Modeling the Inhibition Effect of Straw Checkerboard Barriers on Wind-blown Sand

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Abstract

Straw checkerboard barriers (SCBs) are usually laid to prevent or delay desertification caused by aeolian sand erosion in arid and semiarid regions. Understanding the impact of SCBs and their laying length on aeolian sand erosion is of great significance to reduce damage and laying costs. In this study, a three-dimensional wind-blown sand model in the presence of SCBs was established by introducing the splash process and equivalent sand barriers into a large-eddy simulation airflow. From this model, the inhibition effect of SCBs on wind-blown sand was studied qualitatively, and the sensitivity of aeolian sand erosion to the laying length was investigated. The results showed that the decrease in the wind speed in the SCB area oscillates along the flow direction. Moreover, the longer the laying lengths are, the lower the wind speed and the sand transport rate in the stable stage behind SCBs will be. We further found that
the concentration of sand particles near the side of SCBs is higher than that in its central region, which is qualitatively consistent with previous research. Our results also indicated that whether the wind speed will decrease below the impact threshold or the fluid threshold is the key factor affecting whether sand particles can penetrate the SCBs and form stable wind-blown sand behind the SCBs under the same conditions. Our research provides theoretical support for the minimum laying length of SCBs in anti-desertification projects.

1. Introduction

In arid and semi-arid areas, aeolian sand erosion is becoming increasingly serious. Preventing or delaying the process of desertification is a major challenge worldwide, especially in the transitional areas between deserts and oases. At present, shelterbelts (Wang et al., 2010), sand fences (Bitog et al., 2009; Hatanaka and Hotta, 1997; Li and Sherman (2015); Lima et al., 2017; Pye and Tsoar, 2008; Wilson, 2004), wind-break walls (Bouvet et al., 2006; Santiago et al., 2007), hole plate-type sand barriers (Chen et al., 2019) and straw checkerboard sand barriers (Bo et al., 2015; Huang et al., 2013; Wang and Zheng, 2002; Xu et al., 2018) are the main structures used to prevent desertification. Among these structures, straw checkerboard barriers (SCBs) are the most commonly used in anti-desertification projects because of their advantages of being easy to obtain and relatively low cost (Zheng, 2009). Laying SCBs could play an important role in the ecological restoration of sandy land ecosystems (Zhang et al., 2018) and vegetation restoration. Some research has shown that SCBs can effectively reduce the surface wind speed (Qu et al., 2007), increase the surface roughness
(Zhang et al., 2016), weaken the sand transport rate (Bo et al., 2015), and change the
distribution of aeolian sandy soil particles and soil organic carbon (Dai et al., 2019),
thus protecting the survival of vegetation and achieving sustainable development of
oases and ecological environments.

In recent decades, SCBs have been widely used in Northwest China, which is
seriously damaged by aeolian sand erosion. For example, SCBs have been laid on the
sides of roadbeds along railways such as the Baotou-Lanzhou Railway, Wuda-Jilantai
Railway (Wang, 1996), Gantang-Wuwei Railway (Yang, 1995), Lanzhou-Xinjiang
Railway (Binwen et al., 1998; Cheng et al., 2016), and Qinghai-Tibet Railway (Cheng
and Xue, 2014; Zhang et al., 2010), as well as in windy sand areas beside desert roads
such as the Taklamakan Desert Highway (Li et al., 2006; Qu et al., 2007), Tarim
Desert Highway (Xu et al., 1998) and Minqin Desert Highway. In addition, SCBs are
adopted by some countries that are also affected by aeolian sand erosion, such as
Ghana, Egypt, and Iran (Zheng, 2009). Although SCBs have been widely used, their
design size and laying methods are mainly determined by practical experience or
repeated tests. For example, for the sand fence, which has a similar effect to the SCB,
Li and Sherman (2015) combined experimental and field data to conclude that the
optimal design of a sand fence is closely related to its aerodynamics and
morphodynamics. The effect of sand fences with different porosities, spacings and
heights on the wind field is significant (Lima et al., 2017; Lima et al., 2020). However,
the complexity of the flow field around the SCBs and the movement of sand particles,
as well as the coupling of particles and flow field, make this problem more difficult.
Therefore, it is necessary to study the characteristics of turbulence inside and behind the SCBs as well as the influence mechanism of the laying length on wind speed and erosion.

Wang and Zheng (2002) proposed an ideal single-row uniformly distributed vortex model to simplify the flow field of wind-blown sand. Based on their model, the corresponding relationship between the side length and the height of a single SCB was analysed. Their theoretical results are similar to the size of the SCBs laid in the Tarim Desert Highway (1 m in side length and 15-20 cm in height). Qiu et al. (2004) noted that since the concentration of wind-blown sand below 10 cm near the surface is relatively high, the height of the SCBs should be designed to be 10-20 cm to effectively prevent aeolian sand erosion. The experimental results of Zhang et al. (2018) indicated that the SCB has the best protective effect when its side length is 1 m. These works are of great help to the design of a single SCB. Based on these empirical sizes of the SCBs, researchers have tried to analyse the effect of SCBs on the flow field and particles from the perspective of turbulence. Huang et al. (2013) used a two-dimensional large eddy simulation and discrete particle tracking methods to simulate wind-blown sand movement inside simplified two-dimensional SCBs. The effect of SCBs on surface wind speed was analysed. They found that sand particles could be aggregated at the inner walls of the SCBs due to the influence of the vortex or the backflow. Then, a V-shaped sand trough was formed, which is similar to the actual situation. Bo et al. (2015) equated the SCBs to the source term of the standard $k-\varepsilon$ turbulence model and analysed the influence of SCBs on the wind speed profile in
a two-dimensional flow field without sand particles. They divided the streamwise velocity profile in a flow field containing SCBs into approximately three different log-linear functions and obtained the relationship between them and friction wind speeds. Although these two-dimensional models can reflect the effect of the SCBs on the flow field to some extent, they are far from the real turbulence. Moreover, since the three-dimensional SCB is simplified into a two-dimensional plane with only the streamwise direction and vertical direction, the impact of this simplification is uncertain. For this reason, Xu et al. (2018) simulated wind-blown sand movement on the SCB surface under a three-dimensional flow field using OpenFOAM and mainly analysed the influence of the flow field inside the SCBs on the movement of sand particles. They concluded that the wind vortex is the main cause of the internal morphology of the straw checkerboard. They found that the vortex drives particles inside the SCBs towards the front and sidewalls, making the erosional form in SCB cells low in the middle and high near all sides. However, the SCBs are completely equivalent to the solid as the bottom boundary condition in their model. As a nonsolid material, SCBs can be penetrated by wind in practice. It only weakens the wind speed and is thus not equivalent to a solid. For example, Dupont et al. (2014) equated surface vegetation to a resistance force through the resistance coefficient and leaf area coefficient, that is, the wind will be resisted as it passes through these equivalent regions.

To reasonably introduce the SCBs and consider their coupling with turbulence, SCBs and the surface splash process, the development of a three-dimensional model
is needed. In this paper, a three-dimensional numerical coupled model of wind-blown sand in the presence of SCBs was carried out to study the inhibition effect of the laying length on aeolian sand erosion. The large eddy simulation approach was used to simulate clean air flow with the saltation process. Furthermore, we added a volume drag force into the Navier-Stokes equations by using the drag source method to realize the coupling between the SCBs and the wind-blown sand movement. Section 2 and Section 3 present the three-dimensional numerical coupled model and its validation, respectively. In Section 4, the effects of the SCB laying length on clean air flow and sand-laden flow under different friction wind speeds are studied. Finally, Section 5 summarizes the main conclusions.

2. Models

The Advanced Regional Prediction System (ARPS) has been widely used to simulate turbulent boundary-layer particle-laden flow, such as wind-blown sand (Dupont et al., 2013; Huang, 2020) and wind-blown snow (Huang and Wang, 2016; Li et al., 2018). The standard version of the program is described in the ARPS User’s Manual (Xue et al., 1995), and its validation cases are referred to Xue et al. (2000) and Xue et al. (2001). For this study, some suitable models were added to simulate turbulent boundary-layer flow in the presence of SCBs with saltating sand particles. A detailed description of these modifications is shown in the following subsections.

2.1 Turbulent boundary-layer flow

The basic flow fields in our numerical simulation are established based on ARPS (version 5.3.4). The filtered continuity and momentum equations, including the
viscous drag force terms of sand particles as well as SCBs, are shown as follows (Dupont et al., 2013; Vinkovic et al., 2006):

\[
\frac{\partial \tilde{u}_i}{\partial t} + \frac{\tilde{u}_i}{\partial x_j} \frac{\partial \tilde{u}_i}{\partial x_j} = -\frac{1}{\rho_f} \frac{\partial}{\partial x_i} (\tilde{p} - \nu) \frac{\partial \tilde{p}_j}{\partial x_j} - \frac{\partial \tau_{ij}}{\partial x_j} - \delta_{i3} g \left( \frac{\tilde{\theta}}{c_p} \tilde{p} + \frac{F_i}{\rho_f} \right),
\]

where \( i = 1, 2 \) and \( 3 \) correspond to the streamwise, spanwise and wall-normal directions (i.e., \( x_1 = x, x_2 = y, x_3 = z, u_1 = u, u_2 = v, u_3 = w \)), respectively; \( \tilde{u}_i, \tilde{p} \) and \( \tilde{\theta} \) represent the filtered wind speed, pressure and potential temperature, respectively; \( \nu \) is a damping coefficient of the attenuate acoustic waves; \( \rho_f \) is the air density; \( g \) is the acceleration of gravity; \( F_i = F_{pi} + F_{di} \) is the main feedback force, including the feedback force provided by sand particles \( (F_{pi}, \text{as shown in Section 2.2}) \) and the SCBs \( (F_{di}, \text{as shown in Section 2.5}) \); \( \delta_{ij} = 1 \text{ if } i = j, \text{ otherwise } \delta_{ij} = 0; \tau_{ij} = \tilde{u}_i \tilde{u}_j \tilde{u}_j \) are the SGS (sub-grid-scale) stresses (Smagorinsky, 1963); \( c_p \) and \( c_v \) are the specific heat of air at constant pressure and volume, respectively.

To solve above equations, the SGS stresses can be closed as follows:

\[
\tau_{ij} - \frac{1}{3} \tau_{ik} \delta_{ij} = - (C_{sgs})^2 \frac{1}{\sqrt{2}} \left[ \frac{\partial \tilde{u}_i}{\partial x_j} + \frac{\partial \tilde{u}_j}{\partial x_i} \right] \left[ \frac{\partial \tilde{u}_i}{\partial x_j} + \frac{\partial \tilde{u}_j}{\partial x_i} \right],
\]

where \( \Delta \) is the grid scale; \( C_{sgs} \) depends on the Germano subgrid-scale closure method (Germano et al., 1991).

For the governing equations mentioned above, periodic boundary conditions are applied for the spanwise direction. The upper and lower boundaries are set as a stress-free condition and a rigid ground condition, respectively. The outlet boundary is used as an open radiation condition in this paper. The inlet boundary is a given logarithmic profile:
Here $k=0.41$ is von Kármán constant; $z_0=d_{mean}/30$ is the aerodynamic surface roughness (Kok et al., 2012), and $d_{mean}$ is the mean diameter of the sand particles; $u_e$ is the friction speed of inflow. Additionally, the simulation is driven by a constant flow corresponding to the given logarithmic wind profile. To accelerate the development of boundary layer flow, the LWS method (Lund et al., 1998) is applied to the inlet condition and the recycling plane at $x_{ref}/L_x=12.5\%$ (Inoue and Pullin, 2011). $x_{ref}=5$ m is the position of the recycling plane, and $L_x=40$ m is the total length of the flow direction. The specific method reassigns the calculated mean velocity and fluctuation at the recycling plane to the inlet at each fluid time step. A similar application is described by Xu et al. (2018).

2.2 Movement of the sand particles

Saltating particles are moved by the drag force, gravity, electric field force, Magnus force, Saffman force and so on (Murphy and Hooshiari, 1982). In our model, the drag force and gravity are considered, ignoring other minor factors (Kok et al., 2012; Zou et al., 2007). We employ the Lagrangian point-particle method to describe particle motions, and the equations of particles with different sizes in three directions can be expressed as

$$m_p \frac{d^2 x}{dt^2} = F_{px} = \frac{C_D \pi D^2 \rho_f}{8} \left( \ddot{u} - \frac{dx}{dt} \right)^2 + F_{nx} + F_{ex}, \quad (4)$$

$$m_p \frac{d^2 y}{dt^2} = F_{py} = \frac{C_D \pi D^2 \rho_f}{8} \left( \ddot{v} - \frac{dy}{dt} \right)^2 + F_{ny} + F_{ey}, \quad (5)$$
\[
m_p \frac{d^2 z}{dt^2} = F_{pc} = -\frac{\pi g \rho_p D^3}{6} + \frac{C_D \pi D^2 \rho_f}{8} \left( \ddot{w} - \frac{dz}{dt} \right)^2 + F_{nc} + F_{tc}, \tag{6}
\]

where \(m_p\) is the mass of sand particles; \(C_D = (0.63 + 4.8/Re_p^{0.5})^2\) is the drag coefficient of sand particles (Cheng, 1997). The particle Reynolds number can be expressed as

\[
Re_p = \left( \frac{V_f \rho_p D / \mu}{0.63} \right)^{1/2} \left[ (\ddot{u} - dx / dt)^2 + (\ddot{v} - dy / dt)^2 + (\ddot{w} - dz / dt)^2 \right]^{1/2}. \tag{7}
\]

\(\rho_p\) and \(\rho_f\) are the density of sand particles and air, respectively; \(D\) is the diameter of sand particles; \(V_f = 1 - \sum_{k=1}^{k=n} V_p / \Delta V\) is the bulk fraction which is the total sand volumes within grid to the bulk of unit grid; \(\Delta V\) is the bulk of unit grid; \(\mu\) is the kinetic viscosity coefficient of air; \(F_{nx}, F_{sx}, F_{ny}, F_{sy}, F_{nz}\) and \(F_{sz}\) are the normal and tangential force of contact in three directions.

### 2.3 Particle collision

Modeling the collision process in the air among the ejection particles has been the focus of previous studies (Carneiro et al., 2013; Huang et al., 2007). In this paper, the “spring-damping model” is used to calculate the contact force when particles collide in the air. The contact force can be described as follows (Huang et al., 2017):

The normal force of contact is

\[
\vec{F}_{n_{ij}} = \begin{cases} 
-k_n \zeta_{n_{ij}} - d_n \vec{v}_{n_{ij}}, & \zeta = \left| \vec{R}_i + \vec{R}_j - \vec{r}_{ij} \right| < 0 \\
0, & \zeta < 0
\end{cases}, \tag{8}
\]

where \(k_n = 2 \times 10^6\) is the normal stiffness coefficient; \(\zeta\) is the amount of overlap between particles during contact; \(R_i\) and \(R_j\) are the radius of particle \(i\) and \(j\); \(\vec{r}_{ij}\) is
distance vector between particles; $\mathbf{v}_{n,ij}$ is the normal relative velocity vector. The normal damping coefficient can be expressed as
\[ d_n = \frac{4k_n m_i m_j (\ln \varepsilon)^2}{m_i + m_j \pi^2 + (\ln \varepsilon)^2}, \]  
(9)

where $m_i$ and $m_j$ are the mass of particle $i$ and $j$, and $\varepsilon=0.7$ is restitution coefficient.

The tangential force of contact is
\[
F_{t,ij} = \begin{cases}
-k_t \zeta_{t,ij} \mathbf{r}_{ij} - d_t \mathbf{v}_{t,ij} & |F_{t,ij}| \leq \frac{R_i}{R_j} |F_{n,ij}| \\
-\mu |F_{n,ij}| \mathbf{r}_{ij} & |F_{t,ij}| > \frac{R_i}{R_j} |F_{n,ij}| 
\end{cases},
\]  
(10)

where $k_t = 2 \times 10^6$ is the tangential stiffness coefficient, $\zeta_{t,ij}$ is the tangential displacement, and $\mathbf{v}_{t,ij}$ is the tangential relative velocity vector. The tangential damping coefficient can be expressed as
\[d_t = 2 \sqrt{\frac{m_i m_j}{m_i + m_j} k_t}.\]  
(11)

2.4 Splash process

Splash processes not only serve as an indispensable part of the near-surface particle motions but also relate to the accuracy of emissions during particle upwards transport. There are a large number of collisions between particles and the ground. Meanwhile, other particles will be blown upwards when particles hit the ground, which is referred to as the splash process. If energy-based collision analysis is performed on a single particle, considerable time will be consumed. Therefore, researchers have parameterized some key variables in accordance with the
characteristics of splashing, thereby simplifying the problem. We assume that there are enough sand and dust particles on the ground to splash when the particles impact the surface. If the particle collides with the bed, we assume the rebound probability as

$$p_{reb} = 0.95(1 - e^{-\lambda v_{imp}}), \quad (12)$$

where $v_{imp}$ is the impact speed, and $\lambda$ is an empirical parameter in the order of 2 s/m according to the previous study (Anderson et al., 1991). The rebound sand speed is 0.55 times of the impact sand speed, and the rebound angle $\theta_{reb}$ is 40° (Zhou et al., 2006). Of course, at a certain speed, some new sand particles will be splashed. The ejection number is

$$\overline{N_{ej}} = n_0 \left(1 - \left(A - B \sin \theta_{imp}\right)^2 \right) \left(\frac{v_{imp}}{\zeta \sqrt{gd_{mean}}} - 1\right) e^{\mu_{imp}/C - D}, \quad (13)$$

where $n_0=0.4$, $A=0.68$, $B=0.39$, $\zeta=5$, $C=0.92$, and $D=1.39$ (Huang et al., 2017). $\theta_{imp}$ is the impact angle, $\mu_{imp}$ is the ratio of impact grain size to the mean size of the bed, and $d_{mean}$ is the mean diameter of the sand particles. The ejection angle $\theta_{ej}$ distributes randomly between 50°~60° (Rice et al., 1995). The probability density distribution of the initial lifting speed follows

$$p(v_{ej}) = \exp(-v_{ej}/\overline{v_{ej}})/\overline{v_{ej}}, \quad (14)$$

where $v_{ej}$ is the ejection speed and the overbar represents a mean value (Anderson et al., 1991; Werner, 1990). The mean ejection speed can be expressed as (Kok and Renno, 2009)
Moreover, the sand particles satisfy the periodic boundary condition in the streamwise and spanwise directions. Following the idea of Dupont et al. (2013), aerodynamic entrainment is not considered in our model. A total of 10000 initial particles are randomly released in the flow field (Huang, 2020), and the release height should be lower than 0.3 m (Shao and Raupach, 1992). The results of Dupont et al. (2013) showed that the number of released particles does not affect the final results but only the speed of wind-blown sand development.

2.5 Parameters and the equivalent method of SCBs

According to the experience of laying SCBs in practical engineering (Chang et al., 2000) and the theoretical results of Wang and Zheng (2002), in this paper, the height of the SCB ($S_h$) is set to 10 cm, the side length of a single SCB ($S_l$) is set to 100 cm, and the side thickness of the SCB ($S_n$) is set to 10 cm. The diagram of a single SCB is shown in Fig. 1b. Moreover, to study the inhibition effect of the laying length of SCBs (represented by N) on aeolian sand erosion, we set N=5~10 m, 5~20 m, and 5~30 m in the simulation cases. The diagram of the laying SCBs is shown in Fig. 1a, and the main parameters of the SCBs are listed in Table 1.

**Figure 1.** (a) The diagram of the laying SCBs. (b) The diagram of a single SCB.
The SCBs are equivalent to a volume resistance force through the resistance coefficient and leaf area coefficient; that is, the flow in these regions will be subject to an additional resistance force, which can be expressed as

\[ F_{di} = -C_d a_d |U| u_i, \]

(16)

where \( C_d \) is the drag coefficient, \( a_d \) is the leaf area coefficient, and \( U \) is the inflow wind speed. In the simulation, the value of \( C_d \) is 0.2 according to the parameters of Dupont et al. (2013). Nepf (2012) concluded that when the diameter of vegetation is 4-9 cm, the value of the leaf area coefficient \( a \) can reach 20 m\(^{-1}\). Therefore, according to the side thickness of the SCB presented in this paper, the leaf area coefficient is set as 40 m\(^{-1}\).

Table 1 SCB Parameters

<table>
<thead>
<tr>
<th>Name</th>
<th>Symbol</th>
<th>Value</th>
<th>Unit</th>
</tr>
</thead>
<tbody>
<tr>
<td>SCB height</td>
<td>( S_h )</td>
<td>10</td>
<td>cm</td>
</tr>
<tr>
<td>SCB side length</td>
<td>( S_l )</td>
<td>100</td>
<td>cm</td>
</tr>
<tr>
<td>SCB side thickness</td>
<td>( S_n )</td>
<td>10</td>
<td>cm</td>
</tr>
<tr>
<td>laying length of SCBs</td>
<td>( N )</td>
<td>5<del>10, 5</del>20, 5~30</td>
<td>m</td>
</tr>
<tr>
<td>drag coefficient</td>
<td>( C_d )</td>
<td>0.2</td>
<td></td>
</tr>
<tr>
<td>leaf area coefficient</td>
<td>( a )</td>
<td>40</td>
<td>m(^{-1})</td>
</tr>
</tbody>
</table>

2.6 Calculation parameters

Figure 2. Schematic diagram of three-dimensional wind-blown sand in presence of SCBs.
Wind tunnel experiments conducted by Shao and Raupach (1992) indicated that a complete “overshoot” was more than 10 m in streamwise (Huang et al., 2014; Ma and Zheng, 2011). In Fig. 2, the computational domains are \( L_x = 40 \) m, \( L_y = 5 \) m, and \( L_z = 2 \) m in the streamwise, spanwise and wall-normal directions, respectively. Field experiments conducted by Baas and Sherman (2005) showed that the mean lateral size of sand streamers is approximately 0.2 m. To capture this structure, the mesh spacing is \( N_x = 0.1 \) m and \( N_y = 0.05 \) m in the streamwise and spanwise directions, respectively. In addition, in the near-wall region, logarithmic stretching has been adopted to ensure precision. The mean and minimum mesh spacing in the vertical direction is \( N_z = 0.025 \) m and \( N_{z_{\text{min}}} = 0.005 \) m, respectively. Therefore, the grids of the streamwise, spanwise and vertical directions are \( 400 \times 100 \times 80 \), respectively. The sand particle diameter satisfies the normal distribution: the mean diameter equals 200 μm, and the variance is \( \ln(1.2) \). We first simulate the clean air field flow in the presence of SCBs for 30 seconds to obtain the full development of the flow field. Then, we add sand particles to the flow field to obtain a sand-laden flow. After the wind-blown sand flow becomes saturated, the simulations continue for another 20 seconds to perform the statistics. The fluid time step is \( \Delta t_{\text{f}} = 0.0002 \) s, and the particle time step is \( \Delta t_{\text{p}} = 0.00005 \) s. The sand grain density is 2650 kg/m\(^3\), and the air density is 1.225 kg/m\(^3\). The main calculation parameters are listed in Table 2.
### Table 2 Main Simulation Parameters

<table>
<thead>
<tr>
<th>Name</th>
<th>Symbol</th>
<th>Value</th>
<th>Unit</th>
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</thead>
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<tr>
<td>streamwise computational domain</td>
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<td>m</td>
</tr>
<tr>
<td>spanwise computational domain</td>
<td>$L_y$</td>
<td>5</td>
<td>m</td>
</tr>
<tr>
<td>wall-normal computational domain</td>
<td>$L_z$</td>
<td>2</td>
<td>m</td>
</tr>
<tr>
<td>fluid time step</td>
<td>$\Delta t_s$</td>
<td>0.0002</td>
<td>s</td>
</tr>
<tr>
<td>friction wind speed</td>
<td>$u_*$</td>
<td>0.3, 0.44, 0.6</td>
<td>m/s</td>
</tr>
<tr>
<td>particle time step</td>
<td>$\Delta t_p$</td>
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<td>s</td>
</tr>
<tr>
<td>sand density</td>
<td>$\rho_a$</td>
<td>2650</td>
<td>kg/m$^3$</td>
</tr>
<tr>
<td>air density</td>
<td>$\rho_f$</td>
<td>1.225</td>
<td>kg/m$^3$</td>
</tr>
<tr>
<td>gravity</td>
<td>$g$</td>
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<td>m/s$^2$</td>
</tr>
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<td>m</td>
</tr>
<tr>
<td>spanwise mesh spacing</td>
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<td>m</td>
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<tr>
<td>wall-normal mean mesh spacing</td>
<td>$N_z$</td>
<td>0.025</td>
<td>m</td>
</tr>
</tbody>
</table>

### 3. Model validations

#### 3.1 Particle field validation

![Figure 3](image)

(a) The spatial variation of the streamwise sand transport rate in the sand-laden flow. (b) The streamwise sand transport rate density with the height at the three flow direction positions.

In section 3.1, we will verify the validity of the model from the following two aspects. The sand transport rate is an important physical quantity in wind-blown sand, which is the embodiment of the sediment carrying capacity of the flow field (Zheng, 2009). Therefore, without considering the SCBs, we first compare the spatial variation in the sand transport rate in the sand-laden flow with the experimental results of Shao and Raupach (1992). The sand transport rate is calculated according to the formula...
\[ q(x) = \sum_{z=0}^{L_z} \sum_{y=0}^{L_y} m(x, y, z) / \Delta x / \Delta t_z, \]  

(17)

where \( m(x, y, z) \) represents the sand mass, and \( \Delta x \) is the grid size in the flow direction.

Whether the wind-blown sand flow is saturated depends on the change in sediment transport at a certain streamwise position. The condition for judging saturation is given by Ma and Zheng (2010). The wind tunnel experimental results of Shao and Raupach (1992) showed that the streamwise sand transport rate first increased and then decreased until it was stable, which is called the "overshoot" phenomenon (Anderson and Haff, 1991; McEwan and Willetts, 1991). Fig. 3a shows the comparison between the simulation results of the sand transport rate along the flow direction and the experimental results of Shao and Raupach (1992) under the same friction wind speed. As shown in Fig. 3a, our simulation results also show this phenomenon. However, unlike the other numerical simulation results (Huang et al., 2014; Ma and Zheng, 2011), our sediment transport rate results have an obvious fluctuation characteristic and are not smooth curves, which may be caused by the turbulence intermittency unique to the three-dimensional wind-blown sand model.

Moreover, we give the distribution results of the streamwise sand transport rate density with the height at the three flow direction positions, which are compared with the experimental results. From Fig. 3b, we can see that the distribution of the streamwise sand transport rate density with height follows the trend of exponential decline, and the sand transport rate density at \( x = 6 \) m is significantly higher than that at \( x = 1 \) m and \( x = 14.5 \) m, which is consistent with the experimental results of Shao.
and Raupach (1992). This is because the streamwise position of \( x = 6 \) m is in the peak region of the "overshoot" phenomenon, while the streamwise positions of \( x = 1 \) m and \( x = 14.5 \) m are in the rising region and stable region, respectively. Due to the massive accumulation of sand particles near the surface (0-20 mm), the concentrations cannot be easily measured. In Fig. 3b, our simulation results also show that the distribution of the streamwise sand transport rate density with heights below 10 mm still satisfies the trend of exponential decline. However, at a height of 2~3 mm, there is a slight change in this trend; that is, the rate of increase in the sand transport rate density slows down, which is not revealed in the experimental results. Due to the limitations of the large eddy simulation, the simulation results near the wall may be distorted and requires further experimental verification.

Figure 4. (a) The top view of the sand streamer concentrations, where \( C \) represents the particle concentrations, \( C_{\text{max}} \) represents the maximum particle concentrations. (b) The top view of the whole particle positions and the streamwise velocity diagram of flow field with the height of 0.005 m, and the \( y \) coordinates are correspondingly shifted down by 2, where the black dots represent the sand particles, \( U \) represents the streamwise wind speed of the sand-laden flow (\( u_t = 0.3 \) m/s).
Sand streamers, as a natural phenomenon in wind-blown sand, have been widely studied. Therefore, without considering the SCBs, we analyse the morphology of the sand streamer and its relationship with the flow field. In the meantime, the airborne particle concentration within a certain area can be calculated as

\[
C = \sum_{z=0}^{z=L_z} \sum_{y=0}^{y=L_y} \sum_{x=0}^{x=L_x} m(x, y, z) / L_x / L_y / L_z.
\]  

(18)

Fig. 4a shows the top view of the particle-aggregation morphology in the stable stage of sand-laden flow. It can be seen from Fig. 4a that the concentration of sand particles is intermittent in both streamwise and spanwise directions. Moreover, we can see clearly that the morphological characteristics of the sand streamer are consistent with the observations of Baas and Sherman (2005), that is, it is up to a few metres in the streamwise direction and approximately 0.2 metres in the spanwise direction. Our model can sufficiently reproduce the “sand streamer” phenomenon in wind-blown sand. Here, we need to point out that the intermittence of turbulence complicates particle movement, especially when multiple streamers are connected end to end and the concentration is sufficiently close, and then super sand streamers up to tens of metres long will exist. Whether in sand-laden flow or other two-phase flows, researchers are generally concerned about the aggregation of particles. We plot the position of particles and the streamwise velocity of the flow field in Fig. 4b and find that most particles are assembled in the low-speed streaks, which is consistent with the conclusion of the other particle-laden flow studies (Lee and Lee, 2015; Richter, 2015).
3.2 Velocity field validation

**Figure 5.** The side view of X-Z plane streamwise velocity before (a) and after (b) containing the SCBs ($u_t=0.6$ m/s, N=5~20 m, $y=0$ m). The y coordinates are correspondingly shifted down by 2 in the case (b).

**Figure 6.** (a) The wind speed profiles of different streamwise positions in the clean air flow containing the SCBs ($u_t=0.6$ m/s, N=5~20 m); (b) The dimensionless wind speed varying with dimensionless height, comparison between our simulated results and the existing experiment.

The verification of the flow field part of the program is covered in detail in our previous works (Huang, 2020). In section 3.2, we focus on the flow field verification after considering the SCBs. We verify the difference in the velocity profile as well as the surface roughness in the clean air flow with and without the SCBs. In previous work, the wind speed and surface roughness near the SCBs were well
studied (Dong et al., 2000; Qu et al., 2007; Wang et al., 1999). These works all pointed out that laying the SCBs can effectively increase the surface roughness and reduce the wind speed near the surface to play a role in inhibiting the wind-blown sand and fixing the sand particles. Fig. 5a and 5b are the tangent plane (X-Z plane) of the streamwise wind velocity without and with the SCBs, respectively. It can be seen intuitively that the existence of the SCBs significantly reduces the surface wind speed and increases the boundary layer thickness of the flow field. To reveal the difference quantitatively, we plot the wind speed profiles of different streamwise positions in the clean air flow containing the SCBs in Fig. 6a. The selected positions are \( x = 1, 2, \) and \( 3 \) m in front of the SCBs, \( x = 7.5, 12.5, \) and \( 17.5 \) m in the area containing the SCBs, and \( x = 30, 35, \) and \( 39 \) m behind the SCBs. We can see that the wind speed profiles at the three positions in front of the SCBs are basically the same. In the area containing the SCBs, the existence of the SCBs reduces the surface wind speed and increases the thickness of the boundary layer (equivalent to increasing the surface roughness) as well as the incoming wind speed outside the boundary layer. Moreover, the longer the SCBs are, the thicker the boundary layer becomes, and the incoming wind speed outside the boundary layer will also increase. The flow field behind the SCBs may be complicated by the influence of the attached vortex generated by the SCBs, but the overall trend is the same, and the boundary layer thickness remains consistent. These results are qualitatively consistent with the conclusions of previous work (Dong et al., 2000; Qu et al., 2007; Wang et al., 1999), which indicates that our model has effectively introduced the SCB module.
In addition, we compared the wind speed profiles with the experimental results of Tao et al. (2020). In Figure 6b, the streamwise wind speed in the horizontal coordinate is dimensionless with the reference wind speed $U_{\text{ref}}$ and the height in the vertical coordinate is dimensionless with the reference height $z_{\text{ref}}$. In the wind tunnel experiment conducted by Tao et al. (2020), the maximum boundary layer thickness is given as 0.5 m, so the reference height is taken as $z_{\text{ref}}=0.5$ m. Then, the wind speed at $z=0.5$ m is determined as the reference wind speed $U_{\text{ref}}=12.58$ m/s based on their inlet wind profiles. In our simulation case, $z_{\text{ref}}=0.4$ m is the initial inlet boundary layer thickness, and $U_{\text{ref}}=16.3$ m/s is the reference wind speed. We select the experimental results of wind speed profiles at the SCB belt positions $x_0=2.2$ m and 2.8 m along the flow direction to compare with our numerical results at $x_0=2.5$ m (streamwise position $x=7.5$ m). The dimensionless results show that our results are consistent with the experimental results in quantitative and qualitative, which indicates that our model can well reveal the inhibition effect of SCBs on the flow field. In the following section, we will reveal more about the influence of the laying length on the wind field and its inhibition effect on wind-blown sand.
4. Results and discussion

4.1 Influence of the SCBs on the clean air flow

Figure 7. The top view of X-Y plane streamwise velocity without (a) and with (b) the SCBs ($z=0.005 \text{ m}, \ u_c=0.6 \text{ m/s}, \ N=5\sim20 \text{ m}$).

Figure 8. The streamwise wind speed in the clean air flow containing the SCBs at the height of 0.1 m (a) and the height of 0.2 m (b), $u_c=0.6 \text{ m/s}, \ N=5\sim10 \text{ m}, \ 5\sim20 \text{ m}, \ 5\sim30 \text{ m}$.

Fig. 7a and 7b show that the presence of the SCBs destroys the original streaks of the clean air flow and decreases the wind speed. In most cases, the wind speed in the central area of a single SCB is significantly higher than that in the surrounding area, showing a block of velocity distribution characteristics. Although the wind speed behind the SCBs will recover rapidly, there is a significant difference between the newly formed streaks and the original streaks of the flow field; that is, the streamwise
scale of the streaks behind the SCBs is significantly shorter than before. The variation in streamwise wind speed at the different laying length cases (N=5~10 m, 5~20 m, 5~30 m) under the same friction wind speed (\(u_\tau=0.6\) m/s) is plotted in Fig. 8, where Fig. 8a corresponds to the wind speed at a height of 0.1 m, and Fig. 8b corresponds to the wind speed at a height of 0.2 m. Fig. 8 shows an oscillating decrease in wind speed in the SCBs. In addition, behind the SCBs, the wind speed gradually increases and then stabilizes. The trend of wind speed reduction in the SCBs is consistent with the existing experimental results (Xu et al., 1982). The difference is that the reduction process of the wind speed around the SCBs exhibited an oscillatory attenuation instead of a continuous decrease, which was not revealed in the previous simulation results (Bo et al., 2015). Moreover, when the incoming wind speed is stable, the longer the laying lengths are, the lower the wind speed in the stable stage behind the SCBs will be. This is very useful information. On this basis, we can obtain the relationship between the laying length of the SCBs and the wind speed in the stable stage according to an actual situation. For example, the wind speed in the stable stage can be reduced to the impact threshold or the aerodynamic threshold on both sides of the desert highway to determine the minimum laying length of the SCBs and save laying costs. This is a potential application of our model and needs further experimental verification.
4.2 Effect of sand particles on the flow field and its aggregation location

**Figure 9.** The top view of the particle positions of the wind-blown sand in presence of SCBs, where $U$ represents the speed of the particles ($u_t=0.6$ m/s, $N=5$–20 m).

**Figure 10.** The top view of the sand concentrations in the regions of the SCBs, where $C$ represents the particle concentrations, $C_{\text{max}}$ represents the maximum particle concentrations ($u_t=0.6$ m/s, $N=5$–20 m). The black lines represent the schematic diagram of the side of SCBs.

Sand particles were added to the clean air flow field in the presence of SCBs to fully develop and reach stability. The top view of the particle positions of the
wind-blown sand after reaching a stable state is shown in Fig. 9. From Fig. 9, we can see that when the wind-blown sand passes through the SCBs, the particle number obviously decreases gradually, and the inhibition effect of the SCBs on the wind-blown sand can be visualized. Moreover, the motion of sand particles behind the SCBs returns to complete wind-blown sand movement. We then plot the sand concentrations of the region in the presence of SCBs in Fig. 10. Combining the laying position of the SCBs as well as the corresponding sand concentrations, we can clearly see that the concentration of sand particles near the side of the SCBs is higher than that in its central region, which is consistent with the conclusion of Xu et al. (2018). On the one hand, the wind speed near the side of SCBs is low, and the drag force of the sand particles in these areas will be significantly reduced, so that the sand particles will accumulate or deposit in these regions. On the other hand, the wind speed in the central area of every single SCB is significantly higher than that in the surrounding area, so sand particles do not easily accumulate or fall in these regions. This explains why the side of the SCBs tends to be buried in sandy land and loses its effect after long working hours.
The streamwise wind speed in the sand-laden flow containing the SCBs at the height of 0.1 m (a) and the height of 0.2 m (b), $u_r=0.6 \text{ m/s}$, $N=5\sim10 \text{ m}, 5\sim20 \text{ m}, 5\sim30 \text{ m}$. The comparison of the streamwise wind speed between the clean air flow and the sand-laden flow at the height of 0.1 m (c) and the height of 0.2 m (d), $u_r=0.6 \text{ m/s}$, $N=5\sim20 \text{ m}$. Furthermore, we analyse the effect of sand particles on the wind speed in the sand-laden flow. The streamwise wind speed of the sand-laden flow at the different laying length cases ($N=5\sim10 \text{ m}, 5\sim20 \text{ m}, 5\sim30 \text{ m}$) under the same friction wind speed is plotted in Fig. 11a and 11b. Meanwhile, for the convenience of comparison, the streamwise wind speed under the same laying length ($N=5\sim20 \text{ m}$) in the sand-laden flow and the clean air flow are plotted in Fig. 11c and 11d. Fig. 11a and 11c correspond to the wind speed at a height of 0.1 m, while Fig. 11b and 11d correspond to the wind speed at a height of 0.2 m. From Fig. 11a-d, we can still see an oscillating decrease in the wind speed in the SCBs of the sand-laden. The streamwise wind speed behind the SCBs in the sand-laden flow is significantly lower than that in the clean air flow. Obviously, the presence of sand particles indeed reduces the wind speed. However, the change in wind speed in the SCBs between the sand-laden flow and the clean air flow is not obvious because there are fewer sand particles in the SCBs than behind the SCBs, which has less effect on the overall wind speed.
4.3 Effect of the laying length on the sand transport rate

![Graph showing sand transport rate vs streamwise distance for different laying lengths.](image)

**Figure 12.** The streamwise sand transport rate in the different laying length cases ($u_\tau=0.6$ m/s, $N=5-10$ m, 5~20 m, 5~30 m). Dark lines are the result of smoothing.

The effect of the different laying length cases ($N=5\sim10$ m, 5~20 m, 5~30 m) on the sand transport rate under the same friction wind speed is plotted in Fig. 12. It can be seen from Fig. 12 that the sand transport rate in the SCBs is very low, and as the laying length increases, the sand transport rate in the SCBs decreases. In the case of $N=5\sim30$ m, the sand transport rate in some regions has been reduced to zero. Therefore, this result once again shows that the laying length of the SCBs can be optimized, and we can reduce the laying cost while maintaining the effect of the SCBs. Especially on both sides of the desert highway, our model can give the minimum laying length according to the actual parameters. At the same time, we notice that the sand transport rate will increase rapidly and then reach a stable state behind the SCBs. It is obvious that when $N=5\sim30$ m, the value of the sand transport rate at the stable stage behind the SCBs is significantly lower than the other results of $N=5\sim10$ m and...
N=5~20 m. We also notice that the longer the laying lengths are, the lower the sand transport rate in the stable stage behind the SCBs will be. This result corresponds to the result shown in Fig. 8. Our results indicate that when sandy land is wide, the discontinuous laying method can be considered. That is, the minimum laying length must be determined first, and then the distance between each minimum laying length can be set as needed. In this way, the sand transport rate can be reduced in sections. This is another potential application of our model.

4.4 Particle positions under different friction wind speeds

Figure 13. The top view of the particle positions of the wind-blown sand in presence of SCBs at the time t=2.0 s (a) and t=5.0 s (b), where $U$ represents the speed of the particles ($U_r=0.3$ m/s, N=5~20 m). The y coordinates are correspondingly shifted up by 7.5 per case.
The above analysis is based on the calculation case when the friction wind speed is 0.6 m/s, and the sand particles can easily penetrate the SCBs when the wind speed is large. When the friction wind speed is small, the inhibition effect of the SCBs on wind-blown sand will become more obvious, and the movement behaviour of sand particles will change. We focused on the effect of SCBs on the wind-blown sand within 2 to 5 seconds after the sand-laden flow is saturated. We plot the top view of the particle positions at different moments ($t=2$ s, 5 s) when the friction wind speed is 0.3 m/s and 0.6 m/s in Fig. 13 and Fig. 14, respectively. The initial value of time $t$ in Fig. 13 and Fig. 14 is when sand particles are added. The results show that when the wind speed is small, the sand particles cannot penetrate the SCBs. There is no obvious sand movement in the SCBs, and stable wind-blown sand cannot be formed behind the SCBs. With the passage of time, the wind-blown sand behind the SCBs gradually disappears. It is worth noting that aerodynamic entrainment is not considered in our
model. This is a considerable limitation of our model in the simulation of wind erosion in the presence of SCBs. Therefore, a more reasonable situation is that when the wind speed behind the SCBs returns to the fluid threshold, this part of the wind-blown sand should still develop. When the wind speed is relatively small, on the one hand, the sand particles cannot completely penetrate the regions of the SCBs and cannot continuously provide the impact particles to form the wind-blown sand behind the SCBs. On the other hand, the SCBs affect the surface wind speed behind it, thus also affecting the continuous formation of wind-blown sand. When the wind speed is relatively high, the sand particles can penetrate the SCBs. With increasing laying length, although the inhibition effect on wind-blown sand is more obvious, stable wind-blown sand will still be formed behind the SCBs. We think that when the laying length of the SCBs is fixed, whether the wind speed will decrease below the impact threshold or the fluid threshold is the key to determining whether the sand particles can penetrate the SCBs and form stable wind-blown sand behind the SCBs. To present this phenomenon more clearly, we have animated this process, as shown in the supplementary materials (Video 1 and Video 2). In actual anti-desertification projects, the minimum laying length of the SCBs can be determined by our model according to the local maximum friction wind speed.

5. Conclusion and outlook

In this paper, a three-dimensional wind-blown sand coupling model in the presence of SCBs was established. The model was verified from the following aspects:

(1) spatial distribution of the sand transport rate; (2) morphological characteristics of
the sand streamer resulting from the instantaneous fields; and (3) changes in the
thickness of the boundary layer before and after the SCBs. From this model, the
inhibition effect of SCBs on wind-blown sand was studied qualitatively, and the
sensitivity of aeolian sand erosion to the laying length was investigated. The results
showed that the wind speed in the SCBs of the clean air flow or the sand-laden flow
both decreases in an oscillating manner, which has not been revealed by previous
studies. Moreover, the longer the laying lengths of the SCBs are, the lower the wind
speed and the sand transport rate in the stable stage behind the SCBs will be, which
may provide theoretical support for the minimum laying length of SCBs in
anti-desertification projects. More importantly, we found that the concentration of
sand particles near the side of SCBs is higher than that in its central region, which is
consistent with previous research. This explains why the boundary of the SCBs tends
to be buried in sandy land and loses its effect after long working hours. Our results
also indicated that whether the wind speed will decrease below the impact threshold
or the fluid threshold is the key factor affecting whether sand particles can penetrate
the SCBs and form stable wind-blown sand behind the SCBs under the same
conditions. Although our model has been able to reveal the inhibition effect of the
SCBs on wind-blown sand, there are still some aspects that need improvement, such
as aerodynamic entrainment, particle deposition on the SCB, and collision between
the sand particles and the SCBs. The size of the SCB used in our model is fixed. In
future work, we plan to analyse the effect of different heights and widths of the SCB
on aeolian sand erosion and discuss the reasons for the difference in heights between
the SCB and other obstacles, such as sand fences. Another aspect worth noting is that some additional factors, such as terrain and surface roughness, will affect SCB performance in anti-desertification projects, so the influence of these factors should be considered in the future. Using the proposed model, our work significantly analysed some results that are seemingly simple but lack a theoretical basis from the perspective of turbulence.

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Code and Data availability. All relevant code and data used to generate the figures in this paper can be accessed using the following email: hjhuang@usst.edu.cn.

Competing interests. The authors declare that there are no competing interests

Author contributions. HJ performed the programming, analyzed the results, and wrote the paper.

Video supplement. Video 1 and Video 2 can be downloaded at the following link: https://doi.org/10.5281/zenodo.6937805
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