Assimilation of sea surface salinities from SMOS in an Arctic coupled ocean and sea ice reanalysis

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Abstract

In the Arctic, the sea surface salinity (SSS) plays a key role in processes related to water mixing and sea ice. However, the lack of salinity observations causes large uncertainties in Arctic Ocean forecasts and reanalysis. Recently the Soil Moisture and Ocean Salinity (SMOS) satellite mission was used by the Barcelona Expert Centre to develop an Arctic SSS product. In this study, we evaluate the impact of assimilating this data in a coupled ocean-ice data assimilation system. Using the Deterministic Ensemble Kalman filter from July to December 2016, two assimilation runs respectively assimilated two successive versions of the SMOS SSS product, on top of a pre-existing reanalysis run. The runs were validated against independent in-situ salinity profiles in the Arctic. The results show that the biases and the Root Mean Squared Differences (RMSD) of SSS are reduced by 10% to 50% depending on areas, and highlight the importance of assimilating satellite salinity data. The time series of Freshwater Content (FWC) further shows that its seasonal cycle can be adjusted by assimilation of the SSS products, which is encouraging for its use in a long-time reanalysis to better reproduce the Arctic water cycle.

Keywords: Arctic Ocean; Sea Surface Salinity; FWC; SMOS;
1. Introduction

The Arctic Ocean is undergoing a dramatic warming, resulting in the loss of sea ice, documented by previous studies (Johannessen et al., 1999; Stroeve and Notz, 2018). Sea ice melt contributes freshwater to the Arctic Ocean, together with other sources, and has far-reaching effects on the Arctic Ocean environment (Carmack et al., 2016). The Arctic observing system, compared to other oceans, lacks the capability to provide a complete picture of ocean salinity, particularly because of obstruction by sea ice. A complete reconstruction of Arctic environmental variables thus requires a data assimilative numerical model capable of propagating information below sea ice during the winter as practiced by ocean operational forecast systems (Dombrowsky, 2009; Fuji et al., 2019). As with other ocean data assimilation (DA) applications, Arctic reanalysis products of ocean and sea ice play an important role in understanding climate change and its mechanisms. In recent years, many studies (Storto et al., 2019; Uotila et al., 2019) evaluated the quality of the Arctic reanalysis products and recommended experiments to maximize the usefulness of new observations, as done in Kaminski et al. (2015) and Xie et al. (2018). However, there are no impact studies of salinity observations in the Arctic to our knowledge.

Ocean salinity has been used to study the water cycle for the last 20 years (e.g., Curry et al., 2003; Boyer et al., 2005; Yu, 2011; Yu et al., 2017). A recent review paper showed a stabilization of the Freshwater Content (FWC) in the Arctic Basin, although observations indicate that the Beaufort Gyre keeps freshening. A recent update of the review paper showed a stabilization of the Freshwater Content (FWC) of the Arctic Basin, although observations indicate that the Beaufort Gyre keeps freshening.

Salinity variations have far-reaching implications for ocean mixing, water mass formation, and ocean general circulation, but suffer from large uncertainties in the Arctic, mainly due to sparse observations and the lack of a steady-state reference time period (e.g., Stroh et al., 2015; Xie et al., 2019). Measuring sea surface salinity (SSS) from passive microwave remote sensing is a comparatively new but promising way to reduce the uncertainty in salinity. Launched in November 2009, the Microwave Imaging Radiometer using Aperture Synthesis (MIRAS) instrument of the European Space Agency's (ESA) Soil Moisture and Ocean Salinity (SMOS) mission measures the brightness temperature ($T_b$) on the sea surface. The passive 2-D interferometric radiometer on the satellite operating in L-band (1.4 GHz) is sensitive to water salinity and sufficiently free from electromagnetic interference (e.g., Font et al., 2010; Kerr et al., 2010). Since May 2010, SMOS operationally provides SSS records over the global ocean (Mecklenburg et al., 2012). During the last 12 years, large improvements have been introduced in the SMOS data processing chain, increasing the accuracy and coverage of the salinity data up to levels that were unthinkable at the beginning of the mission (Martin-Neira et al., 2016; Olmedo et al., 2018; Reul et al., 2020; Boutin et al., 2022).
Furthermore, the assimilation of satellite-derived SSS products using an ensemble DA method has been found to significantly improve the surface and subsurface salinity fields in the tropics (Lu et al., 2016). The advantages of assimilating three SSS products from SMOS, Aquarius (ref., Lee et al., 2012), and Soil Moisture Active Passive Mission (SMAP; e.g., Tang et al., 2017) into a global ocean forecast system using 3D-Var DA method have also been demonstrated by Martín et al. (2019). Their results show the benefits of assimilating both the SMOS and SMAP datasets in the intertropical convergence zone in the tropical Pacific.

Recently, under the framework of the ESA project Arctic+Salinity (AO/1-9158/18/I-BG), and further development of the non-Bayesian scheme (Olmedo et al., 2017), the effective resolutions of SSS data were enhanced both in space and time (Martínez et al., 2022).

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new version of the SSS product (V3.1) shows the capability to monitor the mesoscale structures and river discharges (e.g., Martinez et al., 2022). This new product provides daily maps (Level 4) of 9-day averages in the Arctic on a regular 25 km grid and covers a longer time period 2011-2019, and are released through the BEC portal (http://bec.icm.csic.es/ and also at DOI: 10.20350/digitalCSIC/12620; last accessed May 2022). The major differences in the estimation of the two SSS products (V2.0 and V3.1) are detailed in the Algorithm.

The paper is organized as follows: Section 2 describes briefly the coupled ocean and sea ice (Xie et al., 2017). The model validation against independent observations, separated into different ocean basins. Section 4 also examines the impact of SSS assimilation on the weekly increments of other related variables near the surface, and explores the integrated effect on the freshwater simulated by the model. In Section 5, the findings of this study and future perspectives are summarized.

2. Assimilation system and experimental design

2.1 The Arctic ocean and sea-ice coupled data assimilation system

TOPAZ is a coupled ocean and sea ice data assimilation system, built using the Deterministic Ensemble Kalman Filter (DEnKF; Sakov et al., 2012) to simultaneously assimilate multiple types of observations for the ocean and sea ice (Xie et al., 2017). The ocean model in this system uses, version 2.2 of the Hybrid Coordinate Ocean Model (HYCOM; Chassignet et al., 2003) with a low-distortion square grid with a horizontal resolution of 12-16 km. The river discharge input is climatological, using the ERA-Interim runoffs channeled in a simple hydrological model, which tends to underestimate the...
amplitude of the seasonal cycle and thus a saline bias at the surface (Xie et al., 2019). The
coupled sea ice model uses a single-category thermodynamic model (Drange and Simonsen,
1996) and dynamics by the modified elastic-viscous-plastic rheology (Bouillon et al., 2013) in
an early version of the CICE model (Lisæter et al., 2003). The model covers the whole Arctic
Ocean (shown in Fig. 1 in Xie et al., 2017). A seasonal inflow of Pacific Water is imposed
across the Bering Strait, based on observed transports (Woodgate et al., 2012). At all lateral
boundaries, the temperature and salinity stratifications are relaxed to a climatology
combining version 2.0 of WOA2013 and version 3.0 of PHC with a 20-grid cells buffer zone.
To avoid a potential model drift, the surface salinity is relaxed to the combined climatology as
mentioned above, with a 30-day timescale, but the relaxation is suppressed wherever the
difference from climatology exceeds 0.5 psu to avoid the artificial formation of stable surface
freshwater layers.

The two steps of the assimilation system can be translated by the following concept
expressions (update and model propagation):

\[
X_a = X_f + K (Y - H X_f) \quad (1)
\]

\[
X_f = M(X_u) \quad (2)
\]

Where the matrix \( X \) represents the model states with all 3-D and 2-D variables needed by
the model forward integration, represented by the operator \( M \). The subscripts ‘a’ and ‘f’
respectively indicate the analyzed model state obtained through optimization after DA and the
model forecast. The vector \( y \) is composed of the quality-checked observations during the
weekly cycle, the observation operator \( H \) gives the model equivalent matching the
observations. The innovation term (in parentheses in Eq.1) represents the differences
between the model and the various observations on the observation space. The TOPAZ
model runs an ensemble of 100 members. The \( K \) matrix (Kalman gain) is calculated using
the ensemble covariance matrix. On a weekly basis, we use the DEnKF to assimilate
different types of ocean and ice observations, including along-track sea level anomaly (SLA),
sea surface temperature (SST), in-situ profiles of temperature and salinity, sea ice
concentrations (SIC) and sea ice drift products all sourced from the Copernicus Marine
Environment Monitoring Services (CMEMS: https://marine.copernicus.eu). The same TOPAZ
system provides a 10-day forecast of ocean physics and biogeochemistry in the Arctic
(Bertino et al., 2021) every day via the CMEMS portal. Like other square root versions of the
Ensemble Kalman Filter, the DEnKF splits Eq. 1 into two steps: the \( K \) calculation is applied to
the ensemble mean, and the anomalies are updated to match a target analysis covariance
(more details in Sakov et al., 2012).

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2.2. Assimilation experiments and the observation error estimate for SSS

To evaluate the impact of the assimilation of two versions of the SSS products on TOPAZ model runs, a control assimilation experiment (Exp0) and two parallel assimilation experiments (ExpV2, ExpV3) for a 6-month time period (July to December 2016) were performed. Exp0 assimilates all available ocean and sea ice data, except the satellite SSS product. On the other hand, ExpV2 and ExpV3 additionally assimilate the BEC SSS products V2.0 and V3.1, respectively. Details of the three assimilation runs are listed in Table 1.

The observation error is a key parameter in any DA system. Too small values lead to overfitting, while too large values make the assimilation inefficient. The salinity errors from Passive Microwaves were previously estimated by Vinogradova et al. (2014): the zonal average of standard errors north of 60°N was estimated at 0.6 psu. In a recent study, Xie et al. (2019) evaluated the SMOS-based SSS products using in-situ observations and revealed strong regional dependence for the V2.0 product. Errors smaller than 0.4 psu in the Northern Atlantic but increasing dramatically to 1.0 psu in the Nordic seas and over 2.0 psu in the central Arctic. Undoubtedly, the salinity observation errors from Passive Microwaves are higher in high latitudes than elsewhere. Furthermore, in the Beaufort Sea (as Fig. 12a in Xie et al., 2019), the error of the SSS V2.0 product and the Arctic reanalysis product from TOPAZ (same as Exp0 used in this study) both show an inverse relationship between SSS values and SSS errors. Hence, we use an empirical error function for ExpV2 and ExpV3 adjusted to the discrepancies as shown in Eq. 3, following Xie et al. (2019):

\[
E_{\text{SSS}} = \max (E_{\text{mss}}, 10.6 + \frac{6}{1 + e^{0.85 - S}}) \tag{3}
\]

Where \(E_{\text{mss}}\) is the instrumental error variance estimated by the data provider, that part is absent from the V2.0 product. Eq. 3 yields more conservative error estimates than the providers, which also prevent discontinuities caused by strong assimilation updates (as an example noticed by Balibrea-Iniesta et al., 2018). Other precautions are also applied following Sakov et al. (2012). By construction, the observation errors are always larger for the V3.1 than the V2.0 product, but in fresh waters they are identical. This implies that the assimilation may pull the analysis closer to the V2.0 than the V3.1 product in the more saline waters, but they are otherwise treated on equal footing, ignoring the a priori expectation that the most recent product should be more reliable.

3. In situ SSS observations for validation

All in situ salinity profiles were collected from various repositories and cruises (as shown in Fig. 2). Salinity measurements were extracted near the surface over the Arctic domain during the experimental time period. The sanity check procedures include:

- In ExpV2, if... that part is set to zero due...
**Data from the Beaufort Gyre Experiment Project (BGEP)**

The BGEP has maintained an observing system in the Canadian Basin since 2003 and provides in-situ observations over the Beaufort Gyre every summer. Although the BGEP has maintained three bottom-tethered moorings since 2003, the shallowest depth of the measured profiles for temperature and salinity is below 50 m. Hence, in this study, we only use the Conductivity Temperature Depth (CTD) dataset from the cruise in 2016 (https://www2.whoi.edu/site/beaufortgyre/data/ctd-and-geochemistry/, last access: 14th February 2022). SSS observations from these CTD profiles in the time period from 13th Sep to 10th Oct 2016 are represented by the red triangles in Fig. 2.

**Data from Oceans Melting Greenland (OMG)**

The project Oceans Melting Greenland was funded by NASA to understand the role of the ocean in melting Greenland’s glaciers. Over a five-year campaign, this project collected temperature and salinity profiles by Airborne eXpendable Conductivity Temperature Depth (AXCTD) launched from an aircraft (e.g., Fenty, et al, 2016). The deployed probe can sink to a depth of 1000 meters, connected with a float by a wire. The measured temperature and conductivity are then sent back to the aircraft. These salinity profiles collected during the first OMG campaign in 2016 are downloaded from https://podaac.jpl.nasa.gov/dataset/OMG_L2_AXCTD/ (last access: 10th February 2022). The SSS from OMG distributed around Greenland, from 13th Sep to 10th Oct 2016 are shown as the inverted blue triangles in Fig. 2.

**Data from the International Council for the Exploration of the Sea (ICES)**

Salinity profiles were also obtained from the ICES portal (https://www.ices.dk). Shown as blue squares in Fig. 2, the locations of the profiles during the last 6 months of 2016 are dense in the Nordic Seas and restricted to north of 58°N for this study. Valid salinity profiles from ICES (last access: 9th February 2022) are obtained from 6th July to 23rd Nov in 2016.

**Data from other cruises at the Arctic Data Center (ADC)**

Surface salinity observations from scientific cruises are obtained from the Arctic Data Center portal (https://arcticdata.io/catalog/data; last access: 17th Feb 2022). During the model experiment, the first relevant cruise in ADC was SKQ201612S which was operated by University of Alaska Fairbanks with the RV Sikuliaq. This cruise collected data from Nome, Alaska, USA.
through a sea chest below the waterline (e.g., 4-8 m), the uncontaminated seawater was pumped into the ship and the corresponding filtration system supplies samples every 3 hours to the sensors (More details in Goñi et al., 2019). These SSS observations were obtained on the 9th-27th of September, indicated as blue crosses in Fig. 2. Moreover, SSS measurements were also collected from the Seabird CTD on board Sir Wilfrid Laurier (SWL), but only in July 2016. This cruise is part of the annual monitoring from the Canadian Coast Guard Service (Cooper et al., 2019). The SSS observations are obtained near the Bering Strait close to the Pacific boundary of our model.
from ExpV2 or ExpV3 is called $e_2$. Thus, considering the null hypothesis $H_0$: $e_1$, $e_2$, and $e_3$ are the means of indiscernible random draws, the t-value can be calculated as follows:

$$t = \frac{|e_2 - e_1|}{\sqrt{s_1^2/(n_1 - 1) + s_2^2/(n_2 - 1)}}$$

Where $s_1$ ($s_2$) is the standard deviation in the $e_1$ ($e_2$), and $n_1$ ($n_2$) is the number of observations. For every t-value, the p-value from the above equation is the probability that random errors would prove $H_0$ wrong. Low p-values (<0.05) indicate that the change of bias due to assimilation is significant.

4. Results

4.1 Diagnosing using assimilation statistics

The SSS innovations in the two assimilation runs ExpV2 and ExpV3 are compared in Fig. 3, together with the number of assimilated SSS observations and the ensemble spread calculated by the ensemble standard deviation. The total number of observations is at its maximum in September when the sea ice cover is minimal. Since both versions of the SSS product share the same time-frequency (9-day average) and gridded format, the number of assimilated observations in the two runs remains identical (gray lines in Fig. 3). For ExpV2, the Root Mean Square (RMS) of the SSS innovation varies between 0.4 and 1.2 psu, but the mean of SSS innovation, calculated as the observation minus the model simulation (cf. the bracket in Eq. 1), shows the saline bias of 0.4 psu highest in September. However, in ExpV3, the salinity bias quickly disappears after a few data assimilation cycles. The RMS of the SSS innovation is larger in ExpV3 between 0.6 and 1.6 psu, which can partly be explained by the higher effective resolution of the V3.1 product and the double penalty effect. In ExpV3, the RMS of the SSS innovation (the red line) jumps down after the first SSS assimilation step. The RMS of SSS innovations and the observation errors both decrease from summer to winter, following a seasonal cycle as the areas of fresher water get gradually ice-covered. The domain-averaged observation errors are only slightly larger in ExpV3 than in ExpV2, as explained above, and the RMS of SSS innovations become lower than the observation errors near the end of the run, which indicates that the observation errors for the V2.0 SSS have been overestimated.

In the top panels of Fig. 4, the SSS maps present the control run (Exp0) in August and September 2016, respectively. For Exp0 in August, low salinity waters are found in the Beaufort Sea near the Mackenzie River and along the East Siberian coast. In September, the fresher waters, below 30 psu, bridge the two areas in Exp0 probably due to sea ice melt, although the lowest salinity near the Siberian coast remains unchanged from August to September (as indicated by the 28 psu isoline). Compared with the SSS observations from different sources, the SSS innovations become lower than the observation errors in ExpV3. In the bottom panels of Fig. 4, the SSS assimilation is significant.
SMOS (Fig. 1), these two low salinity waters are clearly underestimated in Exp0. Meanwhile, the relatively saline 32 psu isoline crosses both the Eurasian basin and the Baffin Bay. In the Laptev Sea, due to the significant effects of river runoff and ice melt, the salinity shows a strong gradient from the southeast to the northern part. During winter, the salinity increases to 34 psu, and decreases in summer near to 30 psu (Janout et al., 2017). In the northwest of the TP, the Kara Sea freshwater meets with the Atlantic Water pathways from the Fram Strait and Barents Sea (shown in Figure 1 by Janout et al., 2017). Close to the TP, the observations at the mooring profiles in Janout et al. (2017) show much fresher surface salinity (29 psu) than the subsurface salinity (32 psu) in summer. Compared to the SMOS SSS maps (Fig. 1), only the V3.1 product shows the 32 psu isolines around the TP. Another difference between the two SMOS products arises in the Chukchi Sea where the V3.1 product is more saline than both the V2.0 product and SSS in Exp0. Then the middle and bottom panels of Fig. 4 show the SSS differences in August and September 2016 between the SSS assimilation runs and the control run. Fig. 4c and 4d both show a freshening of the coastal areas in the Kara Sea, Laptev Sea, and East Siberian Sea, but in ExpV3 the freshening is stronger and wider (Fig. 4e and 4f). In the Beaufort Sea, ExpV2 mainly brings a local freshening near the mouth of the Mackenzie River in August, which then spreads out along the coast in September. The freshening in the BS brought by ExpV3 affects a broader area, even including the Canadian Archipelago. ExpV3 also freshens the SSS on both sides of Greenland Island. From August onwards, the SSS in ExpV3 freshens by over 1 psu along the whole east Greenland coast, which clearly does not happen in ExpV2. In fact, the 32 psu isoline in ExpV3 (not shown) extends hundreds of kilometers further to the South East Greenland coast in comparison to Exp0 and ExpV2. The rest of the Greenland coast is also fresher by 0.5 psu in ExpV3 during both months. This is a sign of a consistent change in the V3.1 product.

Even though most of the SSS assimilation leads to a freshening of the surface, a few locations show higher salinity than Exp0, these are different from ExpV2 to ExpV3. For example, the saline increment near the Bering Strait is larger in ExpV3 in excess of 1 psu, consistently with the difference between the two remote sensing products (Fig. 1).

Other increases in SSS concern small areas near estuaries and are more common in ExpV3. The increase to the west of the Yamal Peninsula can be explained by a model setup bias in the location of the Ob river but compensated by the SSS assimilation. In the above comparisons of SSS maps, the central Arctic is not discussed, since the region is covered by sea ice and the effect of assimilation is indirect.
4.2 Comparison with independent in-situ observations

Quality-checked in-situ observations in the Central Arctic are very unevenly distributed. After pooling all platforms together, we further investigate the SSS misfits in six subregions of the Arctic (Fig. 2 and Table 2). This section will present statistics of differences to independent in-situ observations, separately considering marginal seas.

Beaufort Sea (BS): Figure 5 shows the scatterplots of SSS in the three runs against in-situ observations from BGEF, OMG, and ICES. In the Beaufort Sea (top panel in Fig. 5), the observed SSS varies in a range of 26-29 psu. The range of SSS in Exp0 is much smaller, between 29-31 psu with a saline bias of 2.6 psu and an RMSD of 2.7 psu, but otherwise, it shows a reasonably linear relationship, \( r = 0.99 \). The SSS bias in Exp0 has the same value as in Xie et al. (2019), although estimated using the BGEF observations in a different time period (2011-2013). The range of SSS in ExpV2 is slightly improved to 28-30.5 psu. Further, the bias is reduced by 0.5 psu, corresponding to bias and RMSD reductions of respectively 13.5% and 10.5% with respect to Exp0. In ExpV3, the SSS range is much closer, between 26.5 and 30.5 psu, and the resulting bias and RMSD reductions of SSS are respectively 26.3% and 17.3% with respect to Exp0. Both the bias reduction in ExpV2 and ExpV3 relative to Exp0 pass the significance test \( (p = 0.05) \) through Student’s t-test. Furthermore, compared to all in-situ SSS in BS (top panels in Fig. 7), the SSS misfits in ExpV3 show a stronger reduction by 26.0% for bias and 20.6% for RMSD. ExpV2 reduces these errors by half as much (13.5% for bias and 11.5% for RMSD). These results clearly indicate that the new version of the SSS is more beneficial for data assimilation in the Beaufort Sea.

Chukchi Sea (CS): Fig. 6a shows the SSS deviations as a function of time during the SKQ cruise route. Figure 6a shows the surface levels from CTDs. The saline bias (2.8 psu) is more pronounced than in the Beaufort Sea, which we attribute to the proximity to the model boundary in the Bering Strait, relaxed to climatological values, where the interannual variability of Pacific water is not included. After assimilating SSS products, a reduction of the bias is observed during September, by 15.5% in ExpV2 and up to 22.2% in ExpV3. The comparison to underway surface water samples (Fig. 6b) also shows an error reduction of around 15%, though fewer differences between ExpV2 and ExpV3.

Considering other cruise data in the CS (Fig. 7; bottom panels), the SSS in Exp0 shows almost uniform values with a saline bias of about 2.3 psu and an RMSD of 2.6 psu. A recent observational study by Goñi et al. (2021) shows that the surface salinity of the CS during late summer varies between 28-30 psu during the time period 2016-2017. The range of SSS observations considered here is slightly broader (27-32 psu). The assimilation of SSS
ExpV3 shows 32 psu, although the saline bias remains (differences less than 0.01 psu). In contrast, lower salinity in these two runs is of Exp0 and ExpV2 are distributed in the North Atlantic and as SSS bias and RMSD are the lowest in ExpV3 in Table 2, even though the reductions are not significantly different compared to Exp0 through the t-test (p = 0.05).

Finally, we examine the SSS deviations in the Barents Sea and the Norwegian Sea. The SSS bias and RMSD are the lowest in ExpV3 in Table 2, even though the reductions are not as significant as in the area of fresher surface waters. Compared to the ICES observations distributed in the North Atlantic and the Nordic Seas (blue squares in Fig. 2), the scatterplots of Exp0 and ExpV2 are nearly identical (see the bottom panels in Fig. 3). The minimum salinity in these two runs is 32 psu. The SSS bias and RMSD in both runs are also similar (differences less than 0.01 psu). In contrast, lower salinity values are found in ExpV3, below 32 psu, although the saline bias remains around 0.5 psu on average. Notably, the SSS in ExpV3 shows that data assimilation can reduce the bias by 15% compared to Exp0, but the RMSD only reduced about 0.03 psu, also possibly due to the double penalty effect. This also brings a reduction of 32.6%/9.4% of the bias and RMSD in the BB. One possible explanation is the double penalty effect.
suggests that the improvements near the coast will be the next challenge for future versions of the SSS product.

### 4.3 Impact analysis of SSS assimilation

The above section has demonstrated that the assimilation of remote sensing SSS generally improves the match to independent in-situ measurements, although the improvements are location-dependent. Since large areas are void of in-situ measurements, the increment of other surface variables caused by assimilation from the three runs will also be meaningful in understanding the impacts incurred. The increments are the differences between the analysis and the forecast. The calculation of them is the result of the innovations of all assimilated observations multiplied by the Kalman gain, as computed in Eq. (1). Since the DEnKF update is multivariate, we present the impact of the assimilation on other model variables closely related to the SSS, SST, and SIC. Since the only difference in the setting between the three runs is the assimilation of SSS, we can attribute the differences to the impact of SSS observations. In theory, if both the model and observations were unbiased, the increments of other assimilated variables should generally decrease because of the presence of a new SSS term in the denominator of the Kalman Gain (the assimilated observations compete with each other), but SSS biases can also spill over to the other model variables and increase the innovations on the following assimilation step and thus the resulting increments. Hypothetically, if the SSS were the only source of errors in TOPAZ, the increments of other variables should vanish over time. Figure 9 compares the time-averaged increments of SIC and seawater temperature in the top 3-m layer (considered as SST here) in the three runs. The sign of the increments remains overall the same across the three experiments, both for SST and SIC. The SST increments in the three runs are negative in the open ocean and positive near the ice edge, as shown in the right column of Fig. 9.

The SST increments in Exp0 and in ExpV2 are nearly identical, but in ExpV3 there are few areas such as in the Kara Sea and in the Laptev Sea where the SST increments have been depressed. These are locations where the SSS and SST are positively correlated, so the updated SSS by assimilation is also helpful in reducing the water temperature misfits near the surface. The changes in SST are however small with respect to the large SSS differences in Figure 4. In Exp0, the SIC increments are small (<5%) inside the ice pack. The satellite SIC observations are assimilated every week and help to correctly position the ice edge (Sakov et al., 2012). The increments exceed 5% along the ice edge, as can be seen in the northern Barents Sea.

The assimilation of the V2.0 SSS product also shows minimal differences from Exp0 partly because of the conservative sea ice mask in the V2.0 SMOS SSS. The SIC increments are...
opposite to those of SST, showing that the assimilation warms the surface water where ice is removed, which is consistent with Lisæter et al. (2003). Only minor differences between ExpV2 and ExpV0 are visible along all areas swept by the ice edge during the 6-month experiment, for example in the Kara Sea. In contrast, the assimilation of the V3.1 SSS product shows larger changes of SIC increments than in ExpV2 with a broader area of negative increments (removed ice) in the northern Barents Sea. This is not visibly related to the SIC increments but to the freshening caused by the assimilation of V3.1 SSS as SSS and SIC are positively correlated in the northern Barents Sea, as shown by Fig. 2 in Sakov et al. (2012). The increased SIC increments may be an indication that the SSS freshening could be excessive.

Since the whole water column is updated by the assimilation, the freshwater content is also modified by the assimilation of SSS. There are however complex relationships between SSS and FWC as shown by Fournier et al. (2020). The changes in FWC in the Arctic are calculated as in Eq. (6) derived from Proshutinsky et al. (2009), although this method was initially intended for the BS. Applying the same formula for interpolation of in-situ observations, Proshutinsky et al. (2020) estimated the time-averaged summer freshwater content in the Beaufort Gyre region in two time periods (1950-1980 and 2013-2018). In the latter period, they located the FWC centre in the BS around (150°W, 75°N) and drew the 20-m isoline over more than 5 degrees of latitude and nearly 30 degrees of longitude on average. When compared to the earlier reference period, the FWC in the BS has increased and its centre has shifted westward.

Following Proshutinsky et al. (2009), the model FWC in the Arctic is estimated as:

\[
FWC = \frac{\int_{\text{ref}}^{\text{max}} (1 - \frac{S(z)}{S_{\text{ref}}}) \, dz}{F_{\text{int}}} \quad (6)
\]

Where the reference salinity value \( S_{\text{ref}} \) is taken at 34.8 psu, \( z_{\text{in}} \) is the depth of the reference salinity of the sea bed, and \( S(z) \) is the salinity profile. Figure 10 shows the FWC on two representative days, September 20th and October 20th, 2016. In Exp0, the reanalysis reproduces the typical FWC distribution in the Arctic with a maximum in the Beaufort Sea. The 20 m isolines in Fig. 10a and 10d show an increase in spatial coverage during October, consistent with Rosenblum et al. (2021), but the 20 m isoline is not extending as far as 170°E compared to Proshutinsky et al. (2020). After assimilation of SSS products (either V2.0 or V3.1), the amplitude and the spatial distribution of the FWC maximum increase slightly in the BS (see Fig. 10b and 10c). A much larger increase of FWC appears on the East Siberian shelf and in the coastal areas of the Laptev Sea and eastern Kara Sea, although to a different extent in ExpV2 and in ExpV3. In the eastern Kara Sea, the FWC increases over a wider area in ExpV2 than in ExpV3. To the west of the Yamal Peninsula, ExpV3 shows a
negative anomaly related to an incorrect location of the model river runoff, corrected in later versions of the model. The SSS assimilation is able to correct the related fresh bias. In the central Arctic, although the assimilated SSS measurements are masked by the sea ice cover, the FWC differences north of 84°N are more pronounced in October than in September, which indicates the advection of SSS increments by the Transpolar Drift Stream (Rigor et al., 2002; Balibrea-Iniesta et al., 2018). These results suggest that the SSS assimilation of both versions of SMOS satellite products will compensate for the insufficient river summer runoff, redistribute the freshwater in the Arctic, and adjust the freshwater budget. However, because of the limited in-situ data, the above assessment remains qualitative.

Further, we compare the daily time series of Arctic-averaged FWC from the three runs to the north of 70°N (Fig. 11). The FWC increases in October-November to reach its maximum, and gradually decreases thereafter. The impact of weekly data assimilation cycles is visible as instantaneous jumps on the three curves of the time series, but the assimilation of SSS does not cause unrealistic imbalances. The FWC increases substantially due to SSS assimilation, by about 25 cm. Notably, the assimilation of version 3.1 SSS causes a faster increase during the first two months. Due to the absence of ground truth data in 2016, the above comparison remains qualitative, but the timing of the peak is in better agreement with the ITP data presented by Rosenblum et al. (2021, their Fig. 4), although the amplitude of the seasonal FWC seems too small in all experiments, which can be related to insufficient thick ice in TOPAZ (Uotila et al., 2019). More concrete evidence about the changed FWC will be provided when the longer assimilation of the satellite-based SSS product is finished in the near future.

5. Summary and discussions.

The gridded SSS products from the SMOS satellite undoubtedly provide a way to constrain errors in salinity, especially for an ocean reanalysis system. The present study is the first observing system simulation experiment for the assimilation of SMOS SSS in the Arctic. In this study, based on the TOPAZ reanalysis system, we compared the reanalysis assimilating conventional observations with and without the assimilation of two successive SMOS SSS products from BEC.

After comparison with independent SSS observations from CTD and surface water samples along the cruises, the near-surface salinity errors have been significantly reduced compared to the control experiment (Exp0). In the Beaufort Sea, the SSS bias and RMSD in ExpV3 are reduced respectively by 26.0% and 20.6%. In ExpV2, the RMSD reduction is smaller, by...
To further improve the SSS product, a combination with the Aquarius sensor using the same assimilation setup for each subregion can be defined by its ability to reduce the SSS bias and RMSD by more than 9% relative to Exp0 (Fig. 2). If both bias and RMSD meet the objective, we give a score of 1, but of 2 if only one of them is met. If neither of them exceeds 9%, the score is set to 3. Thus outside of the central Arctic, the V3.0 SSS product loses its impact on the TOPAZ system, but the V3.1 SSS brings significant impacts across the Arctic and further out, and clearly benefits from its refined effective resolution (Martinez et al., 2022). Since there was little evidence of a double-penalty effect in the validation RMSD apart from Baffin Bay, we consider that the assimilation of the higher resolution signals was efficient. However, the assimilation did not improve the SSS significantly in the Barents Sea or other areas where SSS gradients are weak. These may require higher accuracy to distinguish the Atlantic waters from other water masses of salinity only slightly below 35 psu. To further improve the SSS product, a combination with the Aquarius sensor using the same assimilation setup for each subregion can be defined by its ability to reduce the SSS bias and RMSD by more than 9% relative to Exp0 (Fig. 2). If both bias and RMSD meet the objective, we give a score of 1, but of 2 if only one of them is met. If neither of them exceeds 9%, the score is set to 3. Thus outside of the central Arctic, the V3.0 SSS product loses its impact on the TOPAZ system, but the V3.1 SSS brings significant impacts across the Arctic and further out, and clearly benefits from its refined effective resolution (Martinez et al., 2022). Since there was little evidence of a double-penalty effect in the validation RMSD apart from Baffin Bay, we consider that the assimilation of the higher resolution signals was efficient. However, the assimilation did not improve the SSS significantly in the Barents Sea or other areas where SSS gradients are weak. These may require higher accuracy to
L-band frequency (e.g., Lee et al., 2012), and SMAP (e.g., Tang et al., 2017; Reul et al., 2020) is desirable.

Data availability. All the in-situ observations for validation in this study are open access as indicated in Sect. 3. The model results from Exp0 are the released TOPAZ reanalysis, which is freely available from CMEMS (http://marine.copernicus.eu) or https://doi.org/10.11582/2022.00043. The other assimilation experiments can be provided freely upon personal communication.

Author contributions. JX initiated the design and carried out the assimilation experiments. LB and RR contributed to the result interpretation. JM provided the SSS data. CG and RC contributed to the uncertainty of the satellite data. All the authors contributed to editing and correcting this paper.

Competing interests. The authors declare that they have no conflict of interest.

Acknowledgments. We are grateful to the in-situ data providers: the OMG mission for the released final CTD data via https://podaac.jpl.nasa.gov/omg; the ICES data portal (https://www.ices.dk); the Arctic Data Center (https://arcticdata.io/catalog/data); and the BGEP data were available at the Woods Hole Oceanographic Institution (https://www2.whoi.edu/site/beaufortgyre) in collaboration with researchers from Fisheries and Oceans Canada at the Institute of Ocean Sciences. This study has been supported by the ESA Arctic+Salinity project and the following CCN, and also partly by the Norwegian Research Council project (325242). The assimilation experiments and the plotting of the results were performed on resources provided by Sigma2, the Norwegian Infrastructure for High Performance Computing and Data Storage with the projects nn2293k and nn9481k and the storage areas under the projects ns9481k and ns2993k.

Reference:


Table 1. Settings of the three assimilation runs in 2016 with and without SSS.

<table>
<thead>
<tr>
<th></th>
<th>Assimilated obs.</th>
<th>Initial model states</th>
<th>End date of assimilation</th>
<th>SSS Observation Errors</th>
</tr>
</thead>
<tbody>
<tr>
<td>Exp0</td>
<td>SST, SLA, T/S profile, SIC, SIT, and SID</td>
<td>6th July</td>
<td>28th Dec.</td>
<td>N/A</td>
</tr>
<tr>
<td>ExpV2</td>
<td>SSS V2.0 + obs. used in Exp0</td>
<td>6th July</td>
<td>28th Dec.</td>
<td>N/A</td>
</tr>
<tr>
<td>ExpV3</td>
<td>SSS V3.1 + obs. used in Exp0</td>
<td>6th July</td>
<td>28th Dec.</td>
<td>Eq. 3</td>
</tr>
</tbody>
</table>

Table 2. Evaluation of SSS misfits (unit: psu) in the three assimilation runs according to the 6 areas indicated by the blue dashed lines in Fig. 2. The numbers in bold indicate the smallest misfit with a reduction of at least 9% relative to Exp0. The overall score depends on whether the bias and RMSD are reduced by at least 9%. If both criteria are met, the score equals 1; if only one of them is met, and 3 otherwise. The star subscript means the bias changes passed the significance test using Student’s t-test ($\alpha = 0.05$).

<table>
<thead>
<tr>
<th>Areas in Fig. 2</th>
<th>Number of obs.</th>
<th>Bias (psu)</th>
<th>RMSD (psu)</th>
<th>Overall score</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td>Ex p0</td>
<td>Exp V2</td>
<td>Exp V3</td>
</tr>
<tr>
<td>BS</td>
<td>98</td>
<td>2.8</td>
<td>2.43</td>
<td><strong>2.08</strong></td>
</tr>
<tr>
<td>CS</td>
<td>137</td>
<td>2.3</td>
<td>1.96</td>
<td><strong>1.91</strong></td>
</tr>
<tr>
<td>BSS</td>
<td>189</td>
<td>1.3</td>
<td>1.34</td>
<td>1.30</td>
</tr>
<tr>
<td>NS</td>
<td>669</td>
<td>0.4</td>
<td>0.44</td>
<td><strong>0.37</strong></td>
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<tr>
<td>GS</td>
<td>254</td>
<td>0.5</td>
<td>0.51</td>
<td><strong>0.24</strong></td>
</tr>
<tr>
<td>BB</td>
<td>89</td>
<td>0.3</td>
<td>0.37</td>
<td><strong>0.12</strong></td>
</tr>
</tbody>
</table>
Fig. 1 Monthly SSS of Aug (top line) and Sep (bottom line) in 2016 from SMOS products of BEC V2.0 (left) and V3.1 (right). Note: the solid isolines of SSS are 22, 26, 28, 30, 32, 34, and 35 psu.
Fig. 2 Locations of the observed SSS from in-situ profiles and surface samples by cruises from July to December 2016. The marks note 6 observation sources, see the details in Section 2.3. The marginal seas delineated are the Beaufort Sea (BS), Chukchi Sea (CS), East Siberian Sea (ESS), Laptev Sea (LS), Kara Sea (KS), Barents Sea (BSS), Greenland Sea (GS), Norwegian Sea (NS), and Baffin Bay (BB). The main rivers around the Arctic region are the Mackenzie River (MR), Pechora (PR), the Ob (OB), Yenisey River (YR), Lena River (LR), and Indigirka River (IR). TP indicates the Taymyr Peninsula.
Fig. 3 Innovation statistics of SSS in the Arctic (>60°N) from ExpV2 (a) and ExpV3 (b). The line with red triangles is the root mean squared innovation, and the blue dotted line shows the mean of innovations north of 60°N. The gray line represents the number of observations assimilated, and the green line with inverted triangles is the observation error standard deviation in the two runs.

Deleted: 2. Innovations
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Fig. 4 Top: Monthly simulated SSS (unit: psu) from Exp0 in August (left column) and September 2016 (right column). The black isolines indicate the 26, 28, 30, 32, 34, and 35 psu, respectively. Middle and bottom: monthly SSS differences in ExpV2 (middle line) and ExpV3 (bottom line) with respect to Exp0. The black lines are -3, -1, 1, and 3 psu.
Fig. 5 Scatterplots of SSS in the TOPAZ assimilation runs against in-situ profiles (Top: from BGEP in the Beaufort Sea; Middle: from OMG in both Greenland Seas; Bottom: from ICES in the Nordic Seas as indicated in Fig.1 and descriptions in 2.1). The statistics of SSS misfits are indicated in each panel with the bias and the RMSD, respectively, the number of observations is given between parentheses. The dark dashed line represents the linear regression, and r is the linear correlation coefficient. All the correlation coefficients are over the 95% significance test (α=0.05).
Fig. 6 Model-minus-observations SSS differences in the three assimilation runs against the SSS recorded in the Beaufort Sea and the Chukchi Sea along the SKQ cruise in 2016: a) from CTD profiles; b) from surface water samples underway in the same cruise. The biases are indicated in the same order and the corresponding RMSD are between parentheses.
Fig. 2 Scatterplots of SSS (unit: psu) in the three assimilation runs Exp0, ExpV2, and ExpV3 against the CTD observations collected by different cruises in 2016. **Top**: Beaufort Sea; **Bottom**: Chukchi Sea as shown in Fig. 1. **All the correlation coefficients are over the 95% significance test** ($\alpha=0.01$).
Fig. 8 Scatterplots of SSS (unit: psu) in the three assimilation runs Exp0, ExpV2, and ExpV3 against CTD observations from OMG and ICES in 2016. 

**Upper:** East Greenland Sea; **Bottom:** Baffin Bay as shown in Fig.1. The statistics of SSS misfits are indicated in each panel with the bias and the RMSD respectively, and the number of observations is given between parentheses. The dark dashed line represents the linear regression, and $r$ is the linear correlation coefficient. All the correlation coefficients are over the 95% significance test ($\alpha=0.01$).
Fig 9. Averaged increments for the 6-months period (Top: in Exp0, Middle: in ExpV2, Bottom: in ExpV3). The figure shows the European Arctic for clarity. Left column: sea ice concentration (unit: %) with isolines of ± 5%. Right column: SST with isolines of ± 0.1°C.
**Fig. 10 Top**: Freshwater contents (unit: m) on 20th September and 20th October 2016 in the Arctic Ocean from the three assimilation runs: Exp0. The interval of isolines is 4 meters. **Middle and bottom**; the FWC differences in ExpV2 (middle line) and ExpV3 (bottom line) concerning that in Exp0. The black lines indicate -2 m and 2 m differences.
Fig 11. Arctic-wide averaged freshwater content (unit: m) in the central Arctic (>70°N) from July to December 2016 for Exp0 (dark dashed), ExpV2 (blue dashed), and ExpV3 (red dotted).