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Abstract. Regional emulation tools based on statistical relationships, such as pattern scaling, provide a computationally inexpensive way of projecting ocean dynamic sea-level change for a broad range of climate change scenarios. Such approaches usually require a careful selection of one or more predictor variables of climate change so that the statistical model is properly optimized. Even when appropriate predictors have been selected, spatiotemporal oscillations driven by internal climate variability can be a large source of statistical model error. Using pattern recognition techniques that exploit spatial covariance information can effectively reduce internal variability in simulations of ocean dynamic sea level, significantly reducing random errors in regional emulation tools. Here, we test two pattern recognition methods based on Empirical Orthogonal Functions (EOF), namely signal-to-noise maximising EOF pattern filtering and low-frequency component analysis, for their ability to reduce errors in pattern scaling of ocean dynamic sea-level change. We use the Max Planck Institute Grand Ensemble (MPI-GE) as a testbed for both methods, as it is a type of initial-condition large ensemble designed for an optimal characterization of the externally forced response. We show that the two methods tested here more efficiently reduce errors than conventional approaches such as a simple ensemble average. For instance, filtering only two realizations by characterising their common response to external forcing reduces the random error by almost 60%, a reduction that is only achieved by averaging at least 12 realizations. We further investigate the applicability of both methods to single realization modelling experiments, including four CMIP5 simulations for comparison with previous regional emulation analyses. Pattern filtering leads to a varying degree of error reduction depending on the model and scenario, ranging from more than 20% to about 70% reduction in global-mean
root-mean-squared error compared with unfiltered simulations. Our results highlight the relevance of pattern recognition
methods as a tool to reduce errors in regional emulation tools of ocean dynamic sea-level change, especially when one or only
a few realizations are available. Removing internal variability prior to tuning regional emulation tools can optimize the
performance of the statistical model, leading to substantial differences in emulated dynamic sea level compared to unfiltered
simulations.

1 Introduction

Sea levels are closely linked to the state of the climate. Understanding how increased radiative forcing in the atmosphere will
affect sea-level rise is of utmost importance given the devastating impacts to coastal systems. Global-mean sea level has been
increasing over the 20th century (Fox-Kemper et al., 2021), and its rate has been accelerating over the past decades both globally
(e.g., Dangendorf et al., 2019; Fox-Kemper, 2021; Frederikse et al., 2020; Nerem et al., 2006) and regionally (e.g., Steffelbauer
et al., 2022). This acceleration is expected to continue over the next century for all greenhouse gas (GHG) emissions scenarios
(Fox-Kemper et al., 2021) with the potential to further increase widespread impacts in coastal areas (Cooley et al., 2022).
Increased sea levels will change coastal flood risk through expanding areas under permanent inundation, increasing frequencies
of extreme coastal flooding events (Vitousek et al., 2017; Wahl et al., 2017), and modifying tides (Haigh et al., 2020) and thus
potentially increasing the frequency of tidal-induced flooding (Moftakhari et al., 2015). These processes will not only impact
coastal infrastructure and assets (Hinkel et al., 2014) but also alter coastal ecosystems and the services they provide, from
ecosystem value to natural flood risk protection (Cooley et al., 2022). Understanding how global and regional sea levels evolve
under different scenarios will help to better adapt to changing risks and mitigate their potential impacts in coastal zones
(Haasnoot et al., 2019, 2021).

Global-mean sea-level change is driven by a combination of processes. The melting of the Greenland and Antarctica ice sheets
and glaciers and ice caps, changes in land-water storage, and thermal expansion of the ocean are the processes driving global
mean sea-level rise (e.g., Gregory et al., 2019; Fox-Kemper, 2021). Analogously to global warming, sea-level rise is a global
concern but it is not spatially uniform (e.g., Slangen et al., 2017). There are several processes that determine regional sea-level
change. First, the redistribution of mass on the Earth’s surface, as a result of melting land ice and changes in land-water storage,
causes a regionally variable sea-level change due to gravitational, rotational, and deformational effects (Farrell and Clark,
1976; Mitrovica et al., 2001). Second, vertical land motion also causes relative sea-level changes. The viscoelastic relaxation
of the Earth induced by deglaciation following the last glacial maximum, defined as glacial isostatic adjustment (GIA; e.g.,
Peltier, 1999, 2001) and more local processes driving subsidence (e.g., Nicholls et al., 2021), are the main processes driving
changes in land elevation. Third, ocean circulation, and heat and freshwater fluxes over the ocean, also known as ocean
dynamics (Gregory et al., 2019), change local densities and move water mass around the ocean. Fourth, changes in sea-level
pressure over the oceans, also known as inverted barometer (IB) effects, may lead to regionally varying rates of sea-level
change (Stammer and Hüttemann, 2008). These regional drivers of sea-level change act on a wide range of spatial and temporal
scales, which makes their local assessment essential for impact studies, planning, and adaptation needs. For instance, while ocean dynamics have a typical temporal scale ranging from days to decades, vertical land movements present a much wider range (Durand et al., 2022), as the latter is governed by processes affecting land elevation on significantly different timescales from earthquakes (on the order of seconds) to GIA (on the order of millennia). This study focuses on ocean dynamic sea-level (DSL) change, which is governed by changes in ocean circulation and density. DSL features large spatiotemporal variations across the oceans, which makes it a crucial component to predict regional sea-level changes accurately, yet also one that provides significant uncertainty (Couldrey et al., 2021). Spatial and temporal variability in DSL is driven by internal climate variability (ICV), which are defined as naturally occurring climatic variations controlled by interactions between different components of the Earth system (Hasselmann, 1976; Schwarzwald and Lenssen, 2022), and by a forced response associated with increased radiative forcing in the climate system. DSL is typically projected with Global Climate Models (or related models, hereinafter GCMs), which are state-of-the-art comprehensive climate models that solve a range of environmental variables controlling the Earth’s system, including its climate. GCMs require vast computational resources, and therefore climate modelling experiments have been designed for a limited range of GHG concentration scenarios (O’Neill et al., 2017; Riahi et al., 2017; van Vuuren et al., 2011) within the climate model intercomparison (CMIP) framework (Eyring et al., 2016), so that model differences are somewhat comparable.

To reduce the computational demand, complementary approaches based on parameterizing process-based models are commonly used. This method, also known as emulation, aims to mimic the output of complex models at a reduced computational cost and has been widely used in recent literature to model different aspects of the climate system (e.g., Thomas and Lin, 2018; Edwards et al., 2021; Schwarber et al., 2019). Regional emulation follows the same principle and aims to estimate a spatiotemporal varying variable by mimicking GCMs behavior. One of the most commonly used emulation approaches for projecting changes in a regional variable is pattern scaling (Mitchell, 2003; Perrette et al., 2013; Santer et al., 1990), which consists of relating a local, grid-point variable (predictand) to one or a few global-mean change variables (predictors) via regression. Based on that statistical relationship, a change in a regional variable can be emulated by projecting the global-mean variables via simpler climate models (Goodwin et al., 2018; Meinshausen et al., 2011; Millar et al., 2017; Smith et al., 2018)

Here, we build on the approach proposed by Bilbao et al. (2015), who applied a linear pattern scaling approach to assess the ensemble mean DSL computed from five CMIP5 models and their simulations of several variables describing global changes, including Global Surface Air Temperature (GSAT), Global-Mean Thermosteric Sea-Level Rise (GMTSLR), and ocean-volume mean temperature. While GSAT turned out to be the best predictor of 21st-century DSL change in a high emissions scenario (Representative Concentration Pathway (RCP) 8.5), ocean-volume mean temperature and GMTSLR outperformed the rest of variables considered in lower emissions scenarios (RCP 2.6 and 4.5). As the surface ocean layer responds quicker to air temperature changes than the deeper ocean layer, they speculated that surface warming had a more important role relative to deep warming in a high emissions scenario. Based on Bilbao et al. (2015)’s findings, Yuan and Kopp (2021) used the same set of CMIP5 models to develop a bivariate pattern scaling approach, accounting for the surface and deep ocean layers.
separately. Their goal was to capture the different delayed response of those two layers by using GSAT and global-mean deep ocean temperature changes as predictors. By employing a bivariate pattern scaling approach, Yuan and Kopp (2021) reported a reduction of the predicted DSL error for the period 2271-2290 of 36%, 24%, and 34% for RCP 2.6, 4.5, and 8.5, respectively, compared to a univariate approach based on only GSAT.

The aforementioned studies highlight the importance of selecting appropriate predictors to attain an optimized regional emulator of DSL, and how accounting for different processes driving DSL change (in different layers of the ocean) can help further improve emulator performance. While designing a regional emulator based on performance metrics may provide insights into the global processes driving DSL changes, this process can be obscured by other drivers of emulator error. In particular, random errors contained in the regression forming the pattern scaling approach, are assumed to be mostly caused by ICV (Bilbao et al., 2015) and may be a source of large uncertainty. Thus, if random errors are not minimized prior to emulator training with GCM simulations, their presence could impair a proper selection of global predictors, such that it would be uncertain whether an increase in model performance is due to an appropriate selection of predictors or an artifact of ICV causing a biased selection. In previous studies, this effect has been minimized by computing 30-year means, assuming this cancels out ICV. This step, however, entails a substantial loss of data and does not guarantee ICV is optimally subtracted, and residual ICV, for instance caused by long-memory processes (e.g., Becker et al., 2014; Dangendorf et al., 2014), can remain. We therefore propose to take a different approach to separate ICV from the response driven by external radiative forcing in the Earth, by employing state-of-the-art modelling experiments specifically designed to do so. These are known as Single-Model Initial Condition Large Ensembles (SMILES) and consist of a set of simulations with the same forcing but with the variability evolving in a different phase (Deser et al., 2020). These realizations can be combined through different methods (e.g., Frankcombe et al., 2015) so that ICV cancels out. However, conventional approaches such as computing the ensemble mean or linear trends are not the most efficient tools to do so and tend to lead to the loss of much of the information gained from running large ensembles (Wills et al., 2020). Other methods based on pattern recognition via Empirical Orthogonal Functions (EOFs) exploit spatial covariance information to remove ICV more efficiently (Wills et al., 2020) and have demonstrated to provide a superior agreement between observations and simulations than an ensemble average (Marcos and Amores, 2014). These types of efficient methods for removing ICV hold potential to benefit emulation experiments of DSL for which the number of simulations is limited.

The aim of this study is to characterise the importance of ICV as a driver of random errors in statistically based (pattern-scaled) projections of DSL change. To achieve this aim, we will compare different pattern recognition techniques, including Signal-to-Noise Maximising (S/N M) EOF pattern filtering (Wills et al., 2020) and Low Frequency Component Analysis (LFCA, Wills et al., 2018, 2020). We will use these techniques to truncate ICV in DSL simulations from the Max Planck Institute Grand Ensemble (MPI-GE) SMILE (Maher et al., 2019), and explore their applicability to single realization modelling experiments, including a set of CMIP5 simulations used in previous pattern scaling studies. In this paper, we particularly aim to attain the following objectives:
1) Use a large ensemble (MPI-GE) to determine the forced pattern and examine to which extent pattern recognition techniques isolate the forced response in DSL change more efficiently than conventional methods (Section 4.1).

2) Determine the error reduction in pattern scaling of DSL provided by pattern recognition methods relative to more conventional methods (Section 4.2).

3) Test whether filtering improves pattern scaling in single-realization modelling experiments of DSL (Section 4.3).

2 Climate model data and pre-processing

Separating ICV from the forced response is key for detection and attribution studies in climate change (Labe and Barnes, 2021) and to understand its effects on the climate system (Deser et al., 2020; Mankin et al., 2020). However, the combination of distinct GCMs to analyse ICV should be performed with caution, as this may conflate ICV with model biases (Maher et al., 2021b). In recent literature, this has motivated the development and use of SMILES, which branch each realization at a different model stage in the pre-industrial control simulation (Danabasoglu et al., 2020; Deser et al., 2020; Fasullo et al., 2020; Kay et al., 2015; Maher et al., 2019, 2021a; Mankin et al., 2020). This results in simulations with the same forced response but with variability evolving in a different phase, enabling a separation of the variability from the forced response.

There are two main procedures for creating SMILEs: 1) inducing small round-off level differences in their atmospheric initial conditions (micro-initialization); 2) branching simulations at different times in the control simulation (macro-initialization). Both micro and macro initialization are useful to characterize unpredictable ICV within a model. Macro-initialization, however, provides larger differences in the initial states in both the atmosphere and ocean. Macro-initialized ensembles are therefore better suited than ‘micro’ ensembles to sample uncertainty in an initialized framework (Hawkins et al., 2016; Stainforth et al., 2007), facilitating an assessment of ICV in different aspects of the climate system.

Since we are assessing ocean processes, a macro-initialized ensemble is most suitable for the purpose of this study. From the available macro-initialized SMILES (Deser et al., 2020; Maher et al., 2021a), we decided to use the Max-Planck Institute Grand Ensemble (MPI-GE; Maher et al., 2019) because it contains the largest number of ensemble members available (100) in a SMILE for different RCP scenarios (RCP 2.6, 4.5, and 8.5) up to 2100. MPI-GE simulations assume a stationary and volcano free 1850 climate, and are macro-initialized on the first of January in different years of the control simulation (Table 1 in Maher et al., 2019). The branching separation between realizations varies along the pre-industrial control, ranging from 6 to 24 years and with a median of 16 years. MPI-GE has a relatively lower resolution than other GCMs, representing the atmosphere at an approximate horizontal resolution of 200 km (1.875 degrees) with 47 layers (up to 0.01 hPa ~ 80 km in height). The horizontal resolution of the ocean (including biogeochemistry) varies from 12 to 150 km at 40 layers, whereas the land biosphere has the same horizontal resolution as the atmosphere. Despite its relatively low resolution, Suarez-Gutierrez et al. (2021) show that MPI-GE samples observed ocean variability well in all regions except for the Southern Ocean.

Additionally, we use four CMIP5 models that were used in previous studies of DSL pattern scaling (Bilbao et al., 2015; Yuan and Kopp, 2021), including GISS-E2-R, HadGEM2-ES, IPSL-CM5A-LR, and MPI-ESM-LR. These four GCMs were selected
in the afore-mentioned studies because they were used to calibrate the parameters of the simple climate model used by Geoffroy et al. (2013a, b), which facilitated the design of their emulation tool. Also, these models provide multi-century data (up to 2300) in three emissions scenarios, granting an assessment of the suitability of pattern scaling for long-term projections. We use them here for comparison purposes.

The focus of this study is on DSL change, which is defined at each location and time as the change in local sea-surface height relative to the geoid, with the IB correction applied (Gregory et al., 2019). DSL varies locally due to ocean circulation and horizontal gradients, and its global mean is zero at every time step (Eq. 15 in Gregory et al. 2019), i.e., GMTSLR is excluded. In CMIP models, DSL is diagnosed as ‘zos’ (Griffies et al., 2016) and often expressed as differences in relation to a control state. DSL simulations from GCMs, however, do not include the effect of sea-level pressure on sea level (IB effect) and such effect is not subject of study in our analysis, hence it is not considered here.

Since we are interested in assessing the forced response in DSL for historical and future GHG emissions we will use zos from a range of GCMs for historical and future radiative forcing scenarios, including RCP 2.6, 4.5, and 8.5 (Meinshausen et al., 2011). Once the forced DSL has been characterized, we will proceed to pattern scale each model and scenario using a variable from their respective GCM simulation representing a global change in the state of the climate system. Among other potential global predictors, we chose GMTSLR (diagnosed as ‘zostoga’ in CMIP models), defined as the part of global-mean sea-level rise due to thermal expansion. We deemed GMTSLR as a suitable predictor candidate because it is closely related to DSL and has been successfully used in previous pattern scaling analysis of DSL (e.g., Bilbao et al., 2015; Thomas and Lin, 2018). We refrain from testing other global variables as predictors to ease comparing models and scenarios, and determining to which extent pattern filtering reduces statistical error via reducing ICV.

In this study, we are particularly interested in removing interannual variability, thus we compute annual mean zostoga and zos time series from the raw monthly mean GCM data. In addition, since GCMs are run for a few centuries and the deep ocean usually takes millennia to reach an equilibrium, both zos and zostoga are subject to model drift (Sen Gupta et al., 2013). Model drift in the historical and scenario simulations can be corrected for by subtracting the smoothed long-term change of the pre-industrial control run. To avoid contaminating the drift correction with ICV, ideally the full length of the control run is used to determine the drift (Sen Gupta et al., 2013). Therefore, to dedrift the historical and scenario simulations of zostoga and zos (the latter on a grid cell by grid cell basis) we first fit a quadratic polynomial to the full pre-industrial control simulations of these variables. Then, we evaluate and subtract the polynomial fit over the time period in which the pre-industrial control run and historical and scenario runs overlap, as identified by the branch times of the different simulation realizations and their length, from the historical and scenario runs. Similar to what was found by Hermans et al., (2020) and Hobbs et al. (2016), fitting a linear or quadratic polynomial to the pre-industrial control simulations yields little difference for the drift-correction of the zostoga simulations of GISS-E2-R, HadGEM2-ES, IPSL-CM5A-LR, and MPI-ESM-LR. However, in the pre-industrial simulation of MPI-GE, the increase of zostoga behaves non-linearly and levels off toward the branching time of ensemble member 40, so we only dedrift ensemble members 1 to 39. For zos, some differences are found between linear and quadratic drift correction depending on the model, variant, and location. We assume linear dedrifting is suitable for our purpose, since
we verified that the dedrifting does not substantially affect the pattern scaling performance and it is tedious to assess the best fit on a grid-point basis. After dedrifting, the area-weighted mean of $zos$ is removed at each timestep, and the resulting fields are bilinearly regridded to a common 1 by 1 degree grid.

3 Methods

3.1 Pattern filtering techniques

Both S/N M EOF pattern filtering and LFCA aim to identify those spatial patterns in the data than explain most of the forced climate change signal, by decomposing the data into EOFs. Effectively, this allows to distinguish the forced signal from noise caused by ICV. The difference between S/N M EOF and LFCA lies in their definition of what type of variance (or patterns of variance) in the data belongs to the signal and the noise. Here, only the basics of both methods will be explained. Interested readers can find an extensive methodological explanation about S/N ME EOF pattern filtering applied to an ensemble and LFCA in Wills et al. (2020) and Wills et al (2018), respectively.

S/N M EOF pattern filtering diagnoses the variance that is forced by either assessing a simulation of forced climate change relative to a preindustrial control simulations (DelSole et al., 2011; Marcos and Amores, 2014), or by using an ensemble mean of realizations with the same forcing (Wills et al., 2020). The former is advantageous in single realization GCM experiments, as it only requires one forced realization and one preindustrial control run. However, this could neglect the forced response when external forcing only affects the phase of an ICV mode (Wills et al., 2020). The latter allows to effectively reduce ICV while avoiding phase neglection issues but requires the availability of two or more ensemble members. Since one of our objectives is to determine how efficient pattern filtering methods are compared to an ensemble mean of realizations to reduce ICV in DSL, here we focus on the latter approach.

Essentially, S/N M EOF pattern filtering exploits a SMILE to find patterns where different ensemble members agree on the temporal evolution (forced response), whereas those patterns in which members disagree are considered ICV. S/N M EOF pattern filtering finds spatial patterns (r.h.s. of Fig. 3, for example) associated with the time series $t_k$ of each pattern $k$ (l.h.s. of Fig. 3, for example) that maximize the ratio of (ensemble mean) signal to total variance $s_k$:

$$
\begin{align*}
    s_k &= \frac{\langle t_k \rangle^T \langle t_k \rangle}{\langle t_k^T t_k \rangle} \\
    &= \frac{\langle t_k \rangle^T \langle t_k \rangle}{\langle t_k^T t_k \rangle}, \\
    &\quad \text{(1)}
\end{align*}
$$

where angle brackets represent an ensemble average. The leading S/N patterns (i.e., anomaly patterns with high signal fraction $s_k$) can be combined to isolate the forced response from the ICV (Fig. 1).
Figure 1. Main steps involved in isolating the forced response, including variability decomposition (EOF analysis), finding leading anomaly patterns, and combining leading patterns above a significant statistical level.

To apply S/N M EOF pattern filtering, we must determine two parameters: 1) the number of EOFs retained (N), and 2) the number of S/N patterns used to compose the forced response (M). Following the approach by Wills et al. (2020), we choose N to retain between 75% and 95% of the total variance. We use a block bootstrapping approach to determine M, which consists of taking block samples with replacement from the ensemble members to construct a randomized ensemble where the forced response timing of their realizations should not agree with one another. Here, we choose 30-yr blocks to distinguish forced patterns from ICV, so that most of the ICV in DSL is excluded. S/N EOF pattern filtering is then applied to randomized ensembles and the $s_k$ value of the pattern with the highest S/N ratio is taken as a threshold. This allows us to obtain a distribution of $s_k$ values (one for each randomized ensemble produced) from which a desired confidence level can be estimated. S/N M EOF patterns with a higher $s_k$ value than the threshold can be considered as part of the forced response with the chosen confidence level (Fig. 1). As there is no sufficient statistical evidence to include patterns with a lower $s_k$ value in the forced response, those are considered noise (ICV).
In contrast to S/N M EOF, LFCA identifies the signal that makes it through a low-pass filter. The advantage of LFCA is that it can analyse the forced response in a single ensemble member without relying on the preindustrial control run (Schneider and Held, 2001; Wills et al., 2018). LFCA is similar to S/NP M EOF pattern filtering but, instead of using an ensemble mean, it detects anomaly patterns associated with time series $t_k$ (Eq. 2) that maximize the ratio of low-frequency signal to total variance. The failure to detect some forced variations such as those driven by volcanic activity in surface air temperature and some changes in the seasonal cycle is the main disadvantage of this method being documented in the literature (Wills et al., 2020).

$$r_k = \frac{\overline{\varepsilon_k}^T \overline{\varepsilon_k}}{\overline{t_k}^T \overline{t_k}},$$  \hspace{1cm} (2)

Variations that make it through a low-pass filter (denoted by a tilde), constitute the low-frequency signal (forced response). Here, we apply a linear Lanczos filter (Duchon, 1979) with a 30-yr lowpass filter, so only variability at larger timescales is included. Following the same process as in S/N M EOF, a forced response can be constructed by linearly combining leading anomaly patterns, as illustrated in Fig. 1.

### 3.2 Pattern scaling

Pattern scaling is usually based on grid-point regression against a global variable, and it assumes that a regional change in DSL can be explained by global changes of the predictor(s) of choice. Previous studies have shown such relationships can be a reasonable approximation for different variables of the climate system. For instance, local surface air temperature change (Collins et al., 2013; Hawkins and Sutton, 2012) and local precipitation (Osborn et al., 2016) have successfully been linked to GSAT change. Regional emulation based on pattern scaling assumes that patterns of local response to external forcing remains constant (Tebaldi and Arblaster, 2014), an assumption that can lead to errors (Wells et al., 2022). However, its simplicity and transferability to many regional variables have made it a popular approach for exploring regional changes in climate change studies (Bilbao et al., 2015; Fox-Kemper, 2021; Herger et al., 2015; Mitchell, 2003; Osborn et al., 2016; Perrette et al., 2013; Tebaldi and Arblaster, 2014; Thomas and Lin, 2018; Wells et al., 2022; Wu et al., 2021; Yuan and Kopp, 2021).

Once we have identified the forced DSL within an ensemble of realizations or a single simulation (as outlined in Section 3.1), we will use this forced response as a predictand in our statistical model for projecting regional DSL. There are different forms of pattern scaling, mostly differing in the number of predictors included in the analysis (e.g., univariate, Bilbao et al., 2015; bivariate, Yuan & Kopp, 2021). Here, for simplicity and to ease comparison between raw (de-drifted) DSL and its pattern-filtered equivalent, we only test pattern scaling based on GMTSLR (or zostoga) as a predictor. The univariate case of pattern scaling for relating DSL with GMTSLR can be described by the following linear regression relationship:
\[ \zeta(t, x, y) = \alpha(x, y) \bar{\eta}(t) + b(x, y) + \varepsilon(t, x, y) \]  

Where \( \zeta \) and \( \bar{\eta} \) denote DSL and GMTSLR, respectively. Longitude and latitude are represented by \( x \) and \( y \), whereas \( t \) denotes time. \( \alpha \) is a spatial pattern that captures the scaling relationship between DSL and GMTSLR, and \( b \) is an intercept term, both being only a function of location. \( \varepsilon \) is a residual term regarded as random noise and often assumed to be driven by internally generated variability (Bilbao et al., 2015).

### 4 Results & Discussion

#### 4.1 Forced response in MPI-GE and efficiency of pattern filtering.

In this section, we focus on determining the forced response in DSL within a SMILE (MPI-GE) using S/N M EOF pattern filtering and show the efficiency of the latter to remove ICV compared to the more conventional approach of ensemble averaging. To construct the forced response based on S/N patterns, we follow the block-bootstrapping approach described in Section 3.1 we define blocks in terms of thirty years, so most ICV in DSL is excluded. 30-yr block samples are taken from the 100 historical realizations of the MPI-GE to construct 20 randomized ensembles. A value of 20 is chosen because increasing it further does not lead to substantial changes in the estimation of the 95\textsuperscript{th} percentile of \( S_k \). The estimated ratio \( S_k \) (Eq. 1) for a 95 \% confidence level is 0.08, leading to a total of eight patterns that can be considered as part of the forced response at such a confidence level (Figure 1).
**Figure 2**: Signal fraction of the leading S/N M EOF patterns along with their respective explained forced response variance (%). The significance level (95%) computed using 30-year block-bootstrapping is represented as a dashed line. Patterns are sorted based on the magnitude of their signal fraction, as illustrated in Figure 1.

Even though patterns constructed based on EOFs are created from mathematical constraints, known physical processes can be identified in some patterns. For instance, the S/N M EOF pattern with the highest $S_k$ value pattern 1, (Fig. 3) explains 62% of the forced response variance (Fig. 2) and is similar to the main forced pattern of DSL change field driven by increased radiative forcing due to increased GHG emissions. There is a zonal dipole in the Southern Ocean, with decreased and increased sea level relative to the mean below and above 50°S, respectively (e.g., Frankcombe et al., 2013). Another dipole structure is found in the North Atlantic with a decreased DSL in the north compared to an increased DSL in the southern section, a feature which appears to disagree with some models (e.g., Bouttes et al., 2014). Nonetheless, the North Atlantic Ocean is an area of large model spread in both CMIP5 and CMIP6 models (Lyu et al., 2020), which suggests the representation of such zonal dipole may be model dependent. Other relevant features include a large DSL rise in the Beaufort Sea and an increased DSL in the North-West Pacific Ocean. Most of these features agree with those documented among CMIP6 and earlier models (Church et al., 2013; Ferrero et al., 2021; Landerer et al., 2007; Lowe and Gregory, 2006; Lyu et al., 2020; Slangen et al., 2014). Patterns are similar between RCP scenarios, mainly differing on their intensity.

The three following resulting patterns (patterns 2, 3 and 4, Fig. S1, S2 and S3) represent between 4-1% (Fig. 2) of the forced response variance and, although with a much lower importance than pattern 1, when combined together represent non-linear processes that start to have an effect in DSL after 2050. Patterns 5, 6, 7 and 8 (Fig. S4, S5, S6, and S7) explain between 1-0.7% of the forced response variance (Fig. 2) and show a rather stable temporal evolution except for perturbations that coincide with historical volcanic eruptions from Krakatoa, Agung, El Chinchón, and Pinatubo. Volcano-induced perturbations were also observed in the analysis by Wills et al. (2020), as aerosol changes in the atmosphere can affect global and regional temperatures, subsequently affecting DSL. Patterns number 9 and beyond explain a variance of less than 0.6% and since their $S_k$ value is not statistically significant at the 95% level they could be caused by chance.
Figure 3: Time evolution of DSL standard deviation (a, c, and e) and associated S/N M EOF pattern number 1 for RCP 2.6, 4.5, and 8.5 (b, d, and f respectively). Light coloured lines in a, c, and d represent standard deviation anomalies from ensemble members, whereas dark coloured lines depict ensemble mean evolution of the pattern. In the historical + RCP scenarios DSL is calculated relative to the mean of 1993–2012.

We first compare the efficiency of pattern filtering techniques to that of conventional methods, in particular an ensemble mean, to isolate the forced response in DSL. We follow the approach used by Wills et al. (2020) based on the number of ensemble members needed to constrain a certain level of variance of the forced response using the coefficient of determination r², which indicates the proportion of variance shared between two datasets. As we need two datasets for such a comparison, the 100-member MPI-GE ensemble is divided into two sub-ensembles: one is used for testing (estimate ensemble) and the other is left for reference (reference ensemble). This leaves us with two 50-member sub-ensembles, where all 50 members in the reference sub-ensemble are used to estimate the forced response by either using ensemble averaging or S/N M EOF pattern filtering and this reference sub-ensemble is considered as ground truth. The other (estimate) 50-member ensemble is also used to estimate the forced response, but instead of using all sub-ensemble members we estimate the forced response in an iterative process by increasing the number of members included in the analysis from 2 to 50. As an illustration of the procedure, we start with only 2 members which are used to characterize the forced response in the estimate sub-ensemble and compare the result with the forced response from the 50-member reference sub-ensemble. This comparison is performed via the coefficient of determination between two estimated forced responses on a grid-point basis, identifying where the 80% level is exceeded.
Grid points where the threshold is not reached are used for subsequent analysis where an additional member (3 in total) is included in the estimate sub-ensemble, repeating the same process until the latter reaches 50 members. This procedure enables an evaluation of the number of ensemble members needed in the estimate sub-ensemble to characterize the forced response based on explained variance (i.e., r2) in the reference sub-ensemble. To consider sampling uncertainty, this process is repeated ten times for random choices of realizations, taking the median value of all iterations.

When simple averaging is used, we find that 50 members are not sufficient to constrain at least 80% of the forced response variance of the reference ensemble over most of the ocean surface (Fig. 4a). In contrast, S/N M EOF pattern filtering characterizes the forced response more efficiently than simply averaging, as it requires a much smaller number of realizations to remove ICV (Fig. 4b). While the grid-point median value of the number of ensemble members required is 50 or more when using simple averaging, the median estimate for the filtering method is reduced to eight. Large areas of the ocean benefit from filtering and there are significant reductions, especially the Indian Ocean, South and Northwest Atlantic Ocean, as well as large areas in the Pacific Ocean (Fig. 4b). Other areas, however, remain over the 50-member threshold to explain forced response variance after filtering. Those areas are mostly found where strong western boundary currents exist (Imawaki et al., 2013), as well as in areas influenced by the Antarctic Circumpolar Current (Rintoul et al., 2001). In those locations, variability is higher, and a larger number of realizations is needed to characterize it. Yet, there clearly is an advantage in using S/N M EOF over simple averaging methods, as less realizations are required to explain a significant part of the forced response in DSL, which means that the forced response can also be determined in models with smaller ensembles.

**Figure 4.** The number of ensemble members (realizations) needed to form an MPI-GE sub-ensemble that shares at least 80% of the variance of the forced response with a reference 50-member MPI-GE sub-ensemble using an ensemble average (a) and
using S/N M EOF pattern filtering (b) for RCP 2.6. The reference dataset is an average (a) or S/M EOF-filtered sub-ensemble (b) of 50 members which does not share realizations with the sub-ensemble used for estimation. Values represent the median of ten random choices of realizations sampling for both estimate and reference sub-ensembles. Note that bright yellow indicates more than 50 ensemble members required.

4.2 Improved Pattern Scaling Using SMILES

In this section, we demonstrate how S/N M EOF pattern filtering can increase the capabilities of statistical approaches for explaining DSL based in GMTSLR by reducing ICV within SMILES. For comparison, we first show pattern scaling performance when using single realizations and how conventional methods (ensemble mean) reduces RMSE when using a couple of realizations instead. Second, we examine S/N M EOF as a method for reducing RMSE more efficiently. We compare regional RSME from both ensemble mean and pattern filtering on only two realizations to allow an assessment of the areas that benefit the most from filtering when a few simulations are available. Lastly, we contrast how both ensemble mean and S/N M EOF pattern filtering reduce global mean RMSE as the number of realizations included in the analysis is increased.

As pattern scaling is performed on a grid-point basis, regression performances can be location dependent (Fig. 4a). Despite such regional variations, we found no substantial differences between GHG scenarios for both the regional and global mean RMSE estimates when pattern scaling DSL simulations extending up to 2100. Thus, results shown and discussed here are pertinent to the historical+RCP2.6 scenario for illustrative purposes, unless otherwise stated. When applying pattern scaling on a single realization of DSL from MPI-GE, the area-weighted, ensemble average RMSE is 3.78 cm, a value which is similar to previous estimates from studies performed on some of the CMIP5 models (Bilbao et al., 2015; Yuan and Kopp, 2021). However, pattern scaling performance shows a large spatial variability, ranging from 1.13 to 14.95 cm regionally (Fig. 5a). High RMSE values (i.e., lower regression performance) can be found in places subject to non-linear mesoscale processes driven by strong currents, coinciding with the places where the S/N M EOF technique requires many realizations to explain at least 80% of the forced response variance (Fig. 4b). These are the Antarctic Circumpolar Current (Southern Ocean) or western boundary currents, including the Gulf Stream (West North Atlantic), and Agulhas Current (South Africa), the Kuroshio Current (West North Pacific), and at the Brazil-Malvinas Confluence (West South Atlantic). Low RMSE values are found in the more stable eastern boundary currents, such as the Humboldt (Peru) Current, and in equatorial locations where DSL is relatively less influenced by large modes of climate variability (e.g., Equatorial Atlantic and Indian Ocean).

Despite its inefficiency, using an ensemble average cancels out some of the ICV that varies in a different phase between realizations. When using a 2-member ensemble mean, RMSE reduction is observed both globally and regionally: The area-weighted average RMSE estimate is reduced from 3.78 to 2.77 cm (27% reduction) when two ensembles are used, with regional values ranging from 0.87 to 11.00 cm (Fig. 5b). This translates to increased statistical model capabilities within the entire model domain. While grid-point RMSE reduction ranges from 10 to 30%, the majority of the ocean benefits from a decrease of more than 25% due to the removal of some of the ICV (Fig. 5c). Locations experiencing a lower improvement in regression performance include those that already performed relatively well prior averaging and those with a high ICV.
Figure 5. Regional pattern scaling performance based on regression RMSE when one realization (a) and a two-member ensemble average (b) are used in the univariate regression. Sampling uncertainty is accounted for in (a) by averaging RMSE from pattern scaling performed individually to the 100 realizations, whereas in (b) random pairs (without replacement) are taken for the two-member ensemble average. The difference in regression performance between (a) and (b) is shown in (c) in terms of percentage. Results are shown for RCP 2.6 as an example.

To compare how S/N M EOF pattern filtering improves pattern scaling as opposed to averaging, we take two ensemble members from the MPI-GE historical+RCP2.6 experiment and proceed to remove their ICV by pattern filtering. The 2-member pattern-filtered DSL (Fig. 6a) shows an improved RMSE with similar regional structures compared to its averaged counterpart (Fig. 5b), featuring higher values in western boundary currents and Southern Ocean. Nonetheless, the overall improvement is apparent in all areas: the global estimated RMSE from the regression decreases almost 60% from an average value of 2.77 to 1.12 cm (Fig. 6c and d). Regionally, RMSE ranges from 0.39 to 6.05 cm when filtering is applied on two ensemble members (Fig. 6a and c). The differences between averaged and filtered approaches are substantial and location dependent, with filtering yielding a decrease in RMSE ranging from 12% to about 80% (Fig. 6b). The tropical Indian and
Eastern Pacific Ocean are among the locations benefiting the most from the largest performance improvement, which highlights the skill of pattern filtering to remove variability associated with large climate modes (e.g., ENSO has a large influence on sea level in the Eastern Pacific Ocean). Similar to previous findings when using averaging (Fig. 4c), pattern filtering offers a reduced improvement in areas where regression already performed relatively well or where the presence of meso-scale processes is significant. Regardless of improvement magnitude, pattern filtering provides an overall increase in regression performance that is observable in the entire ocean domain. While averaging also offers an enhancement of pattern scaling skill, filtered 2-member pairs produce a distribution of RMSE that is significantly superior (Fig. 6c).

We further investigate how pattern filtering enhances regression compared to averaging by increasing the number of members included in the analysis (Fig. 6d). Increasing the number of realizations grants ensemble averaging a considerable decrease in RSME. Yet, performance improvement asymptotically reaches a plateau around 20 members after which further reductions in RMSE are modest. Regression based on pattern-filtered DSL also shows an improvement as the number of realizations increases. Such improvement is very limited compared to the one undergone by averaging, although filtering always provides a superior performance regardless of the number of members incorporated in the analysis. Importantly, area-weighted RMSE values differ significantly between the considered approaches when only a small number of realizations are available and become more similar for a larger number. This highlights the role of pattern filtering techniques when only a few ensemble members are available. Based on the analysis performed on the DSL simulations from the MPI-GE, filtering two members provides a regression performance that would only be achieved by averaging at least 12 members.
Figure 6. Regional pattern scaling performance based on regression RMSE when two ensemble members are used to estimate the forced response via S/N M EOF pattern filtering (a). Panel (b): the difference in regression performance between the 2-member average pattern scaling (Fig. 5b) and the S/N M EOF-filtered equivalent (a). Panel (c): Violin plots of RMSE distributions from the 1-member, 2-member average, and 2-member S/N M EOF-filtered approaches. Panel (d): The area weighted average RMSE obtained in the regression as a function of the number ensemble members included when using an ensemble mean (yellow) and filtering (blue). The difference in performances in terms of percentage is shown in green. Analysis for the RCP 2.6 scenario (we observed no discernible differences between scenarios).

4.3 Improved Pattern Scaling Using Single Realizations

Most models in CMIP prior to CMIP6 (and some in CMIP6) provided only one realization of historical and scenario simulations. Therefore, we now test whether pattern filtering could improve regional emulation of single-realization models. To do so, we apply LFCA which uses a similar approach to S/N M EOF (as explained in Section 3.1). In this section, we first examine how LFCA improves the regression RMSE by truncating ICV in a single simulation from the MPI-GE. We then apply LFCA to a range of CMIP5 models that were used in previous patterns scaling analyses of DSL, focusing on the differences between models and RCP scenarios in longer simulations.
LFCA filtering uses the same linear algebra machinery as S/N M EOF, providing a similar regional improvement in pattern scaling (compare Fig. 6a and 6a). Slightly higher RMSE values are observed in LFCA-based regression, for instance, in the equatorial Pacific. This is expected because only one simulation is used, compared to two simulations in S/N M EOF filtering, which enables the latter to identify a larger proportion of ICV. LFCA provides a substantial reduction in RMSE, as compared to using a single simulation in pattern scaling (Fig. 7b-c). Regionally, it shows a similar qualitative pattern of improvement as the other methods shown here (Fig. 7b vs 4c and 5b; averaging and S/N M EOF filtering, respectively). Quantitatively, however, LFCA provides a larger RMSE reduction on a single realization than S/N M EOF performed on two. LFCA provides a reduction of the area weighted average RMSE of 68% for all radiative forcing scenarios (Fig. 7c), while S/N M EOF yields 67% when using two realizations relative to unfiltered 1-member pattern scaling. While both estimates are quite similar, it is worth noting that S/N M EOF requires two ensemble members to provide such reduction, while LFCA leads to a similar performance just using one simulation. Similar to S/N M EOF pattern filtering, no substantial differences are found in pattern scaling RMSE between RCP scenarios up to 2100 (Fig., 6c). This implies that ICV is analogous for different RCP scenarios which, since a reduction in RMSE is due to the removal of ICV, leads to a similar improvement in performance for all RCPs both globally (Fig. 7c) and regionally (not shown).
Figure 7. Regional pattern scaling performance based on regression RMSE when one (RCP 2.6) ensemble member is filtered via LFCA (a). Filtering is performed individually for each ensemble member to compute 100 scaling patterns whose results are averaged to diminish sampling issues. Differences in regression performance between Fig. 5a (unfiltered 1-member pattern scaling) and (a) are shown in (b) in terms of percentage. The area-weighted average RMSE is shown in (c) for RCPs 2.6, 4.5, and 8.5 and depending on whether the ensemble member is (blue) or not (yellow) filtered. Green indicates RMSE reduction between approaches in terms of percentage, whereas values on top of the bars are the absolute differences in cm.

Since the aim of this study is to explore differences in emulated DSL when ICV is reduced, we also assess potential differences between unfiltered and filtered simulations (Fig. 8) when predicting DSL at 2100 using GMTSLR as a predictor. Emulated DSL differences caused by filtering may differ depending on the realization used, as each realization features an ICV evolving in a different phase. Thus, we focus on the maximum emulated DSL differences that filtering causes out of all 100 MPI-GE simulations. Exploring the maximal potential difference in statistically projected DSL is an added benefit of using SMILES, as such analysis can only be done with a large set of realizations with out-of-phase variability.

The difference in emulated DSL varies geographically (Fig. 8), with a spatial variability resembling the RMSE when ICV is reduced (e.g., Fig. 6a and 7a). Areas characterized by high temporal variability, which pattern filtering does not completely remove, experience greater difference in DSL projections (Fig. 8). Unlike RMSE (e.g., Fig. 7a), the difference between emulated DSL differs between RCP scenarios, increasing in magnitude with radiative forcing (Fig. 8). RMSE measures the error throughout the entire regression without accounting for the predictor, so only the effect of reduced ICV is captured. On the other hand, an increasing difference in predicted DSL with stronger RCP is expected since the magnitude of the predictor (GMTSLR) is larger for higher emissions scenarios. However, we observe the opposite behavior when assessing the difference in emulated DSL in relative terms, i.e., when the difference is divided by the emulated unfiltered DSL or by GMTSLR in 2100 (not shown). Despite contrast between RCPs either in total difference (slightly increasing with forcing) or relative terms (decreasing with increasing forcing), RMSE being similar between RCPs highlights pattern filtering may be relevant for all scenarios.

The effect of pattern filtering on differences in slope $\alpha$, a key parameter in pattern scaling, shows again a similar spatial variability to RMSE (Fig. 7 vs Fig. S8). Changes in slopes are substantial in places with high variability, sometimes even showing a sign change (e.g., Fig. S13). Contrary to the total difference in emulated DSL and similar to the relative one, slope differences tend to decrease with higher emissions scenarios (Fig. S8). Since lower radiative forcing means lower signal-to-noise ratio, noise (ICV) can drive large differences in slopes between filtered and unfiltered results, and vice versa. Apart from reducing RMSE and leading to narrower confidence intervals (e.g., Fig., S10-14), pattern filtering finds slopes that are significantly different that the one obtained from applying a moving mean (e.g., Fig., S12 and 14), as the latter does not remove ICV as efficiently and requires neglecting data points for its computation (Fig., S10b-14b). It is worth highlighting that these differences in emulated DSL and slopes showcase an example for a GCM and may not hold as ground truth for other GCMs, scenarios, or predictors used.
Figure 8. Maximum difference between DSL change in 2100 obtained by pattern scaling with coefficients fitted to unfiltered and LFCA-filtered realizations, considering all 100 MPI-GE members, for RCP 2.6, RCP 4.5, and RCP 8.5 (a, b, and c, respectively).

We further explore the performance of LFCA by comparing the pattern scaling results when isolating the forced response for other GCMs. We identify the forced DSL in four CMIP5 models, being GISS-E2-R, HadGEM2-ES, IPSL-CM5A-LR, and MPI-ESM-LR (Fig. 9a-d, respectively), which all provide scenario simulations up to 2300. To ease comparison with results from the MPI-GE, however, we first examine results up to 2100 (Fig. 9a-d, small r.h.s. insets). RMSE from unfiltered simulations up to 2100 vary between models, and so does RMSE reduction provided by LFCA. Nonetheless, error reduction within a model and between scenarios is very similar, as previously observed for the MPI-GE. This implies that, for all models considered here, there are no significant changing behaviours in the relationship between DSL and GMTLSR between RCP scenarios up to 2100.

When considering results up to 2300, pattern scaling of unfiltered DSL against GMTSLR yields similar results as previous studies (Bilbao et al., 2015), showing a global area-weighted mean RMSE between 2 and 4 cm. RMSE in both unfiltered and filtered simulations of DSL increases with radiative forcing for all models considered. As simulations run up to 2300, a decrease in pattern scaling performance for higher RCPs may indicate a more important role of the deeper ocean layer driving
non-linear processes (Bilbao et al., 2015; Yuan and Kopp, 2021). This tendency is also reflected in the error reduction after filtering, which decreases as radiative forcing increases both over time and because of the higher emissions scenario, but the latter is more apparent. Although LFCA filtering improves the performance of pattern scaling for all four CMIP5 models, considerable differences in error reductions are observed. For instance, HadGEM2-ES benefits the most from pattern filtering between all the models, with a ~70% decrease in error for RCP 2.6. Conversely, GISS-E2-R undergoes the lowest reduction after pattern filtering, with about a 50% increase in performance for the same RCP scenario. Differences in model performance pre- and post-filtering do not only highlight differences in how ICV is represented in distinct models but may also reflect model differences in terms of physics representation and modelled forced response.

Figure 9. Area-weighted average RMSE for RCP 2.6, 4.5, and 8.5, indicating whether the ensemble member is (blue) or is not (yellow) filtered via LFCA. Green indicates relative RMSE reduction between approaches (%), whereas values on top of the bars are the absolute differences in cm. Different panels represent different CMIP5 models. The main panel includes simulation data up to 2300, whereas the small inset on the right-hand top corner shows RMSE results up to 2100. Small insets share the same axes as main panels.
5 Conclusions

Regional emulation tools for DSL change are complementary approaches to GCMs that allow for computationally cheap statistical projections. Most DSL regional emulators are based on pattern scaling, a statistical model usually based on a grid-point regression against a global variable representing change in the climate system driven by external forcing. While choosing suitable global predictors is essential for appropriate tuning of the statistical model, random errors can remain leading to high uncertainties in statistically based projections. A portion of these random errors are driven by ICV in DSL and can be characterised using macro-initialised initial condition large ensembles (SMILES), which are designed to facilitate a separation between ICV and external forcings within a model. Here, we applied pattern recognition techniques to a SMILE with the aim to efficiently truncate ICV, demonstrating how these approaches could significantly reduce random errors in regional emulators of DSL and provide substantially different emulated results in areas with high ICV.

Although ICV can be also reduced by using more conventional methods, such as computing an ensemble mean or linear trends, this requires a relatively large number of realizations to do it effectively. This is a significant constraint particularly for modelling experiments featuring a limited number of realizations. A more efficient alternative consists of employing methods that exploit spatial covariance information, such as S/N M EOF pattern filtering and LFCA. We have demonstrated that S/N M EOF applied to two realizations attains the same level of error reduction as averaging 12 realizations. The largest improvement relative to unfiltered simulations was observed when only a few simulations were available, whereas both S/N-filtered and ensemble average model performance tended to converge for a large number of ensemble members. By identifying spatiotemporal coherent structures, the S/N M EOF filtering was particularly skilful at removing ICV due to large modes of climate variability, such as the ENSO influence on sea level in the Eastern Pacific.

S/N M EOF pattern filtering can identify the common response within at least two realizations. This motivated us to also test LFCA, which can remove variability in single realization modelling experiments by applying a lowpass filter. Apart from being computationally more efficient, LFCA outperforms S/N M EOF in improving the performance of DSL pattern scaling when using one or two realizations. Moreover, LFCA applied to individual SMILE realizations allows exploring the maximal potential difference between statistically projected unfiltered and filtered DSL. We found substantial differences in emulated DSL and regression slopes in places with high variability, highlighting the relevance of pattern filtering methods in areas subject to non-mesoscale processes. Despite LFCA versatility and performances results, previous studies have emphasized that S/N M EOF pattern filtering provides a range of benefits compared to LFCA, including: 1) a better isolation of the forced response when the number of ensemble members is large, and 2) the detection of relatively less important forced patterns, such as those driven by volcanism.

We have also investigated LFCA by applying it to longer (up to 2300) CMIP5 simulations. We found that pattern scaling performance is independent of the GHG emission scenario up to 2100 and decreases with radiative forcing beyond 2100. Since we used a linear model, this implies that non-linear processes have different effects on DSL depending on the GHG scenario and this is reflected in a decrease in model performance depending on the emissions. We also found substantial differences
between CMIP5 models, due to variability being represented differently as well as distinct model physics. Nonetheless, the
performance improvement of pattern scaling when applying LFCA filtering is considerable for all models and scenarios,
ranging from 20% to more than 70% reduction relative to the unfiltered results.

Here, we have demonstrated that reducing ICV increases the capabilities of statistical approaches to project DSL. Pattern
recognition techniques are especially advantageous for such a task, as they do not require numerous realizations to significantly
reduce uncertainties in statistical projections and no data is lost (as in 30-year means) when reducing ICV. Previous studies
have not considered removing ICV, which could significantly reduce uncertainties in statistically projected DSL and lead to
substantial differences in emulates DSL. Although the difference in emulated DSL and regression slope varies depending on
scenario, and results shown here are an example and may differ depending on GCM, RCPs, and predictor used, we show that
pattern filtering is a useful approach to consider as a means of enhancing emulated DSL simulations.

**Code availability**

The methods used to perform this study are an adaptation from the ones used by Wills et al. (2020). The code is available at

**Data availability**

Simulations from the MPI-GE can be obtained at https://esgf-data.dkrz.de/projects/mpi-ge/, whereas CMIP5 data can be found
at https://esgf-node.llnl.gov/search/cmip5/.

**Author contribution**

VMS devised, designed, and performed the analysis, and wrote the manuscript. ABAS supervised the study and contributed
to writing. THJH contributed to data pre-processing and manuscript writing. SD and MM provided valuable feedback on
methods and contributed to writing. NM provided MPI-GE data, information on MPI-GE methods, and contributed to writing.

**Competing interests**

The authors declare that they have no conflict of interest.

**Acknowledgements**

VMS, ABAS, THJH were supported by PROTECT. This project has received funding from the European Union’s Horizon
2020 research and innovation programme under grant agreement No 869304, PROTECT contribution number XX. SD
acknowledges David and Jane Flowerree for their support. We acknowledge the World Climate Research Programme’s
Working Group on Coupled Modelling, which is responsible for CMIP, and we thank the climate modelling groups for
producing and making available their model output. For CMIP the U.S. Department of Energy’s Program for Climate Model
Diagnosis and Intercomparison provides coordinating support and led development of software infrastructure in partnership
with the Global Organization for Earth System Science Portals.

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