, C., Butzin, M., Cheng, H., Edwards,
R. L., Friedrich, M., Grootes, P. M., Guilderson, T. P., Hajdas, I., Heaton, T. J., Hogg, A. G., Hughen, K. A., Kromer, B.,
Manning, S. W., Muscheler, R., Palmer, J. G., Pearson, C., van der Plicht, J., Reimer, R. W., Richards, D. A., Scott, E. M.,
720 Southon, J. R., Turney, C. S. M., Wacker, L., Adolphi, F., Büntgen, U., Capano, M., Fahrni, S. M., Fogtmann-Schulz, A.,
Friedrich, R., Köhler, P., Kudsk, S., Miyake, F., Olsen, J., Reinig, F., Sakamoto, M., Sookdeo, A., and Talamo, S.: The IntCal20
Northern Hemisphere Radiocarbon Age Calibration Curve (0–55 cal kBP), *Radiocarbon*, 62, 725–757,
<https://doi.org/10.1017/RDC.2020.41>, 2020.
- Sarnthein, M., Winn, K., Jung, S. J. A., Duplessy, J.-C., Labeyrie, L., Erlenkeuser, H., and Ganssen, G.: Changes in East
725 Atlantic Deepwater Circulation over the last 30,000 years: Eight time slice reconstructions, 9, 209–267,
<https://doi.org/10.1029/93PA03301>, 1994.
- Shackleton, N.: Oxygen Isotope Analyses and Pleistocene Temperatures Re-assessed, *Nature*, 215, 15–17,
<https://doi.org/10.1038/215015a0>, 1967.
- Shackleton, N. J., Hall, M. A., and Vincent, E.: Phase relationships between millennial-scale events 64,000–24,000 years ago,
730 15, 565–569, <https://doi.org/10.1029/2000PA000513>, 2000.
- Shackleton, N. J., Fairbanks, R. G., Chiu, T., and Parrenin, F.: Absolute calibration of the Greenland time scale: implications
for Antarctic time scales and for $\Delta 14C$, *Quaternary Science Reviews*, 23, 1513–1522,
<https://doi.org/10.1016/j.quascirev.2004.03.006>, 2004.
- Sikes, E. L., Allen, K. A., and Lund, D. C.: Enhanced $\delta 13C$ and $\delta 18O$ Differences Between the South Atlantic and South
735 Pacific During the Last Glaciation: The Deep Gateway Hypothesis, *Paleoceanography*, 32, 1000–1017,
<https://doi.org/10.1002/2017PA003118>, 2017.
- Skinner, L. C. and Shackleton, N. J.: An Atlantic lead over Pacific deep-water change across Termination I: implications for
the application of the marine isotope stage stratigraphy, *Quaternary Science Reviews*, 24, 571–580,
<https://doi.org/10.1016/j.quascirev.2004.11.008>, 2005.
- 740 Skinner, L. C., Muschitiello, F., and Scrivner, A. E.: Marine Reservoir Age Variability Over the Last Deglaciation:
Implications for Marine Carbon Cycling and Prospects for Regional Radiocarbon Calibrations, *Paleoceanography and
Paleoclimatology*, 34, 1807–1815, <https://doi.org/10.1029/2019PA003667>, 2019.
- Skinner, L. C., Freeman, E., Hodell, D., Waelbroeck, C., Vazquez Riveiros, N., and Scrivner, A. E.: Atlantic Ocean
Ventilation Changes Across the Last Deglaciation and Their Carbon Cycle Implications, *Paleoceanography and
745 Paleoclimatology*, 36, e2020PA004074, <https://doi.org/10.1029/2020PA004074>, 2021.
- Stern, J. V. and Lisiecki, L. E.: North Atlantic circulation and reservoir age changes over the past 41,000 years, *Geophysical
Research Letters*, 40, 3693–3697, <https://doi.org/10.1002/grl.50679>, 2013.



- Stern, J. V. and Lisiecki, L. E.: Termination 1 timing in radiocarbon-dated regional benthic $\delta^{18}\text{O}$ stacks, 29, 1127–1142, <https://doi.org/10.1002/2014PA002700>, 2014.
- 750 Stuiver, M. and Reimer, P. J.: Extended ^{14}C Data Base and Revised CALIB 3.0 ^{14}C Age Calibration Program, Radiocarbon, 35, 215–230, <https://doi.org/10.1017/S0033822200013904>, 1993.
- Titsias, M. K.: Variational Learning of Inducing Variables in Sparse Gaussian Processes, 8, n.d.
- Tjallingii, R., Claussen, M., Stuut, J.-B. W., Fohlmeister, J., Jahn, A., Bickert, T., Lamy, F., and Röhl, U.: Coherent high- and low-latitude control of the northwest African hydrological balance, Nature Geosci, 1, 670–675, <https://doi.org/10.1038/ngeo289>, 2008.
- 755 Voigt, I., Cruz, A. P. S., Mulitza, S., Chiessi, C. M., Mackensen, A., Lippold, J., Antz, B., Zabel, M., Zhang, Y., Barbosa, C. F., and Tisserand, A. A.: Variability in mid-depth ventilation of the western Atlantic Ocean during the last deglaciation, 32, 948–965, <https://doi.org/10.1002/2017PA003095>, 2017.
- Waelbroeck, C., Duplessy, J.-C., Michel, E., Labeyrie, L., Paillard, D., and Duprat, J.: The timing of the last deglaciation in North Atlantic climate records, 412, 724–727, <https://doi.org/10.1038/35089060>, 2001.
- 760 Waelbroeck, C., Skinner, L. C., Labeyrie, L., Duplessy, J.-C., Michel, E., Vazquez Riveiros, N., Gherardi, J.-M., and Dewilde, F.: The timing of deglacial circulation changes in the Atlantic, 26, <https://doi.org/10.1029/2010PA002007>, 2011.
- Waelbroeck, C., Lougheed, B. C., Vazquez Riveiros, N., Missiaen, L., Pedro, J., Dokken, T., Hajdas, I., Wacker, L., Abbott, P., Dumoulin, J.-P., Thil, F., Eynaud, F., Rossignol, L., Fersi, W., Albuquerque, A. L., Arz, H., Austin, W. E. N., Came, R., Carlson, A. E., Collins, J. A., Dennielou, B., Desprat, S., Dickson, A., Elliot, M., Farmer, C., Giraudeau, J., Gottschalk, J., Henderiks, J., Hughen, K., Jung, S., Knutz, P., Lebreiro, S., Lund, D. C., Lynch-Stieglitz, J., Malaizé, B., Marchitto, T., Martínez-Méndez, G., Mollenhauer, G., Naughton, F., Nave, S., Nürnberg, D., Oppo, D., Peck, V., Peeters, F. J. C., Penaud, A., Portilho-Ramos, R. da C., Repschläger, J., Roberts, J., Rühlemann, C., Salgueiro, E., Sanchez Goni, M. F., Schönfeld, J., Scussolini, P., Skinner, L. C., Skonieczny, C., Thornalley, D., Toucanne, S., Rooij, D. V., Vidal, L., Voelker, A. H. L., Wary, M., Weldeab, S., and Ziegler, M.: Consistently dated Atlantic sediment cores over the last 40 thousand years, Sci Data, 6, 165, <https://doi.org/10.1038/s41597-019-0173-8>, 2019.

775

780