Modelling the barotropic sea level in the Mediterranean Sea using data assimilation

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Abstract. This paper analyses the variability of the sea level barotropic components in the Mediterranean Sea and its reproduction with a barotropic–their reproduction using a hydrodynamic model, with and without applying data assimilation. The impact of data assimilation is considered in hindcast and forecast simulations, considering its usefulness for both reanalysis studies and short-term forecasts both in reanalysis and short-forecast simulations. We used a two-dimensional finite element barotropic model with an ensemble Kalman filter, assimilating Filter, which assimilated hourly sea-level observations data from 50 stations along all the Mediterranean coast in the Mediterranean basin. The results show a great significant improvement given by data assimilation in hindcast simulations for the reproduction of the reanalysis of the astronomical tide, surge and the surge and the barotropic total sea level, even in coastal areas far from the assimilated stations (e.g., the Eastern Mediterranean Sea). The improvement is consistent also in forecasts, especially for forecast simulations, which start from analysis states, improve as well, especially on the first day (−37% average error reduction), and in case of storm surge events with a strong presence of seiche oscillations. Since these oscillations depend and, in the surge and total sea level simulations, when seiche oscillations are triggered. Since seiches are free oscillations depending only on the initial state and not on the boundary conditions, they are corrected very effectively by data assimilation. Finally, based on observations, this article estimates we estimate their periods, which are the periods of the basin’s normal barotropic modes (seiches), both in the Adriatic Sea, where they have been extensively studied, and in the Mediterranean Sea, where the present documentation is scarce.

1 Introduction

The Mediterranean Sea and the Adriatic. Due to its historical and geopolitical importance, the Mediterranean Sea (Fig. 1) which is part of it, are among the most studied basins in the world due to their historical and geopolitical importance. However, the barotropic oscillations was extensively studied from every point of view, including the physical one. Marine circulation, the main physical, chemical and biological parameters are the subject of numerous research at various spatial and temporal scales. As regards the sea level (Pugh, 1996), the most extreme phenomena, which are mainly of a barotropic nature linked to the meteorological situation in conjunction with the astronomical tide (Cavaleri et al., 2019; Ferrarin et al., 2021), are concentrated in the northern Adriatic Sea (Fig. 1). In the rest of the Mediterranean basin, the surge and the seiches (i.e.,
free oscillations following the normal barotropic modes of the basin), are mainly studied in the Adriatic where they are more energetic and can cause flooding in coastal areas and in particular in Venice (Cavaleri et al., 2019; Ferrarin et al., 2021).

These phenomena are less frequent and the sea level variations on a longer time scale and linked to the baroclinic circulation are usually studied. In any case, barotropic sea level variations, which have a time scale of a few hours or less and a typical length of tens to hundreds of kilometres, have a certain importance throughout the Mediterranean and can be subdivided, according to their forcing, into the astronomical tide, surge and free seiche oscillations (Pugh, 1996). In the Adriatic Sea, the shallow water of the continental shelf, present in the central part and especially in the northern and northern parts, favours the growth of barotropic sea-level anomalies, whether they are of astronomical tides, surges or seiches. These sea level signals.

Indeed, the Northern Adriatic Sea is one of the Mediterranean regions (together with the Gulf of Gabes) experiencing the highest tidal oscillation (about 1 m at spring tide; Tsimplis et al., 1995). The presence, especially in autumn, of strong winds from the southeast south-easterly winds (Scirocco), which blow along the main axis of the basin, favour storm surge events in the north; events that in turn can trigger seiche oscillations of considerable intensity (Međugorac et al., 2016). Floods on the northern coasts of the Adriatic may therefore depend on the. Therefore, the floods in the northern Adriatic coasts, but also with minor intensity in the rest of the Mediterranean coasts, can consist of a superimposition of astronomical tides, surges and seiches resulting from pre-existing seiches generated by previous storm surge events.

In densely populated cities with important cultural heritage, such as Venice, Dubrovnik and Alexandria and Dubrovnik in the Adriatic basin or Alexandria in the eastern Mediterranean basin, it is essential to have a correct forecast of the sea level from nowcasting up to about five days of lead time. While the astronomical tide, given its periodic nature, is easily predictable (at least where observations are available), the surge, which depends mainly on the wind, is often affected by errors, mostly due to the incorrect representation of the meteorological forcing (Barbariol et al., 2022). Consequently, the seiche oscillations, resulting from an initial storm surge event, are also incorrect and the error propagates in the following days with the same period and damping as those of the triggered barotropic mode. The forecast error can be reduced by improving the meteorological forcings, as regards the surge component, and improving the initial state regarding the seiche oscillations (Bajo et al., 2019). The use of data assimilation (DA) techniques (Kalnay, 2002; Evensen, 2009a; Carrassi et al., 2018), which aims to reduce the error of the initial state from which to start for a forecast simulation, should be able to reduce both the error on the seiche oscillations and, in the short term, errors in the surge, due to underestimates of the wind, in advance to alert the population and the authorities of possible flooding. In this time window, tides and surges are the main components influencing the sea level variations, since sea-level variations due to the ease of events ongoing at the time of the forecast (Bajo et al., 2017, 2019).

Rivers’ run-off, which could be increased by a storm, are negligible in the Mediterranean Sea. Regarding the situation outside the Adriatic Sea, the barotropic components of the sea level are much weaker. However, the western Mediterranean basin is subject to strong Mistral events (north-west wind) and, in the southern part of the Mediterranean, small but intense cyclones with tropical dynamics (called medicanes) can sometimes form. These extreme weather events have already caused flooding in the past even in areas traditionally not affected by these events (Scicchitano et al., 2021).

Considering the seiche oscillations, although they are less energetic than in the Adriatic Sea, their correct reproduction improves the reproduction of the total sea level. These oscillations, as mentioned earlier, surge events can trigger seiches.
These oscillations have periods determined by the barotropic modes of the basin. While the modes of the Adriatic Sea, being very energetic, have been well studied, those of the Mediterranean Sea are little studied are little known and, to our knowledge, there is only one scientific work with the application of a simple barotropic model, which predicts the form and period of the most important modes (Schwab and Rao, 1983). Therefore, their study in the Mediterranean Sea has scientific significance, but although a correct reproduction of seiche oscillations is necessary mostly in the Adriatic, to correctly predict extreme events, their correct reproduction is still necessary to reproduce the sea level accurately. Finally, it should be remembered that these improves the prediction of the total level also in the rest of the Mediterranean. Furthermore, the barotropic modes of oscillation of a basin can also be triggered by extremely violent events much more extreme phenomena, such as tsunamis, tsunami waves.

The use of the DA is very useful not only in the forecast, but also in hindcast, allowing obtaining reanalysis of the total sea level, or some of its components, much more accurate than those obtainable without. In particular, the calculation of the harmonic components of the astronomical tide is usually possible in areas where there is a tide gauge. In areas where there are no measurements, one is forced to calculate the components based on model data which can be inaccurate. The DA can therefore have a positive impact both in the reproduction of the astronomical tide, locally, and in the study of its spatial structure. Similarly, from the reanalysis of predictability of the various components of sea level depends on the predictability of the forcings that trigger them. The astronomical tide, due to its periodic nature, can be predicted with good accuracy where sea-level in-situ observations are available. However, where these observations lack, the tide must be computed by altimeter data (Birol et al., 2017) or by hydrodynamic models (using good bathymetry data). As regards the surge, in case of severe weather conditions, most of the sea-level error is due to this part. The storm surge has a non-periodic nature, depending on the surface wind and atmospheric pressure, and, due to wrong meteorological forcing, the error can be consistent (Barbariol et al., 2022). Surges can trigger seiches, which propagate the following days carrying the initial error of the surge, with different periods and decay times depending on the excited barotropic modes.

To reduce these errors, data assimilation (DA) procedures can be used. DA aims to reduce the error of the state of a dynamic model at a fixed time by exploiting the available observations of quantities correlated to the model’s variables (Kalnay, 2002; Evensen, 2009a,b). DA can be used both to improve the forecast, providing an accurate initial state, which is called the analysis state or to produce several analysis states to simulate past periods with small errors (reanalysis simulation). The reanalysis simulations, in which the best available forcings and boundary conditions and the best set of observations for DA are used, are much more accurate than analogous simulations made without the use of the DA (here referred to as hindcast simulations).

In this work, we will analyse the impact of DA in the reproduction of tides, surges and the total barotropic sea level composed of these components, both in reanalysis and in forecast simulations, with particular attention to the presence of seiches in the surge component. It is possible to extract spatial information on its propagation and the shape of the seiche oscillations.

This paper analyses the model reproduction of the various components of the marine barotropic level described up to now, using a finite element hydrodynamic model. The impact of the assimilation of...
The amplitudes and phases of the main components and to make tide forecasts in arbitrary locations. Therefore, we will not consider forecast simulations of the tide. The reanalysis of the surge and the total barotropic sea level, is useful mainly as a coastal product, to produce past climatology of extreme events. In the Mediterranean Sea, where the coasts have a large extension compared to the basin’s area and the weather is strongly influenced by the orography, the hindcast products, without DA, often suffer from underestimation issues. We will test if DA can reduce these errors in the reanalysis simulations.

The second use of DA that we consider in this paper is for the improvement of forecast simulations, which are executed with forecast boundary and forcing conditions. DA is used in a one-day period before each daily forecast, to create a final state of analysis from which to start the forecast simulation. In this case, the DA improvement is due to the fact that the initial analysis state has a lower error than the one without DA (background state), but the error of the forecast forcing and boundary condition cannot be corrected. The simulations are executed with a finite element hydrodynamic model, assimilating 50 sea-level coastal stations, done through an ensemble Kalman filter, is also analysed. The results are analysed and discussed both in forecast and hindcast (reanalysis in the case of the use of the DA). A coastal stations using an ensemble Kalman filter. We run the simulations in a two-month simulation period was chosen period, November and December 2019, in which one of the most extreme storm surge events ever recorded in Venice was recorded and, after this in December, a very energetic event of seiche oscillations followed. This period is therefore very particular from a meteorological-marine point of view, not only in the Adriatic Sea but in the entire Mediterranean basin in November and very energetic seiche oscillations were recorded in December.

Below we report first the methodology followed. In the following sections, we report the methodology, with a description of the hydrodynamic model used (Section 2.1), of the observations and their observation collection and processing (Section 2.2.1) and the DA method and setup (Section 2.3), ending with a brief description of the simulations. The section ends with a description of all the simulations that we performed (Section 2.4). Then follows the calibration, we expose the results of the DA calibration (Section 3.1), the model results in hindcast mode hindcast/reanalysis simulations (Section 3.2) and in forecast mode the forecast simulations (Section 3.3), and a part. The second part of Section 3.3 is dedicated to the seiche oscillations (Section 3.3.1) description and reproduction in the forecast mode of the November and December extreme events described before. Finally, the discussion (Section 4) and conclusions (Section 5) are reported follow.

2 Methods

2.1 The hydrodynamic model

The hydrodynamic model we use is called SHYFEM (System of HydrodYnamic Finite Element Module) and was created at the CNR in Venice (Umgiesser and Bergamasco, 1993), where it is largely developed continuously. Its code is available under an open-source license and freely downloadable from the Web (https://github.com/SHYFEM-model/shyfem). SHYFEM is composed of a hydrodynamic core that solves the shallow water equations with the finite element technique and with a semi-implicit time-stepping algorithm, which allows a remarkable speed of execution. Various terms in the equations can be turned on or off, such as momentum advection terms, Coriolis terms, baroclinic terms of density gradients, and tidal potential. The
model can be used in two or three-dimensional modes and various formulations of bottom stress and wind stress are available. Finally, the model can be coupled to various modules or models (e.g., waves, Lagrangian, ecological).

In this application, we use a two-dimensional barotropic formulation given by the following equations:

\[
\begin{align*}
\frac{dU}{dt} - fV &= -H \left( \frac{g}{\rho_w} \frac{\partial \zeta}{\partial x} + \frac{1}{\rho_w} \frac{\partial p_a}{\partial x} \right) + A_H \nabla^2 U + \frac{1}{\rho_w} (\tau_{wx} - \tau_{bx}) \\
\frac{dV}{dt} + fU &= -H \left( \frac{g}{\rho_w} \frac{\partial \zeta}{\partial y} + \frac{1}{\rho_w} \frac{\partial p_a}{\partial y} \right) + A_H \nabla^2 V + \frac{1}{\rho_w} (\tau_{wy} - \tau_{by}) \\
\frac{\partial \zeta}{\partial t} + \frac{\partial U}{\partial x} + \frac{\partial V}{\partial y} &= 0,
\end{align*}
\]

where the independent variables are the time, \( t \), and the spatial variables \( x \) and \( y \). \( U(x, y, t) \) and \( V(x, y, t) \) are the transports along \( x \) and \( y \), \( f(y) \) is the Coriolis coefficient, \( H(x, y, t) \) is the sum of the sea depth with \( \zeta(x, y, t) \), which is the variable level with respect to the resting state; \( g \) is the gravitational acceleration, \( \rho_w \) is the average density of seawater, \( p_a(x, y, t) \) is the atmospheric pressure at sea level and \( A_H \) is the horizontal coefficient of turbulent viscosity, formulated with Smagorinsky (1963), using a dimensionless coefficient equal to 0.2; while \( \nabla^2 [\cdot] \) is the two-dimensional Laplacian operator. \( \tau_{bx}(x, y, t) \) and \( \tau_{by}(x, y, t) \) are the components of the stress at the bottom, expressed with a linear-quadratic formulation with coefficient.
$0.0025$ (Bajo et al., 2019); $\tau_{w,x}(x,y,t)$ and $\tau_{w,y}(x,y,t)$ are the components of wind stress, expressed with the formulation proposed by Hersbach (2011) and with a Charnock coefficient equal to $0.02$.

Furthermore, for the simulations that calculate the tidal level or the total sea level, the terms of tidal potential are also active and four semi-diurnal components ($M_2$, $S_2$, $N_2$ and $K_2$) and four diurnal components ($K_1$, $O_1$, $Q_1$ and $P_1$) are calculated. This formulation or very similar formulations for SHYFEM have been used in the past with success in many works on the storm surge (Bajo et al., 2017, 2019; Cavaleri et al., 2019; Ferrarin et al., 2021) or the total sea level or the tide (Ferrarin et al., 2013, 2018).

The model is applied on a mesh of the Mediterranean Sea, which extends into the Atlantic Ocean up to about $7^\circ$ W and has about $163,000$ triangular elements. The size of the elements is variable, with a gradually greater resolution from the open sea (element side length $\sim 12$ km), to the coasts (element side length $\sim 500$ m), as shown in Fig. 1. The bathymetry derives from the 2020 dataset of the European Marine Observation and Data Network (https://www.emodnet-bathymetry.eu/), which was bilinearly interpolated on the mesh.

This model has already been used successfully in the past, with similar configurations, in many scientific works and is currently used in several operational systems for sea level prediction. For example, the most extreme storm surge events that occurred in 1966, 2018 and 2019 were simulated in Roland et al. (2009), Cavaleri et al. (2019) and Ferrarin et al. (2021). Various operational versions of the model with similar configurations have been used for over fifteen years at the high tide forecasting and warning centre (CP$S$M) in Venice (Bajo et al., 2007; Bajo and Umgiesser, 2010; Bajo, 2020) and at the Italian Institute for Environmental Protection and Research (ISPRA), where a system similar to that here described will be installed in the next months (https://www.venezia.isprambiente.it/ispra/modellistica). SHYFEM, with and old version of DA, was also used to assess the impact of altimeter data on storm surge forecasting (Bajo et al., 2017), and with a more recent DA method to study a particular seiche event (Bajo et al., 2019). As regards the reproduction of the astronomical tide in the Mediterranean (and Black Sea), a first work has been successfully completed (Ferrarin et al., 2018). Finally, there are numerous works performed with other models in barotropic configuration, such as the one used here, for the study and prediction of surges, tides and sea level variations given by these components (see e.g., Flowerdew et al., 2010; Bertin et al., 2014; Fernández-Montblanc et al., 2019; Horsburgh).

### 2.1.1 Surface forcing and lateral boundary condition

The simulations use, as forcing at the surface, 10-m wind and mean sea level pressure hourly fields provided by the BOLAM atmospheric model (Mariani et al., 2015), which is a hydrostatic model-hydrostatic and runs at 8 km ; with hourly fields, of horizontal resolution. The model is nested in the IFS ECMWF operational model (ECMWF Integrated Forecasting System (IFS - https://www.ecmwf.int/en/publications/ifs-documentation). For hindcast In the hindcast/reanalysis simulations, the surface forcing fields are made by the first forecast days chained together are used, while each daily forecast simulation uses , while the forecast simulations, which are daily, use the entire forecast up to five days ahead. Lateral.

The lateral boundary conditions are closed everywhere except in the western border in the Atlantic Ocean, near Gibraltar, where Dirichlet conditions are imposed, with the sea level imposed and water transports being free. For the open boundary
sea level...is imposed and the water transports are free (Dirichlet conditions). The open boundary was chosen outside the Mediterranean Sea to reduce the associated error and different sea level quantities are used, depending on the simulation type. For the simulations computing the total sea level we used the E.U. Copernicus Marine Service Information (CMEMS). The total sea level is used for total sea level simulations, while the variable Sea Surface Height (SSH) by the Mediterranean Sea Physical Analysis and Forecast system (Clementi et al., 2021, https://doi.org/10.25423/CMCC/MEDSEA_ANALYSISFORECAST_PHY_006_013_EAS7), running at the Copernicus Monitoring Environment Marine Service (CMEMS). For the simulations computing only the surge, we used the "de-tided sea level, called Non-Tidal Residual (NTR), is used in the surge simulations. The simulations with the astronomical tide are forced at the boundary of Gibraltar with the tidal signal derived from the same Copernicus model.

Hereafter we will refer with NTR to the residual level obtained by removing the tide from the total water level. The NTR is mainly made up of a meteorological component, forced by wind and pressure, called surge, and by a further possible spurious signal due to seasonal and non-seasonal baroclinic forcing, which is generally at low frequency (in DA part of this signal is removed with the MDT correction explained later). The NTR represents our best estimate of the surge component, calculated from the model. "SSH, available in the same dataset and that we will call Non-Tidal Residual (NTR). This quantity is the residual part of the harmonic analysis of the SSH. Finally, the simulations computing only the tide use the difference between these two quantities (SSH-NTR). The SSH and the NTR of the CMEMS model can contain a baroclinic part, which cannot be filtered, but it is varying at a lower frequency.

The simulations with the DA use the same forcings and boundary conditions as the deterministic simulations (without the DA) but these are perturbed to obtain an ensemble of simulations. This procedure in ensemble DA methods, the independence and the spread of the members improved by perturbing the forcings and the boundary conditions. This was done for the DA simulations and the method is described in Section 2.3.

2.2 **In-situ observations**

2.2.1 **In-situ data**

Sea-level observations were retrieved from the European Joint Research Center database (https://data.jrc.ec.europa.eu/). As shown in Fig. 1, tide gauges are concentrated in the western and central Mediterranean Sea, mostly along the Spanish, French and Italian coasts, while on the northern African coast there is only one station (Melilla) and few stations are present in the eastern Mediterranean Sea. The Adriatic Sea has stations only along the Italian coast and not on the eastern coast, but they are still quite numerous. The stations in the Mediterranean Sea were divided into 50 stations to be assimilated and 13 for validation (Tab. A1). Data is recorded every 10 minutes in the period of October-December 2019. We processed it with the SELENE quality check software (https://puertos-del-estado-medio-fisico.github.io/SELENE/; Pérez et al., 2013) for spikes and outliers detection, stability test, date and time control, flagging and interpolation of short gaps. Subsequently, the quality-checked data were elaborated with the Python binding of UTide (https://github.com/wesleybowman/UTide; http://www.po.gso.uri.edu/~codiga/utide/utide.htm), based on the least squares fitting, to separate the tidal periodic part from the non-periodic part (NTR) in the total sea level. We kept the eight most energetic tidal constituents in the harmonic analysis ($M_2$, $S_2$, $N_2$, $K_2$, $K_1$, $O_1$, $P_1$, $S_1$).
which are the most important in the Mediterranean Sea (Ferrarin et al., 2018). The NTR was further processed by applying a 2-hour moving average, to remove high-frequency signals. The harmonic analysis was not possible for stations 62 and 63, due to a lack of continuous data. Therefore, these stations were used only for the validation of the total sea level.

The observations may have different reference datum according to the monitoring network to which they belong. Therefore, in order to have no bias errors in DA, the measurements were referred to the Mediterranean Dynamic Topography (MDT) of the model, which can be defined as the mean dynamic topography (MDT) of the model (Vidard et al., 2009; Byrne et al., 2021). The MDT of the model is given only by the barotropic terms present in the equations and lacks the baroclinic part due to the temperature and salinity gradients. A similar approach is used in Byrne et al. (2021).

### 2.2.2 Altimeter data

Altimeter data are difficult to use to study the surge even if some attempts were made (Bajo et al., 2017). Since high-frequency signals are badly sampled, usually this part is removed using a barotropic two-dimensional model (Carrère and Lyard, 2003). Normally, in the altimeter products, also the tidal part is removed with a similar model (Lyard et al., 2021). However, since the altimeters measure the sea level in the same locations at every cycle (about 10 days), it is possible to extract the tidal part from the signal.

Recently, the amplitudes and phases of the main harmonic components along the altimeter tracks are available on the AVISO website (https://doi.org/10.6096/CTOH_X-TRACK_Tidal_2018_01). The X-TRACK along-track tidal constants were computed via harmonic analysis of the sea level anomalies for long time series missions (Birol et al., 2017). We used the X-TRACK (based on Topex/Poseidon + Jason-1 + Jason-2) eight most energetic tidal constituents over the Mediterranean Sea (see the list in the previous section) to compute the astronomical tide for the period of our simulations. These tide time series were used for the validation of the tidal reanalysis simulation, as described in Section 3.2.1.

### 2.3 The data assimilation system

In this section and the following ones, we will use some terminologies and concepts typical of the DA, for an introduction to these concepts and the various techniques we recommend reading Carrassi et al. (2018).

The code used for the DA is based on the routines developed and described in Evensen (2003, 2004) and available at https://github.com/geirev/EnKF_analysis. The routines have been adapted and extended to be used by-in the SHYFEM model, allowing the use of different DA techniques, such as the Ensemble Kalman Filter (EnKF) and the Ensemble Square Root Filter (EnSRF), with the chance of using different numerical schemes (https://github.com/marcobj/shyfem). Furthermore, various routines have been created to perturb the forcing and boundary conditions obtaining ensembles of arbitrary size. In this work, we used an EnKF technique, the EnKF with the correction described in Evensen (2004) to avoid the loss of rank in the observation covariance matrix (Kepert, 2004).
As described in Section 2.4, each set-up was decided after numerous test simulations. It was therefore decided to use an ensemble of 81 members (80 perturbed + 1 control) and not to use local analysis (Carrassi et al., 2018). The system uses adaptive inflation (Evensen, 2009a), to avoid narrowing of the ensemble spread, and the observations are considered independent (in fact they come from different stations) and have an error set to 2 cm. Therefore, the observation covariances are set to zero, while the variances are positive and equal in each station. In order to discard innovations that are too high, a simple technique, which checks the values of the variances of the background matrices and the observations, is used (Järvinen and Undén, 1997; Storto, 2016).

Finally, to dampen shocks in the analysis solution near the lateral boundary conditions, in Gibraltar open boundary in the Atlantic ocean, the analysis solution is relaxed to the background one, gradually approaching the boundary. The two states, background and analysis, are weighted through a Gaspari-Cohn (GC) function (Gaspari and Cohn, 1999), with a radius of about 250 km starting from the open boundary nodes prescribing a radius from the nodes of the lateral open boundary. In each node we have the following solution of the whole computational grid the values of the model states after an analysis step are:

\[ A_a^*(x, y) = A_b(x, y)f(x, y) + (1 - f(x, y))A_a^*(x, y), \]  

(2)

where \( x \) and \( y \) define the position of the node in the grid, \( A_b \) is the matrix of the background states, \( A_a^* - A_a \) is that of the analysis states not corrected, \( A_a \) is the one corrected and \( f \) is the function of Gaspari-Cohn GC function, equal to 1 in the open boundary nodes. Since the GC function goes to zero at a distance greater than twice the radius, the solution at greater distances is identical to that of the analysis, while near the boundary is mainly forced by the boundary condition and not affected by the analysis increments. The values the EnKF parameters here described were decided after running several calibration tests, which will be exposed in Section 2.4.

The ensemble of 81 members.

2.3.1 The perturbation methods

The ensemble in all the DA simulations performed was created by perturbing the initial state, the forcing and boundary conditions and a few some model parameters. The perturbation of the initial state is performed only for the levels sea level (variable \( \zeta \) in the eqs. 1), with a technique similar to that for used for the atmospheric pressure (described later), while the water transport is not perturbed. However, for the forecast, this is used only for the first simulation, while the following ones start from an ensemble of states saved from the simulations of transports are not perturbed (barotropic transports reach a dynamic equilibrium quickly depending on the sea level). In the forecast simulations, the initial state is perturbed only in the first daily simulation. In contrast, the following daily simulations start all from the states saved the previous day. Even for hindcast of each forecast.

For the reanalysis simulations, the initial state perturbation is of little importance, perturbation of the initial state is not very important, as the simulation lasts simulations last two months and the influence of the forcing and boundary conditions, as well as the assimilated observations, are far more important. The perturbations of the after some days. The forcing and boundary conditions are maintained perturbed for the entire duration of the DA. The forecast simulations perform a day of assimilation.
and then start from the average analysis state and use the simulations, both in the reanalysis simulations and in the forecast simulations. However, the first ones last two months, while the DA in the daily forecast simulations last only one day and then five days of forecast follow, starting from the analysis ensemble mean and using unperturbed forcings and boundary conditions.

The perturbations are calculated so that in each spatial point the average is, for a scalar physical variable, the mean of the perturbed values should be approximately equal to the non-perturbed value (no bias) and the standard deviation is equal to the estimated error; furthermore, the perturbations must have belong to a Gaussian distribution. Perturbing We used this method for the conditions at the lateral boundary is not very complicated, we have applied open boundary, with the same perturbations to all the nodes of the open boundary. As for the atmospheric fields, their perturbation in each node.

We used this kind of perturbation also for the value of the drag coefficient in the bottom stress, with a distribution centre in the unperturbed value (0.0025) and a standard deviation of 0.0005. In the DA simulations with the tidal forcing, a calibration factor for the loading tide is perturbed as well, with a mean value of 6.0 e-05 and a standard deviation of 1.e-05 (parameter \( \text{tidec} \) in SHYFEM).

Perturbing the two-dimensional atmospheric fields is more complex because, in addition to satisfying the previous condition, there must be. We still impose the same condition for the mean and the standard deviation at each point, but the perturbations must have a spatial correlation and a physical coherence between the variables (wind and pressure) the atmospheric pressure perturbations should be linked to the wind perturbations. We therefore first perturbed the atmospheric pressure field, through a technique to generate two-dimensional pseudo-random fields (Evensen, 1994, 2003), imposing a decorrelation length of about 400 km and a standard deviation of 3.5 hPa. From these two-dimensional waves, These values, slightly different from those used in Sakov et al. (2012), were found empirically and they produce perturbations at a sub-synoptic scale, with a similar size to the typical Mediterranean cyclones (Ferrarin et al., 2021). From these fields of pressure perturbations, we calculated the corresponding perturbations for the velocity components. If the pressure perturbation in one point is \( \delta P \), the perturbations for the wind components, in geostrophic equilibrium, are:

\[
\begin{align*}
\delta u &= -\frac{\delta P}{\partial y} \frac{1}{\rho_a f} \\
\delta v &= \frac{\delta P}{\partial x} \frac{1}{\rho_a f}.
\end{align*}
\]

Using these perturbation fields to be applied to the unperturbed fields of wind and pressure at an instant \( t \), we obtain perturbed fields with a physical coherence.

Again for the atmospheric fields, in addition to this kind of perturbation, a temporal perturbation has also been introduced in which, from a field at time \( t \), an ensemble of equal fields is generated but with reference time \( t + dt_n \), where \( dt_n \) are time perturbations belonging to a Gaussian distribution as well. Other perturbations, again with a Gaussian distribution, have been introduced for the bottom stress and, in the simulations with the tidal potential, for the calibration coefficient of the loading tide.

Finally, as regards the forcing and perturbations of the forcing and the boundary conditions that vary over time, the errors error at a given instant \( t_1 \) must be related to the errors at the instant of the next field, at time correlated to the error at the next instant, \( t_2 \). This type of error, or noise, which is defined as "red noise", is applied and is implemented by calculating a weight
dependent on the time interval between the two fields and **on-by defining** a decay time:

\[ \alpha = 1 - \frac{t_2 - t_1}{\tau}, \]  

where \( \tau \) is the decay time. The perturbation \( \xi_2 \), at time \( t_2 \), becomes a linear combination of the perturbation \( \xi_1 \), at time \( t_1 \), and the newly calculated perturbation \( \xi_2^* \):

\[ \xi_2 = \alpha \xi_1 + \sqrt{1 - \alpha^2} \xi_2^*. \]  

**2.4 Results’ production and post-processing**

In this study, we performed simulations with and without DA, in hindcast and forecast modes. The hindcast simulations extend **Using the tools described above, we ran numerous tide, surge and total sea level simulations.** In the period from the beginning of November to the end of December 2019 we run hindcast simulations, with continuous forcing and boundary conditions, as described in Section 2.1.1, without DA, and were performed considering the total sea level, the surge component and the astronomical component. The hindcast simulations with DA, which can be defined reanalysis simulations, \*the same type of simulations, but using DA (reanalysis simulations). Then, we run daily forecast simulations, starting from initial states made without DA (background states), and initial states made using DA (analysis ensemble means).

The reanalysis simulations assimilate the data from the 50 stations every hour, throughout the two months of simulation. From the ensemble of reanalysis states, the average analysis ensemble mean is calculated, as the best estimate of the real state of the physical system, and is used in the analysis examination of the results.

The forecast simulations were performed by calculating the total sea level and the meteorological component, the surge. The simulations of the astronomical tide have not been carried out, as they are not very useful since there is always the possibility, even for future periods, to calculate pseudo-observations in stations where the harmonic constants are known and use them to perform a simulation with DA.

The forecast simulations were performed identically to In running the forecast simulations we used the same settings as those that would be performed by an operational model used in an operational context. The period is the same as considered in the hindcast November and December 2019, and reanalysis simulations. However, the simulations are performed daily and each one is composed of a hindcast day and five forecast days of which, for (no DA) or analysis (DA) simulation of one day and a five-day forecast simulation. For the sake of brevity, we will show the results for of the first three days. The forecast simulations with DA assimilate the data from the 50 stations, every hour, in the 24 hours of the hindcast period hours preceding the forecast. From the final average analysis state, saved states, the analysis states, we computed the analysis ensemble mean, each day at 00 UTC, each day, the forecast simulation is started, which lasts 5 days. In addition, the final analysis states of the entire ensemble. From this state the five-day forecast starts and the analysis states are saved to be used by the simulation of the next day, as initial states in the next day’s simulation. In this way, the DA always restarts from a state of analysis and is equivalent starts from analysis states and is similar to the cycle performed in hindcast reanalysis, except for the perturbation of the forcing and boundary conditions, which is redone every day.
To analyse the results, each daily forecast simulation was divided into five parts and each part was chained with the corresponding one of the previous and following days. In this way, continuous results are obtained for each forecast day, which 1-day, 2-day and 3-day lead times and can be directly compared with the measurements in the two months considered observations. The forecast timeline is shown in Fig. 2 and is the same for the simulations without and with DA.

To compare the results with the observations, we calculated the standard deviations of the model and observed data, the correlation between them and the Centered Root Mean Squared Error (CRMSE). The standard deviations and CRMSEs were normalised to the standard deviation of the observations at each station and represented by Taylor diagrams (Taylor, 2001). Bias error plots were also calculated, in which bias is calculated as the mean of the differences between the modelled and observed values; while the CRMSE represented in the same plots is not normalised. For the sake of clarity, we reported the various simulations in Tab. 1 with identification labels, which we will use in the following sections.

Regarding the spectral analysis, we used the NTR and the surge calculated by the model for December 2019, in which there is a strong presence of seiche signals, were used. The power spectral density was estimated with the Welch method (Welch, 1967), dividing the period into 8-day windows with 50% overlap. The fast Fourier transform length is rounded up to the nearest integer power of 2 by zero padding.

3 Results

3.1 Calibration of the data assimilation

Before running the definitive simulations, which were final simulations used to produce the results, we carried out numerous experiments to determine the best parameters of the DA. The results of these tests (partially shown in this paper), showed how in this study case, the EnKF gives better results than the EnSRF and that it is not convenient to use data localisation techniques.
(local analysis) values of some DA parameters. The parameters that have been varied are the assimilation scheme (EnKF, EnSRF), the error of the observations (we tested from 1 cm to 3 cm), the radius in eq. 2, the radius in the domain localisation and the number of the ensemble members. Although in fact, the localisation in most cases brings advantages, brings advantages in many applications, in our case the observations available are mainly arranged only on available observations are mainly located in the northern side of the computational domain. This implies that to obtain a spatially uniform analysis correction, a very wide large localisation radius should be used, reaching the other end to reach the other border of the basin.

Furthermore, the correlation radius of a variable (the sea level barotropic sea level perturbations in our case) between a point and its neighbours increases with the speed of propagation of the perturbations of this variable which, in the case of barotropic perturbations, is high—its propagation speed. In the present case, the propagation speed is that of shallow water waves (in the western basin with Mediterranean basin, considering an average depth of about 2000 m there is a speed of, the speed is 140 m/s). To avoid spurious correlations, without the use of For these considerations and after having carried out various tests varying the radius of the local analysis, we have increased the number of members of the ensemble. However, decided not to use it and to increase the system remains quite fast, considering that these are two-dimensional barotropic simulations. We then performed, in hindcast mode, some DA tests by varying the number of members of the ensemble members. A high number of ensemble members avoids problems of spurious correlations and cross-correlations. Moreover, since the simulations are extremely fast and having a workstation with a high number of cores, the execution time has not been much affected. To determine the minimum number of ensemble members to obtain good results without increasing too much the computational load, we performed various total sea level reanalysis simulations. In Fig. 3 we report the Centered-Centred Root Mean Squared Error (CRMSE) of the total sea level analysis ensemble mean, averaged in the validation stations, using a different number of members of the ensemble-ensemble members. The error is reduced from 9.3 cm, in the case without DA, to 3.6 cm using
Figure 3. Performance of the data assimilation, in terms of CRMSE and correlation coefficient, as a function of the number of ensemble members. The red contour highlights the results of the simulation without data assimilation.

101 members, and the correlation increases from 0.75 to 0.95. Since the error pattern is regular and asymptotic, we decided to use 81 members.

Therefore to conclude, the final configuration uses the EnKF with an observation error of 2 cm, a radius in eq. 2 of 250 km, no localisation techniques and 81 members in the ensemble.

3.2 Hindcast/reanalysis simulations

We will analyse first the results in hindcast of the hindcast and reanalysis simulations, for the astronomical tide, the surge and the total sea level. In Fig. 4, the first diagram on the left shows the astronomical tide comparison, in which the tide calculated by the model is compared with that model results, without (hindcast) and with (reanalysis) DA, are compared with the tide calculated by the harmonic constants \((TH, TR_A)\). The results are quite good even without DA in almost all stations, with a certain tendency to overestimate the signal amplitude (higher standard deviation). Station 60 is an exception, where the results in hindcast are poor, probably due to its position in the Aegean Sea, in a morphologically complex area. The results with DA are definitely very good for all the validation stations, reaching almost perfect agreement (correlation about 0.99), with a small deterioration in station 60, which however improves and still achieves a more than good accuracy (CRMSE from 4 cm to 1 cm).

The central diagram shows the reproduction of the surge signal, compared with the NTR extracted from the observations \((SH, SR_A)\). In this case, the distribution of the stations in the deterministic simulation is sparse and nothing particular can be deduced, except that also for the surge-Taylor diagram is sparse for the deterministic simulation and the station 60 is still the
Figure 4. Normalised Taylor diagrams of the hindcast and reanalysis simulations. The deterministic simulations (green diamonds) compared to DA simulations (black squares), for the astronomical tide (left), the surge (centre) and the total sea level (right). The red dot indicates the perfect agreement.

worst. The simulation with DA improves considerably reanalysis simulation improves considerably the surge reproduction in all the stations, arriving to have a very concentrated with a very focused distribution even if not like that of the astronomical tide. For example, in station 60, which is the worst, the CRMSE reduced from 8 cm to 3 cm.

Finally, as regards the simulation the simulations with the total sea level, the quality of the simulations with and without DA is very (ZH, ZRA) have a quality similar to that of the simulations with the surge surge simulations. Some stations are even better, perhaps thanks to the good accuracy with which the model calculates the astronomical tide (in station 60 in the reproduction of the tidal signal. As for the surge simulations, the CRMSE goes from 8 cm in the hindcast simulation to 3 cm in the reanalysis.

In the case of the total sea level, the comparison was also made for we made a comparison also for the stations 62 and 63 which, as previously mentioned, are the only ones in the eastern basin and are at least a thousand kilometres away from the first nearest assimilated station. It is interesting to note that these stations also have a consistent improvement; the CRMSE goes from 9.6 cm to 4 cm for station 62 and from 10.9 cm to 5.7 cm for station 63. This improvement indicates the good quality of is probably due to correct correlations in the background covariance matrix, even for model variables that are very distant from each other, obtained thanks to the high number and good independence of the ensemble members in the EnKF.

3.2.1 Validation of tide with altimeter data

Unlike coastal stations, altimeter data allows the investigation of the astronomical tide in the open sea, far from the coast. The amplitudes and phases of the eight most energetic tidal constants retrieved from the altimetric data were used to calculate the tide oscillations at each point of the satellite tracks in the Mediterranean Sea. To compare this data with the model data, the sea levels from the TH and TRA simulations were extracted at the same coordinates and the CRMSE were calculated. Fig. 5 shows the along-track differences in the CRMSE (i.e., CRMSETRA - CRMSETH). The values are negative almost everywhere.
clearly showing a marked improvement of the DA in reproducing the tidal levels over the whole basin with a reduction of the CRMSE up to 20 cm near the Gibraltar Strait, in the Gulf of Gabes and in the northern Adriatic Sea. It is worth noting that, the DA effect is not local, as the areas in which there is a greater improvement do not correspond totally to those with more assimilated stations (e.g., the eastern Mediterranean Sea). Averaging the CRMSE over the whole basin, we obtain a mean value of 11.6 cm for the simulation without DA ($TH$) and a value of 4.3 cm for the simulation with DA ($TR_A$).

### 3.3 Forecast simulations

In this section we analyse the forecast results for the surge component and for the total sea level. In Fig. 6 the Taylor diagrams are shown for the first, second and third forecast days, both for the data of the model without DA and for those with DA, in all validation stations. The results are starting from the analysis ensemble mean. In the results relative to the surge simulations - The ($SF, SF_A$), the effect of the DA on the first forecast day is evident and the distribution is similar, slightly worse, to that obtained in hindcast. Each validation station improves significantly, including the hindcast and reanalysis simulations in Fig. 4, central panel. The data improves in each validation station, including station 60, which does not have many assimilated stations nearby, is far from the nearest assimilated station. Unfortunately, the data in stations 61 and 62 cannot be used in the validation of the surge simulations, as it was not possible to perform the harmonic analysis to subtract the tide, due to the few available data.

**Figure 5.** CRMSE differences (ass - det) for the tidal level computed using the altimeter X-TRACK along-track tidal constants retrieved from AVISO.
Figure 6. Normalised Taylor diagrams of the forecast simulations with the surge. The deterministic simulations (green diamonds) compared to DA simulations (black squares), for the first (left), the second (centre) and the third (right) -day forecast. The red dot indicates the perfect agreement.

The improvement is reduced smaller on the second day forecast, while on the third day is almost nil or slightly worse, worsening slightly in some stations, although not significantly. This behaviour is due to the fact that the initial state of the system gradually loses its importance as the forecast moves temporally away from it, and so does the decrease in its error as well as the error correction. The forecast without DA has a larger initial state error in the initial state, which mostly counts on the first and second forecast days of forecast.

In Fig. 7 we can see show the bias error for the surge simulations. This graph was not made for the hindcast simulations, as and reanalysis simulations as, in that case, the bias is almost null. The figure shows that the DA improves the results, especially on the first forecast day, then gives a the correction is still positive but weaker correction on the second day, while on the third day the DA slightly worsens the model data original forecast, in agreement with what has been seen for in the Taylor diagrams. The worsening is in any case contained and relates to the third forecast day, which in an operational context, is of secondary importance compared to the first and second forecast days. Still, observing Fig. 7, it can be seen how station 57 deviates from the others, with a much greater bias and CRMSE than the other stations. This is due to the position of this station, in the upper northern Adriatic, where the surge events signals and the associated seiche oscillations have much greater intensity are larger than in the rest of the Mediterranean Sea. However, precisely for this reason, and since there are numerous good-quality stations in the Adriatic Sea, the effect of DA is strong, both in the correction of random and systematic errors.

The last (i.e., the biases) systematic errors, represented by the biases in Fig. 7, are almost all positive, denoting a systematic model overestimation of the NTR, even if this model. This behaviour is true statistically, while for extreme events the trend is normally the opposite.

In Fig. 8 we report the Taylor diagrams relating to for the total sea level (ZF, ZF_A). In this case, the diagrams are slightly better than for the surge. The simulations, both without and with DA, which maintains evident improvements even on the third forecast day. For the total sea level, we can evaluate the improvement also in the comparison is also possible in stations

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Figure 7. Bias diagrams for the first (left), the second (centre) and the third (right) -day forecast of the surge simulations. The deterministic results (green diamonds) are plotted with the assimilation-DA ones (black squares). The red dot is the perfect agreement, while positive bias means an overestimation of the model.

Figure 8. Normalised Taylor diagrams of the forecast simulations with the total sea level. The deterministic simulations (green diamonds) compared to the DA simulations (black squares), for the first (left), the second (centre) and the third (right) -day forecast. The red dot is the perfect agreement.

61 and 62, even if they have a smaller number of data records. As seen for hindcast simulations the hindcast and reanalysis simulations, these stations are important given because of their distance from other similar stations and being assimilated stations and because they are the only stations present in the eastern basin, Mediterranean basin. The DA improvement is large also for the forecast, as well as for the hindcast, there is a notable improvement as it was in the reanalysis simulation.

Fig. 9 shows the bias diagram for the total sea level. In this case, the bias is generally lower than that of the surge, even for the model without DA, even if it is still. As for the surge, the biases are positive in most of the stations, denoting overestimation by the model. A model overestimation. The improvements given by the DA are therefore.

Considering that the oscillations of the total sea level are larger than the surge ones, as they contain the tidal part, the DA improvement is smaller in proportion and present more on. As shown in the Taylor diagrams, also the CRMSEs in Fig. 9

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Figure 9. Bias diagrams for the first (left), second (centre) and third (right) -day forecast of the total sea level simulations. The deterministic results (green diamonds) are plotted with the assimilation-DA ones (black squares). The red dot is the perfect agreement, while positive bias means an overestimation of the model.

3.3.1 12 November 2019’s storm surge event

On 12 November 2019, a particularly intense meteorological perturbation hit the central part of the Mediterranean basin. A sub-synoptic cyclone, centred in the Tyrrhenian Sea, caused a strong Sirocco wind along the entire Adriatic basin, with a fairly typical configuration. However, the CRMSE improves on all three forecast days, as already seen in the Taylor diagram, embedded in the first cyclone, a second meso-beta scale cyclone developed and moved in the north-westward direction over the Adriatic Sea along the Italian coast. This second cyclone moved at a speed close to that of shallow water waves in the northern Adriatic basin and caused a Proudman resonance (Proudman, 1929; Ferrarin et al., 2021). In Venice, the sum of the various sea level contributions produced a maximum which was the second highest ever recorded (Ferrarin et al., 2021).

In Fig. 10, we report the sea level forecast, without and with DA, the day before the main peak, the same day and the day after. The sea level is related to the Venice station and the forecasts are retrieved from the simulations $SF_s$ and has values similar to those of the surge. However, the error is related to the total sea level, which has an oscillation larger than that of the surge alone $SF_s$ with the addition of the tide computed by the harmonic constants. The previous day’s atmospheric forecast underestimated the wind and had strong errors in positioning the cyclones. Consequently, also the sea level forecast had large errors (left panel) and the use of the DA had no effect since the initial state was relative to an instant of calm conditions and did not contain any large errors. The second forecast, shown in Fig. 10 central panel, is relative to the day of the event. The meteorological forecast was accurate, with a good reproduction of the track followed by the smaller cyclone. Consequently, the prediction of the sea level is good even without the use of the DA since, even in this case, the event started after the time of the initial state. The DA does not improve the main peak but it gives a small correction to the previous peak.
Seiches are and level events to much it particularly their flooding strong of system have correct are are and 12:0011/11

![Figure 10](image)

**Figure 10.** Forecasts issued on 11, 12 and 13 November 2019 at the Venice station, from the surge simulations (adding the tide). The observed total sea level (obs) is compared to the forecast without (det) and with (ass) the use of the DA. The sea levels are in CET time and are referred to the local datum (ZMPS).

Finally, we also show the day after’s forecast because a high peak was registered in Venice, even if less extreme than the previous one. This event happened with calm weather conditions and was due to an overlap of the tidal peak to a small seiche peak, probably related to the second mode of the Adriatic basin (A2 in Tab. 2). The forecast without DA missed the reproduction of this peak, probably because of errors in the surge field of the initial state in the Adriatic Sea. In this case, the DA can give a valuable contribution, with a correction of about 15 cm, which is considerable for the particularity of that area (Fig. 10, third panel).

3.4 Seiches

3.3.1 December 2019’s seiche events

As explained in the introduction, the seiches are free barotropic oscillations of the sea level in a basin, triggered by an initial perturbation. Therefore, since they are not forced, their propagation depends solely on a correct initial state and a correct modelling setup. Given that DA has the purpose of reducing the error of the initial state, we expect it to have a strong, as shown in the previous section, a remarkable impact on the reproduction of the seiches. Generally, these oscillations are not studied much in the Mediterranean Sea are not particularly studied, as they are quite small, since they are not very energetic. On the contrary, in the Adriatic Sea, they were deeply studied; being much more energetic, their and a correct reproduction is essential for the correct reproduction of the sea level and of flooding events sea level forecast.
Figure 11. Seiche event happened on December 2019, recorded at the AAOT station (n. 57). The measured total water sea level is plotted with a pink solid line, the residual NTR with a blue dashed-dotted line, and the seiche contribution extracted from the NTR with a green dotted line. The sea levels are in CET time and are referred to the local datum (ZMPS).

In December 2019 (period included in our simulations), significant seiche events, among the most energetic ever recorded in this area, took place (Fig. 11). Despite their intensity, they were not preceded by any strong storm surge, which could have triggered them. A possible explanation could be that these oscillations were triggered by an oscillation of the meteorological forcing, a slightly-periodic atmospheric oscillation at a frequency similar to that of the normal modes of the basin (which are also the resonant frequencies).

These events were generally poorly predicted by storm surge models operating in Venice (none with DA), the city most affected by flooding in the northern Adriatic. Fig. 12 shows the total sea level recorded in station 56 (Venice) and the first three days of forecast from the surge simulations with the addition of the astronomical tide. The oscillations observed in the figure are therefore a superposition of the astronomical tide on the surge signal, which is dominated by the seiche oscillation. At the beginning of the forecast, the DA corrects an error of about 30 cm and maintains a continuous improvement over time, which can also be appreciated after three days of forecast. Although in the previous section we have seen how the statistical improvement at three days is not very appreciable, in the most extreme seiche cases and therefore of greater importance, when these oscillations are considerable the error of the initial state of the model tends to be larger and the DA provides a greater contribution to the correction.

This event demonstrates the particular effectiveness of DA in correcting the sea level in the case of seiche fluctuations in the Adriatic Sea. To better highlight this feature and see if it is also present also in the rest...
of the Mediterranean Sea the effect is positive, we carried out spectral analyses of the NTR extracted from the observations and of the modelled surge from the model, in all the stations for December 2019. Before examining the performances of the model with and without DA in the reproduction of the power spectra, we report below the results obtained for the periods of the observation power spectra in the Adriatic and Mediterranean basins. Although the periods of the main modes are quite well known in the Adriatic Sea (Cerovecki et al., 1997; Vilibić et al., 2005; Vilibić, 2006; Bajo et al., 2019), there are no works (to our knowledge, no works that report the main), based on the analysis of observations, report the periods of the Mediterranean Sea, based on observations: barotropic modes in the Mediterranean Sea. However, Schwab and Rao (1983), using a simple barotropic model, foresees some of them and describes the shape of the main barotropic modes. Below is their shapes. Below we give a brief description of the form and the expected period, comparing it with what their shapes and their periods, as reported in Schwab and Rao (1983) and as we found from the observations (see Tab. 2).

Schwab and Rao (1983), by calculating the eigenvalues of a simplified numerical barotropic model of the Mediterranean Sea, found four Mediterranean modes of oscillation. The first mode (M1) relates to an oscillation with a single positive amphidromic node in the Gulf of Sicily, with an expected period of 38.5 hours. This mode, which should have maximum amplitude
at both borders of the Mediterranean basin, has not been identified by our observations, probably because it has not been solicited by any forcing in the period considered by us that we considered.

The second mode (M2) has a more complex shape with a negative amphidromic node in the western basin, a positive one in the eastern basin and a third one in the Adriatic. This barotropic oscillation mode oscillation has an expected period of 11.4 hours. A similar peak, with a period of 12.8 hours, is present in the power spectra of several stations of the western basin analysed by us (Fig. 14). The difference from the expected peak can be explained by considering the various simplifications and the low resolution of the model used in Schwab and Rao (1983), which dates back many years ago.

The third mode (M3) has three positive amphidromic points in the Mediterranean and two basin and one positive and one negative node in the Adriatic basin. This mode has a period of 8.4 hours and maximum amplitude near Gibraltar the Gibraltar strait and along the west coast of the Adriatic Sea. Indeed, from our measurements, a peak at 8-8.3 hours is quite evident in some stations in the western Mediterranean basin (Fig. 14) and a hinted peak is also present in Trieste (Fig. 13) and in other stations on the western coast of the Adriatic Sea.

Finally, the fourth Mediterranean mode (M4) of 7.4 hours should be related to the main oscillation of the Tunisian bight, where we have no observations and therefore we cannot check its presence. From the observation power spectra that we have analysed, there seems to exist a fifth mode, here that we called M5, which is very evident in the stations of the western Mediterranean basin and with a period of 6.2 hours (Fig. 14). However, we have no information of this oscillation from the scientific literature of our knowledge.

Regarding the Adriatic Sea, the fundamental mode, here referred to as A1, is an oscillation extended to that covers the entire basin, with a nodal line south of the Strait of Otranto, near the bathymetric line of 1000 m bathymetric line, and has a period of about 21.2 hours. This oscillation is the most energetic among those analysed and is clearly visible from the observations in our possession, from which observation power spectra, with a period of 21.3 hours is calculated (Fig. 13).

The second Adriatic mode (A2) has a nodal line that cuts the Adriatic basin north of Ancona and a second line south of the nodal line of the fundamental mode, near the 2000 m bathymetric line. This oscillation is quite energetic, albeit less than the main one, and has a period of about 10.7 hours, which is perfectly confirmed by our observations (Fig. 13). Finally, the third Adriatic mode (A3) has a nodal line under the Po delta, one just above the Gargano peninsula and a third line coinciding with that of the main fundamental mode. This oscillation has a period of about 6.7 hours, but is not present in our observations, we did not detect it in our power spectra. Probably, even this mode was not triggered during the two-month period that we analysed.

In summary, Tab. 2 reports all the periods here described. For a more accurate description of their form and propagation, see Schwab and Rao (1983). Finally, in Trieste and in other Adriatic stations, there is a peak at 5.2 hours, which we called A4. This peak cannot be the Trieste bay seiche, which has a period of 2.7-4.2 hours (Šepić et al., 2022), and was found also by Šepić et al. (2022), with a value of 5.3 hours. Its origin is still unclear.

As already discussed, the seiche propagation should depend on the initial state of the dynamical system and not on its boundary conditions. For this reason, their correct reproduction is not affected by the error of the forcing/boundary conditions.
but only by the error in the initial state. The errors, that in DA are called model and representative errors, are considered small. Consequently, DA should be very effective in reducing the error in the reproduction of seiche oscillations.

Fig. 13 and Fig. 14 show the power spectral density from the NTR and the first day forecast of the surge simulations, with and without DA. After this description of the barotropic modes of the Mediterranean and the Adriatic basins, we show now how the model reproduces them in the first day of the forecast simulations \( SF, SF_A \). Fig. 13 shows the power spectra for two stations in the Adriatic Sea, Trieste, in the northern part, and Bari near the end of the basin in the southern part. Both the peaks of the main fundamental mode, A1 and that of the second mode, A2, are clearly visible in these stations. Note that both the peaks are much more energetic in the first station than in the second Trieste than in Bari, which is located near the nodal lines of the two modes. The two peaks are both underestimated by the model without DA, while with the DA the main peak of the first mode is reproduced very well, especially in the north. The A2 peak remains slightly underestimated at both stations but improves significantly with respect to the simulation without DA. Finally, in the Trieste station, a peak corresponding to the period of the third mode of the Mediterranean Sea (M3) is slightly visible in the observations (as predicted by Schwab and Rao, 1983). However, the spectra of the model power spectra, both with and without DA, are noisy in this part of frequencies and do not reproduce it. Also in Trieste, and in other Adriatic stations (not shown), there is a peak at 5.2 hours of which we do not know the origin and which is generally not reproduced with or without DA. Still in Fig. 13, but only in the Trieste station, the A4 peak is well visible in the observation power spectrum but it is not reproduced by the model. This peak could be related to some local atmospheric phenomenon not present in our forcing.

In Fig. 14 two stations in the Mediterranean Sea near Gibraltar are considered, one on we show the power spectra of two stations near Gibraltar, one in the European coast and one on in the African coast. In both stations the second and third barotropic modes of the Mediterranean basin are well visible (M2, M3). Their energy is much lower than that of the Adriatic

<table>
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Figure 13. Power spectral density of the sea levels in Trieste and Bari, in the Adriatic Sea.

Figure 14. Power spectral density of the sea level in Malaga and Melilla, in the western Mediterranean Sea.

modes (about 1,000 times) and, probably for this reason, they are corrected less by the DA; although some improvement is visible, especially for M2. Both stations and many others in the western Mediterranean basin show a third, more energetic peak, which could be a fifth barotropic mode (M5). We can exclude that this peak is a spurious signal from a partial subtraction of the astronomical tide from the NTR, as it is also present in the surge signal of the model results without DA (det SF). This peak is corrected by the DA even though it is broadened in frequency.
Overall, the DA has shown that it can effectively correct looking at the results just presented, we can state that DA has an overall positive impact on the reproduction of barotropic sea level signals in the Mediterranean Sea. In the case of the astronomical tide, the correction is very effective and can be used to determine the tidal signal spatially and in coastal areas without tide gauge stations. In these areas, it is possible to locally extract the results of the DA ensemble average for a year or more and perform a harmonic analysis to determine, with a small error, the amplitudes and phases of the tidal components. From these quantities, it is then possible to calculate the astronomical tide also in the forecast and use it to predict the total sea level, by adding it to the results of surge simulations. In the case of the astronomical tide, more than for the other components, the DA has shown that it can provide an excellent correction of the simulated level even in areas very far from the assimilated stations. This fact has been confirmed both in the sub-basins with few stations, such as the eastern Mediterranean and in the open sea areas. In fact, although the assimilated stations are all coastal, the altimetric data allowed validation of the results in the open sea. The effectiveness of DA is due to the good number of ensemble members that were used and the fact that the perturbations were created correctly. Furthermore, probably, using localisation techniques, this fact would not have been possible, the improvement would be weaker, since these techniques limit the correction to areas much closer to the assimilated stations. Finally, this is also due to the fact that the barotropic sea levels, especially from a physical point of view, the astronomical tide, have very large spatial correlations as well as the other barotropic components, have large characteristic spatial lengths which translate into sea level correlations at large distances and in greater spatial effectiveness of the DA. What makes the astronomical tide different from the surge and seiches is instead its periodicity and being referred to a mean sea level perfectly constant in time. This avoids any bias in the departures of the assimilation, which are more difficult to deal with in the case of the surge and total sea level. These two facts probably contribute to making the astronomical tide results better than those for the other sea level components.

Reanalysis simulations (hindcast with DA) with the total sea level and the surge showed great accuracy. A further improvement would perhaps be possible using an ensemble Kalman smoother, which is easily applicable to a simulation with the EnKF, such as those performed in this paper. Such simulations can be performed to create sea level reanalyses for very long periods, to be used in climatological studies. In these cases, especially in basins, the surge component is not periodic at all and its error mainly depends on atmospheric forcings. In the case of the Mediterranean Sea, which is surrounded by a complex orography such as the Mediterranean, the meteorological forcings are often underestimated. The error caused by this underestimation is difficult to correct and often subject to complex meteorological situations, the atmospheric models can have big errors, due to the lack of resolution, of processes not resolved (hydrostatic models) and the lack of local DA. This error results in an error in the surge component which cannot be corrected by the DA in the forecast, however, in hindcast, the DA with hourly assimilation manages to remedy these underestimates very well. Furthermore, since components that are not strictly barotropic are also present in the assimilated level (coming from the NTR measures ocean model in the forecast simulations), however, in the reanalysis simulation, if the assimilation step is short enough (e.g., hourly), the reanalysis of the level will also contain this part, providing a good reproduction of the sea level in all its components, as demonstrated by the
good results in the reanalysis we have obtained. From the point of view of the computational load, although there is a need to use a significant number of ensemble members, the simulations are perfectly parallelisable and are not a big issue on a modern server. Each simulation is two-dimensional and barotropic so it is performed very quickly, being able to use high time-steps. The system is strongly driven by DA and the error in the forcing cannot grow too much.

The impact of the DA in the forecast is linked in the forecast simulations, the DA impact is due to the reduction of the error of the initial state, although it would be possible to investigate the possibility of using the DA as a parameter estimator. In the forecast, the error, which initially is due only to the error of the initial state, amplifies over time, mainly propagates over time and sums up the error due to the error of atmospheric forcings. Analysing the results statistically, the simulations without DA do not show much deterioration from the first to the third day of the forecast. However, this is not true in the case of extreme events, where meteorological forcings generally have a greater error. In the case of the forecast, the improvement given by the DA decreases fairly quickly moving away from these cases, even the error of the initial state. On the first day of the forecast, the improvement is still very strong, but it decreases in the following days. However, persistence is greater if seiche oscillations are triggered, which are reproduced correctly only if the initial state has a small error. In any case, by decreasing the error of the initial state, is often larger, due to pre-existing seiches deriving from previous storms. This error can be corrected by DA and the improvement extends several days, depending on the damping time of the seiche oscillations. The DA improves not only the DA also improves the reproduction of all the phenomena taking place error in the seiche part but also those of the other sea level components, such as the tidal part (in the total sea level forecast) or the error of surge phenomena in formation at the time of the analysis, and therefore both the error linked to the astronomical component (in the case of the forecast of the total sea level), both the error linked to surge phenomena in formation. Finally, as in the case of reanalysis, the observed assimilated level may contain non-barotropic components, which are included in the initial state of analysis. However, these components cannot be correctly evolved in the forecast with a barotropic model. In order to catch the formation of a surge in an operational context, the EnKF should be executed with hourly updates, but with one or two updates per day, it is still a valuable tool to correct the seiche and the tide parts.

Regarding the computational load, although there is a need to use a significant number of ensemble members, is rather low. The ensemble member simulations are perfectly parallel and can run independently between each analysis step. Moreover, barotropic simulations are fast as the equations are quite simple and there is no need to simulate the advection-diffusion of temperature and salinity. Our workstation is a single-blade mid-level server, with 96 cores and the 81 ensemble members run in parallel most of the time. It takes about five minutes to generate the ensemble of forcings and perturbed boundary conditions, after which the ensemble simulations run parallel except in the analysis steps, where the code is parallelised as well, which are 24 in a daily simulation. The total time for carrying out the entire assimilation procedure is approximately 25 minutes, to which approximately 5 minutes are added for carrying out five days of forecasting.

Finally, we dedicated the last part of the results to the study of seiche oscillations is a field in which DA is certainly not very used. In the forecast, we have seen that the DA can lead to a significant improvement, especially where these fluctuations are very energetic, as in the Adriatic Sea. The reanalysis of the surge can also be used for an in-depth study of their spatial propagation. As previously mentioned, while the modes of
known and have been studied in numerous papers, the modes of the Mediterranean Sea their characteristics are more studied, with the exception of the oscillation A4 which has an unclear origin, they have not been analysed much in the Mediterranean Sea. The observations in our possession confirm and partially correct the periods found by the Schwab’s simulations in Schwab and Rao (1983), as far as the M2 and M3 modes are concerned. However, we did not detect the period of the main mode of the Mediterranean Sea was not observed, probably due to the short length of the period analysed by us (one month). It can be assumed that during this period the M1 mode was not excited, but more studies are needed. There is also an oscillation at, probably because it has not been triggered in the two months that we have analysed, but further investigation is needed. Then, we detected a Mediterranean barotropic oscillation with a period of 6.2 hours, which we called M5, that but it is not present in the literature but even if it is evident in many validation and calibration stations (shown) and calibration (not shown) stations, along the coasts of the western Mediterranean basin. This oscillation, which is more energetic than the M2 and M3, is underestimated by the model without DA, but even with the use of the DA, it is not reproduced correctly. Considering that oscillations with a longer period are reproduced better even if less energetic, it is possible that the DA has more difficulty in correcting the higher frequency-high-frequency oscillations. This may be due to the frequency of assimilated data assimilation timestep, every hour, which may be too low-long to define these modes.

5 Conclusions

In this paper, we investigated the impact of DA in reproducing the barotropic components of the sea level in the Mediterranean Sea. We analysed the performances both of the model without DA in hindcast and forecast simulating only the astronomical component simulations and with DA with reanalysis and forecast simulations. The barotropic components of the sea level that we considered are the astronomical tide, the surge component, with the associated seiche phenomena, and the total sea level given by their sum. The results are good in all cases, particularly show very good performances of the DA for the reanalysis of the astronomical tide, but also for the other components. The error, with the error in the tide reproduction reduced by a third on average, and slightly worse performances, but always more than good, for the surge and the total sea level. In the case of the surge and the total sea level, the DA corrects them even in the presence of large errors in the forcings, thanks to a sufficiently high assimilation frequency (one hour), a good number of ensemble members and a sufficient number of observation stations. The improvements made by the DA in the forecast simulations is still very low, especially on the first day, gradually increasing depend on the reduction of the error of the initial state, but the error coming from the forcings and boundary conditions cannot be reduced. However, the DA has still a good positive impact, especially in the first-day forecast, gradually less in the following days until it reaches the error, until reaching the performances of the simulations without DA. However, sometimes the improvement can last for the following days, up to five days in some cases, especially longer when seiche oscillations are triggered. Statistically present. The decrease of the error of the initial state is propagated in the following days with a period and decay time equal to those of the triggered barotropic mode (seiche). Finally, still considering the forecast simulations, the total sea level simulations are more accurate overall than those of the surge, even without DA, as they have a lower slightly better than the surge ones thanks to a greater correction of the bias error.
We analysed also the periods of the seiches (barotropic modes) in the Mediterranean Sea. Since these oscillations are mostly studied in the Adriatic, where they are more energetic, in the last part of the results, we have reported analysed the periods of the modes in both barotropic modes (seiches) of the Adriatic and the Mediterranean basins, calculated from the observations in our possession obtained by the observations and reproduced by the model. In Adriatic, we detected the periods of the two main modes (A1, A2), a fourth mode not well known (A4) and the third Mediterranean mode (M3). In the Mediterranean basin, outside the Adriatic sub-basin, we detected the periods of the second and third modes (M2, M3) and of a mode that we called M5, of 6.2 hours. The effect of the DA in. We tested the reproduction of the seiches in forecast mode was analysed as well, considering these periods by the model in the first-day forecast. The analysis of the power spectra shows that the DA improves the reproduction of the peaks, especially for While the periods are well reproduced also without DA, the energy of the spectral peaks improves with DA, thus confirming the better seiche reproduction. We noticed also that DA gives a better improvement in the low-frequency modes, while some difficulties are found in the reproduction of those at higher frequencies it has some difficulties with high-frequency modes. This is probably due to the sampling frequency of one hour, which is not enough high.

Further developments foresee This work provides a preliminary test of the use of the modelling configuration tested here to develop an operational system for forecasting the sea level on the Mediterranean coasts, with a focus on the Italian coasts. This system will be installed at the ISPRA Centre and will use the assimilation of the stations along the Italian coast managed by the Centre, providing a five-day forecast of DA for the total sea level. Regarding the hindcast simulations, these will be extended over time to obtain reanalyses of past periods, trying to retrieve data from other stations in reanalysis of tides and surges in the Mediterranean Sea. Reanalysis simulations can be extended to several years for climatological studies and the Mediterranean Sea and exploiting DA is able to improve these quantities despite the deficiencies of the forcing and boundary conditions. Further improvements in the DA for the reanalysis, where the error must be low during the whole simulation period, can be obtained using an ensemble Kalman smoother (EnKS). The EnKS is easily applicable to simulation with the EnKF if localisation techniques are not used. Always regarding DA methodologies, an improvement for the reanalysis, but also for the forecast, would be the use of parameter estimation techniques, applicable to the enKF with an "augmented state" (Evensen, 2009b). In this way, one could calibrate some parameters, typically the drag coefficient at the bottom. This method could reduce the model error, but the DA in its traditional form must be used to reduce the error of the initial (background) state. Finally, the addition of other observations from in-situ stations and altimeter satellites would lead to further improvement, especially if available in areas currently not covered. However, while the use of in-situ data is quite immediate, the altimetric data are difficult to use for the storm surge improvement (Bajo et al., 2017) and further studies are needed.

The For what concerns the study of the seiche oscillations needs further investigations, especially in the Mediterranean Sea, where some seiches and of the normal barotropic modes of the Mediterranean and Adriatic basins, further investigations are necessary. Some barotropic modes are not well understood to better determine the forms and their shapes, periods and decay times. In such works, the must be determined with more precision. In this context, DA can provide a more accurate spatial description reliable reanalysis of the surge, from which the seiche components can be extracted from which to extract the seiche component.
The modelling configuration tested here will be used in an operational system for forecasting the sea level on the Mediterranean coasts, with a focus on the Italian coasts. This system will be installed at the ISPRA Centre and will use the assimilation of the stations along the Italian coast, providing a five-day forecast of the total sea level.

*Code availability.* The hydrodynamic model can be downloaded at: https://github.com/SHYFEM-model/shyfem. The modified version of the model, with the data assimilation code at: https://github.com/marcobj/shyfem

**Appendix A: In-situ coastal stations**

In this appendix we report the table with the in-situ stations where we retrieved the data used in this paper, their identification numbers and their positions. We used these stations in the paper for the data assimilation and as validation stations.
Table A1. List of stations with sea-level measurements. The stations with an asterisk are those used in the validation, while the others have been assimilated. The numbering is the one used in the paper and the geographical coordinates of their position are reported.

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<th>ID</th>
<th>Lon</th>
<th>Lat</th>
<th>Station</th>
<th>ID</th>
<th>Lon</th>
<th>Lat</th>
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Author contributions. Marco Bajo: writing and reviewing the paper, developing the data assimilation code and its binding to SHYFEM, running some simulations, processing the results. Christian Ferrarin: Reviewing the paper, running some simulations, processing the results. Georg Umgiesser: Developing the SHYFEM code. Andrea Bonometto and Elisa Coraci: Providing the atmospheric forcing, financial support.

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