



Shapley values reveal the drivers of soil organic carbon stocks prediction

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Abstract. Insights into the controlling factors of soil organic carbon (SOC) stocks variation is necessary both for our scientific understanding of the terrestrial carbon balance and to support policies that intend to promote carbon storage in soils to mitigate climate change. In recent years, complex statistical and algorithmic tools from the field of machine learning became popular for modelling and mapping SOC stocks over large areas. In this paper, we report on the development of a statistical method for interpreting complex models, which we implemented for the study of SOC stocks variation. We fitted a random forest machine learning model with 2206 measurements of SOC stocks for the 0-50 cm depth interval from mainland France and using a set of environmental covariates as explanatory variables. We introduce Shapley values, a method from coalitional game theory, and use them to understand how environmental factors influence SOC stocks prediction: what is the functional form of the association in the model between SOC stocks and environmental covariates, and how the covariate importance varies locally from one location to another and between carbon-landscape zones. Results were validated both in light of the existing and well-described soil processes mediating soil carbon storage and with regards to previous studies in the same area. We found that vegetation and topography were overall the most important drivers of SOC stock variation in mainland France but that the set of most important covariates varied greatly among locations and carbon-landscape zones. In two spatial locations with equivalent SOC stocks, there was nearly an opposite pattern in the individual covariates contribution that yielded the prediction: in one case climate variables contributed positively whereas in the second case climate variables contributed negatively, and that this effect was mitigated by landuse. This shows that SOC stock variation is complex and should be interpreted at multiple levels. We demonstrate that Shapley values are a methodological development that yielded useful insights into the importance of factors controlling SOC stocks variation in space. This may provide valuable information to understand whether complex empirical models are predicting a property of interest for the right reasons and to formulate hypotheses on the mechanisms driving the carbon sequestration potential of a soil.

1 Introduction

Understanding how soil organic carbon (SOC) stocks and storage behave with ecosystem change has attracted much attention, not only for scientific purposes but also for policy making and to encourage economic incentives for carbon sequestration. Soils are a major component of the global carbon balance, storing about two third of the terrestrial carbon pool (Batjes, 1996).



25 SOC stocks are related to a number of functions provided by soils (e.g. nutrient cycling, habitat for biodiversity) which are
determinant of the overall soil functioning. There has also been a growing interest by policy makers on the role that soil could
play for carbon sequestration and climate change mitigation. For example, SOC stocks are one of the three Land Degradation
Neutrality indicator developed by the United Nations Convention to Combat Desertification (UNCCD). This interest in soils to
tackle climate change has also led to the development of economic incentives to store soil carbon (e.g. greenhouse gas emission
30 trading scheme, Keenor et al., 2021). For these reasons, there has been many studies that attempted to estimate SOC stocks
spatially for large areas and to understand how SOC stocks vary in space as a result of change in the environment.

Spatial modelling of SOC stock over large areas can be done by statistical models that interpolate soil SOC data from profiles
using a set of environmental covariates of which maps are available, such as remote sensing imagery and terrain attributes. A
recent example study using this approach is Kempen et al. (2019) for mapping SOC stocks in Tanzania using a geostatistical
35 model with a spatially varying mean. Dynamic modelling has mainly be achieved using semi-mechanistic models such as
DNDC, CENTURY or RothC, which were applied, for example, by Lugato et al. (2014) and Martin et al. (2021). Semi-
mechanistic models are attractive because they do more justice to the underlying soil processes involved in SOC storage and
enable the integration of existing knowledge into the modelling. They are also particularly suited when the objective is not only
predicting but also understanding of the factors driving SOC sequestration. There remains, however, several challenges for the
40 application of semi-mechanistic models over large areas (e.g. model parametrization, boundary conditions and forcings), which
have been only partly solved in the literature. In recent years complex, statistical and algorithmic tools from the field of machine
learning became popular for mapping SOC stocks. Martin et al. (2011), for example, used boosted regression for SOC mapping
in mainland France, whereas Guo et al. (2021) used a complex neural network for mapping SOC stocks in agricultural fields of
Iowa in the United States. Complex machine learning models are popular because they usually are more accurate than simple
45 statistical model but obtaining insights into the functioning of these models and their structure is complex.

Methods were developed in the statistical and machine learning literature to extract information from complex machine learning
models, methods which then were applied and became popular to interpret complex model of SOC stocks. Studies in soil
science usually report statistics that measure the relative importance of biotic and abiotic covariates used as predictor in the
model. In a study investigating the factor controlling SOC stocks in agricultural soils of Germany, Vos et al. (2019) calculated
50 the relative importance of a set of biotic and abiotic factors for SOC stocks modelling. Also, in a study over mainland France,
Mulder et al. (2015) reported the covariate importance of a cubist model to understand the large-scale controlling factor of
SOC storage. Reviewing the literature, we found that studies on interpretation of complex models of SOC stocks report a
global variable importance metric, such as a mean decrease in accuracy obtained by permutation of the covariates, in nearly
all cases. While valid and useful, these metrics only report a global measure of variable importance. Variable importance is
55 only one aspect of model understanding, the nature of the relationship between the covariates and the response variables being
another one. Further, in spatial modelling it is sensible to assume that the importance of environmental factors for SOC stocks
modelling vary spatially, and between areas.



This work builds on the recent study of Wadoux and Molnar (2022), in which several methods to interpret complex models of soil variation were reviewed and discussed. They stressed the importance to use global and local methods jointly to interpret differentiable aspects of the model, and showed how methods can reveal the overall covariate importance, but also the functional form of the association between the soil property and the environmental covariates, and how the importance varies from one location to another. It is worthwhile to include these developments for the interpretation of complex models of SOC stocks variation. Interpretation of complex models to help us formulating hypotheses on the underlying soil processes has also recently been highlighted as one of the challenges for pedometric research (Wadoux et al., 2021a, Challenge 3).

Amongst the various methods for the interpretation of complex models, the use of Shapley values was seen as a promising line of research in several recent studies (e.g. Padarian et al., 2020; Mohammadifar et al., 2021; Beucher et al., 2022). The study of Padarian et al. (2020), for example, used SHAP, a local method of for the estimation of Shapley values, to interpret a convolutional neural network model for mapping soil organic carbon in Chile. In Beucher et al. (2022), SHAP was also used to interpret two models: random forest and convolutional neural network, for mapping classes of potential acid sulfate soils in a wetland area of Denmark. In each of these studies, it was found that Shapley values could reveal new insights and that they were particularly suited for use in a spatial context.

In this paper we show how Shapley values can help explain the relationship found by a complex machine learning model between a soil property and environmental covariates for a large area. In a case study in mainland France, we use Shapley values on a random forest model with a large number of tree, and describe how the values are used for i) understanding the average importance of driver of SOC stocks, ii) obtaining insights into the spatial variation of the variable importance, that is, how the importance varies locally, in space and by carbon-landscape areas, and iii) deriving the functional form of the association between SOC stock and environmental factors.

2 Material and Methods

2.1 Study area

Large-scale controlling factors of carbon stocks are investigated mainland France, excluding Corsica and other islands. Mainland France is about 543,965 km² and has a wide variety of landscapes, climates and soil types which are characteristics of continental Western Europe as a whole. Landscapes in France vary from coastal plains with low elevation in the south-west and north to the mountainous areas of Massif Central in the south, of Vosges and Jura in the East, of Pyrenees in the south-west and of the Alps in the south-east with an altitude exceeding 4,000 m. Climate is influenced by both a West-East and North-South gradient with local effects of altitude and relief: average annual temperature increases from North to South whereas precipitation increases markedly with higher altitude while temperature declines. Climate in the South is Mediterranean, and temperate oceanic in the North, and tends to be semi-continental further away from the Atlantic ocean. The varying climate types, landscapes and geological formations, have resulted in a heterogeneity in soil types with large areas covered by sandy soils (Podzols in the Landes and Sologne), fertile loess soils (Luvisols in the North), calcareous soils (Leptosol and Calcisols in



90 Champagne and Ardennes), and soils from the weathering of different parent materials (dystric Cambisols in Massif Central and Brittany). These large differences in soil types are further influenced locally by vegetation and landuse, which results in important differences in stored SOC across France.

2.2 Soil organic carbon and physical properties

Soil organic carbon concentration and physical properties data are available within the framework of the soil monitoring network program (RMQS). This network is based on a systematic random sampling design following a 16 km × 16 km square grid. The sampling units are selected at the centre of the grid cells resulting in about 2206 soil sampling sites for mainland France. In the case of soil being inaccessible at the centre of the cell (i.e. due urban area, road, river, etc.), an alternative location with a natural (i.e. undisturbed or cultivated) soil is selected as close as possible, but within 1 km from the centre of the cell (for more information, see Arrouays et al., 2002). This soil monitoring program covers a broad spectrum of climatic, soil and agricultural conditions. At each site, 25 individual core samples were taken from the top and subsoil (broadly 0–30 and 30–50 cm) using a hand auger according to a unaligned design within a 20 m × 20 m area. Individual samples were mixed to obtain a composite sample for each soil layer.

Bulked soil samples were air-dried and a subsample of 500 g (step 1) was sieved to 2 mm before analysis. From (step 1), a sub-sampling of a 30 g aliquot (step 2) is done using an automatic divisor. This subsample is finely grinded to 250 μm using planetary mill and 50 mg of the resulting earth (step 3) is analyzed by dry combustion (step 4, ISO 10694:1995). In summary, four steps are necessary to measure the SOC content. The Soil Analysis Laboratory of INRAE at Arras, which is the accredited and recognized laboratory for soil and sludge analysis performed all analyses. SOC content was determined for a 0.5–10 g subsample of each composite sample.

The mass of fine earth for each observation site was determined for six samples of known volume that were extracted from a soil pit adjacent to the site. The methods used varied according to the particle size distribution of the samples. The samples were dried prior to analysis. The cylinder method was used for soils with little to no gravel. The cylinder used was 90 mm high with a diameter of 84 mm, i.e. 500 cm³. When the use of the cylinder method was not possible, i.e. for gravelly or stony soils, the water method was applied. The water method is adapted from the sand method. In this method, circular holes of between 1000 and 3000 cm³ are dug into the soil. The exact volume of soil extracted is determined by lining the hole with a plastic bag and measuring the volume of water required to fill the hole.

2.3 SOC conversion to stocks

In this study, SOC stocks were estimated for the 0–50 cm depth interval following the fixed-depth approach (Rovira et al., 2022):

$$\text{SOC stock}_{0-50 \text{ cm}} = \sum_{i=1}^n p_i B D_i \text{SOC}_i (1 - r f_i), \quad (1)$$



120 where n is the number of depth intervals at which measurements of SOC were made within the 0–50 cm depth interval, BD_i (g cm^{-3}), rf_i (%) and SOC_i (%) are the bulk density, percentage of rock fragments (relative to the mass of soil) and the SOC concentration in the i th depth interval, respectively, and p_i is the considered width of the horizon (in meters). The values of SOC stocks obtained this way along with their spatial location are shown in t ha^{-1} in Fig. 1.

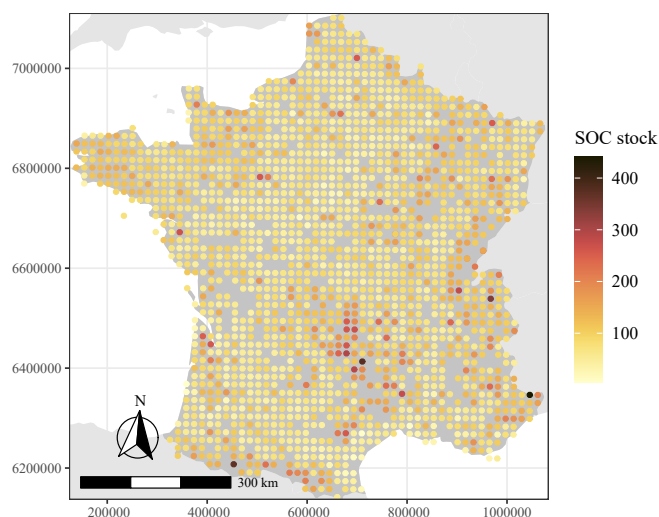


Figure 1. Location of the soil organic carbon stock data (in t ha^{-1}) for mainland France.

2.4 Exhaustive explanatory variables

125 We use a set of 23 publicly available spatially continuous environmental covariates. The covariates provide information on the main biotic and abiotic factors which are known to affect SOC stocks. The main sources of covariates was the database from BioClim, SoilGrids and a SRTM elevation model with derivatives. We also used MODIS products from which the vegetation index NDVI map was calculated from the NIR and RED spectral bands and a high-resolution landcover map with 7 classes obtained by Sentinel-2 images. Covariates were further grouped into six categories representing 1) average climate
130 condition, 2) climate seasonality, 3) extreme climate conditions, 4) topography and terrain derivatives, 5) soil properties and 6) organisms/vegetation. The list of factors, covariates, along with their unit and reference is provided in Table 1.



Table 1. List of environmental covariates used as predictor in the random forest model with unit and associated reference when applicable. Covariates are grouped into categories representing average climate conditions, climate seasonality, extreme climate conditions, topography, soil and organisms/vegetation. Covariates have coordinate system Lambert 93 (EPSG:2154) and extent: 16877.61E - 1251060E; 6028362S - 7141392S.

Factor	Covariate	Acronym	Unit	Reference
Average climate conditions	Annual mean temperature	T_am	°C	Fick and Hijmans (2017)
	Annual precipitation	Prec_am	mm	Fick and Hijmans (2017)
	Long term annual evapotranspiration	ETP_Glob	mm	Zomer et al. (2008)
	Annual mean solar radiations	SolRad_m	$\text{kJ m}^{-2} \text{ day}^{-1}$	Fick and Hijmans (2017)
Climate seasonality	Temperature seasonality (Standard deviation * 100)	T_seasono	°C	Fick and Hijmans (2017)
	Precipitation seasonality	Prec_seasono	Coefficient of Variation	Fick and Hijmans (2017)
	Standard deviation of monthly solar radiation	SolRad_sd	$\text{kJ m}^{-2} \text{ day}^{-1}$	Fick and Hijmans (2017)
Extreme climate conditions	Mean temperature of driest quarter	T_mdq	°C	Fick and Hijmans (2017)
	Mean temperature of warmest quarter	T_mwarmq	°C	Fick and Hijmans (2017)
	Precipitation of wettest month	Prec_Wm	mm	Fick and Hijmans (2017)
	Precipitation of driest month	Prec_Dm	mm	Fick and Hijmans (2017)
	Global Aridity Index	AI_glob	unitless	Trabucco et al. (2008)
Topography	Elevation	Elev	metre	Rabus et al. (2003)
	Slope	Slope	percent	Yamazaki et al. (2017)
	Module Multiresolution Index of Valley Bottom Flatness	MRVBF	unitless	Yamazaki et al. (2017)
	Topographic wetness index	TWI	unitless	Yamazaki et al. (2017)
Soil	Average soil and sedimentary-deposit thickness	SoilSed_thickness	metre	Pelletier et al. (2016)
	Soil water content for 33kPa suction (0-10 cm)	SoilWat_33	volumetric %	Hengl and Gupta (2019)
	Soil water content for 1500kPa suction (0-10 cm)	SoilWat_1500	volumetric %	Hengl and Gupta (2019)
	Sand content	Sand	percent	Poggio et al. (2021)
	Clay content	Clay	percent	Poggio et al. (2021)
Organisms/vegetation	Shannon (EVI Heterogeneity), diversity of EVI	Sha_EVI	unitless	Tuanmu and Jetz (2015)
	Primary Production Gap-Filled Yearly	Terra_PP	$\text{kg} \cdot \text{C/m}^2$	Running and Zhao (2019)
	Long-term average NDVI	NDVI	unitless	Lyapustin et al. (2018)
	Landcover (7 classes)	Landcover	unitless	Thierion et al. (2018)

The original covariate resolution spanned from grid cell sizes of $90 \text{ m} \times 90 \text{ m}$ to $1 \text{ km} \times 1 \text{ km}$ which we brought to a common resolution with grid cells of $250 \text{ m} \times 250 \text{ m}$ by either resampling with bilinear interpolation or aggregation. Covariates were then converted to the coordinate system Lambert 93 and brought to a common extent.

135 2.5 Modelling and mapping of SOC stocks

The SOC stocks data and their matching values of environmental covariates were used to build a regression matrix. The modelling approach to establish the relationship between the SOC stocks and environmental covariates is based on random forest.

140 Random forest (RF, Breiman, 2001) is an ensemble machine learning algorithm based on decision trees. A single decision tree is fitted by partitioning the covariate values of the calibration dataset. Partitions are evaluated based a splitting metric and the partition providing the optimal value of the metric is selected. This procedure is repeated until the a user-defined value of node size is reached. The prediction value of a single tree is taken as the average prediction of all nodes at the terminal leaf. In RF, an additional procedure of bootstrap and aggregating is introduced, where a user-define number of trees are built from bootstrap samples of the calibration data. In each tree, a random perturbation is further introduced where only a subset of the covariates



145 are used for fitting the tree. The final prediction from a RF model is the average of all the decision trees. The theory of RF has been extensively described in the literature and we refer the reader to standard textbooks for more details (e.g. Hastie et al., 2009).

Modelling and mapping of SOC stocks with RF is made with an usual procedure in three steps: i) model parameter selection, ii) model fitting and validation, and iii) prediction. We optimized three parameters: the number of trees, the minimum number
150 of observations in the terminal node and the number of covariates drawn randomly from the covariate set at each split. In the machine learning literature, these parameters are usually denoted `ntree`, `node.size` and `mtry`, respectively. We used the model-based optimization procedure described in Probst et al. (2019) using the mean square error of the out-of-bag prediction as objective function and 500 iterations. The optimal parameters were `ntree` = 500, `node.size` = 12 and `mtry` = 10. All other parameters were held to their default value.

155 The performance of the model with optimized parameters was evaluated using a standard random 10-fold cross-validation strategy. The dataset was randomly split into 10 folds of size approximately equal, where nine folds were used to calibrate the RF model and the remaining fold was left apart for validation. This procedure was repeated 10 times, each time setting aside a single fold. The independent observed values and those predicted by the RF model are used to compute usual validation statistics. The predictions did not show systematic over- of under-prediction (mean error was close to 0), and had a root mean
160 square error of 36.4 t ha⁻¹ and a modelling efficiency coefficient of 0.31.

The final model for prediction is fitted using all available SOC stocks data and the optimized set of RF parameters. Predictions are made for the whole of France at a resolution of 250 m using the spatially exhaustive set of covariates as predictor. This final model along with prediction for the whole of France is used for interpretation with Shapley values.

2.6 Interpretation with Shapley values

165 The RF model is interpreted with Shapley values (Shapley, 1953), which were described and used in soil science in Wadoux and Molnar (2022). Shapley values were originally developed within coalitional game theory. Consider a game where each covariate is a player and the prediction is the payout, Shapley values distribute the gain to the players (i.e. covariates) according to their relative participation to the outcome. The gain is the prediction for a particular unit minus the average prediction and the players are the covariates that contribute to the prediction and “collaborate” to receive a gain.

170 In statistical terms, let a set of covariates of size p be defined by \mathcal{S} , and $\mathcal{S} \subseteq \{1, \dots, p\} \setminus \{j\}$ be a subset of covariates which excludes covariate j . The Shapley value $\phi_{0,j}$ for covariate j for a spatial location composed of the vector of covariates \mathbf{x}_0 is given by:

$$\phi_{0,j} = \sum_{\mathcal{S} \subseteq \{1, \dots, p\} \setminus \{j\}} \frac{|\mathcal{S}|!(p-|\mathcal{S}|-1)!}{p!} \left(\hat{f}^*(\mathbf{x}_{i, \mathcal{S} \cup \{j\}}) - \hat{f}^*(\mathbf{x}_{i, \mathcal{S}}) \right), \quad (2)$$



where $|\mathcal{S}|$ is the size of the subset which excludes the j th covariate, $\mathcal{S} \cup \{j\}$ is the subset \mathcal{S} with the j th covariate added, and $\hat{f}^*(\mathbf{x}_{i,\mathcal{S}}) = \mathbb{E}_{\mathbf{X}_{\mathcal{C}}}[\hat{f}(\mathbf{x}_{i,\mathcal{S}}, \mathbf{X}_{\mathcal{C}})]$ is the prediction function where covariates not contained in \mathcal{S} are marginalized (similar for $\mathcal{S} \cup \{j\}$). The calibrated RF model is defined by \hat{f} and \mathbf{X} is the matrix containing the covariates from the calibration dataset, and $\mathbf{X}_{\mathcal{C}}$ is a subset of covariates where \mathcal{C} represents the set of covariates not included in \mathcal{S} . Note that $\hat{f}^*(\mathbf{x}_{i,\mathcal{S} \cup \{j\}}) - \hat{f}^*(\mathbf{x}_{i,\mathcal{S}})$ can be interpreted as marginal contribution to the prediction when adding covariate j to the subset of covariates \mathcal{S} . Equation 2 has two components: the first is the marginal contribution for a subset of covariates, whereas the second is a weighted average, giving equal weight to each of marginal contributions of all possible subsets of covariates. The contribution of a covariate to the prediction of a single spatial location is then given by $\phi_{0,j}$.

Calculating the exact solution for Eq. 2 is computationally intractable because it requires estimating the sum of the marginal contribution for $2^P - 1$ combination of covariates. To solve this, we use the approximation algorithm developed by Štrumbelj and Kononenko (2014) and based on Monte-Carlo sampling. In Štrumbelj and Kononenko (2014), the covariate effect is approximated by integrating over the observations of the calibration dataset. We refer to Štrumbelj and Kononenko (2014) and Molnar (2020, Chapter 9) for more detail on the approximation algorithm.

A Shapley value should be interpreted as the contribution of a covariate to the difference between the prediction and the average prediction. One advantage of Shapley values is the set of mathematical axioms of which they are derived, which provide the basis for a rigorous interpretation of their meaning. Further, Shapley values are additive and symmetric: the individual contribution of a covariate to a spatial location can be averaged over a region or a dataset. We give three example uses in the next paragraph.

A Shapley value can be obtained for any single value of the calibration dataset and any prediction at unobserved location, in the unit of the prediction (e.g. the soil property of interest). They are usually used to evaluate the individual contribution of a covariate to the prediction of a single location (i.e. to perform a local interpretation the model). Hereafter we describe three uses of the Shapley values for both local and global interpretation.

- Average contribution: absolute Shapley values can be summed over the individual observations from calibration dataset to obtain an overall variable contribution to the prediction. Note that while it is similar to the variable importance plot obtained by permutation and often reported in soil modelling studies with machine learning, average contribution plot has a different interpretation because it is not based on decrease in model accuracy (unlike permutation plots).
- Partial dependence: a scatterplot of the average of Shapley values in the calibration dataset against the value of a single covariate give indication of the functional form of the association between the soil property and the covariate (i.e. the partial dependence, Hastie et al., 2009). To ease visualization, the individual dots in the scatterplot are fitted with a smooth curve.
- Local and spatial evaluation: the local contribution of the covariate to the prediction is obtained by Shapley values and can be used to generate a spatial pattern. This pattern can in turn be used to obtain the average contribution for areas, such as bioclimatic regions or soilscares, or for an individual pedon. This approach is computationally very intensive as



it require estimating Shapley values for all spatial locations (discretized into a finite number of grid cells) in the area of interest.

2.7 Practical implementation and computational aspects

210 We use the R programming language (R Core Team, 2022) for the SOC stock calculation, covariate pre-processing, model parameter selection, model fitting and prediction, and estimation of the Shapley values. The RF model was fitted using the `ranger` package (Wright and Ziegler, 2017) and parameter selected with the `tuneRanger` function from the `tuneRanger` package (Probst et al., 2019). Estimation of Shapley values was made with the `fastshap` package (Greenwell, 2020). The procedure for estimating the Shapley values spatially at was parallelized and combine with a subsampling approach to ease computation.

215 A total of 12,495,098 grid cell locations were taken using a systematic grid sample of 800,000 cells, for which the Shapley values were estimated. We used a number of Monte-Carlo sampling as large a feasible, i.e. 500 in all cases. Calculations were done on a eight-core computer and took approximately 6 days.

3 Results

3.1 Average contribution

220 Figure 2 shows the magnitude of the covariate contribution to the prediction of SOC stocks averaged over the calibration dataset (average of absolute values in Fig. 2) or for each individual point of the calibration dataset (Fig. 2). Fig. 2b indicates that Elevation is on average the most important covariate contributing to the prediction of the SOC stocks. NDVI, mean temperature of warmest quarter and annual mean temperature also have a relatively important contribution to the prediction with an average absolute value of nearly 4 and 3 t ha⁻¹. Fig. 2b further show that the four most important covariates have

225 a wide range of Shapley values. Elevation, for example, has values between -10 to 55 t ha⁻¹. The colour scale in Fig. 2b also shows that large positive values of Shapley for the covariate elevation are obtained for high elevation, whereas negative contribution of this covariate to the prediction are obtained for low value of elevation. Other covariates have a similar pattern. For example, while the covariate soil and sedimentary-deposit thickness (`SoilSed_thickness`) has a small contribution to the prediction (i.e. the average value in Fig. 2a is 0.7 t ha⁻¹), large values of soil and sedimentary-deposit thickness have a strong

230 positive contribution of the prediction of the SOC stocks.

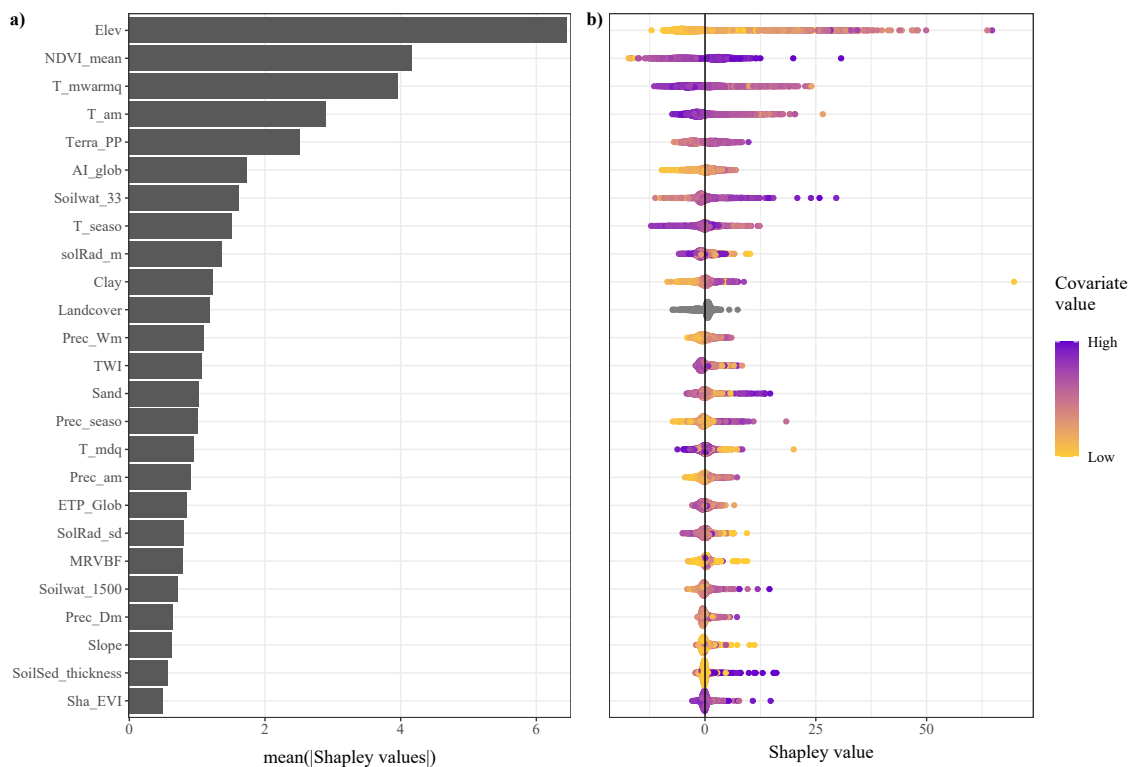


Figure 2. Magnitude of the covariate contribution to the prediction of SOC stocks in France. Plot a) shows the absolute values of Shapley averaged over the calibration dataset whereas plot b) shows the Shapley values for each individual points in the calibration dataset, i.e. the contribution of the covariate to the prediction of the SOC stock at that location. The colour scale represents the covariate value normalized in the range (0,1). Note that plot a) is the average of the absolute values presented in plot b).

3.2 Partial dependence

Figure 3 shows the relative covariate contribution to the individual SOC stock observations of the calibration dataset as a function of covariate values. The four most important covariates of Fig. 2 contributing to the predictions have a well-defined pattern. The covariate contribution to the SOC stocks prediction tend to increase with elevation and temperature for values up to 1800 m and 5°C, respectively, but sharply decreases for higher annual mean temperature or levels off for higher elevation. For high annual mean temperature (i.e. above 10°C), the Shapley values are negative, which means that the covariate contributes negatively to the SOC stocks prediction of these observations. Covariate mean temperature of warmest quarter has a very similar pattern than covariate mean annual temperature. Covariate NDVI contributes negatively to the SOC stocks prediction for NDVI values up to 0.6, after which Shapley values are positive. Large values of NDVI have a strong positive contribution (i.e. above 10 t ha⁻¹) to the prediction of SOC stocks. Shapley values of landcover are nearly always positive for 6 out of the 7 classes, but nearly always negative for the annual crops class.

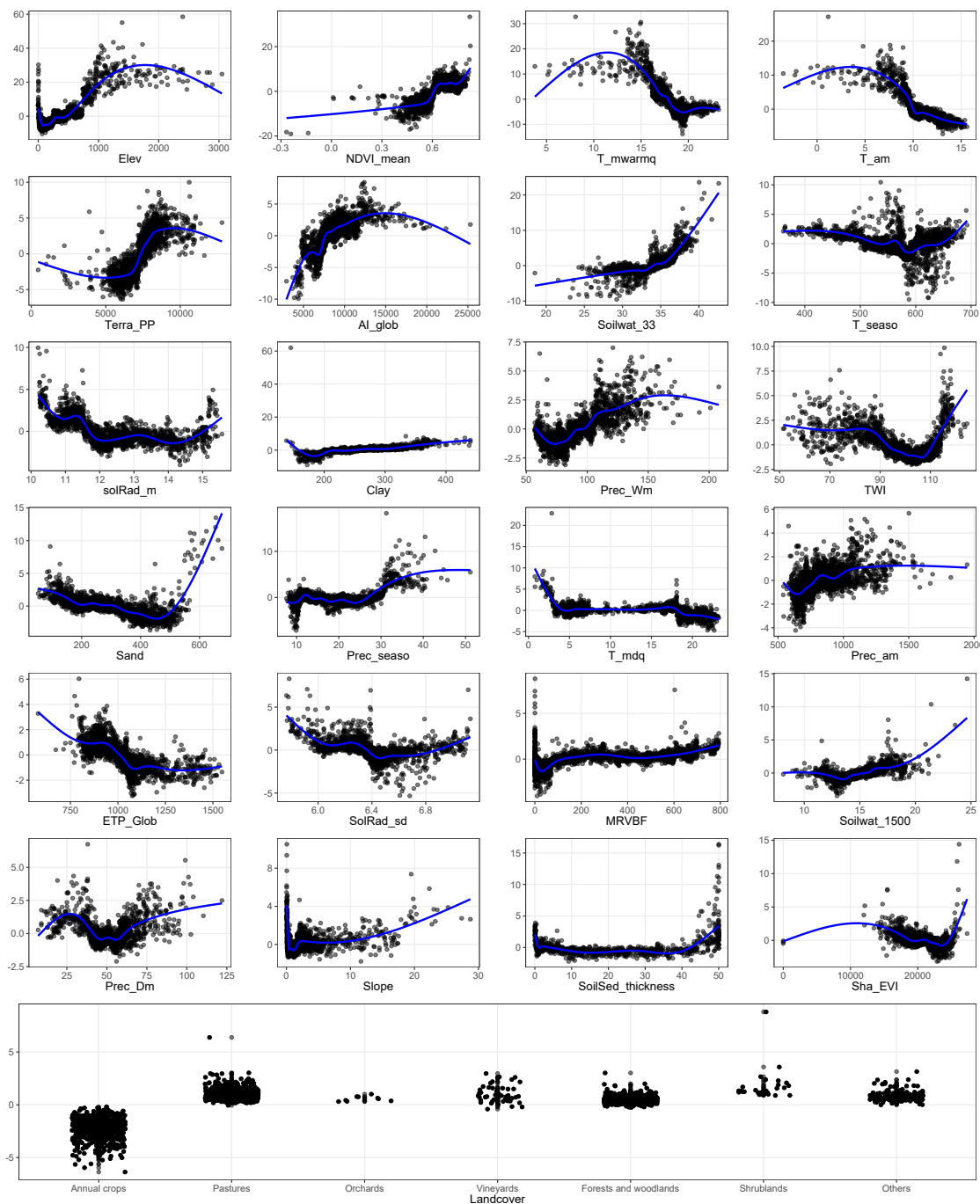


Figure 3. Relative covariate contribution to the SOC stocks prediction of the calibration dataset. The x-axis shows the covariate values and the y-axis the Shapley value of the calibration dataset for this covariate. The blue line is a smoothed curve fitted on the Shapley values for visualization purposes.



3.3 Spatial evaluation

The spatial pattern of Shapley values for the three most important covariates (Fig. 2) is presented in Fig. 4. Note that we present the maps for three covariates, but that maps for all covariates are presented in the Supplementary Materials. The three maps presented in Fig. 4 have a smooth and detailed pattern with significant spatial variation. Both elevation and mean annual temperature have a similar pattern of positive contribution in areas of high elevation (e.g. in the Massif Central, the Pyrenees, and in the Alps mountains), whereas they have negative values in most of South-western France. Elevation seems also to follow the pattern of two main rivers in the Northern part of France, with a noticeable negative contribution of elevation in the stream bed. The map of Shapley values estimated for NDVI shows a different spatial pattern with detailed variation. In the South Mediterranean coast, NDVI has a negative contribution to the SOC stocks prediction. An opposite pattern is found in the Northern Atlantic coast and in Brittany, where NDVI contributes positively to the SOC stocks prediction.

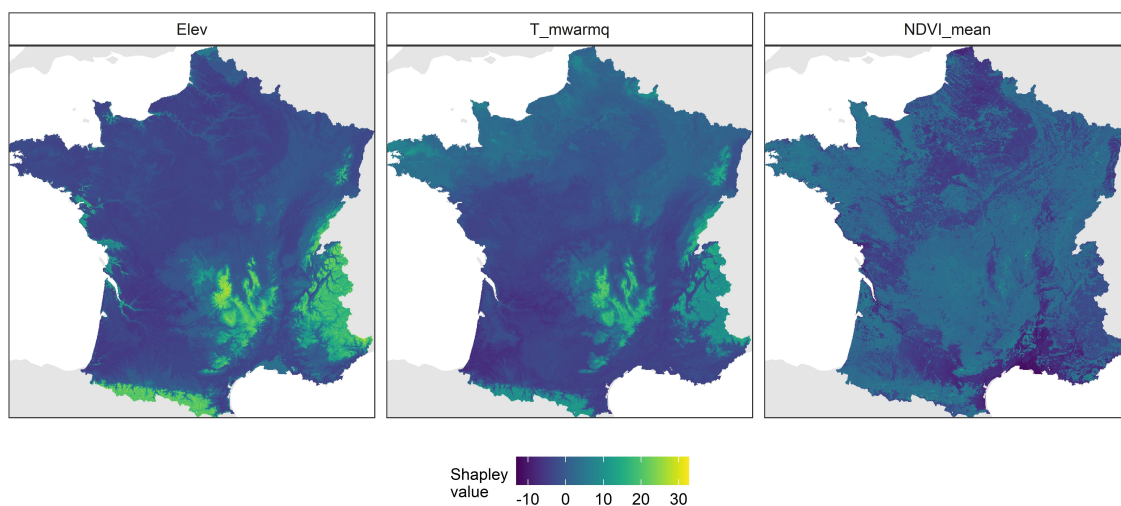


Figure 4. Spatial pattern of the Shapley values over mainland France for the three most important covariates. Dark colour indicate a negative contribution of the covariate to the SOC stocks prediction whereas a bright colour indicate a positive contribution.

Figure 5 is a map of the most important covariates contributing to the SOC stock prediction along with a map showing of the proportion of this covariate contribution to the total. To ease visualization only the five most important covariates are represented. Climate covariates are the most important predictors for nearly all mountainous areas, either T_am in the Massif Central and in the Vosges, or T_mwarmq in the Alps and Pyrenees. Vegetation covariates Terra_PP and NDVI_mean are the most important in a large area in the northern part of France and in the extreme East (Terra_PP), whereas NDVI_mean is the most important locally in larges patches in Brittany and locally around the Massif Central. Elevation is the most important covariates in the South of Landes (South-West) and in small areas in Champagnes (East of Paris). Fig. 5 also shows that the



most important covariate contribute between 20% and 85% of the total SOC stock prediction, but with considerable variation
260 between regions. There is a East-West gradient of decreasing proportion with some local large proportions (e.g. small patches
in the Atlantic coast). Large values of proportion are found for all covariates in the Pyrenees, in the Alps, and also for small
areas in the Massif Central. Small values are found for most of the Eastern part of France, with values lower than 0.4, which
means that in these areas the most important covariate shown in the left-hand side of the Figure is the most important but
contributes in small proportion to the total SOC stock prediction in these areas.

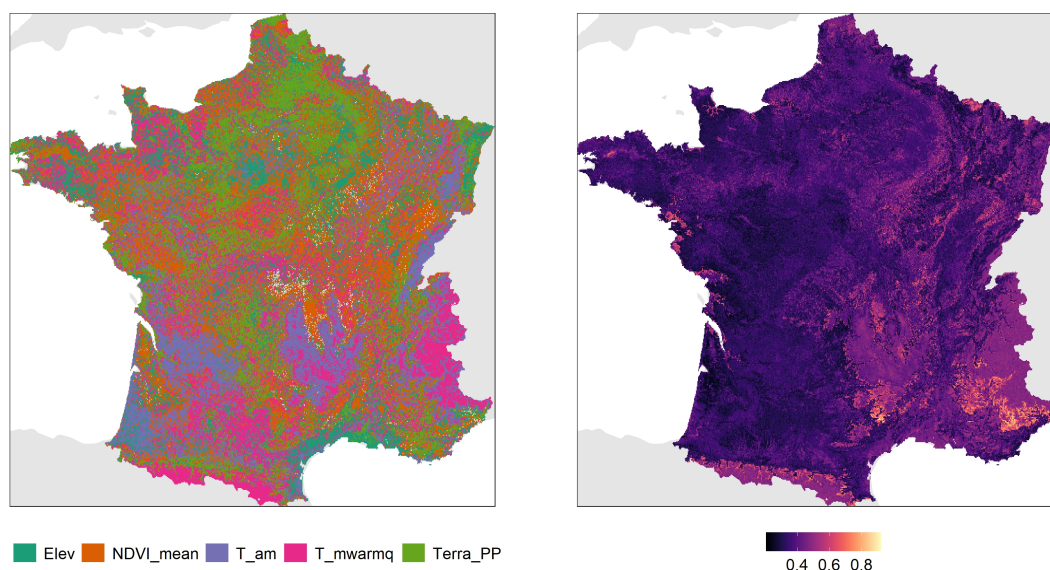


Figure 5. Map of the location-specific most important covariate contributing to the SOC stock prediction (left) for five covariates (out of 24), and proportion of this location-specific covariate to the total SOC stock prediction (right).

265 Figure 6 shows two maps: a map of the most important group of covariates contributing to the SOC stock prediction along with
a map showing the proportion of this group of covariate relative to the total SOC stock contribution of all groups. The group
of covariates related to vegetation is the most important in most parts of France and also show a high proportion relative to the
total (i.e. higher than 0.45). The group topography is the most important in nearly all mountainous areas such as in the Alps,
Pyrenees and Massif Central and have also a relatively high proportion of contribution to the total SOC stock prediction. The
270 three groups of covariates related to climate seem not the most important over large areas but only locally. For example, mean
climate condition covariates are important in South-West of France, whereas the group of extreme climate condition covariates
is the most important in Eastern part of Brittany. Soil group covariates is the most important in a small area in the north of
Landes where it also contribute to the SOC stock prediction with a proportion up to 0.5.

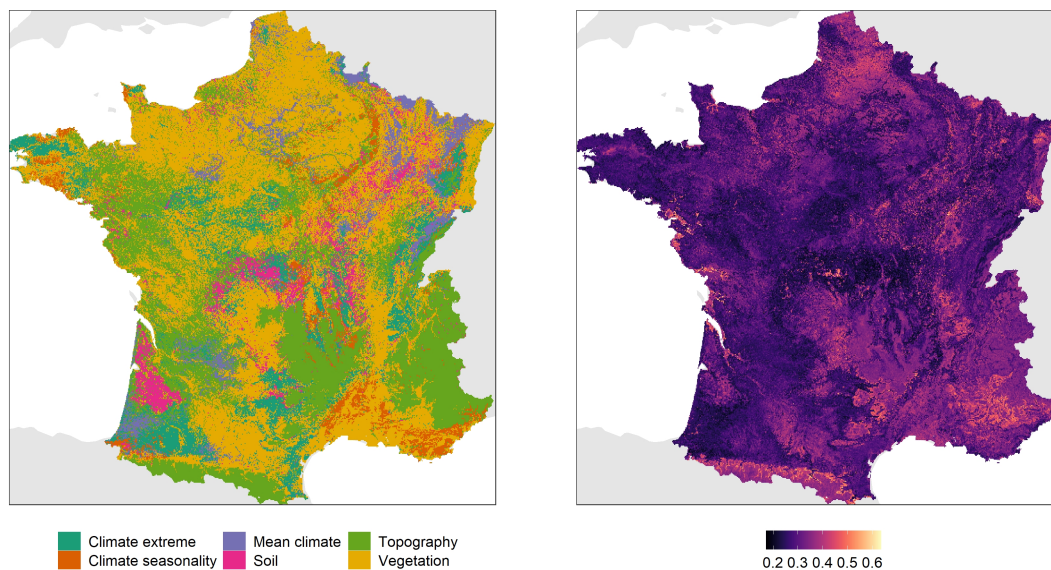


Figure 6. Map of location-specific most important group of covariates contributing to the SOC stock prediction (left), and proportion of this group to the total SOC stock prediction (right).

Using the carbon-landscape zones from Chen et al. (2019) we calculated and reported in Fig. 7 the average absolute value of Shapley for each group of covariates and for each of the 10 carbon-landscape zones (CLZ). Fig. 7 shows that overall some groups of variables are more important than others. For example, vegetation and topography covariates are for nearly all CLZ more important (i.e. with larger absolute values of Shapley) than other groups such as climate seasonality and soil. Mountainous areas which have higher SOC stocks also have high Shapley values for mean and extreme climate conditions but the highest values are found for topography. Vegetation is relatively important in nearly all CLZ and is the most important for the CLZ corresponding to the areas in a large part of South France.

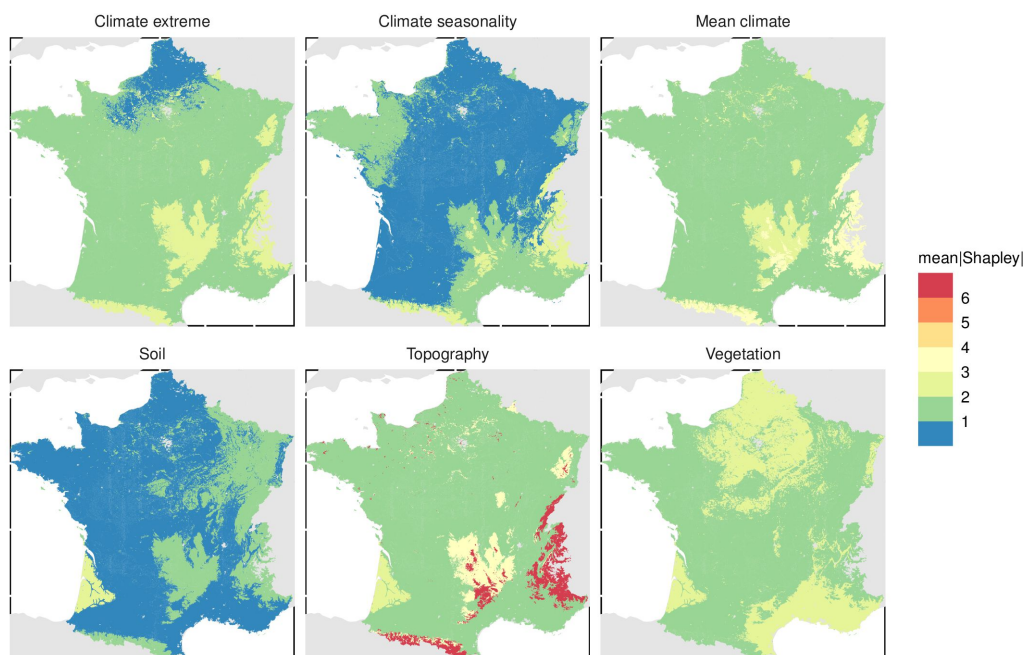


Figure 7. Maps of the most important group contributing to the SOC stocks prediction for the 10 carbon-landscape zones of mainland France. Values are absolute Shapley values averaged spatially by carbon-landscape zone.

3.4 Local evaluation

Figure 8 shows the contribution (i.e. the Shapley values) of the covariates to the SOC stock prediction at two spatial locations in a) a forested area in the Landes (South-West France) and in b) a agricultural area of Champagne (North-East France). The two locations have predicted SOC stock of 98 t ha^{-1} and 92 t ha^{-1} , respectively. There is large difference in the estimates of Shapley values between the two locations. For Landes, the covariate soil and sedimentary thickness is the main positive contributor (8.3 t ha^{-1}) to the SOC stock prediction, followed by NDVI, Terra_PP and sand. The main two negative contributors are Elev and T_mwarmq. A very different pattern is observed for the Shapley values in Champagnes where T_am is the main positive contributor whereas the landcover class annual crops is the main negative contributor with a value of (-4.9 t ha^{-1}) . The variables NDVI_mean and Terra_PP are also major negative contributors.

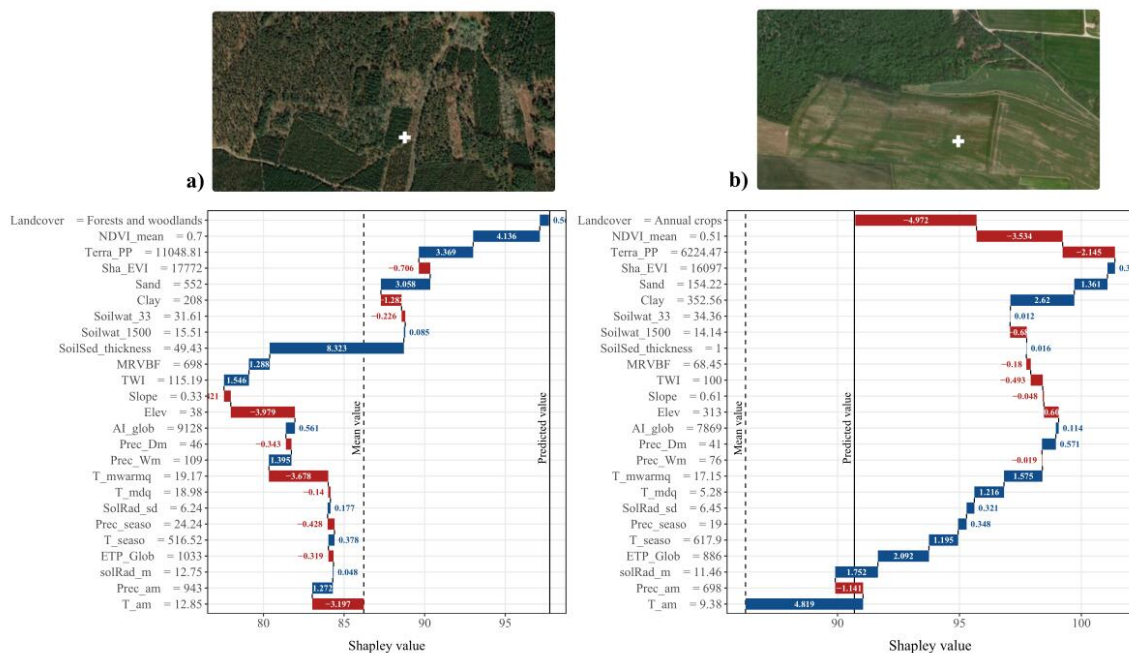


Figure 8. Contribution of the covariates to the SOC stock prediction at two spatial locations in a) a forested area in the Landes (South-West France) and in b) a agricultural area of Champagne (North-East France). Both locations have close range of predicted values of SOC stocks around 95 t ha^{-1} . The blue colour indicates a positive contribution of the covariate to the SOC stock prediction whereas a red colour indicates a negative contribution. The y-axis shows the covariate value for the prediction at the location. Satellite images from © Google Maps [2022, CNES/Airbus, Maxar Technologies] Available through: <https://www.google.com/maps/> [Accessed 2 July 2022].

290 4 Discussion

4.1 Modelling and mapping of SOC stocks

The validation statistics obtained by the RF model was in good agreement with previously published studies, although it is generally difficult to draw conclusion on the quality of the fitted RF model compared to other studies mapping SOC concentration or density. The MEC obtained in our study is within the upper range of the R2 values for large area mapping of SOC reported in Minasny et al. (2013). When mapping SOC stocks over large area, difference in model performance can arise from whether the bulk density is measured or estimated, and from covariate set used to fit the model. Other causes of difference are the modelling procedure and the validation strategy (e.g. (spatial) cross-validation, independent validation with probability sampling) which can all have a substantial impact on the resulting map quality. Our fitted RF model had no bias and a MEC of 0.31. This is similar to previous studies on mapping SOC stock for large areas. For example, Martin et al. (2014) fitted a boosted regression tree model on a similar set of the RMQS sampling sites in France and obtained a R2 of 0.36 and negligible bias, whereas Mishra et al. (2009) obtained a ME and R2 of -0.1 and 0.46, respectively, for mapping SOC stocks in the state of Indiana (USA). Also, Lacoste et al. (2014) reported a R2 of 0.43 for modelling SOC stocks in the O horizon of the French



forest soils. The spatial pattern of the SOC stocks map for the 0-50 cm depth intervals (not shown) obtained by prediction with the RF model also agreed with past studies. Studies by Martin et al. (2011) and later Martin et al. (2014) reported similar patterns of SOC stocks in France for the 0-30 cm depth interval. The later study of Martin et al. (2014) performed a rigorous validation assessment of several modelling approaches to SOC stocks in France, and from which we found no systematic difference with the maps made in this study with the error maps made in Martin et al. (2011) or Meersmans et al. (2012). Overall, the validation statistics and spatial pattern of prediction by the RF model suggest that the RF fitted in this study is sufficiently accurate to serve as basis for the interpretation with Shapley values.

310 4.2 What did Shapley values reveal about the drivers of SOC stocks in mainland France?

The Shapley values revealed that the covariates contribution to the SOC stocks prediction varied greatly among spatial locations and between CLZ. The results suggest relationships between environmental covariates and SOC stocks which have been abundantly documented in the literature and other relationships that may highlight the limitations of empirical modelling for the SOC stocks prediction. Hereafter we describe how group of covariates relates to potential acting processes of soil carbon storage and how the Shapley values revealed potential limitations of the empirical modelling of SOC stocks.

4.2.1 Climate

The effect of climate on SOC stocks, here through the temperature and precipitations variables (i.e. T_{am} and P_{am}), is usually linked to a number of soil carbon decomposition processes as well as plant growth. In our case, covariates related to temperature (i.e. T_{am}, T_{mwarmq} and T_{mdq}) were the most important average contributors to the SOC stock prediction, but the pattern reported in Fig. 2 and 3 show that the relationship with SOC is complex (i.e. non-monotonic, non-linear and with strong discontinuities). In fact, temperature is one of the most important climate drivers affecting SOC mineralization, while at the same time also affecting the net primary productivity (Martin et al., 2011). Here, after a certain threshold (i.e. 6°C), the relationship between SOC and temperature is decreasing, likely because of the combined effects of negative impact of extreme temperatures on plant productivity and of its positive effect on SOC mineralization. The impact of temperature is also exemplified in the CLZ related to high SOC stocks in mountainous areas (Fig. 7), the group of climate covariates has the most important contribution, which may be caused by the low mineralization processes due to cold temperature. Fig. 9 illustrates the combined effect of mean temperature and NDVI on SOC stocks. Optimum conditions in term of SOC stocks correspond to high NDVI mean levels (around 0.75) and moderate temperature (hence mineralization) close to 7.5°C on average. Similar optimal conditions are found for lower NDVI levels, but where low temperature enable slow turn-over of SOM.

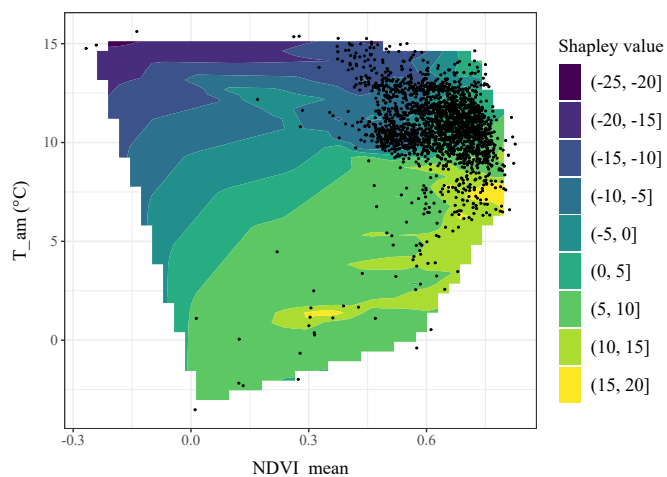


Figure 9. Two-dimensional visualization of NDVI_mean and T_am contributions to the SOC stocks prediction. Black dots indicate a point in the calibration dataset. The colour represent the Shapley values. The surface was obtained by linear interpolation of the Shapley values obtained from the calibration dataset.

330 This relationship is also modulated locally by the extreme climate condition which act as a limiting factor to carbon storage (Reichstein et al., 2013). Indeed, Fig. ?? shows that T_mdq importance is overall greater than the importance of T_am and Fig. 3 that variations of SOC stocks induced by T_mdq are greater than variations of T_am. The shape of the relationship between T_mdq and SOC stocks is close to that of T_am and SOC. This might be because, overall, similar processes relating temperature to both plant productivity and SOM mineralization come into play. Noticeably, for T_mdq above 19°C, SOC
335 stocks remain constant. To our knowledge there is no best explanation, but there is a probable correlations with other variables, such as land use, or other climate variables including precipitation. Typically in areas with a very hot summer, drought possibly also limits SOM mineralization, avoiding temperature increases to further facilitate SOC stocks depletion.

4.2.2 Topography

Topographic covariates control many of the redistribution processes influencing SOC stocks. In our study case, elevation was
340 on average the most important covariate for explaining the SOC stocks variation, with trend (Fig. 2 and 3) of increasing Shapley values for higher elevation (i.e. elevation contribute positively to the SOC stocks prediction). In fact, the higher SOC stocks in France are found in the mountainous areas of the Pyrenees, Massif Central and Alps. This is an expected finding already reported in the literature for various ecosystems (e.g. by Lemenih and Itanna, 2004) and which is usually attributed to the combined effect of temperature, precipitation (Saby et al., 2008). In our study, the Shapley values revealed that the effect of
345 elevation is merely related to its relationship with temperature, see, for example, the inverse relationship between these two variables in Fig. 3. The covariate slope had overall a positive effect on SOC stock prediction (Fig. 2) but the maps of Slope in the Supplementary Materials shows that this occurs both in mountainous areas (e.g. the Alps) and in river stream beds (e.g. the Seine river stream). The effect of slope on SOC stocks is logical in this study case and has already been reported elsewhere



(e.g. Stevens et al., 2014). However, in Stevens et al. (2014) the relationship between slope and SOC stocks is negative. This suggests that in our case the positive effect of slope might be due to the location of steep slopes, i.e. mostly in mountainous areas. Higher SOC stocks with steeper slope might also result from the combined effect of orientation, and resulting effects on moisture and temperature.

4.2.3 Soil

Soil clay has a well-known effect of SOC stock through physical interaction and protection of organic matter from decomposition (Stewart et al., 2008). We found that prediction of SOC stocks was monotonically increasing with higher values of clay, which is consistent with previous study on the same area (e.g. Martin et al., 2011). The soil water regime had a relatively moderate contribution to the SOC stocks, but this was very contrasted locally for the covariate Soilwat_33. For example, large agricultural and semi-mountainous areas from the center to North-West of France had a positive value of Shapley for this covariate (see also the Supplementary Materials). For these areas there might be a contribution of processes relying on soil moisture for SOC storage, such as soil carbon mineralization by microbes (Orchard and Cook, 1983). From the available results, however, this is disputable to draw conclusions on this process. We also found that soil covariate SoilSed_thickness, which represent the soil thickness to the unweathered bedrock, was not an important contributor on average, but that for the deep sandy soils of Landes, this variable was a very important predictor of the SOC stocks. In this regard, the sand covariate was an important factor contributing to SOC stocks prediction in the Landes, because in these areas the SOC stocks are mainly characterized by acidic sandy soils that that were undisturbed for a long time by agriculture. The high SOC stocks in these areas, however, are not due to the sandy soils but due to the combined effect of landuse and carbon input (see below). It is likely that the empirical model of SOC stocks is predicting high values in these areas for the wrong reasons.

4.2.4 Organisms/vegetation

Both NDVI_mean and Terra_PP were important covariates for predicting the SOC stocks on average (Fig. 2) but also locally in many parts of France (Fig. 5 and 6). SOC stocks are mediated by a balance of net C input and net loss and vegetation acts on SOC stocks through C inputs. This is shown in Fig. 4 where the map of Shapley values for NDVI_mean has high values in large forested areas. Landuse has also an important effect of SOC stocks over time. In Fig. 3 it was shown that 6 out of 7 categories have a positive contributions to the SOC stocks prediction, but that for Annual crops the contribution was nearly always negative. This is a realistic result that has been reported abundantly in the literature as arable land cropping systems are characterized by a large human appropriation of the net primary productivity (Plutzer et al., 2016). In the Mediterranean CLZ, conversely, NDVI and Terra_PP covariates were not important. In Mediterranean areas carbon storage is mitigated by landuse and mediated by water availability. We also note the stepped pattern of the NDVI_mean covariates on the SOC stocks prediction shown in Fig. 3. This suggest that NDVI compensate for a missing carbon input covariate or an insufficient number of landuse classes. In our case the Shapley values reveal that the covariates are not sufficiently precise or that potential covariates are missing to predict the SOC stocks. For example, a mitigation occurs by landuse between NDVI and the carbon input.



Finally, the Shapley values presented for two spatial locations in Fig. 8 reveal well-known relationship of SOC stocks with its environment. In Landes the SOC stock is relatively high because despite of sandy acid soils that do not store well the carbon, the system is stable over time with no cultivation and a landuse made of pine forest. This is reflected in the Shapley values: the soil thickness and sand content are important predictors of the SOC stocks, as well as vegetation. This is counter-intuitive and this suggest that the model did not capture well the landuse information, or that we did not have sufficient landuse classes to discriminate historical landuse. The spatial location in Champagnes, conversely, is within an area with relatively high clay content (high physical protection) and low temperature reduces carbon mineralization in cold winters. It is therefore no surprise that the two most important variables contributing to the SOC stocks in this location is temperature and clay content, but that this was strongly mitigated by the landuse class.

390 4.3 Comparison with previous studies

We found no notable difference in results with previous studies investigating the controlling factors of SOC (Arrouays et al., 2001) and SOC stocks variation in France (e.g. Martin et al., 2011; Mulder et al., 2015). In these studies too, they concluded that landuse or vegetation, soil physical and chemical properties and climate had the most important effect of SOC levels. In our case, we had a different set of explanatory variables and we investigated the controlling factors for a single depth intervals (i.e. 0-50 cm). In spite of these differences we also found the climate and vegetation were major factor contributing to the SOC stocks prediction. The reported effect of clay, soil water regime is the same as reported in Martin et al. (2011) but they also reported that rainfall was consistently the most important predictor, whereas in our case temperature was the most important. The effect of these two variables on SOC storage are dependent of many factors (e.g. chemical protection, freezing, plant productivity) which may be accounted for by a different set of covariates. Both precipitation and temperature as important predictors are plausible outcomes of the modelling, but more thorough analysis is need to investigate this. In Mulder et al. (2015), it was found that evapotranspiration, net primary productivity and clay content were important predictors, for both topsoil and subsoils. They too found that the influence of environmental factors varied greatly among soil-landscape zones.

4.4 Limitations of Shapley values and the interpretation of complex models

The results appear realistic, both in relation to the existing known soil carbon storage processes and with regards to previous studies in the same area. One however must take care with interpreting Shapley values as potential causal mechanisms describing the spatial pattern of SOC stocks. Despite that we selected a set of covariates that intended to represent underlying mechanisms involved in SOC storage, first, these are only proxy variables and do not necessarily relate to processes involved in SOC stocks variation. Several studies have argued in this sense (e.g. Wadoux et al., 2020). In this work we limited our analysis of the Shapley values to the connection of the relationship found between environmental covariates and SOC stocks to possible processes involved in soil carbon decomposition and storage, but we did not proceed any further in assuming that we inferred causal conclusion from these values. Doing so would require additional experiments and a more thorough analysis. Another aspect to be considered when interpreting Shapley from the derived relationships between covariates and the response variable is the accuracy of the covariates. This is particularly important when using the covariates rankings provided by Shapley values.



An interesting and novel aspect of the use of Shapley values is the possibility to understand whether the complex model is predicting for the right reasons. Empirical models used in soil mapping studies include little or no pedological knowledge on the property of interest. Instead the mode search for correlation among the data and predict using empirical rules. Often these models are more accurate than simple models (i.e. linear regression), but it is unclear whether they are able to predict because of spurious associations between data or through a correlation that has an underlying causal structure (Wadoux et al., 2021b, Section 5.2). In our study, the Shapley values revealed that in the Landes, for example, SOC stocks were accurately predicted, but that the model used the correlation with the sand to predict this high values, instead of the expected historical landuse and carbon input information. An obvious solution to this problem is to obtain better covariates and more covariates on carbon input and historical landuse, which should allow the model to discern better the controlling factor of SOC storage.

Although we used Shapley values to obtain the pattern of controlling factors in a large area, Shapley values require a lot of computing time. In our case computing took approximately 6 days of parallel processing in a standard 8-cores desktop computer, but processing time is largely determined by the number of Monte-Carlo sampling. We used 500 Monte-Carlo simulations, which we considered sufficient. This was tested by a scatterplot of the Shapley values estimated by a number of Monte-Carlo sampling, against another set of Shapley value estimated by the same number of Monte-Carlo sampling. The results (not shown) suggested that any number greater than 100 would provide a sufficiently accurate estimate of the values. Excessive computing time, however, might usually preclude the use of Shapley values for continental and global studies. To date two approaches exist for approximating Shapley values: the one described in Štrumbelj and Kononenko (2014) that we used in this study, and the one described in (Lundberg and Lee, 2017) called SHAP (see also studies in soil science using SHAP Padarian et al., 2020; Beucher et al., 2022). The SHAP approach might be valuable too although we did not consider it in our case. SHAP can be viewed as a local approximation of Shapley values and might provide a computationally efficient (near) exact approximations of Shapley values for specific families of models such as gradient boosted decision trees. To the best of our knowledge we are not aware of studies describing the differences between the two approaches, and whether this has an impact on the estimated values. This may be investigated further in future works.

5 Conclusions

We introduced and implemented the Shapley values for interpreting a machine learning model. Using the soil organic carbon stocks for the 0-50 cm depth intervals and a large set of environmental covariates as predictors, Shapley values revealed insights into the global and local factors contributing to the SOC stocks variation, and how the model adjusted the prediction locally. The main conclusions are:

- Shapley values revealed the global contribution of environmental factors to the SOC stocks prediction, but also enable to obtain the functional form of this association and a spatial pattern of the covariate contribution to the prediction.
- Covariates contribution varied for SOC stock prediction varied greatly among spatial location and between carbon-landscape zones.



- The results of the interpretation were valid in light on existing and well-described soil processes acting in soil carbon decomposition in the area.
- In a test of predicting SOC stocks to two spatial locations with similar stock values but very different environments, we obtained Shapley values that show individual covariate contribution to the prediction.
- 450 – In our case study, the comparison with existing works investigating the controlling factors of SOC stocks variation showed that Shapley values found similar relationships between SOC stocks and environmental factors.
- We need to further test the use of Shapley values on covariates that are more precise (for example, measured at site) and more directly linked to factors conditioning SOC stocks variation, for example by using covariates linked to carbon inputs instead of NDVI.
- 455 The results and comparison with existing studies suggest that Shapley values were a useful tool to give insight about the controlling factors of SOC stocks variation, both globally and locally for specific spatial locations. We conclude the Shapley values is a promising tool to interpret complex models, and that its main added value is to enable a local interpretation of the environment factors contributing to a prediction.

Competing interests. The authors declare that they have no conflict of interest

- 460 *Data availability.* The SOC stocks data are not publicly available but can be calculated with data from the French Infosol data repository <https://doi.org/10.15454/AIQ9WS>.

Author contributions. AMJCW formulated the research questions, performed the analysis and directed the research. NPAS provided data and helped with data processing. MPM provided insights into SOC stocks controlling factors in mainland France. All authors contributed to the manuscript writing and editing.



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