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2 **Summer surface air temperature proxies point to near sea-ice-free conditions in the Arctic at**  
3 **127 ka.**

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5 Louise C. Sime<sup>1</sup>, Rahul Sivankutty<sup>1</sup>, Irene Vallet-Malmierca<sup>1</sup>, Agatha M. de Boer<sup>2</sup>, and Marie Sicard<sup>2</sup>

6 <sup>1</sup>British Antarctic Survey, Cambridge, UK

7 <sup>2</sup>Department of Geological Sciences, Stockholm University, Sweden.

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9 Correspondence: Louise C. Sime (lsim@bas.ac.uk)

10 **Abstract.**

11 The Last Interglacial (LIG) period, which had higher summer solar insolation than today, has been  
12 suggested as the last time that Arctic summers were ice-free. However, the latest suite of Coupled  
13 Modelling Intercomparison Project 6 Paleoclimate (CMIP6-PMIP4) simulations of the LIG produce a  
14 wide range of Arctic summer minimum sea ice area (SIA) results, ranging from a 30% to 96%  
15 reduction from the pre-industrial (PI). Sea ice proxies are also currently neither abundant nor  
16 consistent enough to determine the most realistic state. Here we estimate LIG minimum SIA  
17 indirectly through the use of 21 proxy records for LIG Summer Surface Air Temperature (SSAT) and  
18 11 CMIP6-PMIP4 models for the LIG. We use two approaches. First, we use two tests to determine  
19 how skilful models are at simulating reconstructed ~~observed~~  $\Delta$ SSAT from proxy records (where  $\Delta$   
20 refers to LIG-PI). This identifies a positive correlation between model skill and the magnitude of  
21  $\Delta$ SIA: the most reliable models simulate a larger sea ice reduction. Averaging the most skilful two  
22 models yields an average SIA of 1.3 mill. km<sup>2</sup> for the LIG. This equates to a 4.5 mill. km<sup>2</sup>, or a 79%,  
23 SIA reduction from the PI to the LIG. ~~Second, across the 11 models, the averaged  $\Delta$ SSAT at the 21~~  
24 ~~proxy locations is inversely correlated with  $\Delta$ SIA ( $r = -0.86$ ).~~ Second, across the 11 models, the  
25 averaged  $\Delta$ SSAT at the 21 proxy locations as well the pan Arctic average delta SSAT, is inversely  
26 correlated with  $\Delta$ SIA ( $r = -0.86$  and  $0.79$  respectively). In other words, the models show that a larger  
27 Arctic warming is associated with a greater sea ice reduction. Using the proxy record-averaged  
28  $\Delta$ SSAT of  $4.5 \pm 1.7$  K and the relationship between  $\Delta$ SSAT and  $\Delta$ SIA, suggests an estimated  $\Delta$ SIA of  
29 4.4 mill. km<sup>2</sup> or 77% less than the PI. The mean proxy-location  $\Delta$ SSAT is well-correlated with the  
30 Arctic-wide  $\Delta$ SSAT north of 60°N ( $r=0.97$ ) and this relationship is used to show that the mean proxy  
31 record  $\Delta$ SSAT is equivalent to an Arctic-wide warming of  $3.7 \pm 0.1$  K at the LIG compared to the PI.  
32 Applying this Arctic-wide  $\Delta$ SSAT and its modelled relationship to  $\Delta$ SIA, results in a similar estimate  
33 of LIG sea ice reduction of 4.5 mill. km<sup>2</sup>. The LIG climatological minimum SIA of 1.3 mill. km<sup>2</sup> is  
34 close to the definition of a summer ice-free Arctic, which is a maximum sea ice extent less than 1  
35 mill. km<sup>2</sup>. The results of this study thus suggest that the Arctic likely experienced a mixture of ice-free  
36 and near ice-free summers during the LIG.



## 38 **1. Introduction**

39 The rapid decline in Arctic sea ice over the last 40 years is an icon of contemporary climate change.  
40 Climate models have struggled to fully capture this sea ice loss (Notz and Community, 2020), which  
41 can sometimes reduce confidence in their future projections (*e.g.* IPCC, 2021). One line of  
42 investigation to address this problem, that has not been fully exploited, is the use of past climates to  
43 provide information on the future (*e.g.* Bracegirdle et al., 2019). Investigating the physics and causes  
44 of sea ice change, concentrating on Arctic changes during the most recent warm climate periods can  
45 help us address this problem (Guarino et al., 2020b). Interglacials are periods of globally higher  
46 temperatures which occur between cold glacial periods (Sime et al., 2009; Otto-Bliesner et al., 2013;  
47 Fischer et al., 2018). The differences between colder glacial and warmer interglacial periods are  
48 driven by climate feedbacks alongside changes in the Earth's orbit which affect incoming radiation.  
49 The Last Interglacial or LIG, occurred 130,000-116,000 years ago. At 127,000 years ago, at high  
50 latitudes orbital forcing led to summertime top-of-atmosphere shortwave radiation  $60\text{--}75 \text{ Wm}^{-2}$   
51 greater than the PI period. Summer temperatures in the Arctic during the LIG are estimated to be  
52 around 4.5 K above those of today (CAPE members, 2006; Kaspar et al., 2005; IPCC, 2013; Capron  
53 et al., 2017). Prior to 2020, most climate models simulated summer LIG temperatures which were too  
54 cool compared with these LIG temperature observations (Otto-Bliesner et al., 2013; IPCC, 2013).  
55 This led Lunt et al. (2013); Otto-Bliesner et al. (2013) and IPCC (2013) to suggest that the  
56 representation of dynamic vegetation changes in the Arctic might be key to understanding LIG  
57 summertime Arctic warmth.

58

59 Guarino et al. (2020b) argued that loss of Arctic sea-ice in the summer could cause the warm summer  
60 Arctic temperatures, without the need for dynamic vegetation. Using the HadGEM3 model, which  
61 was the UK's contribution for the LIG CMIP6-PMIP4 project, Guarino et al. (2020b) found that the  
62 model simulated a fully sea ice-free Arctic during the summer, *i.e.* it had less than 1 mill. km<sup>2</sup> of sea  
63 ice extent at its minimum. This unique, near complete, loss of summer sea ice appears to happen in  
64 the UK model, because it includes a highly advanced representation of melt ponds (Guarino et al.  
65 2020b; Diamond et al. 2021). These are shallow pools of water which form on the surface of Arctic

66 sea ice and which determine how much sunlight is absorbed or reflected by the ice (Guarino et al.,  
67 2020b).

68

69 Malmierca-Vallet et al. (2018) found the signature of summertime Arctic sea ice loss in Greenland ice  
70 cores. Kageyama et al. (2021) then led the international community in compiling all available marine  
71 core Arctic sea ice proxy data for the LIG and testing it against CMIP6-PMIP4 simulations. The  
72 Kageyama et al. (2021) synthesis of ocean core-based proxy records of LIG Arctic sea-ice change,  
73 like Malmierca-Vallet et al. (2018), showed that compared to the PI it is very likely that Arctic sea ice  
74 was reduced. However, Kageyama et al. (2021) also showed that directly determining sea-ice changes  
75 from marine core data is difficult. The marine core observations suffer some conflicting  
76 interpretations of proxy data sometimes from the same core, and imprecision in dating materials to the  
77 LIG period in the high Arctic. Thus, determining the mechanisms and distribution of sea ice loss  
78 during the LIG by directly inferring sea ice presence (or absence) from these preserved biological data  
79 alone is not possible (Kageyama et al., 2021).

80

81 The Coupled Model Intercomparison Project Phase 6 (CMIP6) Paleoclimate Model Intercomparison  
82 Project Phase (PMIP4) or CMIP6-PMIP4 LIG experimental protocol prescribes differences between  
83 the LIG and PI in orbital parameters, as well as differences in trace greenhouse gas concentrations  
84 (Otto-Bliesner et al., 2017). This standardised climate modelling protocol is therefore an ideal  
85 opportunity for the community to use models to explore the causes of Arctic warmth using multi-  
86 model approaches. ~~In particular, it offers the opportunity to address the questions of whether the~~  
87 ~~Arctic sea ice loss is sufficient to explain LIG summertime temperature observations, or whether the~~  
88 ~~Arctic vegetation changes idea (Lunt et al., 2013; Otto-Bliesner et al., 2013; IPCC, 2013), is still~~  
89 ~~potentially required. In particular, the existing non-dynamic-vegetation PMIP4 LIG protocol and~~  
90 ~~associated simulations offer the opportunity to address the question of whether the Arctic sea ice loss~~  
91 ~~alone is sufficient to explain LIG summertime temperature observations, or whether active vegetation~~  
92 ~~modelling, and the idea of vegetation feedbacks (Lunt et al., 2013; Otto-Bliesner et al., 2013; IPCC,~~

93 2013) are required. This said, we recognize that in reality there must also be LIG Arctic vegetation  
94 feedbacks. These should be explored in future modelling work.

95  
96 Guarino et al. (2020b) showed that the HadGEM3, the only CMIP-PMIP4 model with an ice-free  
97 Arctic at the LIG, has an excellent match with observed\_reconstructed Arctic air temperature in  
98 summer. The average  $\Delta$ SSAT in HadGEM3, for all locations with proxy observations, is  $+4.9 \pm 1.2$  K  
99 compared with the observationalproxy mean of  $+4.5 \pm 1.7$  K. This model also matched all, except  
100 one, marine core sea-ice datapoints from Kageyama et al. (2021). Here we investigate whether there  
101 are more CMIP6-PMIP4 models with a similarly good  $\Delta$ SSAT and if so, whether other models with a  
102 good match also suggest a much-reduced sea ice area (SIA) during the LIG. We further compute the  
103 correlation and linear relationship in the models between  $\Delta$ SSAT and  $\Delta$ SIA and subsequently use this  
104 equation and proxies for  $\Delta$ SSAT to estimate  $\Delta$ SIA. Section 2 describes the proxy data and models  
105 used in this study as well as the analysis methods. The results are presented in Section 3 which first  
106 evaluates the modelled PI and LIG sea ice distribution against observationsproxy reconstructions and  
107 then use the above described approaches to estimate the sea ice reduction at the LIG. Section 4  
108 summarises the results and discusses their shortcomings and implications.

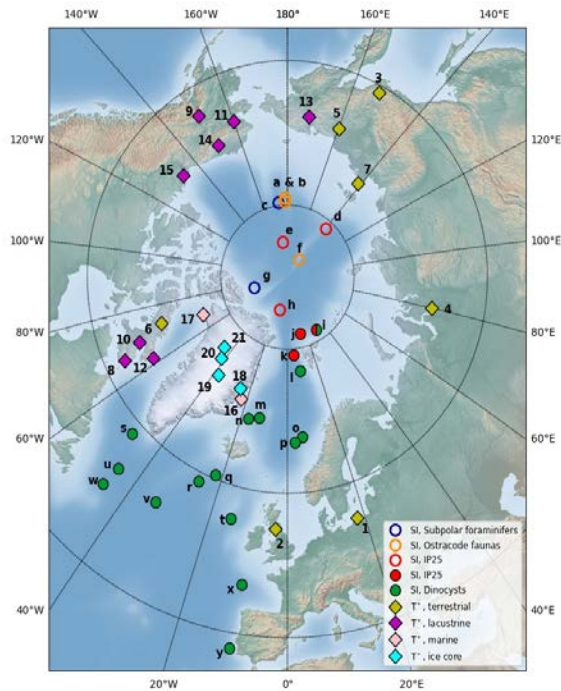
## 110 2. Data and methods

### 111 2.1 Observational dataProxy reconstructions for LIG

112 The LIG SSAT proxy observations used to assess LIG Arctic sea ice in the Guarino et al. (2020b)  
113 study were previously published by CAPE members (2006); Kaspar et al. (2005) and 20 of them were  
114 also used to assess CMIP5 models in the IPCC (2013) report. A detailed description of each  
115 observationrecord is available (CAPE members, 2006; Kaspar et al., 2005; IPCC, 2013; Capron et al.,  
116 2017). Each observationproxy record is thought to be of summer LIG air temperature anomaly  
117 relative to present day and is located in the circum-Arctic region; all sites are from north of  $51^\circ$ N.  
118 There are 7 terrestrial based temperature records; 8 lacustrine records; 2 marine pollen-based records;  
119 and 3 ice core records included in the original IPCC (2013) compilation. Guarino et al. (2020b) added

120 to this an additional new ~~observation~~record from the NEEM Greenland ice core from Capron et al.  
121 (2017), bringing the total number of proxies records to 21 (Table 1). Figure 1 shows the location, and  
122 type, for each numbered ~~observation~~proxy record. Terrestrial climate can be reconstructed from  
123 diagnostic assemblages of biotic proxies preserved in lacustrine, peat, alluvial, and marine archives  
124 and isotopic changes preserved in ice cores and marine and lacustrine carbonates (CAPE, 2006;  
125 Guarino et al., 2020). Quantitative reconstructions of climatic departures from the present-day are  
126 derived from range extensions of individual taxa, mutual climatic range estimations based on groups  
127 of taxa, and analogue techniques (CAPE, 2006). These proxy records are considered to represent the  
128 summer surface air temperature because summer temperature is also the most effective predictor for  
129 most biological processes, though seasonality and moisture availability may influence phenomena  
130 such as evergreen vs. deciduous biotic dominance (Kaplan et al., 2003). Whilst the exact timing of  
131 this peak warmth has not yet been definitively determined, it is reasonable to assume that these  
132 measurements are approximately synchronous across the Arctic. It is however very unlikely that the  
133 peak warmth was synchronous across both hemispheres (see Capron et al. (2014); Govin et al.  
134 (2015)), and further investigation of the synchronicity of peak warmth occurs across the Northern  
135 Hemisphere is merited. For consistency with modelled data, temperature anomalies computed against  
136 present day conditions (i.e. 1961-1990 baseline) were corrected to account for a +0.4K of global  
137 warming between PI (1850) and present day (1961-1990). ~~conditions~~ (Turney and Jones, 2010).  
138 Therefore, Table 1 and Guarino et al. (2020b) values differ slightly (+0.4K) from the original datasets  
139 so that they represent temperature anomalies relative to the PI.

140



141

142 *Figure 1: Map of data locations numbered to match Table 1. This combines the Kageyama et al.*

143 *(2021) sea ice locations 1 to 20 alongside with the temperature proxies from Table 1. Open symbols*

144 *correspond to records with uncertain chronology, and filled symbols correspond to records with good*

145 *chronology.*

146 Most of the sites have temperature uncertainty (one standard deviation) estimates, which are provided

147 in the Table 1. However, for 9 sites, the standard deviation of the temperature data was not available.

148 A standard deviation of  $\pm 0.5\text{K}$  was used to account for this missing uncertainty: this is the smallest

149 standard deviation found in any proxy record across all sites, and is thus as a conservative estimation

150 of the uncertainty associated to proxy data (Guarino et al., 2020b).

151



152 *Table 1: Compilation of LIG-PI summertime surface air temperature (SSAT) anomalies used by*  
 153 *Guarino et al. (2020b).*

Number	Lat	Lon	Site	Observation type	Observation (K)
1	55	18	Europe	Terrestrial: pollen, plant macrofossils	$3.4 \pm 0.5$
2	55	-3	UK	Terrestrial: Pollen, plant macrofossils	$2.4 \pm 0.5$
3	61	152.5	Magadan	Terrestrial: pollen	$6.4 \pm 2$
4	68	80	West-central Siberia	Terrestrial: pollen, plant macrofossils	$5.4 \pm 2$
5	68	160	Northeast Siberia	Terrestrial: pollen	$6.4 \pm 2$
6	70	-72.5	Flitaway	Terrestrial: insects, plant remains	$4.9 \pm 0.5$
7	73.33	141.5	Bolshoy Lyadhovshy	Terrestrial: pollen	$4.9 \pm 0.5$
8	63	-66	Robinson Lake	Lacustrine: pollen	$5.4 \pm 0.5$
9	64	-150	Birch Creek/ky11	Lacustrine: pollen	$1.4 \pm 1$
10	66	-69.2	Amarok Lake	Lacustrine: pollen	$4.9 \pm 0.5$
11	67	-160	Squirrel Lake	Lacustrine: pollen, plant macrofossils	$1.9 \pm 1.5$
12	67	-62	Cumber	Lacustrine: pollen	$5.9 \pm 1.5$
13	67.5	172.08	Lake Elgygytgyn	Lacustrine: pollen	$3.4 \pm 1$
14	69	-151	Ahaliorak Lake	Lacustrine: pollen	$1.9 \pm 1.5$
15	69	-133	Lake Tuk 5	Lacustrine: plant macrofossils and beetles	$2.4 \pm 0.5$
16	71.75	-23	Jameson	Marine: pollen, plant macrofossils, beetles, other invertebrates	$5.4 \pm 0.5$
17	76.35	-68.3	Thule	Marine: pollen, chironomids	$4.4 \pm 0.5$
18	73	-25	Renland	Ice core: d18O, dD	$5.4 \pm 0.5$
19	73	-38	GISP2	Ice core: d18O, dD	$5.4 \pm 0.5$
20	75	-42	NGRIP	Ice core: d18O, dD	$5.4 \pm 0.5$
21	76.4	-44.8	NEEM(ds)	Ice core: d18O, dD	$8 \pm 4$
154	-	-	Arctic	Mean of observations 1 to 21	$4.5 \pm 1.7$

155

## 156 2.2. Models and model output

157 We analyse Tier 1 LIG simulations, based on the standard CMIP6-PMIP4 LIG experimental protocol  
 158 (Otto-Bliesner et al., 2017). The prescribed LIG (127 ka) protocol differs from the CMIP6 PI  
 159 simulation protocol in astronomical parameters and the atmospheric trace GHG concentrations. LIG  
 160 astronomical parameters are prescribed according to orbital constants (Berger and Loutre, 1991), and

161 atmospheric trace GHG concentrations are based on ice core measurements: 275 ppm for CO<sub>2</sub>; 685  
162 ppb for CH<sub>4</sub>; and 255 ppb for N<sub>2</sub>O (Otto-Bliesner et al., 2017).

163

164 The CMIP6-PMIP4 model simulations were run following the Otto-Bliesner et al. (2017) protocol,  
165 except CNRM-CM6-1, which used GHG at their PI values rather than using LIG values. For all  
166 models, all other boundary conditions, including solar activity, ice sheets, aerosol emissions etc., are  
167 identical to the PI simulation. In terms of the Greenland and Antarctica ice sheets, a PI configuration  
168 for the LIG simulation is not unreasonable (Kageyama et al., 2021; Otto-Bliesner et al., 2020). LIG  
169 simulations were initialized either from a previous LIG run, or from the standard CMIP6 protocol PI  
170 simulations, using constant 1850 GHGs, ozone, solar, tropospheric aerosol, stratospheric volcanic  
171 aerosol and land use forcing. Whilst PI and LIG spin-ups vary between the models, with CNRM the  
172 shortest at 100 years, most model groups aimed to allow the land and oceanic masses to attain  
173 approximate steady state *i.e.* to reach atmospheric equilibrium and to achieve an upper-oceanic  
174 equilibrium - which generally seems to take around 300 to 400 years. LIG production runs are all  
175 between 100-200 years long, which is an appropriate length for Arctic sea ice analysis (Guarino et al.,  
176 2020a).

177

178 Whilst fifteen models have run the CMIP6-PMIP4 LIG simulation (Kageyama et al., 2021; Otto-  
179 Bliesner et al., 2020), and have uploaded model data to the Earth System Grid Federation (ESGF), we  
180 exclude four simulations for the following reasons. The AWI-ESM and Nor-ESM models have LIG  
181 simulations with two versions of model. To avoid undue biasing of results, we include only the  
182 simulation from the latest version for each model. Additionally, for INM-CM4-8 model, no ocean or  
183 sea ice fields were available for download, excluding this model from our analysis. Finally, we  
184 exclude the CNRM model in the analysis because apart from using PI instead of LIG GHG  
185 concentrations and a short spin-up time, the model also has known issues with its sea-ice model. The  
186 model produces much too thin sea ice in September and March compared with observational evidence  
187 and the snow layer on the ice is considerably overestimated (Voldoire et al., 2019). As a possible  
188 consequence of these issues, the CNRM model is also an outlier in an otherwise highly correlated

189 (inverse) relationship in the models between the LIG-PI albedo change over the Arctic sea-ice and the  
190 LIG-PI SSAT change over the ice, being the only model that produces a warmer LIG with almost no  
191 reduction in albedo (Figure A1). While we consider the CNRM ice model unreliable for this study, we  
192 note that the inclusion of the model in our analysis only reduces the correlation coefficients but does  
193 not change the overall conclusions.

194

195 We thus analyse the difference between the PI and LIG simulations from eleven models. Out of the  
196 eleven simulations of the LIG, seven have 200 years simulation length (data available to download in  
197 ESGF), the remaining four are 100 years in length. For PI control runs, we use the last 200 years of PI  
198 control run available in ESGF for each model. Details of each model: model denomination, physical  
199 core components, horizontal and vertical grid specifications, details on prescribed vs interactive  
200 boundary conditions, details of published model description, and LIG simulation length (spin-up and  
201 production runs) are contained in (Kageyama et al., 2021). Data was downloaded from the ESGF data  
202 node: <https://esgf-node.llnl.gov/projects/esgf-llnl/> (last downloaded on 23rd June 2021).

203

204 The spatial distribution of sea ice is usually computed in two ways, by its total area or its extent. The  
205 sea ice extent (SIE) is the total area of the Arctic ocean where there is at least 15% ice concentration.  
206 The total sea ice area (SIA) is the sum of the sea ice concentration times the area of a grid cell for all  
207 cells that contain some sea ice. In this paper, the SIA refers to the SIA of the month of minimum sea  
208 ice, as computed by using the climatology of the whole simulation.

209

### 210 **2.3. Assessing model skill to simulate reconstructions of $\Delta$ SSAT**

211 The model skill is quantified using two measures based on 1) the Root Mean Square Error (RMSE) of  
212 the modelled SSAT compared to the proxies ~~the percentage of the 21 proxies for  $\Delta$ SSAT (in Table 1)~~  
213 ~~for which the model produce a value within the error bars~~, and 2) the percentage of the 21 proxies for  
214  $\Delta$ SSAT (in Table 1) for which the model produce a value within the error bars ~~the Root Mean Square~~  
215 ~~Error (RMSE) of the modelled SSAT compared to the proxies~~. To assess whether the model match a

216 proxy point, we compute summer mean (June to August) surface air temperatures for every year for  
217 the PI and LIG for each model. Climatological summer temperature is the time mean of these  
218 summer temperatures for the entire simulation length. Our calculated model uncertainties on the  
219 climatological summer mean temperatures are one standard deviation of summer mean time series for  
220 each model. Bilinear interpolation in latitude-longitude space was used to extract values at the  
221 ~~observation-proxy~~ locations from the gridded model output. For climatological summer mean  
222 temperature, if there is an overlap between ~~observation-proxy~~ SSAT (plus ~~observational~~ uncertainty)  
223 and the simulated SSAT (plus model uncertainty) then, for that location, the result is considered as a  
224 match. Similarly, the RMSE error is calculated using the modelled SSAT values averaged over the  
225 summer months of the entire simulation length.

226

## 227 **3. Results**

### 228 **3.1. Simulated Arctic sea ice distribution**

229 The sea ice distribution in the models have been reported previously in Kageyama et al. (2021) and is  
230 included here to make this work self-reliant. For the PI, the model mean value for summer minimum  
231 monthly SIA is 6.4 mill. km<sup>2</sup>. Due to a lack of direct observations for the PI, the PI model results are  
232 compared with ~~observed~~ 1981 to 2002 satellite observations, keeping in mind that the ~~modernpresent~~  
233 ~~day~~ observations are for a climate with a higher atmospheric CO<sub>2</sub> level of ~380 ppm, compared to the  
234 PI atmospheric CO<sub>2</sub> levels of 280 ppm. The modern observed mean minimum SIA is 5.7 mill km<sup>2</sup>  
235 (Reynolds et al., 2002). In general, the simulations show a realistic representation of the geographical  
236 extent for the summer minimum. More models show a slightly smaller area compared to the present-  
237 day observations, however EC-Earth, FGOALS-g3, and GISS170 E2-1-G simulate too much ice  
238 (Figure 2). Overestimations appear to be due to too much sea ice being simulated in the Barents-Kara  
239 area (FGOALS-g3, GISS-E2-1-G), in the Nordic Seas (EC-Earth, FGOALS-g3) and in Baffin Bay  
240 (EC-Earth). Kageyama et al. (2021) also note that MIROC-ES2L performs rather poorly for the PI,  
241 with insufficient ice close to the continents. The other models have a relatively close match to the

242 15% isoline in the NOAA Optimum Interpolation version 2 data (Reynolds et al., 2002; Kageyama et  
243 al., 2021).

244

245 For the LIG, the model output is compared against the LIG sea ice synthesis of Kageyama et al.  
246 (2021), which include marine cores collected in the Arctic Ocean, Nordic Seas and northern North  
247 Atlantic (Figure 3). These data show that south of 79°N in the Atlantic and Nordic seas the LIG was  
248 seasonally ice-free. These southern sea ice records provide quantitative estimates of sea surface  
249 parameters based on dinoflagellate cysts (dinocysts). North of 79°N the sea-ice-related records are  
250 more difficult to obtain and interpret. A core at 81.5°N brings evidence of summer being probably  
251 seasonally ice-free during the LIG from two indicators: dinocysts and IP25/PIP25. However, an  
252 anomalous core close by at the northernmost location of 81.9°N, with good chronology, shows IP25-  
253 based evidence of substantial (> 75%) sea ice concentration all year round. Other northerly cores do  
254 not currently have good enough chronological control to confidently date material of LIG age. All  
255 models, except FGOALS, generally tend to match the results from proxies of summertime Arctic sea  
256 ice in marine cores with good LIG chronology (Figure 3), apart from the anomalous northernmost  
257 core for which the IP25 evidence suggest perennial sea ice (Kageyama et al., 2021). [Steinet al. \(2017\)](#)  
258 [suggest that PIP25 records obtained from the central Arctic Ocean cores indicating a perennial sea ice](#)  
259 [cover have to be interpreted cautiously, given that biomarker concentrations are very low to absent, so](#)  
260 [it is difficult to know how much weight to place on this particular result. Additionally, given Hillaire-](#)  
261 [Marcel et al. \(2017\) question the age model of the data from the central Arctic Ocean, thus these IP25](#)  
262 [data need to be interpreted with some caution.](#) This may mean that all the models tend to have similar  
263 problems in simulating Arctic sea ice during the LIG or that the LIG IP25 signal in the Arctic  
264 indicates something else. What is clear is that a new approach with other Arctic datasets, such as  
265 SSAT, may be needed to make progress on the LIG Arctic sea ice question.

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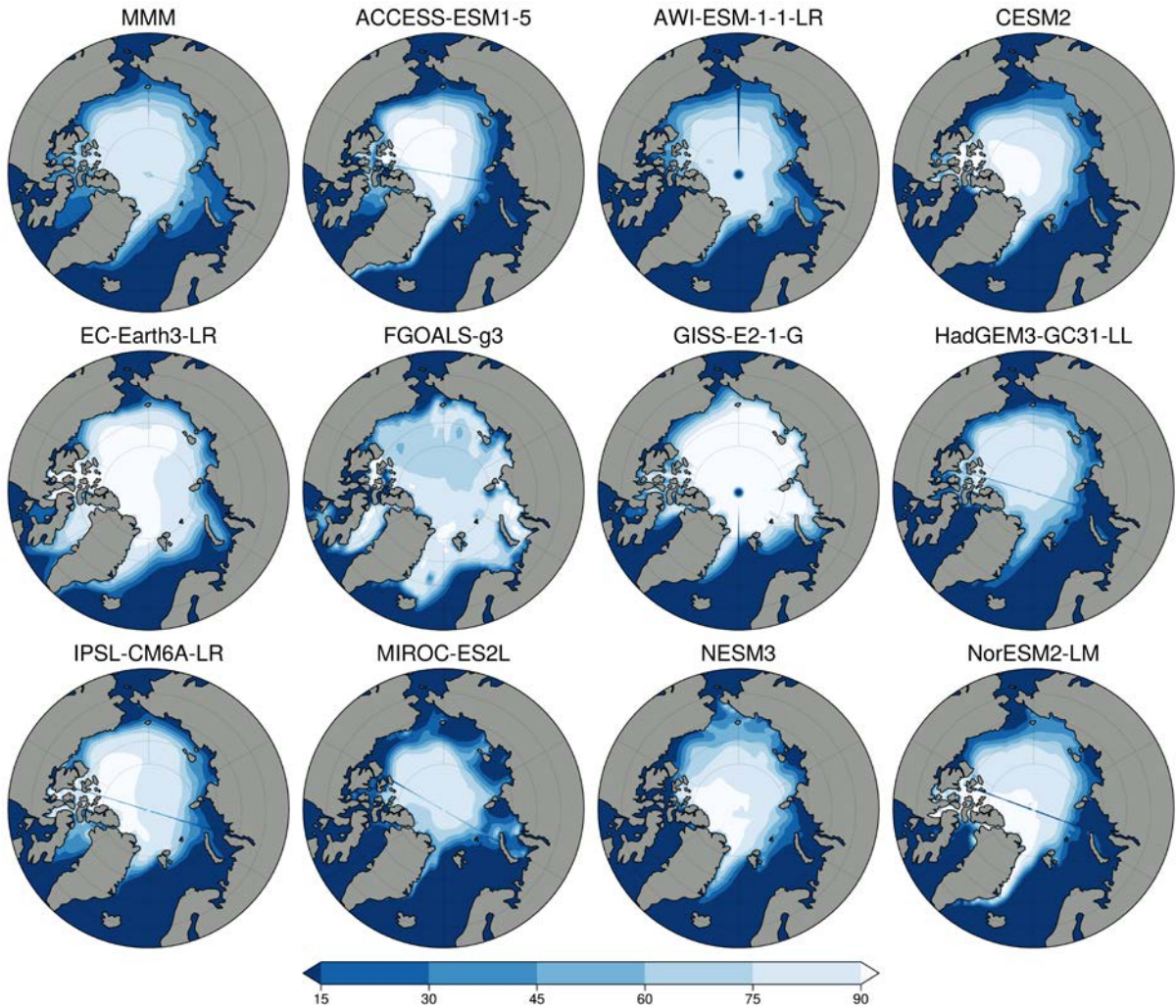
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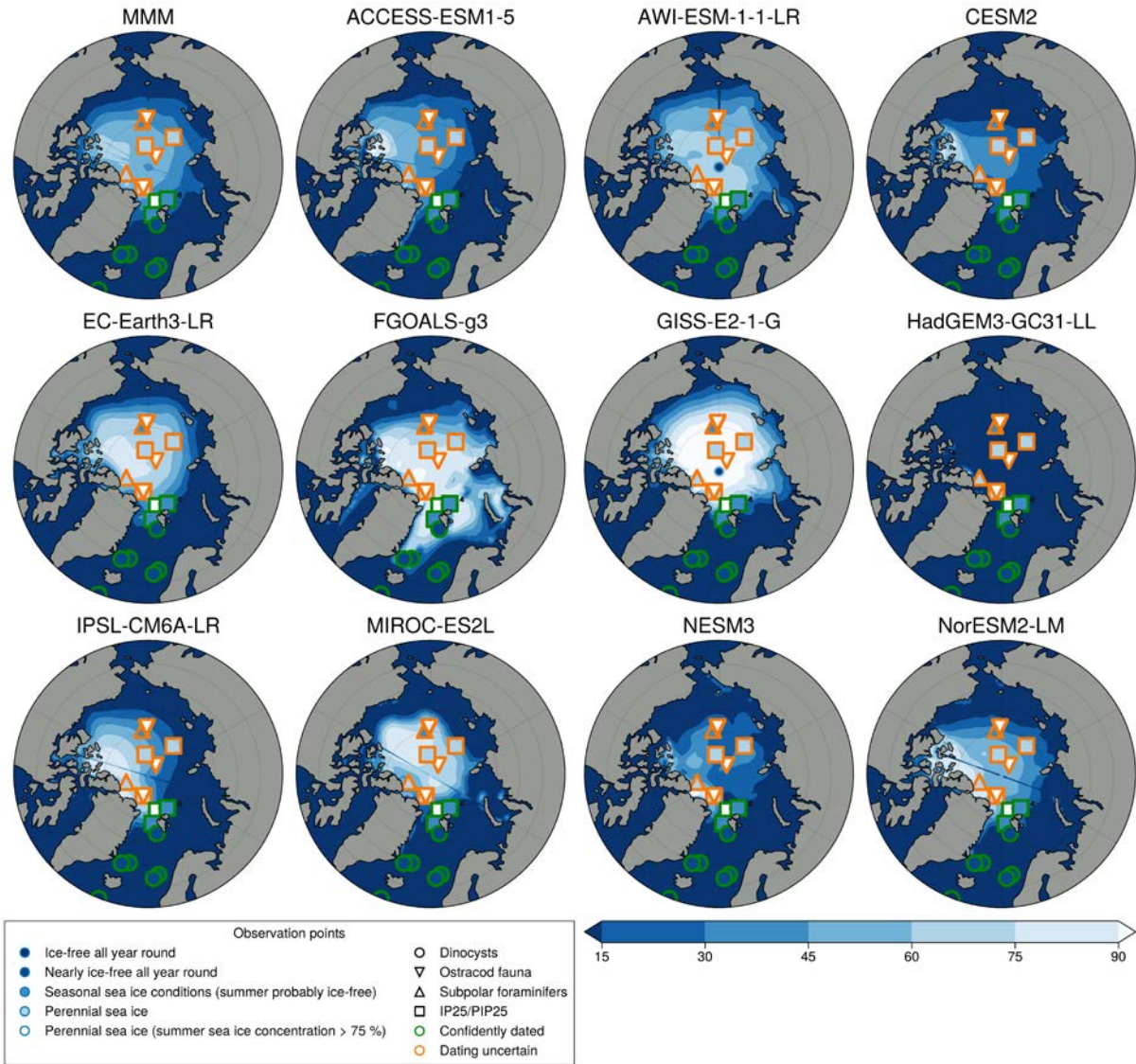
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275 *Figure 2: Climatological Minimum PI sea ice concentration maps for each model. The first panel*

276 *represents the multi model mean (MMM).*





278

279 *Figure 3: Climatological minimum LIG sea ice concentration maps for each model. Marine core*  
 280 *results are from Kageyama et al. (2021); orange outlines indicate that the dating is uncertain; green*  
 281 *outlines indicate the datapoint is from the LIG. The first panel represents the multi model mean.*

282

283 For the LIG, there is very little difference between the maximum (wintertime) Arctic SIA and that of  
 284 the PI (which is 15-16 mill. km<sup>2</sup> between the PI and the LIG in most models), but every model shows  
 285 a reduction in summer sea ice in the LIG compared to the PI (Table 2). Our model mean LIG  
 286 summertime Arctic is 2.9 mill. km<sup>2</sup>, compared to 6.4 mill. km<sup>2</sup> for the PI, or a 55% PI to LIG  
 287 decrease. There is large inter-model variability for the LIG SIA during the summer (Figure 4). All  
 288 models show a larger sea-ice area seasonal amplitude for LIG than for PI, and the range of model SIA  
 289 is larger for LIG than for PI (Figure A2). The results for individual years show that no model is close  
 290 to the ice-free threshold for ~~any model~~ summer during their PI simulation (Figure 4) but for the LIG  
 291 summer SIA, there are three models which are lower than 1 mill. km<sup>2</sup> for at least one summer during  
 292 the LIG simulation (Figure 4). Of these three, HadGEM3, shows a LIG Arctic Ocean free of sea ice in  
 293 all summers, *i.e.* its maximum SIE is lower than 1 mill. km<sup>2</sup> in all LIG simulation years. CESM2 and  
 294 NESM3 show low climatological SIA values (slightly above 2 mill. km<sup>2</sup>) in summer for the LIG  
 295 simulation, and both have at least one year with a SIE minimum which is below 1 mill. km<sup>2</sup>, though  
 296 their average minimum SIE values are just below 3 mill. km<sup>2</sup>. Of these low LIG sea ice models,  
 297 HadGEM3 and CESM2 realistically capture the PI Arctic sea ice seasonal cycle, whilst NESM3  
 298 overestimates winter ice and the amplitude of the seasonal cycle (Cao et al., 2018).

299

300

301 *Table 2: The minimum climatological sea ice area for the PI and the LIG, changes, and the*  
 302 *associated  $\Delta$ SSAT anomalies. Percentage reductions are calculated from PI minimum SIA for each*  
 303 *model.*

<b>MODEL</b> (units)	<b>SIA PI</b> (mill. km <sup>2</sup> )	<b>SIA LIG</b> (mill. km <sup>2</sup> )	<b><math>\Delta</math>SIA</b> (mill. km <sup>2</sup> )	<b>SIA</b> (% loss)	<b><math>\Delta</math>SSAT</b> (K)
MMM	6.36	2.93	-3.43	53.87	3.6±1.3
ACCESS-ESM1-5	5.48	2.39	-3.09	56.44	2.6±1
AWI-ESM-1-1-LR	5.37	3.76	-1.61	29.99	1.7±1.1
CESM2	5.31	1.62	-3.69	69.54	3.3±1



EC-Earth3-LR	8.86	3.65	-5.21	58.84	5.7±2.6
FGOALS-g3	8.83	5.55	-3.29	37.19	4.8±1.5
GISS-E2-1-G	8.87	5.54	-3.32	37.47	3.4±1.4
HadGEM3-GC31-LL	5.21	0.13	-5.07	97.48	4.9±1.2
IPSL-CM6A-LR	6.42	2.46	-3.96	61.74	4.4±1.2
MIROC-ES2L	4.20	2.79	-1.41	33.66	2.1 ± 0.6
NESM3	5.50	1.64	-3.86	70.14	3 ±0.9
NorESM2-LM	5.92	2.75	-3.17	53.52	3.6±1.1

304

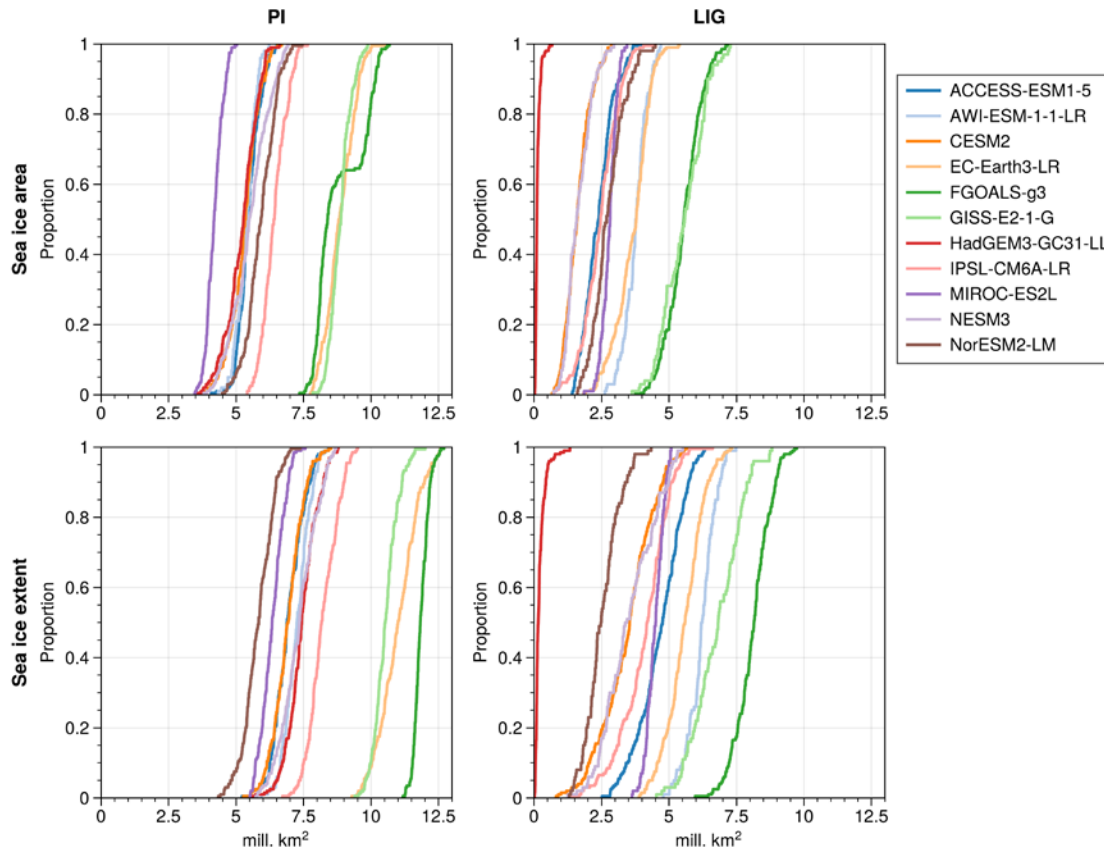


Figure 4: Cumulative distribution of minimum SIA of individual years in LIG and PI simulations, i.e SIA versus proportion of years which fall below the corresponding SIA value. HadGEM3 has minimum SIA below 1 mill km<sup>2</sup> for all years in LIG runs. CESM2 has 6.5%, and NESM3 8%, LIG years with SIA below 1 mill km<sup>2</sup>. Lower Panels are same but for SIE.

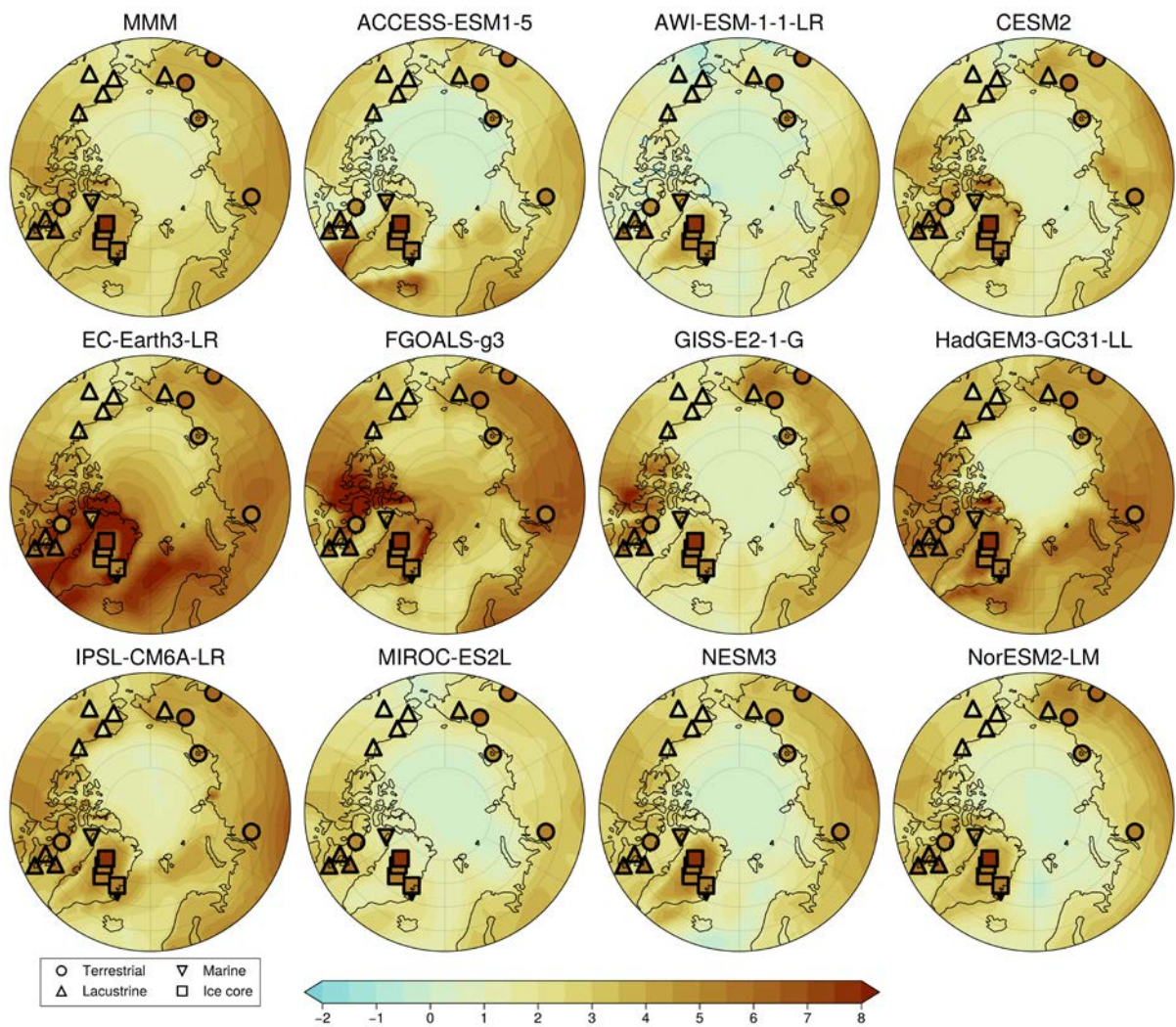
### 305 3.2. Estimating $\Delta$ SIA from model skill to simulate $\Delta$ SSAT

306 We first investigate whether there is a relationship between how well models match proxy  $\Delta$ SSAT  
 307 and the magnitude of SIA reduction that they simulate for the LIG. A visual comparison of modelled  
 308  $\Delta$ SSAT and proxy estimates for  $\Delta$ SSAT is also shown in Figure 5. As described in Section 2, two  
 309 different approaches are used to quantify the skill of the models to simulate  $\Delta$ SSAT, based on 1) the  
 310 RMSE of the model-data  $\Delta$ SSAT at the proxy record locations and 2) the percentage  $\Delta$ SSAT proxies

311 that the model can correctly match, within model and data error. Here the focus is on quantifying  
312 model skill across all data records, but for reference, the model-versus-proxy  $\Delta$ SSAT for each  
313 location is provided for each model individually in Figure A3. The RMSE skill estimate and the  
314 percentage match estimate provide very similar indications of which models have good skill to  
315 reproduce proxy  $\Delta$ SSAT. The five models with the lowest RMSE also have the highest percentage  
316 match and the two models with the highest RMSE have the lowest percentage match (Figure 6). Both  
317 approaches show that the models with better skill to simulate  $\Delta$ SSAT have a high absolute  $\Delta$ SIA. The  
318 only outlier is EC-Earth, which has an average skill (6<sup>th</sup> best model of 11) but a high SIA reduction at  
319 the LIG. This occurs because the EC-Earth PI simulation has an excessive SIA, more than 3 million  
320 km<sup>2</sup> compared ~~with present day estimates~~ ~~observations~~; this enables it to have a large  $\Delta$ SIA value,  
321 whilst likely retaining too much LIG SIA. Quantitatively there is a correlation of  $r=-0.65$  ( $p=0.03$ )  
322 between the magnitude of  $\Delta$ SIA and the RMSE, and a correlation with  $r=0.67$  ( $p=0.02$ ) between the  
323 magnitude of  $\Delta$ SIA and the percentage match of the model (Figure 6). Given that the SIA reduction  
324 from the PI to the LIG could be dependent on the starting SIA at the PI, we repeat the analysis for  
325 percentage SIA loss from the PI (rather than absolute SIA loss) and find that is correlates similarly to  
326 the model skill to reproduce  $\Delta$ SSAT (Figure A4).

327

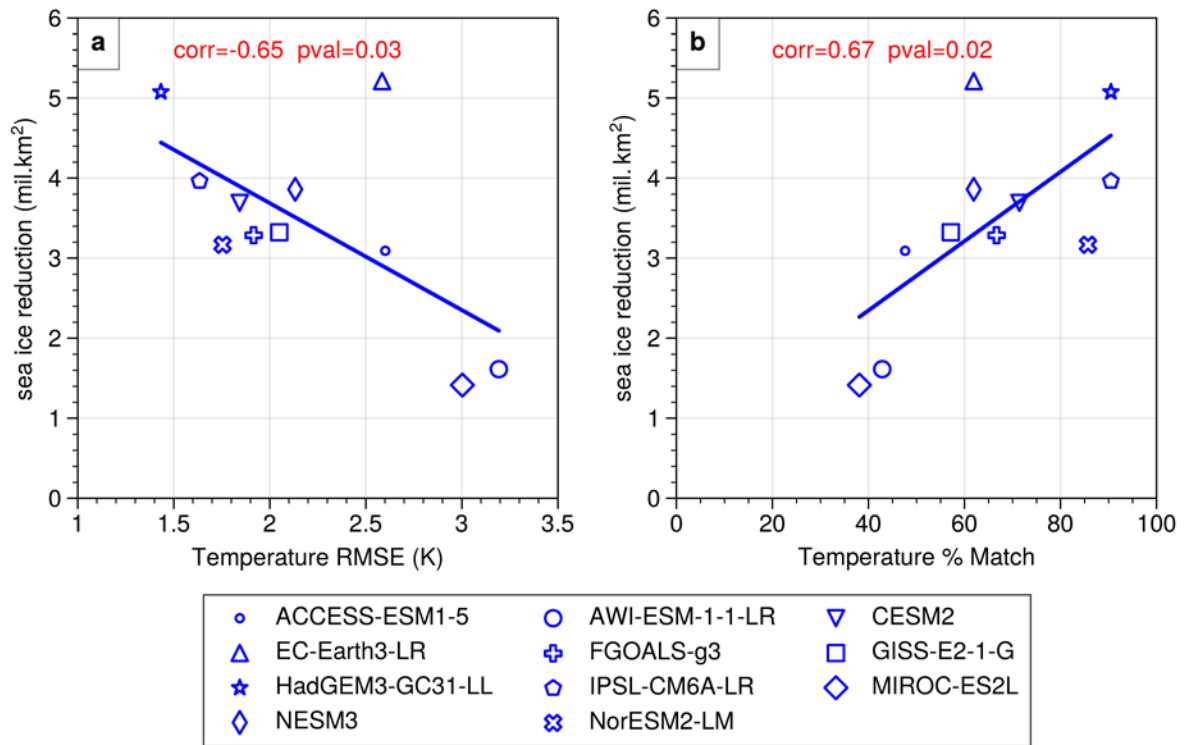
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330 *Figure 5: Summertime surface air temperature (SSAT) anomaly (LIG - PI) maps for each model*  
 331 *overlay by ~~observed~~ reconstructed summer temperature anomalies. Proxies are detailed in Table 1*  
 332 *and Guarino et al. (2020b); colours are the same as used for the underlying model data. The first*  
 333 *panel represents the multi model mean.*

334



335

336

337 *Figure 6: Modelled magnitude of  $\Delta SIA$  versus model skill to simulate proxy  $\Delta SSAT$ . a) The modelled*  
 338 *magnitude of  $\Delta SIA$  is scattered against the RMS error of the modelled  $\Delta SSAT$  compared to the proxy*  
 339  *$\Delta SSAT$  for the 21 data locations. b) The modelled magnitude of  $\Delta SIA$  scattered against the percentage*  
 340 *of  $\Delta SSAT$  data points that the model can match (see methods).*

341

342 In general, where models have a closer match with the  $\Delta SSAT$ , they have a higher absolute  $\Delta SIA$ , as  
 343 well as a larger percentage reduction of SIA from the PI. We thus look at our best performing models  
 344 for an indication of true LIG Arctic sea ice reduction. The four models with the best agreement of  
 345  $\Delta SSAT$  to proxies are in order of skill; HadGEM3, IPSL, NORESM2, and CESM2. The top two  
 346 performing models simulate an average SIA loss of 4.5 mill. km<sup>2</sup> from an average starting PI SIA of  
 347 5.8 mill. km<sup>2</sup> to a final LIG SIA of 1.3 mill. km<sup>2</sup>, which equates to a percentage SIA loss of 79%.  
 348 Including also the two next-best performing models in the average results in an average SIA loss of

349 4.0 mill. km<sup>2</sup> to a final LIG SIA of 1.7 mill. km<sup>2</sup> from an average starting PI SIA of 5.7 mill. km<sup>2</sup>,  
350 which equates to a percentage SIA loss of 71%.

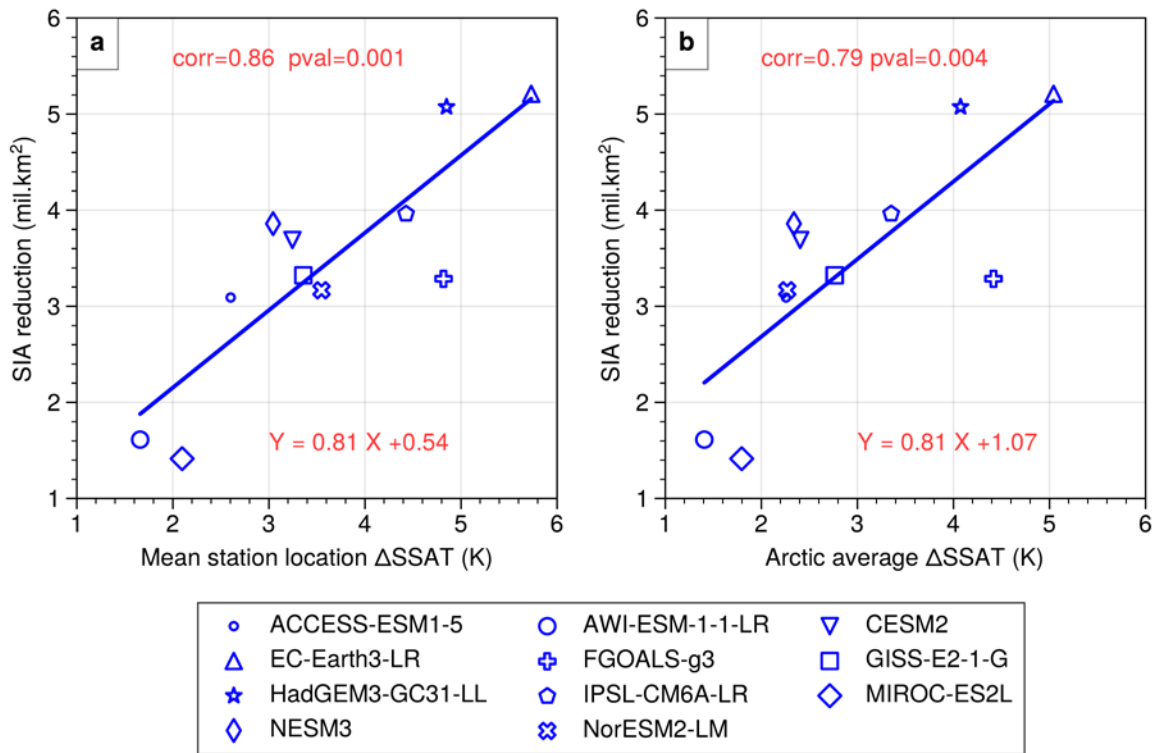
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352 The question arises as to why there is a linear relationship between model skill to simulate Arctic  
353  $\Delta$ SSAT and SIA reduction. One possibility is that the mean proxy  $\Delta$ SSAT of 4.5 K is higher than  
354 what most models produce, and that the warmer models are thus closer to the proxies and also more  
355 likely to reduce sea ice. In the next section, this question is addressed by investigating whether  $\Delta$ SIA  
356 is closely related to  $\Delta$ SSAT itself.

357

### 358 **3.3. Estimating $\Delta$ SIA from the modelled $\Delta$ SIA- $\Delta$ SSAT relationship and proxy $\Delta$ SSAT**

359 Here we investigate whether the models suggest a linear relationship between  $\Delta$ SSAT and  $\Delta$ SIA, and  
360 if so, exploit that together with proxy  $\Delta$ SSAT to estimate the most likely (true) value for  $\Delta$ SIA. We  
361 first calculate the mean  $\Delta$ SSAT in the model at all 21 proxy data locations and compare it to the  
362 magnitude of  $\Delta$ SIA in each model (Figure 7a). The two are well correlated with  $r=0.86$  ( $p=0.001$ ) and  
363 the regression equation provide a dependence of  $\Delta$ SIA on  $\Delta$ SSAT. Using this relation, the ~~observed~~  
364 reconstructed mean  $\Delta$ SSAT at the proxy locations points to a SIA reduction of 4.4 mill. km<sup>2</sup> from the  
365 PI. This constitutes a 77% reduction from the present day observation of 5.7 mill. km<sup>2</sup>, which is also  
366 the average SIA for the PI in the two most skilful models identified in the previous section. Using this  
367 value for the PI sea ice, suggests remaining minimum of 1.3 mill. km<sup>2</sup> of sea ice during the LIG  
368 summer. An average LIG minimum of 1.3 mill. km<sup>2</sup> implies that some LIG summers must have been  
369 ice-free (below 1 mill. km<sup>2</sup> in SIE) but that most summers would have had a small amount of sea ice.



370

371 *Figure 7: Modelled magnitude of  $\Delta SIA$  versus modelled  $\Delta SSAT$  for the Arctic. a) The modelled  $\Delta SIA$*   
 372 *is scattered against mean modelled  $\Delta SSAT$  at the 21 data locations. b) The modelled  $\Delta SIA$  is scattered*  
 373 *against the mean modelled  $\Delta SSAT$  averaged over the Arctic north of  $60^\circ N$ .*

374

375 The  $\Delta SSAT$  relationship to  $\Delta SIA$  has so far been computed using the mean  $\Delta SSAT$  at the locations of  
 376 the data. To test whether this method would also work for the Arctic in general, the  $\Delta SSAT$  is next  
 377 averaged over the whole Arctic north of  $60^\circ N$  and compared with  $\Delta SIA$  (Figure 7b). The correlation  
 378 between  $\Delta SSAT$  and  $\Delta SIA$  is a somewhat reduced when calculating  $\Delta SSAT$  across the whole Arctic,  
 379 though it is still highly significant ( $r=0.79$ ,  $p=0.004$ ). An estimate for proxy-based Arctic-wide  
 380  $\Delta SSAT$  can be derived by applying the close relationship between Arctic  $\Delta SSAT$  and station  $\Delta SSAT$   
 381 in the models (Figure 8,  $r=0.97$ ,  $p < 0.001$ ). Inserting the  $\Delta SSAT$  averaged over all proxy-records, of  
 382 4.5 K, in the regression equation in Figure 8, gives an estimate for proxy-based Arctic-wide  $\Delta SSAT$



383 of  $3.7 \pm 0.1$  K. Applying the regression equation in Figure 7b and using this estimate for Arctic-wide  
384  $\Delta$ SSAT suggests a PI to LIG sea ice reduction of 4.5 mill. km<sup>2</sup>, which is very similar to the estimate  
385 derived from the station data alone (of 4.4 mill. km<sup>2</sup>).

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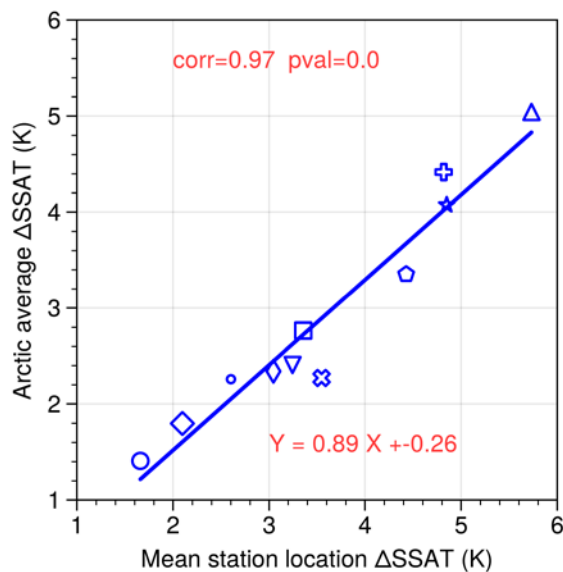
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399 Figure 8: Modelled Arctic-wide  $\Delta$ SSAT versus modelled mean  $\Delta$ SSAT at the data locations for the 11  
400 models. The markers for each model are same as in Figure 7

401

#### 402 4. Discussion and conclusions

403 As discussed in the introduction, neither proxies nor modelling results alone allow currently for a  
404 convincing estimate of the Arctic sea ice reduction at the LIG. Here we apply a joint approach to  
405 make progress. We deduce how much sea ice was reduced during the LIG, using 11 of the most recent  
406 CMIP6-PMIP4 LIG model simulations and proxy observations of summer air temperature changes.  
407 The reduction of sea ice from the PI to the LIG in the models range from 30% to 96% with an average  
408 of 55%. No model is close to the ice-free threshold, of maximum SIE lower than 1 mill. km<sup>2</sup>, for any  
409 model year-summer during their PI simulation. During the LIG, the HadGEM3 model is the only one  
410 that has an Arctic Ocean free of sea ice in all summers, although CESM2 and NESM3 show SIA



411 values of around 2 -mill. km<sup>2</sup>, in association with intermittently ice-free conditions. We found that  
412 larger LIG SIA reduction from the PI is related to greater SSAT warming, the two being correlated  
413 with  $r=0.86$  across the models. ~~In particular, the 8 models with largest SIA reduction are all able to~~  
414 ~~match, within uncertainty, the mean PI to LIG summertime Arctic warming of  $4.5 \pm 1.7$  K at the 21~~  
415 ~~proxy locations.~~In particular, 8 out of 11 models are able to match, within uncertainty, the average PI  
416 to LIG summertime Arctic warming of  $4.5 \pm 1.7$  K as recorded by surface temperature proxies. This  
417 magnitude of warming was difficult to reach with previous generations of LIG models.- Among the  
418 models, two of them capture the magnitude of the observed  $\Delta$ SSAT in more than 60% of the total  
419 proxy locations. These models simulate an average LIG sea ice area of 1.3 mill. km<sup>2</sup> which is a 4.5  
420 mill. km<sup>2</sup> (or 79%) reduction from their PI values.

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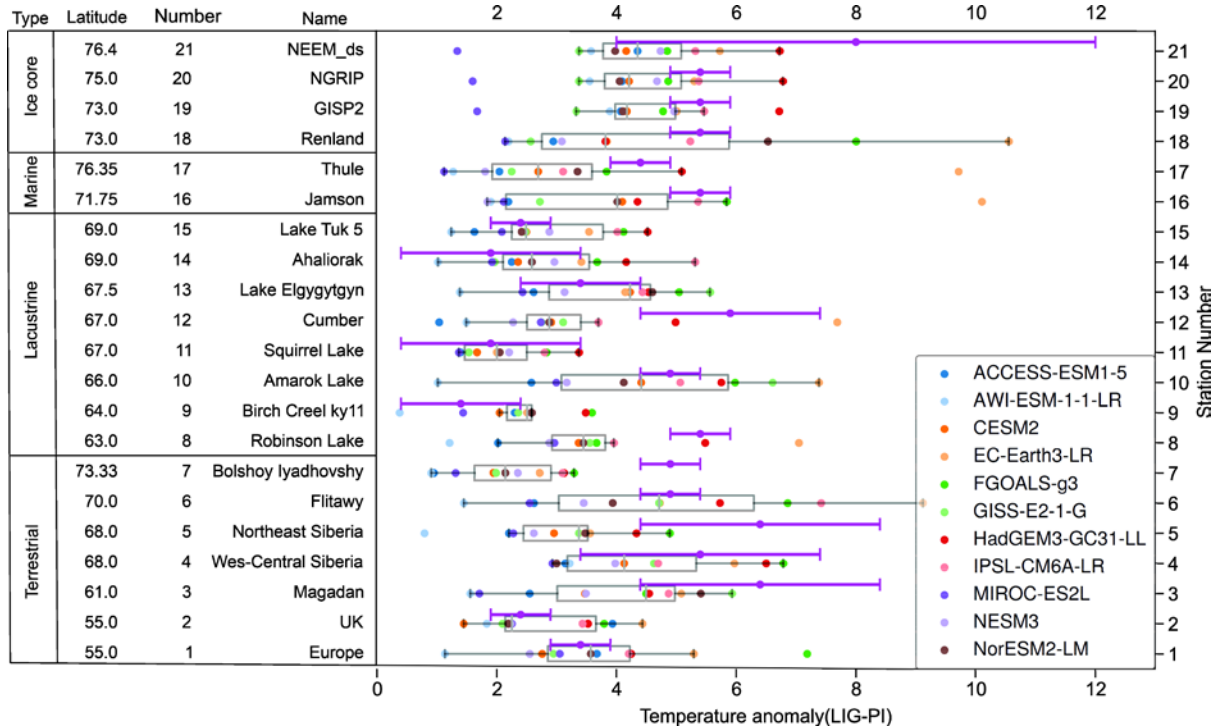
422 We find that the good match between the (ice-free) HadGEM3 and the Guarino et al. (2020b) summer  
423 Arctic temperature dataset is not unique. However, we find that it is not random either and that there  
424 is a correlation between model skill to match the  $\Delta$ SSAT and the reduction of SIA from the PI to the  
425 LIG (both when using an RMSE skill test and when using a best-match skill test). The two most  
426 skilful models simulate an average LIG sea ice area of 1.3 mill. km<sup>2</sup> which is a 4.5 mill. km<sup>2</sup> or 79%  
427 reduction from their PI values. Whilst we cannot assume all model error  $\Delta$ SSAT is attributable to  
428  $\Delta$ SIA, it is reasonable to assume that the better performing models for  $\Delta$ SSAT are also better at  
429 simulating  $\Delta$ SIA, because of the close relationship between warming and sea ice loss.

430

431 Some of the proxies are more difficult for the models to simulate (Figure 9 and Figure A3). In  
432 particular, it appears that the Greenland ice core SSAT value from NEEM of +8 K (~~observatio proxy~~  
433 ~~record~~ 21 in Table 1 Figure 9) is higher than any model simulates; though with a  $\pm 4$  K uncertainty it is  
434 nevertheless matched by some models. Terrestrial proxies three and six, with SSAT values of +6.4 K  
435 are also only rarely matched. Further work on the observational side would be useful. These LIG  
436 SSAT proxy reconstructions were used in the IPCC (2013) report and by Guarino et al. (2020b); and  
437 were previously published by IPCC (2013); CAPE members (2006); Kaspar et al. (2005); Capron et

438 al. (2017). Thus, this dataset should ideally be improved. One start point for this would be adding  
 439 uncertainties to the (nine) sites which do not currently have these numbers.

440



441

442 *Figure 9: Proxy  $\Delta$ SSAT (violet dots and uncertainty bars) and simulated  $\Delta$ SSAT for all models*  
 443 *(coloured dots) for each proxy record location (rows). Grey boxes extend from the 25th to the 75th*  
 444 *percentile of each locations distribution of simulated values and the vertical lines represent the*  
 445 *median.*

446

447 The correlation between model skill to simulate  $\Delta$ SSAT and the magnitude of  $\Delta$ SIA is convincing ( $r=$   
 448  $0.66$  and  $p= 0.003$  on average for the two skill tests). However, the two quantities are not  
 449 straightforward to relate through a dynamical process. On the other hand, it is well known that there is  
 450 a positive feedback between Arctic temperature and Arctic sea-ice, with warmer temperatures more  
 451 likely to melt sea ice, and less sea ice producing a smaller albedo to incoming solar radiation and so  
 452 less cooling from solar reflection. [Figure A6 shows the relationship between summer surface air](#)

453 [temperature anomalies versus September sea ice area. from the observational estimates for the period](#)  
454 [from 1979-2020. In present time, the relationship between minimum SIA and summer SAT is 1.32](#)  
455 [mil. Km<sup>2</sup> decrease per 1K temperature rise.](#) This dynamic [relationship](#) is [also evident in LIG](#)  
456 simulations, [with a](#)-strong correlation of  $r=0.86$  between the magnitude of  $\Delta SIA$  and  $\Delta SSAT$  [across](#)  
457 [all the models](#). The reconstructed  $\Delta SSAT$  from proxies, of  $4.5 \pm 1.7$  K, is larger than most models  
458 simulate, so the models that match the  $\Delta SSAT$  most closely would be the models with a larger  
459  $\Delta SSAT$  than average and thus also a larger  $\Delta SIA$ . The only model that has a large SIA reduction and  
460 not a good skill to match SSAT is EC-Earth, which features a PI simulation with far too much sea ice,  
461 which allows an excessive LIG to PI Arctic warming. An additional result of our study is that the  
462 mean  $\Delta SSAT$  at the proxy locations is strongly correlated to Arctic-wide  $\Delta SSAT$  north of  $60^\circ N$  in the  
463 models ( $r=0.97$ ). Applying the regression relation between the two, implies that the mean  $\Delta SSAT$  at  
464 the proxy locations, of 4.5 K, is equivalent to an Arctic-wide warming at the LIG of 3.7 K. This is  
465 thus a more representative value for the Arctic warming at the LIG, than using the simpler proxy-  
466 location average.

467  
468 The strong linear correlation between the magnitude of  $\Delta SIA$  and  $\Delta SSAT$  is applied to the proxy-  
469 reconstructed  $\Delta SSAT$  to give an estimate of the reduction of SIA from the PI to LIG of 4.4 mill. km<sup>2</sup>,  
470 similar to that derived from our "best skill" approach. A similar value of 4.5 mill. km<sup>2</sup> is obtained  
471 when extrapolating the method to Arctic-wide  $\Delta SSAT$  north of  $60^\circ N$ . The models and data have  
472 uncertainties, and the regressions applied are not between perfectly correlated quantities. However, it  
473 is clear from both applied methods (each with two variants) that proxy-reconstructed  $\Delta SSAT$ , in  
474 combination with the model output, implies a larger sea ice reduction than the climatological multi-  
475 model mean of 55%. It suggests a LIG SIA of  $\sim 1.3$  mill. km<sup>2</sup>, which is consistent with intermittently  
476 ice-free summers – but with (low ice area) ice-present summers likely exceeding the number of ice-  
477 free years.

478  
479 [Whilst we have focussed here on the Arctic SIA response to LIG insolation forcing, Kageyama et al.](#)  
480 [\(2021\) found that the models that respond strongly to LIG insolation forcing also respond strongly to](#)

481 CO<sub>2</sub> forcing. Indeed the models with the weakest response for the LIG had the weakest response to  
482 the CO<sub>2</sub> forcing. This suggests that our assessment here of model skill against Arctic SIA and SSAT  
483 change can also help, to some extent, ascertain the models which have a better Arctic SIA and SSAT  
484 response to CO<sub>2</sub> forcing. Overall the results presented in this study suggest that: (i) the fully-ice free  
485 HadGEM3 model is somewhat too sensitive to forcing; it loses summer sea ice too readily during the  
486 LIG; and (ii) most other PMIP4 models are insufficiently sensitive - these models do not lose enough  
487 sea ice.

488  
489 *Code availability.* Python code used to produce the manuscript plots is available on request from the  
490 authors.

491  
492 *Data availability.* The summer air temperature dataset is available at [https://data.bas.ac.uk/full-](https://data.bas.ac.uk/full-record.php?id=GB/NERC/BAS/PDC/01593)  
493 [record.php?id=GB/NERC/BAS/PDC/01593](https://data.bas.ac.uk/full-record.php?id=GB/NERC/BAS/PDC/01593). All model data is available from the ESGF data node:  
494 <https://esgf-node.llnl.gov/projects/esgf-llnl/>.

495

496

497

## 498 **Appendix**

### 499 **A1. Inter-model differences in LIG Sea ice simulation**

500

501  
502 Sea ice formation and melting can be affected by a large number of factors inherent to the atmosphere  
503 and the ocean dynamics, alongside the representation of sea ice itself within the model (i.e. the type of  
504 sea ice scheme used). In coupled models it can therefore be difficult to identify the causes of this  
505 coupled behavior (Kagayama et al. 2021, Sicard et al,2022). Nevertheless Kagayama et al. (2021;  
506 Section 4), alongside Diamond et al. (2021) address the question of what drives model differences in  
507 summertime LIG sea ice. In summary:

508 1. All model PMIP4-LIG s-simulations show a major loss of summertime Arctic sea ice between the PI  
509 and LIG.

510 2. Across all models, there is an increased downward short-wave flux in spring due to the imposed  
511 insolation forcing and a decreased upward short-wave flux in summer, related to the decrease of the  
512 albedo due to the smaller sea ice cover. Differences between the model results are due to a difference  
513 in phasing of the downward and upward shortwave radiation anomalies.

514 3. The sea ice albedo feedback is most effective in HadGEM3. It is also the only model in which the  
515 anomalies in downward and upward shortwave radiation are exactly in phase.

516 4. The CESM2 and HadGEM3 models (which both simulate significant sea ice loss) exhibit an  
517 Atlantic Meridional Overturning Circulation (AMOC) that is almost unchanged between PI and LIG,  
518 while in the IPSLCM6 model (with moderate sea ice loss) the AMOC weakens. This implies that a  
519 reduced northward oceanic heat transport could reduce sea ice loss in the Central Arctic in some  
520 models.

521 5. The two models (HadGEM3 and CESM2) which had the lowest sea ice loss contain explicit melt  
522 pond schemes, which impact the albedo feedback in these models. Diamond et al. (2021) show that  
523 that the summer ice melt in HadGEM3 is predominantly driven by thermodynamic  
524 processes and those thermodynamic processes are significantly impacted by melt ponds.

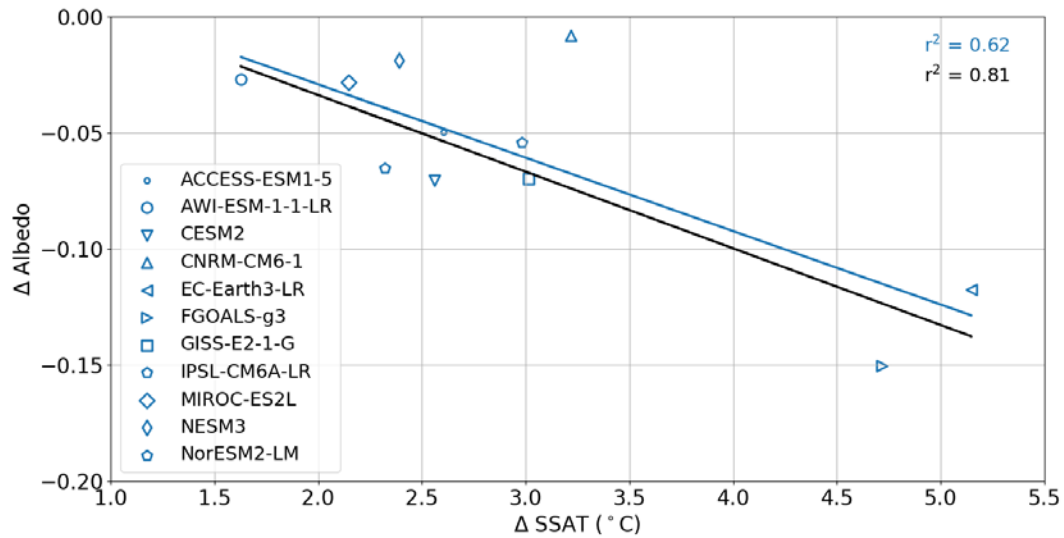
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527 **Appendix Figures**

528

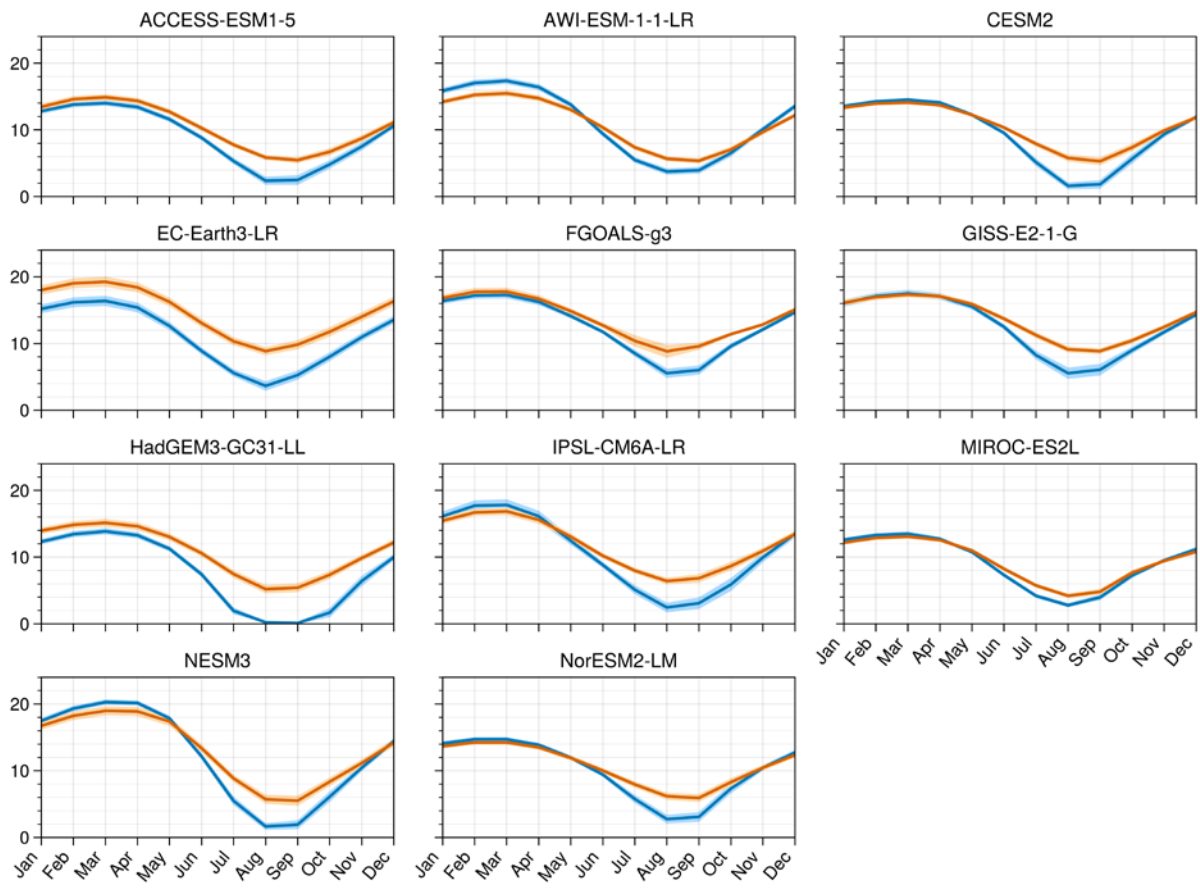
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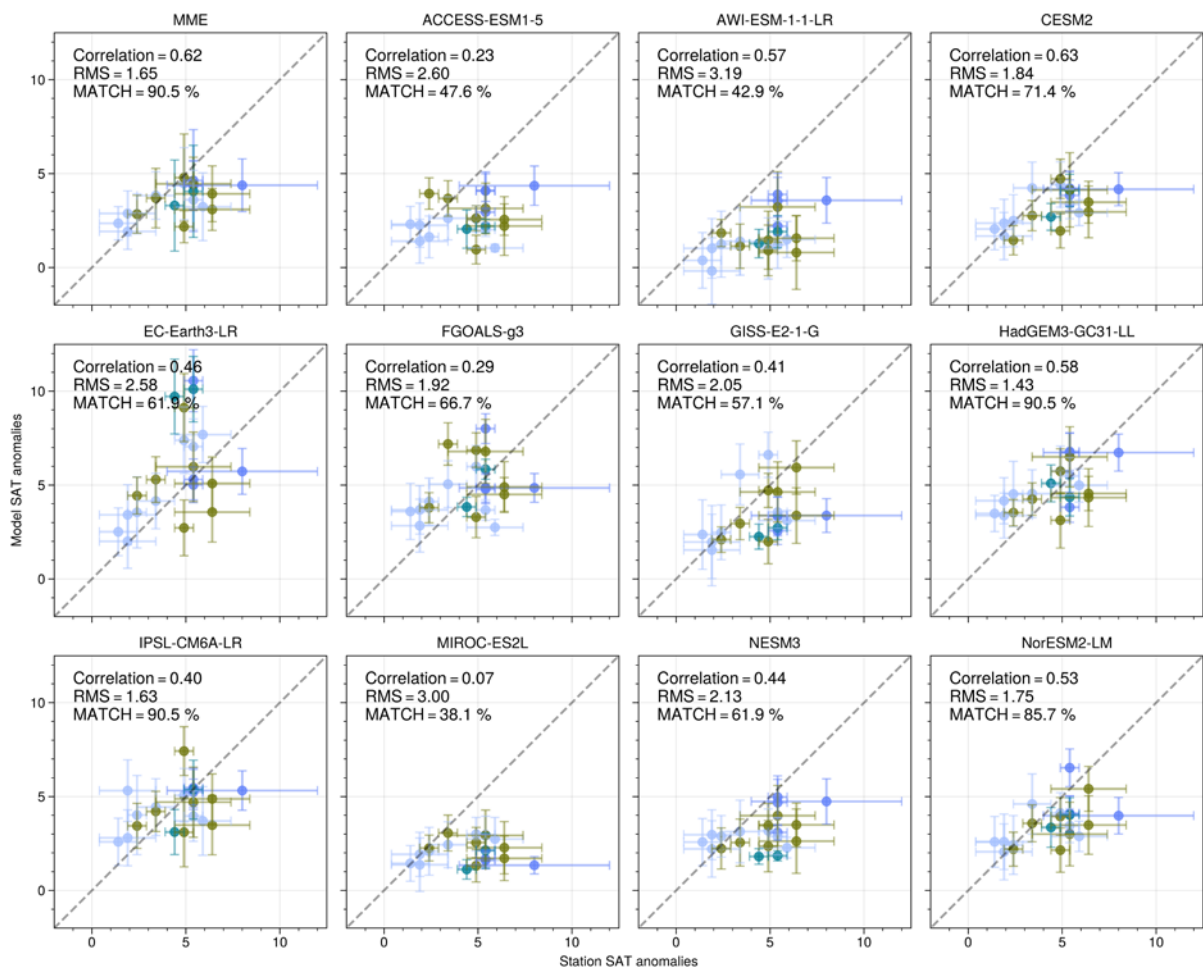
532 Figure A1. LIG-PI change in albedo over Arctic sea-ice as a function of LIG-PI change in SSAT (°C)  
 533 over the ice. The  $r^2$  values and the linear fit lines are for the models including CNRM (blue) and  
 534 excluding CNRM (black). The CNRM model (upside triangle) is an outlier that influences the  
 535 strength rather than the nature of the correlation.



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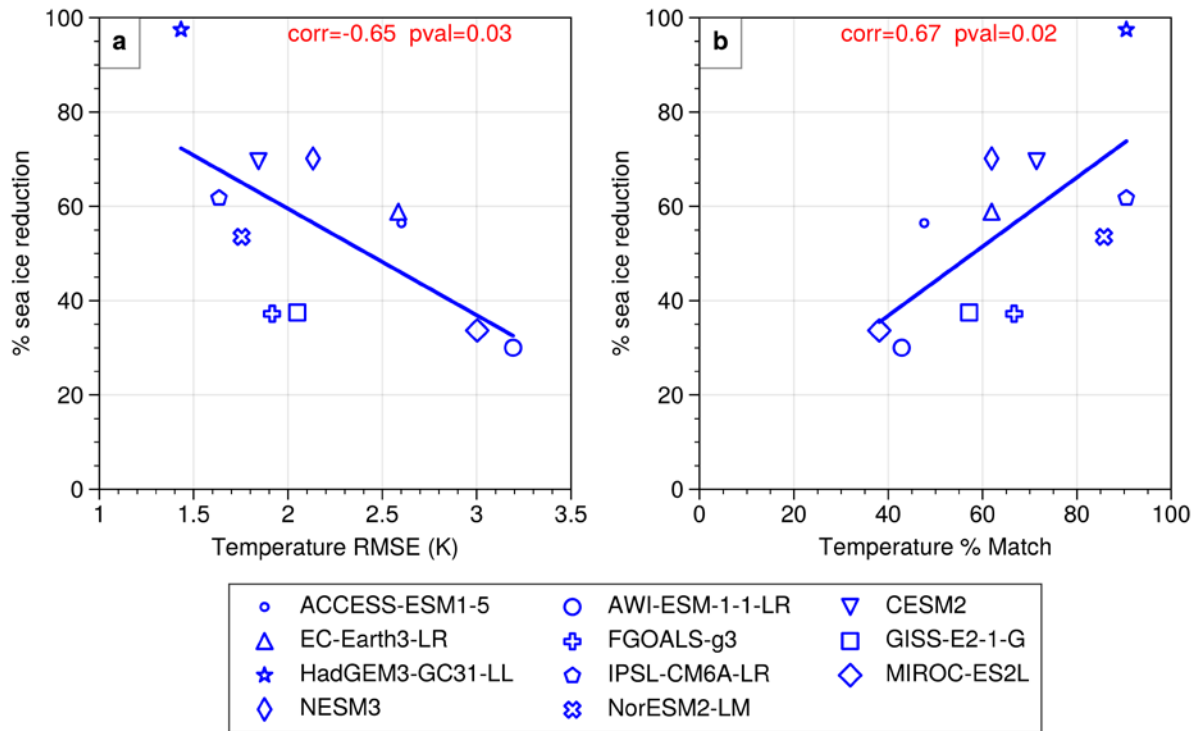
537 Figure A2. Sea ice area climatological seasonal cycle for each model.

538



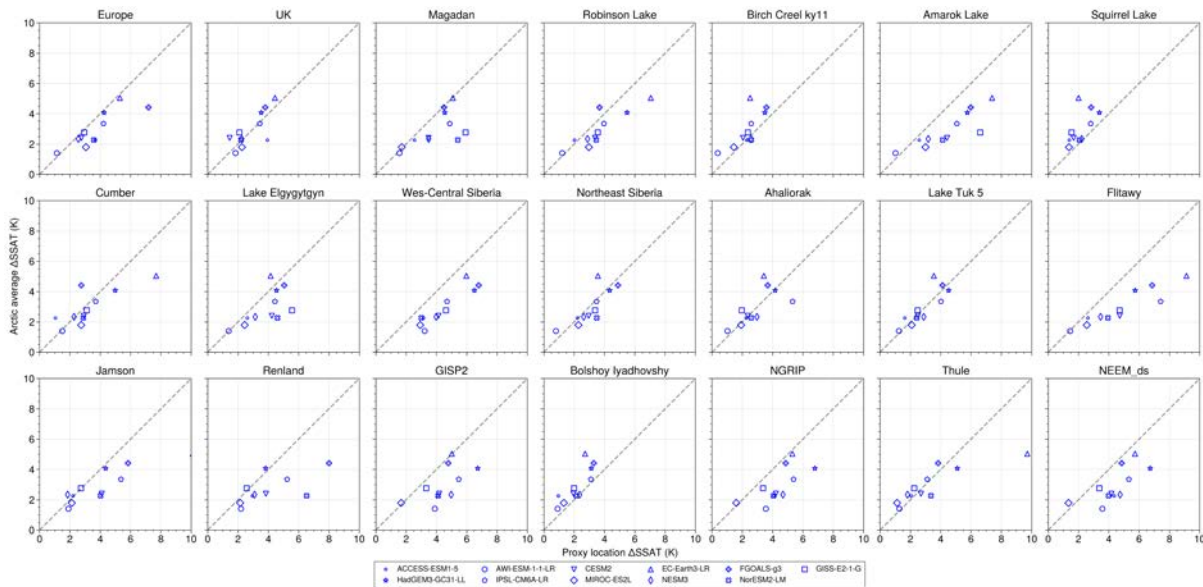
539 Figure A3. Modelled  $\Delta$ SSAT versus proxy  $\Delta$ SSAT. The scatter points show model data versus  
 540 observationsreconstuctions for each proxy location. Error-bars represent one standard deviation on  
 541 either side of the proxy estimate. The correlation coefficients, between X and Y, RMSE and  
 542 percentage matches with observationsproxy data for each model are indicated in each panel.  
 543





544

545 Figure A4: Modelled % sea ice area reduction from the LIG to the PI versus model skill to simulate  
 546 proxy  $\Delta$ SSAT. a) The modelled %SIA reduction is scattered against the RMSE of the modelled  
 547  $\Delta$ SSAT compared to the proxy  $\Delta$ SSAT for the 21 data locations. b) The modelled % SIA reduction  
 548 scattered against the percentage of  $\Delta$ SSAT data points that the model can match (see methods).

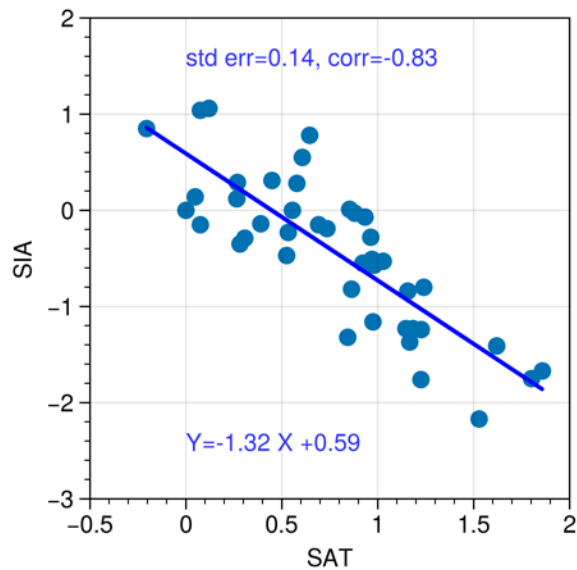


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550 Figure A5. Scatter Plot for climatological  $\Delta$ SSAT at each observational proxy location versus  
 551 climatological  $\Delta$ SSAT averaged north of 60°N over entire Northern Hemisphere in each model

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553



565

566

567 Figure A6:- Scatter plot of SAT versus SIA for current period. JJA surface air temperature versus NH  
568 September Sea ice area for each year from 1979-2020. Anomalies computed from year 1979 values.  
569 SIA is from NSIDC (<https://nsidc.org/data/g02135/versions/3>) and Air temperature (area averaged  
570 north of 60°N) is from ERA5 reanalysis (Hersbach et al. 2020).

571

572

573 *Author contributions.* LCS planned and wrote the original draft. RS analysed model results and  
574 prepared the figures. Figure 1 which was prepared by IVM. AdB wrote the second draft. MS  
575 undertook additional analysis, checks and researched particular model results. All authors contributed  
576 to the final text.

577

578 *Competing interests.* The authors have no competing interests.

579

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584 National Supercomputing Service (<http://www.archer.ac.uk>) and the JASMIN analysis platform  
585 (<https://www.ceda.ac.uk/services/jasmin/>).

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