

1 Estimation of CH₄ emission based on advanced 4D-LETKF assimilation system

2 Jagat S. H. Bisht^{1*}, Prabir K. Patra^{1,2}, Masayuki Takigawa¹, Takashi Sekiya¹, Yugo Kanaya¹, Naoko
3 Saitoh², and Kazuyuki Miyazaki³

4 ¹Research Institute for Global Change, JAMSTEC, Yokohama, 235-0019, Japan

5 ²Center for Environmental Remote Sensing, Chiba University, Chiba, 263-8522, Japan

6 ³Jet Propulsion Laboratory/California Institute for Technology, Pasadena, CA, USA,

7 *corresponding author's e-mail: jagatbisht@jamstec.go.jp

8

9 Abstract

10 Methane (CH₄) is the second major greenhouse gas after carbon dioxide (CO₂) which has
11 substantially increased during last decades in the atmosphere, raising serious sustainability and
12 climate change issues. Here, we develop a data assimilation system for in situ and column averaged
13 concentrations using Local ensemble transform Kalman filter (LETKF) to estimate surface emissions
14 of CH₄. The data assimilation performance is tested and optimized based on idealized settings using
15 Observation System Simulation Experiments (OSSEs) where a known surface emission distribution
16 (the truth) is retrieved from synthetic observations. We tested three covariance inflation methods to
17 avoid covariance underestimation in the emission estimates, namely; fixed multiplicative (FM),
18 relaxation to prior spread (RTPS) and adaptive multiplicative. First, we assimilate the synthetic
19 observations at every grid point at the surface level. In such a case of dense observational data, the
20 normalized Root Mean Square Error (RMSE) in the analyses over global land regions are smaller by
21 10-15% in case of RTPS covariance inflation method compared to FM. We have shown that
22 integrated estimated flux seasonal cycles over 15 regions using RTPS inflation are in reasonable
23 agreement between true and estimated flux with 0.04 global normalized annual mean bias. We have
24 then assimilated the column averaged CH₄ concentration by sampling the model simulations at
25 GOSAT observation locations and time for another OSSE experiment. Similar to the case of dense
26 observational data, RTPS covariance inflation method performs better than FM for GOSAT synthetic
27 observation in terms of normalized RMSE (2-3%) and integrated flux estimation comparison with the
28 true flux. The annual mean averaged normalized RMSE (normalized mean bias) in LETKF CH₄ flux
29 estimation in case of RTPS and FM covariance inflation is found to be 0.59 (0.18) and 0.61 (0.23)
30 respectively. The chi-square test performed for GOSAT synthetic observations assimilation suggests
31 high underestimation of background error covariance in both RTPS and FM covariance inflation

32 methods, however, the underestimation is much higher (>100% always) for FM compared to RTPS
33 covariance inflation method.

34 1. Introduction

35 Methane (CH₄) is the second major greenhouse gas, after carbon dioxide (CO₂), that [has](#)
36 anthropogenic sources. According to the contemporary record of [the global CH₄ budget, the total of](#)
37 [all CH₄ sources ranges 538–593 Tg yr⁻¹ during 2008–2017 \(Saunio et al., 2020\)](#). The primary natural
38 sources are from wetlands (~40%). The [main anthropogenic](#) CH₄ emissions are from microbial
39 emissions associated with ruminant (livestock and waste), rice cultivation, fugitive emissions (oil and
40 gas production and use), [and incomplete combustion of bio and fossil fuels](#). The major fraction of
41 atmospheric CH₄ sinks (range: 474 - 532 Tg yr⁻¹) occurs in the troposphere by oxidation via reaction
42 with hydroxyl (OH) radicals (Patra, et al., 2011; Saunio et al., 2020); other loss processes include
43 oxidation by soil, and reactions with O¹D and Cl. The lifetime of CH₄ in the atmosphere is estimated
44 to be 9.1 ± 0.9 years (Szopa et al. 2021).

45 Regional CH₄ emissions can be estimated from CH₄ concentration fields and chemistry transport
46 models using Bayesian synthesis approaches based on inverse modeling techniques (e.g., Enting,
47 2002). In such approach, emissions are optimized on a coarse resolution (e.g., for a limited number of
48 pre-defined regions) mostly using surface-based observations. CH₄ concentrations are provided by the
49 NOAA cooperative air sampling network sites (Dlugokencky et al., 2020) and other networks by the
50 World Data Centre for Greenhouse Gases (WDCGG) website, hosted by the Japan Meteorological
51 Agency. In the recent years, satellite measurements are made from the Greenhouse Gases Observing
52 Satellite (GOSAT) or the TROPOspheric Monitoring Instrument (TROPOMI) (Lorente et al., 2021),
53 covering the globe with fine spatio-temporal scales. GOSAT provide an extensive global observations
54 of column CH₄ [concentrations](#) since 2009 (Yoshida et al., 2013). Some of the inverse modeling
55 studies utilize the satellite observations for CH₄ flux estimation (Zhang et al., 2021; Maasakkers et al.,
56 2016), but, it requires enormous computational resources while dealing with more flux regions and
57 more observations.

58 Grid-based CH₄ flux optimization is also performed using adjoint technique (4-D Var data
59 assimilation) and Ensemble Kalman Filter (EnKF), but was limited to small sets of observations
60 (Houweling et al., 1999; Meirink et al., 2008; Bruhwiler et al., 2014). Bruhwiler et al. (2014) followed
61 the EnKF method of Peters et al. (2005) to estimate the CH₄ surface fluxes that utilizes an off-line
62 ACTM framework. Techniques such as 4-D Var and EnKF are important to estimate CH₄ fluxes since
63 they can assimilate a large number of observations, manage high-resolution fluxes. In the EnKF
64 system, a flow-dependent forecast error covariance structure is provided by ensemble model forecasts,
65 while it does not need an adjoint model that makes it simple but powerful tool for flux estimation.

66 One of the limitations in EnKF method is the dependence of the resolution of state vector on
67 ensemble size, which can give spurious results if the number of ensemble members is much smaller
68 than the rank of the error covariance matrix (Houtekamer and Zhang, 2016).

69 LETKF is a type of square-root EnKF that performs analysis locally in space without perturbing the
70 observations (Ott et al., 2002, 2004; Hunt et al., 2007). LETKF is computationally efficient since the
71 observations are assimilated simultaneously not serially, it is simple to account for observation error
72 correlation. Miyazaki et al. (2011) and Kang et al. (2012) demonstrated the implementation of
73 LETKF data assimilation system by coupling an ACTM for carbon-cycle research using atmospheric
74 CO₂ observations. It is also extensively applied for the emission estimation of short-lived species
75 using satellite data (Skachko et al., 2016; Miyazaki et al., 2019; Sekiya et al., 2021). In this work, we
76 will estimate the CH₄ fluxes using a LETKF data assimilation system. Assimilation windows ranging
77 from 6 hours (Kang et al., 2012) to several months (Bruhwiler et al., 2014) have been used, depending
78 on the desired time resolution of the estimated emissions, which is often limited by the observational
79 data density. The time frame over which the system behaves linearly, and in what time frame the
80 observations respond to the control variables such as, atmospheric transport, as well as observation
81 abundance, must also be taken into consideration. Within an assimilation window, where and when
82 the fluxes would be constrained by specific observations is to be ascertained by the correlation
83 between ensemble prior fluxes and the ensemble CH₄ concentrations simulation from a forward
84 model (Liu et al., 2016).

85 main objective of this work is to develop an advanced 4-D data assimilation system based on LETKF
86 that simultaneously estimates atmospheric distributions and surface fluxes of CH₄. OSSEs are
87 conducted to assess the performance of LETKF since it is important to test the system against the
88 known emissions or the truth. The OSSE LETKF set-up of top-down CH₄ flux estimation using online
89 ACTM is an essential step before implementing on real in situ and satellite observation.

90 **2. Formulation of LETKF system**

91 We briefly describe the LETKF in the application of CH₄ flux estimation, while detailed derivation of
92 equations and code implementation are given elsewhere (Hunt et al., 2007; Miyazaki et al., 2011;
93 Miyoshi et al., 2010). The notation used here for LETKF formulation is adopted from Kotsuki et al.
94 (2017). In the LETKF, the background ensemble (columns of matrix x^b) in a local region evolved
95 from a set of perturbed initial conditions. The background ensemble mean, \bar{x}^b , and its perturbation,
96 X^b , are estimated from the ensemble forecast such as:

$$\bar{x}^b = \frac{1}{m} \sum_{i=1}^m x_i^b; \quad X_i^b = x_i^b - \bar{x}^b \quad (1)$$

97 Where ‘m’ indicates the ensemble size. The background error covariance matrix P^b in the m-
 98 dimensional ensemble is defined as:

$$P^b = \frac{1}{m-1} X^b [X^b]^T \quad (2)$$

99 The analysis ensemble mean \bar{x}^a is derived using background ensemble mean \bar{x}^b and ensemble
 100 perturbations X^b such as:

$$\bar{x}^a = \bar{x}^b + X^b \tilde{P}^a (Y^b)^T R^{-1} (y^o - H\bar{x}^b) = \bar{x}^b + X^b w^a \quad (3)$$

101 where H, Y, R, and \tilde{P}^a denote the linear observation operator, ensemble perturbation matrix in the
 102 observation space ($Y \equiv Hx$), observation error covariance matrix, and analysis error covariance matrix
 103 in the ensemble space, respectively. The superscripts ‘o’, ‘b’ and ‘a’ denote the observations,
 104 background (prior), and analysis (posterior), respectively. w^a defines the analysis increment (or
 105 analysis weight) in observation space and is derived using the information about observational
 106 increment $y^o - H\bar{x}^b$. The analysis error covariance matrix (\tilde{P}^a) in the m-dimensional ensemble space
 107 is spanned by ensemble perturbation (Hunt et al., 2007) and defined as:

$$\tilde{P}^a = \{(m-1)I + (HX^b)^T R^{-1} HX^b\}^{-1} \quad (4)$$

108 Finally, the analysis ensemble perturbations X^a at the central grid point are derived such as:

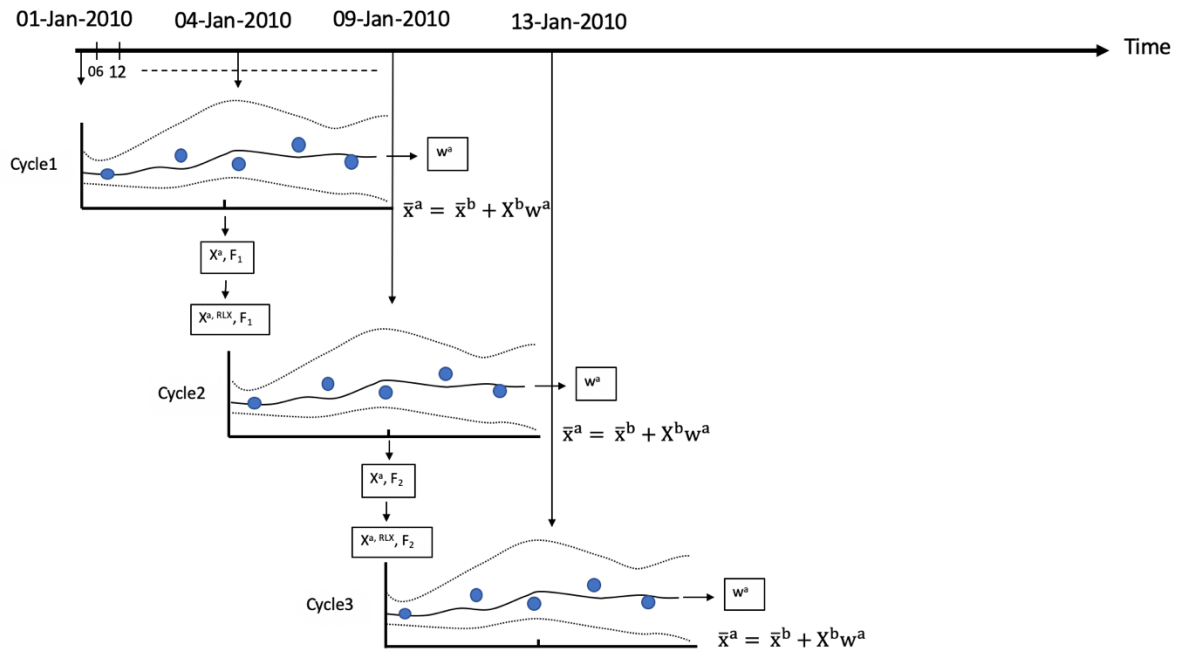
$$X^a = X^b \{(m-1)\tilde{P}^a\}^{1/2} \quad (5)$$

109 Where, $\{(m-1)\tilde{P}^a\}^{1/2}$ is a multiple of the symmetric square root of the local analysis error
 110 covariance matrix in ensemble space and could be computed by singular vector decomposition
 111 method.

112 We have applied a gross error check as a quality control to exclude observations that are far from the
 113 first guess, the appropriate degrees of the gross error check are also examined. Figure 1 shows the
 114 schematic diagram of our LETKF set-up with two ensemble members for 3 consecutive assimilation
 115 cycles with 8 days assimilation window. The analysis is obtained at mid-point time of the assimilation
 116 window (Figure 1). The analyzed (updated) surface flux is used for next data assimilation cycle
 117 starting from the mid-point time of the previous data assimilation window. The state vector
 118 augmentation approach is used to estimate the atmospheric CH₄ surface flux (Kang et al., 2012;
 119 Miyazaki et al., 2011).

120 Assimilation window size and ensemble members are chosen based on computational efficiency and
 121 estimation accuracy. A larger assimilation window means fluxes are constrained by more

122 observations, however, it requires handling of large matrix optimization which is difficult in cases of
 123 dense observation and introduces sampling errors related to transport errors. [In this study](#), few
 124 sensitivity experiments performed to demonstrate the choice of [assimilation window length and](#)
 125 ensemble size when GOSAT synthetic observation are assimilated [in](#) Section 4.2.



126

127 **Figure 1:** Schematic represents the temporal evolution of LETKF cycle. In the first assimilation
 128 window (Cycle1), the [dotted](#) lines show the ensemble forecast of CH₄ concentrations (with 2
 129 ensemble members), the solid line shows the linear combination of the forecasts, the filled circles
 130 show the observations of CH₄ concentration. The data assimilation finds the linear combination of the
 131 ensemble forecast by estimating the weight (w^a) that best fits the observations throughout the
 132 assimilation window. The analysis weight is applied to obtain optimal surface fluxes (F) and the
 133 concentration of CH₄ at the intermediate time of the data assimilation window. The updated analyzed
 134 concentration ensembles are used as initial condition after relaxation ($X^{a,RLX}$) (Eq. 8) for the next
 135 ensemble forecast. The spread of the ensemble members represents the forecast error. The schematic
 136 is adapted from Kalnay & Yang (2010) and Miyazaki et al. (2011).

137 2.1 Covariance inflation

138 The LETKF data assimilation needs variance inflation to mitigate the under dispersive ensemble. We
 139 tested three methods; fixed multiplicative (FM), relaxation-to-prior spread (RTPS), and adaptive
 140 multiplicative covariance inflation.

141 The fixed multiplicative (FM) inflation method (Anderson and Anderson, 1999) inflates the prior
 142 ensemble by inflating the background error covariance matrix P^b defined in equation (Eq. 2) such as:

$$P_{\text{inf}}^{\text{b}} = \gamma P_{\text{tmp}}^{\text{b}} \quad (6)$$

143 where $P_{\text{tmp}}^{\text{b}}$ represents the temporary background error covariance matrix which is inflated by a factor
 144 γ .

145 The other inflation methods used to prevent the reduction of ensemble spread are relaxation-to-prior
 146 perturbation (RTPP) (Zhang et al., 2004) and [relaxation-to-prior spread \(RTPS\)](#) (Whitaker and
 147 Hamill, 2012). The RTPP methods relax the reduction of the ensemble spread after updating the
 148 ensemble perturbations which blends the background and analysis ensemble perturbations as:

$$X_{\text{inf}}^{\text{a}} = \alpha_{\text{RTPP}} X^{\text{b}} + (1 - \alpha_{\text{RTPP}}) X_{\text{tmp}}^{\text{a}} \quad (7)$$

149 where α_{RTPP} denotes the relaxation parameter of the RTPP.

150 [The RTPS inflation method](#) relaxes the reduction of ensemble spread by relaxing the analysis spread
 151 to prior spread such as:

$$X_{\text{RLX}}^{\text{a}} = \left(\frac{\alpha_{\text{RTPS}} \sigma^{\text{b}} + (1 - \alpha_{\text{RTPS}}) \sigma^{\text{a}}}{\sigma^{\text{a}}} \right) X_{\text{tmp}}^{\text{a}} \quad (8)$$

152 where σ and α_{RTPS} denote the ensemble spread, and relaxation parameter of the RTPS, respectively.
 153 The range of parameter α_{RTPS} is bounded by $[0, 1]$. This study focuses mainly on the FM and RTPS
 154 covariance inflation methods.

155 In addition, Miyoshi (2011) applied adaptive inflation by determining the multiplicative inflation
 156 factors at every grid point at every analysis step using the observation-space statistics derived by
 157 Daley (1992) and Desroziers et al. (2005).

$$\langle dd^{\text{T}} \rangle = H P_{\text{inf}}^{\text{b}} H^{\text{T}} + R \quad (9)$$

158 Where the operator ' $\langle \bullet \rangle$ ' denotes the statistical expectation and $d = y^{\text{o}} - H \bar{x}^{\text{b}}$ (observation-minus-
 159 first-guess), and R is the error observation covariance matrix.

160 The impact of using the adaptive multiplication inflation method is discussed in the GOSAT synthetic
 161 observation assimilation experiments in Section 4.2.

162 2.2 MIROC4-ACTM

163 Model for Interdisciplinary Research on Climate, version 4.0 (MIROC4) based ACTM (hereafter
 164 referred to as MIROC4-ACTM) (Patra et al., 2018; Bisht et al., 2021) is used here for CH_4
 165 concentration simulations. The model simulations have been performed at horizontal grid resolution
 166 of approximately $2.8 \times 2.8^\circ$ latitude-longitude grid (T42 spectral truncations) and hybrid vertical

167 coordinate of 67 levels (Earth's surface to 0.0128 hPa, Watanabe et al., 2008). Bisht et al., 2021
168 performed the multi-tracer analysis and demonstrated the importance of very well-resolved
169 stratosphere in the MIROC4-ACTM that illustrates better extratropical stratospheric variabilities, and
170 simulated tropospheric dynamical fields. The meteorological fields in MIROC4-ACTM are nudged to
171 the JMA Re-analysis (JRA-55) data (Kobayashi et al., 2015).

172 **3. Experimental set-up**

173 **3.1 Construction of known surface emissions (truth)**

174 Present OSSEs intend to develop basic tuning strategies before the actual data to be assimilated which
175 is useful to accelerate the operational use of real observations. The OSSE has been discussed here by
176 exploiting the known “truth”. The synthetic observations to be assimilated in the OSSE are generated
177 from nature runs which uses bottom-up surface emission (true) data to simulate global 3-D CH₄
178 concentrations. The true surface CH₄ emissions are prepared on the monthly scale using
179 anthropogenic and natural sectors, minus the surface sinks due to bacterial consumption in the soil
180 (Chandra et al., 2021). The anthropogenic emissions were obtained from the Emission Database for
181 Global Atmospheric Research, version 4.3.2 inventory (EDGARv4.3.2) (Maenhout et al., 2019) that
182 includes the emissions from the major sectors such as; fugitive, enteric fermentation and manure
183 management, solid waste and wastewater handling. The biomass burning emissions are taken from the
184 Global Fire Database (GFEDv4s) (van der Werf et al., 2017) and Goddard Institute for Space Studies
185 emissions (Fung et al., 1991). The wetland and rice emissions are taken from the process-based model
186 of the terrestrial biogeochemical cycle, Vegetation Integrated Simulator of Trace gases (VISIT) (Ito,
187 2019) that is based on Cao et al. (1996). The other natural emission such as, ocean, termites, mud
188 volcano are taken from TransCom-CH₄ inter-comparison experiment (Patra et al., 2011). The total
189 emissions are taken as the truth for the OSSEs and the concentration simulated by MIROC4-ACTM
190 will be referred to as synthetic observations.

191 **3.2 Prior flux preparation and LETKF setting**

192 Based on our understanding of CH₄ inverse modelling, the uncertainty in regional flux estimation is
193 found to be 30% or lower (Chandra et al., 2021). Therefore, we attempted to reproduce the true flux
194 by starting with a prior flux that is lower by 30% of the true flux (prior flux has same seasonal cycles
195 as true flux). The MIROC4-ACTM is initialized with the spin-up of 3 years (2007 – 2009) with prior
196 flux distribution. The initial CH₄ distribution on 01 January 2007 was taken from an earlier simulation
197 of 27 years. An initial perturbation with standard deviation of approximately 6-8% spread is applied
198 to the a priori flux as the initial ensemble spread. The sensitivity of the initial ensemble spread to CH₄
199 flux estimation is discussed in Section 4.2. The uncertainty to perturb prior fluxes is generated based

200 on random positive values with normal distribution. The monthly scale prior emission is linearly
201 interpolated at 6 hourly intervals to be used in the MIROC4-ACTM simulation for data assimilation.
202 This study performs two LETKF data assimilation experiments. In [these experiments](#), we provided
203 initial perturbation on regional basis over land (53 different land regions; Chandra et al., 2021) and at
204 every grid over ocean, no spatial error correlation between grid points is considered among ensemble
205 members. [However, in Section 4.2.5](#), we also discussed the sensitivity of CH₄ data assimilation by
206 [providing](#) initial ensemble [spread](#) at every grid by considering horizontal spatial error correlation
207 between grid points among ensemble members, with a global mean correlation of 20%.

208 3.3 Experiment 1: Synthetic dense observation formulation

209 The OSSE setting with very accurate and dense observation surface [data](#) is an attempt to demonstrate
210 that data assimilation system works reasonably in the estimation of the true surface flux. [Errors in the](#)
211 [estimated flux could arise due to the insufficient ensemble size and also the implemented inflation](#)
212 [methods to overcome the under-sampling, along with](#) simplified forecast process [of emissions](#). In real
213 [data assimilation, there are additional sources of potential errors, such as, atmospheric transports, and](#)
214 [inappropriate prior or observation uncertainties](#). In [our OSSEs](#), CH₄ fluxes as mentioned in Section
215 3.2 are used as “true” fluxes in generating synthetic observations (CH₄ concentrations). [In the](#)
216 [experiment 1, the simulated](#) surface layer CH₄ concentrations at each grid [for the entire globe were](#)
217 [used as synthetic assimilated observations](#). We added a constant measurement uncertainty of 5 ppb,
218 which is typically achieved by the present-day measurement systems (e.g., Dlugokencky et. al, 2020).

219 [In this study, the CH₄ observations are assimilated by applying the observation error covariance](#)
220 [localization](#) (Kotsuki et al., 2020) [to reduce the spurious spatial correlation due to smaller ensemble](#)
221 [size than the degrees of freedom of the system \(\$R \leftarrow R \times \exp\left\(-\frac{1}{2}\{\(d_h/\sigma_h\)^2 + \(d_v/\sigma_v\)^2\}\right\)\$ \)](#). Where
222 [d_h and d_v denote the horizontal distance \(km\) and vertical difference \(log\[Pa\]\) between the analysis](#)
223 [model grid point and observation location](#). The tunable parameters [σ_h and σ_v are the horizontal](#)
224 [localization scale \(km\) and vertical localization scale \(log\[Pa\]\), respectively](#). [Using the spatial](#)
225 [localization technique, we](#) have estimated the CH₄ flux for each grid by choosing the [CH₄](#)
226 [observations](#) that influence the grid point using optimal cutoff radius ($\approx 3.65\sigma_{h,v}$; Miyoshi et al.,
227 2007) [with horizontal covariance localization \(σ_h\)](#) of 2200 km and vertical covariance localization
228 [\(σ_v\)](#) of 0.3 in the natural logarithmic pressure ([log\[Pa\]](#)) coordinate. [The localization is performed to](#)
229 [improve the signal to noise ratio of ensemble-based covariance](#). Numerous sensitivity experiments
230 [have been performed by varying the horizontal and vertical localization length in order to obtain the](#)
231 [optimized CH₄ flux that best compare with the truth](#). The LETKF assimilates the observations within
232 the specified radius to solve the analysis state at each grid point independently (Liu et al., 2016). State
233 vector of the analysis includes the atmospheric CH₄ concentration, which is the prognostic variable of
234 forecast model and the state vector is further augmented by surface CH₄ flux, which is not a model

235 prognostic variable. This augmentation enables the LETKF to directly estimate the parameter through
 236 the background error covariance with observed variables (Baek et al., 2006). The state vector
 237 augmentation is implemented similar to that used by Miyazaki et al. (2011). This approach analyses
 238 CH₄ flux during the analysis step. The purpose of the simultaneous CH₄ emission and concentration
 239 optimization is to reduce the uncertainty of the initial CH₄ concentrations on the CH₄ evolution during
 240 the assimilation window and to maximize the observations potential (Tian et al., 2014).

241 The atmospheric CH₄ concentration is changed during both the analysis and forecast steps. A
 242 challenge of this scheme is that, the analysis increment is added to the model state at each analysis
 243 step, without considering the global total CH₄ mass conservation in the model, but consistent with the
 244 observed local CH₄ abundance.

245 In this case, surface flux at every model grid point is analyzed with 8-days assimilation window
 246 during the year 2010 with the 100 ensemble members. The ensemble size and assimilation window
 247 are chosen based on the CH₄ flux estimation accuracy calculated by performing sensitivity experiment
 248 for ensemble size (60, 80, and 100) and assimilation window (3-days and 8-days), respectively (not
 249 shown).

250 **3.4 Experiment2: synthetic satellite observation formulation**

251 One way to address the real-world CH₄ flux estimation problem is to first make the OSSE dataset like
 252 real observations. In this OSSE experiment, we have assimilated synthetic column average CH₄
 253 concentrations with a coverage mimicking GOSAT satellite observations. We prepared a model
 254 simulated column averaged CH₄ concentrations (XCH₄) dataset that is spatiotemporally sampled with
 255 GOSAT_observations as follows:

$$XCH_4 = XCH_{4(a\ priori)} + \sum_j h_j a_j (CH_{4(ACTM)} - CH_{4(a\ priori)})_j \quad (10)$$

256 Where, XCH₄ is the column-averaged model simulated CH₄ concentration. XCH_{4(a priori)} is a priori
 257 column-averaged concentration. CH_{4(ACTM)} and CH_{4(a priori)} are the CH₄ profile from ACTM and a
 258 priori, respectively. h_j is the pressure weighting function (j is the vertical layer index), and a_j
 259 represents averaging kernel matrix for the column retrieval which is the sensitivity of the retrieved
 260 total column at the various ('j') atmospheric levels. In the next step, we added the same retrieval
 261 (XCH₄) error as GOSAT to the XCH₄(ACTM simulated) to make the OSSE more realistic and then
 262 attempt to estimate the true fluxes.

263 In this case, the CH₄ flux has been estimated for each grid by choosing the CH₄ observation with
 264 cutoff radius ($\simeq 3.65 \sigma_{h,v}$) with horizontal covariance localization (σ_h) of 5000 km and vertical
 265 covariance localization (σ_v) of 0.35 in the natural logarithmic pressure (log[Pa]) coordinate. The

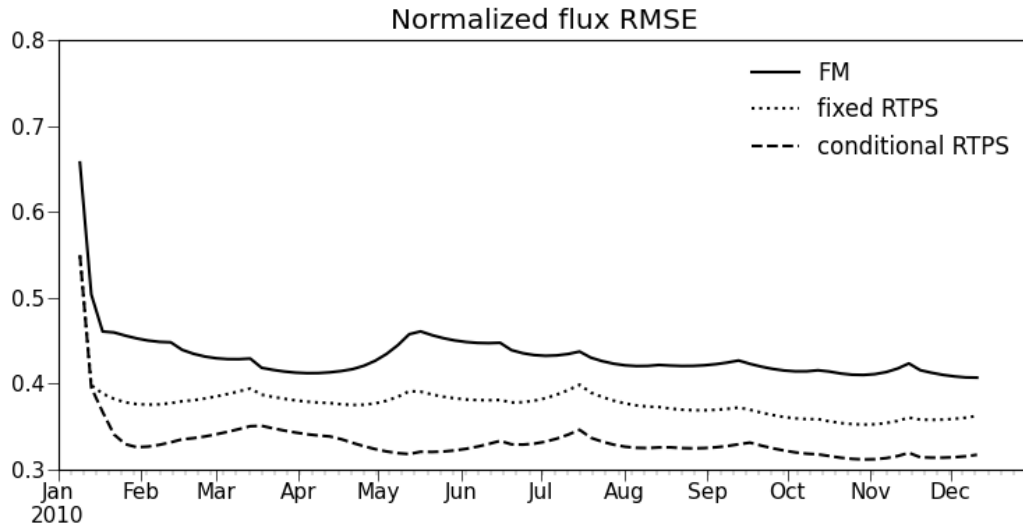
266 optimal [horizontal](#) and vertical covariance localization values are chosen based on trial and error
267 method ([those best fits to estimate CH₄ flux when compared with truth](#)). A long cutoff radius has been
268 chosen due to sparse observational coverage of GOSAT. [The surface flux is analyzed at every model](#)
269 [grid point with 8-days assimilation window and 100 ensemble members those are chosen based on](#)
270 [sensitivity experiments discussed in Section 4.2.](#)

271 4. Results and Discussion

272 4.1 Experiment with dense OSSE

273 The time series of normalized RMSE ($\sqrt{\sum_{i=1}^n (x_i^a - x_i^t)^2 / n / \bar{x}^t}$; x_i^a and x_i^t is the analysis and true
274 state at i th model grid point, n is the total number of grid points, and \bar{x}^t represents the mean of true
275 flux) in the analyses over global landmass region is shown in Figure 2. The normalized global RMSE
276 is calculated using FM and RTPS inflation methods (Fig. 2) after assimilating synthetic observation at
277 every grid (Section 3.4). [Noteworthy is that](#) the experiment with FM inflation method shows 10-15%
278 larger error in estimating the atmospheric surface CH₄ flux compared to RTPS inflation method. One
279 of the reasons of better RMSE using RTPS inflation method is due to the more degrees of freedom
280 provided by relaxation (α_{RTPS}) in ensemble spread (Eq. 8) that could nudge the ensemble of CH₄
281 [concentrations](#) towards observations. The initial flux analysis spread using RTPS and FM is shown in
282 supporting information (Fig. S1) which shows larger initial analysis flux spread over Brazil, tropical
283 America, and Asia in RTPS inflation compared to FM inflation method. We performed numerous
284 sensitivity test with RTPS inflation method and found that uniform relaxation is not substantial, for
285 some of the regions. Figure 2 shows the RMSE for FM, fixed RTPS ($\alpha_{\text{RTPS}} = 0.4$, applied globally,
286 the optimized value is obtained by manual fine tuning) and conditional RTPS ($\alpha_{\text{RTPS}} = 0.3-0.7$
287 applied different α_{RTPS} regionally by manual fine tuning). We find that the conditional RTPS method
288 improves the accuracy by ~5% compared to fixed RTPS and 10-15% compared to FM.

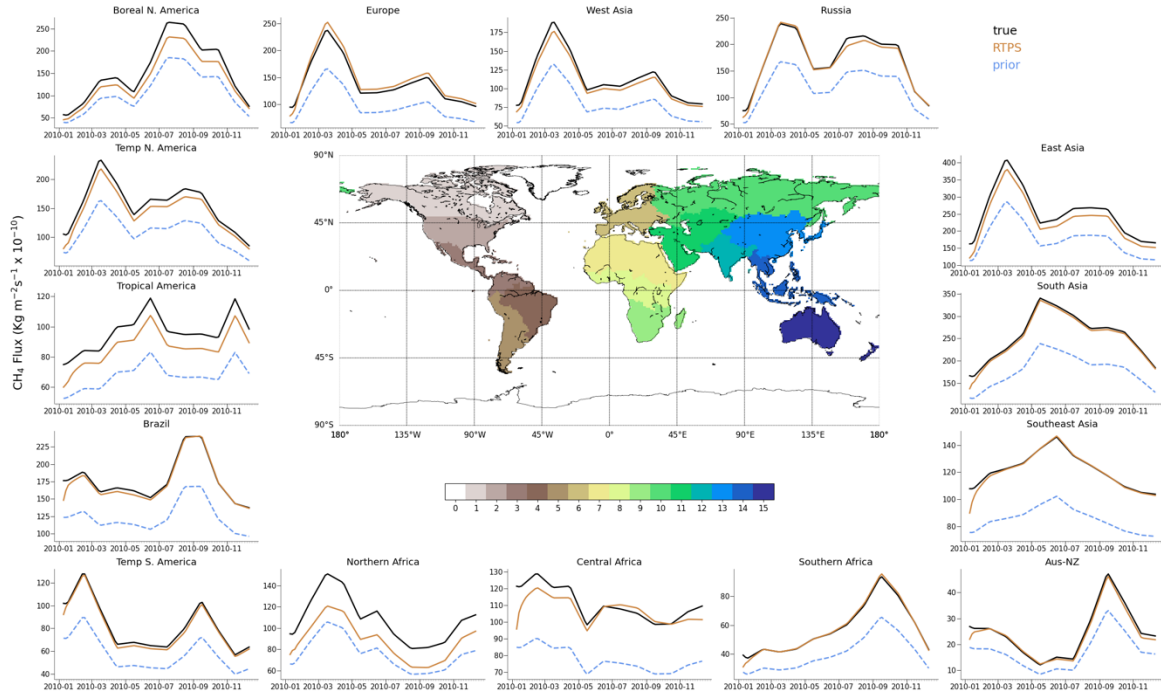
289 We have also shown RMSE (not normalized) of surface flux in supplementary information (Fig. S2).
290 Flux RMSE has been estimated globally for both the inflation methods, and also for south of 20°N (by
291 considering only those land grids which fall into south of 20°N; Fig. S2) for comparative purposes. It
292 could be noticed that (supporting information Fig. S2), above north of 20°N, the flux estimation error
293 is higher, specifically during spring-summer when CH₄ emissions peak over most of the northern
294 hemispheric regions (Fig. 3). The high uncertainty during spring-summer (Fig. S2) in the flux
295 estimation over these regions could appear due to the attenuation of surface observations as a result of
296 active vertical mixing. The RMSE during autumn (Fig. S2) is comparable in case of global and south
297 of 20°N, which indicates RMSE arising from southern hemispheric regions, likely over Brazil as it
298 peaks during autumn (Fig. 3).



299

300 **Figure 2.** Time series of normalized RMSE of surface CH₄ flux analysis, for 1 year of data
 301 assimilation using FM, fixed RTPS, and conditional RTPS inflation methods over global landmass
 302 region.

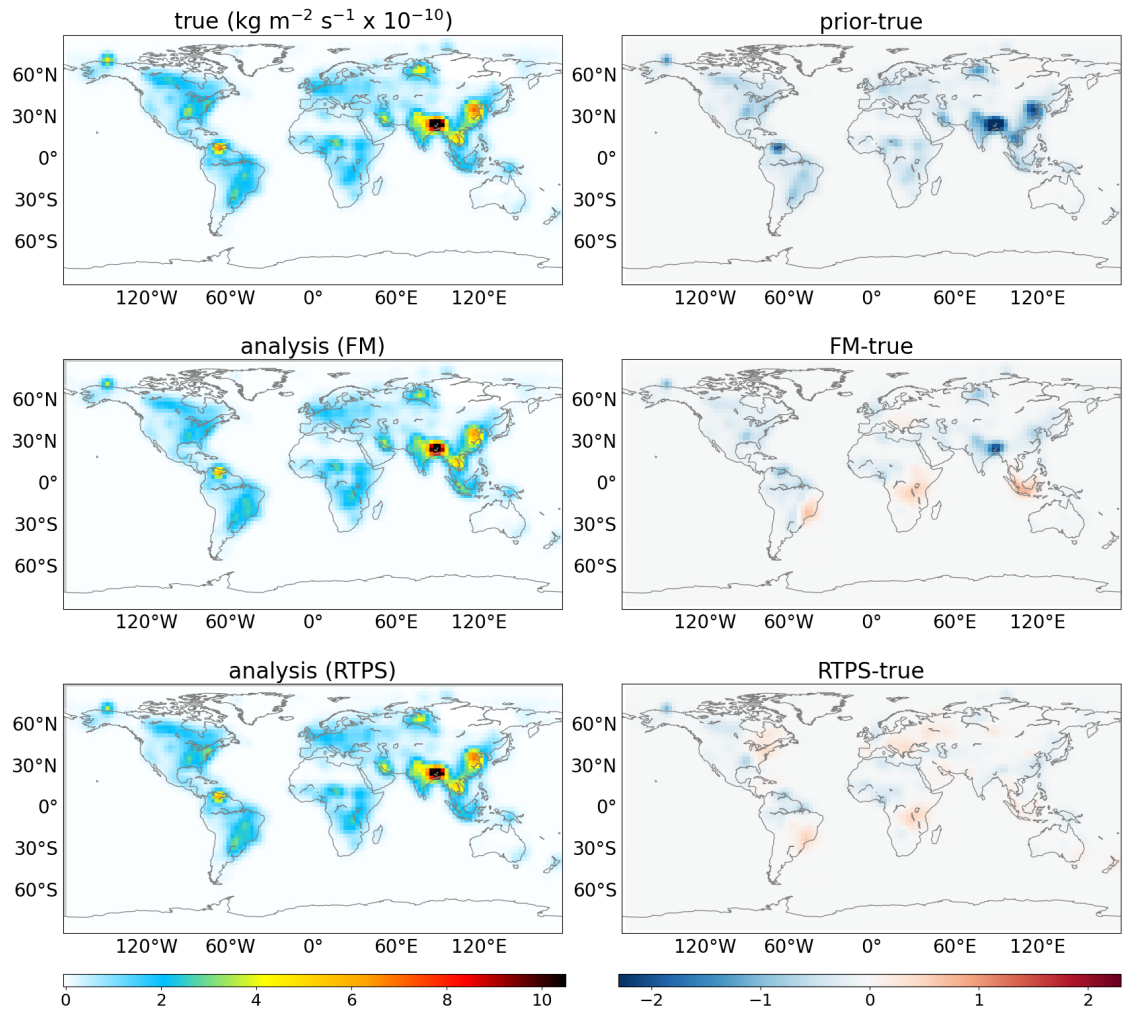
303 Figure 3 shows regional total flux seasonal cycles comparison of the estimated fluxes for 15 terrestrial
 304 regions with those of the prior and true fluxes. The estimated flux retrieved using RTPS inflation
 305 method over different regions agrees well with that of true flux. We intend to show the capability of
 306 LETKF estimated fluxes over these regions using surface observations to mimic the true fluxes in our
 307 understanding of terrestrial biosphere CH₄ cycle. These results are consistent with Figure 2 with
 308 annual global normalized mean bias ($\sum_{i=1}^n(x_i^a - x_i^t)/\sum_{i=1}^n(x_i^t)$) of -0.04. It could also be noticed
 309 from Figure 3 that estimated fluxes converge to true fluxes over most of the regions after about 2-3
 310 months.



311

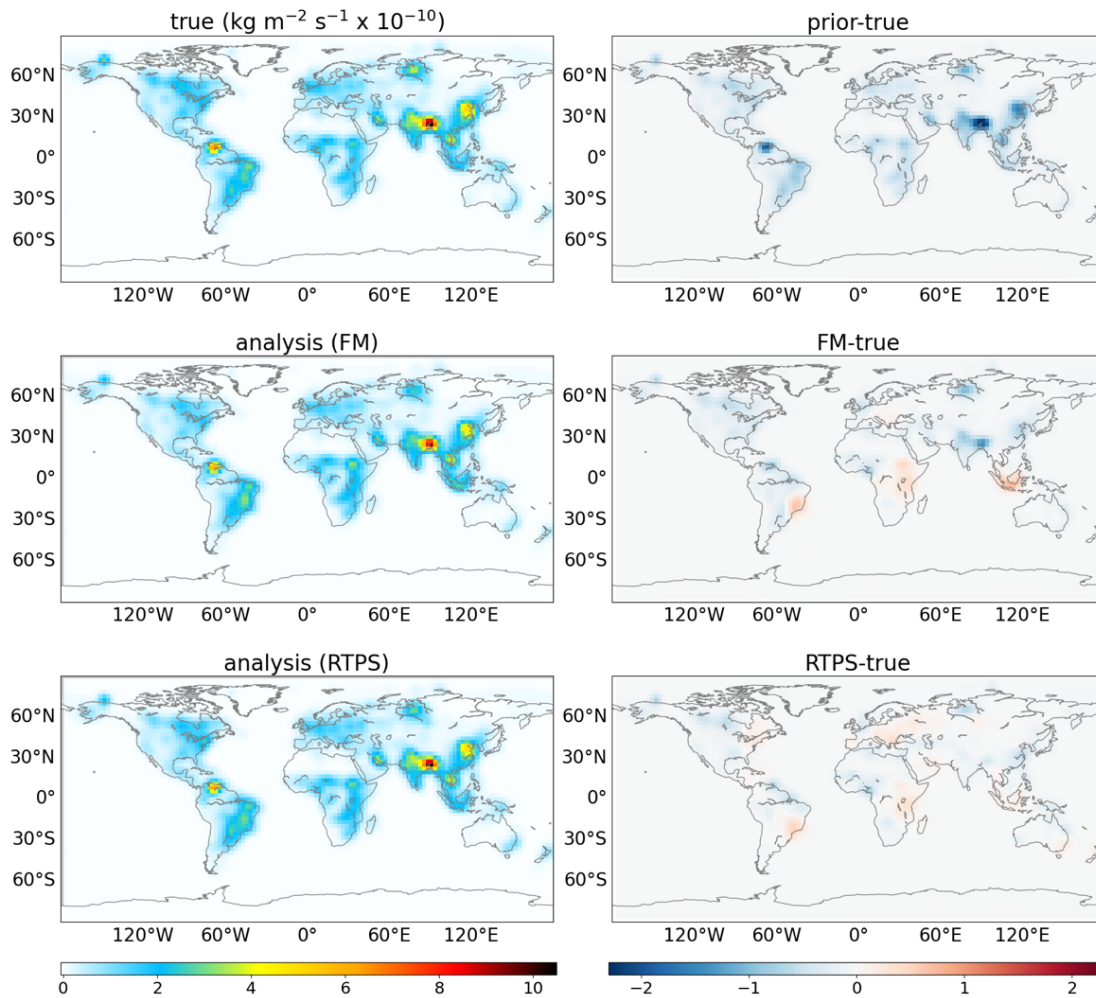
312 **Figure 3.** The 1-year CH₄ total flux seasonal cycles of true (black), prior (blue), and estimated from
 313 the LETKF (orange) RTPS inflation method in 15 regions after assimilating dense synthetic surface
 314 CH₄ observations.

315 To see the degree of similarity in the flux distribution between the estimated and true fluxes, we show
 316 monthly mean spatial flux distribution for June, and November in Figure 4 and 5, respectively, along
 317 with the bias in prior and estimated flux. As shown in Figures 4 and 5, the general spatial patterns of
 318 the true flux are estimated well. These results suggest that, our LETKF system is capable of
 319 reproducing continental spatial flux patterns by using such an idealized dense surface observational
 320 [data](#). However, some clear differences in flux estimation could be noticed from FM and RTPS
 321 inflation method (Figs. 4 and 5), for e.g., over Eurasian and American continent, analysis with RTPS
 322 shows clear improvement compared to FM covariance inflation method. We calculated the global
 323 mean normalized bias with RTPS and FM covariance inflation method which is found to be -0.04 and
 324 -0.11, respectively over land regions that shows RTPS significantly improved the flux estimation
 325 compared to FM covariance inflation method.



326

327 **Figure 4.** Spatial distribution of surface CH₄ fluxes (true; top left panel, FM analysis; middle left
 328 panel, RTPS analysis; bottom left panel) and the associated bias in prior (prior-true; top right panel)
 329 and estimated (FM-true; middle right panel, RTPS-true; bottom right panel) fluxes during June, 2010.



330

331 **Figure 5.** Same as Figure 4 but for November, 2010.

332 **4.2 Experiment by mimicking the real satellite observational data set**

333 In this section we discuss the LETKF flux estimation by assimilation of GOSAT synthetic CH₄
 334 concentration observations. Figure 6 shows the model simulated mean XCH₄ concentration sampled
 335 spatiotemporally with GOSAT observations during January and July for the year 2010 (sampling
 336 method discussed in Section 3.4). In this case we have shown different LETKF sensitivity
 337 experiments such as; LETKF sensitivity to (1) FM, RTPS, adaptive multiplicative inflation (2)
 338 assimilation window (3) ensemble size, (4) chi-square test, (5) prior ensemble spread. In the LETKF
 339 sensitivity experiments from 1-4, the initial ensemble spread provided similar way as Experiment 1.

340 **4.2.1 LETKF sensitivity to FM, RTPS, and adaptive multiplicative inflation**

341 This study mainly emphasizes on FM and RTPS inflation methods used in CH₄ LETKF data
 342 assimilation. The annual average normalized RMSE (absolute bias) with RTPS and FM covariance
 343 inflation is found to be 0.59 (0.18) and 0.64 (0.22), respectively. The RTPS inflation method performs

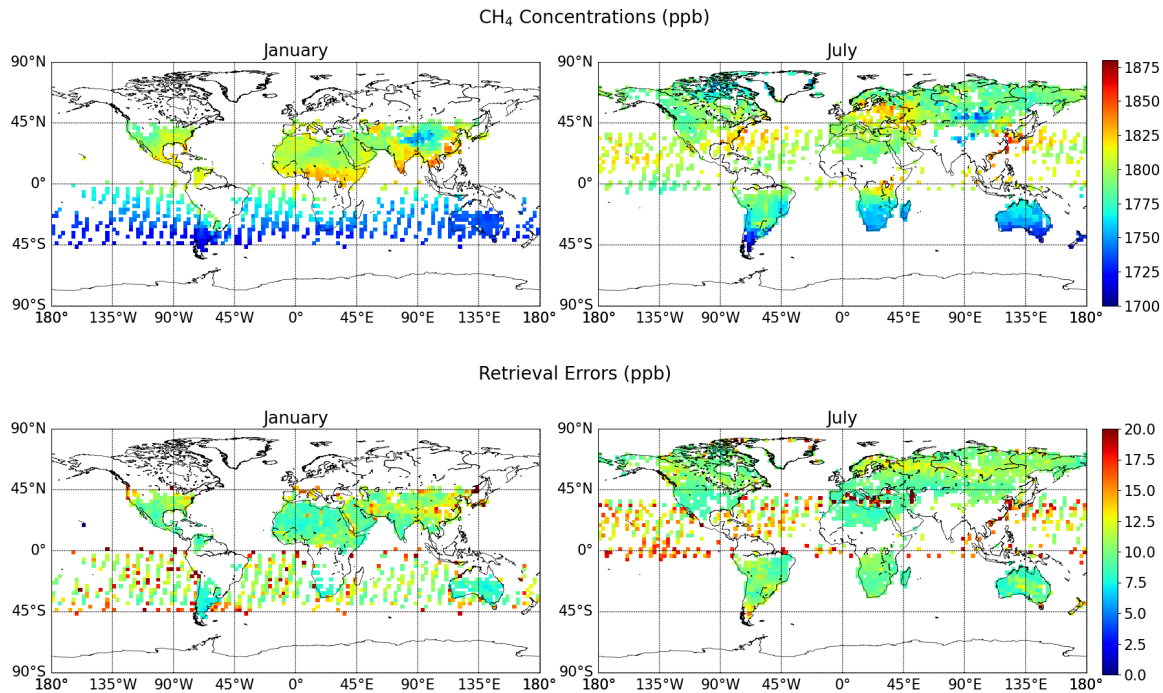
344 better than the FM inflation method overall. In addition to RTPS inflation, sensitivity test is also
345 performed using adaptive multiplicative inflation methods.

346 In the adaptive inflation, we need to provide an initial multiplicative inflation factor at the beginning
347 of data assimilation cycle (Cycle 1 in Fig. 1). Following the method of Deroziers et al. (2005), the
348 multiplication inflation factor information calculated in previous cycle (i.e. Cycle1 in Fig. 1) is used
349 for next data assimilation cycle at every grid point (Cycle 2 in Fig. 1). We perform two sensitivity
350 experiments. In the first (second) case we provided 50% (40%) initial inflation in the beginning of
351 Cycle 1 (Fig. 1). The normalized RMSE in the both the adaptive inflation sensitivity experiments are
352 comparable (0.65, Supporting information Fig. S3a) till July, but from the beginning of August,
353 RMSE increases exponentially in the first experiment. However, in terms of chi-square distribution
354 CH₄ flux estimation with first sensitivity adaptive multiplicative inflation experiment (50% initial
355 inflation case) is better than second sensitivity experiment (Supporting information Fig. S3b; chi-
356 square test described in Section 4.2.4). To identify the regions of high estimated CH₄ flux error, we
357 have shown the background error spread in CH₄ flux estimation over 15 regions (Supporting
358 information Fig. S3c) and found that spread over west and south east Asia rises exponentially post
359 July that indicates the rise of estimated CH₄ flux error over these regions in the first sensitivity
360 adaptive multiplicative inflation experiment. Our analysis suggests that CH₄ flux estimation is
361 depending on the initial inflation factor provided in the beginning of data assimilation cycle (Cycle 1,
362 Fig. 1) in adaptive multiplication method. Also, we need to be very careful to monitor the background
363 error spread evolution with time to estimate the CH₄ flux with adaptive inflation, chi-square
364 distribution analysis is not sufficient.

365 In case of RTPP inflation, we found the parameter α_{RTPP} is very difficult to fine-tuned due to its very
366 high sensitivity to estimate the CH₄ flux. We fail to obtain an optimized α_{RTPP} value to estimate the
367 CH₄ flux. Whitaker & Hamill, 2012, also demonstrated the better accuracy in LETKF meteorological
368 data assimilation with RTPS compared to RTPP covariance inflation method. They found RTPP
369 method produces very large errors if the inflation parameter exceeds the optimal value.

370 **4.2.2 Assimilation window**

371 The LETKF data assimilation window length determines the time span of the observations assimilated
372 in each assimilation cycle. We have shown the sensitivity of two assimilation window size
373 configurations; 3 days and 8 days in supporting information Figure S4. Our sensitivity experiments
374 with window size configurations show that 8 days long assimilation window estimates the CH₄ flux
375 with better accuracy (~10%) compared to 3 days assimilation window, because more observational
376 information is incorporated into the system with 8 days long assimilation window. This study uses 8
377 days assimilation window for CH₄ LETKF data assimilation.

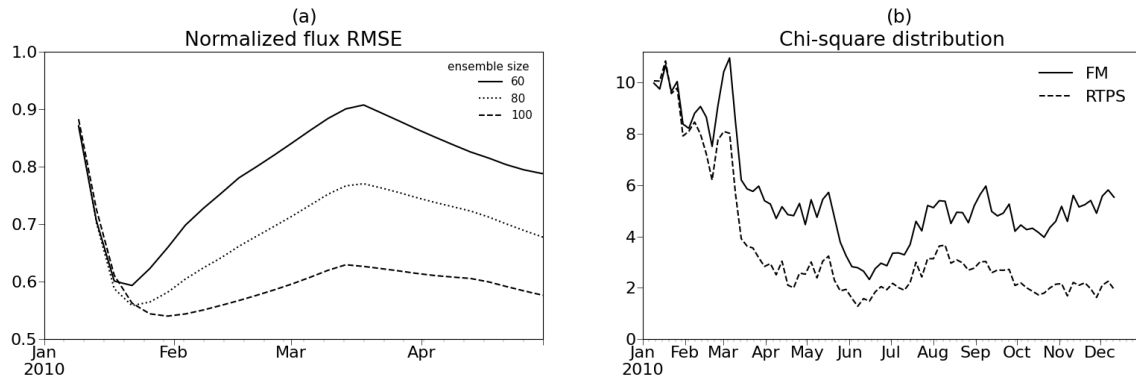


378

379 **Figure 6.** Monthly mean ACTM simulated XCH₄ (ppb) sampled with GOSAT observations to be
 380 assimilated (valid during the year 2010). The actual retrieval errors are added in the synthetic GOSAT
 381 observations. Data are shown for two representative months, depicting the southern and northern
 382 hemisphere differences in data coverage.

383 4.2.3 Ensemble size

384 Figure 7a shows the RMSE using different ensemble members. The optimal α_{RTPS} (Eq. 8) value
 385 ranging from 0 to 1, is applied based on flux estimation accuracy achieved by fine tuning α_{RTPS} value
 386 over different regions. The RMSE stabilizes gradually as the ensemble size increases from 60 to 80 to
 387 100 ensemble members. The ensemble size dependency of flux estimation suggests the further scope
 388 of the improvement in flux estimation by increasing the ensemble members. In this study we stick to
 389 100 ensemble members due to high computational cost while solving large covariance matrices. The
 390 larger error in flux estimation in case of column averaged synthetic GOSAT CH₄ observations
 391 assimilation compared to dense observations (Fig. 2) is likely due to [the weaker constraint on surface](#)
 392 [fluxes provided by satellite observations](#) and sparse observations.



393

394 **Figure 7:** (a) Flux estimation RMSE using different ensemble size with RTPS covariance inflation.
 395 (b) Chi-square distribution using FM and RTPS covariance inflation methods with the ensemble size
 396 of 100.

397 **4.2.4 Chi-square test**

398 We have carried out chi-square test for the evaluation of background error covariance matrix
 399 (Miyazaki et al., 2012). For the χ^2 test, the innovation statistics are diagnosed from the observation
 400 minus forecast ($y^o - Hx^b$), the estimated error covariance in the observation space ($HP^bH^T + R$),
 401 and the number of observations k , such as:

$$Y = \frac{1}{\sqrt{k}} (HP^bH^T + R)^{-1/2} (y^o - Hx^b) \quad (11)$$

402 Using this statistic, the χ^2 is defined as follow:

$$\chi^2 = \text{trace}YY^T \quad (12)$$

403 The performance of background error covariance matrix determined based on the high and lower
 404 value of chi-square. Chi-square value should converge to 1, a value higher (lower) than 1 indicates
 405 underestimation (overestimation) of the background error covariance matrices. Our results suggest
 406 that, background error covariance matrix is highly underestimated in both RTPS and FM covariance
 407 inflation methods (Fig. 7b). However, the chi-square values convergence towards 1 is better in the
 408 case of RTPS compared to FM covariance inflation method which indicates the improved
 409 representation of background errors and then more appropriate data assimilation corrections in the
 410 case of the RTPS inflation method. The chi-square distribution starts saturating after the month of
 411 March. Post March analysis shows the background error covariance matrix underestimation is much
 412 higher (>100%) in case of FM compared to RTPS covariance inflation method.

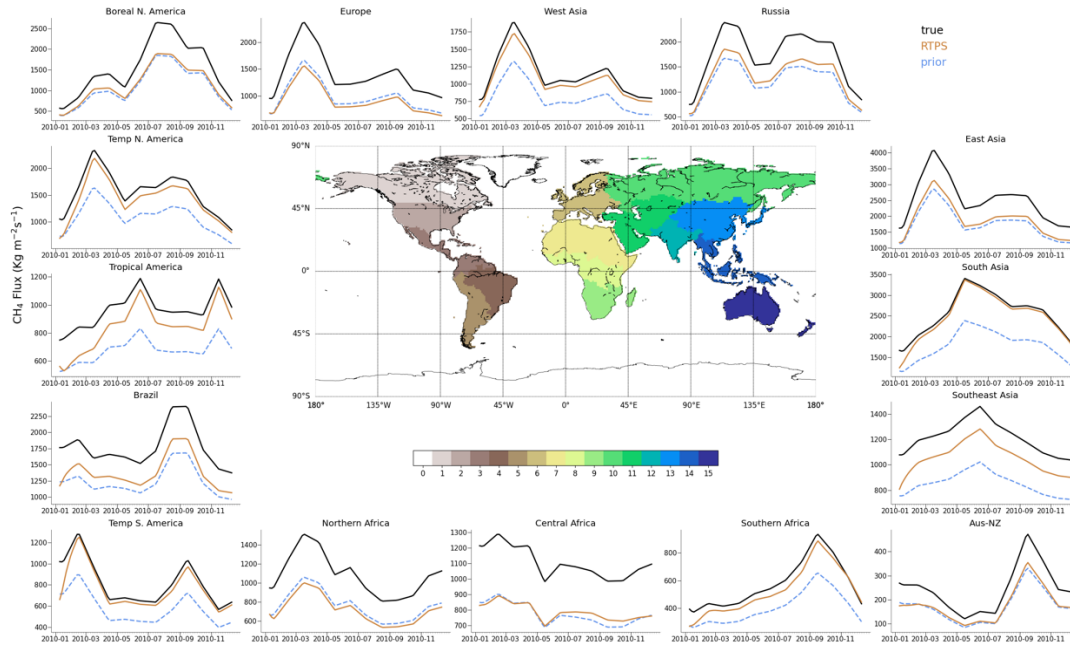
413 **4.2.5 CH₄ LETKF sensitivity to initial ensemble spread**

414 A test case for CH₄ LETKF data assimilation has been performed where the initial spread is provided
415 by considering the initial perturbation on each model grid with spatial error correlation between grid
416 points among ensemble members, with global mean correlation of 20%. In this case, we found that
417 the analysis fluxes are extremely sensitive to the initial ensemble spread if prior fluxes perturbed with
418 more than 5% prior uncertainty. Therefore, we used initial ensemble perturbation with only 2% prior
419 uncertainty. Reducing the initial ensemble spread reduces the CH₄ flux estimation sensitivity (>60%).
420 However, it also poses a challenge to mitigate the under-dispersive background error covariance
421 matrix. We performed LETKF data assimilations in this case with RTPS covariance inflation method
422 ($\alpha_{\text{RTPS}} = 0.9$ optimized value is used here uniformly) with 8-days long assimilation window and 100
423 ensemble members and calculated the normalized RMSE between analysis and true fluxes
424 (Supporting information Fig. S5). Noteworthy that, the estimated error between analysis and true
425 fluxes (Fig. S5) with this setting (grid-wise initial ensemble spread) is still larger (25%) than the case
426 when region-wise initial ensemble spread provided (Fig. 7a; 100 ensemble size). It suggests that,
427 initial ensemble spreads among ensemble members needs to be carefully provided that best represents
428 CH₄ variability among ensembles to estimate the CH₄ flux.

429 **4.2.6 Estimated CH₄ flux analysis**

430 Figure 8 shows the regional fluxes seasonal cycle comparison for the estimated fluxes over 15
431 terrestrial regions with those of the prior and true fluxes. We have also shown assimilation results in
432 case of FM inflation method in supporting information (Fig. S6), which shows the flux estimation
433 disagreement over more regions compared to RTPS inflation method; e.g., for Tropical and North
434 America, whole African continent, Australia-New Zealand.

435 We have shown the GOSAT observations in Figure 6 and supporting information Figure S7. We
436 found very marginal flux estimation improvement over Central Africa after May (Fig. 8), that could
437 be associated with the less GOSAT coverage over this region (Fig. 6). On the other hand, over
438 Northern Africa, no improvement in flux estimation is found. In case of dense OSSE too (Fig. 3), we
439 didn't find satisfactory flux estimation over Northern Africa which is most probably related to the
440 insufficient initial spread among ensemble members over this region (we have used same initial
441 ensemble spread in both OSSE cases). Over Europe, GOSAT observations are remarkably less,
442 specifically for first few months (January-April; supporting information Fig. S7). Therefore, the flux
443 update over Europe would be influenced by the observations from neighboring regions falling under
444 the chosen cutoff radius that are mainly in Northern Africa where the flux estimation itself not
445 satisfactory. It could also be noticed that the retrieval error added in this OSSE case are high over
446 Europe (September-October; supporting information Fig. S7,) and its adjacent Sea (Mediterranean
447 Sea; June-August) which could also affect the surface CH₄ flux estimation.

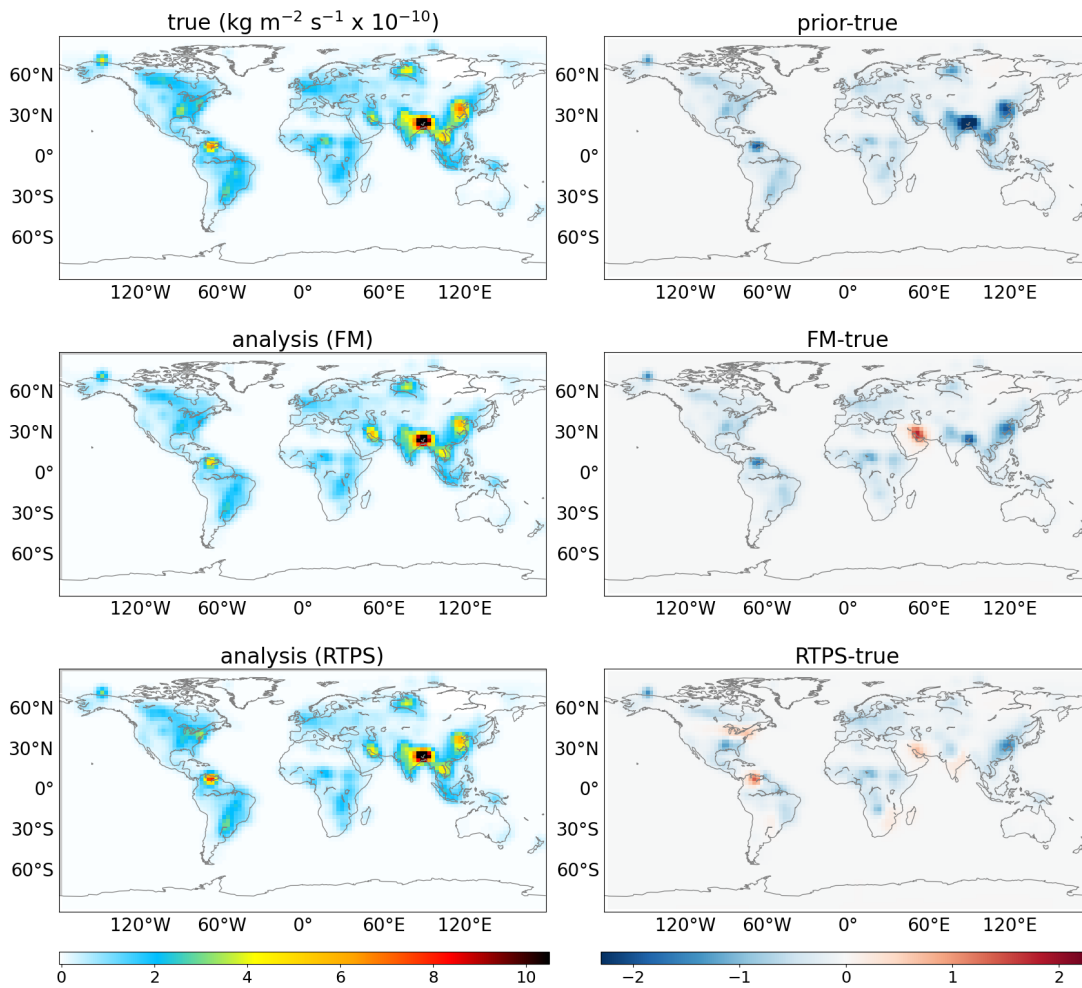


448

449 **Figure 8.** Same as Figure3 but after assimilating synthetic GOSAT observations.

450 Figure 9 and 10 show spatial patterns of the true and estimated fluxes by assimilating the column
 451 averaged CH₄ concentrations during June and November (Fig. 6). It may be noticed that RTPS
 452 covariance inflation method better able to estimate the true flux pattern compared to FM covariance
 453 inflation method. The spatial pattern shown using RTPS inflation method emphasizes the positive and
 454 negative bias in the estimated flux (Figs. 9 and 10), but generally agrees with the flux seasonal cycle
 455 plots shown in Figure 8.

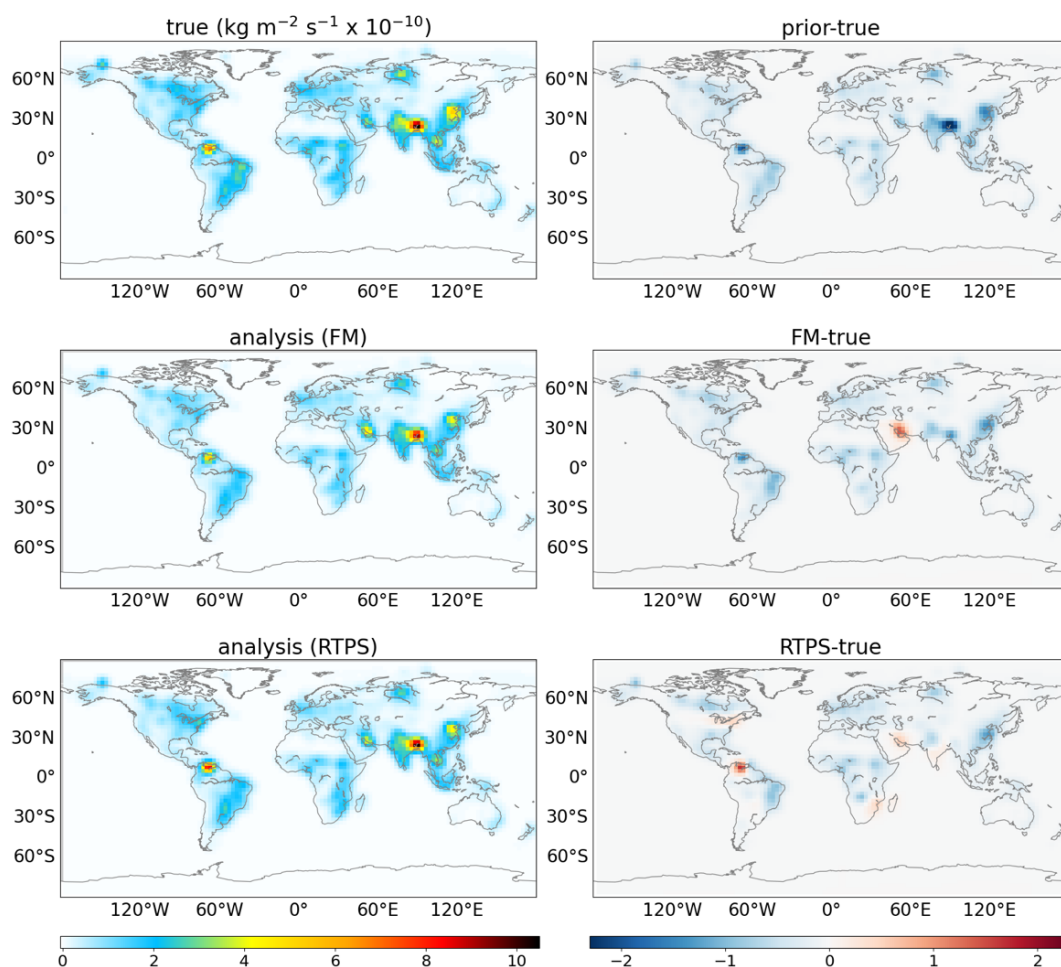
456 Our LETKF CH₄ data assimilation experiment by assimilating GOSAT synthetic observation with the
 457 implementation of the advanced RTPS covariance inflation method better estimate the time-evolving
 458 surface CH₄ fluxes compared to FM covariance inflation method. The difficulty to estimate the
 459 surface CH₄ flux over a few regions may be overcome by applying additional methodologies, such as
 460 the assimilation of surface observations simultaneously, and the use of information about the CH₄
 461 fluxes climatology. A correction factor derived based on empirical formulation that could use CH₄
 462 flux climatology information is needed to apply to maintain the CH₄ mass conservation. This could be
 463 implemented by the checking the simulated CH₄ burden gain between years in comparison with the
 464 observed CH₄ growth rates.



465

466 **Figure 9.** Monthly mean true (true; top left panel) and estimated (FM analysis; middle left panel,
 467 RTPS analysis; bottom left panel) CH₄ flux after assimilating column averaged synthetic CH₄
 468 concentrations (Fig. 6) during June using FM and RTPS inflation methods. The associated bias with
 469 prior and estimated fluxes is also shown (prior-true; top right panel; FM-true; middle right panel,
 470 RTPS-true; bottom right panel).

471



472

473 **Figure 10.** Same as Figure 9 but for November.

474 **5. Summary**

475 In this study, we have introduced 4D-LETKF data assimilation system that utilizes MIROC4-ACTM
 476 as a forward model for CH₄ flux estimation. This study has extensively tested both FM and RTPS
 477 inflation methods for the LETKF CH₄ flux estimation. We have conducted two experiments to
 478 demonstrate the ability of LETKF system to estimate the CH₄ surface flux globally. In Experiment1,
 479 we have assimilated the synthetic dense surface CH₄ observations. While in Experiment2, synthetic
 480 GOSAT CH₄ observations are assimilated. Based on the results of the sensitivity tests using FM and
 481 RTPS inflation methods in Experiment1, we have found that RTPS inflation produces significantly
 482 less normalized RMSE (10-15%) compared to FM inflation method. In Experiment2, we discussed,
 483 LETKF parameters such as, different inflation techniques, ensemble size, assimilation window, initial
 484 [ensemble spread](#) sensitivity, and chi-square test. The ensemble size (this study uses maximum 100
 485 ensemble members) sensitivity test suggests that more ensemble members could help to accurately
 486 represent the covariance matrix with more degrees of freedom. The assimilation window sensitivity

487 test exhibits that 8 days assimilation window reduces the normalized flux RMSE by about 10%
488 compared to 3 days assimilation window in case of GOSAT synthetic observations assimilation.

489 Our approach of assimilation with RTPS inflation could provide more degrees of freedom to fit the
490 ensemble of CH₄ concentrations to the observed ones, resulting the improved analyzed fluxes. The
491 RTPS inflation method is capable of obtaining reasonable flux estimates with normalized annual
492 mean bias of 0.04, and 0.61 in case of dense surface synthetic observations and GOSAT synthetic
493 observations, respectively. We demonstrated in our sensitivity OSSE experiment with synthetic
494 GOSAT observations that, over American and African continents and also over Australia - New
495 Zealand, the LETKF data assimilation with FM inflation method does not show much improvement in
496 the true flux estimation, but RTPS inflation method reasonably estimate the true flux over most of
497 these regions. One of the reasons for better flux estimates from RTPS inflation method is the
498 prevention of analysis spread drastically. In the CH₄ LETKF flux estimation, surface CH₄ flux is not a
499 prognostic state vector in the ACTM, which results in the decay of spread continuously in analysis
500 steps. RTPS inflation method could mitigate such under disperse spread problem. This study finds
501 that spatially homogeneous relaxation is not sufficient. It needs to be fine-tuned and applied
502 conditionally.

503 The sensitivity of LETKF CH₄ flux estimation to initial ensemble spread needed to be carefully dealt
504 with when applied to real data assimilation system. A future OSSE with additive covariance inflation
505 technique could be interesting while applied with RTPS inflation method for CH₄ LETKF data
506 assimilation since in additive covariance inflation initial estimated flux error cannot propagate. The
507 state vector augmentation technique used here updates the flux after each data assimilation cycle but it
508 doesn't conserve the total atmospheric CH₄ amount which is one of the limitations of this work. A
509 correction factor needs to be implemented to conserve the total atmospheric CH₄ amount after
510 completion of a few data assimilation cycles. We have not accounted for the transport error due to
511 meteorological fields in this work (Patra et al., 2011b), in case of real observations data assimilation a
512 week-long window may introduce transport errors in CH₄ analysis because of nonlinear growth of
513 ensemble perturbations.

514 *Code and data availability.* The LETKF source codes can be accessed from
515 <https://doi.org/10.5281/zenodo.7127658>. All the scripts for running the LETKF data assimilation
516 software, input and output results data files are available at <https://doi.org/10.5281/zenodo.7098323>.
517 CH₄ ACTM simulation module coupled with MIROC4-AGCM can be accessed from
518 <https://doi.org/10.5281/zenodo.7118365>. The source code of MIROC4-AGCM is archived at
519 <https://doi.org/10.5281/zenodo.7274240> with restriction because of the copyright policy of the
520 MIROC developer community, and no contribution of this work to the MIROC4 source code
521 development.

522 *Author contributions.* The LETKF data assimilation experiments were designed by JSHB. PKP, MT
523 and TS help to set the LETKF code on MIROC4-ACTM for CH₄ data assimilation. The manuscript is
524 prepared by JSHB and analysis interpretation input and feedback are provided by PKP, TS, KM. [All](#)
525 [coauthors](#), KM, TS, PKP, NS, [MT](#) and YK contributed to writing [and revision of](#) the paper.

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529 LETKF code on MIROC4-ACTM for CH₄.

530

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