



Complex fault system revealed from 3-D seismic reflection data with deep learning and fault network analysis

Thilo Wrona^{1,2*}, Indranil Pan^{3,4,5}, Rebecca E. Bell⁶, Christopher A-L. Jackson⁷, Robert L. Gawthorpe¹, Haakon Fossen⁸, Edoseghe E. Osagiede¹, and Sascha Brune^{2,9}

⁹Institute of Geosciences, University of Potsdam, Potsdam-Golm, Germany. 15

Correspondence to: Thilo Wrona (thilowrona@gmail.com)

Abstract. Understanding where normal faults are is critical to an accurate assessment of seismic hazard, the successful exploration for and production of natural (including low-carbon) resources, and for the safe subsurface storage of CO2. Our current knowledge of normal fault systems is largely derived from seismic reflection data imaging intra-continental rifts and

- continental margins. However, exploitation of these data is limited by interpretation biases, data coverage and resolution, 20 restricting our understanding of fault systems. Applying supervised deep learning to one of the largest offshore 3-D seismic reflection data sets from the northern North Sea allows us to image the complexity of the rift-related fault system. The derived fault score volume allows us to extract almost 8000 individual normal faults of different geometries, which together form an intricate network characterised by a multitude of splays, junctions and intersections. Combining tools from deep
- learning, computer vision and network analysis allows us to map and analyse the fault system in great detail and a fraction of 25 the time required by conventional interpretation methods. As such, this study shows how we can efficiently identify and analyse fault systems in increasingly large 3-D seismic data sets.

1 Introduction

Understanding the geometry and growth of normal fault systems is critical when assessing seismic hazard, when identifying 30 suitable sites for subsurface CO₂ storage and when exploring for natural resources (traditional and low-carbon). For example, whereas probabilistic seismic hazard analyses based on seismic event catalogues are extremely useful when trying to forecast earthquake likelihood and location, high-resolution fault mapping, preferably in 3-D, can help us constrain the slip tendency of faults, where seismic catalogues are discontinuous and/or incomplete (e.g. Morris et al., 1996; Moeck et al., 2009;

⁵

¹Department of Earth Science, University of Bergen, Allégaten 41, N-5007 Bergen, Norway. ²GFZ German Research Centre for Geosciences, Telegrafenberg, 14473 Potsdam, Germany. ³Centre for Process Systems Engineering & Centre for Environmental Policy, Imperial College London, UK. ⁴The Alan Turing Institute, British Library, London, UK. ⁵School of Mathematics, Statistics & Physics, Newcastle University, UK. 10 ⁶Basins Research Group (BRG), Department of Earth Science and Engineering, Imperial College, Prince Consort Road, London, SW7 2BP, UK. ⁷Department of Earth and Environmental Sciences, University of Manchester, Manchester, UK ⁸Museum of Natural History, University of Bergen, Allégaten 41, N-5007 Bergen, Norway.





Yukutake et al., 2015). Moreover, faults can facilitate (or impede) fluid and gas migration to the Earth's surface, thus
determining their geometry and connectivity, as well as their hydraulic properties is key for assessing their role in the long-term subsurface storage of CO₂ (Bissell et al., 2011; Kampman et al., 2014). In both of these examples, we need robust predictions of 3-D fault geometry over large areas and across a wide range of scales (100s m to 100 km).

Accurately mapping fault systems in 2-D and 3-D seismic reflection data typically requires expertise and time (e.g. Bond, 2015). While we can map fault systems in great detail over small areas using 3-D seismic reflection data (e.g. Lohr et

- 40 al., 2008; Wrona et al., 2017; Claringbould et al., 2020), we lack an understanding of the character of 3-D fault populations at the scale of entire rift systems, as regional studies are often limited to only sparse, 2-D seismic sections (e.g. Clerc et al., 2015; Fazlikhani et al., 2017; Phillips et al., 2019). 3-D numerical models are now capable of simulating fault networks at the rift scale; however, there are few observational data sets of the same scale to test the predictions of these models and, therefore, help refine them (e.g. Naliboff et al., 2020; Pan et al., 2021).
- 45 Supervised deep learning allows us to map faults in seismic reflection data (e.g. Wu et al., 2019; Mosser et al., 2020; Wrona et al., 2021a), but up until now these studies have been in the "proof of concept" phase, simply focusing on detecting faults; such studies have yet to provide new insights into the geometry of normal faults. In this study, by applying supervised deep learning to newly-acquired broadband 3-D seismic reflection data imaging much of the northern North Sea rift (161 km wide in E-W, 266 km long area in N-S, 0-20 km deep), we map the fault network associated with a continental
- 50 rift basin at an unprecedented level of detail. Using manually labelled data (<0.1% of data volume), we train a deep convolutional neural network (U-Net) to predict faults in our data set. The predicted score ranges from 0 (no fault) to 1 (fault). Based on this score across the entire 3-D seismic volume we employ a second workflow to extract the normal fault system as a network (a set of nodes and edges) allowing us to investigate the architecture and growth of this extremely complex system consisting of thousands of intersecting faults.

55 2 Geological setting

The study area is located in the northern North Sea (Fig. 1), where continental crust consists of 10–30-km-thick crystalline basement overlain by as much as 12 km of sedimentary strata deposited during, after, and possibly even before periods of rifting in the late Permian–Early Triassic (rift phase 1) and Middle Jurassic–Early Cretaceous (rift phase 2) (e.g. Whipp et al., 2014; Bell et al., 2014; Maystrenko et al., 2017). The extension direction of these two phases has long been debated.
60 Whereas most studies agree that the late Permian–Early Triassic rifting was driven by E-W extension (e.g. Færseth et al., 1997; Torsvik et al., 1997), Middle Jurassic–Early Cretaceous rifting has been associated with both E-W (e.g. Bartholomew et al., 1993; Brun and Tron, 1993) and NW-SE extension (e.g. Færseth, 1996; Doré et al., 1997; Færseth et al., 1997) (Fig. 1B). This debate is further complicated by the fact that some of the largest normal faults on the Horda Platform developed during rift phase 1, but were subsequently reactivated during rift phase 2 (e.g. Whipp et al., 2014; Bell et al., 2014). The

65 crystalline basement underlying the sedimentary strata formed by terrane accretion during the Sveconorwegian (1140-900





Ma) and Caledonian (460–400 Ma) orogenies (Bingen et al., 2008). Several studies argue that this structural template, in particular the ductile shear zones, controlled the location, strike, and overall pattern of rift-related faulting in the overlying sedimentary successions being reactivated as normal faults, or by limiting the along-strike propagation of faults (e.g. Fazlikhani et al., 2017; Phillips et al., 2019; Osagiede et al., 2020; Wiest et al., 2020).

70 3 Data & Methods

3.1 3-D seismic reflection data

In this study, we use one of the largest offshore 3-D seismic data sets ever acquired, which images a large part of the northern North Sea rift across an area of 35,410 km2, and with excellent depth-imaging down to 22 km (i.e., the middle-to-lower crust) (Figs. 1, 2A, 3). The data set was acquired using eight, up to 8-km-long streamers that were towed ~40 m below 75 the water surface. The broadseis technology used for recording covers a wide range of frequencies (2.5-155 Hz), providing high-resolution depth imaging. The data were binned at 12.5 × 18.75 m, with a vertical sample rate of 4 ms. The data was 3-D true amplitude prestack depth-migrated. The seismic volume was zero-phase processed with SEG normal polarity; i.e., a positive reflection (white) corresponds to an acoustic impedance (density × velocity) increase with depth. More details on data acquisition and pre-processing steps are provided by Wrona et al., (2019, 2021a).

80 3.2 Deep learning

Deep learning describes a set of algorithms and models, which learn to perform a specific task (e.g. fault interpretation) on a given data set without explicit feature engineering (e.g. the calculation and calibration of seismic attributes, such as coherence or variance). Deep learning allows the derivation of a fault score volume that highlights normal faults within a 3-D seismic volume. This approach requires that a large number of examples of faults and unfaulted strata are labelled in the

- 85 training seismic data. We extract 80,000 such examples (2-D squares of 128×128 pixels) from 22 interpreted seismic sections oriented perpendicular to the N-trending rift (Figs. 1A, 2). Note that these seismic sections only constitute <0.1% of the entire 3-D seismic volume. Next, we split these examples into three groups; one set for training (80%), one for validation (10%), and one for testing (10%). We use the first of these to train a deep convolutional neural network (U-Net) designed to perform image segmentation tasks (Ronneberger et al., 2015). Using the validation set, we track the accuracy of the model</p>
- 90 during training and stop once the loss does not decrease further. Finally, we apply the model to the entire 3-D seismic volume to derive a fault score volume (Figs. 3, 4), an attribute, which ranges from 0 (no fault) to 1 (fault). All details of the workflow and the code are provided by Wrona et al. (2021b, 2021a).





3.3 Automated fault network extraction and analysis

Extracting a fault network from the 3-D volume allows us to perform a comprehensive geometric analysis of the fault system using our fault analysis toolbox - fatbox (Wrona et al., 2022). The basic idea is to describe a fault system in 2-D as a network (or graph), i.e. sets of nodes and edges (Fig. 5). Each node marks a location along the fault and each edge connects two nodes. All nodes connected to one another by edges are labelled as a (connected) component.

100

Our fault extraction workflow consists of these eight steps: (1) extract horizon, (2) Gaussian blur filter, (3) thresholding, (4) cleaning, (5) skeletonization, (6) connect components, (7) add nodes to graph, (8) add edges to graph and (9) split junctions. While applying it to our North Sea target region, we first attempt to capture as many faults as possible by extracting the fault score along a horizon 500 m below Base Cretaceous Unconformity (BCU) (Fig. 1C). Here we observe a

- 105 large number of faults, which were either formed in the second rift phase, or formed in the first rift phase and reactivated in the second rift phase (Figs. 4, 6A). Second, we apply a Gaussian blur filter to increase fault continuity (Fig. 6B). Third, we apply a threshold of 0.35 to separate the faults from the background in the fault likelihood (Fig. 6C). This threshold is a tradeoff, which balances capturing as many faults as possible (lower values) and identifying clearly resolvable faults (high values). Four, we further restrict this threshold and essentially filter these points by removing areas smaller than 25 pixels
- (Fig. 6D). Five, we collapse the faults to one-pixel wide lines using skeletonization (Guo and Hall, 1992) (Fig. 6E). Six, we label adjacent pixels in the image as connected components (Wu et al., 2009) (Fig. 6F). Each component consists of pixels which are connected to each other. These components represent the faults in the network. At this point, we can build our graph using these connected components of the image (Fig. 6F). Each pixel belonging to a component becomes a node whereas edges are created between neighbouring nodes (Fig 6G-I). This process results in a number of faults with splays,
- 115 junctions or intersections being grouped into one connected component (Fig. 7A). To correct this, we split up junctions (nodes with three edges) based on the similarity of strike, i.e. aligned branches remain connected (Fig. 7B,C). This final network is compared to the Base Late Jurassic horizon mapped by Tillmans et al., (2021) (Fig. 8). Additionally, we perform the exact same workflow on ten slices through the fault score volume (1-10 km depth) to capture 3-D fault geometries with depth (Fig. 9).
- 120 After extracting the fault system, we calculate a series of typical fault properties using our fault analysis toolbox fatbox (Wrona et al., 2022) (Fig. 10). First, we calculate the fault length as the sum of the edge lengths of each component (Fig. 10B). Second, we calculate the strike along the fault from neighbouring nodes (Fig. 10C). If we were to calculate the overall fault strike, we would overlook along-strike variations in strike. If we were to calculate the strike as the orientation of each edge, we would only obtain values of 0, 45 or 90°, because the nodes are closely spaced. Instead, we calculate the strike
- 125 from the 3rd degree neighbouring nodes (i.e. neighbours of neighbours of neighbours). This assures a robust, high resolution fault strike calculation. Combining the fault length and strike, we can generate a length-weighted Rose diagram (Fig. 10C). Finally, we calculate the fault density as the fault length per area (Fig. 10D).





3.4 Comparison to conventional seismic interpretation

- We can ask ourselves, "how good are our results compared to a state-of-the-art fault interpretation from the same data set 130 using conventional fault mapping techniques?" (Fig. 8). Tillmans et al., (2021) map the Base Late Jurassic (base of syn-rift sediments associated with rift phase 2) on the eastern flank of the North Viking Graben (see Figs. 1A, 4 for location) using a combination of manual picking and auto-tracking. This horizon is calibrated with 40 exploration wells, which provide direct constraints on the depth of the surface. Tillmans et al. (2021) highlight the fault system by computing the variance attribute (Chopra and Marfurt, 2007) along the horizon (Fig. 7A). On top of the horizon, we plot the fault network mapped from the 135
- fault score extracted 500 m below the easily-mappable Base Cretaceous Unconformity (BCU) (Fig. 8B). This visual comparison shows that while we are missing a few faults in the southwest of the map, we are able to identify and accurately represent most of the faults identified by Tillmans et al. (2021). The missing faults are either overlooked by our model (i.e. false negatives) or result from the difference in the horizons that we compare: Base Cretaceous Unconformity (our study) 140 versus Base Late Jurassic (Tillmans et al., 2021).

4 Observations

Our fault extraction allows us to map a complex network consisting of 7983 individual faults across an approximately 161 km-wide and 266 km-long area, covering 35,410 km2 of the northern North Sea rift (Fig. 7C).

4.1 Fault length

145 Faults vary in length by 3 orders of magnitude - from 50 m to 75.9 km, with some of the longest faults (>30 km) extending from the Stord Basin and Bjørgvin Arch in the south to the Uer and Lomre Terrace in the north (Fig. 10B). In cross-section, these faults have up to several kilometres of displacement and bound rotated half-graben (e.g. Whipp et al., 2014; Bell et al., 2014) (Fig. 3B,C). While we observe some long (up to 20 km) faults in the Viking Graben and Tampen Spur, most faults (>90%) are closely spaced (< 5 km) and relatively short (<10 km long) (Fig. 10B).

150 4.2 Fault strikes

In map view, we observe a complex network consisting of a large number of variably trending faults that display a broad range of intersection styles (e.g., oblique, perpendicular). These faults show a large range of strikes, varying from NW-SE to NE-SW (Figs. 9, 10C). The length-weighted rose plot shows that most faults strike NW-SE (light blue) or NNE-SSW (light orange), with a large number showing intervening strike directions (Fig. 10C). This general divide occurs between

predominantly NW-SE-striking faults along the eastern part of the rift and NE-SW-striking faults in the central and 155 northwestern part of the rift. This divide becomes most evident when comparing faults on the Lomre Terrace (NE-SW) to the adjacent Bjørgvin Arch (NW-SE), at least at the structural level of the Base Cretaceous Unconformity (Fig. 10C).





4.3 Fault density

160

In map view, we observe large variations in fault density 500 below the BCU (Fig. 10D). While dense networks of intersecting faults result in high density areas (e.g. Lomre Terrace, Bjørgvin Arch) we observe low densities in the Viking and Sogn Graben, where faults occur at greater depths (e.g. Fig. 9C).

4.4 Vertical continuity

The faults extracted at different depths are variable in their vertical continuity (i.e., fault height; Fig. 8). Whereas some faults, in particular in the Stord Basin, the Tampen Spur, and the Magnus Basin show parallel fault traces from 1 to 10 km
165 depth (Fig. 9A), we also observe a large number of faults that occur only at shallower (1-5 km) or at greater depths (6-10 km) (Fig. 9B, C). Upon closer inspection, we observe that the faults, which occur continuously between 1-10 km depth, e.g. in the eastern Stord Basin and the Bjørgvin Arch, are typically large-displacement normal faults with tens of kilometres spacing (e.g. Fig. 3B, C), whereas the other faults, which only occur between 6-10 km depth (e.g. northwestern Stord Basin), are usually shorter and more closely spaced (a few kilometres) (e.g. Fig. 9C).

170 5 Discussion

5.1 Advantages of deep learning based fault interpretation

When comparing our results to conventional interpretation methods, we can ask ourselves "what value does deep learning add?". Here, we highlight the advantages of the supervised deep learning-based fault interpretation workflow which we present in this study. First, we can predict faults in a seismic section in a fraction of the time (5 seconds) required by expert
interpreters (~10 minutes). These differences accumulate, in particular when interpreting such a large data set with >22000 inlines. A conventional fault interpretation of such a large data set can take several months, whereas a trained convolutional neural network can identify faults across the entire volume within a day on a single GPU (GeForce GTX 1080 Ti).

Second, after identifying faults in seismic reflection data, they also need to be mapped before we can perform the relevant fault analysis. Here we map the fault network using a series of tools from computer vision and network analysis toolbox - fatbox (Wrona et al., 2022) (Figs. 6, 7). Our automated workflow extracts the fault network in less than five minutes compared to the several weeks to months that would have been required to manually map the faults in this large data set. Furthermore, once extracted, we can immediately conduct a number of typical fault analyses using predefined functions implemented in fatbox (Wrona et al., 2022) (e.g. Fig. 10).

Third, conventional fault interpretations are often binary (fault vs. no fault), but deep learning delivers a score ranging from 0 (no fault) to 1 (fault), which allows a subsequent analysis of how likely it is to encounter a fault at any point. This type of analysis is particularly useful for assessing the sealing potential of certain layers for CO₂ storage and for predicting fluid flow during geothermal exploration. Fourth, seismic interpreters typically focus on the largest faults,





whereas our model performs the same prediction across the entire data set and does not differentiate between faults based on their size, shape or orientation. Fifth, given the same data, labels, model and training, our model and results are fully 190 reproducible, which is not the case for conventional fault interpretations, where the interpreter has to make a myriad of decisions in the process of mapping a fault network.

5.2 Complex fault system in the northern North Sea

Our study shows how to reveal the complex geometry of normal fault systems in 3-D seismic reflection data using a combination of deep learning and automated fault extraction. We were able to map an intricate network consisting of almost 8000 individual faults that cover an area approximately 161 km wide and 266 km long (e.g. Figs. 4, 6, 10). This fault 195 network shows large variations in fault length, strike and density, with extremely complex splays, junctions and intersections between these faults (Figs. 7-11). As such, our work goes far beyond typical seismic interpretations in previous case studies, which covered only a fraction of the rift (e.g. Duffy et al., 2015; Deng et al., 2017; Tillmans et al., 2021), or regional studies that mapped <100 of the largest faults using primarily sparse, 2-D seismic sections (e.g. Fig. 1B; Fazlikhani et al., 2017; Phillips et al., 2019).

200

5.3 Uncertainties during fault mapping

While there are several advantages to our approach, it is worth remembering the uncertainties associated with mapping faults in seismic reflection data. First, seismic reflection data can only image faults with displacement above the seismic resolution (and level of noise) of the data set. The seismic resolution of our data set decreases from 15 m (vertical) and 30 m (lateral) 205 around 3 km depth down to 180 m (vertical) around 20 km depth (see Wrona et al., 2019; Tillman et al., 2021). Second, the labels we use to train our model are derived from 22 interpreted seismic sections, which, like any seismic interpretation, contains the expertise and biases of the interpreter (e.g. Bond et al., 2007, Bond 2015). Third, the convolutional neural network that we trained achieves an accuracy of 83%, implying that 17% of the data is misclassified (see Wrona et al., 2021). A closer inspection reveals that 36% are false positives (i.e. faults that were overlooked) and 5% are false negatives 210 (i.e. faults that were misinterpreted) (see Wrona et al., 2021). Despite these limitations, the robustness of our approach is evident when considering along-strike fault continuity across a large number of different seismic lines (Fig. 10, 11).

5.4 Future research on automated fault mapping

Based on our work, we can identify three areas for future research on this subject. First, conventional neural networks predict a score from 0 to 1, which we can use as a proxy for how likely it is to encounter a fault at a point. Bayesian neural networks,

on the other hand, allow the prediction of true fault probabilities (e.g. Mosser et al., 2020). Predicting fault probabilities in 215 regional seismic data sets could significantly accelerate the screening for and risk assessment of potential CO2 storage sites (see Wrona and Pan, 2021). Second, in addition to predicting where faults occur, we can explore the prediction of other fault





properties, such as displacement, fault zone permeability or even the time when they were active. This would significantly allow us to study the spatial and temporal evolution of fault systems in high resolution at a regional scale. Third, while our
fault extraction workflow currently focuses on mapping fault networks in a series of 2-D slices or horizons, we really need freely-available methods to generate 3-D fault surfaces, which allow for complex fault splays, junctions and intersections, as observed here.

6 Conclusions

This study shows that the combination of deep learning and network analysis applied to 3-D seismic reflection data allows us, for the first time, to map almost 8000 normal faults across the entire northern North Sea rift. These faults form an intricate network with complex relationships (e.g. splays, junctions, intersections) including large variations in fault length (50 m to 75.9 km) and strikes (NW-SE to NE-SW). As such, this work goes far beyond previous seismic studies by providing high resolution fault maps at a regional scale in a fraction of the time required by conventional interpretation methods.

230 Acknowledgements

We would like to thank The Norwegian Academy of Science and Letters (VISTA), The University of Bergen and The Initiative and Networking Fund of the Helmholtz Association through the project "Advanced Earth System Modelling Capacity (ESM), The Geo.X Network and Deutsche Forschungsgemeinschaft (Projektnummer 460760884) for supporting this research. S. Brune has been funded through the Helmholtz Young Investigators Group CRYSTALS (VH-NG-1132). I. Pan acknowledges the NUAcT fellowship for partially supporting the work. We are grateful to CGG, in particular Stein Åsheim and Jaswinder Mann, for the permission to present this data and publish this work. We thank Schlumberger for

References

235

Bartholomew, I.D., Peters, J.M., and Powell, C.M., Regional structural evolution of the North Sea: Oblique slip and the
 reactivation of basement lineaments, in Petroleum Geology Conference Proceedings, v. 4, p. 1109–1122, doi:10.1144/0041109, 1993.

providing the software Petrel 2019© and Leo Zijerveld for IT support.

Bell, R.E., Jackson, C.A.L., Whipp, P.S., and Clements, B., Strain migration during multiphase extension: Observations from the northern North Sea: Tectonics, v. 33, p. 1936–1963, doi:10.1002/2014TC003551, 2014.





- Bissell, R.C., Vasco, D.W., Atbi, M., Hamdani, M., Okwelegbe, M., and Goldwater, M.H., A full field simulation of the In
 Salah gas production and CO2 storage project using a coupled geo-mechanical and thermal fluid flow simulator:
 Energy Procedia, v. 4, p. 3290–3297, 2011.
 - Bond, C.E., Uncertainty in structural interpretation: Lessons to be learnt: Journal of Structural Geology, v. 74, p. 185–200, doi:10.1016/j.jsg.2015.03.003, 2015.
 - Brun, J.P., and Tron, V., Development of the North Viking Graben: inferences from laboratory modelling: Sedimentary

Geology, v. 86, p. 31-51, doi:10.1016/0037-0738(93)90132-0, 1993.

- Chopra, S., and Marfurt, K.J., Seismic Attributes for Prospect Identification and Reservoir Characterization: Society of Exploration Geophysicists and European Association of Geoscientists and Engineers, doi:10.1190/1.9781560801900, 2007.
- Claringbould, J.S., Bell, R.E., Jackson, C.A.L., Gawthorpe, R.L., and Odinsen, T., Pre-breakup Extension in the Northern
- 255 North Sea Defined by Complex Strain Partitioning and Heterogeneous Extension Rates: Tectonics, v. 39, doi:10.1029/2019TC005924, 2020.
 - Clerc, C., Jolivet, L., and Ringenbach, J.C., Ductile extensional shear zones in the lower crust of a passive margin: Earth and Planetary Science Letters, v. 431, p. 1–7, doi:10.1016/j.epsl.2015.08.038, 2015.
- Deng, C., Fossen, H., Gawthorpe, R.L., Rotevatn, A., Jackson, C.A.L., and FazliKhani, H., Influence of fault reactivation
 during multiphase rifting: The Oseberg area, northern North Sea rift: Marine and Petroleum Geology, v. 86, p. 1252–1272, doi:10.1016/J.MARPETGEO.2017.07.025, 2017.
 - Doré, A.G., Lundin, E.R., Fichler, C., and Olesen, O., Patterns of basement structure and reactivation along the NE Atlantic margin: Journal of the Geological Society, v. 154, p. 85–92, doi:10.1144/gsjgs.154.1.0085, 1997.
- Duffy, O.B., Bell, R.E., Jackson, C.A.L., Gawthorpe, R.L., and Whipp, P.S., Fault growth and interactions in a multiphase
 rift fault network: Horda Platform, Norwegian North Sea: Journal of Structural Geology, v. 80, p. 99–119, doi:10.1016/J.JSG.2015.08.015, 2015.
 - Færseth, R.B., Interaction of permo-triassic and jurassic extensional fault-blocks during the development of the northern North Sea: Journal of the Geological Society, v. 153, p. 931–944, doi:10.1144/gsjgs.153.6.0931, 1996.
 - Færseth, R.B., Knudsen, B.E., Liljedahl, T., Midbøe, P.S., and Søderstrøm, B., Oblique rifting and sequential faulting in the
- Jurassic development of the northern North Sea: Journal of Structural Geology, v. 19, p. 1285–1302, doi:10.1016/s0191-8141(97)00045-x, 1997.
 - Fazlikhani, H., Fossen, H., Gawthorpe, R.L., Faleide, J.I., and Bell, R.E., Basement structure and its influence on the structural configuration of the northern North Sea rift: Tectonics, v. 36, p. 1151–1177, doi:10.1002/2017TC004514, 2017.
- 275 Guo, Z., and Hall, R.W., Fast fully parallel thinning algorithms: CVGIP: Image Understanding, v. 55, p. 317–328, doi:10.1016/1049-9660(92)90029-3, 1992.





- Kampman, N., Bickle, M., Wigley, M., and Dubacq, B., Fluid flow and CO2–fluid–mineral interactions during CO2-storage in sedimentary basins: Chemical Geology, v. 369, p. 22–50, 2014.
- Lohr, T., Krawczyk, C.M., Oncken, O., and Tanner, D.C., Evolution of a fault surface from 3D attribute analysis and displacement measurements: Journal of Structural Geology, v. 30, p. 690–700, doi:10.1016/j.jsg.2008.02.009, 2008.
- Maystrenko, Y.P., Olesen, O., Ebbing, J., and Nasuti, A., Deep structure of the northern north sea and southwestern Norway based on 3D density and magnetic modelling: Norsk Geologisk Tidsskrift, v. 97, p. 169–210, doi:10.17850/njg97-3-01, 2017.
- Moeck, I., Kwiatek, G., and Zimmermann, G., Slip tendency analysis, fault reactivation potential and induced seismicity in a deep geothermal reservoir: Journal of Structural Geology, v. 31, p. 1174–1182, 2009.
 - Morris, A., Ferrill, D.A., and Henderson, D.B., Slip-tendency analysis and fault reactivation: Geology, v. 24, p. 275–278, 1996.
 - Mosser, L., Purves, S., and Naeini, E.Z., Deep bayesian neural networks for fault identification and uncertainty quantification: 1st EAGE Digitalization Conference and Exhibition, doi:10.3997/2214-4609.202032036, 2020.
- 290 Naliboff, J.B., Glerum, A., Brune, S., Péron-Pinvidic, G., and Wrona, T., Development of 3D rift heterogeneity through fault network evolution: Geophysical Research Letters, doi:10.1029/2019gl086611, 2020.
 - Osagiede, E.E., Rotevatn, A., Gawthorpe, R., Kristensen, T.B., Jackson, C.A., and Marsh, N., Pre-existing intra-basement shear zones influence growth and geometry of non-colinear normal faults, western Utsira High–Heimdal Terrace, North Sea: Journal of Structural Geology, v. 130, p. 103908, 2020.
- 295 Pan, S., Naliboff, J., Bell, R.E., and Jackson, C., Bridging spatiotemporal scales of normal fault growth using numerical models of continental extension: EarthArXiv, doi:10.31223/X5DG7M, 2021.
 - Phillips, T.B., Fazlikhani, H., Gawthorpe, R.L., Fossen, H., Jackson, C.A.L., Bell, R.E., Faleide, J.I., and Rotevatn, A., The Influence of Structural Inheritance and Multiphase Extension on Rift Development, the NorthernNorth Sea: Tectonics, v. 38, p. 4099–4126, doi:10.1029/2019TC005756, 2019.
- 300 Tillmans, F., Gawthorpe, R.L., Jackson, C.A. -L., and Rotevatn, A., Syn-rift sediment gravity flow deposition on a Late Jurassic fault-terraced slope, northern North Sea: Basin Research, v. 33, p. 1844–1879, doi:10.1111/BRE.12538, 2021.
 - Torsvik, T.H., Andersen, T.B., Eide, E.A., and Walderhaug, H.J., The age and tectonic significance of dolerite dykes in western Norway: Journal of the Geological Society, v. 154, p. 961–973, doi:10.1144/gsjgs.154.6.0961, 1997.
- 305 Whipp, P.S., Jackson, C.A.L., Gawthorpe, R.L., Dreyer, T., and Quinn, D., Normal fault array evolution above a reactivated rift fabric; a subsurface example from the northern Horda Platform, Norwegian North Sea: Basin Research, v. 26, p. 523–549, doi:10.1111/bre.12050, 2014.
 - Wiest, J.D., Wrona, T., Bauck, M.S., Fossen, H., Gawthorpe, R.L., Osmundsen, P.T., and Faleide, J.I., From Caledonian Collapse to North Sea Rift: The Extended History of a Metamorphic Core Complex: Tectonics, v. 39, doi:10.1029/2020TC006178, 2020.





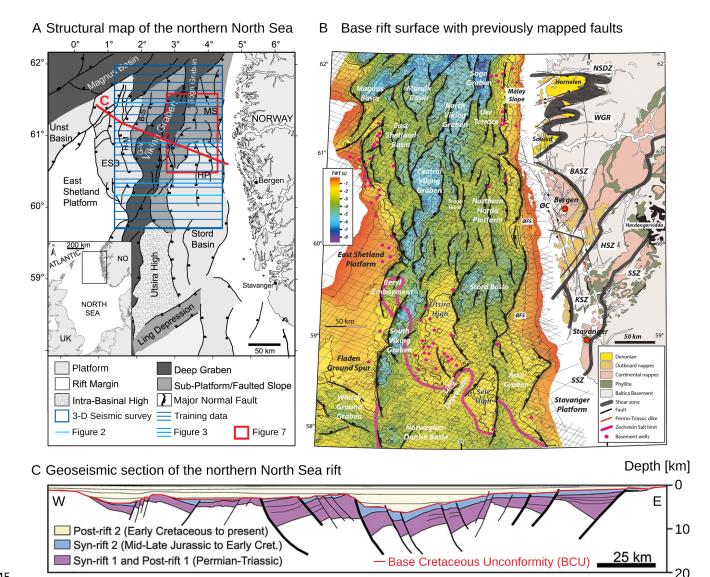
- Wrona, T., Brune, S., Gayrin, P., and Hake, T., Fatbox Fault Analysis Toolbox: GFZ Data Services, doi:10.5880/GFZ.2.5.2022.002, 2022.
- Wrona, T., Magee, C., Fossen, H., Gawthorpe, R.L.L., Bell, R.E.E., Jackson, C.A.-L.A.L., and Faleide, J.I.I., 3-D seismic images of an extensive igneous sill in the lower crust: Geology, v. 47, p. 729–733, doi:10.1130/G46150.1, 2019.
- 315 Wrona, T., Magee, C., Jackson, C.A.L.C.A.-L.C.A.L., Huuse, M., and Taylor, K.G.K.G., Kinematics of polygonal fault systems: Observations from the northern north sea: Frontiers in Earth Science, v. 5, p. 101, doi:10.3389/feart.2017.00101, 2017.
 - Wrona, T., and Pan, I., Can machine learning improve carbon storage? Synergies of deep learning, uncertainty quantification and intelligent process control, 2021.
- 320 Wrona, T., Pan, I., Bell, R.E., Gawthorpe, R.L., Fossen, H., and Brune, S., 3D seismic interpretation with deep learning: A brief introduction: Society of Exploration Geophysicists, v. 40, p. 524–532, doi:10.1190/tle40070524.1, 2021a.
 - Wrona, T., Pan, I., Bell, R.E., Gawthorpe, R.L., Fossen, H., and Brune, S., 3-D seismic interpretation with deep learning: a set of Python tutorials:, doi:10.5880/GFZ.2.5.2021.001, 2021b.
- Wu, X., Liang, L., Shi, Y., and Fomel, S., FaultSeg3D: Using synthetic data sets to train an end-to-end convolutional neural
 network for 3D seismic fault segmentation: GEOPHYSICS, v. 84, p. IM35–IM45, doi:10.1190/geo2018-0646.1, 2019.
 - Wu, K., Otoo, E., and Suzuki, K., Optimizing two-pass connected-component labeling algorithms: Pattern Analysis and Applications, v. 12, p. 117–135, doi:10.1007/S10044-008-0109-Y, 2009.

Yukutake, Y., Takeda, T., and Yoshida, A., The applicability of frictional reactivation theory to active faults in Japan based on slip tendency analysis: Earth and Planetary Science Letters, v. 411, p. 188–198, 2015.

335







345

350

Figure 1: A Structural overview map of the northern North Sea basin system (from Tillmans et al., 2021 after Færseth, 1996). Blue rectangle marks the outline of the seismic survey in this study. ESB = East Shetland Basin, B-S = Brent-Statfjord Fault, G-V = Gullfaks-Visund Fault, MS = Måløy Slope, HP = Horda Platform. B The base rift surface (base Permo-Triassic rifting) time-structure map in the northern North Sea rift (from Fazlikhani et al., 2017) and the geology of southwestern Norway, showing the general onshore and offshore structural configuration in the study area. Bold black lines highlight major rift-related normal faults displacing the base rift surface where all units older than Upper Permian are considered basement. Black lines in the background show some of the 2-D seismic reflection surveys used by Fazlikhani et al. (2017). NSDZ, Nordfjord-Sogn Detachment Zone; BASZ, Bergen Arc Shear Zone; WGR, Western Gneiss Region; ØC, Øygarden Complex (gneiss); ØFS, Øygarden Fault System; HSZ, KSZ, and; SSZ: Hardangerfjord, Karmøy, and Stavanger shear zones, respectively. C Regional interpretation of the structure of

355 the northern North Sea after Færseth (1996).





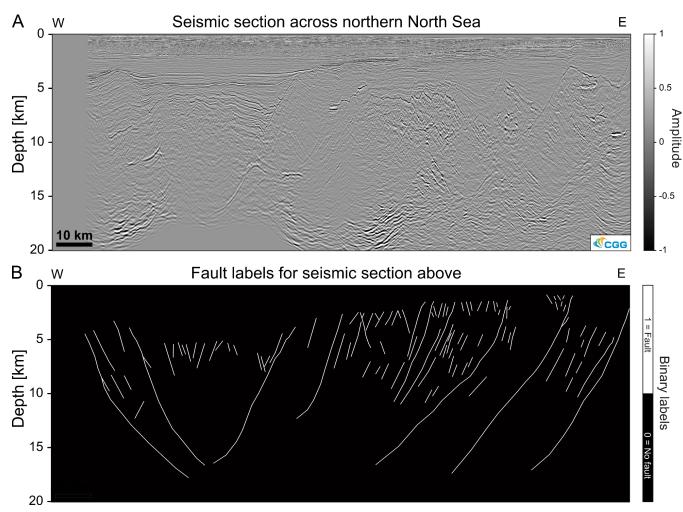


Figure 2: A Example seismic section across the northern North Sea. Amplitudes are scaled for machine learning B Example of fault interpretation of the section used to train a deep convolutional neural network for fault prediction.

365





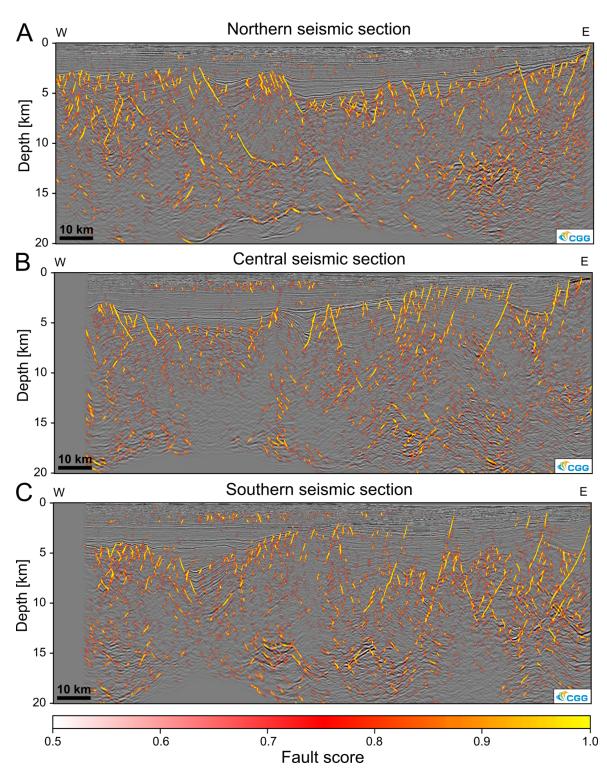


Figure 3: Examples of seismic sections extracted from fault score volume of the 3-D seismic data set. Note that these sections were not part of the training data, but are actually 6.25 km away from the closest interpreted seismic section (see Fig. 1A).





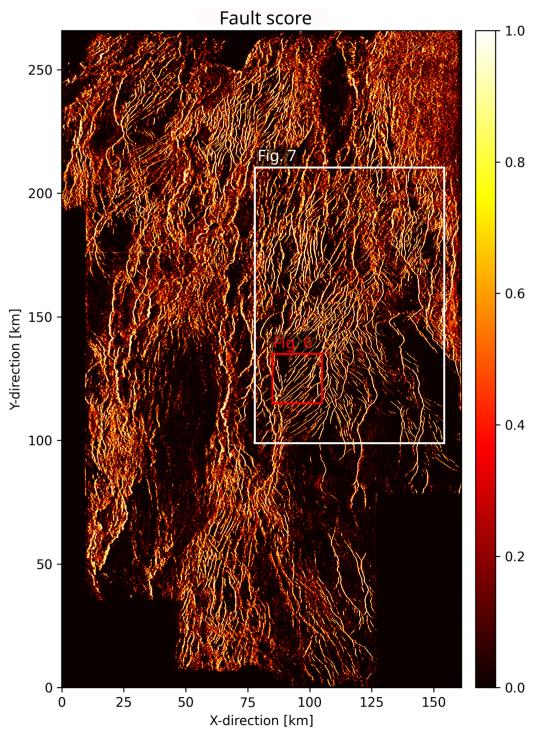


Figure 4: Surface capturing tectonic faults extracted from fault likelihood volume. The surface was extracted 500 m below the Base Cretaceous Unconformity, where we observe a large number of faults, which were either formed or reactivated in the second rift phase. White rectangle shows the area used for validation (Fig. 8) and the red rectangle indicates the area where we demonstrate our fault network extraction workflow (Fig. 6).





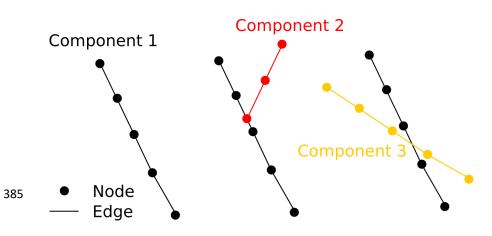
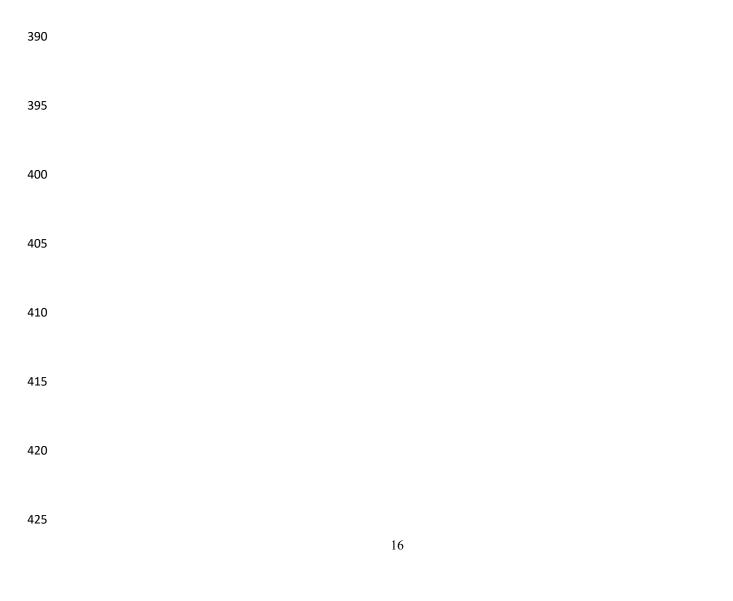
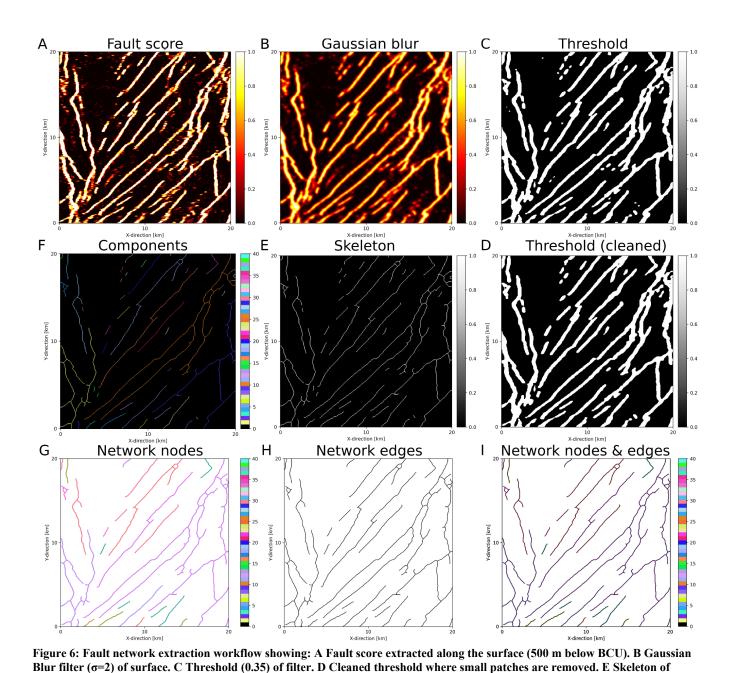


Figure 5: Schematic illustration of fault network (or graph) with nodes, edges and components. Each node marks a location along the fault. Each edge connects two nodes and each (connected) component indicates all nodes connected to one another by edges.

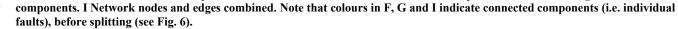








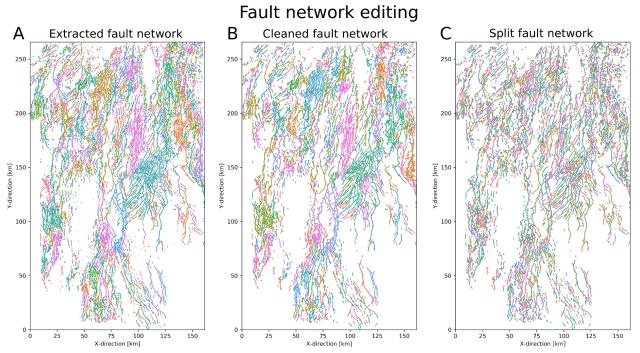
430



cleaned threshold. F Connected components of skeleton. G Network nodes based on components. H Network edges based on







440 Figure 7: A Fault network extracted from BCU (Fig. 4D). Note the large areas with the same colours resulting from multiple faults being grouped into one connected component B Fault network after removal of noise (i.e. small components). C Fault network after splitting junctions previously connecting splaying and intersecting faults. Note that large connected components are split up and individual faults are highlighted by different colours.

445

450

455

460





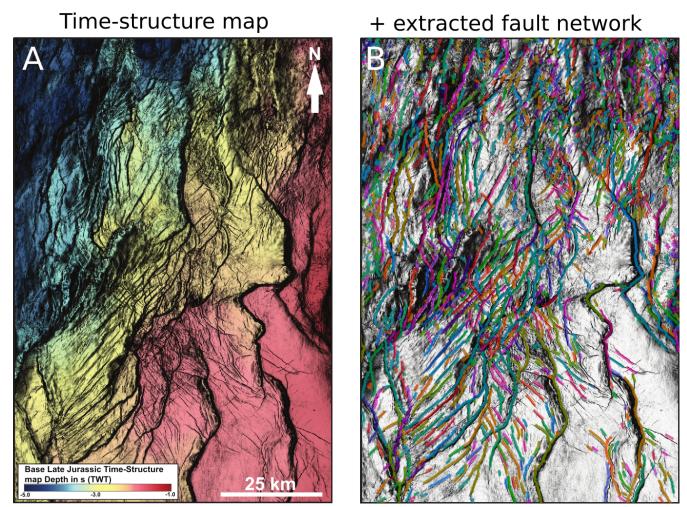


Figure 8: Comparison of A Base Late Jurassic time-structure map interpreted by Tillmans et al., (2021) and B Automaticallyextracted fault network 500 m below Base Cretaceous Unconformity. Faults are distinguished by colour.

475

480





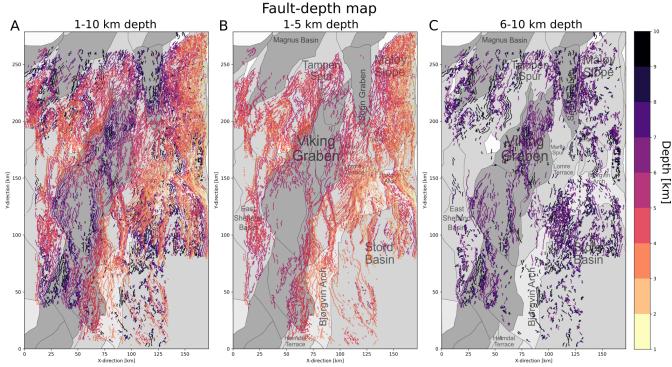


Figure 9: Fault map of the northern North Sea extracted every kilometre between 1-10 km depth (A), 1-5 km depth (B) and 6-10 km depth (C) with structural elements from the Norwegian Petroleum Directorate or NPD (2022).

500

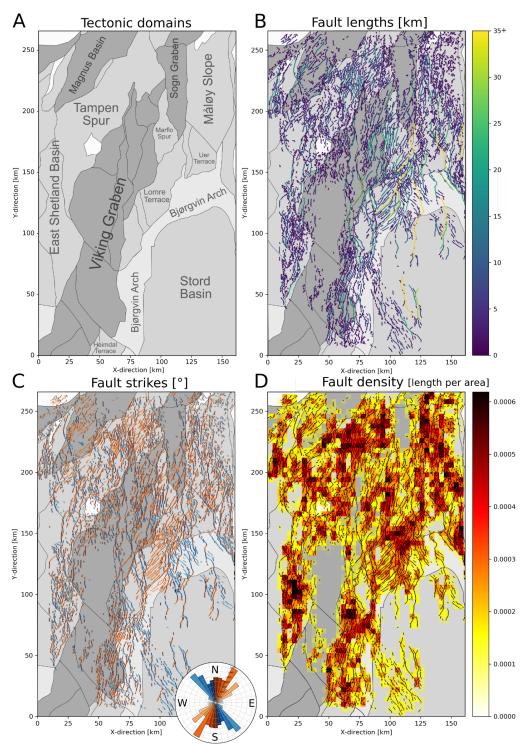
495

505

510







520 Figure 10: A Structural elements of the northern North Sea Rift (NPD, 2022) B Fault lengths (500 m below BCU) on top of structural elements. C Fault strikes (500 m below BCU) on top of structural elements with length-weighted Rose diagram. D Fault density on top of structural elements.





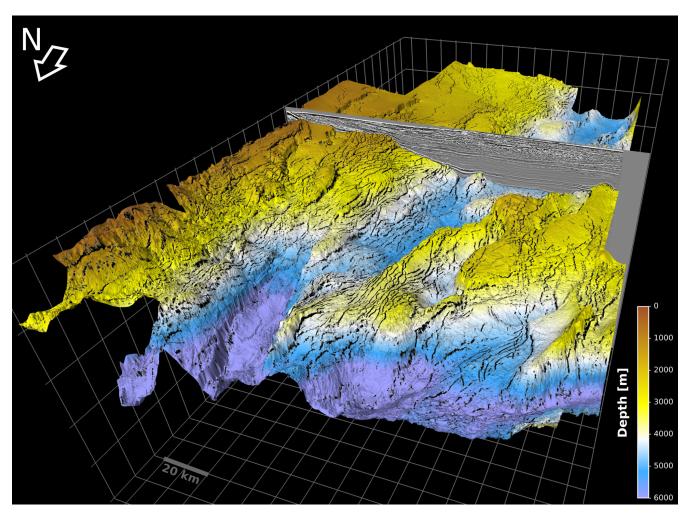


Figure 11: 3-D perspective of the northern North Sea rift showing the Base Cretaceous Unconformity overlain with faults (black) extracted from 3-D seismic reflection data with deep learning. Vertical exaggeration of 5.