~~Scaled~~Generalized Kendrick ~~Mass Defect~~ Analysis for Improved Visualization of Atmospheric Mass Spectral Data

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Abstract. Mass spectrometry is an important analytical technique within the field of atmospheric chemistry. Owing to advances in instrumentation, particularly with regards to mass resolving power and instrument response factors (sensitivities), hundreds of different mass-to-charge (*m/z*) signals are routinely measured. This large number of detected ions creates challenges for data visualization. Furthermore, assignment of chemical formulas to these ions is time-consuming and increases in difficulty at the higher *m/z* ranges. ~~We present a technique called scaled~~Here, we describe generalized Kendrick ~~mass defect (SKMD)~~ analysis (GKA) to facilitate the visualization and peak identification processes for typical atmospheric organic (and to some extent inorganic) compounds. ~~SKMD~~GKA is closely related to ~~the previously proposed~~ resolution enhanced Kendrick mass defect analysis (REKMD~~). SKMD~~) which introduces a tunable integer ~~scaling factor~~ into the ~~mass defect~~Kendrick equation that effectively contracts or expands the mass scale. ~~The SKMD transformation maintains~~A characteristic of all Kendrick analysis methods is that these changes maintain the horizontal alignment of ion series related by integer multiples of the chosen base unit ~~that is characteristic of~~. Compared to traditional Kendrick ~~mass defect~~ analysis~~. However, the~~, GKA and REKMD use a tunable ~~integer acts~~parameter ("scaling factor") to alter the mass defect spacing between different homologue ion series. As a result, the entire mass defect range (-0.5 to 0.5) is more effectively used simplifying data visualization and facilitating chemical formula assignment. We describe the mechanism of this transformation and discuss base unit and scaling factor selections appropriate for compounds typically found in atmospheric measurements. We present an open-source graphical user interface (GUI) for calculating and visualizing ~~SKMD analysis~~GKA results within the Igor Pro Environment.

1 Introduction

Recent improvements to the sensitivities, resolving power, and time-response of chemical ionization mass spectrometers used frequently in atmospheric measurements has led to a fundamental change in the understanding of atmospheric chemistry and the composition of the Earth's atmosphere. However, these advances have also created challenges in visualizing and interpreting the measurements. For typical resolving powers of time-of-flight mass spectrometers used in atmospheric chemistry, a conventional display of a mass spectrum as intensity versus mass-to-charge ratio *(m/z)* can only be used to visually resolve the individual peaks across a narrow mass range. The intensity versus *m/z* visualization also gives little information about the composition of the ions being measured. To provide more chemical insight, various data visualization methods have been used to identify chemical relationships and trends. Some visualization methods display ions on a plot based on properties of their elemental composition, such as their H:C versus O:C ratios (van Krevelen plot; Van Krevelen, 1950) or average carbon oxidation state versus number of carbons (Kroll diagram; Kroll et al., 2011) of assigned ions. Other analyses relate compositional variables, such as the number of oxygen atoms, hydrogen atoms, or double bond equivalency of the assigned formula. However, the analyses just mentioned require formula assignments for each of the identified ions.

Analyses that do not rely on assigned chemical formulas of observed ions are advantageous for aiding in composition assignment and in visualizing data that contains ions of unassigned composition., One such analysis that can be visualized with minimal knowledge of the sample composition is plotting the difference between an ion's exact and ~~and nominal mass~~ integer mass (mass defect), against the ~~nominal~~ integer mass (Kendrick, 1963; Sleno, 2012) or exact mass. Since an ion's exact mass is determined by its elemental composition, the difference between an ion's ~~mass defect~~ integer and exact mass retains compositional information. By plotting the mass defect versus exact or nominal IUPAC mass, isobaric ions can be separated along the y-axis, thus improving the visualization (as compared to a typical intensity versus *m/z* mass spectrum) of closely spaced ions particularly across a wide mass range.

Previous literature has referred to the difference between the integer and exact mass as mass defect (Kendrick, 1963; Craig and Errock, 1959). However, we note that the terminology of "mass defect" in this application is incorrect as mass defect refers specifically to the difference in mass between the sum of the individual proton and neutrons in an atom and the actual mass of the nucleus due to the atom's binding energy. The difference between a molecule's integer mass and exact mass is due to how the mass scale of atoms is defined, not solely due to the binding energy of the nuclei, therefore, "mass defect" should not be used (Pourshahian, 2017). For example, the

mass defect of a ^{12}C atom in mass spectral analysis is 0 amu, while in physics it is 0.1 amu. Alternative names such as mass excess could be used in lieu of mass defect, though the previous adaptation of "mass defect" within the mass spectrometry community makes this transition difficult. Therefore, while we keep the term "mass defect" in this work, we have adopted the term generalized Kendrick analysis (GKA) when referring to quantities similar to those previously referred to as Kendrick mass defects. We do this to attempt to move away from incorrect terminology while also noting that with the use of the round function in Eqs. (2) and (3), the result is not technically a mass.

Kendrick analysis is one way in which mass defect analysis can be adapted to provide easier visualization of composition. In Kendrick analysis, the mass scale is redefined such that the mass of a base unit, ~~R_{IUPAC}, is rounded to its integer value~~ R, is set to its nucleon number, i.e. the number of protons and neutrons the molecule has (Kendrick, 1963; Hughey et al., 2001). For our purposes, we assume singly charged ions as they are most important in atmospheric chemistry real-time measurements. Multiple charges could be included in the future, but non-linearities will arise as the mass of the additional electrons contribute to its mass defect differently than the sum of individual elements in a molecule, which will need to be accounted for. Originally proposed using CH_2 as a base unit, the Kendrick mass transformation has since been generalized to other base units (e.g., O, CH_2O, etc.). Equation (1) shows this transformation:

$$\text{~~KM}(m/z, R_{IUPAC}) = \frac{m}{z} \times \frac{\text{round}(R_{IUPAC})}{R_{IUPAC}}~~ \quad \text{(1)}$$

$$m_k\left(\frac{m}{z}, R\right) = \frac{m}{z} \times \frac{A(R)}{R} \quad \text{(1)}$$

where ~~R_{IUPAC}~~R is the IUPAC mass of the base unit R., m_K is the mass of the molecule after the Kendrick unit conversion, and A is a nucleon number function describing the number of neutrons and protons in the base unit. As the electron involved in ionization changes the actual mass of the ion, the mass-to-charge ratio is not equal to mass even with single charges, therefore we use mass-to-charge in this work. The Kendrick mass defect is calculated using ~~Equation~~ Eq. (2.).

$$\text{~~KMD}(m/z, R_{IUPAC}) = KM(m/z, R_{IUPAC}) - \text{round}(KM(m/z, R_{IUPAC}))~~$$

$$KMD\left(\frac{m}{z}, R\right) = \frac{m}{z} \times \frac{A(R)}{R} - \text{round}\left(\frac{m}{z} \times \frac{A(R)}{R}\right) \quad \text{(2)}$$

Note that the order of the terms in Eq. (2) is determined mainly by convention within specific fields; we adopt the convention widely used in atmospheric chemistry. The round(m) functions similarly to the nucleon number function (A) in Eq. (1) as it is the difference between the exact numerical value and its nearest integer, which for the purposes

of computation we represent as round(). As a result of this transformation, ion series differing by an integer number of R units will have identical Kendrick mass defects. Typically, the result has been visualized in the two-dimensional space of Kendrick mass defect versus integer Kendrick mass, however integer IUPAC mass or exact IUPAC mass are also acceptable. In these spaces, homologous ion series differing by R will align horizontally. Traditional Kendrick mass defect analysis has proven to be an instrumental tool for visualizing mass spectral information from a variety of fields including petroleomics, proteomics, and atmospheric measurements (Taguchi et al., 2010; Marshall and Rodgers, 2004; Junninen et al., 2010; Sleno, 2012).

Kendrick ~~mass~~ analysis only requires the exact mass of the identified ion, not the assigned molecular formula, allowing for identification of ion series related by the molecular subunit R. Errors in the assignment of exact masses, particularly for ions with an unassigned elemental composition, will result in a "fuzzy" appearance to the horizontal alignment due to peak-fitting errors. Using traditional ~~KMD~~Kendrick analysis~~.~~ (Eqs. (1) and (2)), the data points tend to only occupy a small fraction of the available ~~KMD~~Kendrick mass defect space (defined mathematically from -0.5 to +0.5) resulting in congested data visualizations that can make it challenging to identify homologous ion series. The limited range of the ~~KMD~~Kendrick mass defect space arises because of "dead-~~ ~~space" between the masses of common chemical formulas. Particularly for compounds present in complex environmental mixtures, observed ions masses tend to be periodically spaced with ~1 atomic mass unit (amu) gaps and the Kendrick transformation maintains this spacing. The existence of the dead-~~ ~~space can be explained because environmental molecules are generally made of a limited number of elements (H, C, O, N, S).

$$\text{REKM}(m/z, R_{IUPAC}, X) = \frac{m}{z} \times \frac{\text{round}\left(\frac{R_{IUPAC}}{X}\right)}{\frac{R_{IUPAC}}{X}} \quad (3)$$

~~REKMD is defined analogously to Equation 2 using REKM rather than KM, as shown in Equation 4.~~

$$\text{REKMD}(m/z, R_{IUPAC}, X) = \text{REKM}(m/z, R_{IUPAC}, X) - \text{round}(\text{REKM}(m/z, R_{IUPAC}, X)) \quad (4)$$

Recently Fouquet and Sato (Fouquet and Sato, 2017c, a, b; Fouquet et al., 2018) have introduced the concept of "resolution enhanced Kendrick mass defect" (REKMD) analysis to provide improved visualization and analysis of mass spectrometry data, particularly for polymers. REKMD introduces the concept of fractional base units by using integer divisors (X) as shown in ~~Equation 3:~~ Eq. (3):

$$\text{REKMD}(\frac{m}{z}, R, X) = \frac{m}{z} \times \frac{\text{round}\left(\frac{R}{X}\right)}{\frac{R}{X}} - \text{round}\left(\frac{m}{z} \times \frac{\text{round}\left(\frac{R}{X}\right)}{\frac{R}{X}}\right) \quad (3)$$

For integer values of X, ions differing by integer numbers of R will have identical REKMD values. Specific ~~non-integer~~ rational values of x can also be used as shown previously (Fouquet and Sato, 2017b). We will use x to denote

rational values and X to denote integer values for the REKMD equations. Appropriate selection of X or x amplifies mass defect variations increasing the range of mass defect space occupied by a given dataset and improving horizontal alignment of homologous ion series. REKMD analysis method has been used in polymer chemistry previously (Fouquet and Sato, 2017a, b; Fouquet et al., 2018), but to our knowledge has not been previously applied to atmospheric samples. It should be emphasized that the REKMD transformation has no impact on the mass resolution of the data, but rather alters the separation of ions in mass defect space. Through appropriate selection of X or x, the separation in mass defect space can be tuned to enable easier visualization of homologous ion series resulting in an apparent "resolution enhancement."

~~In this work, we present a variation of REKMD analysis, which we term scaled Kendrick mass defect (SKMD) and discuss in general terms the principles of the mechanisms by which the mass defect space is expanded. We demonstrate its application for visualization of atmospheric trace gas composition, describe how choices of R and *X*, which we term scaling factor when used in SKMD, will affect the visualization, show how the technique can aid in molecular formula assignment to unknown ions, and describe an open-source graphical user interface (GUI) for performing the analysis. We suggest that this analysis can be used not only for understanding ambient atmospheric gas-phase measurements as shown here, but could have potential use in aerosol measurements, and more broadly for other types of mass spectrometric data.~~

In this work, we expand this previously reported analysis tool for use in atmospheric chemistry. We call this analysis generalized Kendrick analysis (GKA) as it is a slight rearrangement of the original Kendrick mass equation and of the REKMD equation. Ultimately, it may be appropriate to drop the term "generalized", but we maintain the term in this work to distinguish it from the standard Kendrick analysis commonly used in atmospheric chemistry. We then discuss in general terms the principles of the mechanisms by which the mass defect space is expanded. We demonstrate its application for visualization of atmospheric trace gas composition, describe how choices of R and X, which we term scaling factor when used in GKA, will affect the visualization, show how the technique can aid in molecular formula assignment to unknown ions, and describe an open-source graphical user interface (GUI) for performing the analysis. We suggest that this analysis can be used not only for understanding ambient atmospheric gas-phase measurements as shown here, but could have potential use in aerosol measurements, and more broadly for other types of mass spectrometric data as has been demonstrated previously (Fouquet and Sato, 2017c; Zheng et al., 2019; Fouquet, 2019).

2 Vocus Proton Transfer Mass Spectrometer

For illustrating the applications of ~~SKMD analysis~~ GKA for atmospheric chemistry, we use measurements from an Aerodyne and Tofwerk Vocus Proton-transfer mass spectrometer. Details of this instrument are discussed

elsewhere (Krechmer et al., 2018). This measurement technique is commonly used in atmospheric chemistry as it can detect and quantify a large number of hydrocarbons (with the exception of small alkanes) as well as oxygen, nitrogen, and sulfur containing organic molecules found in the environment (Sekimoto et al., 2017). The instrument was deployed in Billerica, MA from March to August of 2021, with 1 Hz data averaged to 30 minutes before analysis. For the purposes of this discussion, we will be discussing the data collected on July 9, 2020, from 4:00 to 23:00 local time (UTC – 4). All data was analyzed in Tofware v3.2.5 within the Igor Pro v9.0.0.10 environment (Wavemetrics, Inc., Portland, OR). Only signals above a certain threshold (1 count per second) and which changed more than 30% between evening and morning were included in the analysis. The reagent ions were also removed from the analysis. This ambient dataset is used in Sect. 3 to demonstrate the principles of Kendrick analysis and illustrate how different scaling factors separate mass spectral data. The same data is used in Sect. 4 to present how Kendrick analysis can aid in understanding chemical composition in measured mass spectra. Individual ion signals are also purposefully unassigned and refit to demonstrate the usefulness of this tool for determining unidentified signals.

3 ~~SKMD~~Generalized Kendrick Analysis – Concepts and Method

3.1 ~~Scaled~~Generalized Kendrick ~~Mass Defect~~Analysis

Traditional Kendrick mass defect analysis uses round(R_{IUPAC}R) (or the nucleon number of R) as the ~~nominal~~integer mass for the mass scale transformation (~~Equation~~Eq. (1)~~;~~)); however, it is mathematically acceptable to use other integer values to maintain horizontal alignment of ion series related by an integer number of R. In fact, one can expand or contract the mass scale by replacing round(R_{IUPAC}R) in ~~Equation~~Eqs. (1) and (2) with an integer scaling factor X as in ~~Equations 5 and 6:~~Eq. (4) (generalized Kendrick analysis):

$$\mathrm{SKM}(m/z, \mathrm{R_{IUPAC}}, X) = \frac{m}{z} \times \frac{X}{\mathrm{R_{IUPAC}}} \quad (5)$$

$$\mathrm{SKMD}(m/z, \mathrm{R_{IUPAC}}, X) = \mathrm{SKM}(m/z, \mathrm{R_{IUPAC}}, X) - \mathrm{round}(\mathrm{SKM}(m/z, \mathrm{R_{IUPAC}}, X)) \quad (6)$$

~~with X values less than round(R_{IUPAC}) contracting the scale and values greater than round(R_{IUPAC}) expanding the scale.~~

~~When analyzing mass spectral data with Kendrick mass defect~~

$$\mathrm{GKA}\left(\frac{m}{z}, \mathrm{R}, X\right) = \frac{m}{z} \times \frac{X}{\mathrm{R}} - \mathrm{round}\left(\frac{m}{z} \times \frac{X}{\mathrm{R}}\right) \quad (4)$$

with X values less than round(R) contracting the scale and values greater than round(R) expanding the scale. Note that this form of the equation has been demonstrated before in polymer mass spectrometry (Fouquet, 2019). However, its applications and advantages with respect to visualization and ion assignment as used in atmospheric

chemistry has yet to be identified and discussed. When inspecting mass spectral data using generalized Kendrick analysis, the main goal is to identify horizontal lines of ions related by integer numbers of R. When X is introduced into the equation and the scale changes, this horizontal alignment is preserved, however, the lines are separated more clearly in the mass defect dimension allowing for simpler identification of related ions. ~~We label this scaled Kendrick mass (SKM) and scaled Kendrick mass defect (SKMD).~~ For the two-dimensional visualizations of ~~scaled~~generalized Kendrick mass defect versus mass, we find the exact or ~~nominal~~integer IUPAC mass rather than ~~SKM~~Kendrick mass to be the most intuitive x-axis.

~~SKMD~~GKA (Eq. ~~6)~~(4)) is mathematically identical to REKMD (~~Equation 4)~~Eq. (3)) for integer scaling factors (X) satisfying ~~Equation 7:~~Eq. (5):

$$\text{round}(\frac{\cancel{2 \times R_{IUPAC}}}{3} \frac{2 \times R}{3}) < X \le \text{round}(2 \times \cancel{R_{IUPAC})} \; (7 R) \quad (5)$$

~~since round(R_{IUPAC}/X) will equal 1. This range of X coincides with the recommended range of integer divisors for REKMD analysis (Nakamura et al., 2019). SKMD differs from REKMD in that the mass defect expansion is linear in X at values of $X \le$ round(2 R_{IUPAC}/3) unlike the non-linear expansion for REKMD (Fig. S1). These smaller X values can be useful when analyzing large mass ranges. Additionally, unlike REKMD, no upper limit on X exists for SKMD analysis (Fig. S1) which can be useful in tuning the separation of homologous ion series when larger separation in the y-axis is desired as will be discussed later. However, unlike REKMD for which select real values of X provide mathematically acceptable solutions, only integer X are allowed for SKMD to maintain horizontal alignments. Integer values provide similar separation in REKMD analysis as real values (Fouquet et al., 2019), suggesting that limiting X to integers does not restrict this analysis.~~

~~Compared to a traditional KM/KMD analysis, SKM/SKMD has two advantages: 1) for select combinations of R and X, SKMD visualization will provide increased information on chemical composition and 2) the increased range of mass defect space will lead to clearer alignment of homologue ion series enabling better visual identification and potentially aiding in chemical formula assignment of ions. For both KMD and SKMD~~since round(R/X) will equal 1. This range of X coincides with the recommended range of integer divisors for REKMD analysis (Nakamura et al., 2019). GKA differs from REKMD in that the mass defect expansion is linear in X at values of $X \le$ round(2 *R/3) unlike the non-linear expansion for REKMD (Fig. S1). These smaller X values can be useful when analyzing large mass ranges. Additionally, no upper limit on X exists for GKA analysis (Fig. S1) which can be useful in tuning the separation of homologous ion series when larger separation in the y-axis is desired as will be discussed later. The increased expansion or contraction ability of GKA compared to REKMD may not be useful for every set of mass spectrometric data, as the range of X available in REKMD may be sufficient. Though as will be discussed, the increased expansion may lead to easier visualization of the different ions. As previously mentioned, REKMD can

use select rational values of x. To maintain horizontal alignment of homologous series, only rational values of x satisfying $x*\text{round}(R/x)$ = integer are allowed (Fouquet, 2019). Substituting that condition into Eq. (3) results in

$$\text{REKMD}\left(\frac{m}{z}, R, x\right) = \frac{m}{z} \times \frac{integer}{R} - \text{round}\left(\frac{m}{z} \times \frac{integer}{R}\right) \quad (6)$$

Showing that all expansions achievable with REKMD using rational values of x can also be achieved with GKA. With GKA, pseudo-continuous expansion becomes possible without introducing extra multiplication factors as is necessary in REKMD (Fouquet, 2019) and thus it is appropriate to consider GKA as a generalization of traditional Kendrick analysis and REKMD.

For both KMD and GKA analysis, ions differing by integer units of R will align horizontally in these spaces. Note that any R can be used, though for the purposes of this work we focus on the divisors when the Kendrick base is ^{16}O.

3.2 Visualization of chemical composition

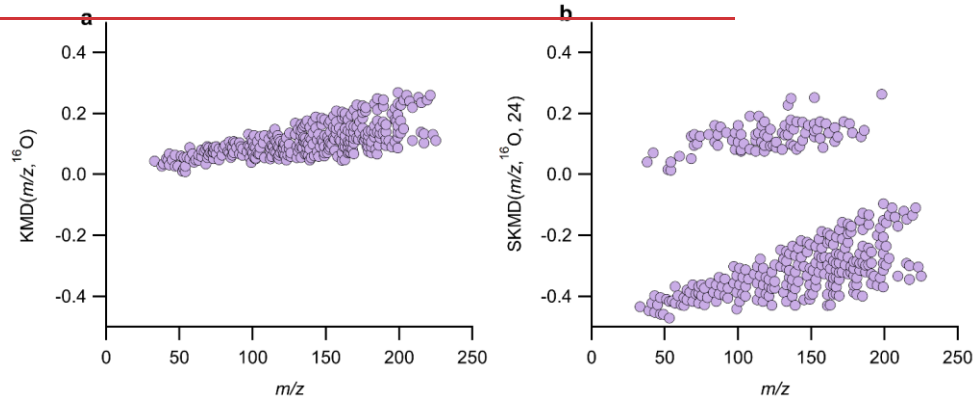
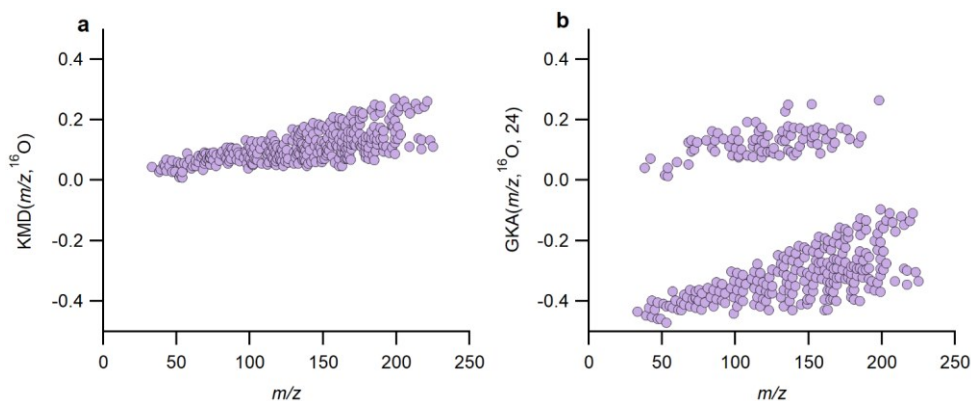



Figure 1 Using ambient data collected by the Vocus in Billerica, MA, (a) traditional KMD plot using a base of ^{16}O and (b) ~~SKMD~~GKA plot using a base of ^{16}O and X=24, where the two groupings correspond to even (positive ~~SKMD~~GKA values, odd number of nitrogen atoms) and odd (negative ~~SKMD~~GKA values, zero/even number of nitrogen atoms) nominal ~~m/z~~mass. Fig. S2 shows (a) zoomed in to illustrate that ion alignment remains blurred even with different y-axis scaling.

The combined choice of ~~R_{IUPAC}~~R and X impacts the mass scale expansion/contraction and will dictate how ~~SKMD analysis~~GKA aids visualization of composition and alignment of homologous ion series. Figs. 1a and 1b compare ~~KMD~~KM(m/z,^{16}O) and ~~SKMD~~GKA(m/z, ^{16}O, 24)~~.~~). For the ~~SKMD~~GKA(m/z, ^{16}O, 24) analysis, the mass scale is expanded by a factor of ~3/2~~.~~ (derived from the approximate reduced fraction of X/R, or 24/15.995). As a result of this scaling, ions with odd nominal masses in IUPAC mass space will be shifted towards half-integer masses while even nominal masses in IUPAC space will remain at approximately integer values. Assuming positive mass defects in IUPAC mass space, nominally odd mass ions will typically have negative ~~scaled Kendrick mass defects~~GKA values and nominally even mass ions will have positive ~~scaled Kendrick mass defects~~GKA values leading to the two groupings in Fig. 1b. This transformation of the ~~scaled~~generalized Kendrick masses is also shown in ~~Fig. 2~~Figure 2~~Figure 2~~. Figs. 2a and 2b show how ions in IUPAC m/z or KM space span a narrow mass defect range whereas Fig. 2c shows that for the ~~SKM~~GKA(m/z, ^{16}O,24), a transformation of ~3/2, nominally odd mass ions (in IUPAC m/z) have a ~~SKMD~~GKA(m/z, ^{16}O, 24) of around -0.5 while the ~~SKMD~~GKA(m/z, ^{16}O, 24) of even mass ions remains around zero.

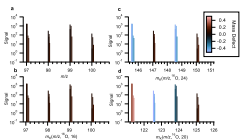
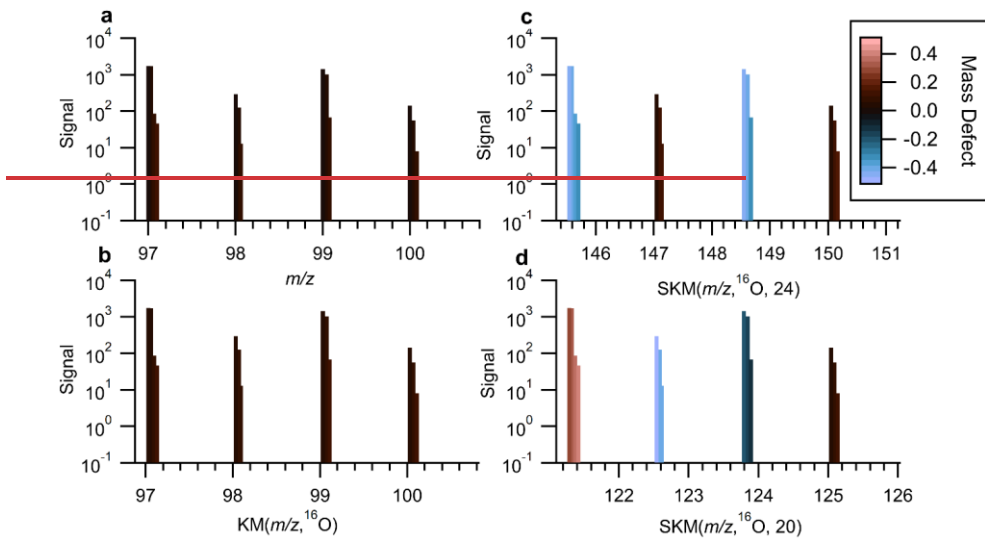



Figure 2 (a) An example section of a mass spectra of ambient data measurements plotted against the IUPAC mass-to-charge values. (b) The same series of identified peaks plotted against Kendrick mass with a base unit of ^{16}O and $X = A(^{16}O) = 16$, (c) ~~scaled~~generalized Kendrick mass with R=^{16}O and ~~X=24~~, and (d) generalized Kendrick mass with R=^{16}O and X=20~~, and (d) scaled Kendrick mass with R=^{16}O and X=24~~. In all plots, the identified ions are colored by the mass defects after the mass transformation.

By separating even and odd nominal IUPAC masses into different regions, the ~~SKMD~~GKA(m/z, ^{16}O, ~~24~~) visualization provides information on chemical composition not available with a standard KMD plot. Specifically, for de-isotoped data sets comprised of compounds following the nitrogen rule, the two groups will represent compounds with odd or even/zero nitrogen atoms. For atmospheric chemistry measurements, compounds with two or more nitrogen atoms are usually minor (both in abundance and in number of species) compared to compounds with no nitrogen atoms and thus the ~~SKMD~~GKA with $X/$~~R$_{IUPAC}$~~R of ~3/2 provides visual information on nitrogen versus non-nitrogen containing compounds. A notable exception would be situations in which organic dinitrates are abundant. In our data, we identified only 15 compounds (3% of the total number of ions included in analysis) that contained 2 nitrogen atoms. Although other methods can be used to separate even and odd m/z (masking, making multiple plots, etc.), ~~SKMD~~GKA can separate the even and odd masses on the same plot making comparison between the groups of ions simpler.

One can intuit how the choice of R and X affects the degree of expansion through inspection of the approximate reduced ~~fraction~~fractional value of $X/$~~R$_{IUPAC}$~~R. The reciprocal of the denominator of the reduced fraction represents the fractional mass intervals IUPAC integer masses are transformed to. As such, the number of groupings from a certain transformation is the reciprocal of the denominator. Note that the reduced fractional value of $X/$R does not determine the amount of contraction or expansion of the mass defects, but rather determines the number of individual groupings of related ions. For instance, for R=^{16}O and X = 8 or 24, the approximate fractions are 1/2 and 3/2 and thus interval IUPAC masses will be transformed to half-integer and integer ~~SKM~~GKA masses (Fig. 2c) resulting in two groupings. Fig. S3 shows the results of $X/$~~R$_{IUPAC}$~~R of ~3/2 for other choices of ~~R$_{IUPAC}$~~R. For R = ^{16}O and X = 4, 12, or 20, the approximate reduced fractions are 1/4, 3/4, and 5/4, respectively, and all these choices will transform even IUPAC integer masses to integer or half-integer ~~SKM~~GKA values and odd IUPAC integer masses to quarter and three-quarter integer values (Fig. 2d). Thus, ~~SKMD~~GKA values will roughly start around 0.0, ±0.25, and ±0.5 and this transformation ~~result~~results in four "groupings" of ~~SKMD~~GKA values (~~Fig.~~Figure ~~Figure~~ 3a). Although four groupings will result for X = 4, 12, or 20, the exact ~~SKMD~~GKA value of a given ion will depend on X. Likewise, for R=^{16}O and X = 2, 6, 10, or 14 will result in 8 groupings with the groups representing alternating even and odd ~~nominal~~ integer IUPAC masses. When the denominator of the reduced fraction is large, as would happen for X =17 with R=^{16}O (a reduced fraction of 17/16), the groupings overlap significantly (Fig. 3b). For odd

denominators, such as encountered for R=^{12}CH$_2$ with $X = 8$ (approximate reduced fraction of 4/7), the groups will no longer correspond to even/odd ~~nominal~~ integer IUPAC masses, but rather a different metric, and thus the ~~SKMD~~GKA visualizations will provide alternate but complimentary information. Despite the limitations in these last two examples, visualization can still be improved compared to a traditional KMD plot since the homologous series will be separated more clearly into individual horizontal lines, as seen in Fig. 3b. These other scaling factors may be useful when looking at spectra with fewer identified ions, as separating horizontal homologous ion series can be more useful than creating groupings of ions with the same number of nitrogen atoms or other grouping criteria.

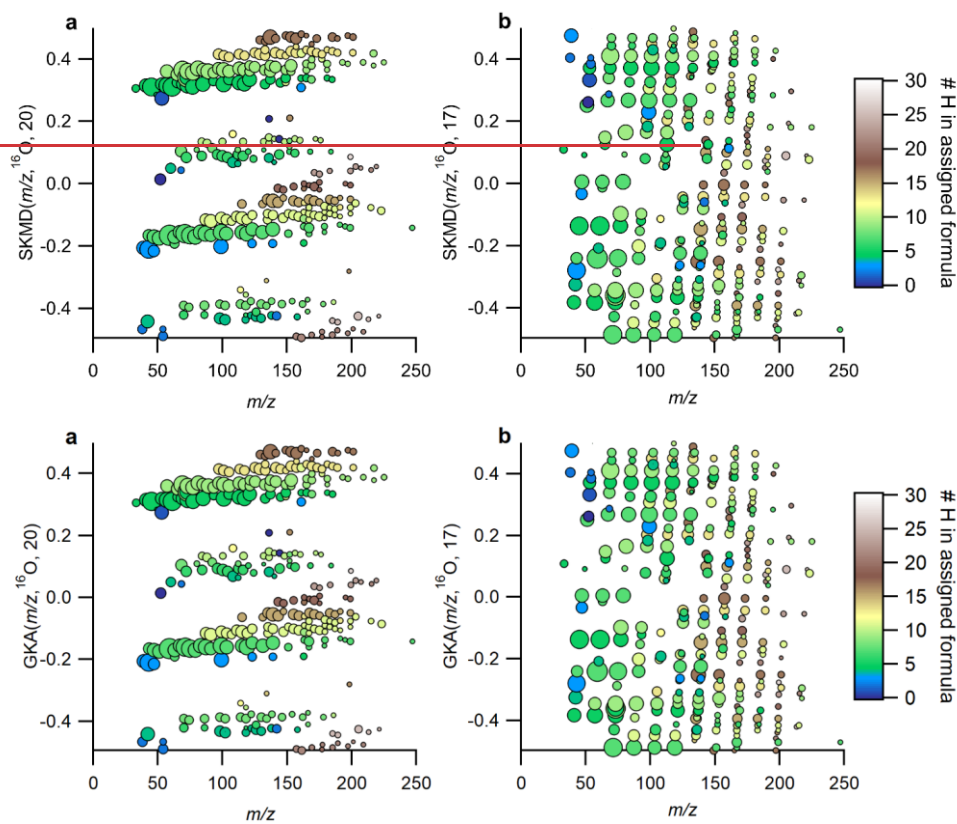



Figure ~~3~~3 (a) ~~SKMD~~GKA plot of data obtained from Vocus ambient measurements with base of ^{16}O, and (a) $X =$ 20 (b) $X = 17$. The points are colored by the number of hydrogens in the assigned formula and sized by the log of the measured intensity. Fig. S4 shows this same transformation but zoomed into a small section to show how the chemical formulas of the ions in a horizontal line are related.

The numerator of the reduced fraction is important for understanding the degree of expansion/contraction of the mass scale. At low numerator values, the mass scale contraction reduces the spread of ~~SKMD~~GKA values around a given nominal IUPAC mass, while higher numerator values increase the spread (Fig. 4). At sufficiently high values of X, "aliasing" or "wrap-around" is introduced (+0.5 is transformed to -0.5), which can be seen in Fig. ~~S4~~S5 when $X=20$ around m/z 100-250. Aliasing is non-linear with X and is more common when dealing with divisors that give increased numbers of "groupings" thus explaining why $X=40$ (approximate reduced fraction of 5/2)

displays negligible aliasing compared to $X=20$ (approximate reduced fraction of 5/4; Figs. 4 and ~~S4~~S5) As aliasing can complicate the interpretation of the data, it is recommended to either manually anti-alias data (most applicable for small data sets) or select X that maximally expands the data in ~~SMKD~~GKA space while also minimizing aliasing. This can be determined by plotting the defect spreads (difference between highest and lowest ~~SKMD~~GKA(m/z, ~~R$_{IUPAC}$~~R, X)) as a function of m/z with various values for X.

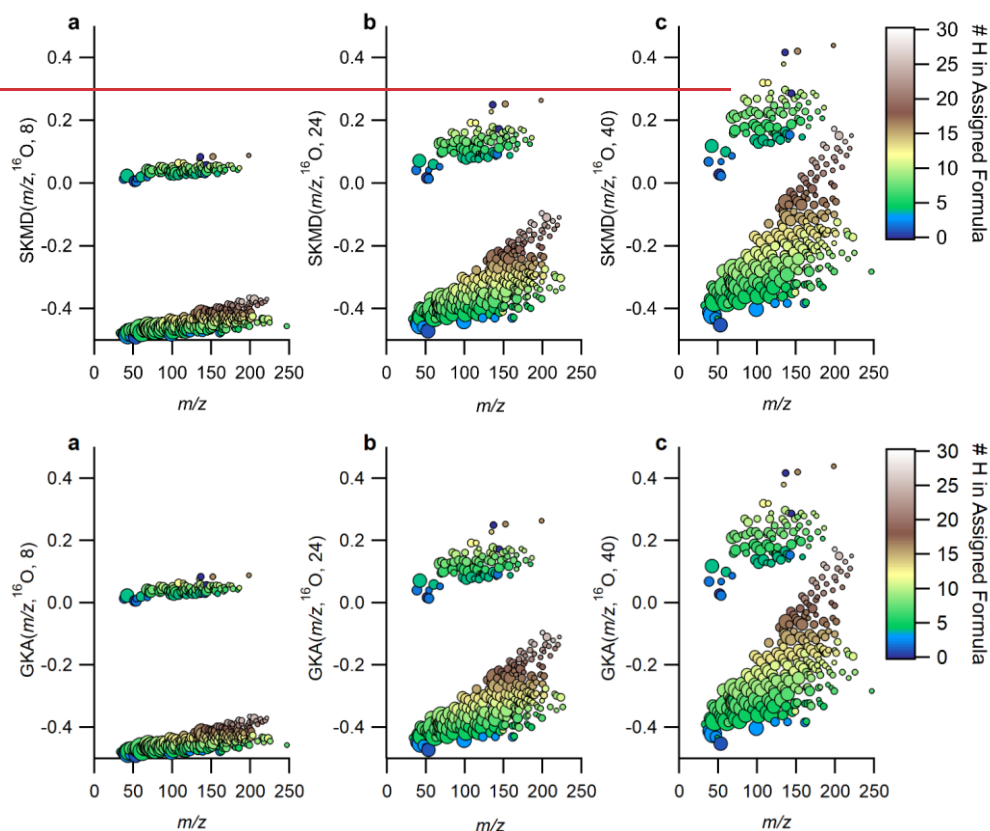



Figure ~~4~~4 Expansion of the same data in ~~SKMD~~GKA space as the values for X are increased while using ^{16}O as R. ~~An X value of 40 would not be possible in REKMD analysis, however, for the data visualized here, it provides acceptable resolution.~~ The

points are colored by the number of hydrogens in the assigned formula and sized by the log of the measured intensity.

300   In addition to the even/odd ~~nominal~~ integer IUPAC m/z separation, and corresponding information on the number of nitrogen atoms discussed earlier, select combinations of X and ~~R_{IUPAC}~~R provide further information on chemical composition. For instance, for $C_xH_yO_zN_w$ compounds for w of 0 and/or 1 and base units of ~~R_{IUPAC}~~R ^{16}O or ^{12}C, select values of X will lead to grouping of compounds with the same number of hydrogen atoms in the same area of the ~~SKMD~~GKA plot (e.g., Figs. 3a and 4). Moreover, within each grouping of a constant number of hydrogen

305   atoms, each horizontal line will correspond to a constant number of carbon atoms when using a base of ^{16}O or a constant number of oxygen atoms when using a base of ^{12}C. For a base unit of ^{16}O, the number of carbon atoms will increase as one moves towards more positive mass defects while for the base unit of ^{12}C, the number of oxygen atoms will increase as one moves towards more negative mass defects. The separation by number of hydrogen atoms (and other groupings) is further explained in Sect. S2 and Fig. ~~S5~~S6 of the Supplement.

310   As in traditional KMD analysis, select choices of ~~R_{IUPAC}~~R provide information on double bond equivalency (DBE), an estimation of the number of double bonds (or degrees of unsaturation, including rings) in an elemental formula shown in ~~Equation 8:~~Eq. (7):

$$\text{DBE} = c - \frac{h}{2} + \frac{n}{2} + 1 \quad (8)$$

$$\text{DBE} = c - \frac{h}{2} + \frac{n}{2} + 1 \quad (7)$$

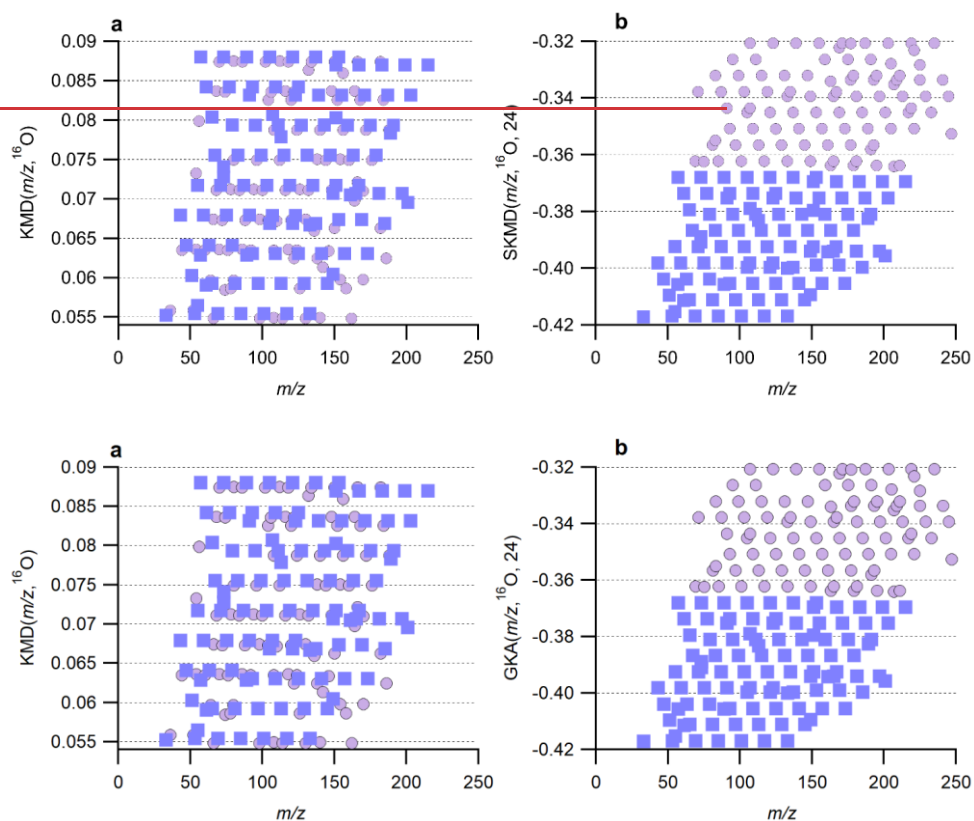
315   where c, h, and n are the number of carbon, hydrogen, and nitrogen atoms in the formula, respectively. For ~~R_{IUPAC}~~R of ^{16}O or ^{12}CH$_2$ horizontal lines correspond to constant DBE while for ^{12}C, DBE will increase moving from left to right across a horizontal line.

3.3 Improved visual alignment of homologue ion series

Figs. 5a and 5b show an example of the improved visual alignment of homologue ion series. Both panels contain

320   the same number of points, with ~50% of the points identical in both panels. The horizontal alignment of the points is visually clearer with ~~SKMD~~GKA(m/z, ^{16}O, 24) compared to normal KMD(m/z, ^{16}O). The apparent improvement in alignment results from the increased vertical spacing between the different horizontal lines. This increase in spacing is achieved by increasing the mass defect range occupied by the data and by moving the masses at +1 m/z to a different area of the ~~SKMD~~GKA(m/z, ^{16}O, 24) plot. Once the identified ions are separated into related

325   groupings, using the software tool presented here, a subset of these ions can be easily selected and re-analyzed with

a different $R_{\text{IUPAC}}R$ and X, as will be discussed in Sect. 3.4, providing more in-depth information about a specific subset of ions.

330   **Figure 3** A zoomed in section of the (a) KMD plot from Fig. 1a and (b) the ~~SKMD~~GKA plot from Fig. 1b. Both subpanels contain the same number of total points. The square purple points correspond to the same ions in the subpanels. The circle lilac points represent ions unique to each subpanel. Note the different y-axis range in each subpanel.

3.4 GUI for ~~REKMD Analysis~~GKA in Igor Pro Environment

The data in this work was analyzed using a graphical user interface (GUI) we built that operates inside the Igor Pro Environment (Wavemetrics, Lake Oswego, OR; Igor Pro v9 and above). The GUI allows the user to select a data set to perform ~~SKMD~~GKA analysis with the R and X of their choice. The code currently has $^{12}CH_2$, ^{16}O, ^{14}N, ^{12}C, and isoprene (C_5H_8) available to choose from, though other bases can be added to the list by small modifications to the code. The GUI also provides optional inputs for intensity data for sizing/coloring of the points made in the ~~SKMD~~GKA plots. The GUI allows interactive point filtering by providing an option for the user to draw a polygon around a set of points and recalculate the ~~SKMD~~GKA plot on just those points, with the option of using a different R or X for the analysis. Filtering options are included to remove the points with the largest and smallest signals for easier visualization. The code for the GUI is available for download ~~from~~as part of the Supporting Information with any future updates stored on GitHub, with more information in Sect. S3 and Fig. ~~S6~~S7 of the Supporting Information.

4 Example Applications of ~~REKMD Analysis~~GKA

4.1 Visualizing Composition

To explore the utility of ~~SKMD~~ GKA, we delve further into the data collected in Billerica, MA presented in the previous sections to show how homologous ion series alignments can be used. Ions were assigned based on high-resolution fully constrained peak fitting (Cubison and Jimenez, 2015; Stark et al., 2015) though this analysis technique works without prior knowledge of the molecular formulas, just the exact measured m/z (and mass with knowledge of the charge). High-resolution, fully constrained, peak fitting can possibly aid in determining if a peak assignment is missing from the measured data; however, this becomes more difficult at higher m/z and with higher complexity samples (Timonen et al., 2016; Cubison and Jimenez, 2015). An example of the peak fitting has been demonstrated previously (Cubison and Jimenez, 2015). In Fig. 6, the GKA plots of the ambient data collected in Billerica, MA are shown, with points colored by the percent change in intensity of the signal between morning and evening. For this analysis, we focus on early morning and late afternoon as times when emissions, photochemistry, and dynamics are known to be different. The ions plotted are limited to those which satisfy the following conditions: 1) have an average intensity above 1 count per second (cps), 2) change more than 30% between the morning and evening, 3) are not the primary reagent ions. The percent difference is calculated as the difference between the morning and evening integrated intensities divided by the intensity in the morning, leading to positive values reflecting an increase in signal in the afternoon compared to the morning. As some ions have intensities of 0 ions/s

in the morning, the percent change can be undefined, therefore points with percentage increases greater than 250%, including undefined increases, are the same color.

Fig. 6a shows that the points at the center of each of the groups increase the most (colored black), while those with slightly higher or lower GKA ~~Fig. 6, the SKMD~~SKMD(m/z, ^{16}O, 24) increase less or even decrease. Additionally, as this divisor separates odd and even m/z, this plot also shows that the odd m/z ions, consisting of $(C_xH_yO_z)H^+$ compounds and compounds with an even number of nitrogen atoms (assuming closed electron shell molecules ionized via proton transfer), have the largest fractional increase. Using the polygon selection tool in the GUI, we can reperform the ~~SKMD~~GKA analysis on just the $C_xH_yO_z$ compounds (and the 15 identified $C_xH_yO_zN_{2w}$ compounds). Fig. 6b shows the results of performing the ~~SKMD~~GKA analysis on this subset of data using a different X, in this case, 20. Note that manual anti-aliasing has been applied. With an approximate reduced fraction of 5/4, this new transformation would nominally result in 4 groupings, however since only ions with odd nominal IUPAC m/z were included, only 2 groupings are visible. These groupings are separated by ~2 amu in IUPAC m/z space and, as such, chemical formulas will be related by the addition of 2 hydrogen atoms. For instance, $C_7H_{10}O_5H^+$ will be in the lower group while $C_7H_{12}O_5H^+$ will be in the higher group with ~~SKMD~~GKA(m/z, ^{16}O, 20) values of -0.105 and 0.415, respectively. Arrows are included to show the transitions between chemical formulas within the groupings. ~~This plot has the advantage of further spacing out the ions allowing for clearer chemical groupings and alignments. It shows that the compounds with the greatest number of hydrogen atoms~~This plot shows that the most reduced species (those at the top of each grouping) decrease the most between the morning and evening hours. Some of the signals that increase the most have 5, 9, or 10 carbon atoms, suggesting they could be from isoprene or monoterpene oxidation over the course of the day. Some specific formulas (and potential identifications) that increase are $(C_5H_8)H^+$ (isoprene or an isomer or an ion fragment), $(C_5H_{10}O_4)H^+$ (a monosaccharide), $(C_9H_{14}O_4)H^+$, and $(C_{10}H_{17}O_4)H^+$ (possible monoterpene oxidation products). These ion signals could correspond to the emission and oxidation of biogenic compounds, such as terpenes, which are anticipated to increase as biological activity and atmospheric oxidation occurs. Relatedly, the compounds that increased the most have either 9, 11, 13, or 15 hydrogen atoms in the assigned formulas, including the proton from ionization. This analysis can aid in understanding general atmospheric chemistry and how oxidation affects molecular structures and saturation in a bulk method.

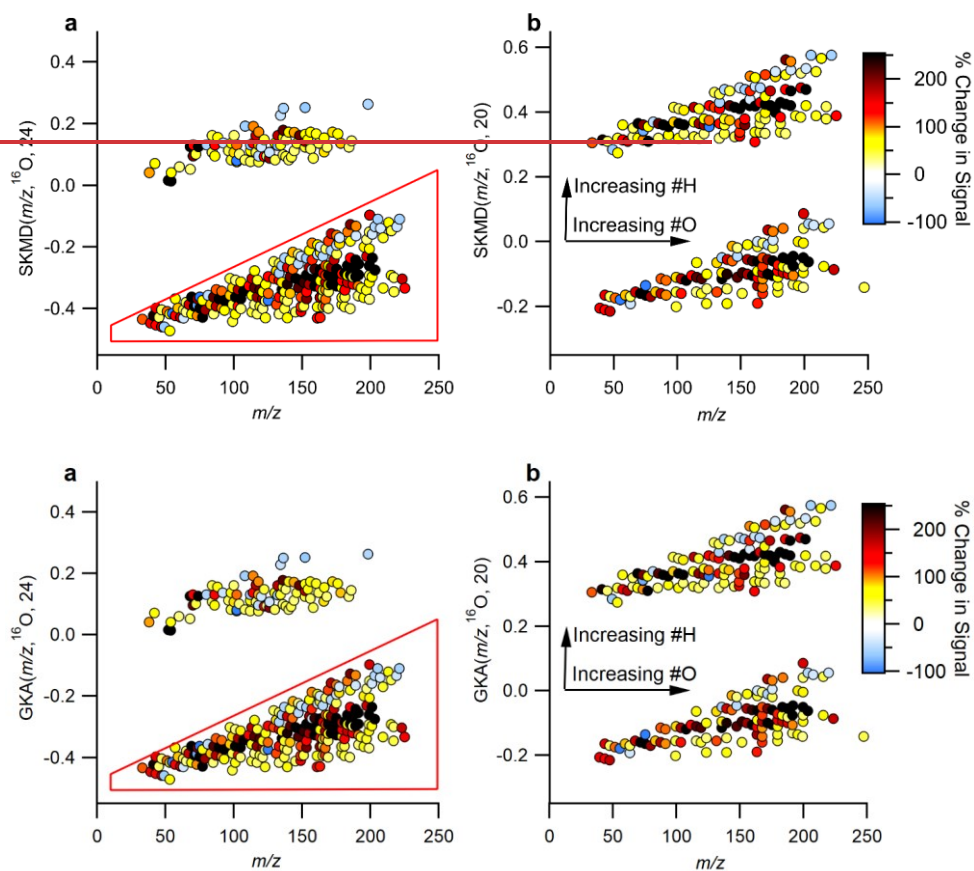



Figure 4 (a) ~~SKMD~~GKA plot using X=24 with a ^{16}O base. Points are colored by the percent change in the signal between the morning and evening during one day of measurements. (b) Using the points selected with the polygon tool in the GUI, the ~~SKMD~~GKA plot is remade using X=20. The arrows correspond to the changes in an individual grouping. Another split is created when re-calculating ~~SKMD~~GKA with a different X based on number of hydrogen atoms in the formulas. Note that manual anti-aliasing has been applied in panel (b) to keep related ions together ~~and that the y-axis range of the two subpanels differs~~.

4.2 Using ~~REKMD~~GKA for Chemical Formula Assignment

By increasing the separation in mass defect space, ~~SKMD analysis~~GKA can aid in chemical formula assignment, particularly when extension of homologue series is an appropriate tool for aiding in assignment. ~~SKMD analysis~~ GKA can also provide insight into potential ion misassignment. Fig. 7a shows a normal KMD plot, KMD(m/z, ^{16}O), while Fig. 7b shows ~~SKMD~~GKA(m/z, ^{16}O, 20). The colored points are the same identified ion signals in both figures. The grey points in Fig. 7~~b~~a are points that appear within the mass defect space using a traditional KMD analysis but are not visible with GKA (Fig. 7~~a~~b) since they are shifted to another area of the mass defect space. The points are colored by the number of carbon atoms and all formulas have 9 hydrogen atoms in the assigned formula. The turquoise points are assigned ions that were removed, then added back into the peak list as "unknowns" with Tofware's automatic peak fitting procedure. ~~The grey points in Fig. 7a are points that are not present in Fig. 7b.~~ This figure shows that there is significantly more overlap with other ions in a KMD(m/z, ^{16}O, 16) plot than ~~SKMD~~GKA(m/z, ^{16}O, 20). The separation of ions can aid in ion formula identification. As horizontal lines are made for ions with increasing number of ^{16}O atoms in the formula, and the same number of hydrogens and carbon atoms, identifying missing ions is a simple matter of adding or subtracting an O atom from the adjacent formula to find the missing ion. These horizontal relationships can be useful for automatic or semi-automatic ion identification in the future. Note that the homologous ion series are still present in Fig. 7a but are just visually more difficult to see without prior knowledge of the ion identities.

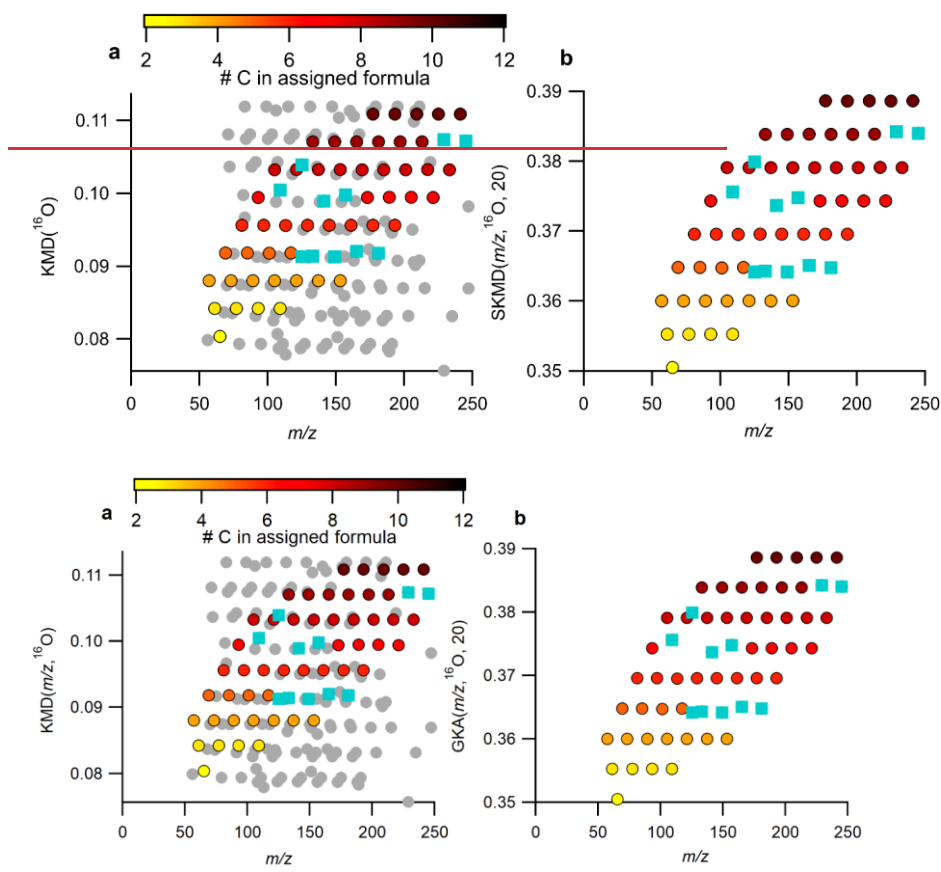



Figure 5 ~~A subset of the ambient VOCUS data in (a) **a** KMD plot with base ¹⁶O and (b) a SKMD plot using ¹⁶O as the base and X=20.~~ ~~The grey points in (a) are points that appear within the field of view due to the compression of the KMD space. Colored points are the same~~ ~~ions in both subpanels. Circles are colored by the number of carbon atoms in the formula. Ions that were removed and then re-added using~~ ~~Tofware's built-in peak addition, with no human intervention to improve the fitting, are shown in blue squares. Note that in order to better~~ ~~represent the peak assignment process, this figure contains all identified peaks, not just those passing the filtering criteria identified in Sects.~~ ~~2 and 4.1.~~ A subset of the ambient VOCUS data in (a) a KMD plot with base ^{16}O and (b) a GKA plot with base ^{16}O and X=20. Colored points are the same ions in both subpanels, Circles are colored by the number of carbon atoms in the formula. Ions that were removed and then re-added using Tofware's built-in peak addition, with no human intervention to improve the fitting, are shown in blue squares. The grey points are points that appear within the field of view in panel a are due to the compression of the KMD space a normal analysis uses. The grey points are not removed from panel b, rather they are shifted to a different GKA outside of the range of view.

5. Conclusions

We present ~~SKMD analysis~~GKA as a technique to improve visualization and peak identification in mass spectrometric measurements, particularly for atmospheric measurements. As demonstrated here, this method can aid in the identification of unknown ions and show chemical trends in a clearer manner than ~~regular~~traditional Kendrick ~~mass defect~~analysis plots. Additionally, with appropriate selection of X, certain classes of ions can be grouped, such as by the number of hydrogen atoms or the number of nitrogen atoms. Using this separation technique, ions can be more easily characterized and visualized, allowing for easier interpretations and assignments of chemical formulas. This analysis can be used as an initial tool to better understand what ions change more over the course of a measurement, identify which ions are likely misidentified, and facilitate interpretation of the measured chemical composition. We focus on gas-phase atmospheric measurements for our analysis, but ~~SKMD~~GKA can be applied to the mass spectra obtained from aerosol samples, with promise as a tool to understand polymerization products' contributions to aerosol. Additionally, these plots will be beneficial for something like looking at the chemical composition of positive matrix factorization (PMF) factors.

Code Availability. Procedure file containing the code to run the ~~SKMD~~GKA panel in the Igor Pro v9 environment (.ipf) is available at ~~https://github.com/BrowneLab/SKMDGKA Panel.git~~ https://github.com/BrowneLab/GeneralizedKendrickAnalysis_Panel.

Supplement. The supplement related to this article is available online~~.~~ at:

Competing interests. The authors declare they have no competing interests.

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Author Contributions. ECB conceptualized the work. MWA and ECB developed ~~SKMD~~GKA and the applications to atmospheric chemistry data sets. Data was collected by MC. Code was developed by MWA with guidance from ECB and HS. All authors have given approval to the final version of the manuscript. The manuscript was written by MWA with guidance from ECB.

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Supporting information for:

~~Scaled~~Generalized Kendrick ~~Mass Defect~~ Analysis for Improved Visualization of Atmospheric Mass Spectral Data

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This file includes:

6 Pages

Figures S1-~~S6~~S7

Equations S1-S2

Text S1-S3

References

S1. Mass ~~defect~~difference expansion behavior as a function of ~~R$_{IUPAC}$~~R and X

The ability for a given X to separate ions related by certain chemical groups other than ~~R$_{IUPAC}$~~R can be calculated by ~~Equation~~ Eq. (S1~~.~~):

$$\Delta SKMD(\Delta m/z, R_{IUPAC}, X) \Delta GKA(\Delta m/z, R, X) = \Delta m/z \frac{\cancel{X}}{\cancel{R_{IUPAC}}} \frac{X}{R} - \text{round}\cancel{\left(\Delta m/z \frac{\cancel{X}}{\cancel{R_{IUPAC}}}\right)}\left(\Delta m/z, \frac{X}{R}\right) \quad (S1)$$

605 where $\Delta m/z$ is the mass-to-charge difference between the two ions. In this example, we calculate the resolving power between ions spaced ~1 amu apart and related by $+^{14}N - ^{12}C - ^{1}H = 0.995249$ amu. ~~As noted in Fouquet and Sato (2017), this equation relies on anti-aliasing (i.e., wrap around correcting) to be strictly true. Figure S1 shows the separation for REKMD and SKMD analysis as a function of X. Note that outside of the range of round($\frac{2\times R_{IUPAC}}{3}$) < X ≤ round(2 × R$_{IUPAC}$) (the recommended range for REKMD analysis), the change in ΔREKMD(0.995249, ^{16}O, X) is no longer linear with X, whereas it is with~~

610 ~~ΔSKMD~~As noted in (Fouquet and Sato, 2017), this equation relies on anti-aliasing (i.e., wrap around correcting) to be strictly true. Figure S1 shows the separation for REKMD and GKA analysis as a function of X. Note that outside of the range of round$(\frac{2\times R}{3})$ < X ≤ round(2 × R) (the recommended range for REKMD analysis), the change in ΔREKMD(0.995249, ^{16}O, X) is no longer linear with X, whereas it is with ΔGKA(0.995249, ^{16}O, X) .

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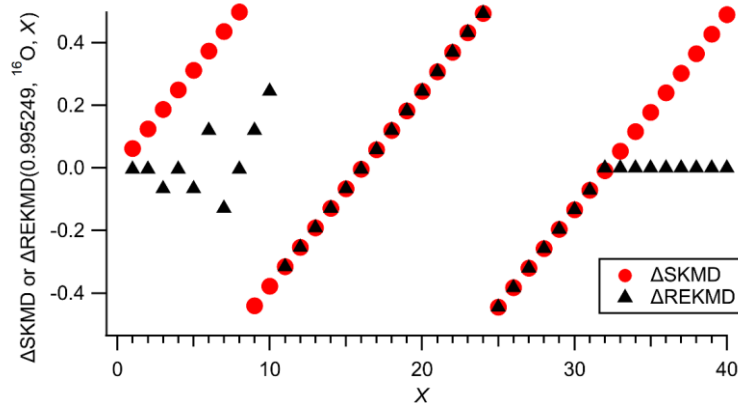
Figure S1 The difference in REKMD (Fouquet and Sato, 2017) (Eq. (3) in main text) and GKA (Eq. (4) in the main text) between ions related by the addition of one nitrogen atom and one less each of carbon and hydrogen for different X using ^{16}O as R. Note the transition from positive to negative values are an artifact from aliasing, though the absolute difference determines the separation between ions. The vertical grey lines indicate the limit of linear expansions with different X in REKMD.

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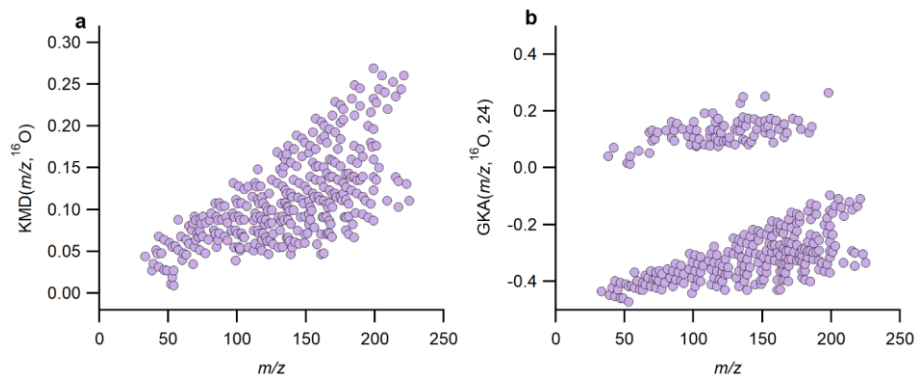
Figure S2 Reproduction of Fig. 1 in the main text with (a) a smaller y-axis range to illustrate the overlapping points do not separate well simply with zooming in and (b) ~~Figure~~Fig. 1b from the main text for comparison.

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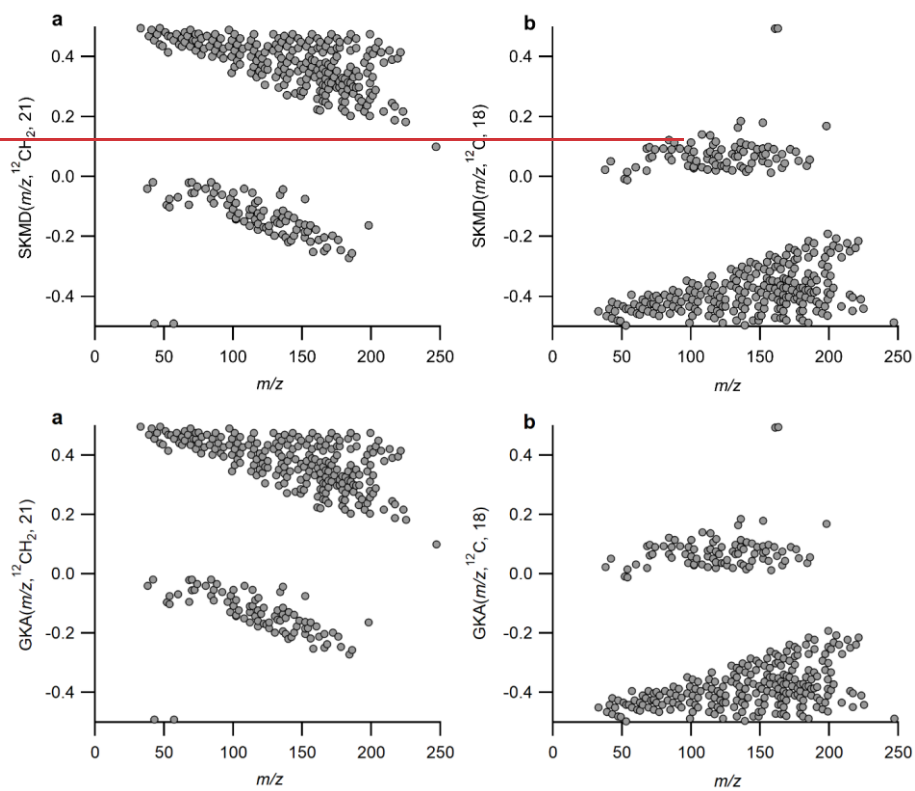
Figure S3 ~~SKMD~~GKA plots with (a) $^{12}CH_2$ and (b) ^{12}C using X that leads to X/R_{IUPAC} of ~3/2 showing that the separation into the same number of groups is consistent even with different bases.
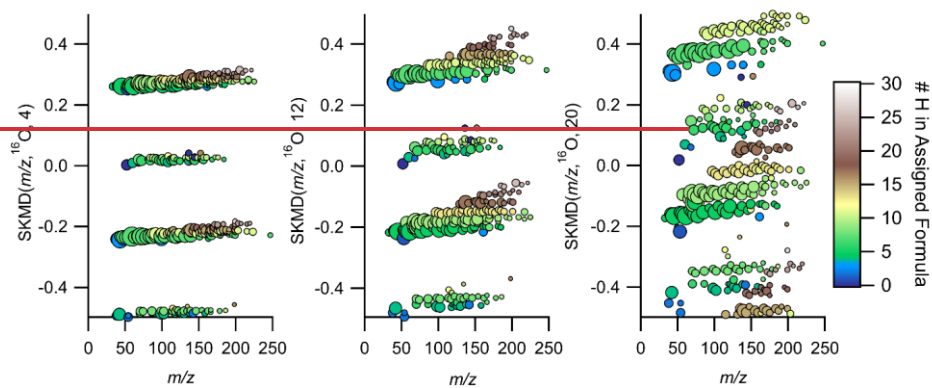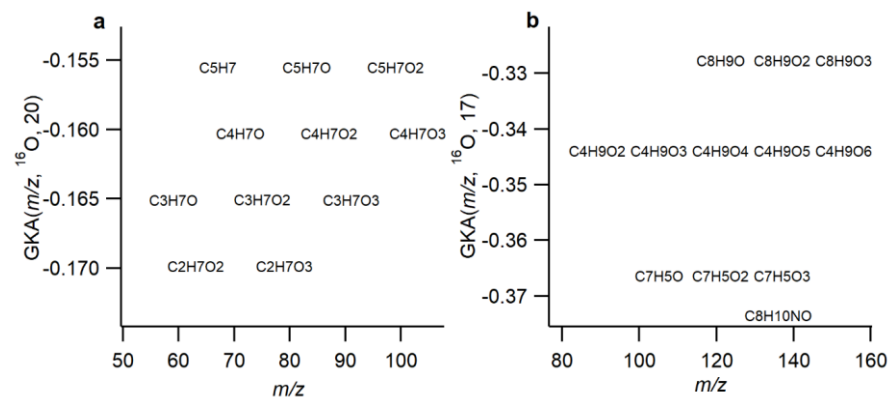
Figure S4 A reproduction of Fig. 3 in the main text, but zoomed into individual lines to show how related chemical formulas are distributed on a horizontal. Each formula has a +1 charge, not shown.
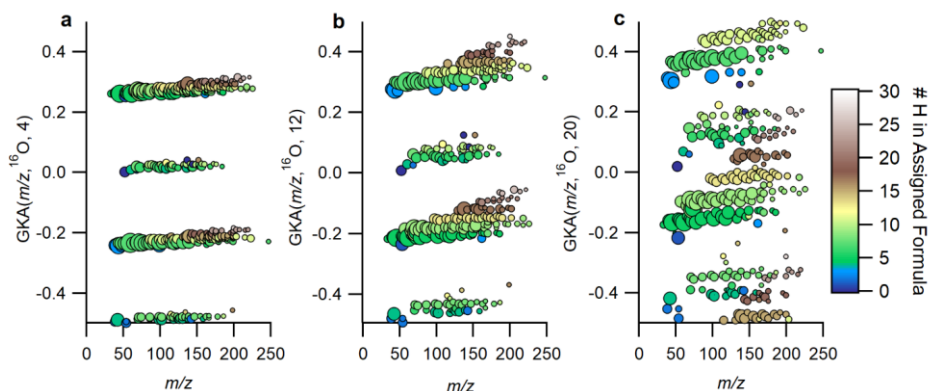
Figure S5 Similar to Fig. 4 in the main text but showing X values that lead to denominators of 4 for the approximate reduced fraction. R is ^{16}O in all subplots. Panel (c) illustrates how "aliasing" (0.5 to -0.5 transformation) will impact visualization. Points with the highest numbers of hydrogen atoms that appear in panel (b) with ~~SKMD(~~GKA(m/z, ^{16}O, 12) values approximately > 0.4 appear in panel (c) at ~~SKMD(~~GKA(m/z, ^{16}O, 20) values of approximately <-0.3. The points are colored by the number of hydrogens in the assigned formula and sized by the log of the measured intensity.

S2. Further explanation on groupings

Values of X leading to grouping by the number of hydrogen atoms are ones that minimize the absolute value of the ~~SKMD~~GKA difference (Eq. (S1~~)~~)) between ions that maintain the same number of hydrogen atoms. In measurements of atmospheric composition, such ions would be related, for instance, by the addition of an oxygen atom and the loss of a carbon atom (e.g., $C_9H_{14}OH^+$ and $C_8H_{14}O_2H^+$) and would differ by 3.9942 m/z. As shown in Fig. ~~S5~~S6, the absolute value of ~~ΔSKMD~~ΔGKA(3.9942, ^{16}O, X) is minimum for X divisible by 4. However, not all the X values fulfilling this criterion separate compounds differing by the number of hydrogen atoms equally well. In particular, $X = 16z$ for integer $z \geq 1$ will not lead to distinct regions of equal number of hydrogen atoms owing to the overlap in ~~SKMD~~GKA (or KMD in the case of $X = 16$) space between $C_xH_yO_z^+$ and $C_xH_yO_zN_w^+$ ions. To further refine appropriate X values, one should consider selections that minimize the ~~SKMD~~GKA difference in ions differing by $+^{16}O - ^{12}C$ (3.9942 amu; defined below as $\Delta m/z_1$) while maximizing the gain between ions spaced ~ 1 m/z apart ($\Delta m/z_2$). Here we use ions that differ by the addition of a nitrogen atom and loss of a carbon atom and a hydrogen atom ($\Delta m/z_2 = 0.9953$; e.g., $C_6H_{10}O_4H^+$ and $C_5H_9NO_4H^+$) Values of X satisfying these criteria will be the minima of the following quantity, termed RANK2 in ~~Nakamura et al. (2019)~~(Nakamura et al., 2019).

$$RANK2\left(\Delta m/z_1, \Delta m/z_2, R_{IUPAC}, X\right)\left(\Delta m/z_1, \Delta m/z_2, R, X\right)$$
$$= \frac{\left|\Delta SKMD\left(\Delta m/z_1, R_{IUPAC}, X\right)\right| - \left|\Delta SKMD\left(\Delta m/z_2, R_{IUPAC}, X\right)\right|}{\left|\Delta SKMD\left(\Delta m/z_1, R_{IUPAC}, X\right)\right| + \left|\Delta SKMD\left(\Delta m/z_2, R_{IUPAC}, X\right)\right|} \frac{\left|\Delta GKA\left(\Delta m/z_1, R, X\right)\right| - \left|\Delta GKA\left(\Delta m/z_2, R, X\right)\right|}{\left|\Delta GKA\left(\Delta m/z_1, R, X\right)\right| + \left|\Delta GKA\left(\Delta m/z_2, R, X\right)\right|} \quad (S2)$$

As seen in Fig. ~~S5~~S6, values of X satisfying this relationship now exclude multiples of 16. The same reasoning can be followed to show that for R_{IUPAC} of ^{12}C, X divisible by 3 but not 12 will lead to groupings associated with the number of hydrogen atoms.

665 Although in theory Eq. (S2) can be used to find X values that minimize/maximize ~~SKMD~~GKA spacing for other chemical relations as has previously been shown for analysis of polymer samples ~~(Nakamura et al., 2019)~~(Nakamura et al., 2019), such analysis is of limited success for complex mixtures. Analysis of simpler mixtures, such as those encountered in chamber experiments, may benefit from identification of other useful groupings.
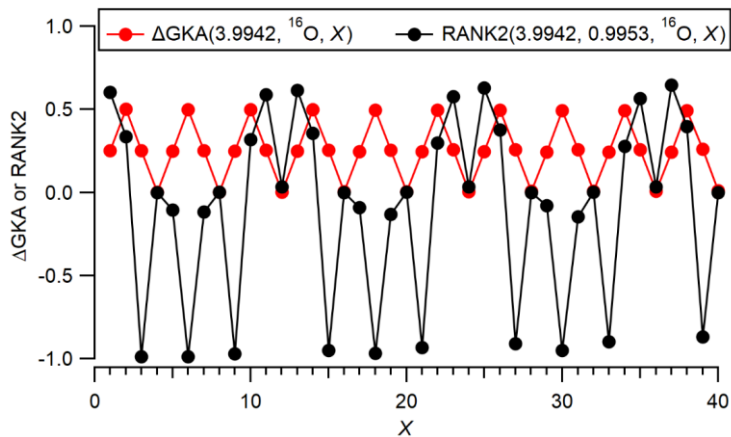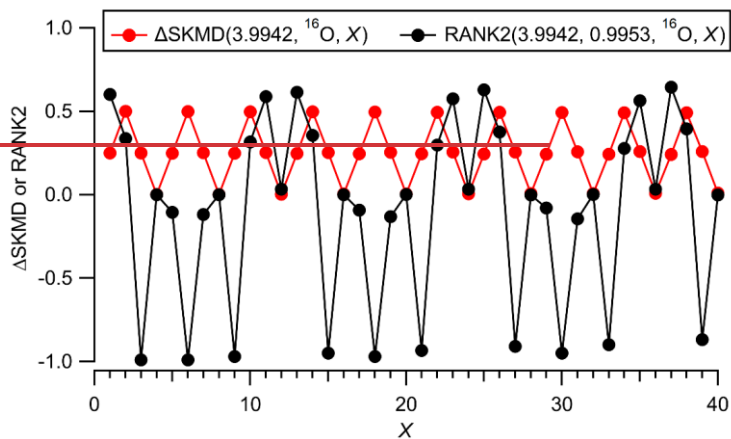
Figure ~~S5~~S6 Change in the ~~SKMD~~GKA (red) for ions differing by the addition of an oxygen atom and the loss of a carbon atom ($\Delta m/z_1$ = 3.9942) for different values of X. Results of RANK2 (S2; black) equation minimizing the ~~SKMD~~GKA gain between ions differing by the addition of an oxygen atom and the loss of a carbon atom ($\Delta m/z_1$ = 3.9942) and maximizing the gain from ions differing by the addition of a nitrogen atom and the loss of a carbon atom and a hydrogen atom ($\Delta m/z_2 = 0.9953$).

S3. Obtaining and running the ~~REKMD~~GKA panel code

The code and any future updates are available at Github at the following link: ~~https://github.com/BrowneLab/SKMD_Panel.git~~
https://github.com/BrowneLab/GeneralizedKendrickAnalysis_Panel

680   Once the ~~.~~ipf is loaded into Igor Pro and compiled, a menu option will appear called "~~SKMD~~Kendrick Analysis Panel" which can be used to generate the panel shown in Figure ~~S5~~S7.

Figure ~~S6~~S7 The main panel that is made to run the ~~SKMD~~GKA analysis within Igor Pro v9 and above.

685   **References**

Fouquet, T. and Sato, H.: Improving the Resolution of Kendrick Mass Defect Analysis for Polymer Ions with Fractional Base Units, Mass Spectrometry, 6, A0055–A0055, https://doi.org/10.5702/massspectrometry.a0055, 2017.

Nakamura, S., Cody, R. B., Sato, H., and Fouquet, T.: Graphical Ranking of Divisors to Get the Most out of a Resolution-Enhanced Kendrick Mass Defect Plot, Analytical Chemistry, 91, 2004–2012, https://doi.org/10.1021/acs.analchem.8b04371, 2019.

690