Hydrological modelling on atmospheric grids; using graphs of sub-grid elements to transport energy and water

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Abstract.

Land Surface Models (LSMs) use the atmospheric grid as their basic spatial decomposition because their main objective is to provide the lower boundary conditions to the atmosphere. Lateral water flows at the surface on the other hand require a much higher spatial discretization as they are closely linked to topographic details. We propose here a methodology to automatically

5   tile the atmospheric grid into hydrological coherent units which are connected through a graph. As water is transported on sub-grids of the LSM, land variables can easily be transferred to the routing network and advected if needed. This is demonstrated here for temperature. The quality of the river networks generated, as represented by the connected hydrological transfer units, are compared to the original data in order to quantify the degradation introduced by the discretization method. The conditions the sub-grid elements impose on the time step of the water transport scheme are evaluated and a methodology is proposed to

10   find an optimal value. Finally the scheme is applied in an off-line version of the ORCHIDEE LSM over Europe to show that realistic river discharge and temperatures are predicted over the major catchments of the region. The simulated solutions are largely independent of the atmospheric grid used thanks to the proposed sub-grid approach.

1 Introduction

Lateral water transport over continents plays an important role in the Earth system but its implementation in models focusses on

15   different objectives depending on resolution. In global Earth System Models (ESM), tailored to address climate change issues, the main need is to transport the excess water over land to the oceans so as to close the water cycle. Because of their coarse resolution the main focus will be on the largest rivers. Regional ESM, as those used for process studies and downscaling of climate projections, will usually attempt to reproduce more details in the continental water cycle. Lateral water transports will thus also serve to predict levels of in-land water bodies or inundations and the impact of freshwater flows on coastal processes.

20 Finally for km-scale ESM currently being developed to better represent rainfall and convective processes, lateral flows allow to redistribute moisture along hill-slopes (Fan et al., 2019). At these resolutions the hypothesis that evaporation is only fed by local precipitation is not valid any more. For example, rain falling on mountain slopes needs to flow into the valleys where the vegetation is located which will be able to evaporate it. These are resolutions where hill-slope processes will start to be important.

25 Furthermore rivers also transport energy and biogeochemical species (Liu et al., 2020; Lauerwald et al., 2017). Thus their correct representation allows to close the associated global cycles of the Earth system and improve the coupling between continental and oceanic processes. To enhance the representation of coastal processes in ESMs at all scales, the energy and nutrient contribution by rivers will be a major topic in the years to come.

Land surface models, the components within ESMs dealing with continental processes, have implemented over the last 30
30 years a very uni-dimensional vision of the water and energy processes at the surface. The main driver of their development was to provide the lower boundary to the atmosphere. As a consequence they have also adopted the spatial discretization of the atmosphere so as not to introduce any discontinuity in this important coupling. Interpolating land surface fluxes and surface state variables on which they depend (surface temperature in particular) cannot preserve their consistency on two different grids because of the non-linearity involved. The lateral water transport cuts across this one dimensional vision and also challenges the
35 use of the atmospheric grid. Indeed, lateral water movements require often higher resolution than the atmosphere as topographic features are a stronger constraint for the flow of water on land than for the atmosphere. The hydrological community has been free of this constraint of the coupling to the atmosphere and could adopt appropriate spatial discretization, which is often at km-scale, for the representation of rivers.

ESMs have adopted over the last decades two different and complementary approaches to try and deal with the lateral
40 water transport on continents. The first and most widespread approach is to abandon the atmospheric grid and interpolate the fields of water exiting the one dimensional soil moisture (generally surface runoff and deep drainage) towards the grid which will be used to simulate river flows (Decharme et al., 2012; Branstetter, 2003). From this grid the discharge to the seas is then transmitted to the ocean model. The river routing model becomes an independent component of the ESM meaning it can be developed and validated separately. Sharing this component with other groups is also facilitated (Kauffeldt et al.,
45 2016). The main drawback of this approach is that it creates a division in the interactions between the vertical and horizontal motions of water on continents. It complicates the representation of such important processes as floodplains or irrigation. The interpolations between the atmospheric and routing grids will need to fulfil the conservation principles and preserve gradients in surface processes.

The second approach is to use directly the atmospheric grid for the lateral flows (Miguez-Macho et al., 2007). This has
50 been successfully applied in regional and km-scale ESMs for which the horizontal atmospheric grid is compatible with hydro-logical processes. The methodology has been particularly successful for flood forecasting where lead time for predictions are short (Yucel et al., 2015). A complementary methodology is to use a hydrological tiling of the atmospheric grid to achieve the effective resolution needed (Ngo-Duc et al., 2007; Clark et al., 2015). The general principle is to keep the vertical movements of water on the atmospheric grid but distribute the excess moisture over hydrologically consistent and connected tiles so that it

can flow horizontally. In principle this methodology should be able to bridge the gap between coarser atmospheric resolutions and the level of detail needed for surface flows while keeping a close link between the vertical and horizontal processes.

Using the nomenclature proposed by Yamazaki et al. (2013) this last method can be labelled hybrid river models. It uses the vector-based methodology within the atmospheric grid as water is transported between unit-catchments and then uses a grid-based approach when the flow leaves the grid cell. The combination of both yields graphs of hydrological transfer units (HTU) along which the water will flow within and from grid cell to grid cell. In the list of criteria established by Kauffeldt et al. (2016) to classify large-scale hydrological models, a hybrid routing addresses in particular the two linked to the grid (flexibility to grid structure and resolution). It should be able to deal with any atmospheric grid and in particular those based on the more complex icosahedron (Dubos et al., 2015) or cubed-sphere (Kim et al., 2021). The flexibility in resolution is given as the hydrological information which cannot be resolved with the grid-based flow, is treated with the vector-based transport.

Preserving the link between the atmospheric resolution and the sub-grid hydrology facilitates the representation of all the processes which involve exchanges between vertical and lateral water movements. It allows to represent floodplains and their impact on evaporation (Schrapffer, 2022) or water extractions for human activities (de Rosnay et al., 2003; Zhou et al., 2021). In this context the stream temperature can also be more easily simulated as the energy balance performed on the atmospheric grid can directly interact with open water areas which are part of the lateral flows.

The proposed study explores the numerical properties of such a hybrid routing scheme and in particular how it handles different atmospheric grids. In the first part of the paper we will show how the graph of HTU can be built and which properties of the hydrological network need to be preserved. Then we will present criteria which allow to verify the fidelity of the HTU graph and in particular how many sub-grid elements are needed for different resolutions of the atmospheric grid to preserve the original hydrological information. Once water is transported, criteria are needed to select a time step which ensures that the numerical solution converges. Finally we will show with the ORCHIDEE land surface model that the simplification of the digital elevation model introduced by the transport on a graph of HTUs is small compared to the uncertainty in the atmospheric forcing. The methodology will also be used to demonstrate the value of a simple implementation of stream temperature.

2 The river flow model

Before presenting the construction of the graph of hydrological transfer units (HTU), the equations used to transport water and heat along the network of rivers are presented. They give indications on the properties of the graph which need to be preserved.

2.1 Water transport

The flow of water occurs on a directional graph towards the outflow point (Diestel, 2012). As for the moment the focus is on simulating river flows, it is the $stream$ reservoirs which connect the various HTUs in the graph. Each HTU i is contained in only one atmospheric grid cell $\widehat{i}$ and covers the area fraction $\delta_{i,\widehat{i}}$ with the sum of all HTU areas equal to the continental surface provided by the atmospheric model. Thus for the fraction of land in the grid we have : $\sum_{i \in \widehat{i}} \delta_{i,\widehat{i}} = 1$. This means that the HTUs

are a connected supermesh of the land fraction within the atmospheric grid (Farrell et al., 2009) and which represent the river graph.

As the graph is directional we can pose the following indexing convention :

- $i+1$ is the downstream store of HTU i. Because we are in a directional graph the vertex $i+1$ is unique and at some point downstream the graph should end in the ocean or a water body for endorheic basins.

- For an HTU i there is an ensemble of upstream HTUs which will be denoted with $\{i-1\}$. For a basin head the ensemble will be empty.

- Fluxes connecting two HTUs are denoted with half indices. The flux leaving HTU i is placed at $i+1/2$

Given the above notation, the prognostic equations for water transports are given by :

$$\frac{\partial W_{i,stream}}{\partial t} = \sum_{j\in\{i-1\}} (Q_{j+\frac{1}{2},slow} + Q_{j+\frac{1}{2},fast} + Q_{j+\frac{1}{2},stream}) - Q_{i+\frac{1}{2},stream} \tag{1}$$

$$\frac{\partial W_{i,fast}}{\partial t} = \delta_{i,\widehat{i}} R_{\widehat{i}} - Q_{i+\frac{1}{2},fast} \tag{2}$$

$$\frac{\partial W_{i,slow}}{\partial t} = \delta_{i,\widehat{i}} D_{\widehat{i}} - Q_{i+\frac{1}{2},slow} \tag{3}$$

$$\tag{4}$$

Here $R_{\widehat{i}}$ is the surface runoff (i.e. water which does not infiltrate into the unsaturated zone of the LSM) on the atmospheric grid and $D_{\widehat{i}}$ the drainage exiting the soil moisture reservoir. Both of these fluxes are computed by the land surface model and thus behave according to the assumptions made there. The reservoir volumes are designated with W_X with $X \in \{stream, fast, slow\}$. The fluxes out of these reservoirs are $Q_{i+\frac{1}{2},slow}, Q_{i+\frac{1}{2},fast}, Q_{i+\frac{1}{2},stream})$ and are expressed in kg/s. They are defined as follows :

$$Q^t_{i+\frac{1}{2},X} = \frac{W^t_{i,X}}{\lambda_{i,X}\, g_X} \text{ with } X \in \{stream, fast, slow\} \tag{5}$$

The flow is thus given by the reservoir's water mass divided by the residence time. This characteristic time of each reservoir is the product of a geometric property (g_X, the inverse of a time), the topographic index symbolized by λ in km, and a constant in s/km which needs to be determined. We chose to distinguish the topographic index of the stream flow ($\lambda_{i,stream}$) and the one for the aquifers of the HTU (λ_i). The first one can be evaluated based on the geometry of the main river within the HTU. The second one provides a more aggregated view of the geometry of the HTU. The general principle for computing these parameters is :

$$\lambda = \sqrt{\frac{d^3}{dz}} \tag{6}$$

where d is the relevant length over which the water flows within the HTU and dz the elevation change along that path. In the section covering the construction of the HTU graph the computation of the topographic indices is detailed for each case (see section 3.5).

2.2 Stream temperature

The advection of heat content with lateral water transport is given by the advection of the aquifer temperatures and the interactions with the surrounding landscape and the atmosphere. In order to implement these processes, an initial temperature has to be chosen for the water in the fast and slow reservoirs. The assumption here is that they are determined by the temperature of the soils of the corresponding atmospheric grid. Our initial assumption is :

$$T_{i,fast} = T_{\widehat{i},up} \tag{7}$$

$$T_{i,slow} = T_{\widehat{i},low} \tag{8}$$

where $T_{\widehat{i},up}$ is the soil temperature averaged over the top $0.3\,m$ and $T_{\widehat{i},low}$ the mean value over the $3.5-17.5\,m$ layers. Currently the deepest node in the soil temperature diffusion model in ORCHIDEE is $17.5\,m$ thus imposing a lower limit on the depth for the temperature of the slowest aquifer. This situation can evolve in future versions of ORCHIDEE.

Evaluating the stream temperature through the advection of heat has to deal with the singularity arising when the reservoir content goes to zero. A relaxation towards the upper soil temperature was chosen to deal with this indetermination. This allows to write the following set of equations :

$$\frac{\partial T_{i,stream}}{\partial t} = \frac{1}{W_{i,stream}} \sum_{j \in \{i-1\}} (Q_{j+\frac{1}{2},slow}T_{j,slow} + Q_{j+\frac{1}{2},fast}T_{j,fast} + Q_{j+\frac{1}{2},stream}T_{j,stream})$$
$$- \frac{1}{W_{i,stream}}Q_{i+\frac{1}{2},stream}T_{i,stream} + K(T_{\widehat{i},up} - T_{i,stream}) \tag{9}$$

and

$$K_i = \frac{1}{1 + a\rho^{-1}W_{i,stream}/A_i} \tag{10}$$

where A_i is the area of the HTU and is used to transform the water mass in the stream multiplied by its density ρ into an equivalent height. a is a scaling parameter which allows to adjust the role of the relaxation term and thus explore the relative importance of initial temperatures and interactions with the environment surrounding the river in the determination of $T_{i,stream}$. If a is large, Eq 9 will behave like a pure advection scheme and only adjust the temperature of stream with shallow water levels to the top soil temperatures. As a decreases the interaction of the stream temperature with its environment will increase. This relaxation will mostly be active on HTUs with low stream reservoir which is physically reasonable. In areas where water flows in small streams the temperature of the water will be close to the one of the upper soils. This simple relaxation obviously does not cover the complex interactions of lakes or large rivers with the atmosphere and which are known to impact strongly stream temperature.

The numerical solution of these equations is discussed later (Section 5) as it depends on the definition of the HTUs.

Table 1. The atmospheric grids and land/sea masks for which HTU graphs were built to test the methodology.

grid name	Source	Resolution	Projection
WFDEI	WFDEI forcing dataset (Weedon et al., 2014)	$0.5°$	Regular longitude and latitude
E2OFD	MSWEP precipitation product (Beck et al., 2017)	$0.25°$	Regular longitude and latitude
MEDCORDEX	MED-CORDEX configuration	$20\,km$	Lambert conformal
EuroCORDEX	EuroCORDEX configuration	$11\,km$	Cassini projection

3 Building the graph of hydrological transfer units (HTU)

This section presents the methodology for constructing hydrological transfer units (HTUs) and connecting them to build a hydrological network suitable to simulate surface water transport. In contrast to the tiling of the atmospheric grid for vegetation (Ducoudré et al., 1993; Koster and Suarez, 1992), the connectivity of the sub-grid elements needs to be preserved and form a convergent hydrological graph. It is an evolution of the method discussed by Nguyen-Quang et al. (2018).

For the present study, the methodology for tiling the atmospheric mesh into graphs of HTUs is exemplified on 4 grids covering the Euro-Mediterranean region (Table 1) which are either used for off-line or coupled simulations of ORCHIDEE. To clarify the discussion, the polygons building the atmospheric mesh will be named grid cells while those of the hydrological digital elevation model's (HDEM) mesh will be designated as pixels. The domain of computation used is at least from $20°$ West to $60°$ East and $20°$ to $60°$ North. To illustrate the diversity of grids a small sample over the lower Seine is provided in Figure 1. Only rectangular meshes are considered here but the methodology can be extended to triangular ones. Schrapffer (2022), which presents the floodplains parametrization, uses HTU graphs built for two atmospheric grids over South America.

The methodology works on any atmospheric grid as long as the polygons constitutive of the mesh are provided together with the land/sea mask.

3.1 Hydrological digital elevation models

To perform the HTU decomposition and compute their properties a hydrological digital elevation model (HDEM) is needed. The minimal information required is elevation, flow direction, flow accumulation and distance to the ocean for each pixel. The elevation should be hydrologically consistent in the sense that no flow should lead water to gain elevation. As we will show below (section 4), this is not a strict requirement. The three data sets listed in Table 2 fulfil these criteria and have been used here to test the methodology. They needed to be standardized as each of these HDEM had a different set of variables required and were not using the same conventions.

The original HDEM used in IPSL's ESM is from Fekete et al. (2000) which is at $0.5°$ resolution. It has been enhanced by flow directions in Antarctica in order to carry meltwater to the ocean and close the global water cycle. Its low resolution was perfectly suited for the global models used in climate studies such as Ngo-Duc et al. (2007). The advent of higher resolution atmospheric models means that its usefulness is diminishing. For regional applications the HydroSHEDS data (Lehner and Grill, 2013) was
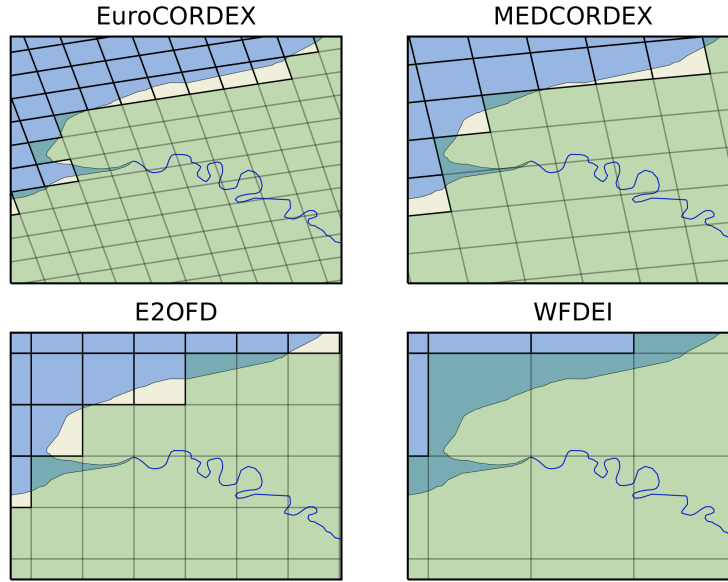
Figure 1. Samples over the lower Seine basin of the four atmospheric grids considered here (Table 1). The green colour indicates which meshes are land for the atmospheric model overlaid over the actual land outline in yellow/blue.

Table 2. The hydrological digital elevation models (HDEM) used in this study to evaluate the building of routing graph and the simulated river discharge.

Data set name	Source	Resolution	Domain covered	Constants used $[s/km]$		
				g_{stream}	g_{fast}	g_{slow}
FV	Fekete et al. (2000)	$0.5°$	Global including Antarctica	6.0	80.0	600
HydroSHEDS	Lehner and Grill (2013)	$30\,acrsec$	South of $60°N$ and excluding Antarctica	6.3	80.0	600
MERIT	Yamazaki et al. (2019)	$60\,arcsec$	Globe without Antarctica	6.3	80.0	600

used in ORCHIDEE over the Mediterranean region by Nguyen-Quang et al. (2018). The fact that this HDEM is not global means that it is only applicable for regional studies which do not cover the polar regions. In order to bridge this gap between global coarse and regional high resolution HDEMs we have chosen to also use a $60\,arcsec$ version of MERIT (Yamazaki et al., 2019). This version of MERIT was obtained by upscaling from the high-resolution flow direction data ($3\,arcsec$ MERIT
170 Hydro) with the Iterative Hydrography Upscaling (IHU) method (Eilander et al., 2021).

3.2 Supermesh between an atmospheric grid and a HDEM

The HTUs are built from the supermesh (Farrell et al., 2009) between the atmospheric grid and the hydrological digital elevation model (HDEM). The initial step is to create this supermesh by calculating the set of polygons of the HDEM grid overlapping with the coarser atmospheric mesh. The result is for each atmospheric grid cell the list of intersecting polygones and their area. At the borders of the atmospheric grid cell a number of small polygons with their areas and flow direction will be created. This generates some numerical noise but which will be absorbed during the HTU construction process. More importantly it allows to preserve catchment areas and the diversity of flow directions out of the atmospheric grid cell. A further complexity is introduced by HDEM pixels overlapping more than one atmospheric cell. All polygons generated by the supermeshing are kept but the largest is considered to dominate and to determine the connectivity of the graph between grid cells.

This process is performed using the *SphericalGeometry* library (https://github.com/spacetelescope/spherical_geometry) implemented in Python, which allows to calculate intersections of polygons over a sphere. This supermesh between the atmospheric grid and the HDEM can be saved into a NetCDF file to avoid having to perform this calculation again on the same combination of grids. The advantage of this procedure is that it is applicable to any atmospheric grid even unstructured ones. This is particularly important as atmospheric models evolve towards more complex grids (Dubos et al., 2015).

3.3 First construction of HTUs

A first set of coarse HTUs is built by joining all polygons of the supermesh which flow out of the atmospheric grid cell to a neighbouring grid cell. Their local upstream area is computed using the the area of the overlapping HDEM pixels. This first set of HTUs is quite coarse but ensures that all rivers and flow directions out of the atmospheric grid are preserved. The example in Figure 2c) (for the user selected truncation $nbmax = 18$) still carries some elements of this decomposition with the HTU 18 flowing out of the Eastern part of the Northern edges of the atmospheric grid. These small HTUs will not transport large water amounts but ensure that the total upstream area of rivers to which they contribute remains correct. At this stage all pixels which contribute to the main outlet of the Rhone in the lower left corner are still in the same HTU. This first step will conclude with as many HTUs as there are arrows pointing out of the grid cell, as illustrated in Figure 2.

3.4 Sub-division of HTUs

An algorithm is needed to sub-divide the larger HTUs to better represent the river network within the atmospheric mesh. The objective is to divide the HTU at important confluences. There are two types of confluences which need to be considered:

- Two large rivers (large global upstream area) meet as illustrated in Figure 2a) around Valence. Figure 2b) shows three rivers with a large global flow accumulation joining the Rhone river in the grid.

- A local river (large local upstream) joins a large river. This is for instance the case for HTU 8 in Figure 2c) which corresponds to La Barberolle flowing into the Rhone river in Valence.
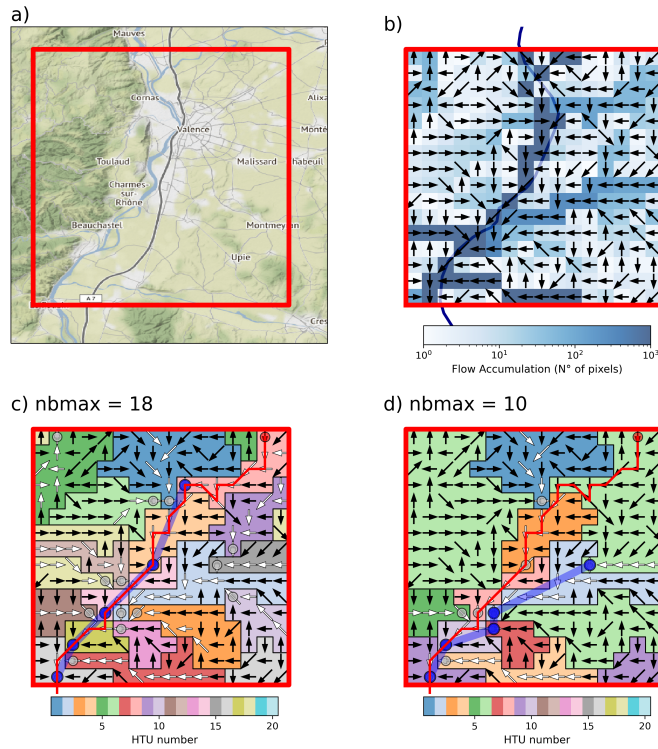
Figure 2. A sample case of a regular atmospheric grid cell decomposed into HTUs over the Rhone valley. a) The geographical context of the Rhone at Valence, France. b) Flow directions and accumulation for the HDEM pixels overlapping the atmospheric grid cell. c) Resulting HTU decomposition using $nbmax = 18$. d) As previously but for $nbmax = 10$. The white arrows within each HTU highlight the river segment used to determine the geometric properties used to compute the residence time of the stream reservoir. The grey dots indicate the location where one HTU flows into the downstream one. In the two lower panels the red line highlights a sample river segment in the HDEM as is used to statistically evaluate the river graphs (Section 4). The blue line is the corresponding river segment but now in HTU space.

The section is made at the confluence pixel between the main river and its tributary. This produces 3 new HTUs : (1) the part of the main river upstream of the confluence and with this pixel of the HDEM as it outflow location, (2) the downstream part of the main river which keeps the initial outflow pixel and (3) the tributary which has as outflow pixel the one before the confluence. If the subdivision (1) or (2) is too small, the HTU is only divided into two parts : the HTU of the main river and the confluence. The tributary will now flow directly to the outflow point of the original HTU and thus potentially creating a small topological error. The aim is to avoid generating too small HTUs on the main rivers.

This algorithm is iterated until one of two conditions is met :

- the tributary has the 4th highest global flow accumulation.

- The local upstream area is less than 10% of the grid cell area.

3.5 Computing topographic indices

The residence time of water in the stream reservoirs is given by the topographic index ($\lambda_{i,stream}$) and a constant (g_{stream}) as shown in Eq 5. $\lambda_{i,stream}$ is determined using Eq 6 with the length and elevation change of the river between the inflow pixel with the largest upstream area and the outflow of the HTU. If the HTU is a headwater, then the longest path is used until an elevation change larger than 30% on the HDEM is reached when moving upstream. This avoids taking into account the steepest parts of the catchment. The aim is to capture the geometrical feature of the main river flowing through the unit. In Figure 2d) this would be the elevation change and length along the pixels with a white arrow within each HTU.

For the fast and slow reservoirs, the topographic index λ_i should represent the general characteristics of the whole HTU and its complexity when computing the outflow in Eq 5. Therefore, another approach is used based on the hypothesis that there is a set of small streams or subterranean flows contributing to the main stream of the HTU. Starting from the topographic index computed on each pixel of the hydrological grid, sums are computed along all streams down to the outflow point of the HTU. These sums are then averaged to provide an integrated property for the HTU. This allows to produce a λ_i which is representative of the soils and hill-slopes surrounding the river. This was found to work best in the proposed set-up but is only a crude simplification of what is known of hill-slope and riparian processes.

If other variables of the LSM, soil moisture for instance, are also simulated at the HTU level then the hill-slope processes which govern the riparian water exchanges could be parametrized. As suggested by Picourlat et al. (2022) the geometric characteristics of the HTU and its soil moisture can be used to predict the flow of near surface groundwater into the river.

3.6 Reaggregation

At this stage, the atmospheric grid cell can contain more HTUs than requested by the user with the $nbmax$ parameter. The user may want to choose a simpler river network in order to reduce the memory footprint of the routing scheme. This depends on the configuration best suited for the user's need. But we would not recommend to select a value of $nbmax$ below 8 on a rectangular grid as then the number of outflow directions of the meshes is limited. The reaggregation step of the routing pre-processor is to reduce the number of HTU on all grid cells of the atmospheric mesh to the $nbmax$ value chosen by the user. The merger of HTUs will be performed by always favouring the largest HTU or the one with the largest upstream area while trying to preserve the diversity of outflow directions out of the atmospheric grid cell. The elimination of the smallest HTUs is performed in 5 steps until the $nbmax$ value is reached :

1. Merge all HTUs of an atmospheric grid cell which flow into the ocean,

2. Merge HTUs which flow to the same neighbouring grid cell by starting with the smallest. This reduces the border noise by merging the smallest HTUs which have been generated by the supermesh methodology.

3. Merge HTUs which belong to the same river and flow out of the mesh. As this is also performed for HTUs flowing out in different directions it generates topological errors.

4. Merge HTUs which flow into a downstream HTU within the same atmospheric grid cell,

5. Finally a brute-force method is used to merge the smaller HTUs until $nbmax$ is reached. If this method has to be applied to HTUs with an area higher than 5% of the grid cell the user is warned that a higher $nbmax$ should be considered.

During the reaggregation step, the HTUs do not need to be connected when merged. This leads to situations like HTU 6 in
Figures 2d) which is composed of areas East and West of the Rhone.

As highlighted in the discussion above, in order to simulate a realistic river discharge the length and slope of the main rivers need to be well preserved in the HTU decomposition. It is clear that if the truncation steps have to be carried too far because of a poor choice by the user, a poor quality graph will be obtained and a reliable simulation of the stream flow cannot be expected. Below we will present a methodology which allows to verify the quality of the graph and estimate an optimal number of HTUs for a given atmospheric grid resolution.

3.7 Positioning of gauging stations

Stream gauging stations are precious tools to validate the simulated water cycle of land system models at catchment scale. For this reason, it is important to be able to localize these stations in the HTU space. Obviously, depending on the fidelity of the river graph in the HTU space more or less stations can be reliably placed. The position of the stations will be made according to their geographic position and the error in the upstream area within the model. The user can choose the maximum error in distance and fraction of upstream area which can be tolerated.

After the construction of the HTU graph, the pre-processor will attempt to place each station within the tolerance selected by the user. The errors will then be minimized to select the HTU which will be considered representative for the given station. This information will then be archived with the HTU network so that the land surface model can monitor the flow out of the HTU corresponding to the station during the simulation. As the stations are placed in the HTU space, when the characteristics of the graph change more or less stations can be positioned within the allowed errors.

4 Validation of HTU graph

A method is needed in order to statistically validate the quality of the HTU graph and identify the deviation from the original HDEM induced by the reduction of effective resolution operated by the algorithm described above. As HTU graph construction is designed to work without human supervision and at global scale, a visual inspection is not sufficient.

The validation method samples randomly a large number of river segments which are representative of the network. The length and elevation changes for each of these segments are computed on the HDEM and on the HTU graph to evaluate the errors. The red lines in Figures 2c) and d) represent one such segment. Its length and elevation change computed on the HDEM by summing over all pixels it traverses is our reference. In HTU space, the river segment is represented by the blue lines and illustrates the large differences with the selected truncation ($nbmax = 18$ and 10 in Figures 2). The properties of the stream within the HTU is given by the white arrows within the area to which the outflow points belong (represented by a grey circle). The properties of the segment in HTU space can thus be computed by summing the HTU's stream length and elevation

change along the blue lines. By comparing it to the reference the degradation of the stream properties in the HTU space can be estimated.

275 The errors of segment properties can be decomposed into a cell and a topological error. Within each HTU we can compare the sub-segment's properties computed with the HDEM to the one used for the HTU. This will be called the cellular error. In Figure 2c) the properties of HTU 8 are given by the white arrows and they are different from those of the red line. We will thus have a small cellular error here. In the downstream HTU (number 4) on the other hand, the cellular error is zero as the segment overlaps with the main river (white arrows). The topological error describes differences in the path followed by the

280 rivers. In Figure 2c) at $nbmax = 18$ the river La Barberolle passes through Valence on its way into the Rhone. For $nbmax = 10$ (Figure 2d)) this river flows into another one south of the city before joining the Rhone. This is a topological error which is independent of the properties of each of the HTUs. As this error is difficult to quantify, it will be estimated by subtracting the cellular error from the total error.

This methodology is applied over the largest European rivers (Danube, Rhone, Rhine, Loire and Elbe) for the four atmo-

285 spheric grids presented above. The relative errors and their statistics are computed over a sample of 8000 segments. To ensure a good representativeness the length of the segments is chosen between 100 and $1000\,km$. To avoid unrepresentative starting points, their upstream area should be at least of $10\,km^2$. Other values for these parameters of the sampling method were tested but it did not change the results.
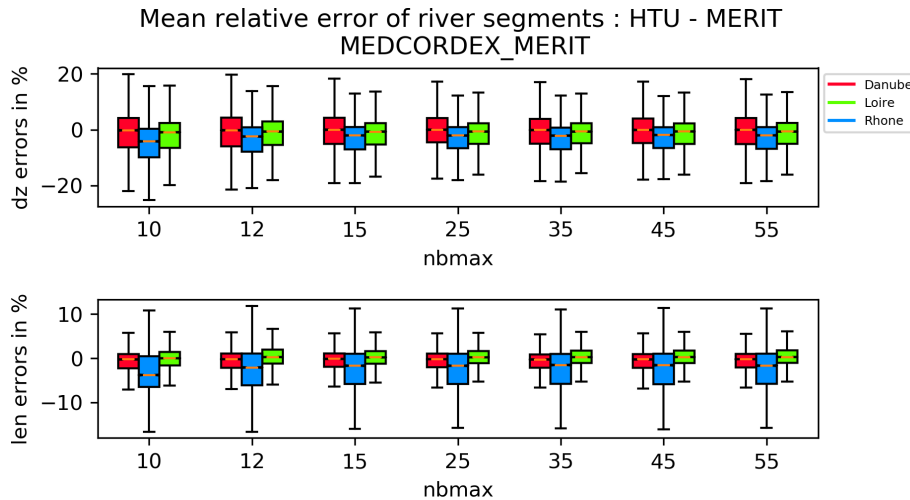
Figure 3. Figure provides the distribution of errors for the elevation change (dz) and length (len) for the 8000 samples over 7 different truncations. The error bars represent the standard deviation of the error sample.

Figure 3 shows the dependence of the average relative errors with the chosen truncation ($nbmax$). The error bars in the

290 figure provide the variance of relative errors within the sample of river segments. The variance is driven by the diversity of segments drawn in terms of length (affecting the relative errors) and the complexity of the hydrological structure. This analysis
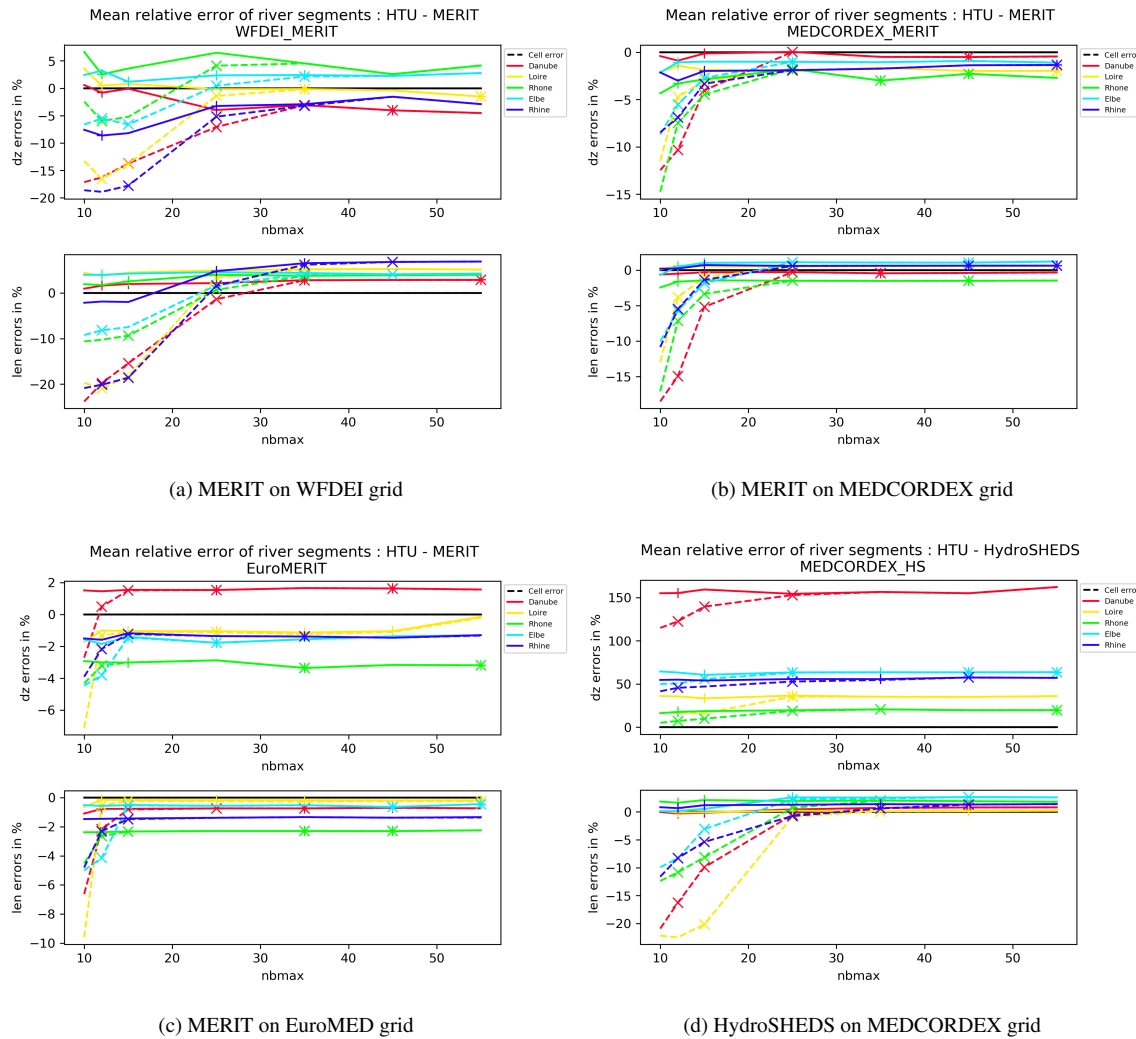
Figure 4. Error decomposition for the segment's elevation changes and length for 5 rivers at 3 different atmospheric resolutions and two different HDEMs. The solid lines provide the total relative errors while the dashed lines show the cellular contribution. Symbols on the lines indicate that the change relative to the next coarser truncation (lower value of nbmax) is significant.

is only displayed over 3 basins not to clutter the graphics too much. For the length of the segments the errors are within a range of $\pm 10\%$ with the largest standard deviation found for the smallest truncations. For elevation change most relative errors are smaller than 25% with again the largest spread obtained for $nbmax = 10$. The large variance of errors around the mean imposes that variations of the mean relative errors need to be tested statistically. To this end the mean errors are compared to the next higher truncation using a simple t-test for two independent samples. This will allow to show if increasing the number of HTUs used to represent the rivers significantly improves the quality of the graph or not.

295

Let us now analyse how the quality of the HTU graph depends on the resolution of the atmospheric grid and the maximum number of HTUs allowed per grid ($nbmax$). First we examine in Figure 4a) the evolution of the mean relative error with increasing $nbmax$ on the coarsest grid (WFDEI). For the lowest truncation ($nbmax = 10$) on the Rhine the mean segment elevation changes (dz) are lower than those in the HDEM by about 10%. This error is larger at the cell level (dashed lines), meaning that on average the dz of the HTUs are smaller than the corresponding sub-segment by over 15%. This difference of errors is explained by the fact that on average the connections between HTUs are further downstream than on the HDEM, thus compensating partly the cellular error. This large difference between the total and cell mean errors is not an ideal solution as it means that the actual course of the river is not well respected by the cascade of HTUs. The same behaviour is also found for the length of the river segments with an even larger compensation by the topology of the river. Figure 4a) also demonstrates that as $nbmax$ increases the total mean error reduces and is overwhelmingly explained by the cell error. For the WFDEI grid the optimum is obtained for $nbmax = 35$. Above this value increasing truncation does not significantly change the mean error any more according to the t-test. At this point we have enough HTUs per $0.5°$ grid cell that the only error in the selected river segments are those linked to the fact that the HTU's properties are slightly different from the elements of the segments crossing them. It can also be noted that from this truncation onward the mean relative errors in elevation changes and segment length are stable and small.

Figure 4c) shows the same results for the mesh with the highest resolution considered here ($11\,km$). The mean relative errors in dz and len are smaller than the coarser mesh considered above, also for high $nbmax$ values. It also demonstrates that the convergence of the cell and total relative errors occurs already at $nbmax = 15$. The higher atmospheric resolution facilitates the aggregation of the hydrological information of the MERIT HDEM which is at $60\,arcsec$ resolution. There are about 8 grid cells of the EuroMED grid in each WFDI grid. But we can obtain similar qualities for the HTU graph in WFDEI with only a little more than twice the number of HTUs. This shows that the algorithm to aggregate the hydrological information at the atmospheric grid captures well the main features which determine the flow of water along the network. Obviously, would the HDEM be of higher resolution (MERIT is available at 90m) then also for the EuroMED grid more HTUs would be needed to describe the network.

For the MEDCORDEX grid at $20\,km$ we have build the HTU network with two different HDEMs. For the MERIT HDEM ($60\,arcsec$ resolution) the convergence of cell and total relative errors occurs at $nbmax = 25$. Errors are smaller than 5% for both the elevation change and length of samples (Figure 4b). When HydroSHEDS ($30\,arcsec$ resolution) is used the behaviour changes slightly. Let us first examine the errors for the length. The convergence of errors occurs at $nbmax = 35$. Because of the higher resolved hydrological information more HTUs are required for its proper representation. For the segment length, the mean errors are similar than for the MERIT HDEM. The situation is more complex for the elevation changes of the segments. Because HydroSHEDS does not provide a hydrologically corrected topography, the errors are much larger than for MERIT (Yamazaki et al., 2012). When following downstream the segments in HydroSHEDS a number of situations are encountered where the elevation change is negative, i.e. water flow into a pixel with a higher elevation. For shorter segments this occurs for about 20% of the pixels while for longer segments, which are more likely to traverse flat areas, it can reach 30%. On the HDEM, for the full segment, these errors compensate and the total elevation change can be assumed to be correct.

(a) WFDEI grid and MERIT   (b) EuroMED grid and MERIT
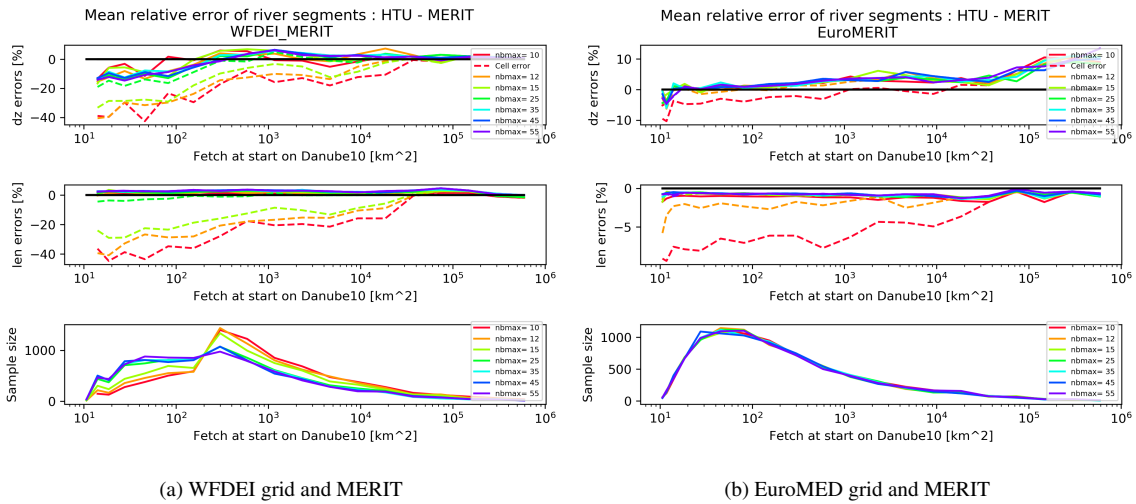
Figure 5. Distribution of errors along the upstream area (or fetch) of the starting point of the segments for the Danube. The solid lines provide the total errors while the dashed lines show the cellular errors.

But when decomposing it into pieces the compensations can be interrupted. Furthermore when constructing the HTUs we have imposed that dz cannot be smaller than $0.1\,m$ thus creating a large discrepancy with the segment as defined in the HDEM.

335   Figure 4d) shows that for rivers with large flat areas such as the Danube the error is largest while it is relatively small for catchments dominated by mountainous areas such as the Rhone.

To determine the main sources of errors in our samples, their distributions relative to the upstream area of the initial point are analysed for the Danube as an example. Figure 5 displays these distributions for the coarsest and finest grids analysed here. First it has to be observed that because of the dominance of small sub-catchments in any river basin, the sample of segments

340   favours starting points with about $100\,km^2$ of fetch. Again we can see for which $nbmax$ the cell and total errors converge but also that the higher truncations are less needed for larger basins as the convergence there is faster. The mean error in segment length is stable with changing upstream area. On the coarse grid we can note that for small rivers (fetch $< 300\,m^2$) the dz error is relatively large. This error is amplified by sampling bias and thus has a major contribution to the mean error. This error in dz for small catchments is consistent with the hypothesis of the decomposition algorithm which favours the properties of the

345   largest river in a grid cell to guide the graph construction. This leads to small catchments having a higher probability to display segment properties that do not match those of the HTU.

It must be noted that for the EuroMED grid the error in dz increases with the size of the upstream area. This is simply because segments with large upstream areas are more likely to cross flat areas of the Danube basin. The distribution of segment errors was also computed against the length of the sample (not shown). For both the length and elevation change errors it is

350   found that they are quite constant except for short segments. As they are likely to have also small upstream areas they display a relatively large cell error.

Table 3. The parameters used for the four atmospheric grids for which HTU graphs were built to validate the numerical method. If not specified otherwise, the MERIT HDEM is used. The HTU graph on the MEDCORDEX mesh using the HydroSHEDS HDEM is labelled MEDCORDEXHS.

grid name	Resolution	Optimal truncation for MERIT ($nbmax$)	Optimal time step [s]
WFDEI	$0.5°$	35	1800
E2OFD	$0.25°$	15	900
MEDCORDEX	$20\,km$	12	900
		HydroSHEDS = 25	450
EuroCORDEX	$11\,km$	10	450

In conclusion of this section we provide the optimal truncation for each grid used here (Table 3). The values for $nbmax$ are derived from the statistical analysis presented above and chosen to be the point where reductions in errors in the graph are not any more justified. Higher values would only bring extra computational cost.

5 Validation of the numerical implementation

For the constructed HTU graphs the constants g_X, which are the inverse of a velocity, need to be estimated. Tests with OR-CHIDEE have shown that for the two high resolution HDEMs the same values can be used and for the coarser one the constant for the stream needs to be changed slightly (see Table 2)(Schrapffer, 2022). It is quite likely that these parameters are more dependent on the land surface scheme used here than the HDEM. The repartition of water fluxes between surface runoff ($R_{\widehat{i}}$) and drainage ($D_{\widehat{i}}$) as well as the inertia of the soil moisture model will play a key role for these constants. Thus the values given in Table 2 are probably only valid for ORCHIDEE's current soil moisture model (de Rosnay et al., 2002; d'Orgeval et al., 2008) in its $2m$ depth configuration. Using the HTU graphs produced here in any other land surface model will probably require to readjust these parameters.

The water continuity (Eq 5) is discretized in time using an explicit numerical scheme. This means that the fluxes $Q_{j,X}$ are evaluated before the reservoir content ($W_{i,X}$) is updated. This choice simplifies the implementation and the interaction with the parallelisation of the ORCHIDEE code. The heat transport Eq 9 is also implemented using an explicit method. In order for the relaxation term to be able to efficiently avoid the singularity of empty reservoirs it is evaluated implicitly. This flux will thus depend on the current upper soil temperature and the stream temperature at the next time step.

The Courant–Friedrichs–Lewy (CFL) condition mandates that for a convergence of the numerical solution the time step needs to be smaller or equal to the residence time ($\lambda_{i,X} g_{i,X}$) of the water in the fastest reservoir of the HTU: the stream. Given the decomposition of the atmospheric grid into HTUs for a finer representation of the hydrological connectivity, a wide distribution of residence times will be obtained with some values being very short. It is thus not practical to select a time step for the routing scheme based on the smallest residence time on the domain. The scheme thus needs to be able to cope with

unstable flux calculations. To this end the numerical solution for the continuity equation (Eq 5) also includes a flux limiter given by : $Q_{j,X} \leq W_{i,X} \Delta t$. This condition should only activate for reservoirs with low water contents and short residence times. As this flux limiter also determines the numerical quality of the simulated discharge, the model monitors how often this condition has to be imposed.

A practical solution for choosing the time step of the routing scheme is to select a position within the area weighted distribution of residence times of all HTUs within the computational domain. It is proposed to select the time step corresponding to the 25% quantile of this distribution. This means that 75% of all HTU by area will not violate the CFL criteria while for the others there is a risk that the solution will not be correct. As a consequence it needs to be verified that this compromise on the quality of the numerical solution on some HTUs will not affect the simulated discharge at the spatial scales of interest. We found that the time steps determined with this method are more dependent on the atmospheric resolution than the hydrological truncation. This is quite convenient as with a refining of the atmospheric grid the time step of the processes which have the land surface scheme as a lower boundary will also decrease. Thus increasing the frequency at which the routing scheme will need to be called is not a strong constraint.

This section explores the convergence of the simulated discharge with the selected time step (Δt), the number of HTUs ($nbmax$) and the resolution of the atmospheric grid. The analysis is performed on a number of simulations over the Euro-Mediterranean domain discretized with the atmospheric grids presented in Table 1. To focus on the numerical properties of the routing scheme, a version decoupled from ORCHIDEE is used which is directly forced with daily mean surface runoff, drainage and temperature profiles extracted from a previous WFDEI-GPCC (Weedon et al., 2014) forced simulation of ORCHIDEE. These fields have been interpolated to the selected time-step for the routing and to the spatial resolution of the atmospheric grid on which the routing scheme is to be evaluated.

These simulations are evaluated at a limited number of gauging stations which cover a range of upstream areas and climates. From the over 3800 stations placed on the river graphs of the Euro-Mediterranean region only a few were selected with upstream areas ranging from 2500 to $8\,10^5\,km^2$. The lower limit is given by the spatial resolution of the WFDEI forcing and ensures that the smallest catchments contain at least one atmospheric grid cell. The largest catchment is the one of the Danube. The list of these stations is provided in Appendix A. At each of these points in the graph, the simulated river discharge and temperature are evaluated against a reference configuration. The metrics used to quantify the change of behaviour of the model are the Nash–Sutcliffe model efficiency (NSE), the correlation and ratio of standard deviation. These metrics are computed with daily values over an 11 year period going from 1983 to 1993. The chosen methodology limits the numerical evaluation of the scheme presented here to spatial resolutions of atmospheric features of about $0.5°$ and daily mean discharge values.

5.1 Role of the time step

The length of the time step is first tested on the graph produced with MERIT for the WFDEI grid using $nbmax = 35$ based on the evaluation in section 4. The time step is progressively increased from $225\,s$ to $5\,h$ and the smallest value is considered to be our reference.
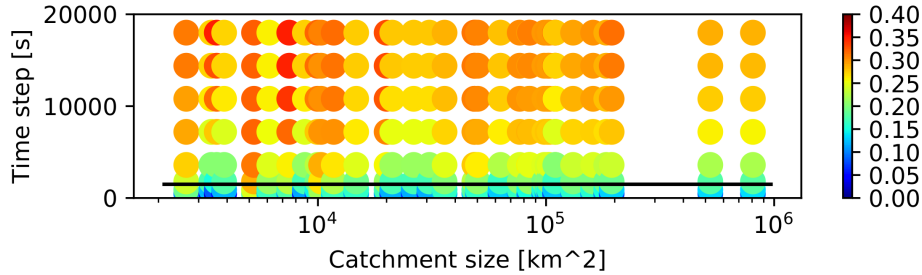
Figure 6. At each station and for the range of time steps tested, the fraction of HTUs for which the flux limiter has been activated in the upstream catchment. The black line indicates the recommended time step for the WFDEI grid and MERIT HDEM.

As a first step, we examine the fraction of HTUs where the flux limiter has to be applied to stream flow. As this variable is quite constant throughout the period analysed, only the mean is shown in Figure 6 with the selected stations ordered by up-stream area along the x-axis. In the y direction the tested time steps are plotted and each dot measures the quality of one
410 simulation compared to the reference. This graphic demonstrates that the flux limiter applies to all catchments independently of their size but the frequency of its activation is a strong function of the time step used. The horizontal line shows the time step at which 75% of HTU satisfy the CFL criteria. At this level the flux limiter has to be applied to less than 20% of the HTUs. Thus, when looking at the convergence of the solution with the time step we have to consider that not only the CFL criteria deteriorates the solution but also the flux limiter.

415 Figure 7 compares for the same set of experiments but now examining the degradation of discharge and stream temperature with time step when compared to the shortest value ($\Delta t = 225\,s$) using the three metrics discussed above. The Nash–Sutcliffe model efficiency is close to one for all simulations performed with time steps close to or lower to the recommended value (horizontal line). The correlation between the reference and the test simulation remains close to one as well as the ratio of variance. In this range of time steps we can consider that the numerical solution has converged for catchments larger than
420 $2500\,km^2$. Once the 25% quantile of residence times is passed some stations show quick degradation in the simulated discharge and we can note that generally small catchments are more sensitive than larger ones. On the most downstream stations of the Danube (to the right of the x-axis) the degradation only becomes apparent for time steps of a few hours. For smaller catchments this can occur much earlier. This degradation is not a linear function of up-stream area as it also depends on the complexity of the river graph and the topography. The degradation of the river discharge is manifested by a reduction of the correlation of
425 daily discharge values with respect to the reference and a decrease of variance. The peak discharges are more strongly affected by increasing time steps than the base flows.

The right column in Figure 7 shows that stream temperature is much less sensitive than discharge to increasing time steps. This is not surprising given that the rivers have relatively slow fluctuating temperatures. The mass flux is thus the driving constraint for the temporal discretization of the routing scheme.

(a) Discharge WFDEI MERIT

(b) Stream temperature MERIT
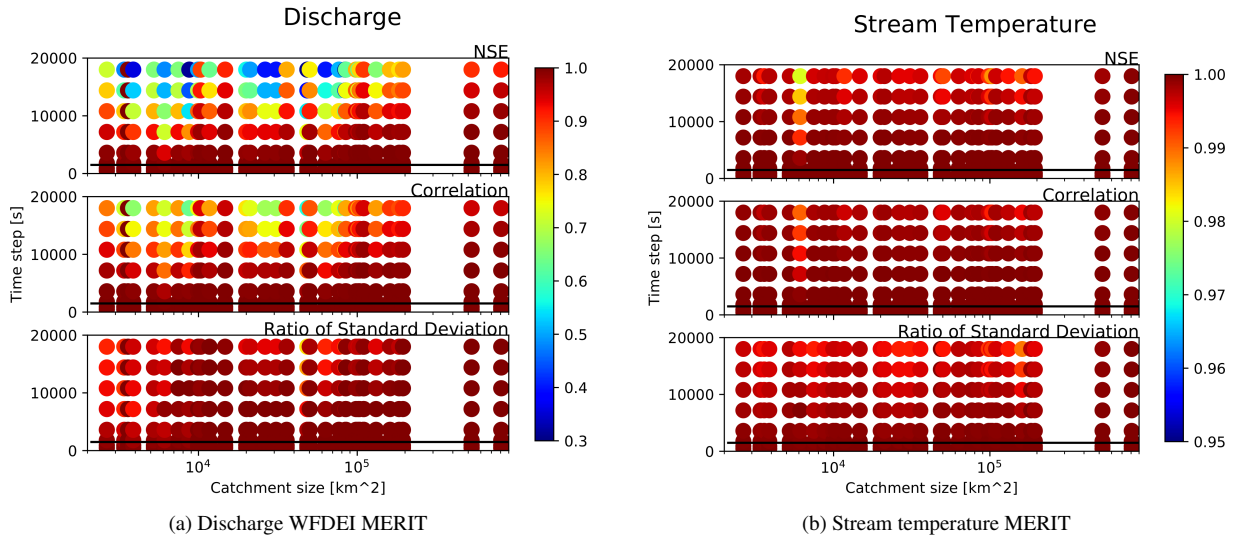
Figure 7. Comparing simulations on the WFDEI grid (with the MERIT HDEM and $nbmax$=35) with increasing time step to the reference at $\Delta t = 225\,s$ (black line).

Figure 8 shows only the NSE metric but now for three atmospheric grids and in one case for HTU graphs built with a different HDEM (HydroSHEDS). The results are very similar to the ones presented above. We can conclude that the 25% quantile of the residence time is a quite robust method to determine the time step which satisfies the CFL criteria and keeps the flux limiter to an acceptable level. Comparing the figures in the upper row shows that the criteria recommends a shorter time step for the HydroSHEDS HDEM (See table 3) as it provides hydrological information at $30\,arcsec$ resolution. The degradation of the comparison to the reference occurs for longer time steps than for MERIT although we are on the same atmospheric grid (MEDCORDEX). This can probably be traced back to the quality of the hydrological information provided by both HDEMs. In both cases the methodology for selecting the time step seems to be too conservative on this $20\,km$ grid. This result is confirmed on the E2OFD and EuroMED grids as the degradation of the numerical solution occurs for time steps larger than the recommended value. But it has to be kept in mind that the runoff forcing used here is an extrapolation of data from a $0.5°$ grid and thus it is of lower temporal and spatial variability than one would expect at the higher resolutions presented here. Furthermore on the higher resolution grids, given the appropriate atmospheric forcing, the user would want to analyse smaller catchments and more extreme hydrological events.

5.2 Role of truncation in HTU space

The same type of analysis can be performed to explore the impact of the number of HTUs used per grid cell on the time step. Using small values for $nbmax$ reduces the memory footprint and computational time of the routing scheme. For each case we use the time step proposed by the 25% quantile of the residence time distribution. As the discharge is evaluated at gauging stations, when $nbmax$ is modified the position of the station within the graph can also be affected. Thus the results presented
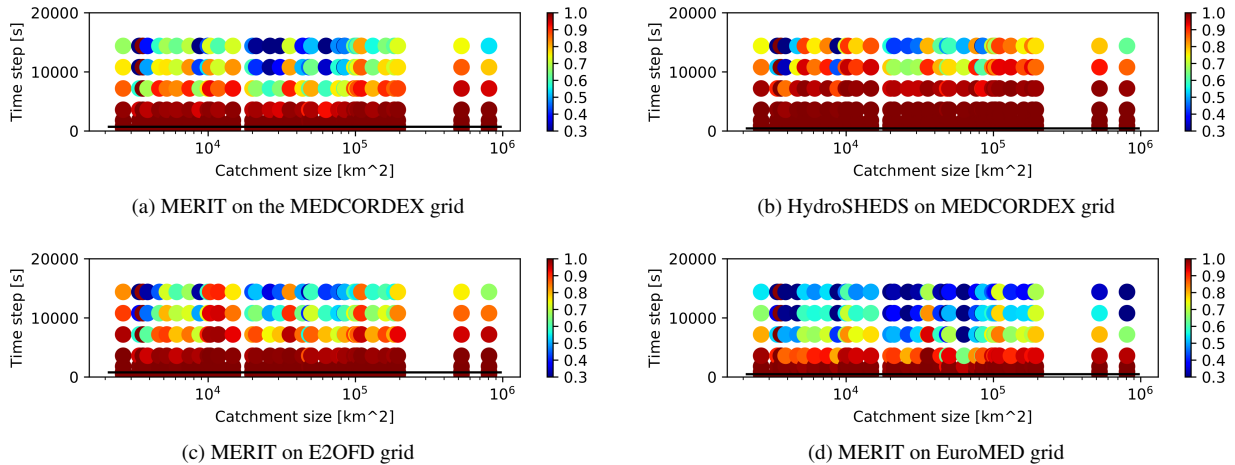
Figure 8. Convergence of simulated discharge with increasing time steps on the three different grids presented in Table 1 and the two HDEM for the MEDCORDEX grid. Only the Nash-Sutcliffe efficiency is displayed.

here not only evaluate the impact of the truncation on the simulated discharge but also the positioning of the sampled point. These two factors are not independent and both affect our ability to reproduce observed river flows.

450   The y-axis of Figure 9 now shows the maximum number of HTUs per atmospheric grid cell ranging from 10 to 45. The configuration $nbmax = 55$ is considered as our reference here. The graphics show that the truncation is of less consequence to the quality of stream levels and temperature, within the range considered here, than the time step. For the smallest value of $nbmax$ the NSE only falls to 0.75. In none of the three metrics considered here there is an indication that the result depends on catchment size. If one were to consider maximum number of HTUs lower than 8, then not all outflow directions of the

455   rectangular atmospheric grids can be represented and the impact on the simulation would probably be more severe. These extremely low values of $nbmax$ were not considered as they defeat the point of a sub-grid approach to routing.

All stations where a significant degradation of the simulation occur, it takes place below $nbmax = 35$. This result is consistent with the statistical analysis of the river graphs presented above (Section 4). For MERIT on the WFDEI grid, the quality of the segments starts to decrease for $nbmax$ below 30. This point is not as clearly visible here as the analysed stations all

460   have a relatively large up-stream area. As demonstrated with Figure 5 the errors in the river segments are more pronounced for catchments smaller than $10^4 \, km^2$. To demonstrate the loss of numerical convergence for discharge caused by a coarse HTU graph stations in small catchments would need to be sampled. But this would not be consistent with a forcing at $0.5°$ resolution.

5.3   Role of the resolution of the atmospheric grid

Based on the analysis of the graphs presented in Section 4 an optimal value for $nbmax$ and time step has been selected for

465   each combination of atmospheric grid and HDEM (See Table 3). The objective here is to determine how sensitive the simulated
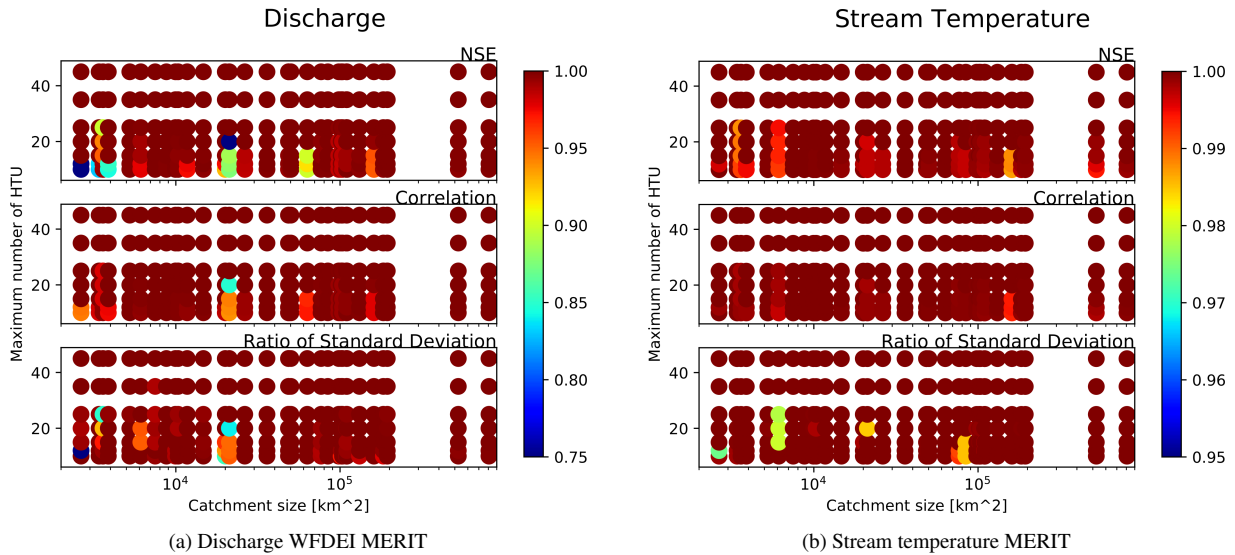
Figure 9. Simulations on the WFDEI grid (with the MERIT HDEM and $\Delta t = 900\,s$) with increasing maximum number of HTU are compared to the reference which is chosen to have $nbmax = 55$.

discharge is to the atmospheric grid given the same runoff and discharge fields. As they originate from a WFDEI simulation on the $0.5°$ grid this will be used as our reference here.

Figure 10 shows for the selected stations the deviation of the three other configurations from the WFDEI-MERIT case. One can note that the changes in the three metrics used are generally small. There is no systematic dependence of the numerical quality with the grid or catchment size even though the resolutions and projections are quite different. One may note that there is systematic degradation of the NSE efficiency, correlation and ratio of standard deviation when changing the HDME on the MEDCORDEX grid. The MEDCORDEXHS simulation differ particularly for stations with a catchment larger than $7\,10^4\,km^2$. This can be expected as it is based on another description of the topography and river flow directions than the reference. Difference accumulate with the size of the basin. When only the resolution changes (E2OFD, MEDCORDEX, EuroMED), the impact on the simulated variables is low except for a few stations. For the E2OFD configuration the station Rekingen on the Rhine (catchment area of $1.4\,10^4\,km^2$) stands out. As it is mostly the correlation and the NSE which are affected it has to be assumed that it is positioned differently in the river graph.

5.4 Convergence of the numerical solutions

It is an important result that for the range of atmospheric grids tested here, an optimal truncation and time step can be selected according to the criteria defined above which provides a converged solution. That is, the simulated stream flow and temperatures are relatively insensitive to higher truncation or shorter time steps thus optimizing the numerical cost of the model. This also removes the necessity to adjust the parameters g_X of the routing scheme when running at different resolutions.
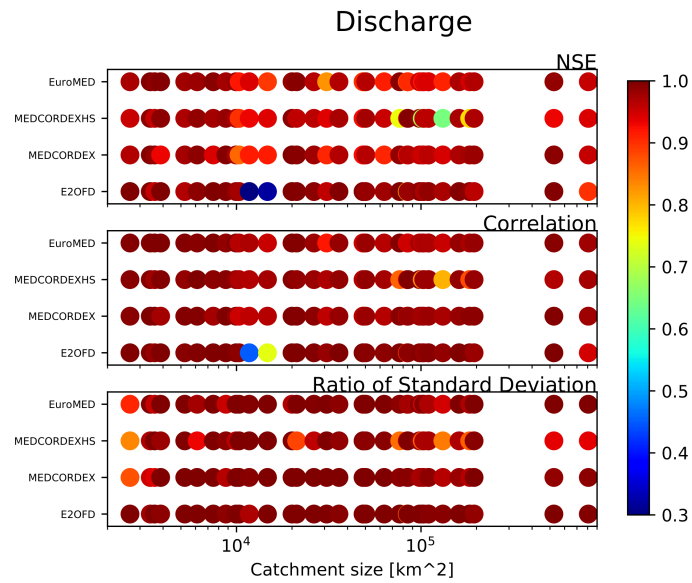
Figure 10. The impact of the atmospheric grid is evaluated by comparing the WFDEI simulation to the three other grids (E2OFD, EuroMED and MEDCORDEX) for the MERIT HDEM. The MEDCORDEXHS label indicates the MEDCORDEX grid using the HydroSHEDS HDEM (See Table 3).

Nevertheless, some caveats have to be kept in mind. The numerical verifications presented above were performed using output from an ORCHIDEE simulation forced by the WFDEI-GPCC forcing at $0.5°$ resolution. Because of its 3 hourly forcing

485   there is little diurnal variability in the surface runoff and generally the spatial variance is limited by the coarse atmospheric information. The higher resolutions evaluated here were run with variables which do not include all the spatial and temporal variability which would be expected. Thus, when using the routing at high resolution within regional Earth system models the criteria for selecting the time step might need to be revisited. In particular when moving to convection permitting resolutions when the intensity of simulated rainfall will modify the behaviour of the land surface model and thus the dynamics of the fluxes

490   which feed river flows. It is nevertheless reassuring to see in the analysis presented above that for higher resolutions a margin exists for the time step.

Once reliable km-scale atmospheric forcing are available the numerical analysis presented here should be revisited with a particular attention to flood events in small catchments. It will allow to evaluate at which stage a smaller quantile in the residence time should be selected and how important this choice is for representing the extreme hydrological events we are

495   interested in.
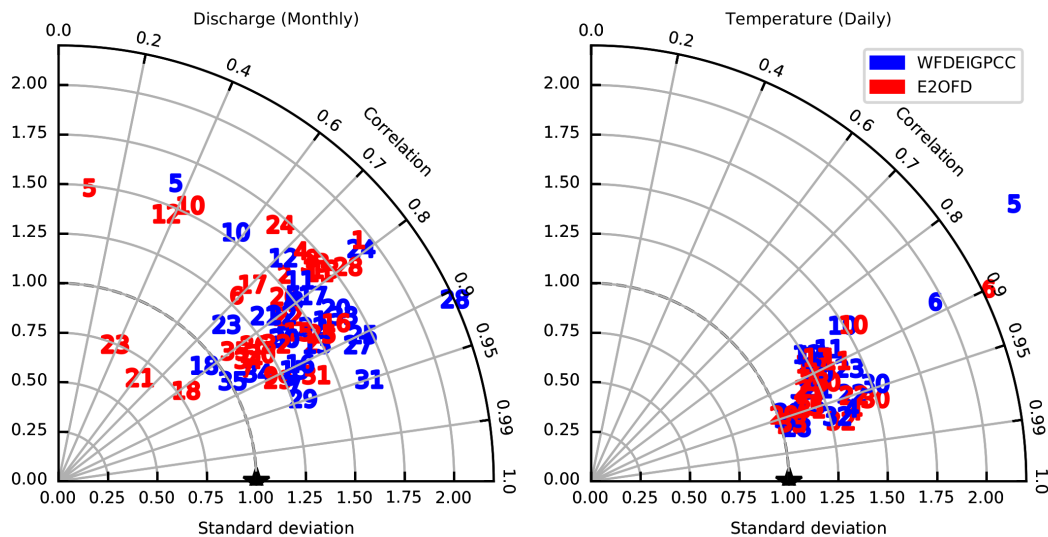
Figure 11. Taylor diagrams comparing observed and simulated monthly discharge and daily stream temperature to observations available at the 35 stations listed in Table A1. The numbers indicated in the figures correspond to those in the table.

6 Validation of the routing scheme in ORCHIDEE

In order to appreciate the importance of the numerical choices presented above, the routing scheme is evaluated jointly with ORCHIDEE at two different resolutions but only using the MERIT HDEM. WFDEI and E2OFD (Marthews et al., 2020) are two state of the art atmospheric forcings for land surface models both based on the ERA-I re-analysis (Weedon et al., 2014). With the advent of higher resolution precipitation products it was decided to interpolate WFDEI to the MSWEP (Beck et al., 2017) grid (0.25°) and use it to bias correct rainfall from the re-analysis. Thus the two driving data are not only available on different atmospheric grids but also differ in the precipitation intensity and spatial distribution. The WFDEI version which was bias corrected with GPCC (Becker et al., 2013; Schneider et al., 2014) is used here.

Figure 11 shows on a Taylor diagram the quality of the simulated discharge when compared to observations at the 35 stations presented in appendix A. For discharge, the database of GRDC (Fekete et al., 2000) (http://grdc.bafg.de) is used. It has been enhanced with national sources of information for a number of European countries. The stream temperatures were obtained through the GESM database (United Nations Environment Programme, 2017) (https://gemstat.org/). The diagnostics are computed with the available observations over the period 1983-2002.

For discharge these results are well in-line with previous validations of ORCHIDEE (Ngo-Duc et al., 2005) and the experience gained during the data assimilation experiments performed (Wang et al., 2018). The discrepancies between the models in the Euro-Mediterranean region can be attributed to missing processes in the land surface model. In this region in particular, human management of surface water is missing as it has not yet been included in the version of the model used here (Zhou

et al., 2021). The differences between both simulations are of more interest here. Based on the analysis above, we know that if the forcing are the same, the correlation of discharge is better than 0.9 (except for stations 10 and 11) and the ratio of standard deviation is close to 1. These metrics can be transferred to the Taylor diagram to see that the difference in disagreement of both simulations with observations cannot be explained by the numerical scheme. This confirms that the difference of imposed atmospheric conditions is the dominant cause of differences in behaviour of the model (Marthews et al., 2020).

More original for ORCHIDEE is to verify the quality of the simulated stream temperature. The Taylor diagram might give the reassuring impression that the relatively simplistic model used here for temperature is satisfactory. First and foremost we have to remember that stream temperature is less affected by water management than water levels. The temperature in streams is driven by the seasonal cycle of its values over land surfaces and thus the temporal correlations can be expected to be high. On the ratio of standard deviation it can already be noted that the amplitude of the stream temperature is overestimated with the simple model proposed here. The stations of Porte du Scex and Diepoldsau (Stations 5 and 6 respectively) are outliers and will be considered in more detail in the next section.

To better understand the qualities and limitations of the simple temperature scheme proposed here let us examine two stations with a large upstream area and an excellent observational record : Lobith on the Rhine and Nagymaros on the Danube (Stations 31 and 32 respectively). These stations where also used as validation points by models which attempt to incorporate a much wider set of processes governing stream temperature (van Vliet et al., 2012; Tokuda et al., 2019; Liu et al., 2020). One notes that on the Rhine the model has a systematic cold bias (Figure 12). Because of the strongly underestimated winter temperatures $(-5\,K)$, the amplitude of the annual cycle is too large. On the Danube the annual cycle of temperature is closer to observations, in particular in summer. But again, the strong cold bias in winter exaggerates the amplitude of the annual cycle. The underestimated winter temperatures is something which was also found in the HEAT-LINK model on the Danube (Tokuda et al., 2019) while the VIC model (van Vliet et al., 2012) had stream temperatures for the Rhine which were overestimated in winter. Another striking feature is that all three models predict a too rapid cooling of the rivers in autumn.

Figure 13 confirms that this diagnostic is valid over the 25 stations with a temperature record and is general over the region. The two reference simulations show a systematic underestimation of stream temperature in winter and relatively reliable summer values. These biases do not depend on the size of the catchment and are larger than the differences between the forcing data. Thus there is room for improvement. It has to be remembered that the soil temperatures over the top $0.3\,m$ are essentially driven by the land surface temperature (LST) simulated by ORCHIDEE. This variable is well known to be affected by modelling assumptions and errors in the driving data (Huntingford et al., 2000). Previous studies have shown that reproducing remote sensed LST in land surface models is challenging (Barella-Ortiz et al., 2017).

Given that our approach is relatively simple, it is feasible to better understand the origin of these biases in the simulated annual cycle of stream temperature.

6.1 Sensitivity of the stream temperature to model assumptions

Stream temperature is determined by two fundamental drivers :
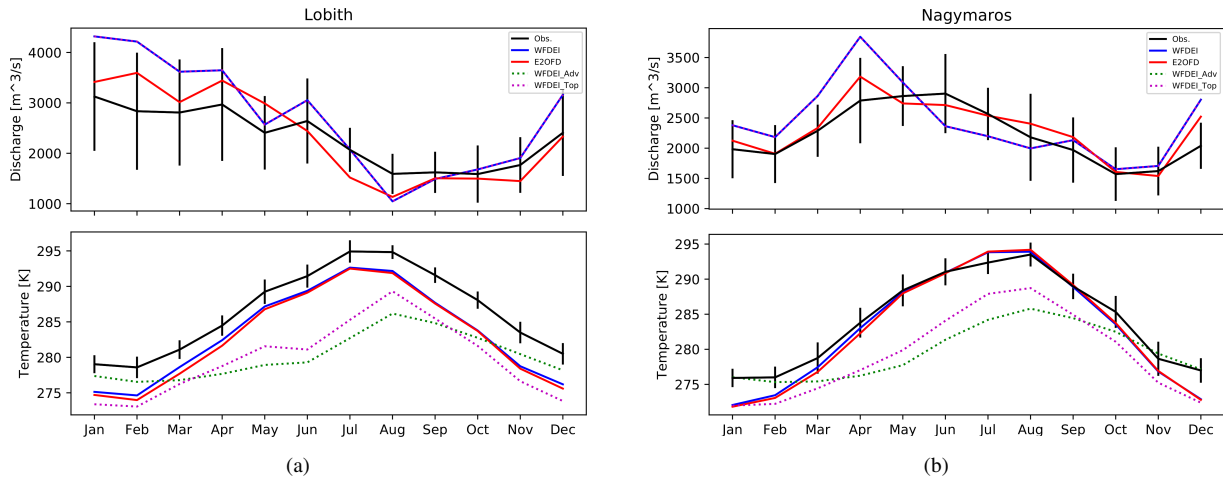
Figure 12. Mean annual cycle of monthly mean river discharge and temperature at the Lobith station on the Rhine and Nagymaros on the Danube. For the observations the inter-annual variability of the monthly values is displayed as error bars. The two reference configurations (WFDEI and E2OFD) are drawn with plain colors while the two sensitivity experiments carried out with WFDEI are given as dotted lines.

- the temperature at which the water leaves the ground and often referred to as headwater temperature. For instance, van Vliet et al. (2012) compared an empirical relation for the headwater temperature with the case when daily soil temperature is chosen, without specifying at which depth. Tokuda et al. (2019) use the temperature of runoff water without specifying how it is estimated in MATSIRO (Takata et al., 2003). Here it is proposed to add to this boundary condition the distinction between temperature of surface runoff and deep drainage temperatures (Section 2.2).

- The energy gained by the stream through interaction with the atmosphere and the landscape as it flows to the ocean. These processes are represented with great detail in some models like HEAT-LINK and VIC. Here they are simplified to a very basic relaxation towards top ground temperature and thus a variable closely related to LST.

Separating these two factors in the deficiencies of the models is key to future developments of the scheme so that errors in the assumptions for the boundary conditions are not compensated by biases in the interactions of the river with the landscape and atmosphere.

To determine the largest source of error in the simulated stream temperature two sensitivity experiments are carried out with the WFDEI configuration in which the interaction with the atmosphere and landscape are suppressed by setting $a = 10^5$. This means that the relaxation term only serves its numerical purpose as it is different from zero only when the HTU water levels tend to zero. The two experiments proposed here are :

WFDEI_Adv Runoff and drainage have the temperatures as defined in Section 2.2.

WFDEI_Top Both water fluxes leaving the soil moisture scheme have the temperature of the top soil layers $(0 - 0.3\,m)$.
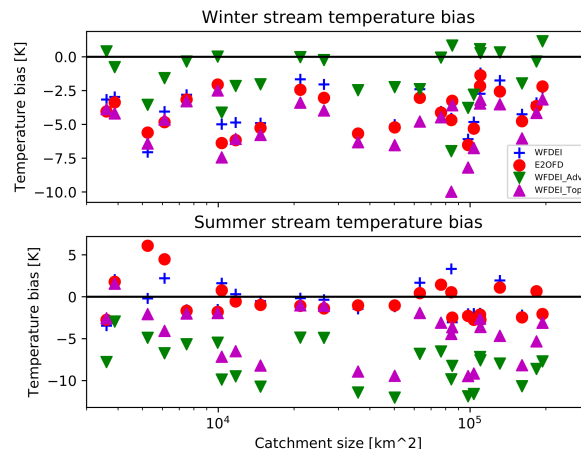
Figure 13. Seasonal biases at 25 stations where stream temperature is available for the two reference simulations (blue + symbols DEI and red dots for E2OFD) and for both sensitivity experiments (green downward triangles for the pure advection of both temperatures and purple upward triangles for top temperature advection).

The fact that the interaction with the atmosphere and landscape is suppressed in both these experiments leads to a strong underestimation of the summer stream temperature (Figure 13). The two largest stations on the Danube and Rhine (Figure 12) show that without the additional energy brought to the stream by the environment the amplitude of their annual cycle is much lower. When the near surface temperature is used for both runoff and drainage (WFDEI_Top), the amplitude increases slightly but it is still not at the correct level. Figure 13 shows that this result is valid for all catchment sizes. The differences between WFDEI and WFDEI_Adv do not systematically increase as the stations have a larger catchment. A conclusion which can be drawn at this stage is that if rivers only obtain their temperature from the headwaters they do not warm-up enough in summer. This demonstrates the importance of the exchanges with the atmosphere and landscape during this season. The relaxation to the top soil temperature used here is just a simple transfer of the energy balance performed within ORCHIDEE to the streams. In view of the importance of this process a more complete representation of these exchanges should be aimed for. This includes the simulation of lake thermodynamics (Bernus and Ottlé, 2022). It also explains why simple empirical relations relating near surface air temperature and stream temperature work so well (Ducharne, 2008).

More interesting for the model development is the dependence of the winter temperature bias on the assumption made for the headwater values. Figure 13 shows that the case when drainage has the deep soil temperature and no atmospheric interaction is allowed (WFDEI_Adv) the results are more realistic. In this region, winter is the period when the flows are dominated by the groundwater contribution in mountain catchments. Attributing to drainage the warmer deep soil temperature in this season is a step in the right direction. This is corroborated by the fact that the two stations where the winter errors are the largest (Port du Scex on the Rhone and Diepoldsau on the Rhine), and which are upstream of major lakes, are at the outflow of the Alps. In these topologically complex regions the contribution of groundwater to the low flows is particularly important (Floriancic et al., 2019). Rain and melt water from the previous season transits through deep aquifers before reaching the rivers at the

bottom of the valley. It has also to be considered that the rivers flowing out of the Alps are affected by hydropower generation. This has been shown to significantly warm the streams in winter (Fette et al., 2007).

585   It is expected that in winter the interaction with the landscape and the atmosphere will cool streams as they are warmer than their environment. This is also what is found here when comparing WFDEI and WFDEI_Adv. Thus, in order to have simultaneously the correct interaction with the atmosphere and correct headwater temperature, the drainage temperature should be warmer than the $3 - 17m$ assumed here. The comparison with WFDEI_Top shows that when cooler near surface soil temperatures are used the streams are indeed colder, even without atmospheric interactions. This reveals a strong limitation of

590 the routing scheme proposed here. As we do not represent well ground water, we do not know its depth or its residence time at different horizons. Thus its temperature when it emerges at the surface cannot be correctly established. As wintertime cold bias is also present in the mid-latitude basins reported by Takata et al. (2003) and they have assumed initial temperature to be that of runoff, the cause is probably the same as in our configuration. This highlights the importance of temperature to validate the groundwater component simulated in land system models.

595   In the Alpine region, winter stream temperatures have been shown to warm more slowly than in other seasons (Michel et al., 2020). As it is attributed to groundwater processes, land system models will need to better simulate this slower component of the aquifer in order to be able to reproduce the observed trends in stream temperature and predict future evolution when coupled to ESM.

7   Discussion and conclusion

600 This paper proposes a methodology to decompose any atmospheric grid into a graph of hydrological Transfer Units (HTU) based on a digital elevation model which includes flow directions (HDEM). This network allows to perform a hybrid routing which combines a vector-based with a grid-based approach (Yamazaki et al., 2013). It combines the water balance simulated on the atmospheric cells with the higher hydrological resolution needed to predict the horizontal transfers at the surface.

    The algorithm introduces a truncation parameter which determines the maximum number of HTU as chosen by the user.

605 This allows for applications which do not require all the hydrological details of river flows to reduce the memory consumption of their land surface model by specifying a lower number of sub-grid elements. With a statistical sampling of random river segments the error introduced by the aggregation of the HDEM information at the HTU level is quantified. We recommend to use a truncation which reduces the total average error of the segments to the cell level error. This ensures that the graphs are correctly connected and minimizes the topological error. The optimal truncation will depend on the resolution of the

610 atmospheric grid and the HDEM used.

    The graphs of HTU would be useless if the water continuity equation could not be solved with a reasonable time step. We propose to use the 25% quantile of the area weighted residence time as an optimal time step for the routing scheme. This ensures that 75% of the HTUs by area are numerically stable. It yields a time step which is compatible with the one of the land surface model. We find that the time step varies more with the spatial resolution of the atmospheric grid than the truncation

615 of the graph. For the four resolutions tested it is equal or larger as the one typically used for ORCHIDEE when coupled to

the atmosphere. The time step can probably be increased if the continuity equation on the sub-grid part of the graph is solved implicitly. This would increase the computational efficiency of the routing scheme as it could be called less frequently by the land surface scheme.

Any routing scheme will have adjustable parameters in order to determine the residence time in the aquifers and surface reservoirs. ORCHIDEE has one parameter per reservoir represented in the transport scheme. We find that changing the resolution of the atmospheric grid or the truncation does not require to readjust these parameters. The simulated discharge is not affected in any significant way by the resolution changes. Tests comparing two km-scale HDEMs also show that the parameters were largely independent of the hydrological information used to build the HTU graph. This is a very important result as it means that the routing scheme can be used over a large range of configurations of the ESM without having to be adjusted. Thus expertise can be transferred from one resolution to the other. Our hypothesis is that the repartition between surface runoff and drainage of excess water in the soil moisture reservoir is the main driver for the optimal values of the parameters. Thus as the representation of the unsaturated soils evolves in ORCHIDEE the parameters of the routing scheme will have to be verified.

To demonstrate the value of the hybrid routing scheme on a graph of HTU a simple temperature transport scheme is implemented. It is remarkable that it produces results comparable to much more elaborated schemes. We attribute this to the fact that in summer the energy balance over open water is relatively close to the one simulated by ORCHIDEE and thus a simple relaxation is a good first approximation. More importantly, the simplicity of the scheme allows to reveal the reason for the poor performance in winter which is also found in more complex models. During this season the bias is caused by the boundary condition of the temperature scheme. The water appears not to stay long or deep enough in the ground in order to reach the streams with a sufficiently high temperature. It points to a limitation of the groundwater representation in the current formulation of the routing scheme rather than the temperature scheme.

This demonstration of the numerical robustness of the hybrid routing scheme of ORCHIDEE is an excellent starting point for future developments. Schrapffer (2022) shows how the elevation information within the HTU can be used to predict their flooding and overflow into neighbouring HTUs. This allows to represent the functioning of fluvial floodplains and their contribution to evaporation and vegetation functioning within ORCHIDEE.

Lakes, artificial reservoirs or dams can be placed onto the HDEM. During the construction phase of the HTUs this information can then be transferred and aggregated to the level of the hybrid routing scheme. It can then be used to predict water volumes and functioning of these hydrological elements. This can then be combined with the lake energy balance model (Bernus and Ottlé, 2022) in order to represent consistently the lateral transport of water volumes and thermal energy over continents within ESMs.

The HTU graph can be enhanced with adduction networks. They link demand points like irrigated areas, power plants (for hydro power generation or cooling of other plants) or domestic needs to the most appropriate river. Should the demands not be satisfied locally they can be propagated upstream on the adjoint HTU graph so that water is released by the appropriate dam (Zhou et al., 2021). The proposed vision of lateral water transports within Earth system is an extremely powerful tool which will enable us to integrate in land surface models the impact of human water management on the hydrological system and predict its interaction with the climate.

The representation of deeper groundwater will need more attention in the future developments of ORCHIDEE as recommended by the community (Gleeson et al., 2021). We have noted that probably only a more realistic representation of groundwater transport will enable to correctly simulate temperatures and water quality parameters in areas with complex hydrogeological structures. It will have to be seen if a specific HTU graph taking into account the hydrogeology needs to be implemented or if a full three dimensional representation will be required (Maxwell and Miller, 2005).

Code and data availability. The code version and data used for this study are available at https://doi.org/10.5281/zenodo.7788209. The hydrological digital elevation models provided are a reformatted version of the data freely distributed here : http://hydro.iis.u-tokyo.ac.jp/~yamadai/MERIT_Hydro/ and urlhttps://www.hydrosheds.org/products/hydrosheds. The pre-processor for ORCHIDEE's routing scheme is an evolving code which can be followed on the GitLab server of the French research organisations : https://gitlab.in2p3.fr/ipsl/lmd/intro/routingpp

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Author contributions JP developped the code, designed and executed the numerical evaluations, AS contributed to the code development and evaluation, ED and OB contributed the temperature advection development, LR and JS evaluated the scheme during its development, XZ contributed to the code development and provided the MERIT HDEM, all co-authors discussed the methodology and contributed to the manuscript.

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Appendix A: Stations used for analysis

				Available observations	
Number	River	Station name	up-stream area $[km^2]$	Discharge	Temperature
1	Danube River	Hundersingen	2647.01	1983-2002	-
2	La Seine	Troyes	3410.00	1983-2002	-
3	Vechte	Vechterweerd	3600.00	-	1983-1995
4	La Seine	Mery-sur-seine	3880.00	1983-2002	1983-1996
5	Rhone	Porte Du Scex	5244.00	1983-2002	1983-2002
6	Rhine River	Diepoldsau, Rietbruecke	6119.000	1983-2002	1983-2002
7	Trent, River	Colwick	7486.00	1983-2002	1983-2002
8	La Seine	Pont-sur-seine	8760.00	1983-2002	-
9	Thames, River	Kingston	9948.00	1983-2002	1983-2002
10	Rhone	Chancy, Aux Ripes	10323.00	1983-2002	1986-2002
11	Aare	Brugg	11726.00	1983-2002	1983-2002
12	Rhine River	Rekingen	14718.00	1983-2002	1983-2002
13	Danube River	Ingolstadt	20001.00	1983-2002	-
14	La Seine	Montereau-fault-yonne	21178.00	-	1983-1996
15	La Seine	Saint-fargeau-ponthierry	26290.00	1999-2002	1983-1996
16	La Seine	Alfortville	30800.00	1983-2002	-
17	Rhine River	Basel, Schifflaende	35905.00	1983-1995	1983-2002
18	Guadiana	Badajoz	48530.00	1995-2002	-
19	Guadalquivir	Sevilla	48548.00	-	-
20	Rhine River	Maxau	50196.00	1983-2002	1985-1995
21	Duero	Fonfria	63160.00	1983-1995	1990-1995
22	Danube River	Achleiten	76653.00	1983-2002	1985-1995
23	Ebro, Rio	Tortosa	84230.00	1983-2002	1990-1995
24	Vistula	Warsaw	84945.17	1983-1990	1992-2002
25	Rhine River	Mainz	98206.00	1983-2002	1985-1995
26	Danube River	Korneuburg	101536.60	1996-2002	-
27	Rhine River	Kaub	103488.00	1983-2002	1985-1995
28	Oder River	Hohensaaten-Finow Ap	109564.00	1983-2002	1992-2002
29	La Loire	Montjean-sur-loire	109930.00	1983-2002	1983-1996
30	Danube River	Bratislava	131331.00	1983-2002	1995-1995
31	Rhine River	Lobith	160800.00	1983-2002	1983-1995
32	Danube River	Nagymaros	183533.00	1983-1999	1983-1996
33	Vistula	Tczew	193922.91	1983-2002	1992-2002
34	Danube River	Pancevo	525009.00	1983-2002	-
35	Danube River	Ceatal Izmail	807000.00	1983-2002	-

Table A1. Stations used for the evaluation of the numerical stability and quality of the simulated discharge and stream temperature.