Assimilation of Meteosat Third Generation (MTG) Lightning Imager (LI) pseudo-observations in AROME-France – Proof of Concept

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Abstract. This study develops a Lightning Data Assimilation (LDA) scheme for the regional, convection-permitting NWP model AROME-France. The LDA scheme intends to assimilate total lightning, i.e., cloud-to-ground (CG) and inter- and intra-cloud (IC), of the future Meteosat Third Generation (MTG) Lightning Imager (LI). MTG-LI proxy data are created and Flash Extent Density (FED) fields are derived. An FED forward observation operator (FFO) is trained based on modeled, column integrated graupel mass from 24 storm days in 2018. The FFO is successfully verified for 2 independent storm days. With the FFO, the LDA adapts a 1-dimensional Bayesian (1DBay) retrieval followed by a 3-dimensional variational (3DVar) assimilation approach that is currently run operationally in AROME-France for radar reflectivity data. The 1DBay retrieval derives relative humidity profiles from the background by comparing the FED observations to the FED inferred from the background. Retrieved relative humidity profiles are assimilated as sounding data. The evaluation of the LDA comprises different LDA experiments and four case studies. It is found that all LDA experiments can increase the background integrated water vapor (IWV) in regions where the observed FED exceeds the FED inferred from AROME-France outputs. In addition, IWV can be reduced where spurious FED is modeled. A qualitative analysis of 6-hour accumulated rainfall fields reveals that the LDA is capable of locating and initiating some local precipitation fields better than a radar data assimilation (RDA) experiment. However, the LDA also leads to too high rainfall accumulations at some locations. Fractions Skill Scores (FSSs) of 6-hour accumulated rainfall are overall similar for the developed LDA and RDA experiments. An approach aiming at mitigating effects due to differences in the optical extents of lightning flashes and the area of the corresponding cloud was developed and included in the LDA, however, it does not always improve the FSS.

1 Introduction

Convective weather phenomena such as thunderstorms threaten the society by producing severe weather and related impacts, e.g., flash floods, large hail, tornadoes, and strong winds. Cloud electrification and subsequent lightning discharges are caused by interactions of different ice particles inside convective clouds. The process makes lightning an effective tracer of deep

convection. The new type of lightning locating systems (LLSs) on geostationary (GEO) satellites allows for continuous large-scale monitoring of total, i.e., cloud-to-ground (CG) and inter/intra-cloud (IC), lightning activity. The Geostationary Lightning Mappers (GLMs) on the GOES-R series satellites cover the Americas and the adjacent oceans (Goodman et al., 2013). A similar

25 instrument, the Lightning Imager (LI), was launched in December 2022 aboard the first Meteosat Third Generation (MTG) satellite to monitor lightning over Europe, Africa, and large portions of the Atlantic Ocean, among other regions (Dobber and Grandell, 2014). High-quality GEO data is also available in data-sparse regions with limited access, such as over oceans and mountainous terrain as well as countries without radar networks. GEO lightning data may become important for numerical weather prediction (NWP),

30 potentially improving the initial state of the model and the accuracy of the predicted storm location, timing, and intensity. Lightning data assimilation (LDA) addresses this objective.

However, LDA is not trivial. Operational models, e.g., the Application of Research to Operations at Mesoscale (AROME) model (Brousseau et al., 2016), the regional operational model of Météo-France, do not include any explicit representation of lightning. Other difficulties of lightning data assimilation include the ephemeral nature of lightning relative to the life cycle of

35 thunderstorms and time-space shifts between observations and the background, which are usual at the storm scale, challenge up-to-date data assimilation systems (zero-spread, zero-gradient problems) (e.g., Janisková and Lopez, 2013). Background errors are not Gaussian, and lightning is more related to lower-impact variables such as hydrometeor content and vertical velocity than to thermodynamic variables. Despite those difficulties, previous studies have shown the benefits of LDA for forecasts of convection and related phenomena.

40 Early LDA studies used NWP models that parametrize convection. Lightning data controlled the activation of the convective parametrization scheme (CPS). Often nudging techniques were applied to modify the model humidity and wind fields (e.g., Papadopoulos et al., 2005; Mansell et al., 2007; Lagouvardos et al., 2013; Giannaros et al., 2016), or latent heat (e.g., Pessi and Businger, 2009). These studies reported positive effects of LDA on the score of precipitation forecasts, especially for the location and quantity of heavy rain.

45 When NWP models resolve convection (<3km horizontal resolution), so-called lightning proxies can be used to relate NWP output to lightning observations. Some previous studies suggested and tested cloud top height, cloud top pressure, and cold cloud depth as predictors to estimate the lightning density (e.g., Price and Rind, 1992, 1993; Allen and Pickering, 2002; Wong et al., 2013; Giannaros et al., 2015; Karagiannidis et al., 2019).

Recent development corroborates using cloud dynamics or ice hydrometeors, e.g., graupel, for reliable lightning proxies.
50 Indeed, field campaigns as those reported by Deierling et al. (2008) found a strong correlation between lightning activity and ice mass fluxes. Deierling and Petersen (2008) showed a robust relationship between total lightning rate and updraft characteristics, especially the updraft volume. Buiat et al. (2017) analyzed CloudSat Cloud Profiling Radar (CPR) to relate cloud ice water content (IWC) and effective radius (ER) to LINET (Betz et al., 2009) lightning strokes. They found that high IWC and high ER are favorable to CG strokes. Graupel contributes to both high IWC and high ER. Strong on-going updraughts
55 can cause high IWC. Hence, the findings agree with the studies of Deierling et al. (2008); Deierling and Petersen (2008).

Various lightning proxies have been tested in NWP studies. McCaul et al. (2009) related domain-wide peaks of proxies based on ice-phase hydrometeor fields, one related to upward fluxes and the second related to vertically integrated ice content, to peaks of the flash rate density, and suggested a blended solution using both proxies. Yair et al. (2010) introduced a lightning potential index (LPI) that is calculated using the simulated grid-scale vertical velocity and simulated hydrometeor mass mixing ratios of liquid water, cloud ice, snow, and graupel. Barthe et al. (2010) concluded that none of precipitation ice mass, ice water path, ice mass flux product, updraft volume, maximum vertical velocity, and cloud top height could predict the lightning flash rates and trends well for both of their two cases. However, more recent studies of Formenton et al. (2013); Federico et al. (2014); Bovalo et al. (2019) confirm a key role of graupel in the cloud electrification and use ice and /or graupel content for lightning simulation and proxy definition.

With the lightning proxies, lightning observation operators are created to compare the model output to the lightning observations and assimilate the lightning data. Most of the recent LDA schemes use lightning operators based on ice hydrometeors or updraft characteristics, e.g., graupel mass or updraft volume. In the following, a brief overview of LDA techniques is presented, with the focus on 3-dimensional variational (3DVar) LDA and studies to assimilate GLM data.

Fierro et al. (2012) put forward a widely used (e.g., Dixon et al., 2016; Wang et al., 2017a; Federico et al., 2017; Wang et al., 2017b) concept of lightning proxy calculating water vapor mixing ratio from simulated graupel mass and observed flash rates. They then increased the water vapor mixing ratio in the 0°C to -20°C layer where lightning was observed and the relative humidity (RH) of the background was less than 81%. Precipitating convection was better correlated with observed reflectivity fields for the LDA than for the control experiment. The method was further tested by Fierro et al. (2014) using 10-minute Flash Extent Density (FED). Lynn et al. (2015); Marchand and Fuelberg (2014) refined the nudging technique of Fierro et al. (2012) to increase the virtual temperature perturbation and favor static instability or by warming the source layer of the convective updraft, respectively. Lynn et al. (2015) also introduced an extension to suppress spurious convection. Other nudging-based LDA make use of ice-phase particle mixing ratios (e.g., Qie et al., 2014; Wang et al., 2018) and pseudo radar reflectivity (Wang et al., 2014).

Mansell (2014); Allen et al. (2016) assimilated synthetic GLM total lightning represented as FED using an Ensemble Kalman Filter (EnKF). Mansell (2014) used both the simulated flash rate and a linear relationship between total lightning and graupel volume as observation operators. Allen et al. (2016) recommend a linear best fit operator based on graupel mass and graupel volume. In preparation of a hybrid variational-ensemble LDA technique for GLM, Apodaca et al. (2014) assimilated World Wide Lightning Location Network (WWLLN) data in WRF. However, the use of WWLLN as a GLM proxy is debatable as WWLLN mainly detects CG flashes, whereas GLM detects total lightning.

A 3DVar LDA was applied by Wang et al. (2017b) using the relationship given by Fierro et al. (2012) and assimilated pseudo RH profiles in the form of sounding data. They noted increased forecasts skills in general, but also that the method still needs improvement to suppress spurious convection. Fierro et al. (2016) replaced their previous nudging by a 3DVar LDA with 10-minute FED. They found that the Radar Data Assimilation (RDA) yielded better forecasts of convective cells during the first 30min of the forecast, while the LDA gave better storm structures one hour into the forecast. The combination of both RDA and LDA provided the highest forecast skill. Fierro et al. (2019) tested the 3DVar LDA technique developed for ground-based

data with GLM total lightning observations. It adjusts water vapor mass mixing ratio (q_v) in regions of lightning by setting RH to 95% in a layer of 3km above the LCL if the background RH is less than 95%. Both LDA and RDA improved the short-term accumulated precipitation and radar reflectivity composite. Hu et al. (2020) adopted the technique of Fierro and found, as also previously reported, a wet bias in the model that increased with the forecast time. The method still misses a suppression of spurious convection in regions without lightning. They also conducted a layer depth sensitivity study with similar results for adding q_v in layers of 2km to 10km depth. Kong et al. (2020) present an LDA of real GLM data in an EnKF framework. FED at 10km pixel resolution is assimilated using both graupel mass and graupel volume-based observation operators, with positive results on the convection forecasts. LDA of Chinese satellite Fengyun-4 (FY4) lightning data was realized by Liu et al. (2020) through creating pseudo-RH profiles and by Chen et al. (2020) through retrieving maximum proxy-reflectivity and finally pseudo-reflectivity profiles from the lightning data.

The main goal of this work is to develop a 3DVar LDA for MTG-LI data to improve analyses and forecasts, especially in convective situations. Pseudo-observations of the MTG-LI are generated to form the lightning data base (Section 3). A novel LDA scheme is developed for the regional, operational, convective-scale model AROME-France of Météo-France. Various approaches in which FED is assimilated together with or without radar reflectivity and Doppler wind are compared to assess the added value of the developed LDA. Recent Var LDAs using GLM data, e.g., Fierro et al. (2019); Hu et al. (2020) cannot suppress spurious convection. Our LDA of GEO lightning data should promote convection if needed and also suppress spurious convection.

The NWP model configuration and lightning data as used for this work are briefly explained in Sections 2 and 3, respectively. Section 4 introduces the lightning observation operator developed for this study. Then, our LDA method and the model experiments are explained in Sections 5 and 6. Section 7 ~~describe~~ describes the AROME-France analysis resulting from LDA. One of four case studies is detailed using different assimilation experiments, including the new LDA. Finally, Section 9 concludes this work.

2 Model configuration

AROME-France is the convective-scale, limited-area model run operationally by Météo-France since 2008 (Seity et al., 2011). It provides 36 to 42-hour forecasts five times a day (00 UTC, 03 UTC, 06 UTC, 12 UTC, 18 UTC). After an update in 2015, the model grid comprises 1440×1536 grid points in the horizontal with uniform 1.3km horizontal resolution. The physical model domain and model topography are shown in Figure 1. In the vertical, the lowest model level is situated at around 5m above ground. Each column extends up to pressure level 10hPa. The vertical resolution is refined homogeneously from top to bottom by a factor of 1.5. In total, 90 vertical levels (33 levels below 2000m) are computed. Model time steps equal 50s. Model dynamics are non-hydrostatic, semi-implicit, and semi-Lagrangian. Lateral boundary conditions (LBCs) are extracted from the global model ARPEGE (Bouyssel et al., 2022). AROME-France features a Davies relaxation (Davies, 1976) coupling and ARPEGE synchronization. The initial conditions rely on a 3DVar data assimilation technique (Section 5).
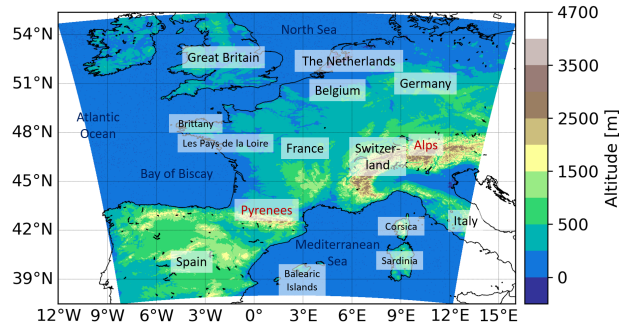
Figure 1. AROME-France physical domain and model topography. The AROME-France horizontal grid is equidistant at 1.3km resolution.

Deep convection is expected to be mostly resolved on the model grid (Fischer et al., 2018). Parametrization of sub-grid scale shallow convection is based on Pergaud et al. (2009). AROME-France uses a mixed-phase microphysical scheme with riming processes and graupel (Seity et al., 2011). In particular, the microphysics scheme of AROME-France separates five prognostic hydrometeor variables, that are specific contents of precipitating species rain (q_r), snow (q_s), and graupel (q_g) and the two non-precipitating species ice crystals (q_i) and cloud droplets (q_c). In addition, the water vapor specific content q_v (also termed specific humidity) is computed. Hail is assumed to behave as large graupel particles. Overall, more than 25 processes are parametrized into the microphysics scheme (Lascaux et al., 2006). AROME-France physics include a 1-dimensional (1D) turbulence parametrization as combination of a prognostic turbulent kinetic energy (TKE) equation with a diagnostic mixing length. An Externalized Surface (SURFEX) scheme and the European Center for Medium-Range Weather Forecasts (ECMWF) radiation parametrization are other components of AROME-France model physics. Details can be found in Seity et al. (2011); Brousseau et al. (2016).

3 Lightning data

This work adapts the GEO lightning pseudo-observation generator as developed by Erdmann et al. (2022). It was trained using low frequency (LF) ground-based National Lightning Detection Network (NLDN) records collected over the South-East US. The LF ground-based lightning observations in this study are provided by the French network Meteorage (Schulz et al., 2016; Pédeboy, 2015) as input. Meteorage locates total lightning with a discrimination between CG strokes and IC pulses. They are clustered to the flash level data using the same method as Erdmann et al. (2020), i.e., a spatiotemporal clustering with criteria of 20km and 0.4s. To verify Meteorage data as suitable input to the generator, Meteorage and NLDN observations were compared to space-borne ISS-LIS data as common reference (Erdmann, 2020): The flash detection effiency (DE) of NLDN relative to ISS-LIS was about 76%. ISS-LIS detected about 59% of the NLDN flashes. In France, Meteorage flash DE relative to ISS-LIS was about 83% while ISS-LIS detected about 57% of the Meteorage flashes. It should be mentioned that the low earth orbit, optical ISS-LIS observes lightning in a different way than the ground-based LF networks, with different detection efficiencies for CG and IC flashes, respectively (e.g., Erdmann et al., 2020; Zhang et al., 2019). The statistical evaluation of general

flash characteristics revealed that NLDN and Meteorage flashes feature similar distributions of flash extent (average of about 7.0km), flash duration (average of about 0.2s), stroke/pulse number per flash (average of about 3.6). Meteorage, with shorter baseline distance than NLDN, recorded on average higher LF currents for the occurring flashes (average of 9.5kA and 8.3kA for Meteorage and NLDN, respectively). In all cases, flashes with large extent, long duration, or with a high number of ISS-LIS events or LF strokes/pulses were more likely detected by both LLSs than the small, short duration flashes. Overall, Meteorage was validated as a suitable input to the GEO lightning pseudo-observation generator. Pseudo-observations of MTG-LI are then generated on a regular latitude-longitude grid with average pixel resolution of 7km, which approximates the expected MTG-LI resolution over France (personal communication Bartolomeo Viticchiè, 2020). FEDs are calculated per 5-minute interval that can then be summed as needed for the assimilation. This work uses a 10-minute interval of FED data in the LDA that is centered at the time of the analysis (as done by Fierro et al., 2016; Hu et al., 2020). The short period around the analysis reduces displacement errors in the analysis. The domain is limited to 40°N to 51°N and 5.5°W to 10°E, which is inside the AROME-France physical model domain. The pseudo MTG-LI FED is referred to as FED observation hereafter to avoid confusion with the pseudo-observations (POs) created by the 1-dimensional Bayesian (1DBay) retrieval.

An example of simulated MTG-LI is provided in Figure 2(a) for the entire study domain, and Figure 2(b) zoomed on the FED maximum on 09 Aug. 2018, 13:55 UTC to 14:00 UTC. The regular latitude-longitude grid of the FED is obvious in Figure 2(b). Throughout the domain, the FED pixels have a size of roughly 7km times 7km.

Figure 2(c) superimposes the zoomed-in simulated FED and the Meteorage CG strokes and IC pulses that were used as input to the GEO lightning pseudo-observation generator. The vast majority of strokes and pulses lies within the area of non-zero FED. Figure 2(d) illustrates that the simulated MTG-LI flash centroids are situated within the corresponding Meteorage stroke and pulse distribution.

4 Lightning observation operator

Previous studies suggest that graupel is a reliable proxy for lightning (see Section 1). Our observation operator is trained using the relationship found between MTG-LI FED observations and simulated graupel mass (m_g) from the 1-hour forecast of AROME-France, for 24 days in 2018 (2 days per month). FED time periods of 10min are used (e.g., as in Fierro et al., 2016; Hu et al., 2020) centered at the corresponding time of the AROME-France analysis. The m_g profile is extracted from the AROME-France grid point closest to the FED pixel center. Thus, one specific m_g profile is related to one FED value. This gives an equal count of FED and column integrated m_g values that are used to train and validate our observation operator. Following Deierling et al. (2008), m_g is taken from layers where the temperature was below -5°C. As a reminder, AROME-France graupel mass combines graupel and hail. All FED and column graupel mass values are further processed as climatological distributions (see Figure 3) regardless of observation location and time. This approach is different from Deierling et al. (2008); Barthe et al. (2010) who used storm-based relationships of case studies, and from McCaul et al. (2009) who used the domain-wide peak values. Pixel-to-pixel m_g and FED were barely correlated in our study, with about 0.09 Pearson correlation coefficient, likely as a consequence of a typical displacement of convection in the model by more than the FED spatial resolution of 7km. The
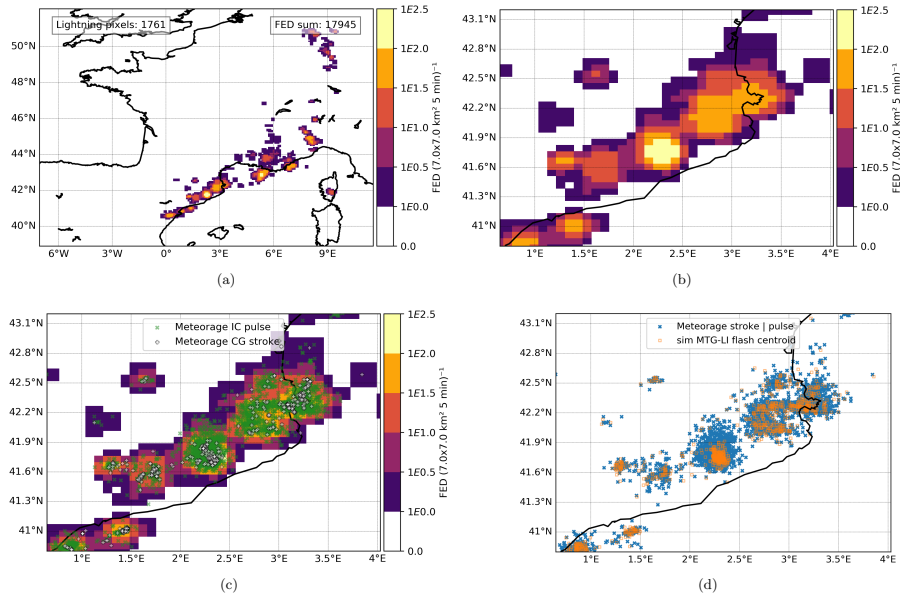
Figure 2. Simulated MTG-LI FED in the entire domain (a) and zoomed on the region of the maximum FED value (b) on 7km × 7km grid. The Meteorage strokes and pulses that were used to generate the MTG-LI flashes are superimposed on the FED in (c). Simulated MTG-LI flash centroids and the corresponding Meteorage strokes+pulses in (d). Example for the period from 09 Aug. 2018, 13:55 UTC to 14:00 UTC.

second approach with domain-wide peak values was not further tested as it reduces the sample size for a regression analysis
180 drastically. Our observation operator uses a simple linear regression between observed FED and simulated column graupel mass. It is unbiased by definition. Our approach optimizes both the slope factor and the y-intercept of the regression, whereas, e.g., McCaul et al. (2009) only used a proportionality between FED and a proxy.

Figure 3 presents the analyzed linear relationship between FED and column integrated graupel mass m_g. The functions are obtained after sorting both the FED and m_g data individually. Paired datapoints in Figure 3 are geographically independent
185 values as described in Combarnous et al. (2022). It should be noted that all pixels with either FED equal to zero or m_g equal to zero are removed from the data. The observation operator represents the cases when lightning was actually observed. The training data (24 days) results are shown in Figure 3(a) and the results for 06 and 07 October 2018 as validation period can be seen in Figure 3(b). The Pearson correlation coefficient equals 0.97 for the training data and 0.92 for the validation data (0.96 combined).

190 Analyzing the training data, the linear relationship fits the majority of the data well. A discrepancy is identified for the largest graupel mass and FED values (Figure 3). Here, the observation operator tends to underestimate the FED for a given graupel mass. The high values (of both FED and graupel mass) are rare relative to the lower values as indicated by the colored pixels in Figure 3(a). Hence, this observed discrepancy litte affects the Pearson correlation coefficient. It should still be considered that high FED values are systematically underestimated. It is further noted that the y-intercept is negative, meaning that statistically
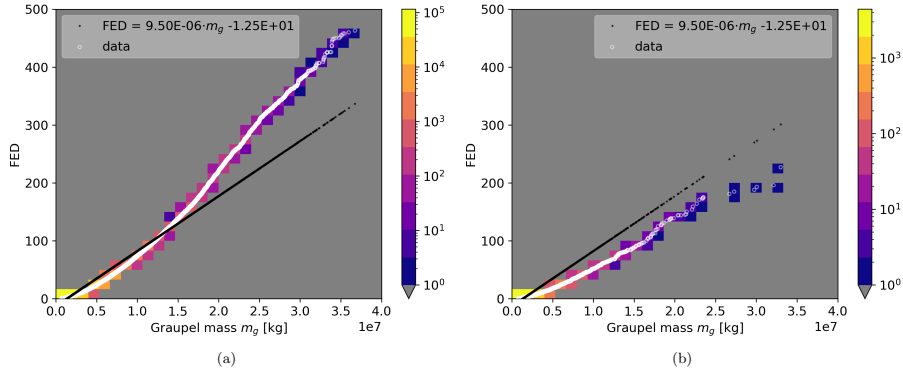
Figure 3. The observed FED, per 10min and on 7km × 7km pixels, climatological distribution versus the climatological distribution of AROME-France graupel mass m_g at model grid points closest to each FED observation. The graupel mass is integrated vertically over the AROME-France grid point for a 1.3km × 1.3km pixel. Grid points with any of FED or m_g equal to zero are not considered. (a) shows the training of a linear regression for 24 days in 2018, and (b) shows the results of a validation for independent data of 2 additional days in 2018. Colors indicate the number of samples, the white circles plot the data points, and black dots applied the m_g values in the linear regression equation (see Figure legend).

a certain mass of graupel is required to initiate lightning. This result is well in accordance with the widely accepted non-inductive charging as main electrification process in extratropical storms.

The validation data (Figure 3(b)) roughly follow the regression line inferred from the training data. One can see, however, that the slope is smaller than that of the black regression line, i.e., observed values of FED are always lower for a given m_g than the training data implies. The number of FED-m_g-pairs is significantly lower for the 48-hour validation case than for the 24-day training dataset. Furthermore, the validation data comprises one single meteorological situation, while the training data includes several weather situations in different seasons. The observed discrepancy is considered during the evaluation of results.

5 1DBay+3DVar assimilation method

FED cannot be assimilated directly since lightning is not predicted by AROME-France. The previously described observation operator relates the FED observations to the prognostic variables of the NWP model and allows for comparing background and observations. The final step prior to the assimilation creates pseudo observations that can be ingested in the 3DVar system. Unlike Fierro et al. (2019); Hu et al. (2020) and others who used an empirical method to adjust moisture in thunderstorms, the expected water vapor PO is retrieved for each model grid column (applying Bayes' Theorem) in a 1DBay approach. This allows to i) replace the humidity field in spurious convection areas with that of their convection-free environment, and thus in principle abolish the wet bias that results from data assimilation techniques that only consider the occurrence of lightning (e.g., Fierro et al., 2012, 2019; Hu et al., 2020), and ii) make use of the FED value to modulate the humidity field in observed

lightning areas by leveraging the model's ability to create consistent, flow-dependent humidity and graupel profiles near the observation. Technically speaking, synthetic profiles are created and assimilated as sounding data.

5.1 1DBay retrieval

215 All FED values are transformed to units of dB as $10 \cdot \log_{10}(\text{FED}/(7\text{km} \times 7\text{km} \ 10\text{min})^{-1})$ to account for the large range of scales, referred to as dBFED. FED equal to zero is transformed to dBFED of -10dB. In general, dBFED below 0dB means linear FED less than 1^1 $(7\text{km} \times 7\text{km} \ 10\text{min})^{-1}$, i.e., no lightning activity. The 1DBay retrieval of POs of relative humidity RH, $y_{\text{po}}^{\text{RH}}$, is defined as

$$y_{\text{po}}^{\text{RH}} = \sum_i x_i^{\text{RH}} \frac{W_i}{\sum_j W_j} \tag{1}$$

220 with the weights W_i for each point as

$$W_i = \exp\left\{-\frac{1}{2} \frac{[\text{dBFED} - \text{dBFFO}(x_i)]^2}{\sigma_o^2}\right\} \tag{2}$$

where i, j are counters for the grid points within the defined area, referred to as vicinity, FFO means the FED forward operator as specific observation operator, and σ_o the standard deviation of the 1DBay retrieval. $\text{dBFFO}(x_i)$ then defines the simulated AROME-France dBFED ~~from using dB units for~~ by converting the output of the FFO to dB units.

225 Equations (1) and (2) can be used with different model variables or diagnostics, e.g., the sensitivity test for σ_o as described in the following used x_i^{FED} rather than x_i^{RH}.

Each RH PO is the best estimation from a weighted linear combination of RH profiles taken from the model background in the vicinity of the FED observation.

The method was proposed by Caumont et al. (2010), used in the operational model AROME-France (Wattrelot et al., 2014), 230 and applied by Borderies et al. (2019) for radar reflectivity data, and Duruisseau et al. (2019) for microwave radiances. Here, weights are calculated based on differences between observed and simulated FED. The 1DBay retrieves the best estimate of RH at the center of each observed FED pixel from the background using Bayes' Theorem. It is expected that the model can predict a quantity similar to the observation within a certain area in most cases. The vicinity is initially fixed to a square of 160km × 160km centered at the observation. This size follows the suggestion of Borderies et al. (2018, 2019). However, the 235 FED pixels (about 7km) are significantly larger than the radar reflectivity pixels (about 1km) and a given vicinity contains less FED than radar datapoints to retrieve the expected profile. Hence, the vicinity is adapted to the specifications of the FED data. 1DBay vicinities of 160km, 320km, and 500km were tested regarding the RMSE between observed FED and retrieved FED (not shown). It was found that larger vicinities give lower overall RMSE as there are more background profiles to feed the retrieval and to find grid points that are similar to the FED observation. In consequence, all LDA experiments presented in the 240 following use a 1DBay vicinity of 500km.

The database comprises model forecasts at the observation time and in the vicinity of the observation location. Since FED has no vertical dimension, the covariance matrix is reduced to a single value of variance, σ_o^2, which is assumed to be constant.

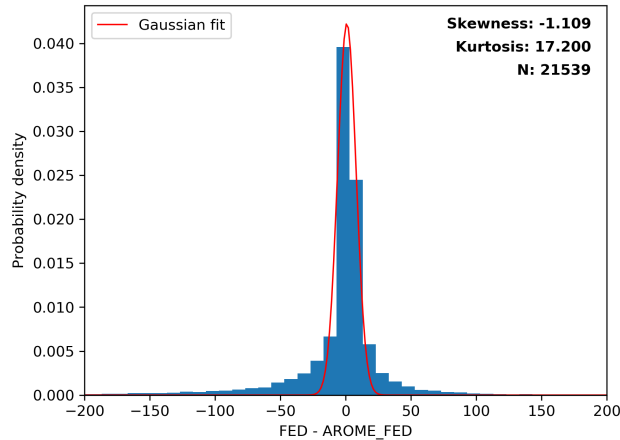[1] Non-integer FED values are possible when applying the observation operator.

Figure 4. Innovations of FED observation minus AROME_FED for the 24-hour assimialtion ~~cylces~~ cycles on 08 Aug. 2018. Skewness, kurtosis, and the sample size N are given. The red line shows the Gaussian fit on the PDF of the innovations.

A small σ_o means that the retrieval favors columns with values close to the FED observation. This can produce accurate retrievals; however, no retrieval can be created when the difference between all simulated FED in the vicinity and the observed FED is large relative to σ_o (see Equation (2) where weights approach 0 in that case). Large values of σ_o cause smoothing over all grid points in the vicinity of the observation. In that case, the likelihood to retrieve POs is high, at the cost of a less accurate retrieval potentially independent of the observation.

An assumption of the Bayesian retrieval is that differences between the observation and the model background, referred to as innovations, are Gaussian distributed. Figure 4 shows the PDF of innovations (dBFED observation minus AROME_dBFED) for the 24-hour assimilation ~~cylces~~ cycles on 08 Aug. 2018. The distribution is bell-shaped and centered at 0. It is symmetric and the skewness is close to 0. Although the kurtosis is higher than for a classical Gaussian distribution, this distribution of innovations sufficiently fulfills the assumption of the 1DBay method to justify its use in this study.

The value for the standard deviation σ_o of the observation and observation operator is inferred from a sensitivity study. It aims at minimizing the root mean square error (RMSE) between observed and retrieved pseudo FED for the 24 training days also used in Section 4. Pixel-to-pixel RMSE is used for all non-zero FED pixels and 10-minute intervals centered at each full hour. The pseudo FED is computed from joint use of the observation operator and the 1DBay retrieval. Figure 5(a) shows the curve of the RMSE between dBFED observation (from pseudo MTG-LI) and retrieved pseudo dBFED from the 1DBay retrieval for different σ_o. The RMSE between AROME-France background dBFED (AROME_dBFED), that was obtained from the observation operator without additional 1DBay, is shown as reference. Including the 1DBay retrieval (blue curve in Figure 5(a)) produces pseudo dBFED much closer to the dBFED observation, i.e., lower RMSE, than the AROME_dBFED (orange curve in Figure 5(a)). The minimum RMSE for the retrieval is found at σ_o of 2.0dB. This value is used for retrieving the pseudo-RH profiles in the following.
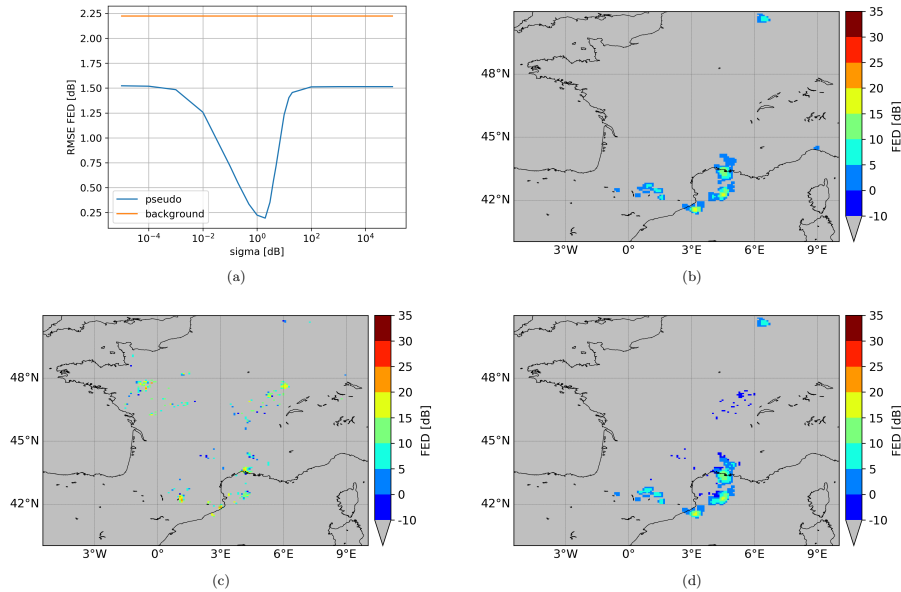
Figure 5. (a) The sensitivity test for standard deviation σ_o of the 1DBay retrieval as inferred from the pixel-to-pixel RMSE between the dBFED observation and the AROME_dBFED (background) as well as the 1DBay retrieved pseudo dBFED (pseudo). 07 Oct. 2018, 00:00 UTC, case with the MTG-LI dBFED observation (b), the model background AROME_dBFED (c), and the 1DBay retrieved pseudo dBFED with a σ_o of 2 (d). Grey color means no lightning.

Case studies of fields of observed, background, and retrieved dBFED are conducted to visualize the effect of σ_o on the pseudo dBFED. The example of 07 Oct. 2018, 00:00 UTC is presented in Figure 5(b-d). The dBFED observation in Figure 5(b) shows

265   lightning activity mainly in the south center of the domain. Figure 5(c) indicates positive background dBFED in the region of lightning observations, however, also widespread near the center of the domain and over western France. The map of the 1DBay retrieved pseudo dBFED in Figure 5(d) demonstrates that the method effectively reduces the spurious dBFED in these regions (retrieved dBFED below 0, grey and marine blue). In some regions, the 1DBay retrieves pseudo dBFED to completely remove the spurious lightning, e.g., over western France and for some grid points over Switzerland. Spurious high values

270   of AROME_dBFED near the center of the domain (Figure 5c) are effectively decreased to negative dBFED (marine blue in Figure 5d) in other words no lightning activity, similar to the observation in that region (Figure 5b). Furthermore, the pseudo dBFED values and areas of positive pseudo dBFED in the south center of the domain closely match the dBFED observation. The observed, weak dBFED over the Gulf of Genoa could not be reproduced by the 1DBay retrieval as the background does not provide any positive dBFED in the retrieval vicinity.

275   An additional method, the humidity adjustment (HA), is applied if lightning (i.e., positive FED) is observed but all background FED values in the vicinity are zero. In this case, there is no estimated profile at this point and all W_i in the vicinity equal zero. The HA is also applied if all background dBFED values within the vicinity of the FED observation are at least 10dB smaller than the observed dBFED value. Although the sum of W_i can become greater than zero in this case, the retrieval

would generate a profile that is too dry with respect to the FED observation. To produce RH POs, the layer between lifted condensation level (LCL) and 13km is saturated (i.e., RH set to 100%) at all levels where the modeled RH is less than 100%. This is conceptually similar to the method of Fierro et al. (2019), among others. However, the HA is only applied for few pseudo-RH profiles where the 1DBay method did not retrieve POs. ~~In example~~For instance, the HA ~~generates~~ only contributes to 1.6% of almost 20,000 assimilated profiles during 08 Aug. 2018, the study case that is detailed below.

Another case with Equations (1) and (2) equal to 0 for all weights may occur if the observed FED equals 0 and the background FED is positive for all grid points in its vicinity. This behavior was observed for the initial 160-km vicinity, but not within the 320-km and 500-km vicinity. Thus, if the vicinity has a sufficient size, there are background grid points without lightning activity that can be used in the 1DBay retrieval. If, however, the specified vicinity were too small, one would need to artificially remove spurious FED, i.e., convection and humidity, from the model.

Eventually, no pseudo-RH profiles are created if both the observed FED and the closest (in space) AROME-France background FED equal zero.

It should be mentioned that the 1DBay retrieval method was initially developed and applied to retrieve humidity and cloud profiles from passive and active remote sensing data (e.g., Olson et al., 1996; Kummerow et al., 2001). Caumont et al. (2010) brought this approach forward by restricting the 1DBay method to use model profiles at the forecast time and in the neighborhood of the observation. This approach was successfully applied by Wattrelot et al. (2014); Borderies et al. (2019) for radar reflectivity assimilation in AROME-France. However, a 1DBay has not yet been used to retrieve humidity profiles from FED data. Whereas an FED greater than zero is always related to the presence of graupel and thus a RH profile with a cloud, an FED equal to zero does not necessarily mean a location without cloud coverage. It is the same problem which is faced for radar reflectivity, but presumably more marked than for the centimeter wavelength radars (Caumont et al., 2010) and even more than for the millimeter wavelength radars which are even more sensitive to the small hydrometeors (Borderies et al., 2019). In addition, FED is a 2D variable without vertical extent while the 1DBay retrieves vertical RH profiles. The use of integrated column graupel mass as proxy addresses the latter aspect by converting the 3D AROME-France outputs into a 2D variable comparable to FED. RH-profiles are assimilated since assimilating hydrometeor contents when VAR is able to update these variables often results in poor performances because the cross correlations with key variables such as temperature and humidity are poorly represented in climatological $\mathbf{B}$ matrices. To mitigate this effect, some recent studies assimilate humidity along with hydrometeor contents (see, e.g., Wang et al., 2013; Do et al., 2022, for radar reflectivity).

5.2 3DVar assimilation

The retrieved pseudo-RH profiles are assimilated as sounding data in the 3DVar assimilation system of AROME-France. AROME-France uses a one-hour assimilation window. The short assimilation cycles aim at partially overcoming the missing temporal dimension and at allowing the assimilation of more high-frequency observations that can improve the initial conditions especially on the convective scale. AROME-France operationally assimilates surface (e.g., ground-stations, ships, buoys) and aircraft measurements, Global Positioning System (GPS) Zenith Tropospheric Delay (ZTD) data, satellite brightness temperatures of several polar orbiting satellites and from Meteosat Second Generation (MSG) SEVIRI, satellite-based atmospheric

motion vectors, and radar velocity and reflectivity data (Seity et al., 2011; Brousseau et al., 2016). The control variables are temperature, specific humidity, surface pressure, and horizontal wind components. The 3DVar system minimizes the 3DVar
315   cost function J of the state vector x:

$$J(x) = \frac{1}{2}(x - x_b)^T \mathbf{B}^{-1}(x - x_b) + \frac{1}{2}[y_o - H(x)]^T \mathbf{R}^{-1}[y_o - H(x)] \tag{3}$$

with the state vector of the background x_b, the observation vector y_o, the observation operator H, and the observation error covariance matrix $\mathbf{R}$. The climatological background error covariance matrix $\mathbf{B}$ is inferred from offline AROME-France ensemble assimilation as a multivariate set of calculations for the control variable covariances and cross-covariances (Brousseau
320   et al., 2014).

6   Experimental set-up

This section evaluates the effect of LDA relative to RDA. Since the application of the 1DBay retrieval for FED data constitutes a new approach, different experiments of AROME-France with respect to LDA are conducted. All experiments are initiated at 0000 UTC and run for a forecast period of 30 hours until 0600 UTC the following day.

325   Table 1 lists the six different assimilation experiments. First, there is a control experiment used as reference without RDA, without Doppler wind velocity assimilation, and without LDA. It is called *CTRL*. The second experiment includes the use of radar data and is similar to the current operational AROME-France. It is referred to as *RDA*. All RDA experiments shown here assimilate both reflectivity and Doppler wind velocity.

While analyzing first LDA experiments, it was evident that the use of all FED observations led to wrong results, i.e., the
330   changes to the AROME-France background humidity contradicted the assimilated pseudo-RH profiles (not shown). This behavior is known to occur because the $\mathbf{R}$ matrix is diagonal whereas observation error cross-correlations are actually present, which leads to sub-optimal solutions (e.g., Rabier, 2006). It could be mitigated by reducing the number of assimilated observations (*thinning* Järvinen and Undén, 1997). In this work, FED data are thinned by a factor of 2 in latitude and longitude direction, i.e., 1 in 4 observations are assimilated, so that no observations of adjacent FED pixels are used. Tests revealed
335   that this thinning was sufficient to eliminate the FED observation error correlations. For comparison, 1 in 64 radar observations, with a higher horizontal resolution than our FED data, are assimilated in AROME-France (Michel, 2018). The thinning, thus, prevents from assimilating observations with correlated observation errors, which would contradict the assumption of a diagonal $\mathbf{R}$ matrix. The resulting LDA without RDA is labeled *LDA*.

The second LDA experiment without RDA ,*LDAnC*, adds a so-called *noCloud*-filter. This *noCloud*-filter is utilized for
340   locations where the observed FED equals zero but the AROME_FED exhibits lightning activity. Then, the distance to the closest positive FED observation, d_{FED}, is computed. If d_{FED} remains within 21km, i.e., a maximum of three FED pixels, it is assumed that the profile is still situated within the same thundercloud being responsible for observed FED greater than zero. In this case, the RH profile of the background is kept to avoid reducing the RH if observed FED equals zero but the location is likely associated with a cloud. In the case where d_{FED} exceeds 21km, AROME-France profiles within 21km are

Table 1. Simulation and assimilation techniques of the different AROME-France experiments. They differ by the use of radar data assimilation (RDA) and lightning data assimilation (LDA), as well as the application of the *noCloud*(nC)-filter as described in the text.

Experiment	Assimilation	*noCloud*-filter
R (CTRL)	Reference (control)	no
RDA	CTRL + RDA	no
LDA	CTRL + LDA	no
LDAnC	CTRL + LDA	yes
RDA_LDA	CTRL + RDA + LDA	no
RDA_LDAnC	CTRL + RDA + LDA	yes

not considered in the 1DBay as they probably belong to spurious simulated thunderclouds. Hence, the *noCloud*-filter should help to effectively reduce background humidity in spurious convection.

The two remaining experiments combine both LDA methods with RDA. They are labeled *RDA_LDA* and *RDA_LDAnc*, respectively.

All model experiments are initiated one day prior to the start of the model forecast. During the first 24 hours, the 3DVar assimilation system of AROME-France creates 23 analyses (there is no analysis for the time of initialization). The reference, LDA, and RDA experiments are conducted for 23 hours prior to the evaluated analysis. This time period has been chosen because convection was continuously observed inside the model domain. In addition, the long assimilation period allows AROME-France to efficiently ingest all available observations.

7 The AROME-France analysis and forecast assimilating FED observations

This section describes the LDA ability to modify and update the model background. The following sections briefly introduce the four test cases, detail one case, and discuss i) the LDA effects on the AROME-France background and ii) AROME-France rainfall forecasts for this selected case. AROME-France simulations are mainly analyzed for the first 12 hours of the forecast since the strongest impacts of RDA and LDA are expected during these forecast hours, as seen in Fierro et al. (2019), for example. The influence of the lateral boundary conditions becomes predominant after 12 hours (Vié et al., 2011).

7.1 Case 1: 08 to 10 August 2018

Strong convection and lightning activity was observed over France on 07 Aug., and the electrical cells were still active over northern France and Belgium during the early hours of 08 Aug. Moist and warm air created unstable conditions over southeastern France where lightning was observed during the entire day. Whereas a dominant southwest flow was present aloft, winds in lower levels were calm but caused slight warm air advection. The 2-meter temperatures reached up to $33°C$ while the dew point temperatures exceeded $20°C$ over southwestern France. CAPE values far beyond $1000 \mathrm{Jkg}^{-1}$ indicated potential for
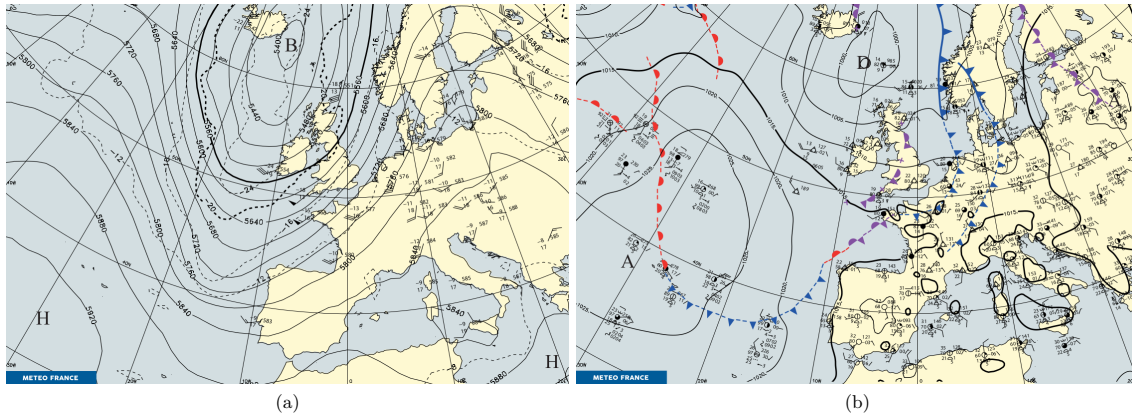
Figure 6. (a) Météo-France 500hPa analysis of geopotential height (in geopotential metres, gpm, solid lines) and temperature (in °C, dashed lines) with centers of low ("B") and high ("H") geopotential, and (b) Météo-France surface analysis with low- and high-pressure centers shown as "D" and "A", respectively, on 08 Aug. 2018, 12:00 UTC. Surface (altitude) low-pressure centres are indicated by "D" ("B") and high-pressure centres by "A" ("H"). Maps from the Météo-France daily weather bulletin archive https://donneespubliques.meteofrance.fr/?fond=produit&id_produit=129&id_rubrique=52 (accessed 19 October 2022).

widespread deep convection and thunderstorm activity. Figure 6(a) and (b) show the 500hPa map and surface analysis, respectively, on 08 Aug. 2018, 12:00 UTC. The amplifying trough over the Atlantic is evident, and the major cold front was about to enter the study domain at this time. In the evening of 08 Aug., the trough that was situated over the Atlantic amplified and the associated cold front started to impact the weather in the domain. Strong convective cells formed over Spain and propagated

370 all the way over France to Belgium and western Germany following the air mass boundary and the eastward movement of the trough. The storms left the study domain in the afternoon of 09 Aug. At that time, new cells formed over southeastern France and remained quasi-stationary until the end of the day. Then, only few cells developed over the northern Mediterranean Sea until the end of the forecast period. The 30-hour forecast starts 09 Aug. 2018, 00:00 UTC, preceded by a 24-hour period with hourly data assimilation.

375 **7.1.1 AROME-France analysis**

Details to create the AROME-France analysis are presented in Figure 7 for experiment *LDAnC* on 08 Aug. 2018, 23:00 UTC. The first row of the figure (a-c) includes (a) the AROME_dBFED, (b) the 1DBay dBFED, and (c) the dBFED observation. AROME-France could not predict most of the lightning activity over the Bay of Biscay and southwestern France (a and c; see Figure 1 for the locations of the regions of interest). The region of the highest observed dBFED is correctly predicted, however,

380 with underestimated dBFED values (Figure 7 a,b versus c). The 1DBay dBFED (Figure 7b) shows positive dBFED patterns that match the observed dBFED (Figure 7c) despite the fragmented dBFED in the AROME-France background (Figure 7a). Hence, Figure 7(g) shows that IWV is added to the background in regions where the AROME-France background underestimates the dBFED. Over southern France, the marine blue spots in Figure 7(b) indicate that the 1DBay retrieval succeeds in reducing the

15

spurious AROME_dBFED (Figure 7a versus c). Hence, IWV should be reduced here by the assimilation. Consequently, the

385 PO IWV (Figure 7e) clearly decreases compared to the background IWV (Figure 7d) as shown in Figure 7(g). In addition, the LDA experiment reduces the model IWV at rare locations where the AROME_dBFED exceeded the observed dBFED, e.g., due to a slight spatial shift of the local dBFED maxima at about 44.3°N and 0.8°E (compare Figure 7a,c and g at this location).

The 1DBay method aims at finding the profiles that are physically consistent with FED observations in terms of relative humidity. Indeed, the analysis (Figure 7f) adds humidity to the background over the southwestern regions and for the cell

390 over eastern France. It can also be seen in the difference between analysis IWV and background IWV (Figure 7i) where LDA reduces model IWV where spurious lightning activity was predicted. In addition, Figure 7(h) displays the IWV as output of the 1DBay retrieval method where no background IWV is included. It is intended that the 1DBay retrieves complete profiles, whereas the HA only adds humidity to certain layers. A smaller IWV from pure PO (Figure 7(h)) than from background plus PO (Figure 7(e)) means that the HA method was used. The comparison of Figure 7(e) and (h) shows the same IWV values

395 for most points with PO. This result means that the HA is rarely used, and the preferred 1DBay method, that retrieves flow consistent PO profiles, is mostly used to get the POs.

Figure 8 illustrates RH vertical structure on the 44°N latitude between 4°W et 5°E at the same time as fields in Figure 7 are taken. AROME-France background RH (a) and the difference of analysis minus background (b) are included. The latitude was chosen as the analysis increases and decreases the background IWV here (Figure 7i). The latitude also exhibits regions

400 where AROME-France over- and underestimated the FED (Figure 7a,c). In Figure 8(b), higher RH in the analysis than the background (positive values) from 4°W to 2°W (-4 to -2 in the figure) corresponds well with Figure 7(g, i) where humidity as evidenced by IWV was added to the background since AROME_FED was lower than the FED observation. RH is reduced in columns near 4°E where spurious AROME_FED was found (Figure 7a,c). Figure 8 also shows that the RH is not changed when observed FED was higher than AROME_FED but the background RH was at least 100% (e.g., altitudes up to 4km and

405 from 4°W to 2°W). All in all, the vertical cross-section shows that changes induced by the LDA result in physically consistent analysis in the vertical struture.

7.1.2 AROME-France rainfall forecasts

The *Antilope* rainfall accumulation (RA) combines the data of the operational radar network of Météo-France and rain gauges on a 0.01°resolution grid at each hour (Laurantin, 2008, 2013). RA maps for the first 6 hours of the forecast are shown in

410 Figure 9a to d for (a)*Antilope* and experiments (b)*CTRL*, (c)*RDA*, (d)*LDA*, and (e)*LDAnC*.

Three major thunderstorm tracks, labeled 1 to 3 from north to south hereafter, produce the bands of high RAs over the northwestern part of the domain (Figure 9a). The local maximum with very high RA up to 150mm per 6 hours over southern France is caused by a quasi-stationary thunderstorm development. The AROME-France experiments (Figure 9b-e) predict the RA of track 1 relatively well. Experiment *CTRL* (Figure 9b) and the two LDA experiments (Figure 9d,e) underestimate the

415 area of high RA in the northwest of the domain for track 1. Experiments *RDA* (Figure 9c) and *LDA* (Figure 9d) ~~overestimates~~ overestimate the maximum RA over this region by about 20mm and 5mm, respectively. Track 2 is best predicted by experiment *LDA*, with good agreement in maximum RA and area of high RAs to the observation (Figure 9a). Experiment *LDAnC*
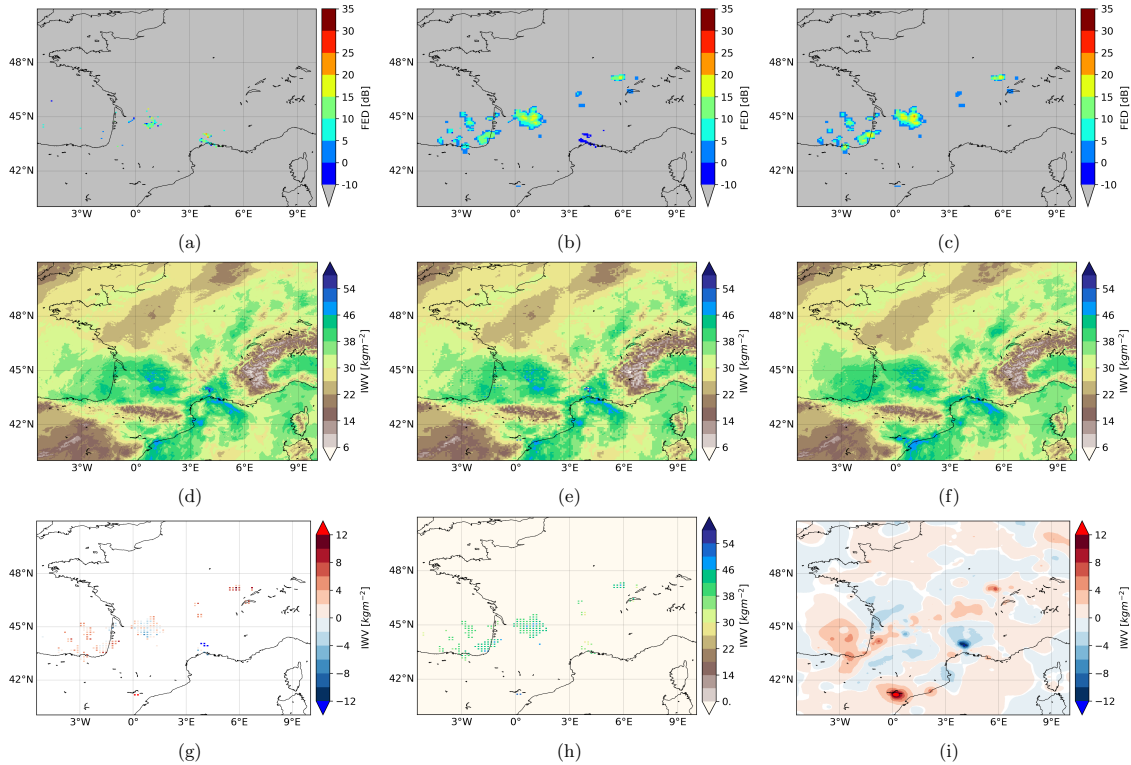
Figure 7. (a) The background AROME_dBFED, (b) the 1DBay retrieved dBFED, (c) the MTG-LI dBFED observation, (d) the AROME-France background IWV, (e) PO IWV merged with the background where no profiles were retrieved, (f) the IWV of the analysis, (g) the difference between the PO IWV minus the background IWV, and (h) the 1DBay-only IWV including only points where RH was retrieved, and (i) the difference in IWV of analysis and background. Results for 08 Aug. 2018, 23:00 UTC and model experiment *LDAnC*.

(Figure 9e) also predicts the extent of the RAs related to track 2, but underestimates the RA amounts especially for the northern part of the track, i.e., most recent storm location to the prediction time. Experiment *CTRL* and the experiment using RDA without LDA poorly predict the high RAs related to track 2. It is not clear whether the storm is modeled at all or placed too far south. RAs of track 3 are similarly predicted by the RDA and LDA AROME-France experiments that all underestimate the RA of the southern part, i.e., during the beginning of the forecast period, and overestimate the RA of the northern part of the track, i.e., the most recent RA. Experiment *CTRL* predicts the southern part of track 3 arguably better than the RDA and LDA experiments. 6-hour RAs related to the local thunderstorm over southern France are best predicted by *CTRL* and *RDA*. Both LDA experiments somewhat underestimate the local RA maximum and the area of high RAs. In addition, the LDA experiment produces a spurious, local high RA cluster over northeastern Spain.

This case study implies that LDA without both RDA and the *noCloud*-filter of FED has the highest Fraction Skill Score (FSS, not shown, see Section 8) for predicting heavy precipitation. In that it differs from the other three case studies where the
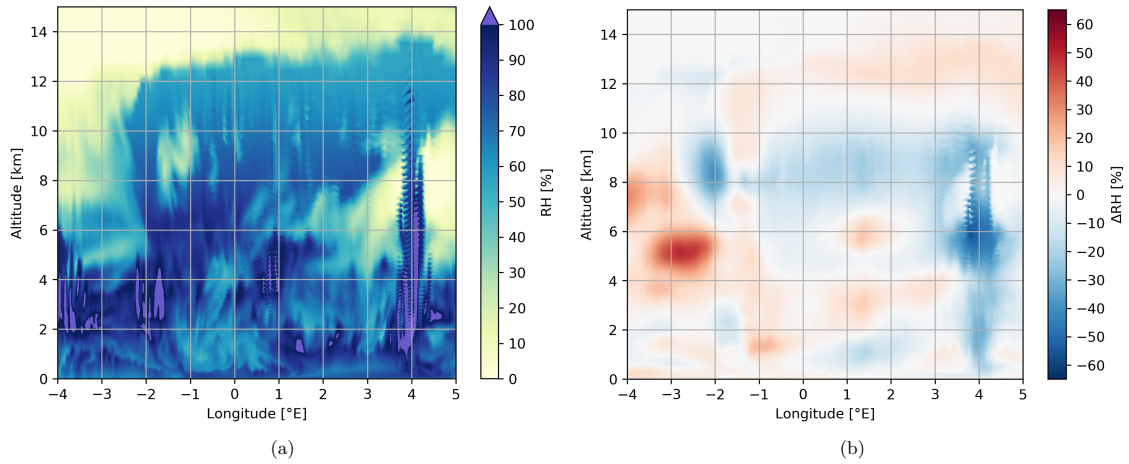
Figure 8. Vertical cross-sections ~~on~~ along 44°N of (a) the AROME background RH and (b) the difference of analysis minus background RH. Sawtooth features visible at 4°E are interpolation artefacts caused by the grid's irregularity. Results for 08 Aug. 2018, 23:00 UTC and model experiment *LDAnC*.
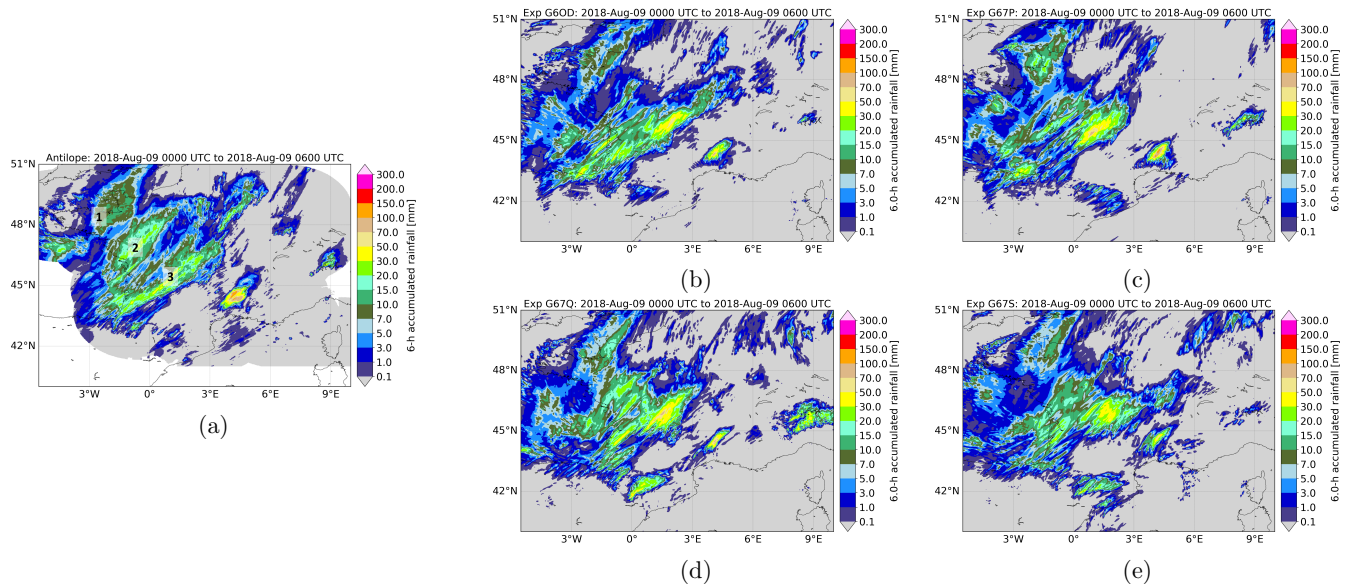

Figure 9. 6-hour rainfall accumulations (RAs) for the period until 09 Aug. 2018, 06:00 UTC, i.e., the first 6 hours of the 30-hour forecast. (a) RA observations, the AROME-France experiments (b) *CTRL*, (c) *RDA*, (d) *LDA*, and (e) *LDAnC*. Three main thunderstorm tracks are labeled with black numbers 1 to 3 in a.

Table 2. Summary of the 4 case studies.

Case	Dates (2018)	Weather conditions	Main precipitation source
1	08 to 10 Aug	instability, warm and moist low levels	deep convection, cold front
2	06 to 08 Oct	dissipating cyclone	cold front
3	01 to 03 Feb	trough and baroclinic wave	shallow convection, cold front
4	27 to 29 May	unstable conditions, low level moisture	deep convection, mesoscale system

noCloud-filter improves the LDA experiment skill. A future analysis might detail why the RDA and LDA with *noCloud*-filter
430   have lower skill than the *LDA*. Such an analysis is beyond the present proof-of-concept scope.

7.2   Cases 2, 3, and 4

All case studies are summarized in Table 2. Besides the detailed case 1, the other case studies analalyzed a cyclone with mainly
frontal precipitation in autumn (case 2), shallow convection in winter (case 3), and widespread deep convection in late spring
(case 4). The evaluation of these three cases revealed that the RDA and LDA improve the RA forecast skill for convection within
435   the study domain over western Europe. Once *RDA* and once *LDAnC* provide the best RA forecast. Experiments combining RDA
and LDA exhibit FSS values between *RDA* and *LDA*, thus, mean the best trade-off overall. In the future, a coupled assimilation
of RDA and LDA could be tested. For example, PO RH profiles could be retrieved from a weighted product that includes both
radar reflectivity and FED thereby adapting the 1DBay.

In situations, where convection from the Atlantic Ocean is advected into the study domain from the west, i.e., case 3, RDA
440   and LDA could not improve the control run. Both RDA and LDA currently rely on ground-based observations with limited
coverage over the Atlantic ocean. It is expected that the real MTG-LI observations will help to predict cloud systems forming
over the ocean with higher efficiency than the LDA using the generated MTG-LI observations derived from ground-based
observations.

8   Quantitative skill of AROME-France RA forecasts

445   This section compares the predicted 6-hour RAs of different AROME-France experiments (Table 1) and the observations in a
statistical way. The forecast skill is quantified calculating Fractions Skill Scores (FSSs). The FSS was introduced by Roberts
and Lean (2008): The FSS can be calculated as skill score from the mean squared error (MSE) for the observed and forecast

fraction $O_{(n)}$ and $M_{(n)}$, respectively, from a neighborhood of length n as

$$\text{FSS}_{(n)} = 1 - \frac{\text{MSE}_{(n)}}{\text{MSE}_{(n)ref}}$$

with

$$\text{MSE}_{(n)} = \frac{1}{N_x N_y} \sum_{i=1}^{N_x} \sum_{j=1}^{N_y} \left[O_{(n)i,j} - M_{(n)i,j} \right]^2$$

$$\text{MSE}_{(n)ref} = \frac{1}{N_x N_y} \left[\sum_{i=1}^{N_x} \sum_{j=1}^{N_y} O_{(n)i,j}^2 + \sum_{i=1}^{N_x} \sum_{j=1}^{N_y} M_{(n)i,j}^2 \right]$$

and

$$O_{(n)i,j} = \frac{1}{n^2} \sum_{k=1}^{n} \sum_{l=1}^{n} I_O \left[i + k - 1 - \frac{n-1}{2}, j + l - 1 - \frac{n-1}{2} \right]$$

$$M_{(n)i,j} = \frac{1}{n^2} \sum_{k=1}^{n} \sum_{l=1}^{n} I_M \left[i + k - 1 - \frac{n-1}{2}, j + l - 1 - \frac{n-1}{2} \right]$$

450
(4)

with the observation and forecast binary fields I_O and I_M that equal 0 if the field value is smaller than the threshold, and 1 otherwise. Our implementation uses the fast calculation of FSS in Python as proposed by Faggian et al. (2015). The FSS is calculated hourly for 6-hour RAs with a sliding 6-hour time window for the 30-hour forecast period. Forecasts are initiated at 00:00 UTC. The FSS can be generalized to yield an average score if the numerator and denominator are averaged separately

455   and then the FSS is calculated (Faggian et al., 2015). This allows to achieve overall FSSs including forecasts of all four case studies.

Here, 6-hour RA thresholds of 0.1mm, 1.0mm, and 10.0mm are used to represent different RA categories. An FSS neighborhood of 0.5°is used. Figure 10 shows the FSSs for the entire forecast period of 30 hours and combination of the four cases.

460   FSS of 0.8 to 0.9 during the first 15 hours of the forecast for the RA thresholds 0.1mm and 1.0mm (Figure 10a and b, respectively) indicate that regions with precipitation were equally well identified by all six AROME-France experiments. RDA or LDA effects on the FSS diminish beyond 12 hours of the forecast as the effect of the boundary conditions becomes predominant. The LDA without RDA and without the *noCloud*-filter (*LDA*) gains the highest FSS for the high RA threshold and during the first 12 hours of the forecast (Figure 10c). This finding demonstrates the high potential of LDA in AROME-France.

465   The *noCloud*-filter cannot always improve the LDA. *RDA* exhibits the lowest FSS during the first 6 hours of the forecast due to a low skill during the Aug case where high RAs of storm track 2 over *les Pays de la Loire* were not predicted (see also Figure 9). The combination of LDA and RDA (*RDA_LDA*) gives FSS between the skill of RDA and LDA.

This proof-of-concept study uses four cases, a rather low amount of data. Usually, scores are calculated over several months for evaluating whether a new method improves an existing NWP model. FSS curves appeared noisy for high thresholds and
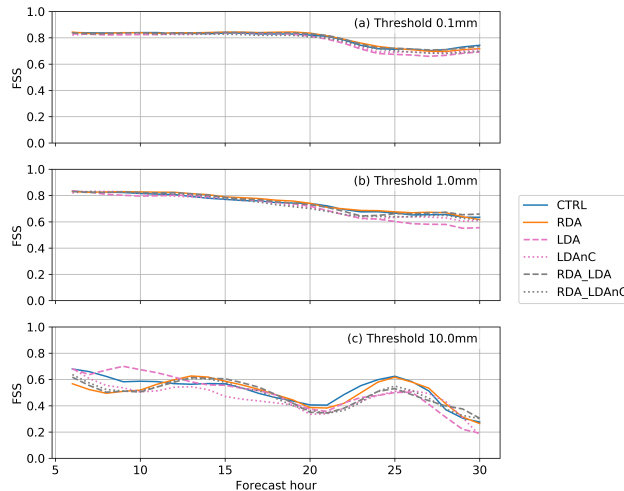
Figure 10. FSS average of 6-hour RAs calculated hourly for a sliding window during the 30-hour forecast initiated 00:00 UTC for the four study cases. The colors and line style indicate the model experiments as defined in Section 6. 3 different RA thresholds are used, (a) 0.1mm, (b) 1.0mm, and (c) 10.0mm. The size of the ~~domain~~ neighborhood used to calculate the FSS ~~equals~~ was set to 0.5°.

470   short accumulation periods (not shown) as a result. The main conclusion here is that there is likely not enough data to show significant differences, however, the encouraging point being that the effect of the assimilation is neutral.

9   Conclusions

The objective of this work is to design an assimilation technique for the upcoming MTG-LI data for the regional, convection-permitting model AROME-France. To date, AROME-France applies a 3DVar assimilation system. A tailored 1DBay+3DVar

475   assimilation technique (Caumont et al., 2010) is used to assimilate pseudo MTG-LI flash extent density (FED) in AROME-France. A similar assimilation technique is currently used operationally for radar reflectivity data assimilation in AROME-France, but has not yet been tested for LDA.

     This work first generated MTG-LI data that are used to create the FED observations (Erdmann et al., 2022). Then, an observation operator for FED is developed based on a linear, climatological relationship between observed FED and the column

480   integrated AROME-France graupel mass, m_g, above the -5°C isotherm. The operator is trained for 24 days in 2018, and validated for 2 independent days in 2018. Pearson correlation coefficients of 0.97 and 0.92 for the training and validation data, respectively, reveal a very strong relation between the distributions of observed FED and model m_g. Nevertheless, the observation operator systematically overestimates the FED for m_g values greater than 1.5e7kg per AROME-France grid cell of $1.3\text{km} \times 1.3\text{km}$. More sophisticated observation operators are currently tested (Combarnous et al., 2022) but have not been

485   included in this work yet.

21

The observation operator is then used to compare AROME-France-derived background FED (AROME_FED) to the FED observations. The 1DBay method identifies the best estimation of the FED from the background to in turn create pseudo-observations (POs) of RH-profiles based on both the FED observation and the AROME-France background fields. As background profiles are processed, the 1DBay method maintains model physics and flow characteristics.

The PO RH profiles add humidity to the AROME-France background where the observed FED exceeds the AROME_FED. It is further found that the 1DBay retrieval leads to reduction of humidity where the observed FED equals zero and the AROME_FED is positive, i.e., in regions of spurious convection with substantial m_g. Hence, the LDA technique improves the AROME-France background humidity. It is capable of both promoting convection in regions with lightning and suppressing spurious convection. This was successfully verified in four case studies where the new LDA technique provided similar skill than the operational RDA in AROME-France.

FED exhibits the highest values near the convective core of a thunderstorm and the lightning activity does not always cover the entire cloud size. In fact, zero FED exists at cloudy locations. In order to address the specific nature of FED data, the 1DBay retrieval method is adapted. In detail, a wider vicinity is used to identify vertical profiles in the 1DBay method and a so-called *noCloud*-filter is introduced. First results reveal that this adaption of the method can help to more effectively reduce the background humidity in regions of spurious convection, and to avoid a reduction of the background humidity if the profile occurs at the location of a cloud. Nonetheless, one of the four case studies revealed more skill in the LDA without the *noCloud*-filter than the LDA using this modification. The *noCloud*-filter is a first approach trying to overcome this issue by keeping the background humidity constant when lightning was correctly simulated but not observed. The authors encourage further research on how the specifications of FED data can best be addressed by the LDA scheme, i.e., through correlations between lightning locations and cloud cover.

In addition, this study found that thinning of the FED observations (on a grid of resolution of 7km) was necessary to avoid the effect of correlations between the observation errors that violates the assumptions of a diagonal observation error matrix in the AROME-France 3DVar data assimilation system (not shown).

Finally, forecasts of 6-hour rain accumulations are evaluated through FSS analysis. The developed LDA scheme can in general compete with the established RDA, an encouraging result for further testing and development of the LDA in AROME-France. Positive effects on the forecast of rainfall by both RDA and LDA are found mainly for the high precipitation threshold and during the first 9 to 12 hours of the forecast. Longer forecast times show small spread in FSS between control run, RDA, and LDA for the three RA thresholds indicating that the assimilated radar and FED data do not significant effect the model forecast after 12 hours. The FSS of the combination of RDA and LDA indicate in most cases skill between the RDA and the LDA. The combined RDA-LDA approach provides the best trade-off in general sense and with respect to the assimilated observations. The case of 02 February 2018 was unique in that neither RDA nor LDA improved the FSS of the control run. This case was significantly influenced by weather phenomena over the Atlantic Ocean, with limited radar and Meteorage coverage. Real MTG-LI data will provide more accurate lightning records over the Atlantic than the synthetic MTG-LI data based on Meteorage observations used in this study, and the LDA performance might improve in such situations.

520   It could be further studied whether the radar reflectivity and LDA can be coupled. A coupled approach may help to overcome some issues explained for zero FED at cloudy locations in general or at least for precipitating clouds, and, at the same time benefit from the successful promotion and suppression of convection by both RDA and LDA. As the LDA explored here is based on satellite observations, such a coupled approach will also benefit forecasts over regions with limited radar coverage. The specific improvement over regions such as oceans and mountain ranges has not been studied here since our pseudo MTG-

525   LI observations are based on ground-based Meteorage records. A study addressing in particular the skill over such regions would be of great interest as soon as real MTG-LI data become available.

Author contributions. FE wrote the paper text and created the figures. OC and ED were involved in content creation. All contributed to article reviews. OC and FE developed the assimilation technique.

Competing interests. The authors declare that they have no conflict of interest.

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