

Assimilation of sea surface salinities from SMOS in an Arctic coupled ocean and sea ice reanalysis

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1 **Abstract**

2 In the Arctic, the [Sea Surface Salinity](#) (SSS) plays a key role in processes related to
3 water mixing and sea ice. However, the lack of salinity observations causes large
4 uncertainties in Arctic Ocean forecasts and reanalysis. Recently the Soil Moisture and Ocean
5 Salinity (SMOS) satellite mission was used by the Barcelona Expert Centre to develop an
6 Arctic SSS product. In this study, we evaluate the impact of assimilating this data in a
7 coupled ocean-ice data assimilation system. Using the Deterministic Ensemble Kalman filter
8 from July to December 2016, two assimilation runs respectively assimilated two successive
9 versions of the SMOS SSS product, on top of a pre-existing reanalysis run. The runs were
10 validated against independent in-situ salinity profiles in the Arctic. The results show that the
11 biases and the Root Mean Squared Differences (RMSD) of SSS are reduced by 10% to 50%
12 depending on [the area](#), and highlight the importance of assimilating satellite salinity
13 data. The time series of Freshwater Content (FWC) further shows that its seasonal cycle can
14 be adjusted by assimilation of the SSS products, which is encouraging [to assimilate SSS](#) in a
15 long-time reanalysis to better reproduce the Arctic water cycle.

16
17 **Keywords:** Arctic Ocean; Sea Surface Salinity; FWC; SMOS;

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21 **1. Introduction**

22 The Arctic Ocean is undergoing a dramatic warming, resulting in the loss of sea ice
23 documented by previous studies (e.g., Johannessen et al., 1999; Stroeve and Notz, 2018).
24 Sea ice melt contributes freshwater to the Arctic Ocean, together with precipitation and river
25 flux, and has far-reaching effects on the Arctic Ocean environment (Carmack et al., 2016).
26 The Arctic observing system, compared to other oceans, lacks the capability to provide a
27 complete picture of ocean salinity, particularly because of obstruction by sea ice. A complete
28 reconstruction of Arctic environmental variables thus requires a data assimilative numerical
29 model capable of propagating information below sea ice during the winter as practiced by
30 ocean operational forecast systems (such as Dombrowsky, 2009; Fujii et al., 2019). As with
31 other ocean data assimilation (DA) applications, Arctic reanalysis products of ocean and sea
32 ice play an important role in understanding climate change and its mechanisms. In recent
33 years, many studies (e.g., Storto et al., 2019; Uotila et al., 2019) evaluated the quality of the
34 Arctic reanalysis products and recommended experiments to maximize the usefulness of
35 new observations, as done by Kaminski et al. (2015) and Xie et al. (2018). However, there
36 are no impact studies of salinity observations in the Arctic to our knowledge.
37 Ocean salinity has been used to study the water cycle for the last 20 years (e.g., Curry et al.,
38 2003; Boyer et al., 2005; Yu, 2011; Yu et al., 2017). A recent review paper showed a
39 stabilization of the Freshwater Content (FWC) in the Arctic Basin, although observations
40 indicate that the Beaufort Gyre keeps getting fresher (Solomon et al., 2021). Salinity
41 variations have far-reaching implications for ocean mixing, water mass formation, and ocean
42 general circulation, but suffer from large uncertainties in the Arctic, mainly due to sparse
43 observations and the lack of a steady-state reference time period (e.g., Stroh et al., 2015; Xie
44 et al., 2019). Measuring Sea Surface Salinity (SSS) from passive microwave remote sensing
45 is a comparatively new but promising way to reduce the uncertainty in salinity. Launched in
46 November 2009, the Microwave Imaging Radiometer using Aperture Synthesis (MIRAS)
47 instrument of the European Space Agency's (ESA) Soil Moisture and Ocean Salinity (SMOS)
48 mission measures the brightness temperatures (T_B) of the sea surface at different frequency
49 bins. The passive 2-D interferometric radiometer on the satellite operating in L-band (1.4
50 GHz) is sensitive to water salinity and sufficiently free from electromagnetic interference
51 (e.g., Font et al., 2010; Kerr et al., 2010). Since May 2010, SMOS operationally provides
52 SSS records over the global ocean (Mecklenburg et al., 2012). During the last 12 years,
53 large improvements have been introduced in the SMOS data processing chain, increasing
54 the accuracy and coverage of the salinity data up to levels that were unthinkable at the
55 beginning of the mission (Martin-Neira et al. 2016, Olmedo et al., 2018; Reul et al., 2020;
56 Boutin et al., 2022).

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61 Furthermore, the assimilation of satellite-derived SSS products using an ensemble DA
62 method has been found to significantly improve the surface and subsurface salinity fields in
63 the tropics (Lu et al. 2016). The advantages of assimilating three SSS products from SMOS,
64 Aquarius (ref., Lee et al, 2012), and [the](#) Soil Moisture Active Passive Mission (SMAP; e.g.,
65 Tang et al., 2017) into a global ocean forecast system using [a](#) 3D-Var DA method have also
66 been demonstrated by Martin et al (2019). Their results show the benefits of assimilating
67 both the SMOS and SMAP datasets in the intertropical convergence zone in the tropical
68 Pacific. However, very few studies [have](#) investigated the impact of assimilating SSS products
69 in the Arctic or high latitudes. Since the beginning, [the](#) SSS retrieval from SMOS in cold
70 regions has been very challenging for three main reasons: i) the lower sensitivity of T_B [to](#)
71 [salinity](#) in cold waters [leads](#) to larger [errors](#), (Yueh et al., 2001; e.g. the sensitivity drops from
72 0.5 to 0.3 K PSU⁻¹ when sea surface temperature decreases from 15 to 5°C); ii) [land](#)-sea
73 and ice-sea [contaminations](#) resulting from abrupt changes of T_B values across these two
74 interfaces, combined with the large ground footprint of SMOS; iii) the requirement of a well-
75 observed steady-state period for the removal of biases. Addressing these challenges in the
76 SMOS salinity retrieval approach, Olmedo et al. (2017) introduced a non-Bayesian retrieval
77 method to [de-bias](#) the Level 1 baseline (L1B) salinity against the reference SSS from Argo
78 data ([Argo, 2022](#)). Level 1 data from the satellite is available within 24 hours, but the
79 additional processing steps require high-quality auxiliary data so [Level](#) 3 and 4 SSS are only
80 provided in delayed mode. Starting with the ESA L1B (v620) product from SMOS, the
81 Barcelona Expert Centre (BEC) released Version 2.0 of the Arctic gridded SSS product (25
82 km resolution; Olmedo et al., 2018). Xie et al. (2019) evaluated the V2.0 SSS product and
83 another gridded Arctic SMOS SSS product developed by LOCEAN (Boutin et al., 2018)
84 during the years 2011-2013. These two SSS [observation sets](#), together with an Arctic
85 reanalysis (Xie et al., 2017) and one objective analysis product ([Greiner et al., \(2021\)](#)
86 [describe an updated version of this product](#)), were validated against in-situ observations and
87 compared with two climatology datasets: the World Ocean Atlas of 2013 (WOA2013, Zweng
88 et al., 2013) and the Polar science center Hydrographic Climatology (PHC 3.0, Steele et al.,
89 2001). They found considerable discrepancies among the different gridded SSS products,
90 especially in the freshest seawater (<24 psu). The intercomparison of these Arctic SSS
91 products shows room for improvement of the SMOS-based SSS in the Arctic.
92 [Recently](#), under the framework of the ESA project Arctic+Salinity (AO/1-9158/18/I-BG), and
93 further development of the non-Bayesian scheme (Olmedo et al., 2017), the effective
94 [resolution](#) of SSS data [was](#) enhanced both in space and time (Martínez et al., 2022). The
95 new version of the SSS product (V3.1) [has](#) the capability to monitor mesoscale structures
96 and river discharges (e.g., Martínez et al., 2022). This new product provides daily maps

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114 (Level 4) of 9-day averages in the Arctic on a regular 25 km grid and covers a longer time
115 period 2011-2019, and are released through the BEC portal (<http://bec.icm.csic.es/> and also
116 at DOI: [10.20350/digitalCSIC/12620](https://doi.org/10.20350/digitalCSIC/12620); last accessed May 2022). The major differences in the
117 estimation of the two SSS products (V2.0 and V3.1) are detailed in the Algorithm Theoretical
118 Baseline Document (ATBD) of the Arctic+Salinity project (Martínez et al., 2020). Figure 1
119 shows that in comparison to V2.0, V3.1 provides wider coverage in the marginal seas around
120 the Arctic and is also fresher as indicated by the 26 psu isoline.

121 The two successive versions of the BEC SMOS SSS products are assimilated into the
122 TOPAZ Arctic reanalysis system (detailed in Section 2) during the summer of 2016. These
123 two assimilation runs are compared to the Arctic reanalysis without assimilation of satellite
124 SSS data which is identical to the product ARCTIC_REANALYSIS_PHYS_002_003 in the
125 Copernicus Marine Services. The model validation against independent observations
126 presents the differences stemming from these two SSS products, although they are from the
127 same initial data source (SMOS). Their impact on the assimilation in the Arctic coupled ice-
128 ocean model shows large differences, thereby motivating further efforts to improve SSS
129 retrievals in the cold Arctic.

130 The paper is organized as follows: Section 2 ~~briefly~~ describes the coupled ocean and sea ice
131 data assimilation system and the assimilation experiments; Section 3 describes the in-situ
132 observations and the validation metrics; results presented in Section 4 include the validation
133 using independent SSS observations, separated into different ocean basins. Section 4 also
134 examines the impact of SSS assimilation on the weekly increments of other related variables
135 near the surface, and explores the integrated effect on the freshwater simulated by the
136 model. In Section 5, the findings of this study and future perspectives are summarized.

138 2. Assimilation system and experimental design

139 2.1 The Arctic ocean and sea-ice coupled data assimilation system

140 TOPAZ is a coupled ocean and sea ice data assimilation system, built using the
141 Deterministic Ensemble Kalman Filter (DEnKF; Sakov et al., 2012) to simultaneously
142 assimilate multiple types of observations for the ocean and sea ice (Xie et al., 2017). The
143 ocean model in this system uses version 2.2 of the Hybrid Coordinate Ocean Model
144 (HYCOM; Chassignet et al., 2003) with a low-distortion square grid ~~at~~ a horizontal resolution
145 of 12-16 km. The river discharge input is climatological, using the ERA-Interim (Dee et al.,
146 2011) runoffs channeled in a simple hydrological model, which tends to underestimate the
147 amplitude of the seasonal cycle and thus ~~produces~~ a saline bias at the surface (Xie et al.
148 2019). The coupled sea ice model uses a single-category thermodynamic model (Drange

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151 and Simonsen, 1996) and dynamics by the modified elastic-viscous-plastic rheology
 152 (Bouillon et al., 2013) from an early version of the CICE model (Lisæter et al. 2003). The
 153 model covers the Arctic Ocean and the whole north Atlantic Ocean (shown in Fig. 1 in Xie et
 154 al., 2017). A seasonal inflow of Pacific Water is imposed across the Bering Strait, based on
 155 observed transports (Woodgate et al., 2012). At all lateral boundaries, the temperature and
 156 salinity stratifications are relaxed to a climatology combining version 2.0 of WOA2013 and
 157 version 3.0 of PHC with a 20-grid cells buffer zone. To avoid a potential model drift, the
 158 surface salinity is relaxed to the combined climatology as mentioned above, with a 30-day
 159 timescale, but the relaxation is suppressed wherever the difference from climatology exceeds
 160 0.5 psu to avoid the artificial formation of bulk surface freshwater layers.

161 For simplification, the two steps of the assimilation system can be translated by the
 162 following concept expressions (update and model propagation):

$$163 \quad \mathbf{X}_a = \mathbf{X}_f + \mathbf{K}(\mathbf{y} - H\mathbf{X}_f) \quad (1)$$

$$164 \quad \mathbf{X}_f = M(\mathbf{X}_a) \quad (2)$$

165 Where the matrix \mathbf{X} represents the model state with all 3-D and 2-D variables needed by
 166 the model forward integration, represented by the operator M . The subscripts 'a' and 'f'
 167 respectively indicate the analyzed model state obtained through optimization after DA and
 168 the model forecast. The vector \mathbf{y} is composed of the quality-checked observations during the
 169 weekly cycle, and the observation operator H gives the model equivalent of the observations.
 170 The innovation term (in parentheses in Eq.1) represents the differences between the model
 171 and the various observations in the observation space.

172 For the ensemble data assimilation method, the matrix \mathbf{X} includes the dynamical members
 173 of the model states as different columns and further evolves according to Eqs. 1 and 2 as
 174 described in the DEnKF. The TOPAZ model runs an ensemble of 100 members. The \mathbf{K}
 175 matrix (Kalman gain) is calculated using the ensemble covariance matrix. Like other square
 176 root versions of the Ensemble Kalman Filter, the DEnKF splits Eq. 1 into two steps: the \mathbf{K}
 177 calculation is applied to the ensemble mean, and the anomalies are updated to match a
 178 target analysis covariance (more details in Sakov et al., 2012). Using a 7-day assimilation
 179 cycle, we use the DEnKF to assimilate different types of ocean and ice observations,
 180 including along-track sea level anomaly (SLA), sea surface temperature (SST), in-situ
 181 profiles of temperature and salinity, sea ice concentrations (SIC) and sea ice drift products all
 182 sourced from the Copernicus Marine Environment Monitoring Services (CMEMS;
 183 <https://marine.copernicus.eu>). The same TOPAZ system provides a 10-day forecast of ocean
 184 physics and biogeochemistry in the Arctic (Bertino et al., 2021) every day via the CMEMS
 185 portal.

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2.2 Assimilation experiments and the observation error estimate for SSS

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$$E_{SSS} = \max \left\{ E_{int}, \left[0.6 + \frac{6}{1 + \exp\left(\frac{SSS - 16}{5}\right)} \right]^2 \right\} \quad (3)$$

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3. In-situ SSS observations for validation

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247 All in-situ salinity profiles were collected from various repositories and cruises (as shown in
248 Fig. 2). Salinity measurements were extracted near the surface over the Arctic domain during
249 the experimental time period. The sanity check procedures include: i) location check to
250 remove SSS observations in the model land mask; ii) omit the invalid profiles if the top depth
251 is deeper than 8 m; iii) remove redundant observations. Since the model does not reproduce
252 local gradients of the vertical salinity profiles shown in Supply et al. (2020), all the salinity
253 profiles are averaged over the upper 8 meters below the surface. This also avoids the loss of
254 the profiles that do not reach the surface.

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255 • *Data from the Beaufort Gyre Experiment Project (BGEP)*

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256 The BGEP has maintained an observing system in the Canadian Basin since 2003 and
257 provides in-situ observations over the Beaufort Gyre every summer. Although the BGEP has
258 maintained three bottom-tethered moorings since 2003, the shallowest depth of the
259 measured profiles for temperature and salinity is below 50 m. Hence, in this study, we only
260 use the Conductivity Temperature Depth (CTD) dataset from the cruise in 2016
261 (<https://www2.who.edu/site/beaufortgyre/data/ctd-and-geochemistry/>, last access: 14th
262 February 2022). SSS observations from these CTD profiles in the time period from 13th Sep
263 to 10th Oct 2016 are represented by the red triangles in Fig. 2.

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264 • *Data from Oceans Melting Greenland (OMG)*

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265 The project Oceans Melting Greenland was funded by NASA to understand the role of the
266 ocean in melting Greenland's glaciers. Over a five-year campaign, this project collected
267 temperature and salinity profiles by Airborne eXpendable Conductivity Temperature Depth
268 (AXCTD) launched from an aircraft (e.g., Fenty, et al, 2016). The deployed probe can sink to
269 a depth of 1000 meters, connected with a float by a wire. The measured temperature and
270 conductivity are then sent back to the aircraft. These salinity profiles collected during the first
271 OMG campaign in 2016 are downloaded from
272 https://podaac.jpl.nasa.gov/dataset/OMG_L2_AXCTD/ (last access: 10th February 2022). The
273 SSS from OMG distributed around Greenland, from 13th Sep to 10th Oct 2016 are shown as
274 the inverted blue triangles in Fig. 2.

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275 • *Data from the International Council for the Exploration of the Sea (ICES)*

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276 Salinity profiles were also obtained from the ICES portal (<https://www.ices.dk>). Shown as
277 blue squares in Fig. 2, the locations of the profiles during the last 6 months of 2016 are
278 dense in the Nordic Seas and restricted to north of 58°N for this study. Valid salinity profiles
279 from ICES (last access: 9th February 2022) are obtained from 6th July to 23rd Nov in 2016.

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280 • *Data from other cruises at the Arctic Data Center (ADC)*

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284 Surface salinity observations from scientific cruises are obtained from the Arctic Data
 285 Center portal (<https://arcticdata.io/catalog/data>; last access: 17th Feb 2022). During the
 286 model experiment, the first relevant cruise in ADC was SKQ201612S which was operated by
 287 University of Alaska Fairbanks with the RV Sikuliaq. This cruise collected data from Nome,
 288 Alaska on 3rd September, to the northeast Chukchi Sea, and then back to Nome at the end of
 289 September 2016. The temperature and salinity profiles were collected by a Sea-Bird 911
 290 CTD instrument package. All measurements at each station were done both down- and up-
 291 cast ways. To produce water column profiles at each station, the down-cast data were
 292 binned at 1 m intervals (Goñi et al., 2021). Besides the CTD profiles of SKQ201612S, more
 293 seawater samples were collected via the surface underway system on the RV Sikuliaq.
 294 Through a sea chest below the waterline (e.g., 4-8 m), the uncontaminated seawater was
 295 pumped into the ship and the corresponding filtration system supplies samples every 3 hours
 296 to the sensors (More details in Goñi et al., 2019). These SSS observations were obtained on
 297 the 9th-27th of September, indicated as blue crosses in Fig. 2.

298 Moreover, SSS measurements were also collected from the Seabird CTD on board Sir
 299 Wilfrid Laurier (SWL), but only in July 2016. This cruise is part of the annual monitoring from
 300 the Canadian Coast Guard Service (Cooper et al., 2019). The SSS observations are
 301 obtained near the Bering Strait close to the Pacific boundary of our model.

302 After filtering the diurnal signals by daily averages in observed surface salinity, all valid SSS
 303 measurements from the above data sources are compared with the daily average SSS of the
 304 three assimilation experiments listed in Table 1. The model data has been collocated with
 305 the observations for validation. To estimate the forecast differences to observations, we use
 306 the standard statistical moments:

$$Bias = \frac{\sum_{i=1}^N \sum_1^{O_i} (H\mathbf{X}_i - \mathbf{y}_i)}{\sum_{i=1}^N O_i} \quad (4),$$

$$MSD = \sqrt{\frac{\sum_{i=1}^N \sum_1^{O_i} (H\mathbf{X}_i - \mathbf{y}_i)^2}{\sum_{i=1}^N O_i}} \quad (5),$$

309 Where i is the i th day, O_i represents the number of observations on this day, and N
 310 represents the total number of days depending on the source of observations. Then \mathbf{X}_i
 311 represents the model daily average of the ensemble mean at the observation time, H is an
 312 operator to extract the SSS simulation from the model at the observed location. The model
 313 performance can then be quantitatively compared between the three assimilation runs.
 314 In addition, we further introduce a two-sample Student's t-test to evaluate the significance of
 315 the change of SSS bias in ExpV2/ExpV3 with respect to Exp0. Compared to in-situ
 316 observations, the SSS misfits in Exp0 are the error array \mathbf{e}_1 . The corresponding error array

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330 from ExpV2 or ExpV3 is called \mathbf{e}_2 . Thus, considering the null hypothesis H_0 : \mathbf{e}_1 and \mathbf{e}_2 are
331 the means of indiscernible random draws, the t-value can be calculated as follows:

$$t = \frac{|\mathbf{e}_2 - \mathbf{e}_1|}{\sqrt{s_1^2/(n_1 - 1) + s_2^2/(n_2 - 1)}}$$

332
333 Where s_1 (s_2) is the standard deviation in the \mathbf{e}_1 (\mathbf{e}_2), and n_1 (n_2) is the number of observations.
334 For every t-value, the p-value from the above equation is the probability that random errors
335 would prove H_0 wrong. Low p-values (<0.05) indicate that the change of bias due to
336 assimilation is significant.

337 4. Results

338 4.1 Diagnosing using assimilation statistics

339 The SSS innovations in the two assimilation runs of ExpV2 and ExpV3 are compared in Fig.
340 3, together with the number of assimilated SSS observations and the ensemble spread
341 3, together with the number of assimilated SSS observations and the ensemble spread
342 calculated by the ensemble standard deviation. The total number of observations is at its
343 maximum in September when the sea ice cover is minimal. Since both versions of the SSS
344 product share the same time frequency (9-day average) and gridded format, the number of
345 assimilated observations in the two runs reached a maximum in the middle of September
346 (gray lines in Fig. 3). But the maximal number of SSS in ExpV3 shows higher than in ExpV2.
347 For ExpV2, the Root Mean Square (RMS) of the SSS innovation varies between 0.4 and 1.2
348 psu, but the mean of SSS innovation, calculated as the observation minus the model
349 simulation (cf. the bracket in Eq.1), shows a saline bias of 0.4 psu, highest in September.
350 However, in ExpV3 the salinity bias quickly disappears after a few data assimilation cycles.
351 The RMS of the SSS innovation is larger in ExpV3 between 0.6 and 1.6 psu, which can partly
352 be explained by the higher effective resolution of the V3.1 product and the double penalty
353 effect. In ExpV3, the RMS of the SSS innovation (the red line) jumps down after the first SSS
354 assimilation step. The RMS of SSS innovations and the observation errors both decrease
355 from summer to winter, following a seasonal cycle as the areas of fresher water get gradually
356 ice-covered. The domain-averaged observation errors are only slightly larger in ExpV3 than
357 in ExpV2, as explained above, and the RMS of SSS innovations becomes lower than the
358 observation errors near the end of the run, which indicates that the observation errors for the
359 V2.0 SSS have been overestimated.

360 In the top panels of Fig. 4, the SSS maps are shown for the control run (Exp0) in August and
361 September 2016, respectively. For Exp0 in August, low salinity waters are found in the
362 Beaufort Sea near the Mackenzie River and along the East Siberian coast. In September, the
363 fresher waters, below 30 psu, bridge the two areas in Exp0 probably due to sea ice melt,

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371 although the lowest salinity near the Siberian coast remains unchanged from August to
372 September (as indicated by the 28 psu isoline). Compared with the SSS observations from
373 SMOS (Fig. 1), these two low salinity waters are clearly underestimated in Exp0. Meanwhile,
374 the relatively saline 32 psu isoline crosses both the Eurasian basin and the Baffin Bay. In the
375 Laptev Sea, due to the significant effects of river runoff and ice melt, the salinity shows a
376 strong gradient from the southeast to the northern part. During winter, the salinity increases
377 to 34 psu, and decreases in summer near to 30 psu (Janout et al., 2017). In the northwest
378 Laptev Sea, the saline tongue of 32 psu extends eastward to the Taymyr Peninsula (TP).
379 North of the TP, the Kara Sea freshwater meets with the Atlantic Water pathways from the
380 Fram Strait and Barents Sea (shown in Figure 1 of Janout et al., 2017). Close to the TP, the
381 observations at the mooring profiles in Janout et al. (2017) show much fresher surface
382 salinity (29 psu) than the subsurface salinity (32 psu) in summer. Compared to the SMOS
383 SSS maps (shown in Fig. 1), only the V3.1 product shows the 32 psu isolines around the TP.
384 Another difference between the two SMOS products arises in the Chukchi Sea where the
385 V3.1 product is more saline than both the V2.0 product and SSS in Exp0.

386 The middle and bottom panels of Fig. 4 show the SSS differences in August and
387 September 2016 between the SSS assimilation runs and the control run. Figure 4c and 4d
388 both show a freshening of the coastal areas in the Kara Sea, Laptev Sea, and East Siberian
389 Sea, but in ExpV3 the freshening is stronger and wider (Fig. 4e and 4f). In the Beaufort Sea,
390 ExpV2 mainly brings a local freshening near the mouth of the Mackenzie River in August,
391 which then spreads out along the coast in September. The freshening in the BS brought by
392 ExpV3 affects a broader area, even including the Canadian Archipelago. ExpV3 also
393 freshens the SSS on both sides of Greenland Island. From August onwards, the SSS in
394 ExpV3 freshens by over 1 psu along the whole east Greenland coast, which clearly does not
395 happen in ExpV2. In fact, the 32 psu isoline in ExpV3 (not shown) extends hundreds of
396 kilometers further to the South East Greenland coast in comparison to Exp0 and ExpV2. The
397 rest of the Greenland coast is also fresher by 0.5 psu in ExpV3 during both months. This is a
398 sign of a consistent change in the V3.1 product.

399 Even though most of the SSS assimilation leads to a freshening of the surface, a few
400 locations show higher salinity than Exp0, these are different from ExpV2 to ExpV3. For
401 example, the saline increment near the Bering Strait is larger in ExpV3 in excess of 1 psu,
402 consistently with the difference between the two remote sensing products (Fig. 1).
403 Other increases in SSS concern small areas near estuaries and are more common in ExpV3.
404 The increase to the west of the Yamal Peninsula can be explained by a model setup bias in
405 the location of the Ob river but compensated by the SSS assimilation. In the above

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412 comparisons of SSS maps, the central Arctic is not discussed, since the region is covered by
413 sea ice and the effect of assimilation is indirect.

414

415 4.2 Comparison with independent in-situ observations

416 Quality-checked in-situ observations in the Central Arctic are very unevenly distributed. After
417 pooling all platforms together, we further investigate the SSS misfits in six subregions of the
418 Arctic (Fig. 2 and Table 2). This section will present statistics of differences to independent
419 in-situ observations, separately considering marginal seas.

420

421 *Beaufort Sea (BS)*: Figure 5 shows the scatterplots of SSS in the three runs against in-situ
422 observations from BGEF, OMG, and ICES. In the Beaufort Sea (top panel in Fig. 5), the
423 observed SSS varies in a range of 26-29 psu. The range of SSS in Exp0 is much smaller,
424 between 29-31 psu with a saline bias of 2.6 psu and an RMSD of 2.7 psu, but otherwise, it
425 shows a reasonably linear relationship ($r=0.59$). The SSS bias in Exp0 has the same value
426 as in Xie et al. (2019), although estimated using the BGEF observations in a different time
427 period (2011-2013). The range of SSS in ExpV2 is slightly improved to 28-30.5 psu. Further,
428 the bias is reduced by 0.5 psu, corresponding to bias and RMSD reductions of respectively
429 13.5% and 10.5% with respect to Exp0. In ExpV3, the SSS range is much closer, between
430 26.5 and 30.5 psu, and the resulting bias and RMSD reductions of SSS are respectively
431 26.3% and 17.3% with respect to Exp0. Both the bias reduction in ExpV2 and ExpV3 relative
432 to Exp0 pass the significance test ($\alpha = 0.05$) through Student's t-test. Furthermore,
433 compared to [all in-situ SSS in BS](#) (top panels in Fig. 7), the SSS misfits in ExpV3 show a
434 stronger reduction by 26.0% for bias and 20.6% for RMSD. ExpV2 reduces these errors by
435 half as much (13.5% for bias and 11.5% for RMSD). These results clearly indicate that the
436 new version of the SSS is more beneficial for data assimilation in the Beaufort Sea.

437

438 *Chukchi Sea (CS)*: Fig. 6 shows the SSS deviations as a function of time during the SKQ
439 cruise route. Figure 6a shows the surface levels from CTDs. The saline bias (2.8 psu) is
440 more pronounced than in the Beaufort Sea, which we attribute to the proximity to the model
441 boundary in the Bering Strait, relaxed to climatological values, where the interannual
442 variability of Pacific water is not included. After assimilating SSS products, a reduction of the
443 bias is observed during September, by 15.5% in ExpV2 and up to 22.2% in ExpV3. The
444 comparison to underway surface water samples (Fig. 6b) also shows an error reduction of
445 around 15%, though fewer differences between ExpV2 and ExpV3.

446 Considering other cruise data in the CS (Fig. 7; bottom panels), the SSS in Exp0 shows
447 almost uniform values with a saline bias of about 2.3 psu and an RMSD of 2.6 psu. A recent

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449 observational study by Goñi et al. (2021) shows that the surface salinity of the CS during late
450 summer varies between 28-30 psu during the time period 2016-2017. The range of SSS
451 observations considered here is slightly broader (27-32 psu). The assimilation of SSS
452 products reduces the misfits (bias and RMSD). As in the BS, the SSS in ExpV3 has more
453 significant reductions in bias (17.7%) and RMSD (16.4%). After assimilation, the deviations
454 are in the same range as found in the BS. All the bias reductions in ExpV2 and ExpV3 are
455 significant compared to Exp0 through the t-test ($\alpha = 0.05$).

456

457 *Greenland Sea (GS)*: Most SSS observations around Greenland are from the OMG
458 programme, shown as the blue downward triangles in Fig. 2. Considering first all SSS
459 observations from OMG, the SSS misfits in the three runs (shown in the middle panels of Fig.
460 5) show smaller bias and RMSD than in the BS and the CS. However, the SSS in ExpV3 still
461 brings significant error reductions with a reduction of 32.6%/9.4% of the bias and RMSD
462 compared to Exp0. Notably, the SSS misfits in ExpV2 are almost identical to Exp0, which
463 indicates that the V2.0 SSS product was not informative there.

464 We now separate the evaluation in the East and West of Greenland covering the GS and
465 Baffin Bay (BB) areas as shown in Fig. 2 (also listed in Table 2). The top panel of Fig. 8
466 shows that [all](#) SSS observations [available](#) in the GS vary between 27 and 35 psu. This large
467 range includes fresh coastal waters, Arctic water, and Atlantic Water. The three assimilation
468 runs show different saline biases, especially for salinities lower than 30 psu. While in
469 observations the minimum salinity is below 28 psu, it only reaches 30 psu in ExpV3, and 31
470 psu in both Exp0 and ExpV2. As a result, the bias reduction in ExpV3 is over 50% and the
471 RMSD decreased by about 10.5% in the GS. ExpV2 is disappointingly similar to Exp0. This
472 is also the case in BB (shown in Fig. 8 bottom row), where differences between ExpV2 and
473 Exp0 are less than 0.02 psu. In contrast, ExpV3 reduces the SSS bias but does not
474 significantly reduce the RMSD in the BB. One possible explanation is the double-penalty
475 effect because the V3.1 product has a higher effective resolution than V2.0. This can be
476 seen in Fig. 8 as the ExpV3 values are more scattered.

477 Finally, we examine the SSS deviations in the Barents Sea and the Norwegian Sea. The
478 SSS bias and RMSD are the lowest in ExpV3 in Table 2, even though the reductions are not
479 as significant as in the area of fresher surface waters. Compared to the ICES observations
480 distributed in the North Atlantic and the Nordic Seas (blue squares in Fig. 2), the scatterplots
481 of Exp0 and ExpV2 are nearly identical (see the bottom panels in Fig. 5). The minimum
482 salinity in these two runs is 32 psu. The SSS bias and RMSD in both runs are also similar
483 (differences less than 0.01 psu). In contrast, lower salinity values are found in ExpV3, below
484 32 psu, although the saline bias remains around 0.5 psu on average. Notably, the SSS in

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486 ExpV3 shows that data assimilation can reduce the bias by 15% compared to Exp0, but the
487 RMSD only reduced about 0.03 psu, also possibly due to the double penalty effect. This also
488 suggests that the improvements near the coast will be the next challenge for future versions
489 of the SSS product.

490

491 4.3 Impact analysis of SSS assimilation

492 The above section has demonstrated that the assimilation of remote sensing SSS generally
493 improves the match to independent in-situ measurements, although the improvements are
494 location-dependent. Since large areas are void of in-situ measurements, the increment for
495 other surface variables will also be interpreted for understanding the impacts incurred. The
496 increments are the differences between the analysis and the forecast. The calculation of
497 them is the result of the innovations of all assimilated observations multiplied by the Kalman
498 gain, as computed in Eq. (1). Since the DEnKF update is multivariate, we present the impact
499 of the assimilation on other model variables closely related to the SSS: SST and SIC. Since
500 the only difference in the setting between the three runs is the assimilation of SSS, we can
501 attribute the differences to the impact of SSS observations. In theory, if both the model and
502 observations were unbiased, the increments of other assimilated variables should generally
503 decrease because of the presence of a new SSS term in the denominator of the Kalman
504 Gain (The ensemble covariance matrices contain off-diagonal blocks of correlation between
505 SSS and dynamically related variables and so the assimilated observations usually compete
506 with each other). However, the SSS biases originating either from the model or observations
507 also affect the other model variables and increase the innovations on the following
508 assimilation step and thus the consecutive increments. Hypothetically, wherever the forecast
509 errors are caused by SSS errors, the increments of other variables should diminish. Figure 9
510 compares the time-averaged increments of SIC and seawater temperature in the top 3-m
511 layer (considered as SST here) in the three runs. The sign of the increments remains overall
512 the same across the three experiments, both for SST and SIC. The SST increments in the
513 three runs are negative in the open ocean and positive near the ice edge, as shown in the
514 right column of Fig. 9.

515 The SST increments in Exp0 and in ExpV2 are nearly identical, but in ExpV3 there are few
516 areas such as in the Kara Sea and in the Laptev Sea where the SST increments have been
517 suppressed. These are locations where the SSS and SST are positively correlated, so the
518 updated SSS by assimilation is also helpful in reducing the water temperature misfits near
519 the surface. The changes in SST are however small with respect to the large SSS
520 differences in Figure 4. In Exp0, the SIC increments are small (<5%) inside the ice pack. The

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534 satellite SIC observations are assimilated every week and help to correctly position the ice
535 edge (Sakov et al., 2012). The increments exceed 5% along the ice edge, as can be seen in
536 the northern Barents Sea.

537 The assimilation of the V2.0 SSS product also shows minimal differences from Exp0 partly
538 because of the conservative sea ice mask in the V2.0 SMOS SSS. The SIC increments are
539 opposite to those of SST, showing that the assimilation warms the surface water where ice is
540 removed, which is consistent with Lisæter et al. (2003). Only minor differences between
541 ExpV2 and ExpV0 are visible along all areas swept by the ice edge during the 6-month
542 experiment, for example in the Kara Sea. In contrast, the assimilation of the V3.1 SSS
543 product shows larger changes in SIC increments than in ExpV2 with a broader area of
544 negative increments (removed ice) in the northern Barents Sea. This is not visibly related to
545 the SST increments but to the freshening caused by the assimilation of V3.1 SSS as SSS
546 and SIC are positively correlated in the northern Barents Sea, as shown by Fig. 2 in Sakov et
547 al. (2012). The increased SIC increments may be an indication that the SSS freshening could
548 be excessive.

549 Since the whole water column is updated by assimilation, the freshwater content is also
550 modified by the assimilation of SSS. There are however complex relationships between SSS
551 and FWC as shown by Fournier et al. (2020). The changes in FWC in the Arctic are
552 calculated as in Eq. (6) derived from Proshutinsky et al. (2009), although this method was
553 initially intended for the Beaufort Sea. Applying the same formula for interpolation of in-situ
554 observations, Proshutinsky et al. (2020) estimated the time-averaged summer freshwater
555 content in the Beaufort Gyre region in two time periods (1950-1980 and 2013-2018). In the
556 latter period, they located the FWC centre in the Beaufort Sea around (150°W, 75°N) and
557 drew the 20-m isoline over more than 5 degrees of latitude and nearly 30 degrees of
558 longitude on average. When compared to the earlier reference period, the FWC in the Beaufort Sea
559 Beaufort Sea has increased and its centre has shifted westward.

560 Following Proshutinsky et al. (2009), the model FWC in the Arctic is estimated as:

$$561 \quad FWC = \int_{z_0}^{z_{ref}} \left(1 - \frac{S(z)}{S_{ref}}\right) dz \quad (6)$$

562 Where the reference salinity value S_{ref} is taken at 34.8 psu, z_{ref} is the depth of the reference
563 salinity or the sea bed, and $S(z)$ is the salinity profile. Figure 10 shows the FWC on two
564 representative days, September 20th and October 20th, 2016. In Exp0, the reanalysis
565 reproduces the typical FWC distribution in the Arctic with a maximum in the Beaufort Sea.
566 The 20 m isolines in Fig. 10a and 10d show an increase in spatial coverage during October,
567 consistent with Rosenblum et al. (2021), but the 20 m isoline is not extending as far as 170°E
568 compared to Proshutinsky et al. (2020). After the assimilation of SSS products (either V2.0 or

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574 V3.1), the amplitude and the spatial distribution of the FWC maximum increase slightly in the
 575 [Beaufort Sea](#) (see Fig. 10b and 10c). A much larger increase of FWC appears on the East
 576 Siberian shelf and in the coastal areas of the Laptev Sea and eastern Kara Sea, although to
 577 a different extent in ExpV2 and in ExpV3. In the eastern Kara Sea, the FWC increases over a
 578 wider area in ExpV2 than in ExpV3. To the west of the Yamal Peninsula, ExpV3 shows a
 579 negative anomaly related to an incorrect location of the model river runoff, corrected in later
 580 versions of the model. The SSS assimilation is able to correct the related fresh bias. In the
 581 central Arctic, although the assimilated SSS measurements are masked by the sea ice
 582 cover, the FWC differences north of 84°N are more pronounced in October than in
 583 September, which indicates the advection of SSS increments by the Transpolar Drift Stream
 584 (Rigor et al., 2002; Balibrea-Iniesta et al., 2018). These results suggest that the SSS
 585 assimilation of both versions of SMOS satellite ~~based acts compensates~~ for the insufficient
 586 river summer runoff, ~~redistributes~~ the freshwater in the Arctic, and ~~adjusts~~ the freshwater
 587 budget. However, because of the limited in-situ data, the above assessment remains
 588 ~~preliminary~~.
 589 Further, we compare the daily time series of Arctic-averaged FWC from the three runs to the
 590 north of 70°N (Fig. 11). The FWC increases in October-November to reach its maximum, and
 591 gradually decreases thereafter. The impact of ~~the week-long~~ data assimilation cycles is
 592 visible as instantaneous jumps on the three curves of the time series, but the assimilation of
 593 SSS does not cause unrealistic imbalances. The FWC increases substantially due to SSS
 594 assimilation, by about 25 cm. Notably, the assimilation of version 3.1 SSS causes a faster
 595 increase during the first two months. Due to the absence of ground truth data in 2016, the
 596 above comparison ~~is not fully verified~~, but the timing of the peak is in better agreement with
 597 the ~~seasonal freshwater storage~~ presented by ~~the Ice-Tethered Profiler (ITP) data in Fig. 4a~~
 598 ~~of Rosenblum et al. (2021)~~. ~~In addition, we also notice that~~ the amplitude of the seasonal
 599 FWC seems too small in all experiments ~~in Fig. 11~~, which can be related to insufficient thick
 600 ice in TOPAZ (Uotila et al., 2019). More concrete evidence about the changed FWC will be
 601 provided when the longer assimilation of the satellite-based SSS product is finished in the
 602 near future.

603

604 **5. Summary and discussions.**

605 The gridded SSS products from the SMOS satellite undoubtedly provide a way to constrain
 606 errors in salinity, especially for an ocean reanalysis system. The present study is the first
 607 observing system simulation experiment for the assimilation of SMOS SSS in the Arctic. In
 608 this study, based on the TOPAZ reanalysis system, we compared ~~a~~ reanalysis assimilating

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619 conventional observations with [two new reanalysis runs which additionally assimilated two](#)
620 [versions of the SMOS SSS products from BEC](#).
621 After comparison with independent SSS observations from CTD and surface water samples
622 along [cruise tracks](#), near-surface salinity errors have been significantly reduced compared to
623 the control experiment (Exp0). In the Beaufort Sea, the SSS bias and RMSD in ExpV3 are
624 reduced respectively by 26.0% and 20.6%. In ExpV2, the RMSD reduction is smaller (by
625 11.5%). In the Chukchi Sea, the reduction in SSS misfits in ExpV3 (bias:17.7%; RMSD:
626 16.4%) is also larger than in ExpV2 (bias: 15.5%; RMSD: 13.7%). Around Greenland, the
627 difference between the two products is even more pronounced, with a significant reduction in
628 the SSS bias (32.6%) and RMSD (9.4%) in ExpV3, while there is no notable improvement in
629 ExpV2. The difference is larger in the East Greenland Sea. The direct assimilation of SSS
630 from SMOS is more efficient at constraining the near-surface salinity than the multivariate
631 impact of other observations. This finding is also consistent with other SSS assimilation
632 experiments in the tropics (Chakraborty et al., 2015; Tranchant et al., 2019). Conversely,
633 when considering the multivariate impact of SSS on SIC (in Fig. 9) we find that the
634 assimilation of the V2 product does not affect the assimilation of sea ice concentrations while
635 the V3.1 product causes an increase in the negative increments, which could be an
636 indication of excessive freshening along the Siberian [coast](#). In contrast, the increments of
637 SST in the open ocean are smaller in ExpV3, indicating a synergy effect of SST and SSS.
638 Overall, our data assimilation system did not detect obvious inconsistencies between the
639 SMOS SSS product and other assimilated observations.

640
641 Furthermore, this study shows error reductions of SSS when assimilating the V3.1 product
642 from SMOS even outside of the central Arctic in the Nordic Seas and along the Norwegian
643 coast. Moreover, our analysis shows how the spatial distribution of Arctic FWC changes as a
644 result of assimilating the two SMOS products. The time series of averaged FWC north of
645 70°N shows that the FWC in the whole central Arctic can be increased by about 25 cm using
646 DA. Our experiments show that the Arctic FWC can be redistributed horizontally after
647 assimilation, but the latter effect requires a longer assimilation run to be evaluated.
648 As a summary of the quantitative SSS comparisons (Table 2), the overall score of each
649 assimilation setup for each subregion can be defined by its ability to reduce the SSS bias
650 and RMSD by more than 9% relative to Exp0 (Fig. 2). [The threshold value of 9% is not fully](#)
651 [arbitrary, referring to the reduction of SSS RMSD in GS, where the bias reduction is](#)
652 [significant \(through the t-test\)](#). If both bias and RMSD meet [this](#) objective, we give a score of
653 1, but of 2 if only one of them is met. If neither of them exceeds 9%, the score is set to 3.
654 Thus outside of the central Arctic, the v2.0 SSS product loses its impact on the TOPAZ

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662 system, but the V3.1 SSS brings significant impacts across the Arctic and further out, and
663 clearly benefits from its refined effective resolution (Martínez et al., 2022). Since there was
664 little evidence of a double-penalty effect in the validation RMSD apart from Baffin Bay, we
665 consider that the assimilation of the higher-resolution signals was efficient. However, the
666 assimilation did not improve the SSS significantly in the Barents Sea or other areas where
667 SSS gradients are weak. These may require higher accuracy to distinguish the Atlantic
668 waters from other water masses of salinity only slightly below 35 psu. To further improve the
669 SSS product, a combination with the Aquarius sensor using the same L-band frequency
670 (e.g., Lee et al, 2012), and SMAP (e.g., Tang et al., 2017; Reul et al., 2020) is desirable.
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672 **Data availability.** All the in-situ observations for validation in this study are open access as
673 indicated in Sect. 3. The model results from Exp0 are the released TOPAZ reanalysis, which
674 is freely available from CMEMS (<http://marine.copernicus.eu>) or
675 <https://doi.org/10.11582/2022.00043>. The other assimilation experiments can be provided
676 freely upon personal communication.

677

678 **Author contributions.** JX initiated the design and carried out the assimilation
679 experiments. LB and RR contributed to the result interpretation. JM provided the SSS data.
680 CG and RC contributed to the uncertainty of the satellite data. All the authors contributed to
681 editing and correcting this paper.

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683 **Competing interests.** The authors declare that they have no conflict of interest.

684

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688 portal (<https://www.ices.dk>); the Arctic Data Center (<https://arcticdata.io/catalog/data>); and
689 the BGEP data were available at the Woods Hole Oceanographic Institution
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697 the storage areas under the projects ns9481k and ns2993k.

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Caption and figures:

Table 1. Settings of the three assimilation runs in 2016 with and without SSS.

	Assimilated obs.	Initial model states	End date of assimilation	SSS Observation Errors
Exp0	SST, SLA, T/S profile, SIC, SIT, and SID	6 th July	28 th Dec.	N/A
ExpV2	SSS V2.0 + obs. used in Exp0	6 th July	28 th Dec.	Eq. 3
ExpV3	SSS V3.1 + obs. used in Exp0	6 th July	28 th Dec.	Eq. 3

Table 2. Evaluation of SSS misfits (unit: psu) in the three assimilation runs according to the 6 areas indicated by the blue dashed lines in Fig. 2. The numbers in bold indicate the smallest misfit with a reduction of more than 9% relative to Exp0. The overall score depends on whether the bias and RMSD are reduced by at least 9%. If both criteria are met, the score equals 1, it is 2 if only one of them is met, and 3 otherwise. The start superscript means the bias changes passed the significance test using Student's t-test ($\alpha = 0.05$).

Areas in Fig. 2	Number of obs.	Bias (psu)			RMSD (psu)			Overall score	
		Exp 0	ExpV 2	ExpV 3	Exp 0	ExpV 2	ExpV 3	ExpV2	ExpV3
BS	98	2.81	2.43	2.08	2.87	2.54	2.28	1*	1*
CS	137	2.32	1.96	1.91	2.62	2.26	2.19	1*	1*
BSS	189	1.35	1.34	1.30	2.50	2.49	2.47	3	3
NS	669	0.43	0.44	0.37	1.19	1.19	1.16	3	2
GS	254	0.50	0.51	0.24	1.43	1.43	1.28	3	1*
BB	89	0.35	0.37	0.12	1.22	1.20	1.22	3	2

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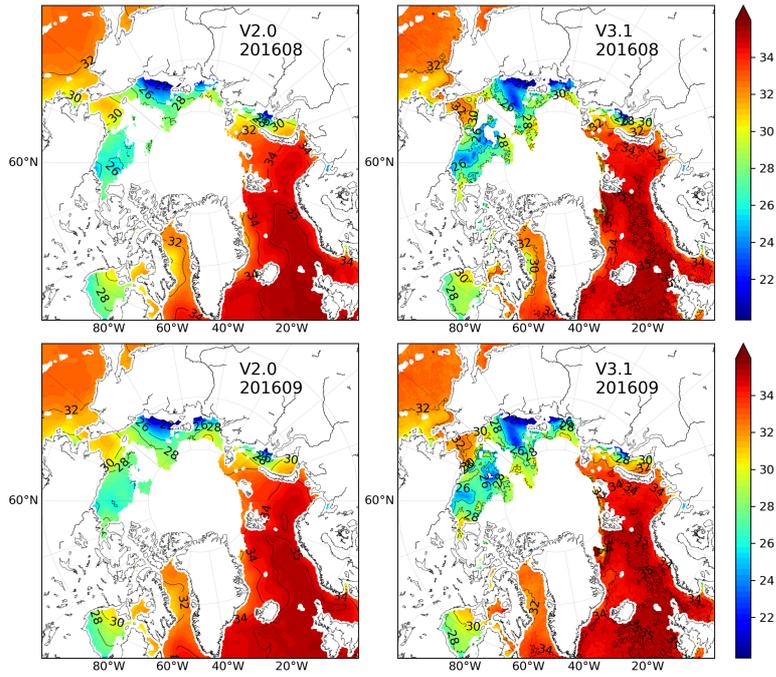
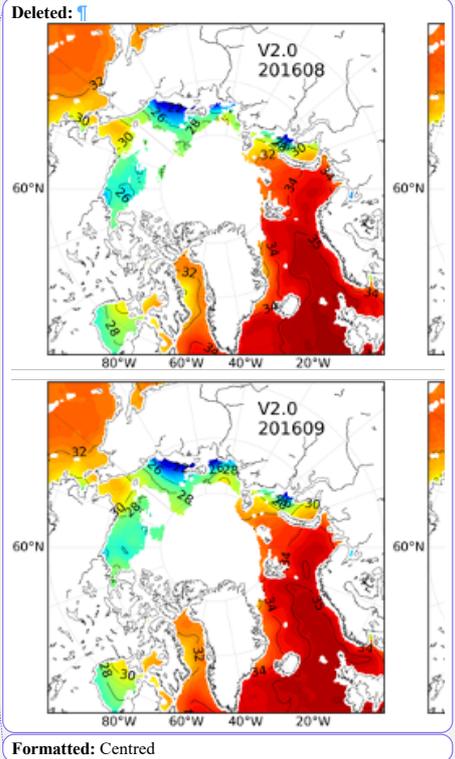
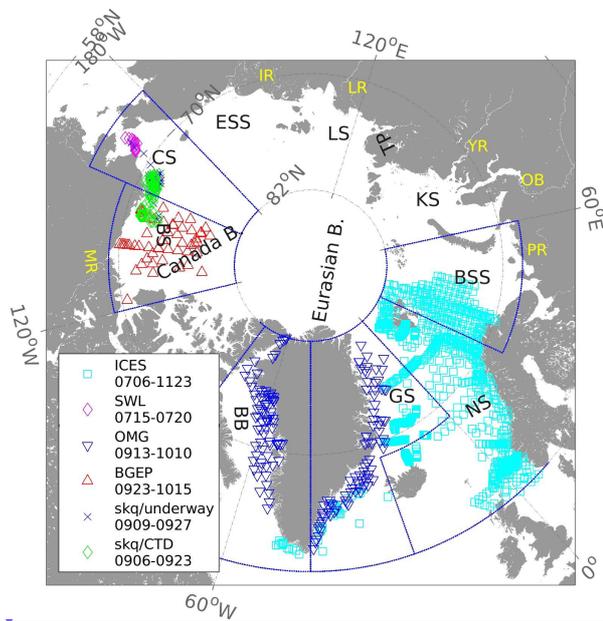


Fig. 1 Monthly SSS of Aug (top line) and Sep (bottom line) in 2016 from SMOS products of BEC V2.0 (left) and V3.1 (right). Note: the solid isolines of SSS are 22, 26, 28, 30, 32, 34, and 35 psu.





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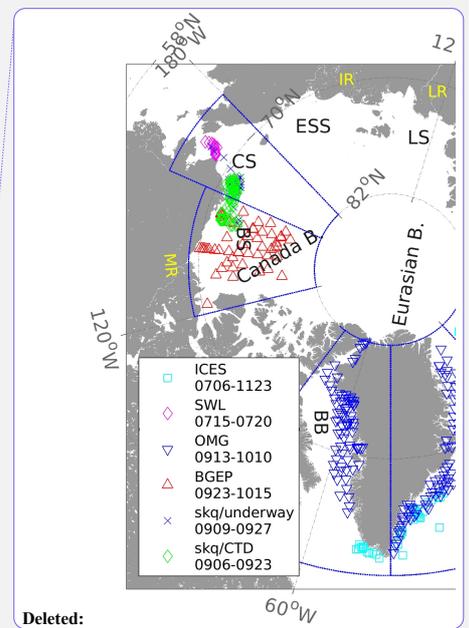


Fig. 2 Locations of the observed SSS from in-situ profiles and surface samples by cruises from July to December 2016. The marks note 6 observation sources, see the details in Section 2.3. The marginal seas delineated are the Beaufort Sea (BS), Chukchi Sea (CS), East Siberian Sea (ESS), Laptev Sea (LS), Kara Sea (KS), Barents Sea (BSS), Greenland Sea (GS), Norwegian Sea (NS), and Baffin Bay (BB). The main rivers around the Arctic region are the Mackenzie River (MR), Pechora (PR), the Ob (OB), Yenisey River (YR), Lena River (LR), and Indigirka River (IR). TP indicates the Taymyr Peninsula.

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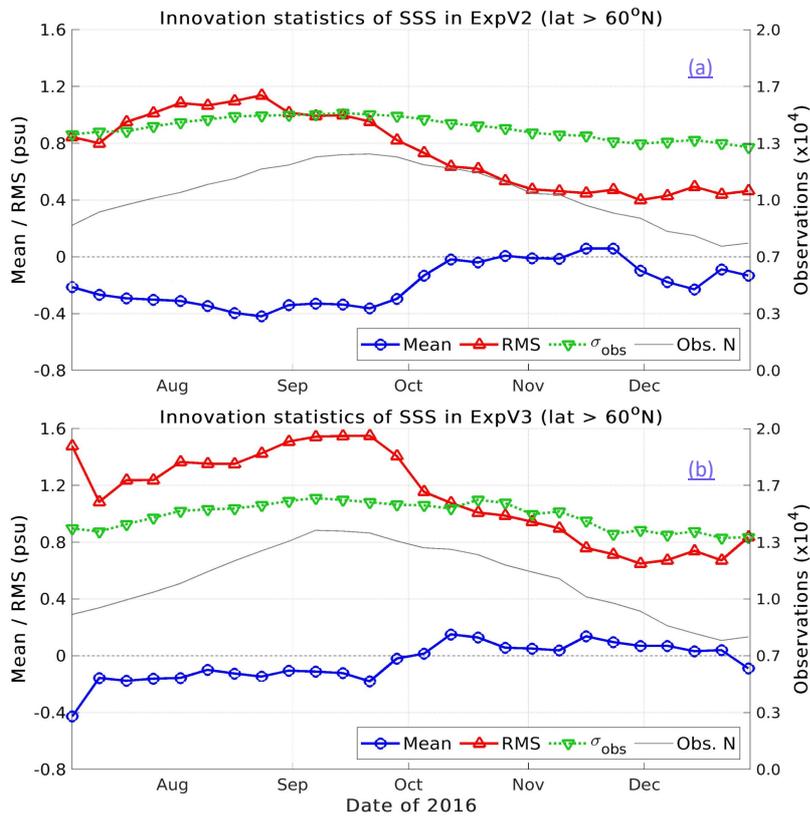


Fig. 3 Innovation statistics of SSS in the Arctic (>60°N) from ExpV2 (a) and ExpV3 (b). The line with red triangles is the root mean squared innovation, and the blue dotted line shows the mean of innovations north of 60°N. The gray line represents the number of observations assimilated, and the green line with inverted triangles is the observation error standard deviation in the two runs.

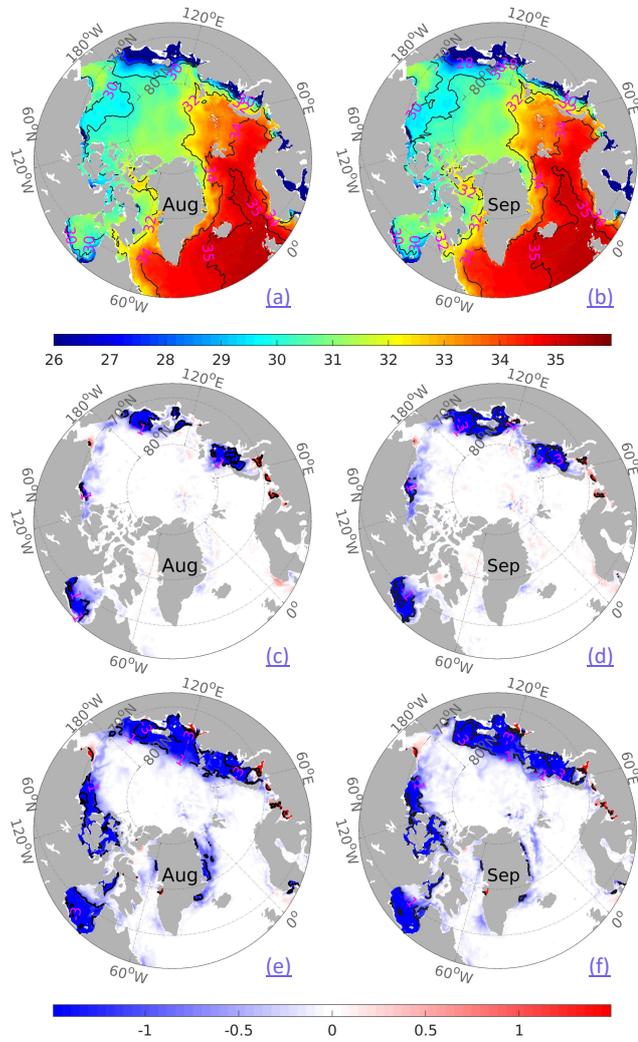


Fig. 4 Top: Monthly simulated SSS (unit: psu) from Exp0 in August (left column) and September 2016 (right column). The black isolines indicate the 26, 28, 30, 32, 34, and 35 psu, respectively. **Middle and bottom:** monthly SSS differences in ExpV2 (middle line) and ExpV3 (bottom line) with respect to Exp0. The black lines are -3, -1, 1, and 3 psu.

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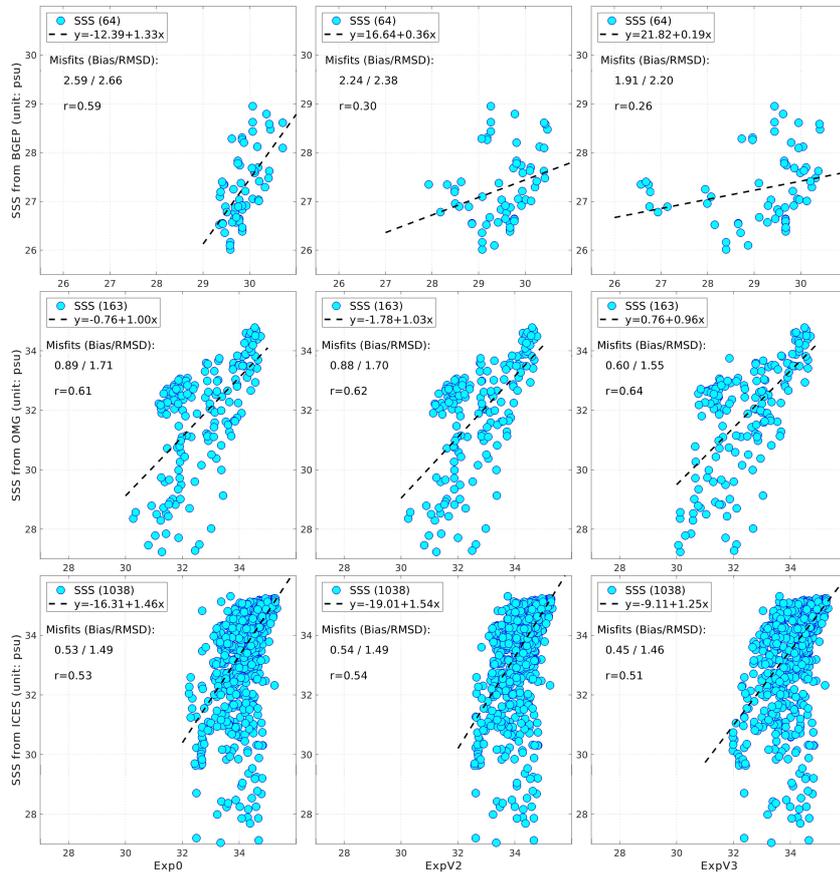


Fig. 5 Scatterplots of SSS in the TOPAZ assimilation runs against in-situ profiles (Top: from BGEF in the Beaufort Sea; Middle: from OMG in both Greenland Seas; Bottom: from ICES in the Nordic Seas as indicated in Fig.1 and descriptions in 2.1). The statistics of SSS misfits are indicated in each panel with the bias and the RMSD, respectively, the number of observations is given between parentheses. The dark dashed line represents the linear regression, and r is the linear correlation coefficient. All the correlation coefficients are over the 95% significance test.

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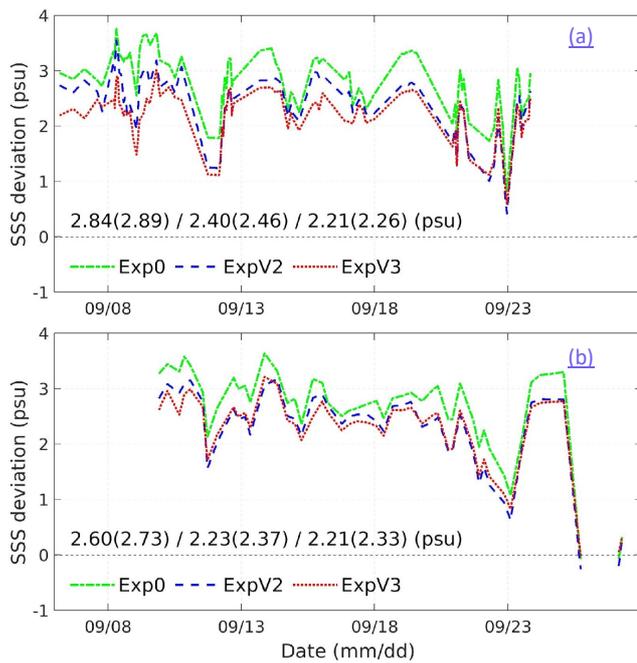


Fig. 6 Model-minus-observations SSS differences in the three assimilation runs against the SSS recorded in the Beaufort Sea and the Chukchi Sea along the SKQ cruise in 2016: a) from CTD profiles; b) from surface water samples underway in the same cruise. The biases are indicated in the same order as the legend from Exp0 to ExpV3. and the corresponding RMSD are inside parentheses.

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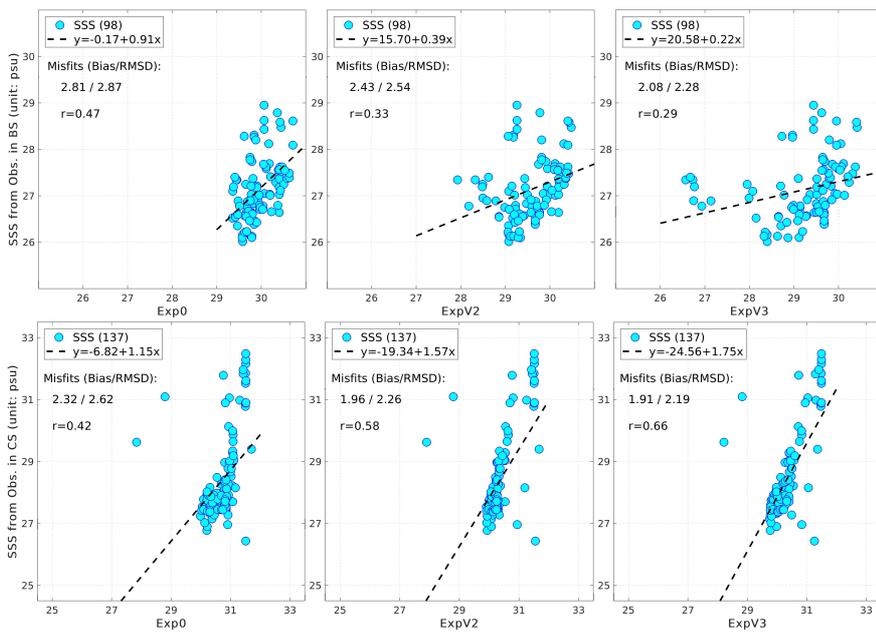


Fig. 7 Scatterplots of SSS (unit: psu) in the three assimilation runs Exp0, ExpV2, and ExpV3 against the CTD observations collected by different cruises in 2016. **Top**: Beaufort Sea; **Bottom**: Chukchi Sea as shown in Fig.1. All the correlation coefficients are over the 95% significance test.

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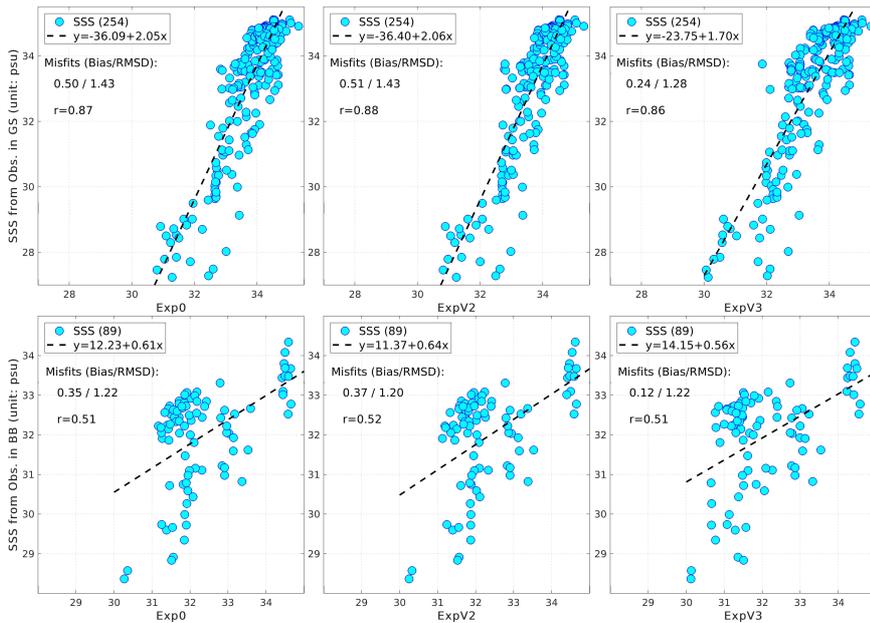
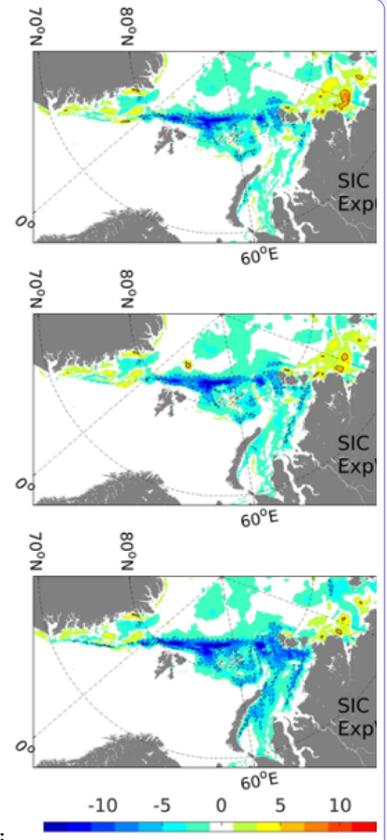


Fig. 8 Scatterplots of SSS (unit: psu) in the three assimilation runs Exp0, ExpV2, and ExpV3 against CTD observations from OMG and ICES in 2016. **Upper:** East Greenland Sea; **Bottom:** Baffin Bay as shown in Fig.1. The statistics of SSS misfits are indicated in each panel with the bias and the RMSD respectively, and the number of observations is given between parentheses. The dark dashed line represents the linear regression, and r is the linear correlation coefficient. All the correlation coefficients are over the 95% significance test.

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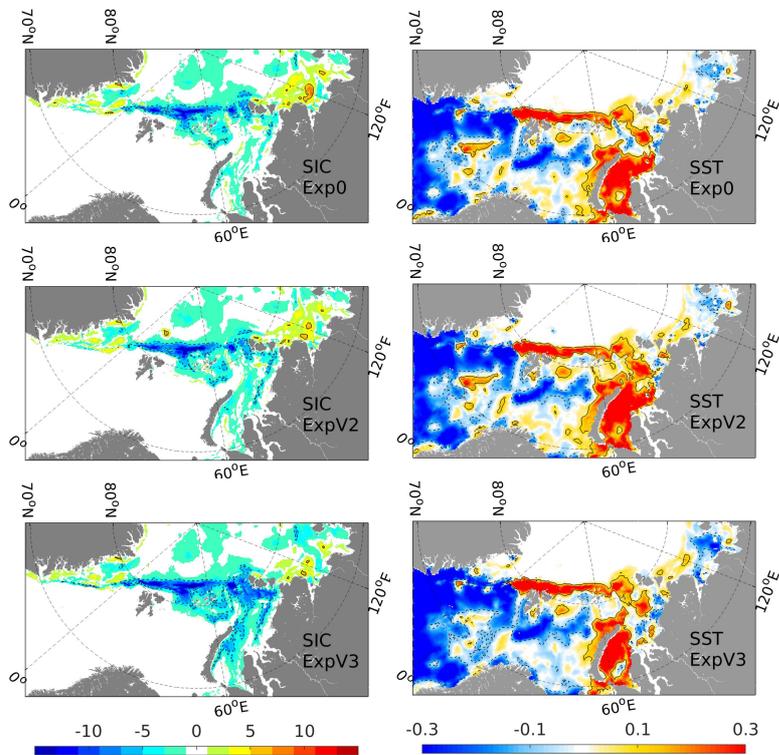


Fig 9. Mean of SIC and SST increments for the 6-months period (Top: in Exp0; Middle: in ExpV2; Bottom: in ExpV3). The figure shows the European Arctic for clarity. Left column: sea ice concentration (unit: %) with isolines of $\pm 5\%$. Right column: SST with isolines of $\pm 0.1^\circ\text{C}$.

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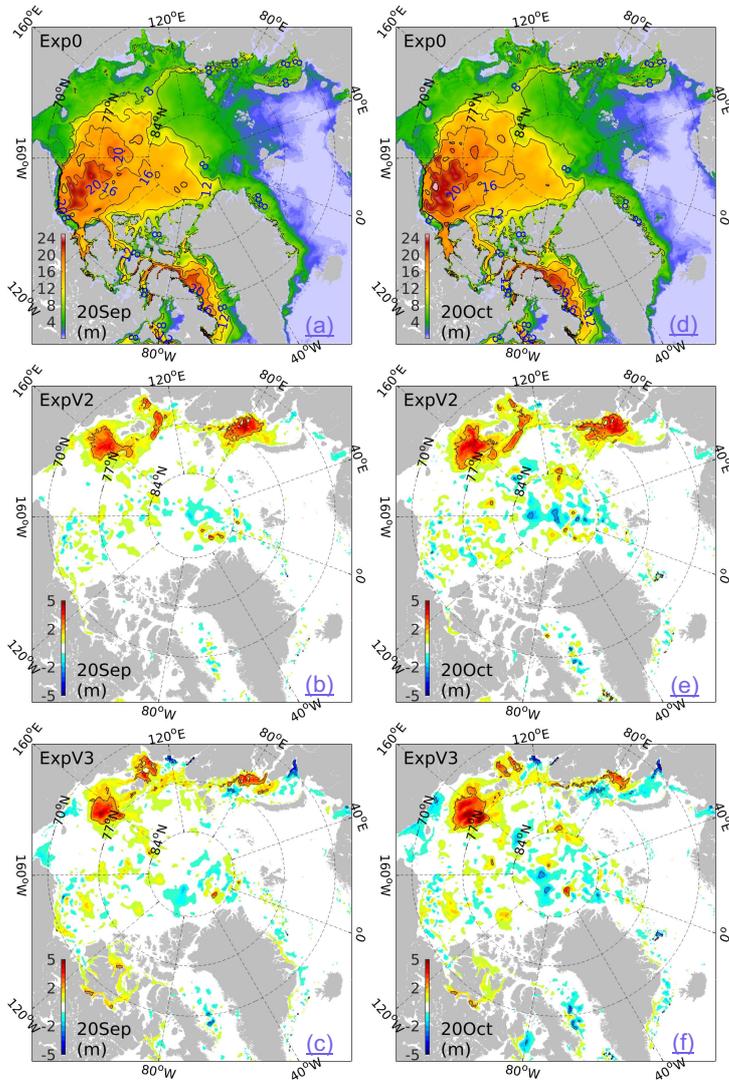


Fig. 10 Top: Freshwater contents (unit: m) on 20th September (left) and 20th October (right) 2016 in the Arctic Ocean from the three assimilation runs: Exp0. The interval of isolines is 4 meters. **Middle and bottom:** the FWC differences in ExpV2 (middle line) and ExpV3 (bottom line) concerning that in Exp0. The black lines indicate -2 m and 2 m differences.

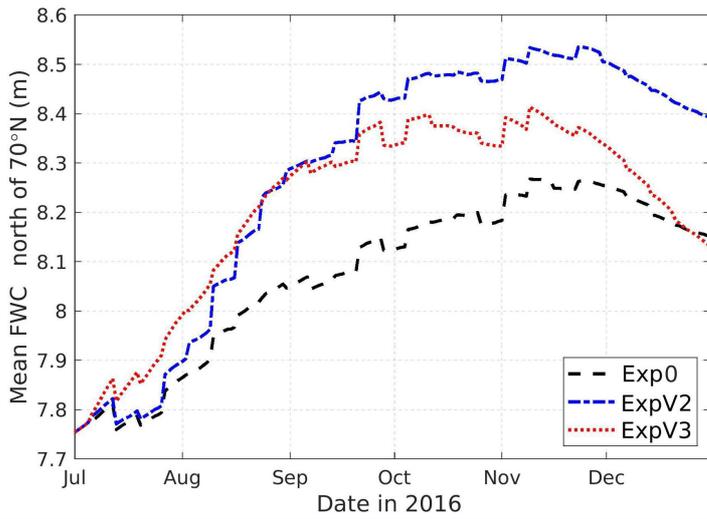
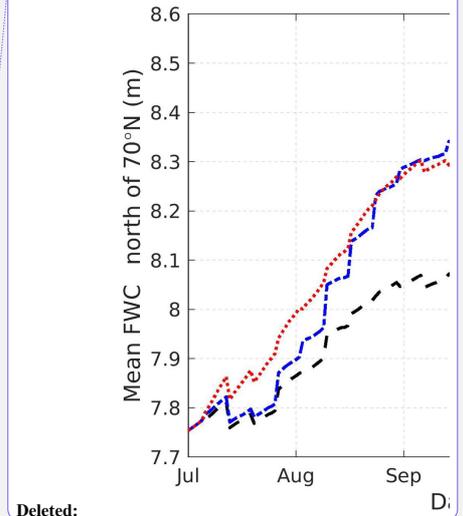


Fig 11. Arctic-wide means of freshwater content (unit: m) in the central Arctic (>70°N) from July to December 2016 for Exp0 (dark dashed), ExpV2 (blue dashed), and ExpV3 (red dotted).

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